

Lab 9 – Manipulating Grammars

Ryan Munger
Ryan.Munger1@marist.edu

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1 Crafting a Compiler

1.1 Exercise 5.5 – LL(1) Grammar

Transform the following grammar into LL(1) form using the techniques presented in Section 5.5.

```
1 DeclList      → DeclList ; Decl
2               | Decl
3 Decl          → IdList : Type
4 IdList        → IdList , id
5               | id
6 Type          → ScalarType
7               | array ( ScalarTypeList ) of Type
8 ScalarType    → id
9               | Bound . . Bound
10 Bound        → Sign intconstant
11              | id
12 Sign         → +
13              | -
14              | Epsilon
15 ScalarTypeList → ScalarTypeList , ScalarType
16              | ScalarType
```

LL(1) requires a unique prediction for each combination of nonterminal and lookahead symbols. We must eliminate common prefixes and left recursion.

Updated grammar:

```
1 DeclList      → Decl DeclList'
2 DeclList'     → ; Decl DeclList'
3               | Epsilon
4 Decl          → IdList : Type
5 IdList        → id IdList'
6 IdList'       → , id IdList'
7               | Epsilon
8 Type          → ScalarType
9               | array ( ScalarTypeList ) of Type
10 ScalarType    → id
11               | Bound . . Bound
12 Bound        → Sign intconstant
13               | id
14 Sign         → +
15               | -
16               | Epsilon
17 ScalarTypeList → ScalarType ScalarTypeList'
18 ScalarTypeList' → , ScalarType ScalarTypeList'
19               | Epsilon
20
```

2 Dragon Book

2.1 Exercise 4.5.3 – Bottom-Up Parsing

Give bottom-up parses for the following input strings and grammars.

Input: 000111

Grammar: $S \rightarrow 0S1|01$

Bottom-Up/Shift Reduce Parse:

Input:	Operation	Stack
000111	Shift 0	Eps
00111	Shift 0	0
0111	Shift 0	00
111	Shift 1	000
11	Reduce 01	0001
11	Shift 1	00S
1	Reduce 0S1	00S1
1	Shift 1	0S
Eps	Reduce 0S1	0S1
Eps	Accept S	S

Input: aaa^*a^{++}

Grammar $S \rightarrow SS + | SS * | a$

Bottom-Up/Shift Reduce Parse:

Input:	Operation	Stack
aaa^*a^{++}	Shift a	Eps
aa^*a^{++}	Reduce a	a
aa^*a^{++}	Shift a	S
a^*a^{++}	Reduce a	Sa
a^*a^{++}	Shift a	SS
$*a^{++}$	Reduce a	SSa
$*a^{++}$	Shift $*$	SSS
a^{++}	Reduce $SS*$	SSS^*
$^{++}$	Shift a	SS
$^{++}$	Reduce a	SSa
$^{++}$	Shift $+$	SSS
$+$	Reduce $SS+$	SSS^+
$+$	Shift $+$	SS
Eps	Reduce $SS+$	SS^+
Eps	Accept S	S