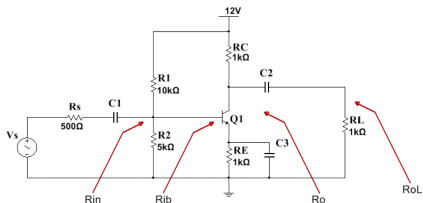


1. Consider the following common emitter amplifier circuit where $\beta = 70$, $V_{BE(ON)} = 0.7$ V, $V_A = 100$ V, $v_s = 10$ mV and $V_{CE(sat)} = 0.2$ V. Determine: small-signal parameters (r_π , r_o , r_o and g_m), R_{in} , R_{ib} , R_o , R_{oL} , signal current in collector (i_c), signal voltage at collector (v_c). Use π model and do not ignore output resistance r_o . Assume that the capacitors are large enough for the signal frequency.

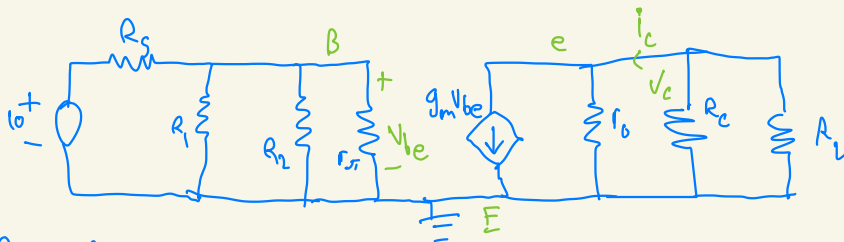


small signal analysis

$$r_\pi = \frac{V_T}{I_B} = 563.1 \quad r_e = \frac{V_T}{I_E} = 7.94 \Omega$$

$$r_o = \frac{V_A}{I_C} = 32.15 k\Omega \quad g_m = \frac{I_C}{V_T} = 124.3 mA/V$$

small signal model



$$R_{ib} = r_\pi = 563.1 \Omega$$

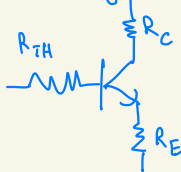
$$R_{in} = R_1 \parallel R_2 \parallel r_\pi = 481.6 \Omega$$

$$V_{be} = \frac{v_s R_{in}}{R_s + R_{in}} = 4.91 mV$$

$$v_c = -g_m V_{be} (r_o \parallel R_C \parallel R_L) = -300.7 mV$$

$$i_c = v_c / (R_C \parallel R_L) = 601.4 \mu A$$

DC analysis



$$R_{TH} = 10 k\Omega \parallel 5 k\Omega = 3.33 k\Omega$$

$$V_{TH} = \frac{A_2}{A_1 + A_2} V_{CC} = \frac{5}{10 + 5} \times 12 = 4V$$

$$I_B = \frac{V_{TH} - V_{BE}}{R_{TH} + R_E (\beta + 1)}$$

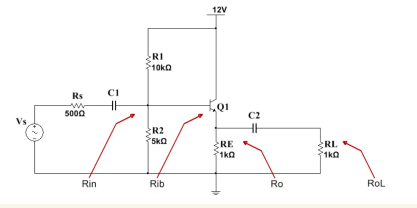
$$\text{where } I_B = 44.4 \mu A$$

$$I_C = \beta I_B = 3.100 mA$$

$$I_C + I_B = I_E = 3.15 mA$$

2. q4 is their q8

2. Consider the following common collector amplifier circuit where $\beta = 70$, $V_{BE(ON)} = 0.7$ V, $V_A = 100$ V, $V_s = 10$ mV and $V_{CE(sat)} = 0.2$ V. Determine the small-signal parameters (r_π , r_o , β and g_m), R_{in} , R_{ib} , R_o , R_{out} , voltage across the load R_L . Use T model and do not ignore output resistance r_o . Assume that the capacitors are large enough for the signal frequency.



similar to q1

$$R_{th} = 3.33 \text{ k}\Omega$$

$$V_{CE} = 12 - I_E R_E = 8.85 \text{ V}$$

$$V_{TH} = 4 \text{ V}$$

$$V_{th} - I_B R_{th} - V_{BE} - I_E R_E = 0$$

$$I_E = 3.1522 \text{ mA}$$

$$\text{so, } I_C = \frac{\beta}{\beta + 1} I_E = 3.11 \mu\text{A}$$

small signal parameters

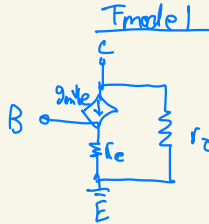
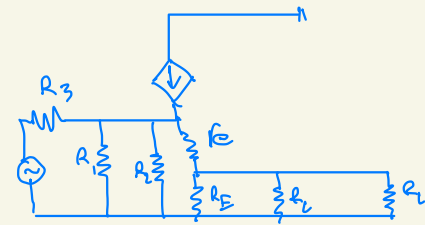
$$g_m = \frac{I_C}{V_T} = 124.3 \text{ mA/V}$$

$$r_e = \frac{V_T}{I_E} = 7.43 \Omega$$

$$r_\pi = \frac{V_T}{I_B} = 563.1 \Omega$$

$$r_o = \frac{V_A}{I_C} = 32.2 \text{ k}\Omega$$

AC analysis



left side

$$R_{ib} = (\beta + 1) [r_e + (R_E \parallel R_o \parallel R_L)] = 36 \text{ k}\Omega$$

$$R_{in} = R_1 \parallel R_2 \parallel R_{ib} = 3.1 \text{ k}\Omega$$

right

$$R_o = [r_e + \frac{R_1 \parallel R_2 \parallel R_3}{\beta + 1}] = 14 \Omega$$

$$R_{oL} = R_o \parallel R_L = 13.8 \Omega$$

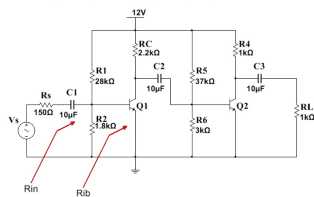
AC

$$V_i = V_s \cdot \frac{R_{in}}{R_s + R_{in}} = 8.7 \text{ mV}$$

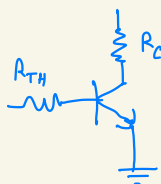
$$i_c = \frac{V_i}{r_e + R_E \parallel R_o \parallel R_L} = 17.4 \mu\text{A}$$

$$V_o = i_c (R_E \parallel R_o \parallel R_L) = 8.6 \text{ mV}$$

3. Consider the following two-stage common emitter amplifier circuit where the transistors are identical. Given that $\beta = 70$, $V_{BE(ON)} = 0.7$ V, $V_A = 100$ V, $V_i = 10$ mV and $V_{CE(sat)} = 0.2$ V. Determine: small-signal parameters ($r_{\pi 1}$, $r_{\pi 2}$, r_{e1} , r_{e2} , $r_{\pi 1}$, $r_{\pi 2}$ and $\beta = \beta_{ac}$), R_{in} , R_{out} , signal currents flowing in both collectors (i_{c1} , i_{c2}) signal voltage at both collectors (V_{c1} , V_{c2}). Do not ignore output resistance r_o . Assume that the capacitors are large enough for the signal frequency.



DC analysis



$$R_{TH} = 28k \parallel 1.8k = 1.69k\Omega$$

$$V_{TH} = \frac{R_2}{R_1 + R_2} V_A = 0.72V$$

$$I_B = \frac{0.72 - 0.7}{R_{TH}} = 14.67\mu A$$

$$I_C = 1.03mA$$

$$I_E = 1.04mA$$

$$r_{\pi 1} = 1.7k\Omega \quad r_{e1} = 24\Omega \quad r_{o1} = 9.4k\Omega$$

$$g_{m1} = 41.1mA/V$$

DC analysis Q2

$$R_{TH2} = R_5 \parallel R_6 = 2.78k\Omega$$

$$V_{TH2} = \frac{R_6}{R_5 + R_6} \cdot 12 = 0.9V$$

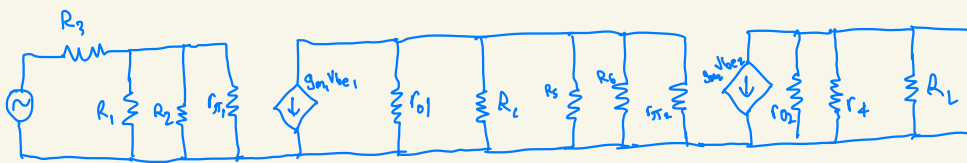
$$I_{B2} = \frac{0.9 - 0.7}{2.78k} = 72.1\mu A$$

$$I_{C2} = 5.05mA$$

$$I_{E2} = 5.12mA$$

$$g_{m2} = 201.9mA/V \quad r_{e2} = 4.9\Omega \quad r_{\pi 2} = 346.8\Omega \quad r_{o2} = 19.81k\Omega$$

AC analysis



$$V_4 = -g_{m1} V_{be1} \left(\frac{r_{o1} \parallel R_C \parallel R_5 \parallel R_6 \parallel r_{\pi 2}}{269.8\Omega} \right) = -41.1e^{-3} \cdot 8.5e^{-3} \cdot 269.8 = -94.2mV$$

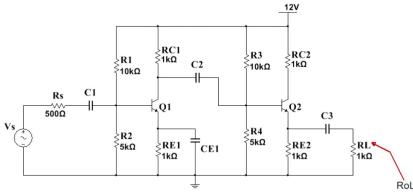
$$I_{c1} = \frac{V_{c1}}{(R_C \parallel R_5 \parallel R_6 \parallel r_{\pi 2})} = 348.2\mu A$$

$$V_{c2} = g_{m2} V_{be2} \left(\frac{r_{o2} \parallel R_4 \parallel R_2}{487.7\Omega} \right) = 201.9e^{-3} \cdot 94.2e^{-3} \cdot 487.7 = 9.3V$$

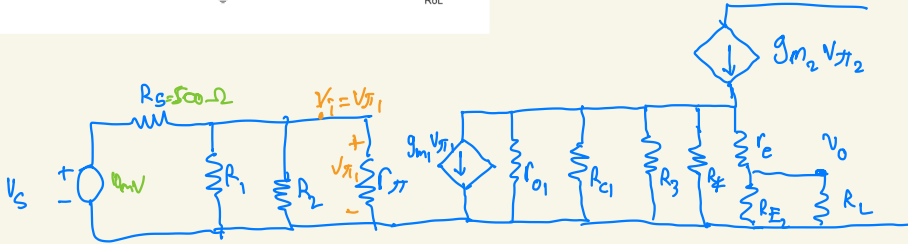
Finally

$$I_{C2} = \frac{V_{C2}}{R_4 \parallel R_2} = \frac{9.3}{500} = 18.6mA$$

4. Consider the following two-stage amplifier circuit where the transistors are identical. Given that $\beta = 70$, $V_{BE(ON)} = 0.7$ V, $V_A = 100$ V, $v_s = 10$ mV and $V_{CE(Sat)} = 0.2$ V. Determine: the voltage across load resistor R_L and output resistance R_{oL} as indicated in the circuit below. Do not ignore output resistance r_o . Assume that the capacitors are large enough for the signal frequency.



Biasing and small signal are same as before



$$R_{oL} = R_L // R_o = 18.2 \Omega$$

$$R_o = R_{E2} // [r_e + R_x (\beta + 1)] = 18.5 \Omega$$

$$R_x = R_4 // R_3 // R_{C1} // R_{A1} = 750 \Omega$$

$$V_i = v_s = \frac{R_{A1}}{R_2 + R_{in1}} \quad \dots R_{in1} = R_1 // R_2 // r_{\pi}$$

$$R_y = r_{o1} // R_{E1} // R_3 // R_4 // [(r_e + R_{E2} // R_L) \cdot (\beta + 1)]$$

$$V_{o1} = -g_{m1} V_i R_y$$

$$V_o = i_{c2} (R_{E2} // R_L)$$

$$i_{c2} = \frac{V_{o1}}{r_e + R_{E2} // R_L} \quad \therefore V_o = \frac{V_{o1}}{r_e + R_{E2} // R_L}$$

$$(R_{E2} // R_L) \approx V_{o1}$$

$$[\therefore R_{E2} // R_L \gg r_e]$$