```
abalone <- read.csv(here::here("data", "abalone_raw.csv"))
source(here::here("R", "utils.R"))
library(ggplot2)
```

The three separate weight variables don't quite sum to total weight, suggesting measurement error. Still,

```
including all three would be a bad idea because it would make the model matrix nearly singular.
summary(with(abalone, Whole.weight - Shucked.weight - Viscera.weight - Shell.weight))
##
       Min. 1st Qu.
                       Median
                                         3rd Qu.
                                   Mean
## -0.44750 0.01800 0.03700 0.04995 0.06800
##
       Max.
##
   0.60800
I fit an initial J-1 logits baseline model using sex, dimensions, and whole weight as predictors.
library(nnet)
abalone[["Sex"]] <- factor(abalone[["Sex"]], levels = c("I", "F", "M"))
set.seed(12345)
train_i <- sample(nrow(abalone), floor(nrow(abalone) * 0.8), replace = FALSE)
train <- abalone[train_i, ]</pre>
test <- abalone[-train_i, ]</pre>
initial_model <- multinom(Sex ~ Whole.weight + Length + Diameter + Height + Rings, data = train)</pre>
## # weights: 21 (12 variable)
## initial value 3670.463656
## iter 10 value 2905.758366
## iter 20 value 2882.357358
## final value 2882.199105
## converged
summary(initial_model)
## Warning: partial match of 'fitted' to
## 'fitted.values'
## Call:
## multinom(formula = Sex ~ Whole.weight + Length + Diameter + Height +
##
       Rings, data = train)
##
## Coefficients:
##
     (Intercept) Whole.weight
                                  Length Diameter
     -2.9529624
                      5.393145 -16.57827 10.991562
## M -0.2375642
                      6.313870 -17.91517 6.360789
       Height
##
                  Rings
## F 8.401644 0.2278654
## M 5.226298 0.2117678
##
## Std. Errors:
```

(Intercept) Whole.weight Length Diameter

```
0.5507693
                     0.5022835 3.140566 3.875729
## M
       0.4250026
                    0.4694815 3.004851 3.735638
       Height
                   Rings
## F 3.720682 0.02680181
## M 3.619428 0.02618252
##
## Residual Deviance: 5764.398
## AIC: 5788.398
anova(update(initial_model, . ~ . - .), initial_model)
## # weights: 6 (2 variable)
## initial value 3670.463656
## final value 3662.593993
## converged
##
                                                   Model
## 1
## 2 Whole.weight + Length + Diameter + Height + Rings
                                     Df LR stat.
     Resid. df Resid. Dev
                             Test
## 1
          6680
                 7325.188
                                     NA
                                               NA
## 2
          6670
                 5764.398 1 vs 2
                                     10 1560.79
     Pr(Chi)
##
## 1
          NA
## 2
Most of the estimated coefficients are significant under Wald tests, even after applying the Bonferroni cor-
rection to p-values.
summarized <- broom::tidy(initial_model)</pre>
## Warning: partial match of 'fitted' to
## 'fitted.values'
summarized[["p.value"]] <- p.adjust(summarized[["p.value"]], method = "bonferroni")</pre>
summarized
## # A tibble: 12 x 6
##
      y.level term
                          estimate std.error statistic
##
      <chr>
              <chr>>
                             <dbl>
                                       <dbl>
                                                  <dbl>
   1 F
              (Intercep~
                            -2.95
                                       0.551
                                                 -5.36
   2 F
                             5.39
                                       0.502
                                                 10.7
##
              Whole.wei~
## 3 F
              Length
                           -16.6
                                       3.14
                                                 -5.28
   4 F
##
              Diameter
                            11.0
                                       3.88
                                                  2.84
##
   5 F
                             8.40
                                       3.72
                                                  2.26
              Height
##
   6 F
              Rings
                             0.228
                                       0.0268
                                                  8.50
  7 M
##
              (Intercep~
                            -0.238
                                       0.425
                                                 -0.559
  8 M
              Whole.wei~
                             6.31
                                       0.469
                                                 13.4
                                                 -5.96
## 9 M
                           -17.9
                                       3.00
              Length
## 10 M
              Diameter
                             6.36
                                       3.74
                                                  1.70
## 11 M
              Height
                             5.23
                                       3.62
                                                  1.44
## 12 M
                             0.212
                                       0.0262
                                                  8.09
              Rings
```

## # ... with 1 more variable: p.value <dbl>

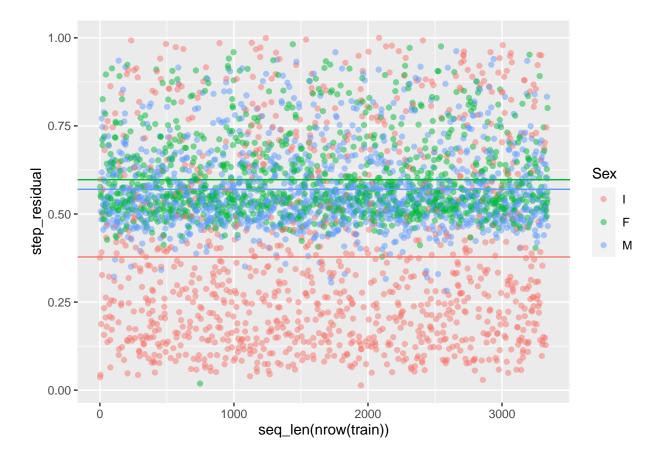
```
rich <- generate_rich_model(initial_model,
  model_data = train[, colnames(coef(initial_model))[-1]],
  model_formula = Sex ~ Whole.weight + Length + Diameter + Height + Rings
)</pre>
```

Stepwise selection chooses a model with a few interactions. Note that using stepwise selection violates some of the assumptions behind inferential model statistics.

```
step_model <- suppressMessages(step(initial_model, scope = list(upper = rich, lower = Sex ~ Whole.weigh
step_residual <- extract_by_level(residuals(step_model, "std.res"), as.integer(train[["Sex"]]))
step_fitted <- extract_by_level(step_model[["fitted.values"]], as.integer(train[["Sex"]]))
step_model</pre>
```

Average standardized residuals are notably lower for infants than for adults

```
ggplot(
  data.frame(step_fitted, step_residual,
        Sex = train[["Sex"]],
        yintercept = ave(step_residual, train[["Sex"]], FUN = mean)
    ),
    aes(x = seq_len(nrow(train)), y = step_residual, color = Sex)
) +
    geom_point(alpha = .5, size = 1.5) +
    geom_hline(aes(yintercept = yintercept, color = Sex), show.legend = FALSE)
```



## ## Model Testing

## [1] 1

A likelihood-ratio test of the step-selected model over the initial model is highly significant. A goodness-of-fit test for the step-selected model has a p-value that is computationally 1, providing no evidence against the null of a good fit

```
lr_test(initial_model, step_model)

## Statistic: 112.255

## Degrees of freedom: 6

## Threshhold: 12.59159

## p = 6.86951e-22

pchisq(sum(extract_by_level(
    residuals(step_model, "pearson"),
    as.integer(train[["Sex"]])
)^2),

df = nrow(train) - length(coef(step_model)), lower.tail = FALSE
)
```

A type II ANOVA test shows that all predictors aside from diameter significantly improve the fit when included. Whole.weight is by far the most important, followed by Rings and the interactions.

```
car::Anova(step_model)
```

```
## Analysis of Deviance Table (Type II tests)
##
## Response: Sex
##
                        LR Chisq Df Pr(>Chisq)
## Whole.weight
                         288.530 2 < 2.2e-16 ***
## Length
                          52.765 2 3.485e-12 ***
## Diameter
                           4.480 2 0.1064769
## Height
                           5.602 2 0.0607488 .
## Rings
                          80.745 2 < 2.2e-16 ***
## Whole.weight:Rings
                          16.054 2 0.0003266 ***
## Height:Rings
                          12.566 2 0.0018676 **
## Whole.weight:Diameter
                           4.609 2 0.0998088 .
## ---
## Signif. codes:
## 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' ' 1
```

Next I try refitting the model with all four available weight variables (including replacing the interaction) and comparing AIC. It turns out whole weight has the lowest, but the differences are minor.

```
weight_vars <- c("Whole.weight", "Shucked.weight", "Viscera.weight", "Shell.weight")
names(weight_vars) <- weight_vars
weight_vars <- lapply(weight_vars, as.symbol)</pre>
```

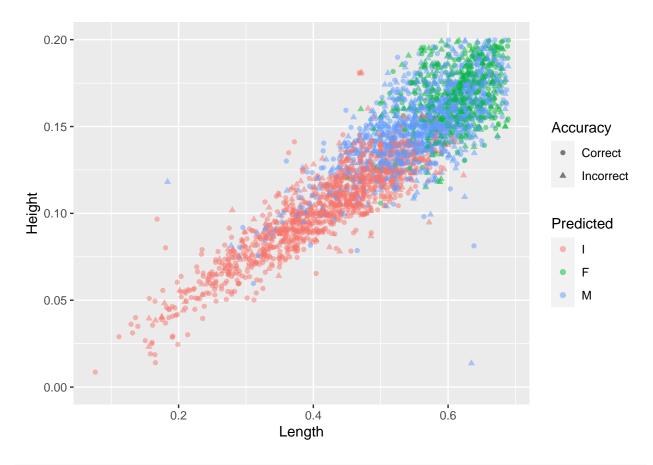
```
lapply(weight_vars, function(x) {
   update_formula(step_model, Whole.weight, x, indirect = TRUE)[["AIC"]]
})

train_preds <- predict(step_model, newdata = train, type = "class")

## Warning in model.matrix.default(Terms, m,
## contrasts = object$contrasts): partial argument
## match of 'contrasts' to 'contrasts.arg'</pre>
```

Plotting predicted class by height and width shows again that infants are well separated from adults.

```
## Warning: Removed 258 rows containing missing values
## (geom_point).
```



## ## Model Validation

On both training and testing sets, sensitivity, specificity, and precision are much higher for the infant than the adult classes. However, test error was only a little higher than train error. Still,

```
mean(train_preds == train[["Sex"]])
## [1] 0.5636037
train_cm <- confusion_matrix(train[["Sex"]], train_preds)</pre>
train_cm
##
        predicted
##
   truth
           Ι
##
       I 859 48 162
##
       F 154 330 566
       M 240 288 694
##
analyze_cm(train_cm)
```

```
test_preds <- predict(step_model, newdata = test, type = "class")</pre>
## Warning in model.matrix.default(Terms, m,
## contrasts = object$contrasts): partial argument
## match of 'contrasts' to 'contrasts.arg'
mean(test_preds == test[["Sex"]])
## [1] 0.5681818
test_cm <- confusion_matrix(test[["Sex"]], test_preds)</pre>
test_cm
       predicted
##
## truth I F M
      I 223 14 36
      F 36 82 139
##
      M 67 69 170
##
analyze_cm(test_cm)
##
                       Ι
                                F
## sensitivity 0.8168498 0.3190661 0.5555556
## specificity 0.8344371 0.6919014 0.6916100
## precision 0.6840491 0.4969697 0.4927536
analyze_cm(train_cm) - analyze_cm(test_cm)
##
                          Ι
## sensitivity -0.013295093 -0.004780434
## specificity -0.004615368 -0.008663397
## precision 0.001505589 -0.001474201
##
## sensitivity 0.0123658847
## specificity 0.0008769184
## precision -0.0047086162
```