# Tutorial 6 — Query Optimization, Planning, Evaluation

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March 5, 2018

ECE 356 Winter 2018 1/1

Give instances of relations R and S that show that the following pairs of relational algebra expressions are not equivalent:

1 
$$\pi_A(R-S)$$
 and  $\pi_A(R)-\pi_A(S)$ 

 $\sigma_{\theta}(R \bowtie S)$  and  $R \bowtie \sigma_{\theta}(S)$ , where  $\theta$  uses only attributes of S

ECE 356 Winter 2018 2

# Exercise 6-1 Solution (1/2)

We are showing that  $\pi_A(R - S)$  and  $\pi_A(R) - \pi_A(S)$  are not equivalent. Let our schemas be R(A, B) and S(A, B). Let  $R = \{(1, 2)\}, S = \{(1, 3)\}.$ 

$$LHS = \pi_{A}(R - S)$$

$$= \pi_{A}(\{(1, 2)\} - \{(1, 3)\})$$

$$= \pi_{A}(\{(1, 2)\})$$

$$= \{(1)\}$$

$$RHS = \pi_{A}(R) - \pi_{A}(S)$$

$$= \pi_{A}(\{(1, 2)\}) - \pi_{A}(\{(1, 3)\})$$

$$= \{(1)\} - \{(1)\}$$

$$= \emptyset$$

$$LHS \neq RHS$$

ECE 356 Winter 2018 3/1

## Exercise 6-1 Solution (2/2)

We are showing that  $\sigma_{\theta}(R \bowtie S)$  and  $R \bowtie \sigma_{\theta}(S)$  are not equivalent when  $\theta$  uses only attributes of S.

Let our schemas be R(A, B) and S(A, C).

Let  $R = \{(1,2)\}$ ,  $S = \{(42,1337)\}$ .

Let  $\theta$  be a predicate like C=1, or anything that satisifies no elements in C.

$$LHS = \sigma_{\theta}(R \bowtie S)$$

$$= \sigma_{C=1}(\{(1,2)\} \bowtie \{(42,1337)\})$$

$$= \sigma_{C=1}(\emptyset)$$

$$= \emptyset$$

$$RHS = R \bowtie \sigma_{\theta}(S)$$

$$= \{(1,2)\} \bowtie \sigma_{C=1}(\{(42,1337)\})$$

$$= \{(1,2)\} \bowtie \emptyset$$

$$= \{(1,2,null)\}$$

$$LHS \neq RHS$$

ECE 356 Winter 2018 4/1

## Exercise 6-2

Consider relations R(A, B, C), S(C, D, E), T(E, F), where A, C, and E are their respective primary keys.

Suppose  $n_R = 1000, n_S = 1500, n_T = 500$ .

- What is the tightest upper bound we can place on  $n_{R\bowtie S\bowtie T}$ ?
- 2 How could we compute the join efficiently?

ECE 356 Winter 2018 5/1

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n_R = 1000, n_S = 1500, n_T = 500.
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Note that the size of the fully-joined relation  $(n_{R\bowtie S\bowtie T})$  will be the same no matter the order we execute the joins in, since natural joins are associative and commutative.

Suppose we consider the execution order  $((R \bowtie S) \bowtie T)$ .

$$n_{R\bowtie S} \leq n_R$$
 since C is a key of S  $n_{(R\bowtie S)\bowtie T} \leq n_{R\bowtie S}$  since E is a key of T  $n_{R\bowtie S\bowtie T} = n_{(R\bowtie S)\bowtie T}$  by associativity  $\leq n_{R\bowtie S}$   $\leq n_R$   $= 1000$ 

So  $n_{R\bowtie S\bowtie T}$  < 1000.

To efficiently compute the join, it helps to have indices on the primary keys of S and T, and to use those indices to prevent linear scans of those relations during the join.

## Exercise 6-3

Using the relational algebra equivalence rules, show how to derive the RHS expression from the LHS expression.

$$\bullet \sigma_{\theta_1 \wedge \theta_2 \wedge \theta_3}(R) = \sigma_{\theta_1}(\sigma_{\theta_2}(\sigma_{\theta_3}(R)))$$

 $\sigma_{\theta_1 \wedge \theta_2}(R \bowtie_{\theta_3} S) = \sigma_{\theta_1}(R \bowtie_{\theta_3} \sigma_{\theta_2}(S))$ , where  $\theta_2$  uses only attributes of S

ECE 356 Winter 2018 7

# Exercise 6-3 Solution (1/2)

$$\begin{aligned} \textit{LHS} &= \sigma_{\theta_1 \wedge \theta_2 \wedge \theta_3}(R) \\ &= \sigma_{\theta_1 \wedge \theta_2}(\sigma_{\theta_3}(R)) \\ &= \sigma_{\theta_1}(\sigma_{\theta_2}(\sigma_{\theta_3}(R))) \\ &= \textit{RHS} \end{aligned}$$

by  $\sigma$ -cascade (rule 1) by  $\sigma$ -cascade (rule 1)

ECE 356 Winter 2018 8/1

## Exercise 6-3 Solution (2/2)

$$\begin{split} \textit{LHS} &= \sigma_{\theta_1 \wedge \theta_2}(R \bowtie_{\theta_3} S) \\ &= \sigma_{\theta_1}(\sigma_{\theta_2}(R \bowtie_{\theta_3} S) & \text{by $\sigma$-cascase (rule 1)} \\ &= \sigma_{\theta_1}(R \bowtie_{\theta_3} \sigma_{\theta_2}(S)) & \text{since $\theta_2$ only uses attributes of $S$,} \\ &= \textit{RHS} & \text{we can distribute $\sigma_{\theta_2}$ over $\bowtie_{\theta_3}$} \end{split}$$

ECE 356 Winter 2018 9/1

Let R be our relation with  $n_r$  records.

Suppose  $s_i$  records in R match a predicate  $\theta_i$ : that is,  $\sigma_{\theta_i}(R) = s_i$ .

The selectivity of  $\theta_i$ ,  $sel_{\theta_i}(R)$  is defined to be  $\frac{s_i}{R}$ . This represents the probability that a record in R satisifies  $\theta_i$ .

Derive the selectivity formulas for the following complex selections:

- **1** conjunction:  $\sigma_{\theta_1 \wedge \theta_2 \wedge ... \wedge \theta_m}(R)$
- **2** negation:  $\sigma_{\neg \theta}(R)$
- **3** disjunction:  $\sigma_{\theta_1 \vee \theta_2 \vee ... \vee \theta_m}(R)$

ECE 356 Winter 2018 10/

### **Exercise 6-4 Solution**

We make the simplifying assumption that predicates are independent of one another, allowing us to use standard probability rules for dealing with independent events.

$$\blacksquare$$
  $sel_{\theta_1 \wedge \theta_2 \wedge ... \wedge \theta_m}(R) = \prod_{i=1}^m sel_{\theta_i}(R)$ 

$$2 \operatorname{sel}_{\neg \theta}(R) = 1 - \operatorname{sel}_{\theta_i}(R)$$

3 
$$sel_{\theta_1 \vee \theta_2 \vee ... \vee \theta_m}(R) = 1 - sel_{\neg \theta_1 \vee \theta_2 \vee ... \vee \theta_m}(R)$$
  
 $= 1 - \prod_{i=1}^m sel_{\neg \theta_i}(R)$   
 $= 1 - \prod_{i=1}^m 1 - sel_{\theta_i}(R)$ 

ECE 356 Winter 2018 11,

## Exercise 6-5

What are some strategies that a query optimizer could use to reduce the cost of query plan selection, or the cost of the query itself?

ECE 356 Winter 2018 12/1

### **Exercise 6-5 Solution**

- limit the size of intermediate results early on in the plan (select and project ASAP)
- cache subplans
- materialize commonly used views which result from expensive queries
- remove unnecessary joins
- reinterpret subqueries as joins
- pipeline where possible
- and more...

ECE 356 Winter 2018 13 / 1