

1. Consider the following definition of a `Vector2D` class:

```
class Vector2D {
    private double x;
    private double y;

    public Vector2D(double x, double y) {
        this.x = x;
        this.y = y;
    }

    public void add(Vector2D v) {
        this.x = this.x + v.x;
        this.y = this.y + v.y;
        // line A
    }
}
```

Suppose that the following program fragment is in a `main` method,

```
Vector2D v1 = new Vector2D(1, 1);
Vector2D v2 = new Vector2D(2, 2);
v1.add(v2);
```

- (a) Show the content of the stack and the heap when the execution reaches the line labeled `A` above. Label your variables and the values they hold clearly. You can use arrows to indicate object references. Draw boxes around the stack frames of the methods `main` and `add`, and label them.
- (b) Suppose that the representation of `x` and `y` have been changed to a `double` array:

```
class Vector2D {
    private double[] coord2D;
    :
}
```

What changes do you need for the other parts of class `Vector2D`?

Would the program fragment above still be valid?

2. Study the following `Point` and `Circle` classes.

```
public class Point {
    private double x;
    private double y;

    public Point(double x, double y) {
        this.x = x;
        this.y = y;
    }
}

public class Circle {

    private Point centre;
    private int radius;

    public Circle(Point centre, int radius) {
```

```
    this.centre = centre;
    this.radius = radius;
}

@Override
public boolean equals(Object obj) {
    System.out.println("equals(Object) called");
    if (obj == this) {
        return true;
    }
    if (obj instanceof Circle) {
        Circle circle = (Circle) obj;
        return (circle.centre.equals(centre) && circle.radius == radius);
    } else {
        return false;
    }
}

public boolean equals(Circle circle) {
    System.out.println("equals(Circle) called");
    return circle.centre.equals(centre) && circle.radius == radius;
}
}
```

Given the following program fragment,

```
Circle c1 = new Circle(new Point(0, 0), 10);
Circle c2 = new Circle(new Point(0, 0), 10);
Object o1 = c1;
Object o2 = c2;
```

- (a) What is the return value of `c1.equals(c2)`? Explain.
- (b) For each of the statement below, trace through the two-step dynamic binding process to show which `equals` method is invoked during run-time.
- (i) `o1.equals(o2);`
  - (ii) `o1.equals((Circle) o2);`
  - (iii) `o1.equals(c2);`
  - (iv) `c1.equals(o2);`
  - (v) `c1.equals((Circle) o2);`
  - (vi) `c1.equals(c2);`