

ENEL 619

Assignment 2

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Problem 1

$$P(F_1) = 0.01$$

$$P(F_2) = 0.03$$

$$P(F_3) = 0.02$$

$$P(F_4) = 0.01$$

$$P(F_1') = 0.99$$

$$P(F_2') = 0.97$$

$$P(F_3') = 0.98$$

$$P(F_4') = 0.99$$

$$\begin{aligned} P(\text{pass}) &= 0.99 \times 0.97 \times 0.98 \times 0.99 \\ &= 0.93168306 \approx 0.9317 \end{aligned}$$

$$a) P(\text{fail}) = 1 - P(\text{pass}) \approx \boxed{0.06832}$$

$$\begin{aligned} b) P(\text{Failed } F_2 \text{ or/and } F_3) &= P(F_2 \text{ and } F_3) \text{ or } P(F_2) \text{ or } P(F_3) \\ &= 0.03 \times 0.02 + 0.03 + 0.02 \\ &= \boxed{0.0506} \end{aligned}$$

Problem 2

26 letters in alphabet
6 sides to die

$$\begin{array}{cc} \overline{\quad} & \overline{\quad} \\ \uparrow & \uparrow \\ 26 & 6 \end{array}$$

Total elements in sample space:
2 spaces to fill

26 possibilities $\xrightarrow{\quad}$ $\xleftarrow{\quad}$ 6 possibilities

$$26 \times 6 \text{ possibilities} = 156$$

Problem 3

a) no. of ways :
$$\frac{10!}{1! \times 2! \times 4! \times 3!}$$

$$\boxed{= 12600}$$

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b) 3 types, Red (R), Green (G), Blue (B)

$$\frac{6!}{3! \times (6-3)!} = 20 \quad \text{Total ways to arrange balls}$$

\nearrow
 $\binom{6}{3} \text{ or } \binom{6}{3}$

$3! = 6$ ways to get 1 Red, 1 blue, 1 green.

So probability $P(1R, 1B, 1G) = \frac{6}{20}$

$$= 0.3$$

c) number of ways to have 2 defective out of 5:

$$\binom{4}{3} \times \binom{3}{2} = \frac{4!}{3!(4-3)!} \times \frac{3!}{2!(3-2)!}$$

$$= 4 \times 3 = 12$$

number of ways to have 3 defective out of 5:

$$\binom{4}{2} \times \binom{3}{3} = \frac{4!}{2!(4-2)!} \times \frac{3!}{3! \cdot 0!} = 6 \times 1 = 6$$

Total ways to have at least 2 defective

$$12 + 6 = 18$$

Problem 4

a) if order matters :

$$P_3^8 = \frac{8!}{(8-3)!} = \boxed{336}$$

b) if order doesn't matter:

$$C_3^8 = \binom{8}{3} = \frac{8!}{3!(8-3)!} = \boxed{56}$$

Problem 5

a) X random variable for no. of jazz CDs

Total combinations to select 4 CDs

$$C_4^{10} = \frac{10!}{4!(10-4)!} = 210$$

There are $C_x^5 \times C_{4-x}^5$ combinations to pick X jazz CDs into the 4 CD combination.

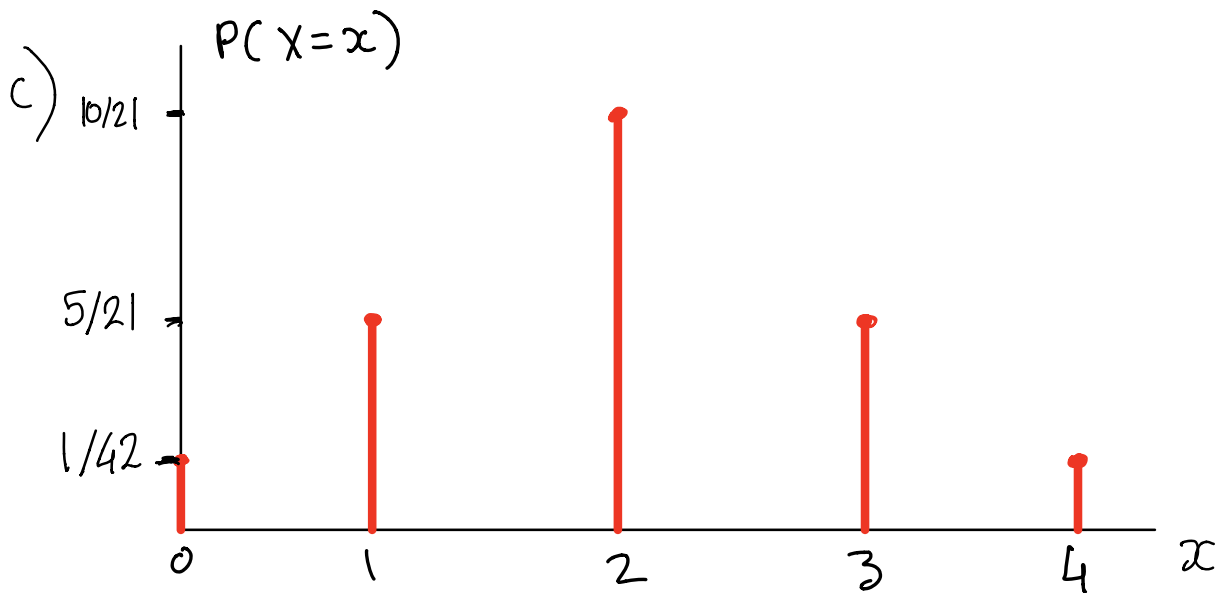
$$S_0, \\ P(X=x) = \frac{\binom{5}{x} \times \binom{5}{4-x}}{\binom{10}{4}} \quad \text{for } x \in \{0, 1, 2, 3, 4\}$$

$$= \frac{\frac{5!}{x!(5-x)!} \times \frac{5!}{(4-x)!(1+x)!}}{210} = \frac{(5!)^2}{210} \left(\frac{1}{x!(5-x)!} \times \frac{1}{(4-x)!(1+x)!} \right)$$

b)

x	$P(X=x)$
0	1/42
1	5/21
2	10/21
3	5/21
4	1/42

$$\frac{120}{210} = \frac{4}{7}$$



d) CDF $F_X(X=x) = P(X \leq x) = \sum_{x_i \leq x} P(X=x_i)$

x	$F_X(X=x)$
0	$1/42$
1	$11/42$
2	$31/42$
3	$41/42$
4	1

