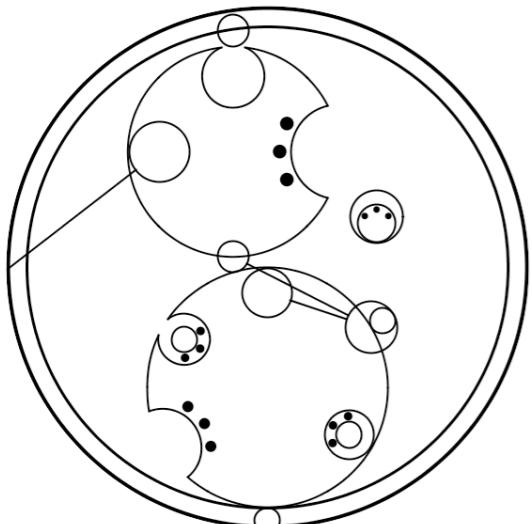
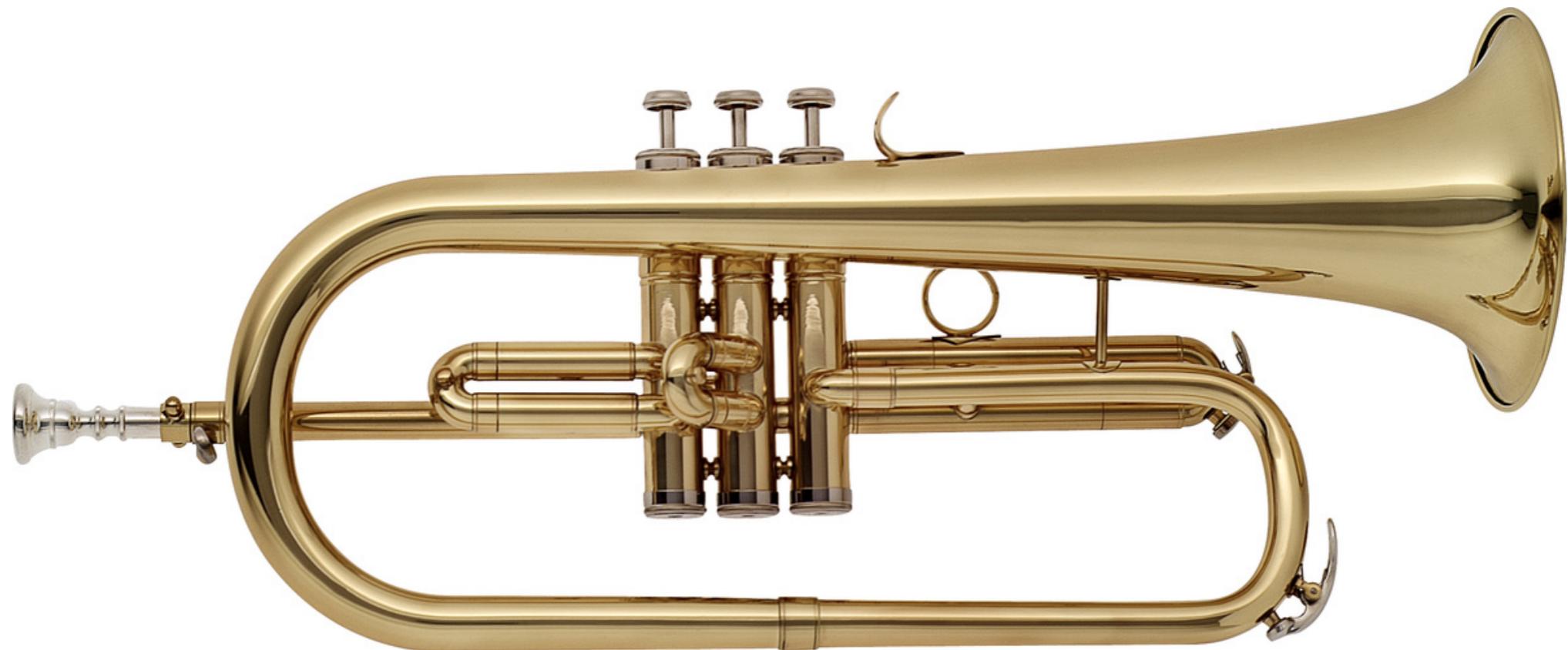


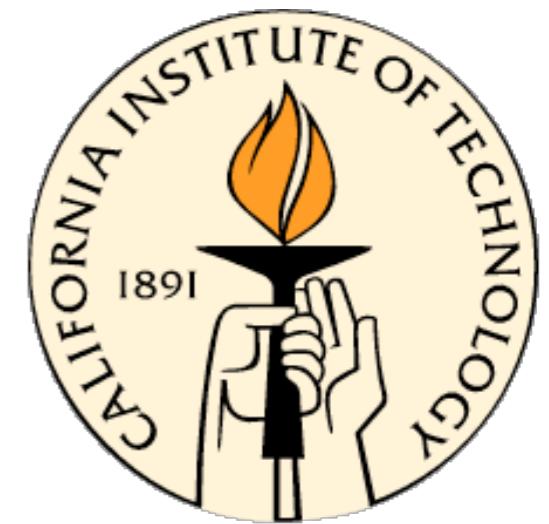
# vibrations 'n waves

lecture 12 (+/- 1)



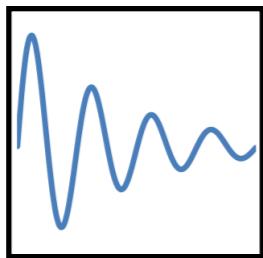
Alex Urban  
(in for Prof. Rana Adhikari)  
California Institute of Technology

2 November 2017



# What are we going to look at today?

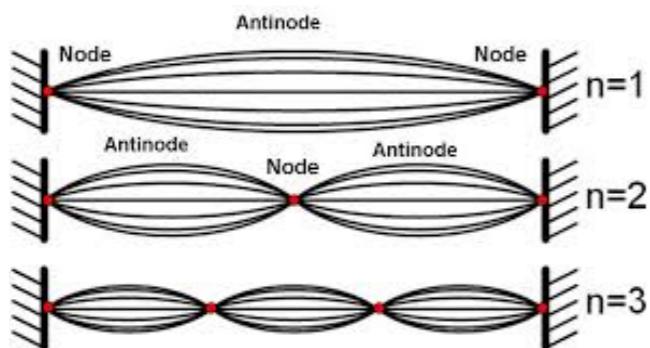
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**REFRESHER:** FOURIER SERIES



**MUSIC:** BRASS INSTRUMENTS,  
TIMBRE, BEAT PHENOMENA



**PROBLEMS:** 2-D TRAVELING WAVES

# How does this work, again?

---

$$h(x) = \sum_{n=1}^{\infty} a_n \cos(nx) + \sum_{m=1}^{\infty} b_m \sin(mx)$$

$$a_n = \frac{1}{\pi} \int_{-\infty}^{\infty} h(x) \cos(nx) \, dx$$

$$b_m = \frac{1}{\pi} \int_{-\infty}^{\infty} h(x) \sin(mx) \, dx$$

**Fourier series:** a representation of periodic functions, written as sines and cosines of different frequencies

# How does this work, again?

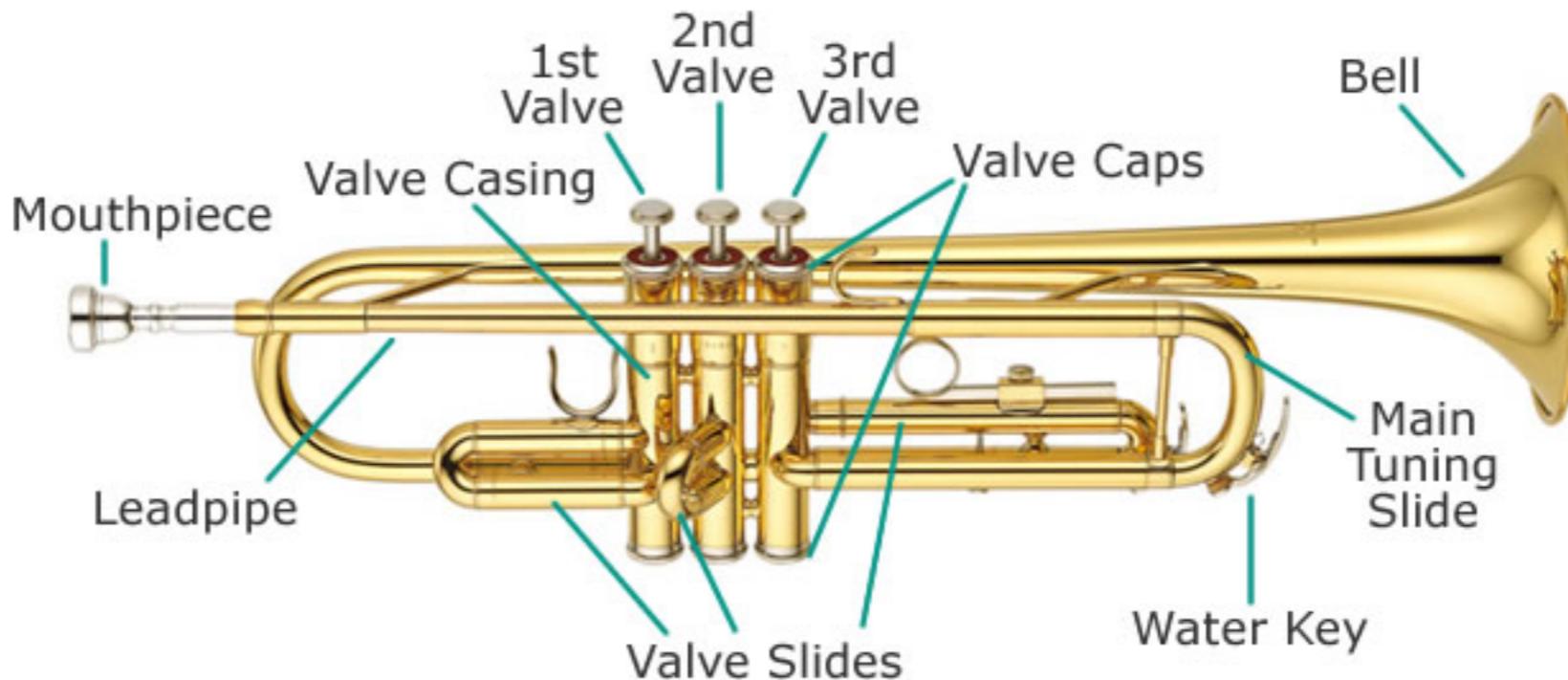
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**Fourier series:** a representation of periodic functions, written as sines and cosines of different frequencies



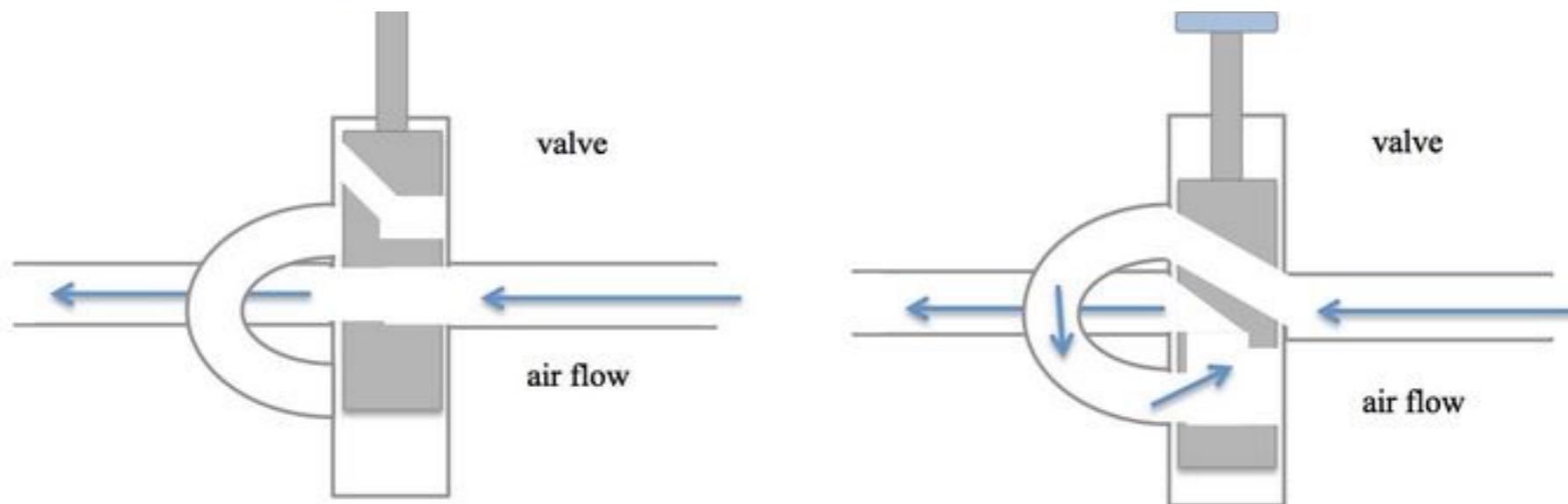
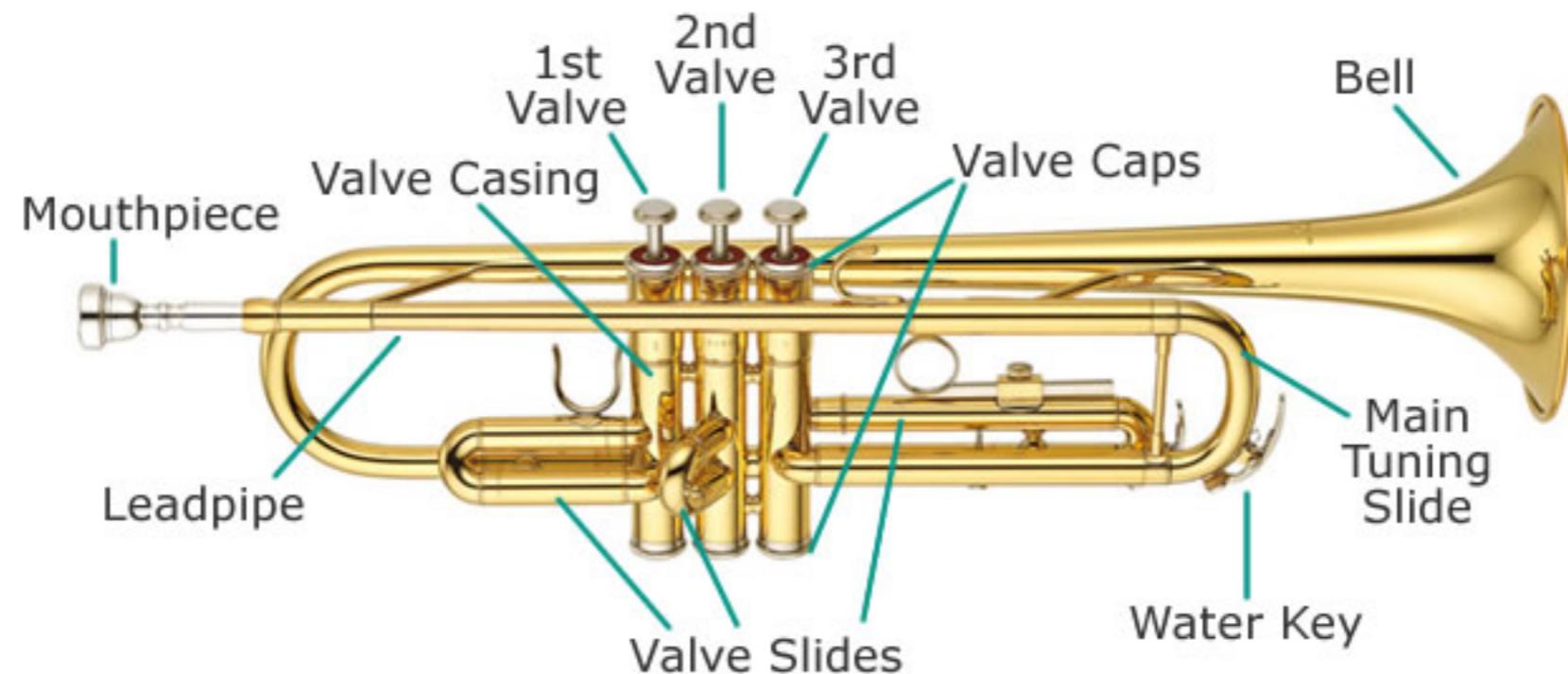
# example: brass instruments



**Sympathetic resonance:** a system responding to external vibrations that share harmonics

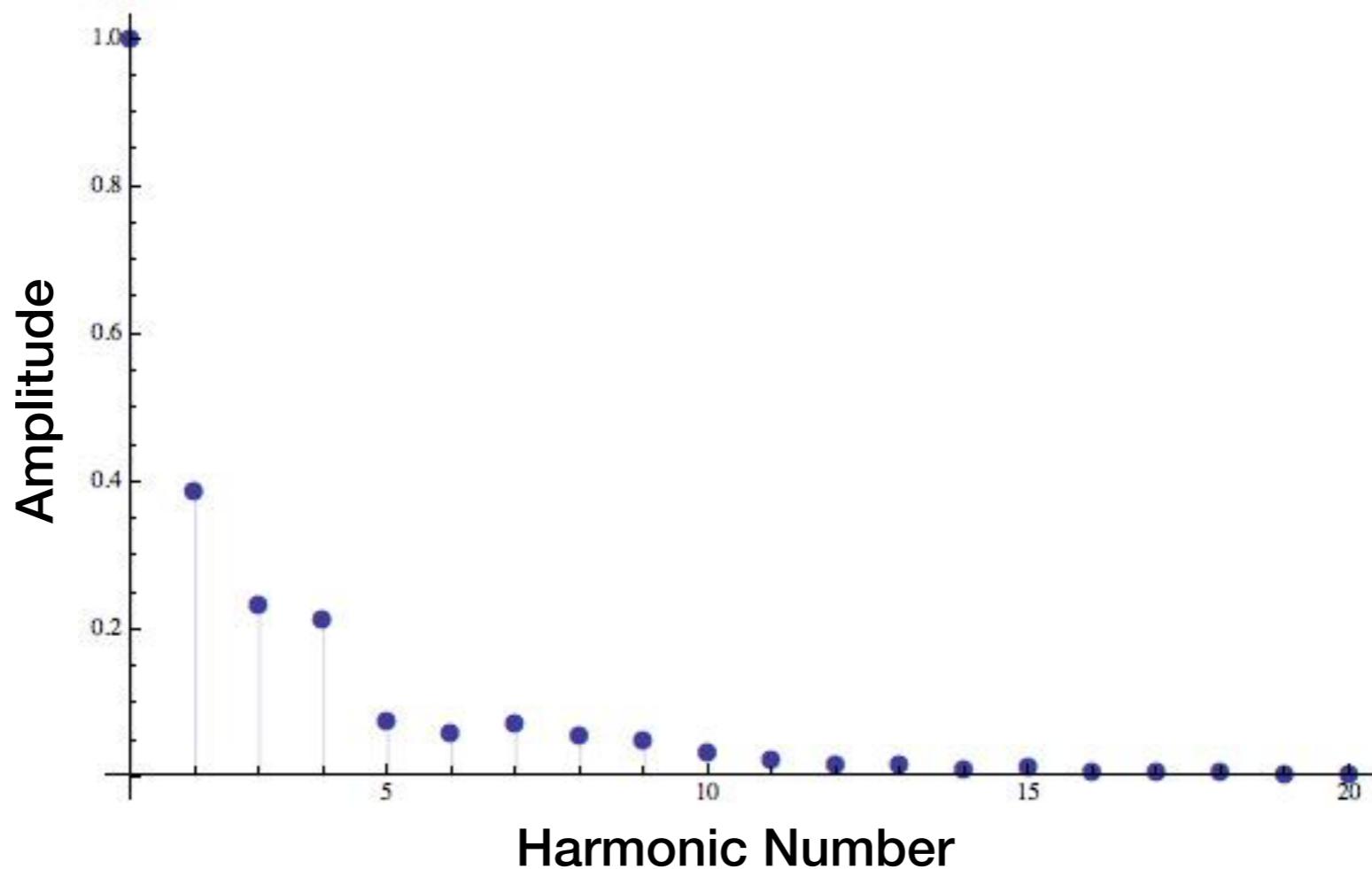
let's watch: <https://youtu.be/sxRkOQmzLgo?t=1m31s>

# example: brass instruments

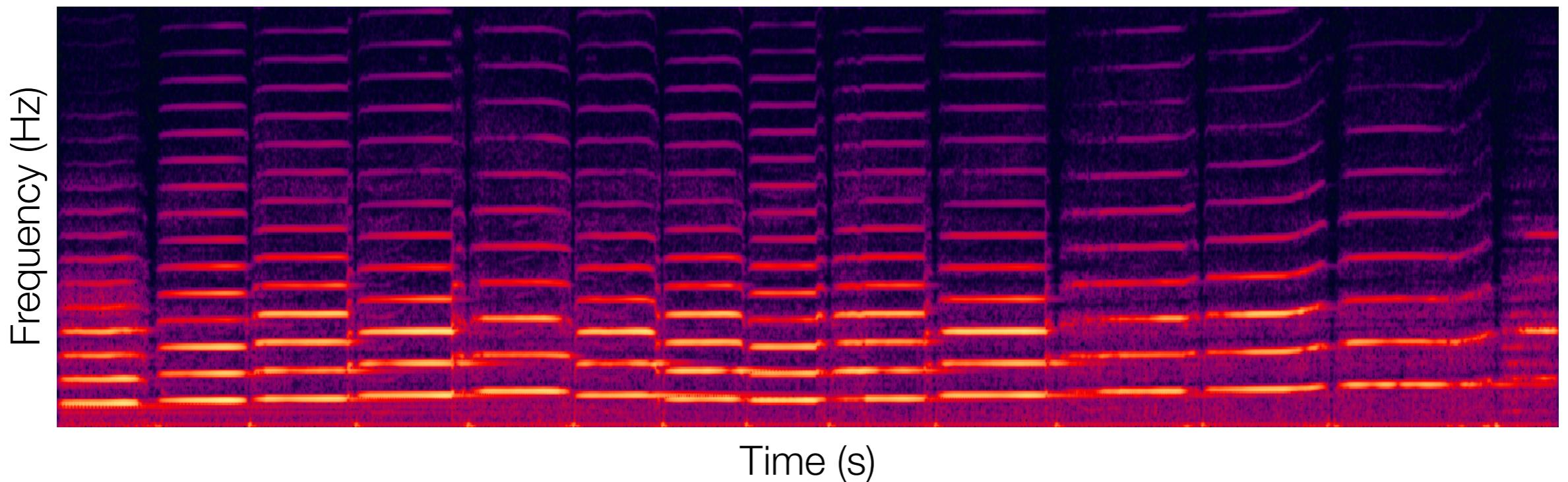


slides and valves used to change the length of tubing;  
embouchure, lip tension, air flow control specific harmonics

# example: brass instruments

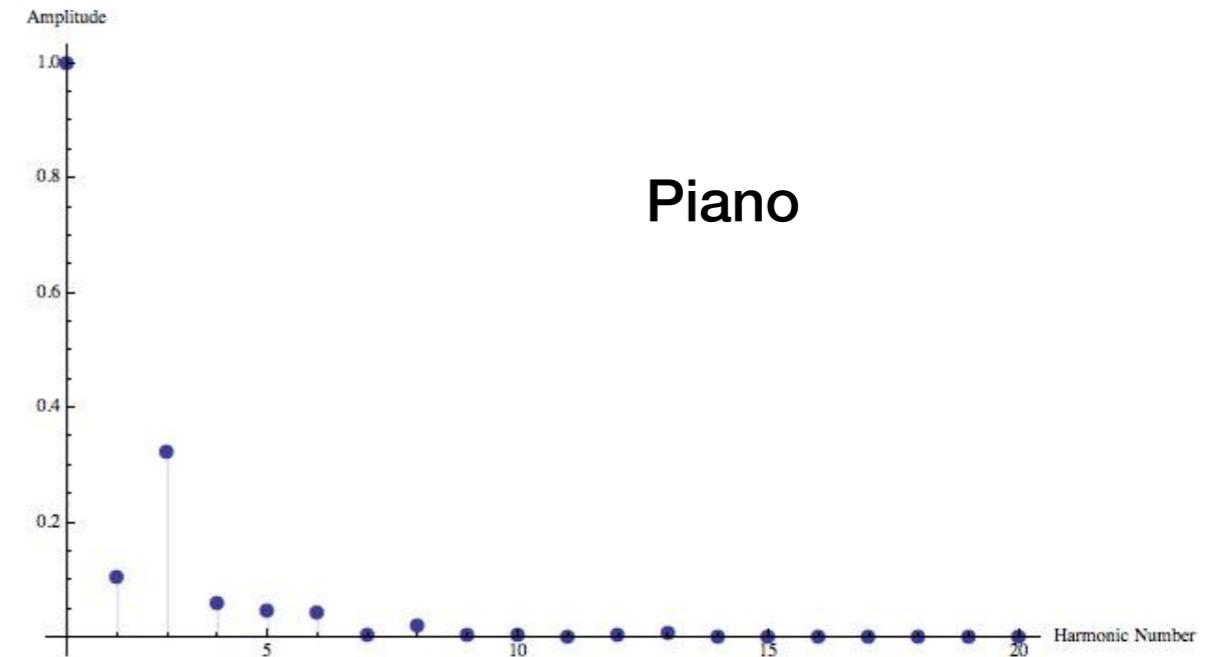
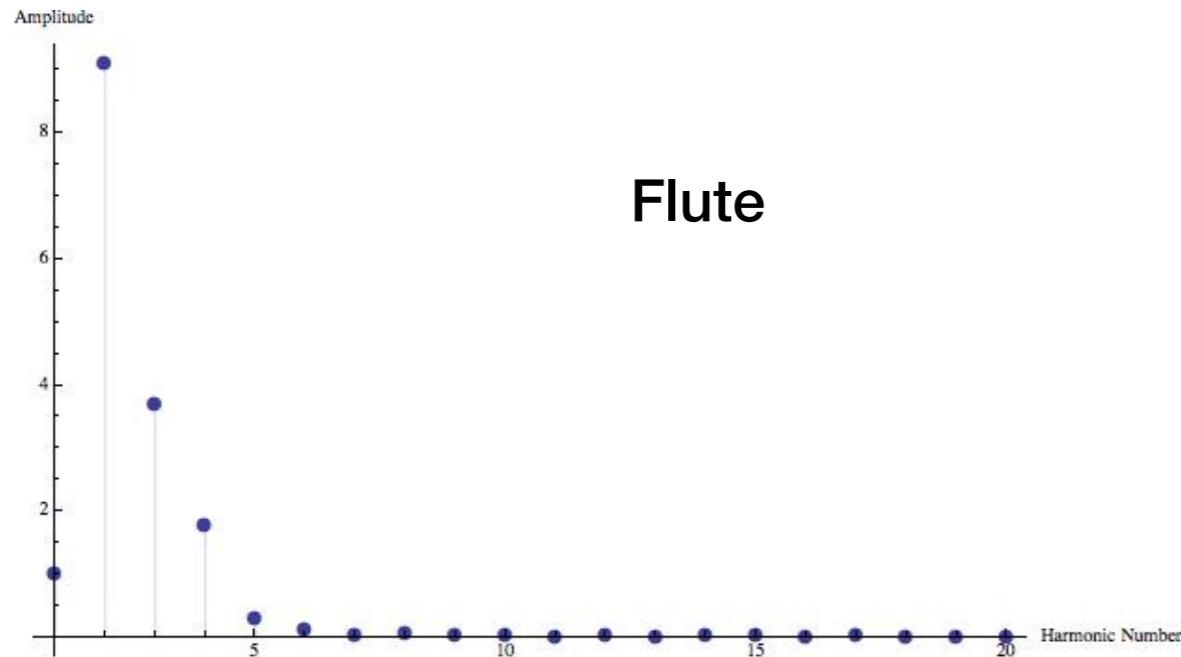


# example: string instruments



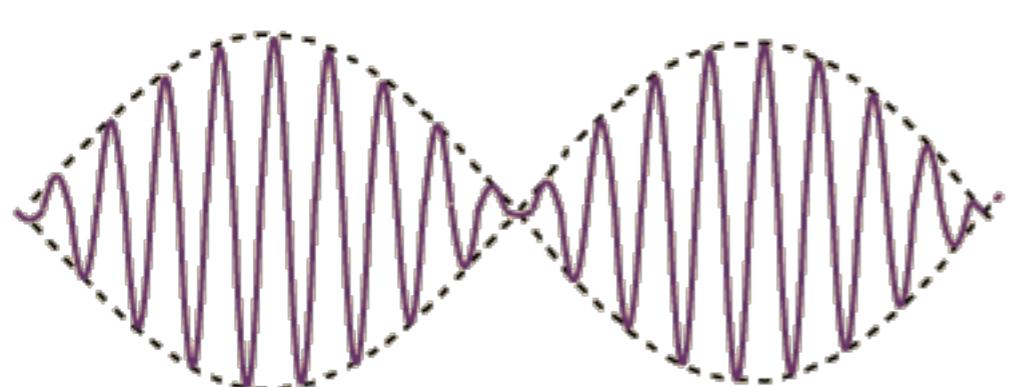
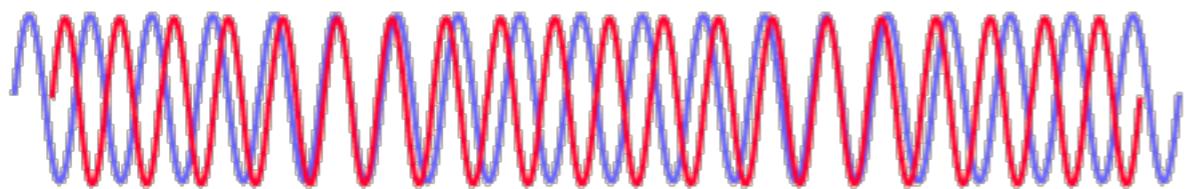
# why do separate instruments playing the same tone sound so different?

I'M YELLING 'TIMBRE!'



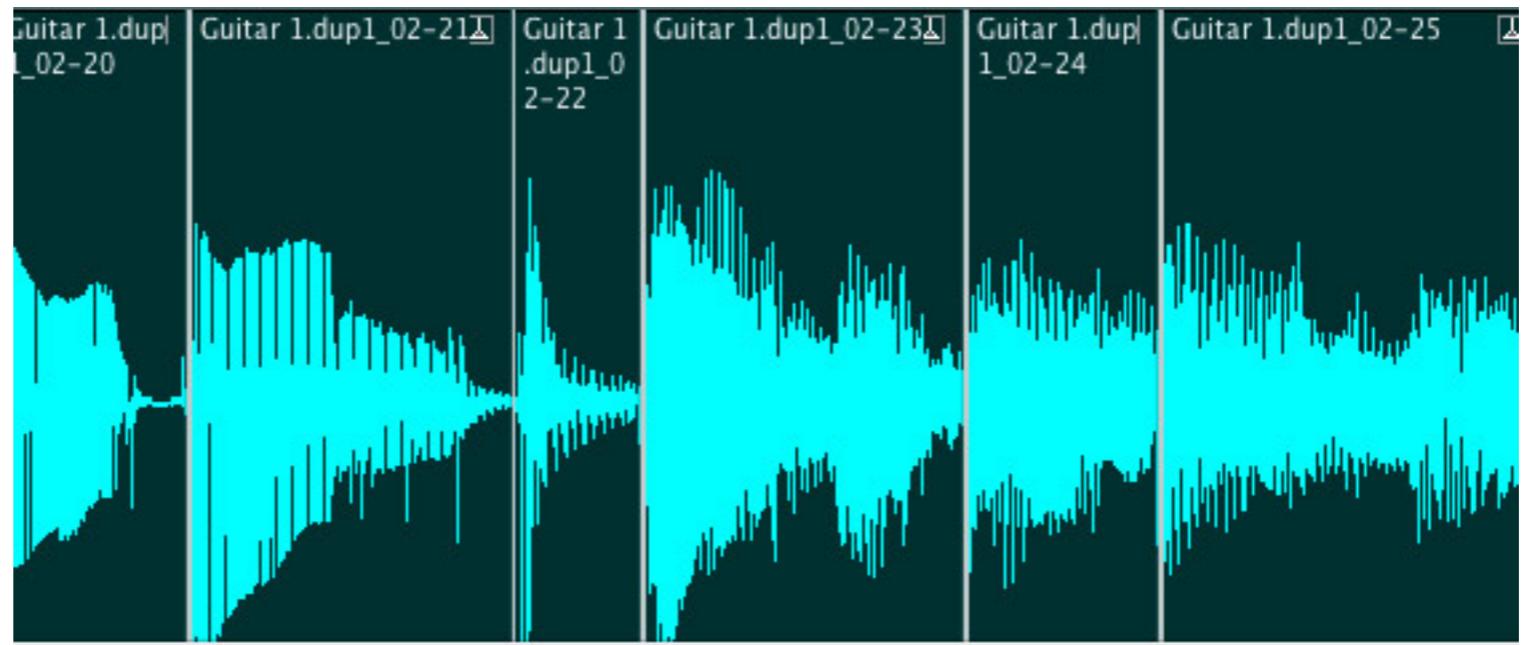
another example  
(play for sound)

# example: beat notes



$$\sin(\alpha \pm \beta) = \sin(\alpha)\cos(\beta) \pm \cos(\alpha)\sin(\beta)$$
$$\cos(\alpha \pm \beta) = \cos(\alpha)\cos(\beta) \mp \sin(\alpha)\sin(\beta)$$

guitar melody



# 2-D traveling waves

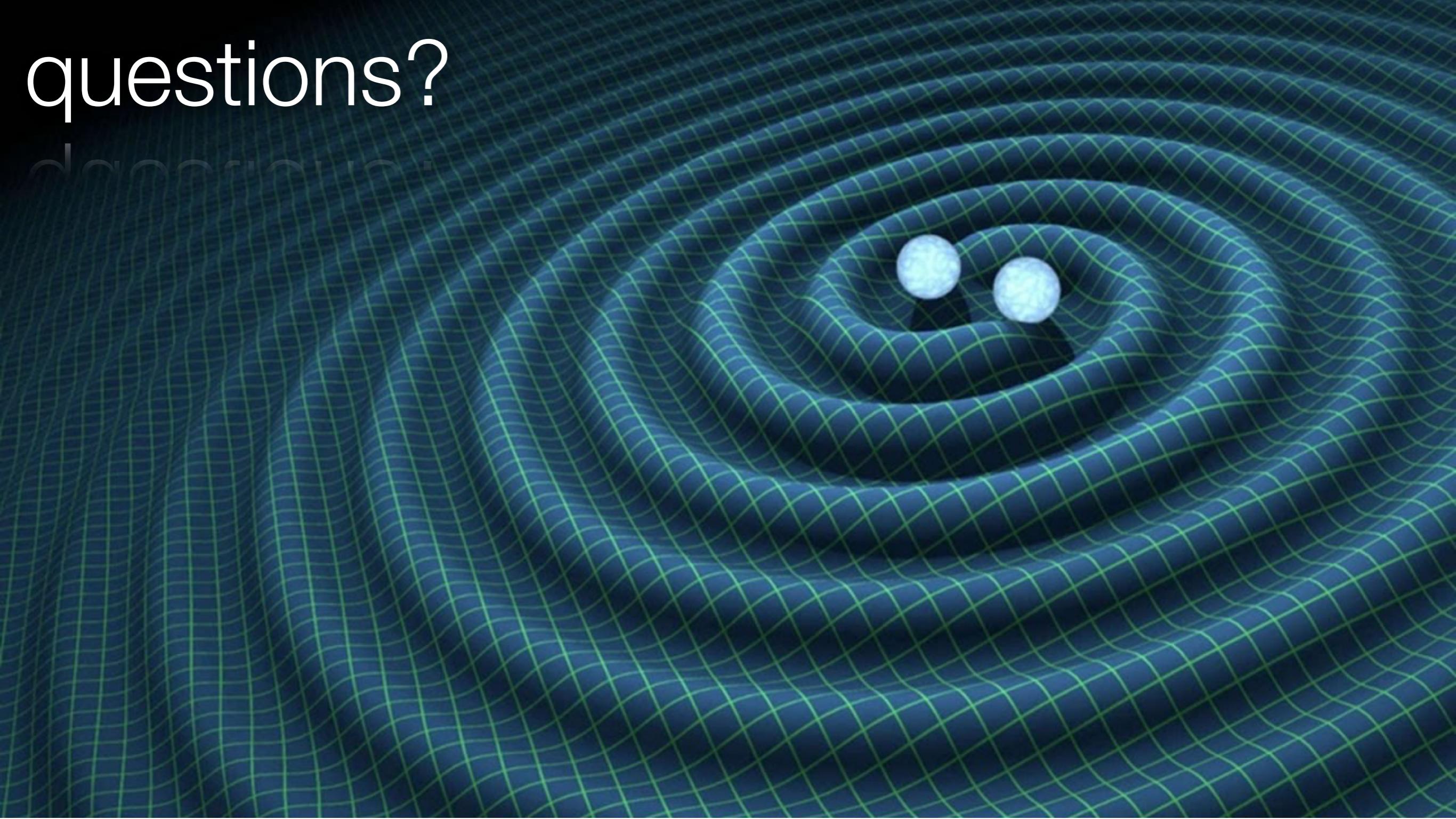
$$\frac{1}{v^2} \frac{\partial^2 h}{\partial t^2} = \frac{\partial^2 h}{\partial x^2} + \frac{\partial^2 h}{\partial y^2}$$

**2-D wave equation**  
 $h = h(x, y, t)$

# standing waves

questions?

dangerous.



**“every human being has, like Socrates, an attendant spirit; and wise are they who obey its signals.”**

**lydia m. child**

*philothea: a grecian romance*