Formula Sheet for ENEL 419 Final Exam:

	ENEL 419 Final Exam:
$P[\bar{A}] = 1 - P[A]$	$P[A B] = \frac{P[B A]P[A]}{P[B]}$
$P[A \cup B] = P[A] + P[B] - P[A \cap B]$	$P[A B] = \frac{P[B]}{P[B]}$
$P[A \cap B]$	$P[B A_i]P[A_i]$
$P[A B] = \frac{P[A \cap B]}{P[B]}$	$P[A_i B] = \frac{P[B A_i]P[A_i]}{\sum_{i=1}^{n} P[B A_i]P[A_i]}$
I [D]	$\sum_{i=1}^{n} P[B A_i]P[A_i]$
$f_X(x) = \int_{-\infty}^{\infty} f_{XY}(x, y) dy$	$f_{X Y}(x y) = \left(\frac{f_{XY}(x,y)}{f_{Y}(y)}\right)$
$J_X(x) = \int_{-\infty}^{\infty} J_{XY}(x,y) dy$	$J_{X Y}(x y) = \left(\frac{f_{Y}(y)}{f_{Y}(y)}\right)$
V – &	()1 () /
n!	n!
$_{n}P_{k}=\frac{n!}{(n-k)!}$	$\binom{n}{k} = \frac{n!}{(n-k)! k!}$
$(n-\kappa)!$	$(n-\kappa)!\kappa!$
	, ,
$N = \binom{n}{n_1} \binom{n-n_1}{n_2} \dots \binom{n-n_1-\dots-n_{K-1}}{n_2}$	$P[a \le X \le b, c \le Y \le d] = \int_{c}^{d} \int_{a}^{b} f_{XY}(x, y) dx dy$
an l	$P[a \le X \le b, c \le I \le a] = \int_a^b \int_{XY} (x, y) dx dy$
$=\frac{n!}{n!}$	Jc Ja
$= \frac{n!}{n_1! n_2! \dots n_K!}$ $F_{XY}(x, y) = P[X \le x, Y \le y]$	
$F_{YY}(x,y) = P[X \le x, Y \le y]$	$P[X > x] = Q\left(\frac{x - \mu_X}{\sigma_X}\right); \ \ Q(-\gamma) = 1 - Q(\gamma)$
AT C 70 Z	$ I[X > X] = Q \left(\int_{\sigma_X} f(Y) - I - Q(Y) \right) $
r.∞	2 11(14 12) 1 11(14) 2
$E[X^n] = \int_{-\infty}^{\infty} X^n f_X(x) dx; n = 1, 2,, n$	$\sigma_X^2 = E[(X - \mu_X)^2] = E[X^2] - \mu_X^2$
$\int_{-\infty}^{\infty} \int_{-\infty}^{\infty} (x) dx, n = 1, 2,, n$	
$E[g(x)] = \int_{-\infty}^{\infty} g(x) f_X(x) dx$	$C_{XY} = E[(X - \mu_X)(Y - \mu_Y)] = E[XY] - \mu_X \mu_Y$
$E[g(x)] = \int g(x)f_X(x)dx$	AI CONTACT INTO CONTACT
$J_{-\infty}$	
i _ 0.5	aT.
$p_i = \frac{i - 0.5}{n}; \ P[X_{(i)} \le z_i] = p_i$	$E[T] = \int_0^T R_T(t)dt$
n, -1 ,	$L[I] = \int_0^L R_I(t) dt$
	· ·
$F_T(t) = 1 - R(t)$	
	$R_T(t) = \int_{t}^{\infty} f_T(t)dt$
	J_t
	n
$\bar{X} = \frac{1}{n} \sum_{i=1}^{n} X_i$	$S_X^2 = \frac{1}{n-1} \sum_{i=1}^{N} (X_i - \bar{X})^2$
$A = \frac{1}{n} \sum_{i} A_{i}$	$S_X - \frac{1}{n-1} \sum_{i=1}^{n} (X_i - X_i)$
i=1	i=1
$1\sum_{n=1}^{n}$	$Z = \frac{X - \mu_X}{\sigma_Y / \sqrt{n}} \Rightarrow Gaussian distributed$
$S_X^2 = \frac{1}{n} \sum_{i=1}^{n} (X_i - \mu_X)^2$	$Z = \frac{1}{\sigma_{xx}/\sqrt{n}} \Rightarrow Gaussian aistributea$
i=1	οχ/ γ .ι.
$\bar{X} - \mu_X$	ρς .σ. Ι. Δ
$T = \frac{X - \mu_X}{S_X / \sqrt{n}} \Rightarrow t - distributed, v = n - 1$	$P[-z_c \le Z \le z_c] = 1 - \alpha \implies Q(z_c) = \frac{\alpha}{2}$
degrees of freedom	
	α
	$P[-t_c \le T \le t_c] = 1 - \alpha \implies Q(t_c) = \frac{\alpha}{2}$
	2
Bernoulli(p)	Binomial(n, p)
$p_X(x) = p^x (1 - p)^{1 - x}, x \in \{0, 1\}$	(12)
$p_X(x) = p (1-p) , x \in \{0, 1\}$	$p_X(x) = \binom{n}{x} p^x (1-p)^{n-x}; \ x = 0, 1,, n$
2	
$\mu_X = p; \sigma_X^2 = p(1-p)$	$\mu_X = np; \sigma_X^2 = np(1-p)$
	L-V X L b)
Geometric(p)	Uniform (k, l)
$p_X(x) = (1-p)^{x-1}p, \ x = 1, 2,, n$	
	$\mu_X = \frac{l+k}{2}; \sigma_X^2 = \frac{(l-k)(l-k+2)}{12}$
$1 \qquad (1-n)$	Z 1Z
$\mu_X = \frac{1}{2}; \sigma_X^2 = \frac{(1 - P)}{2}$	
$\mu_X = \frac{1}{p}; \sigma_X^2 = \frac{(1-p)}{p^2}$ $Poisson(\lambda)$	
$Poisson(\lambda)$	$ ho_{XY} = rac{C_{XY}}{\sigma_X \sigma_Y}$
$p_X(x) = \frac{\lambda^x}{x!} e^{-\lambda}, x = 0, 1, 2,$	$\rho_{XY} - \sigma_X \sigma_Y$
$p_X(x) - \frac{1}{x!}e^{-x}, x = 0, 1, 2, \dots$	
$\mu_X = \lambda; \sigma_X^2 = \lambda$	
A	
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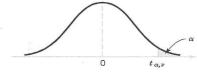
H_0	Value of Test Statistic	H_1	Critical Region
$\mu = \mu_0$	$z = \frac{\bar{x} - \mu_0}{\sigma / \sqrt{n}}; \sigma \text{ known}$	$\mu < \mu_0$	$z < -z_{\alpha}$
		$\mu > \mu_0$	$z>z_{lpha}$
		$\mu eq \mu_0$	$z < -z_{\alpha/2}$ or $z > z_{\alpha/2}$
$\mu = \mu_0$	$\bar{x} - \mu_0$	$\mu < \mu_0$	$t < -t_{\alpha}$
	$t = \frac{\bar{x} - \mu_0}{s/\sqrt{n}}; v = n - 1,$	$\mu > \mu_0$	$t > t_{\alpha}$
	σ unknown	$\mu \neq \mu_0$	$t < -t_{\alpha/2} \text{ or } t > t_{\alpha/2}$
$\mu_1 - \mu_2 = d_0$	$(ar{x}_1-ar{x}_2)-d_0$	$\mu_1 - \mu_2 < d_0$	
	$z = \frac{(\bar{x}_1 - \bar{x}_2) - d_0}{\sqrt{\sigma_1^2/n_1 + \sigma_2^2/n_2}};$	$\mu_1 - \mu_2 > d_0$	$z > z_{\alpha}$
	σ_1 and σ_2 known	$\mu_1 - \mu_2 \neq d_0$	$z < -z_{\alpha/2}$ or $z > z_{\alpha/2}$
$_1 - \mu_2 = d_0$	$t = \frac{(\bar{x}_1 - \bar{x}_2) - d_0}{s_p \sqrt{1/n_1 + 1/n_2}};$ $v = n_1 + n_2 - 2,$ $\sigma_1 = \sigma_2 \text{ but unknown,}$ $s_p^2 = \frac{(n_1 - 1)s_1^2 + (n_2 - 1)s_2^2}{n_1 + n_2 - 2}$	$\mu_1 - \mu_2 < d_0$ $\mu_1 - \mu_2 > d_0$ $\mu_1 - \mu_2 \neq d_0$	
$_1 - \mu_2 = d_0$	$t' = \frac{(\bar{x}_1 - \bar{x}_2) - d_0}{\sqrt{s_1^2/n_1 + s_2^2/n_2}};$ $v = \frac{(s_1^2/n_1 + s_2^2/n_2)^2}{\frac{(s_1^2/n_1)^2}{n_1 - 1} + \frac{(s_2^2/n_2)^2}{n_2 - 1}};$ $\sigma_1 \neq \sigma_2 \text{ and unknown}$	$\mu_1 - \mu_2 < d_0$ $\mu_1 - \mu_2 > d_0$ $\mu_1 - \mu_2 \neq d_0$	
$d_D = d_0$	$\overline{d}-d_0$	$\mu_D < d_0$	$t < -t_{\alpha}$
$_{ m ired}$	$t = \frac{\overline{d} - d_0}{s_d / \sqrt{n}};$	$\mu_D > d_0$	$t > t_{\alpha}$
oservations	v = n - 1	$\mu_D \neq d_0$	$t < -t_{\alpha/2}$ or $t > t_{\alpha/2}$

Table 1: Values of Q(x) for $0 \le x \le 9$

Table 1. Values of $Q(x)$ for $0 \le x \le 9$	
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	$X \qquad Q(X)$
$0.00 0.5$ $2.30 0.010724$ $4.55 2.6823 \times 10^{-6}$	6.80 5.231 \times 10 ⁻¹²
$0.05 0.48006$ $2.35 0.0093867$ $4.60 2.1125 \times 10^{-6}$	$6.85\ 3.6925 \times 10^{-12}$
$0.10 0.46017$ $2.40 0.0081975$ $4.65 1.6597 \times 10^{-6}$	$6.90\ 2.6001 \times 10^{-12}$
$0.15 0.44038$ $2.45 0.0071428$ $4.70 1.3008 \times 10^{-6}$	$6.95 \ 1.8264 \times 10^{-12}$
$0.20 0.42074$ $2.50 0.0062097$ $4.75 1.0171 \times 10^{-6}$	$7.00\ 1.2798 \times 10^{-12}$
$0.25 0.40129$ $2.55 0.0053861$ $4.80 7.9333 \times 10^{-7}$	$7.05\ 8.9459 \times 10^{-13}$
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	$7.106.2378 \times 10^{-13}$
$0.35 0.36317$ $2.65 0.0040246$ $4.90 4.7918 \times 10^{-7}$	$7.15 4.3389 \times 10^{-13}$
$0.40 0.34458$ $2.70 0.003467$ $4.95 3.7107 \times 10^{-7}$	$7.20\ 3.0106 \times 10^{-13}$
$0.45 0.32636$ $2.75 0.0029798$ $5.00 2.8665 \times 10^{-7}$	$7.25\ 2.0839 \times 10^{-13}$
$0.50 0.30854$ $2.80 0.0025551$ $5.05 2.2091 \times 10^{-7}$	$7.30\ 1.4388 \times 10^{-13}$
$0.55 0.29116$ $2.85 0.002186$ $5.10 1.6983 \times 10^{-7}$	$7.35 \ 9.9103 \times 10^{-14}$
$0.60 0.27425$ $2.90 0.0018658$ $5.15 1.3024 \times 10^{-7}$	$7.40 \ 6.8092 \times 10^{-14}$
$0.65 0.25785$ $2.95 0.0015889$ $5.20 9.9644 \times 10^{-8}$	7.45 4.667×10^{-14}
$0.70 0.24196$ $3.00 0.0013499$ $5.25 7.605 \times 10^{-8}$	$7.50\ 3\ .1909 \times 10^{-14}$
$0.75 0.22663$ $3.05 0.0011442$ $5.30 5.7901 \times 10^{-8}$	$7.55\ 2\ .1763 \times 10^{-14}$
$0.80 0.21186 \qquad 3.10 0.0009676 5.35 4.3977 \times 10^{-8}$	$7.60\ 1.4807 \times 10^{-14}$
$0.85 0.19766 \qquad 3.15 0.00081635 5.40 3.332 \times 10^{-8}$	$7.65\ 1.0049 \times 10^{-14}$
$\begin{vmatrix} 0.90 & 0.18406 & \begin{vmatrix} 3.20 & 0.00068714 & \end{vmatrix} & 5.45 & 2.5185 \times 10^{-8} \end{vmatrix}$	$7.70 \ 6.8033 \times 10^{-15}$
$0.95 0.17106$ $3.25 0.00057703$ $5.50 1.899 \times 10^{-8}$	$7.75 \cdot 4.5946 \times 10^{-15}$
$\begin{vmatrix} 1.00 & 0.15866 \\ \end{vmatrix}$ $\begin{vmatrix} 3.30 & 0.00048342 \\ \end{vmatrix}$ $\begin{vmatrix} 5.55 & 1.4283 \times 10^{-8} \\ \end{vmatrix}$	$7.80\ 3\ .0954 \times 10^{-15}$
1.05 0.14686	$7.85\ 2.0802 \times 10^{-15}$
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	$7.90\ 1.3945 \times 10^{-15}$
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	$7.95\ 9\ .3256 \times 10^{-16}$
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	$8.00 6.221 \times 10^{-16}$
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	$8.05 \cdot 4.1397 \times 10^{-16}$
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	$8.10 2.748 \times 10^{-16}$
$\frac{1}{5}$	$8.15 \ 1.8196 \times 10^{-16}$
5 95 340/ \$10 ?	$8.20 \ 1.2019 \times 10^{-16}$
$\begin{vmatrix} 1.45 & 0.07520 & & 2.75 & 0.0417 & 40-5 & & 6.00 & 9.8659 \times 10^{-10} \end{vmatrix}$	$8.257.9197 \times 10^{-17}$
- 6.05 /.2423 <i>X</i> 10 ¹⁰	$8.30\ 5.2056 \times 10^{-17}$
1.50 0.066807 3.80 7.2348 \times 10 ⁻⁵ 6.10 5.3034 \times 10 ⁻¹⁰	$8.35\ 3.4131 \times 10^{-17}$
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	$8.40\ 2.2324 \times 10^{-17}$
1.60 0.054799 3.90 4.8096×10^{-5} 6.20 2.8232×10^{-10}	$8.45 \ 1.4565 \times 10^{-17}$
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	$8.50\ 9.4795 \times 10^{-18}$
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	$8.556.1544 \times 10^{-18}$
1.75 0.040059 4.05 2.5609 $\times 10^{-5}$ 6.35 1.766 $\times 10^{-10}$	$8.60\ 3.9858 \times 10^{-18}$
1.80 0.03593 4.10 2.0658 \times 10 ⁻⁵ 6.40 7.7688 \times 10 ⁻¹¹	$8.65 \ 2.575 \times 10^{-18}$
1.85 0.032157 4.15 1.6624×10^{-5} 6.45 5.5925×10^{-11}	$8.70\ 1.6594 \times 10^{-18}$
1.90 0.028717 4.20 1.3346×10^{-5} 6.50 4.016×10^{-11}	$8.75\ 1.0668 \times 10^{-18}$
$\begin{vmatrix} 1.95 & 0.025588 \end{vmatrix}$ $\begin{vmatrix} 4.25 & 1.0689 \times 10^{-5} \\ 4.25 & 0.5322 & 4.36 \end{vmatrix}$ $\begin{vmatrix} 6.55 & 2.8769 \times 10^{-11} \\ 6.55 & 0.8769 \times 10^{-11} \end{vmatrix}$	8.80 6 .8408 × 10 ⁻¹⁹
$\begin{vmatrix} 2.00 & 0.02275 \end{vmatrix}$ $\begin{vmatrix} 4.30 & 8.5399 \times 10 \end{vmatrix}$ $\begin{vmatrix} 6.60 & 2.0559 \times 10^{-11} \end{vmatrix}$	$8.85 4.376 \times 10^{-19}$
$\begin{vmatrix} 2.05 & 0.020182 \end{vmatrix}$ $\begin{vmatrix} 4.35 & 6.8069 \times 10 \end{vmatrix}$ $\begin{vmatrix} 6.65 & 1.4655 \times 10^{-11} \end{vmatrix}$	$8.90 \ 2.7923 \times 10^{-19}$
$\begin{vmatrix} 2.10 & 0.017864 \end{vmatrix}$ $\begin{vmatrix} 4.40 & 5.4125 \times 10 \end{vmatrix}$ $\begin{vmatrix} 6.70 & 1.0421 \times 10^{-11} \end{vmatrix}$	$8.95 \ 1.7774 \times 10^{-19}$
$2.15 \ 0.015778$ $4.45 \ 4.2935 \times 10^{-12}$	$9.00 \ 1.1286 \times 10^{-19}$
$2.20 \ 0.013903$ $4.50 \ 3.3977 \times 10^{-6}$ $0.73 \ 7.3723 \times 10^{-6}$	1111 = 122007,20
2.25 0.012224	

https://www.usna.edu/ECE/ee354/Handouts/Q-function.pd

Table of Student t-Distribution Functions



TABLEV Percentage Points $t_{\alpha,\nu}$ of the t Distribution .40 .25 .0025 .0005 .10 .05 .025 .01 .005 .001 1 .325 1.000 3.078 6.314 12.706 31.821 63.657 127.32 318.31 636.62 2 .289 .816 1.886 2.920 4.303 6.965 9.925 14.089 23.326 31.598 .765 3 .277 1.638 2.353 3.182 4.541 5.841 7.453 10.213 12.924 4 .271 .741 1.533 2.132 2.776 3.747 4.604 5.598 7.173 8.610 5 .267 .727 1.476 2.015 2.571 3.365 4.032 4.773 5.893 6.869 .718 .265 1.440 2.447 3.707 4.317 5.208 5.959 6 1.943 3.143 7 .263 .711 1.415 1.895 2.365 2.998 3.499 4.029 4.785 5.408 8 .262 .706 1.397 1.860 2.306 2.896 3.355 3.833 4.501 5.041 9 .703 .261 1.383 1.833 2.262 2.821 3.250 3.690 4.297 4.781 10 .260 .700 1.372 1.812 2.228 2.764 3.169 3.581 4.144 4.587 11 .260 .697 1.363 1.796 2.201 2.718 3.106 3.497 4.025 4.437 3.428 3.930 12 .259 .695 1.356 1.782 2.179 2.681 3.055 4.318 .259 .694 1.350 1.771 2.160 2.650 3.012 3.372 3.852 4.221 13 14 .258 .692 1.345 1.761 2.145 2.624 2.977 3.326 3.787 4.140 3.286 15 .258 .691 1.341 1.753 2.131 2.602 2.947 3.733 4.073 .258 2.120 2.583 3.252 4.015 16 .690 1.337 1.746 2.921 3.686 17 .257 .689 1.333 1.740 2.110 2.567 2.898 3.222 3.646 3.965 18 .257 .688 1.330 1.734 2.101 2.552 2.878 3.197 3.610 3.922 3.579 19 .257 1.328 1.729 2.093 2.539 2.861 3.174 3.883 .688 20 .257 1.725 2.086 2.528 2.845 3.153 3.552 3.850 .687 1.325 21 .257 .686 1.323 1.721 2.080 2.518 2.831 3.135 3.527 3.819 22 2.074 2.508 2.819 3.119 3.505 3.792 .256 .686 1.321 1.717 2.500 2.807 3.104 3.485 3.767 23 .256 .685 1.319 1.714 2.069 24 .256 .685 1.318 1.711 2.064 2.492 2.797 3.091 3.467 3.745 25 3.078 3.725 .256 1.316 1.708 2.060 2.485 2.787 3.450 .684 26 .256 .684 1.315 1.706 2.056 2.479 2.779 3.067 3.435 3.707 27 .256 .684 1.314 1.703 2.052 2.473 2.771 3.057 3.421 3.690 28 .256 .683 1.701 2.048 2.467 2.763 3.047 3.408 3.674 1.313 29 .256 .683 1.311 1.699 2.045 2.462 2.756 3.038 3.396 3.659 30 .256 .683 1.310 1.697 2.042 2.457 2.750 3.030 3.385 3.646 40 255 .681 1.303 1.684 2.021 2.423 2.704 2.971 3.307 3.551 60 .254 .679 1.296 1.671 2.000 2.390 2.660 2.915 3.232 3.460 120 .254 .677 1.289 1.658 1.980 2.358 2.617 2.860 3.160 3.373 2.576 2.807 3.090 3.291 00 .253 .674 1.282 1.645 1.960 2.326

v =degrees of freedom.