$\int_{\chi_y} f(x,y) = \left\{ \begin{array}{c} \frac{2(1+3y^2)}{4}, & 0 < x < 1 \\ 0, & \text{otherwise} \end{array} \right.$

Independent if $f_{xy}(x,y) = f_{x}(x) \cdot f_{y}(y)$

 $f_{x}(x) = \int_{0}^{1} f_{xy}(x,y) dy = \left[\frac{xy}{4} + \frac{xy^{3}}{4} \right]_{0}^{1} = \left[\frac{x+x}{4} \right] - 0 = \frac{x}{2}$

 $f_{y}(y) = \int_{0}^{2} f_{xy}(2y) dx = \left[\frac{27}{8}(1+3y^{2})\right]_{0}^{2} = \frac{4}{8}(1+3y^{2}) - 0 = \frac{1+3y^{2}}{2}$

 $f_{xy}(z_{,y}) = f_{x}(z) \cdot f_{y}(y) = \frac{z}{z} \left(\frac{(+3y^{2})}{z} \right) = \frac{z(+3y^{2})}{4}$

Random variables X and Y are independent

$$\int_{xy} (x_1 y) = \begin{cases} \frac{3}{2}(x^2 + y^2) & 0 \le x \le 1, 0 \le y \le 1 \\ 0 & \text{otherwise} \end{cases}$$

a)
$$f_{x}(z) = \int_{0}^{1} \frac{3}{2} (z^{2} + y^{2}) dy = \left[\frac{3y x^{2}}{2} + \frac{1}{2}y^{3} \right]_{0}^{1} = \frac{3z^{2}}{2} + \frac{1}{2}$$

$$f_{x}(y) = \int_{0}^{1} \frac{3}{2} (x^{2} + y^{2}) dx = \left[\frac{1}{2} x^{3} + \frac{3y^{2}x}{2} \right]_{0}^{1} = \frac{1}{2} + \frac{3y^{2}}{2}$$

$$f_{xy}(z, y) \neq f_{x}(z) f_{x}(y)$$

$$X = \left[\frac{1}{2} x^{3} + \frac{3y^{2}x}{2} \right]_{0}^{1} = \frac{1}{2} + \frac{3y^{2}}{2}$$

$$X = \left[\frac{1}{2} x^{3} + \frac{3y^{2}x}{2} \right]_{0}^{1} = \frac{1}{2} + \frac{3y^{2}x}{2}$$

$$E(X+Y) = M_X + M_Y$$

$$M_{x} = \int_{0}^{1} f_{x}(x) dx = \int_{0}^{1} \left(\frac{3x^{2}+1}{2}\right) dx = \left(\frac{3}{8}x^{4} + \frac{z^{2}}{4}\right)^{1} = \frac{5}{8}$$

$$M_{y} = \int_{0}^{1} f_{y}(y) dy = \int_{0}^{1} y \left(\frac{3y^{2}+1}{2}\right) dy = \left(\frac{3}{8}y^{4} + \frac{y^{2}}{4}\right)^{1} = \frac{5}{8}$$

$$E(X+Y) = \frac{5}{8} + \frac{5}{8} = \frac{10}{8} = 1.25$$

c)
$$E(XY) = \iint_{0}^{1} \frac{32y}{2}(x^{2}+y^{2}) dx dy$$

$$= \iint_{0}^{1} \frac{32y}{2}(x^{2}+y^{2}) dx dy$$

$$= \iint_{0}^{1} \frac{3}{8}x^{4}y + \frac{3}{4}x^{2}y^{3} \Big|_{0}^{1} dy = \iint_{0}^{1} \frac{3}{8}y + \frac{3}{4}y^{3} dy$$

$$= \left[\frac{3}{16}y^{2} + \frac{3}{16}y^{4}\right]_{0}^{1} = \frac{3}{16} + \frac{3}{16} = \frac{6}{16} = \frac{3}{8}$$

$$\begin{cases}
\sqrt{\sqrt{2}} & = \int_{0}^{1} x^{2} f_{x}(x) dx - F(x)^{2} = \int_{0}^{1} \frac{x^{2}(3x^{2}+1)}{2x} dx - \left(\frac{5}{8}\right)^{2} \\
& = \left(\frac{3}{10}x^{5} + \frac{23}{6}\right)_{0}^{1} = \frac{3}{10} + \frac{1}{6} - \frac{25}{64} = \frac{73}{960} = 6.076
\end{cases}$$

$$e) \sqrt{\sqrt{\sqrt{2}}} \left(\frac{3}{2}\right) dy - E(y)^{2} = \int_{0}^{1} \frac{y^{2}(3y^{2}+1)}{2x} dx - \frac{5}{8}y^{2} dx - \frac{5}{$$

3] Show (ov(aX,bY) = ab(ov(X,X)) (ov(aX,bY) = E[abXY] - Max Mbx E[XY] E[XY] $E[AbXY] = \int abxyf_{xx}(x,y) dx dy = ab\int \int xyf_{xx}(x,y) dx dy$ = ab E[XY] $Max = \int axf_{x}(x) dx = a \int xf_{x}(x) dx = a Mx$ $Mby = \int by f_{y}(y) dy = b \int yf_{y}(y) dy = b My$ (ov(aX,bY) = E[abX] - Max Mbx = ab E[XY] - axb Mx

= $ab(E[XY] - M_X M_Y) = ab(ou(X,Y))$