ID#: 30080225	Last Name: AL-khou(Y	First Name:
	Start time	Due date and time
Quiz #3	Thursday, October 29, 2020	Friday 30, 2020, 5:0pm

Question 1:

A random variable X, has a PDF given by

$$f_X(x) = \begin{cases} cx^2, & -2 < x < 2, \\ 0, & \text{otherwise.} \end{cases}$$

- (a) Find the value of c and use it to
- (b) Find the CDF
- (c) Evaluate the probability $P\left[\left|X \frac{1}{2}\right| < 1\right]$.

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Question 2:

Suppose men's shirt sizes are approximately Gaussian distributed with mean 16.2 inches and variance 0.81 square inches.

- (a) Find the probability that the neck size of a randomly selected man lies in the range 13.5" and 18.9". Express your answer to four decimal places.
- (b) Suppose we change the mean to 16.0 inches. Find the value of the variance such that the probability of the neck size of a randomly selected man lying in the range 13.5" and 18.5" remains the same as in part (a).

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a)
$$f_{\chi} = \left(\begin{array}{ccc} c \chi^2 & -2 \mathcal{L} \chi \angle 2 \\ 0 & \text{otherwise} \end{array} \right)$$

$$\int_{-\infty}^{\infty} f_{x}(x) dx = 1 \Rightarrow \int_{-2}^{2} c x^{2} dx = 1$$

$$\frac{1}{3}x^{3} \cdot c \Big|_{-2}^{2} = \frac{8}{3}c - \left(-\frac{8}{3}c\right) = \frac{16}{3} \cdot c = 1$$

$$C = \frac{3}{16}$$

b) (OF of
$$X = F_x(x) = P(X \leq x)$$

$$F_{\pi}(x) = \int_{-\infty}^{x} f_{u}(u) du$$

$$F_{\chi}(x) = \int_{-\infty}^{\chi} f_{u}(u) du = \int_{-\infty}^{\chi} o du = 0$$

$$F_{x}(x) = \int_{-2}^{x} f_{u}(u) du = \int_{-2}^{x} c u^{2} du = \int_{-2}^{x} \frac{3}{16} u^{2} du = \frac{1}{16} \left[u^{3} \Big|_{-2}^{x} \right] = \frac{1}{16} x^{3} - \left(\frac{1}{16} \cdot -8 \right)$$

$$= \frac{1}{16} x^{3} + \frac{1}{2} = \left[\frac{x^{3} + 8}{16} \right]$$

$$F_{x}(x) = \int_{0}^{x} 0 du = 0$$

$$\begin{array}{l} \text{C} \quad P \left[| X - \frac{1}{2} | < 1 \right] = P \left[-1 < X - \frac{1}{2} < 1 \right] \\ \text{V} = X - \frac{1}{2} \quad X = Y + \frac{1}{2} \quad (\text{orge of } Y =) \quad -\frac{6}{2} < y < \frac{3}{2} \\ \text{J} \quad y = \frac{1}{2} \cdot \frac{1}{2} \cdot \frac{1}{2} = \frac{3}{16} \left[y + \frac{1}{2} \right]^2 = \frac{3}{16} \left[y^2 + y + \frac{1}{4} \right] \\ \text{J} \quad y = \frac{1}{2} \cdot \frac{1}{2}$$

P[13.5 < X < 189] = 0.9973002

$$P[13.5 < \times < 18.5] = P[13.5 < \times < 18.9] = 0.9973002$$

$$P[Z < \frac{18.5 - \mu}{\sigma}] - P[Z < \frac{13.5 - \mu}{\sigma}] = 0.9973002$$

$$\frac{18.5 - 16}{\sigma} = 3$$

$$\frac{13.5 - 16}{\sigma} = -3$$

$$\sqrt{\sigma} = \frac{5}{6}$$