DEVELOPMENT OF A MODEL AND IMBALANCE DETECTION SYSTEM FOR THE CAL POLY WIND TURBINE

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by

Ryan Takatsuka

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COMMITTEE MEMBERSHIP

TITLE: Development of a Model and Imbalance

Detection System for the Cal Poly Wind

Turbine

AUTHOR: Ryan Takatsuka

DATE SUBMITTED: April 2019

COMMITTEE CHAIR: John Ridgely, Ph.D.

Professor of Mechanical Engineering

COMMITTEE MEMBER: Glen Thorncroft, Ph.D.

Professor of Mechanical Engineering

COMMITTEE MEMBER: Patrick Lemieux, Ph.D.

Professor of Mechanical Engineering

ABSTRACT

Development of a Model and Imbalance Detection System for the Cal Poly Wind

Turbine

Ryan Takatsuka

This thesis develops a model of the Cal Poly Wind Turbine that is used to determine

if there is an imbalance in the turbine. A theoretical model is derived to estimate

the expected vibrations when there is an imbalance in the rotor. Vibration and

acceleration data are collected from the turbine tower during operation to confirm

the model is useful and accurate for determining imbalances in the turbine.

Various signal processing techniques for analyzing the vibration data are explored

and tested with the simulation. This includes frequency shifts, lock-in amplifiers,

phase-locked loops, discrete Fourier transforms, and various filters. The processed

data is fed into an algorithm that determines if there is an imbalance.

The detection algorithm consists of a machine learning classification model that uses

experimental data to train and increase the success rate of the imbalance detection.

The model uses the maximum frequency component and magnitude as an input to

classify the data as "balanced" or "not balanced" using the K-nearest neighbors

algorithm. While this classification algorithm requires slightly more computational

power than others, it is simple to implement and has a high accuracy rating.

TODO: Add a quick summary of the results.

iv

TABLE OF CONTENTS

					Page			
LI	ST O	F TAB	LES		vii			
LI	ST O	F FIGU	URES .		viii			
CI	НАРТ	TER						
1	Intro	oductio	n		1			
	1.1	System Overview						
	1.2	Objec	tive		2			
	1.3	Backg	round .		2			
	1.4	Turbii	ne Failure	S	3			
	1.5	Tower	Vibratio	n Research	4			
2	Mat	Mathematical Model						
	2.1	Assun	nptions/P	roblem Statement	6			
	2.2	Varial	ole Defini	tions	6			
	2.3	Calcul	ating Tower Vibrations					
		2.3.1	Determi	ning Effective Force	9			
		2.3.2	Determi	ning Effective Spring Constant	10			
			2.3.2.1	Mathematical derivation of the y -direction spring constant, K_y	10			
			2.3.2.2	Numerical calculation of the y -direction spring constant, K_y	13			
		2.3.3	Determi	ning Effective Mass	18			
		2.3.4	Develop	ing State Space Equations	19			
3	Digi	tal Sigr	nal Proces	ssing Model	21			
	3 1	Model	Block D	iagram	21			

3.2	Proce	essing the data			
	3.2.1	DFT review	24		
	3.2.2	Lock-In Amplifier	26		
		3.2.2.1 Types of low-pass filters	29		
	3.2.3	Identifying the rotor frequency from the tower accelerations .	32		
	3.2.4	Zoom FFT	33		
		3.2.4.1 Frequency translation	38		
		3.2.4.2 Decimation/downsampling	40		
		3.2.4.3 An optimized Zoom FFT implementation	40		
		3.2.4.4 Estimating processor performance	43		
	3.2.5	Goertzel Algorithm	46		
4 Imb	alance	Detection Algorithm	49		
4.1	Overv	riew	49		
	4.1.1	Machine learning background	49		
4.2	The t	raining data	50		
4.3	K-Nea	arest Neighbor algorithm	52		
4.4	About	t the algorithm	52		
	4.4.1	Choosing the data	53		
	4.4.2	Algorithm Results	54		
4.5	Logist	cic Regression	58		
	4.5.1	About the algorithm	58		
PIDLIOCD ADHV					

LIST OF TABLES

Table		Page
2.1	Variable Definitions	8
2.2	Calculated spring constant and natural frequency for the y -direction vibration	15
2.3	Turbine parameters used in the MATLAB analysis for calculating k_{\parallel}	y 18
3.1	Zoom FFT parameters	41
3.2	Cycle counts for a STM32 floating-point processor. The exponential* operation is estimated from a floating-point performance analysis [?] because it is not stated in the STM32 datasheet.	45
4.1	An example of the terminology for the confusion matrix in Equation 4.3. Class A and Class B represent the different classes of data. These can be related to a balanced and imbalanced rotor with proper data set labels	56

LIST OF FIGURES

Figure		Page
1.1	Data used for the SCADA Alarms and Failure Analysis [15]. TODO: Describe/explain the results in the SCADA table	3
1.2	Correlation between different turbine parameters [17]. TODO: get less blurry picture and add some more explanation	4
2.1	The simplified wind turbine model showing the forces from an eccentric mass on the rotor. This figure also shows the coordinate system that will be used for the tower analysis	7
2.2	The intermediate variables from the numerical spring constant calculation in MATLAB	17
2.3	A cantilever beam model [16]	18
3.1	A block diagram showing the lock-in amplifier and the turbine tower simulation	21
3.2	The simulated displacement for a rotor imbalance at 230 RPM. The imbalance mass is placed at the end of the blade, which causes accelerations and displacements at the top of the tower	23
3.3	This figure shows the simulated displacement data in the frequency domain. The rotor frequency is 230 RPM in this simulation \dots .	24
3.4	A block diagram showing the details of a lock-in amplifier [2]. This figure was created with Draw.io	27
3.5	The output of the lock-in amplifier from the simulated data shown in Figure 3.2	28
3.6	A block diagram of a standard IIR filter. [6]	29
3.7	The filter response of the Butterworth IIR filter (Equation ??) compared to a moving average filter with a window size of 4. This figure was created in MATLAB with 2 simulated filter designs	30
3.8	A block diagram of a standard FIR filter. [5]	31

3.9	The block diagram of a phase-locked loop implementation when detecting rotor frequencies from acceleration measurements [14]. This diagram was created with Draw.io [?]	34
3.10	The output of the PLL when detecting frequency from the data shown in Figure 3.2. The frequency of the input data oscillates from 190 RPM to 210 RPM to simulate a real turbine controller that may oscillate between frequencies	34
3.11	A block diagram for a simple envelope detector. The signal is first squared and multiplied by a gain of 2. This signal (which should be entirely positive) is sent through a lowpass filter to remove the high frequency information. The lowpass filter needs to reject $2f$, which is the resulting frequency when a signal with frequency, f is squared. The square root of the resulting signal produces the the amplitude of the signal. This figure was created with Draw.io	35
3.12	A block diagram showing the zoom FFT algorithm. This figure was created with Draw.io	37
3.13	A diagram showing the percent computational workload reduction of a $\frac{N}{D}$ -point Zoom FFT relative to a standard n -points FFT [14]	38
3.14	This figure shows an example of frequency translation. The black signal is the frequency spectrum of some input signal that has a strong component at 5 Hz. The blue signal shows the frequency shifted spectrum that results from multiplying the input signal by a reference signal with a frequency of 5 Hz (as shown in Equation 3.21). The dotted blue line shows the digital filter response. This figure was generated with MATLAB	39
3.15	This figure shows the results of a Zoom FFT using the parameters listed in Table 3.1. The top plot shows the frequency spectrum from a standard FFT (black) and a Zoom FFT (red). The bottom plot shows the same data as the top plot, but zoomed into a narrow frequency range. The standard FFT has a length of 2048, while the Zoom FFT has a length of 128. This figure was created with MATLAB.	44
3.16	The direct-form realization of the Goertzel Algorithm[12]	47
3.17	This figure shows the frequency spectrum calculated with a standard FFT (black) and a few points calculated with the Goertzel algorithm (red). This figure was created in MATLAB	48
4.1	This figure shows the spectrogram of the tower accelerations	51

4.2	A visualization of the KNN algorithm [?]. The training data for a 2-class problem with 2 inputs is shown as blue and orange dots. For $K=3$, a circle is drawn around the new point (star) until 3 training data points fall within the circle. The classification of the new point is then determined by the majority of the points inside the circle. In	
	this case, there are more $Class\ B$ points than $Class\ A$ points, so the new point (star) will be classified as $Class\ B$	52
4.3	This figure shows a single DFT result (a single column from Figure 4.1)	54
4.4	This figure shows a the 2-dimensional data used as an input to the KNN classification algorithm	55
4.5	This figure shows the classification boundary for the KNN algorithm with $K=3$ for all of the training data	57
4.6	This figure shows the sigmoid function plot	60

Chapter 1

INTRODUCTION

TODO: Add a short section about the significance of wind turbine failures and the advantages of using conditioning monitoring.

1.1 System Overview

The wind turbine that is analyzed in this thesis is part of the Cal Poly Wind Power Research Center. This is designed for research into smaller wind turbines and to educate engineers in all aspects of the wind power industry. The Cal Poly Wind Turbine Tower supports a 3 kW Horizontal-Axis Wind Turbine, and the tower was analyzed by Tae-gyun (Tom) Gwon[11]. In Gwon's thesis paper, an ABAQUS model of the tower is developed to analyze natural frequencies and vibrations. An FEM model, such as this one, is too complicated to run on a cheap microcontroller; however, the results of this model can be compared with the simple lumped-parameter model to determine the validity of the simplifications.

The Cal Poly Wind Turbine has no current method of detecting an imbalance. It is possible to install an intrusive and expensive device that monitors all many tower parameters (such as multiple acceleration measurements at various positions on the tower and blades), but it would be much more desirable to have an inexpensive, device that can accurately detect an imbalance with zero to no setup/installation effort.

1.2 Objective

The primary objective of this thesis is to develop a method for identifying a blade imbalance in the field. This method must be simple enough to perform on a microcontroller in real time, while maintaining the ability to be mounted to any small scale wind turbine. This will help to prevent any catastrophic failures resulting in damaged blades and an inoperable wind turbine. Additionally, maintenance costs can be reduced because the turbines in good condition won't have to be inspected as often. The main focus of the paper will be introducing a simplified turbine tower model and providing a digital signal processing method for analyzing the data.

A simplified tower model will help to develop and test various signal processing methods. It is difficult and time consuming to obtain experimental data from the tower, so having a tower model will speed up the algorithm design process. Once the signal processing method has been tested and refined on the analytic model, it can then be tested on experimental tower data will minimal tuning.

1.3 Background

Cal Poly's wind turbine is in the Escuela Ranch in an unpopulated area. The tower is a tapered tubular pole made of ASTM A572 Grade-50 Steel. The tower has a tilting feature which allows relatively easy access to the nacelle. The tower is rotated about 2 ball bearings at the base via a winch attached to the CPWPRC truck. More details about the tower design and analysis can be found in *Structural Analyses of Wind Turbine Tower for 3 KW Horizontal-Axis Wind Turbine* [11].

SCADA System	${ m WT}$ ${ m Make}$	Technology	Rated Capacity (kW)	Nb of Tur- bines	Failures per Turbine	Alarms per Turbine
1	A	Geared	1500	55	0.709	4170.07
2	B, C	Dir. Drive	2000	57	0.632	1120.35
3	D	Geared	850	77	2.208	2778.78
4	\mathbf{E}	Geared	2000	168	1.780	4704.57
5	F, G	Geared	1800 & 2000	83	1.313	572.14

Figure 1.1: Data used for the SCADA Alarms and Failure Analysis [15]. TODO: Describe/explain the results in the SCADA table.

1.4 Turbine Failures

The goal of this project is to develop a method for detecting a rotor imbalance that could be potentially harmful to the turbine. This would allow the turbine to be shut down before any failures occur.

A common method for tracking and preventing turbine failures is the use of Supervisory Control and Data Acquisition (SCADA) alarms[9]. SCADA is a control system architecture that uses high-level graphical user interfaces networked with peripheral devices (such as PLCs and PID controllers). This is an effective method for predicting turbine failure, but can be expensive and complicated to implement. An example of SCADA alarm results are shown in Figure 1.1.

According to a report on UK wind farms[19], there have been 1500 wind turbinerelated accidents within 5 years. Of those accidents, there were a total of 400 injuries to workers. Many of these accidents are preventable if there is a reliable selfdiagnosing system installed on the turbine. This report also mentions incidents where ice has build up on the blades. Most of these failures should be preventable if the rotor imbalance was detected right away and the turbine was shut down.

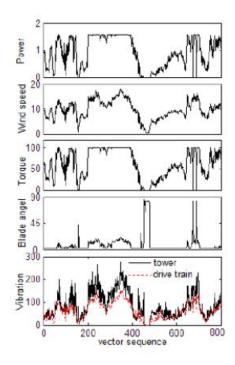


Figure 1.2: Correlation between different turbine parameters [17]. TODO: get less blurry picture and add some more explanation.

1.5 Tower Vibration Research

Wind turbine tower vibrations are important to the health of turbines and have been studied before. In one study, a nonlinear state estimation technique[17] (NSET) is used to attempt to predict wind turbine failures. This model uses SCADA data to relate different operating parameters to the health of the turbine. Figure 1.2 shows the correlation of power, wind speed, torque, blade angle, and tower vibration. According to this paper, the tower vibrations are not enough information to predict turbine failures.

The research in [17] attempts to detect *any* turbine failure, while detecting only rotor imbalances may be slightly easier.

Most tower vibration analyses are empirically derived because of the stochastic nature of the wind speed and the amount of variables affecting the turbine. Data-driven models[20] are very common in the wind power space, especially with monitoring systems such as SCADA.

Chapter 2

MATHEMATICAL MODEL

2.1 Assumptions/Problem Statement

The turbine tower is modeled as a cantilever beam with a concentrated mass at the end. The tower is assumed to be the cantilever beam, and the nacelle is assumed to be the concentrated mass at the end of the simplified beam.

This problem is treated as forced vibration, where the forcing function is a periodic force caused from an eccentric mass on the rotor. This eccentric mass represents an imbalance in the turbine, and will cause vibrations in the tower. Figure 2.1 shows the simplified wind turbine model with the applied forces. The cross-section of the tower is assumed to taper linearly from the base to the top.

2.2 Variable Definitions

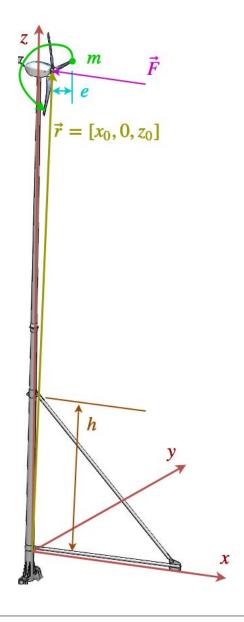


Figure 2.1: The simplified wind turbine model showing the forces from an eccentric mass on the rotor. This figure also shows the coordinate system that will be used for the tower analysis.

Table 2.1: Variable Definitions

Variable	Description	
$ec{E}$	The original force applied to the end of the rotor due to	
$ec{F}_{original}$	an imbalance in the blades	
F_0	The magnitude of the force caused by the eccentric mass	
ω	The rotational speed of the blades	
t	Time	
m	Eccentric mass	
	Distance the eccentric mass is from the axis of rotation	
e	of the rotor	
$ec{M}$	Moment that the eccentric force applies after the force is	
1VI	translated to the tower axis	
$ec{r}$	The position vector for the top of the rotor with respect	
1	to the bottom of the turbine tower $(r = [x_0, 0, z_0])$	
M_x	The moment function in the x -direction	
M_y	The moment function in the y -direction	
I_b	The area moment of inertia at the base of the tower	
I_t	The area moment of inertia at the top of the tower	
b	The distance from the base of the tower to the ginpole	
h	pin-joint on the tower	
E	Modulus of elasticity of the tower (steel)	
d_b	Diameter at the base of the tower	
d_t	Diameter at the top of the tower	

2.3 Calculating Tower Vibrations

2.3.1 Determining Effective Force

An eccentric mass, m, on the rotor causes a force defined by the following equation:

$$\vec{F}(t) = \begin{bmatrix} 0 \\ F_0 \sin(\omega t) \\ F_0 \cos(\omega t) \end{bmatrix}$$
(2.1)

where

$$F_0 = me\omega^2 \tag{2.2}$$

In order to treat the system as a cantilever beam, the force has to be acting in the center of the nacelle and on the same axis as the tower. When the force vector (Equation 2.1) is translated to the axis of the tower, a moment needs to be introduced to account for the force vector translation:

$$\vec{M} = \vec{r} \times \vec{F} = \begin{bmatrix} -F_0 z_0 \sin(\omega t) \\ -F_0 x_0 \cos(\omega t) \\ F_0 x_0 \sin(\omega t) \end{bmatrix}$$
(2.3)

The moment in (Equation 2.3) creates an effective force at the top of the tower that needs to be added to the original force (Equation 2.1). The moment about the z-axis is ignored because torsional effects on the tower are negligible when determining nacelle displacement. This results in the following effective force on the top of the tower:

$$\vec{F}_{effective} = \vec{F}_{original} + \vec{F}_{moment}$$

$$\vec{F}_{effective} = \begin{bmatrix} 0 \\ F_0 \sin(\omega t) \\ F_0 \cos(\omega t) \end{bmatrix} + \begin{bmatrix} -\frac{F_0 x_0}{z_0} \cos(\omega t) \\ F_0 \sin(\omega t) \\ 0 \end{bmatrix}$$

$$(2.4)$$

$$\vec{F}_{effective} = \begin{bmatrix} -\frac{F_0 x_0}{z_0} \cos(\omega t) \\ 2F_0 \sin(\omega t) \\ F_0 \cos(\omega t) \end{bmatrix}$$
(2.5)

2.3.2 Determining Effective Spring Constant

The tower model has a different spring constant for the x and y directions. In the y direction, the ginpole has a negligible effect on the stiffness of the tower, so the tower acts as a tapered cantilever beam.

2.3.2.1 Mathematical derivation of the y-direction spring constant, K_y

Assuming the tower acts like a cantilever beam in this direction with a concentrated force at the end of the beam, the moment, $M_x(y)$ can be expressed as:

$$M_x(y) = F_y z - F_y z_0 (2.6)$$

Because the beam is linearly tapered, the diameter, d, can be written as a function of tower height, z_0 .

$$d(z) = d_b - \frac{z (d_b - d_t)}{z_0}$$
 (2.7)

 d_b is the diameter of the tower at the bottom, and d_t is the diameter of the tower at the top. The moment of inertia, assuming a hollow tube with thickness t, can be written as a function of z using Equation 2.7.

$$I_y(z) = \frac{\pi}{64}d^4 - \frac{\pi}{64}(d - 2t)^4 \tag{2.8}$$

$$I_y(z) = \frac{\pi \left(d_b - \frac{z(d_b - d_t)}{z_0}\right)^4}{64} - \frac{\pi \left(2t - d_b + \frac{z(d_b - d_t)}{z_0}\right)^4}{64}$$
(2.9)

The deflection of the beam can be calculated using the Euler–Bernoulli equation:

$$\frac{d^2y_d}{dz^2} = -\frac{M_x}{E\,I_y(z)}\tag{2.10}$$

$$\frac{d^2 y_d}{dz^2} = -\frac{M_x}{E I_y(z)}$$

$$\frac{d^2 y_d}{dz^2} = -\frac{F_y z - F_y z_0}{E \left(\frac{\pi \left(d_b - \frac{z(d_b - d_t)}{z_0}\right)^4}{64} - \frac{\pi \left(2t - d_b + \frac{z(d_b - d_t)}{z_0}\right)^4}{64}\right)}$$
(2.10)

The slope of the beam, θ_y , can be calculated by integrating Equation 2.11:

$$\theta_{y} = \frac{dy_{d}}{dz} = \int -\frac{F_{y} z - F_{y} z_{0}}{E \left(\frac{\pi \left(d_{b} - \frac{z(d_{b} - d_{t})}{z_{0}}\right)^{4}}{64} - \frac{\pi \left(2t - d_{b} + \frac{z(d_{b} - d_{t})}{z_{0}}\right)^{4}}{64}\right)} dz$$
(2.12)

Integrating the equation above results in the following equation for θ_y :

$$\theta_{y} = \frac{\ln\left(d_{b}z - d_{t}z - d_{b}z_{0} + tz_{0}\right) \left(8F_{y}d_{t}z_{0}^{2} - 8F_{y}tz_{0}^{2}\right)}{E\pi d_{b}^{2} t^{3} - 2E\pi d_{b} d_{t} t^{3} + E\pi d_{t}^{2} t^{3}} - \frac{4\ln\left(d_{b}z - d_{t}z - d_{b}z_{0} + tz_{0}\left(1 - i\right)\right) \left(F_{y}d_{t}z_{0}^{2} + F_{y}tz_{0}^{2}\left(-1 + 1i\right)\right)}{E\pi d_{b}^{2} t^{3} - 2E\pi d_{b} d_{t} t^{3} + E\pi d_{t}^{2} t^{3}} - \frac{4\ln\left(d_{b}z - d_{t}z - d_{b}z_{0} + tz_{0}\left(1 + 1i\right)\right) \left(F_{y}d_{t}z_{0}^{2} + F_{y}tz_{0}^{2}\left(-1 - i\right)\right)}{E\pi d_{b}^{2} t^{3} - 2E\pi d_{b} d_{t} t^{3} + E\pi d_{t}^{2} t^{3}} + C_{y1}$$

$$(2.13)$$

The tower is fixed at the base (no translation or rotation about the x-axis), so the slope at z = 0 is $\theta = 0$. Using this boundary condition, C_{y1} can be determined:

$$C_{y1} = -\frac{4 F_y z_0^2 Q_1(z)}{E t^3 \pi (d_b - d_t)^2}$$
(2.14)

where,

$$Q_1(z) = 2 d_t \ln(-z_0 (d_b - t)) - d_t \ln(-z_0 (d_b + t (-1 - i)))$$

$$- d_t \ln(-z_0 (d_b + t (-1 + 1i))) - 2 t \ln(-z_0 (d_b - t))$$

$$+ t \ln(-z_0 (d_b + t (-1 - i))) (1 + 1i)$$

$$+ t \ln(-z_0 (d_b + t (-1 + 1i))) (1 - i)$$

This results in the following slope equation:

$$\theta_y = \frac{4 F_y z_0^2 Q_2(z)}{E t^3 \pi (d_b - d_t)^2} + C_{y1}$$
(2.15)

where,

$$Q_{2}(z) = 2 d_{t} \ln (d_{b} z - d_{t} z - d_{b} z_{0} + t z_{0})$$

$$- d_{t} \ln (d_{b} z - d_{t} z - d_{b} z_{0} + t z_{0} (1 - i))$$

$$- d_{t} \ln (d_{b} z - d_{t} z - d_{b} z_{0} + t z_{0} (1 + 1i))$$

$$- 2 d_{t} \ln (-z_{0} (d_{b} - t)) + d_{t} \ln (-z_{0} (d_{b} + t (-1 - i)))$$

$$+ d_{t} \ln (-z_{0} (d_{b} + t (-1 + 1i)))$$

$$- 2 t \ln (d_{b} z - d_{t} z - d_{b} z_{0} + t z_{0})$$

$$+ t \ln (d_{b} z - d_{t} z - d_{b} z_{0} + t z_{0} (1 - i)) (1 - i)$$

$$+ t \ln (d_{b} z - d_{t} z - d_{b} z_{0} + t z_{0} (1 + 1i)) (1 + 1i)$$

$$+ 2 t \ln (-z_{0} (d_{b} - t)) + t \ln (-z_{0} (d_{b} + t (-1 - i))) (-1 - i)$$

$$+ t \ln (-z_{0} (d_{b} + t (-1 + 1i))) (-1 + 1i)$$

At this point, it has become clear that an analytic solution for the spring constant is not practical. Integrating the slope equation (Equation 2.15) would produce the deflection equation; however this integral become extremely complicated. A cleaner option is to calculate the spring constants numerically.

2.3.2.2 Numerical calculation of the y-direction spring constant, K_y

To determine the spring constant numerically, a vector of z values must be created to be used in the numerical integration.

To calculate the slope of the tower, θ , the curvature equation needs to be numerically integrated:

$$\theta(z) = \int_0^{z_0} \frac{-M(z)}{E\,I(z)} \, dz \tag{2.16}$$

The applied force, F_y , in the moment equation (Equation 2.6) can be factored out because it is not a function of z. This results in the following equation for the slope:

$$\theta(z) = \frac{F_y}{E} \int_0^{z_0} \frac{z_0 - z}{I(z)} dz \tag{2.17}$$

The integral in Equation 2.17 can be approximated by a sum of n elements and calculated numerically.

$$\theta(z) = \frac{F_y}{E} \sum_{i=0}^{n} \frac{z_0 - z_i}{I(z_i)} \Delta z_i$$
 (2.18)

Equation 2.18 is a much simpler method for calculating the beam slope compared to the analytic solution shown in Equation 2.15. The deflection of the tower, y_d , can be calculated by integrating the slope equation.

$$y_d = \int_0^{z_0} \theta(z) dz = \int_0^{z_0} \left(\frac{F_y}{E} \sum_{i=0}^n \frac{z_0 - z_i}{I(z_i)} \Delta z_i \right) dz$$
 (2.19)

The above equation can be numerically approximated with a summation of m elements as follows:

$$y_d = \sum_{j=0}^{m} \left(\frac{F_y}{E} \sum_{i=0}^{n} \frac{z_0 - z_{ij}}{I(z_{ij})} \Delta z_i \right) \Delta z_j$$
 (2.20)

$$y_d = \frac{F_y}{E} \sum_{i=0}^{m} \sum_{i=0}^{n} \frac{z_0 - z_{ij}}{I(z_{ij})} \Delta z_i \Delta z_j$$
 (2.21)

To determine the spring constant, the deflection equation should be rewritten in the

Table 2.2: Calculated spring constant and natural frequency for the y-direction vibration.

Parameter	Constant Top Area	Tapered Beam	Constant Bottom Area	FEA value
k_y	1283 N/m	8966 N/m	16213 N/m	4233 N/m
f_y	0.34 Hz	0.84 Hz	1.1 Hz	0.58 Hz

form, F = -kx, which in this case is:

$$F_y = -k_y y_d (2.22)$$

$$F_{y} = \frac{E}{\sum_{j=0}^{m} \sum_{i=0}^{n} \frac{z_{ij} - z_{0}}{I(z_{ij})} \Delta z_{i} \Delta z_{j}} y_{d}$$
 (2.23)

From Equation 2.23, is can be seen that the spring constant is:

$$k_y = \frac{E}{\sum_{j=0}^{m} \sum_{i=0}^{n} \frac{z_{ij} - z_0}{I(z_{ij})} \Delta z_i \Delta z_j}$$
 (2.24)

Table ?? shows the calculated spring constant values and natural frequencies in the y-direction for the turbine parameters. The constant top area value is the spring constant calculated assuming a uniform circular cross-section beam with a profile equal to the top of the tower. The constant bottom area value is the spring constant calculated assuming a uniform circular cross-section beam with a profile equal to the bottom of the tower. The FEA values are derived in Tom Gwon's analysis [11], although it is unclear whether these values apply for the y or x direction. The tapered beam calculation is performed in MATLAB using the following code (with turbine parameters listed in Table 2.3):

 $z = linspace(0, z_0, 1000); % [m] Create the vector of z values$

The intermediate variables from the MATLAB calculation are shown in Figure 2.2. The curvature, slope, and displacement are all with respect to force, since it cancels out of the equation and is not used. The spring constant is calculated by taking the inverse of the displacement/force curve at the largest z value. These plots were created using a z-vector of 1000 elements.

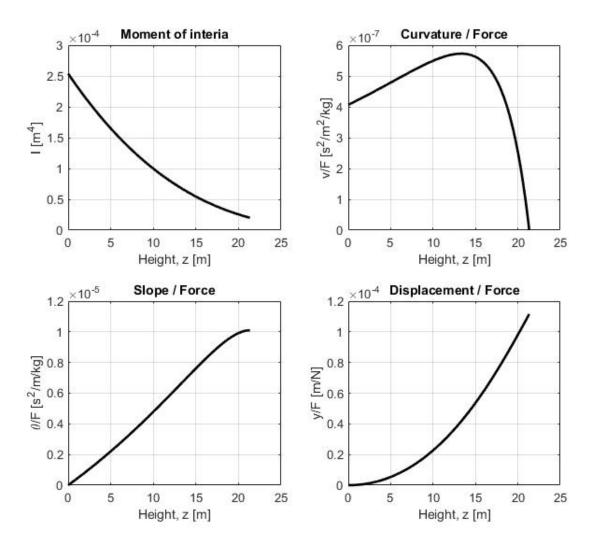


Figure 2.2: The intermediate variables from the numerical spring constant calculation in MATLAB.

Table 2.3: Turbine parameters used in the MATLAB analysis for calculating $\boldsymbol{k_y}$

Variable	Value	Description
z_0	70 ft	The total height of the tower
d_b	20 in	The diameter of the bottom of the tower
d_t	8.7 in	The diameter of the top of the tower
E	30 Mpsi	The modulus of elasticity for ASTM A572 Grade-50 Steel
t	0.2 in	The thickness of the turbine tower tube

2.3.3 Determining Effective Mass

The cantilever beam (Figure 2.3) can be simplified to a massless beam with all of the mass concentrated at the end of the beam.

TODO: Redo this derivation assuming I is a function of x: I(x)

The total potential energy, P, in the beam is [16]:

$$P = \frac{EI}{2} \int_0^L \left(\frac{d^2y}{dx^2}\right)^2 dx$$
$$= \frac{1}{64} \pi^4 \left[\frac{EI}{L^3}\right] y_0^2 \tag{2.25}$$

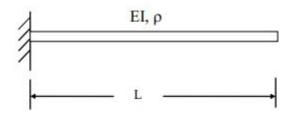


Figure 2.3: A cantilever beam model [16]

The total kinetic energy, T, in the beam is:

$$T = \frac{1}{2}\rho_L \omega_n^2 \int_0^L y^2 dx$$

= $\frac{1}{4}\rho \omega_n^2 y_0^2 L \left(3 - \frac{8}{\pi}\right)$ (2.26)

Equation 2.25 and Equation 2.26 results in the following equation for natural frequency f_n [Hz]:

$$f_n = \frac{\pi}{8L^2} \sqrt{\frac{EI}{\rho \left(3 - \frac{8}{\pi}\right)}} \tag{2.27}$$

The stiffness at the free end of a cantilever beam is:

$$k = \frac{3E}{L^3}I\tag{2.28}$$

The natural frequency of a beam is a function of the stiffness and effective mass:

$$\omega_n = 2\pi f_n = \sqrt{k/m_{eff}} \tag{2.29}$$

Simplifying the previous few equations results in the following equation for the effective mass at the end of a mass-less beam:

$$m_{eff} = \frac{48L}{\pi^4} \rho \left(3 - \frac{8}{\pi} \right) \tag{2.30}$$

2.3.4 Developing State Space Equations

Vibrations in the x and y directions can be split up into 2 independent 2nd order differential equations:

$$\ddot{x} + \frac{C_x}{m}\dot{x} + \frac{k_x}{m}x = \frac{1}{m}F_x(t)$$
 (2.31)

$$\ddot{y} + \frac{C_y}{m}\dot{y} + \frac{k_y}{m}x = \frac{1}{m}F_y(t)$$
 (2.32)

These equations can be converted to state space form:

$$\dot{\boldsymbol{x}} = \boldsymbol{A}_{\boldsymbol{x}} \boldsymbol{x} + \boldsymbol{B}_{\boldsymbol{x}} F_{\boldsymbol{x}}(t) \tag{2.33}$$

$$x = C_x x + D_x F_x(t) \tag{2.34}$$

$$\dot{\boldsymbol{y}} = \boldsymbol{A}_{\boldsymbol{y}} \boldsymbol{y} + \boldsymbol{B}_{\boldsymbol{y}} F_{\boldsymbol{y}}(t) \tag{2.35}$$

$$y = C_y y + D_y F_y(t) \tag{2.36}$$

Where the full equations are written out as follows:

$$\begin{bmatrix} \dot{x}_1 \\ \dot{x}_2 \end{bmatrix} = \begin{bmatrix} 0 & 1 \\ -\frac{k_x}{m} & -\frac{C_x}{m} \end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \end{bmatrix} + \begin{bmatrix} 0 \\ \frac{1}{m} \end{bmatrix} \cdot F_x(t)$$
 (2.37)

$$x = \begin{bmatrix} 1 & 0 \end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \end{bmatrix} + 0 \cdot F_x(t) \tag{2.38}$$

$$\begin{bmatrix} \dot{y}_1 \\ \dot{y}_2 \end{bmatrix} = \begin{bmatrix} 0 & 1 \\ -\frac{k_y}{m} & -\frac{C_y}{m} \end{bmatrix} \begin{bmatrix} y_1 \\ y_2 \end{bmatrix} + \begin{bmatrix} 0 \\ \frac{1}{m} \end{bmatrix} \cdot F_y(t)$$
 (2.39)

$$y = \begin{bmatrix} 1 & 0 \end{bmatrix} \begin{bmatrix} y_1 \\ y_2 \end{bmatrix} + 0 \cdot F_y(t) \tag{2.40}$$

These equations are for a simple cantilever model with a lumped mass at the end of the beam (lumped mass accounts for nacelle and tower mass). The resulting natural frequency from this model matches the ABAQUS FEA results from Gwon's paper [11]. A comparison between the resulting natural frequency from this model and the ABAQUS FEA results in Gwon's analysis [11] can be seen in Table 2.2.

Chapter 3

DIGITAL SIGNAL PROCESSING MODEL

3.1 Model Block Diagram

The blade imbalance detection is simulated using MATLAB/Simulink. Figure 3.1 shows the block diagram for a method of imbalance detection where the rotor frequency is known. This is an accurate method, but requires the information from an encoder on the shaft or an accurate phase-locked loop (PLL) controller.

The force due to an imbalance is given in Equation 2.1. It is a periodic function with the same frequency as the rotor and is proportional to the effective imbalance mass, m. The variable forcing function is the input for the lumped parameter turbine tower state space model. These vibrations are then read by an acceleration sensor with a sampling rate of 100 Hz. The frequency of interest is demodulated using a lock-in amplifier or DFT, which should result in the acceleration from only the imbalance. The acceleration at the top of the tower should have higher intensity vibrations at the rotor frequency when there is an imbalance in the blades (causing an eccentric mass).

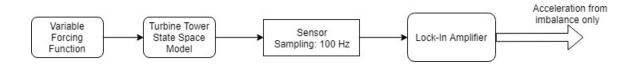


Figure 3.1: A block diagram showing the lock-in amplifier and the turbine tower simulation.

3.2 Processing the data

This paper describes a few ways to process the acceleration data from the turbine tower. One method relies on accurate frequency information to precisely demodulate the signal at the rotor frequency. An alternative method is to lock onto the strong frequency vibration of the tower using a phased-lock loop controller. Finally, a discrete Fourier transform can be calculated to transform the time domain data to the frequency domain. There are various ways to make this process more efficient, including zoom FFTs and the Goertzel algorithm.

The simulation and turbine tower state space model produce displacements shown in Figure 3.2. The same simulation data is shown in the frequency domain in Figure 3.3. From the frequency domain, it can be seen that there is resonance at 0.84 Hz (the natural frequency of the tower in the x-direction). Additionally, there is an excitation at the rotor frequency that has a magnitude proportional to the amount of mass at the end of the blade. This simplified linear model produces an displacement signal that can be represented by the sum of sines as shown in Equation 3.1 (this can be seen in Figure 3.2).

$$y = C_1 \sin(\omega_n t + \phi_1) + C_2 \sin(\omega_{drive} t + \phi_2)$$
(3.1)

The first method for processing the acceleration data utilizes lock-in amplifier to translate the data in the frequency domain. This new data, with the rotor frequency shifted to 0 Hz, is filtered and results in a DC acceleration that should be proportional to the imbalance mass. The second method utilizes a zoom FFT, which provides higher resolution than a typical FFT in the bandwidth of interest. The third method uses a Goertzel algorithm to calculate the bin of interest in the DFT.

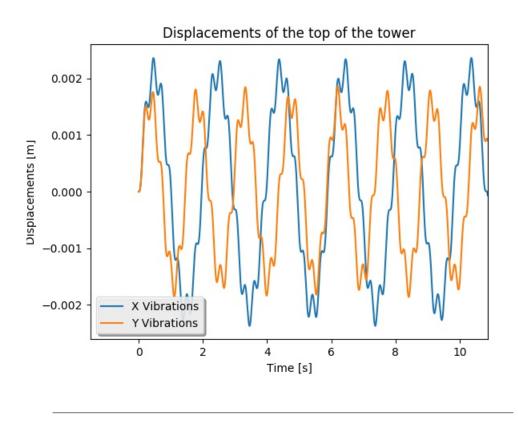


Figure 3.2: The simulated displacement for a rotor imbalance at 230 RPM. The imbalance mass is placed at the end of the blade, which causes accelerations and displacements at the top of the tower.

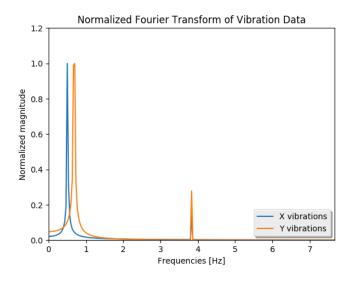


Figure 3.3: This figure shows the simulated displacement data in the frequency domain. The rotor frequency is 230 RPM in this simulation

3.2.1 DFT review

A Discrete Fourier Transform (DFT) converts a signal from the time domain to the frequency domain. Typically, this is performed with using the Fast Fourier Transform (FFT) algorithm, which is an efficient method for calculating the DFT. The DFT is defined by the formula in Equation 3.2 [?].

$$X_k = \sum_{n=0}^{N-1} x_n \cdot e^{-\frac{i2\pi}{N}kn}$$
 (3.2)

 \vec{x} is the original signal in the time domain with N elements, and \vec{X} is the signal in the frequency domain with N elements. Equation 3.2 can be rewritten using Euler's formula to show DFT equation in terms of sine and cosine values (this is important for understanding the lock-in amplifier in a future section). Equation 3.3 shows the new expression for the DFT equation.

$$X_k = \sum_{n=0}^{N-1} x_n \cdot \left[\cos \left(\frac{2\pi kn}{N} \right) - j \sin \left(\frac{2\pi kn}{N} \right) \right]$$
 (3.3)

From Equation 3.3, it can be seen that the DFT can be calculated by mixing the signal, \vec{x} , with a sine and cosine signal and summing the result for each frequency. The DFT equation can be further rewritten using vector notation as in Equation 3.7 and defining some reference vectors. This equation shows that the DFT of a signal is an imaginary vector that can be created from the dot products of the original signal and some reference sine and cosine signals.

$$\vec{n}_r = \begin{bmatrix} 0/N \\ 1/N \\ 2/N \\ \vdots \\ (N-1)/N \end{bmatrix}$$
(3.4)

$$\vec{r}_{sin} = \sin\left(2\pi k \vec{n}_r\right) \tag{3.5}$$

$$\vec{r}_{cos} = \cos\left(2\pi k \vec{n}_r\right) \tag{3.6}$$

$$X_k = \vec{x}^T \cdot \vec{r}_{cos} - j\vec{x}^T \cdot \vec{r}_{sin} \tag{3.7}$$

Another way of looking at the DFT (from the form in Equation 3.7) is as a time domain convolution with a low pass filter. The summation (shown explicitly in the form from Equation 3.3) acts as a simple finite impulse response (FIR) decimation filter with unity coefficients and a decimation rate of d = N, commonly known as an averaging filter. When thinking about the DFT in this way, some possible optimization methods start to become clear. For example, we may not need to calculate the frequency component for every kth element in \vec{X} , and we may choose to use a better filter that has stronger attenuation at higher frequencies. This is the basis for the lock-in amplifier design described in the next section.

3.2.2 Lock-In Amplifier

A lock-in amplifier is used to measure AC signals in particularly noisy environments (Figure 3.4). It works by multiplying the noisy signal by a reference signal created by an internal oscillator. By using 2 reference signals out of phase, the real and imaginary parts of the signal at the specified carrier frequency can be calculated[3]. Let's say there is an unknown sinusoidal signal with high frequency noise ($\omega_2 \gg \omega_1$):

$$y = A\sin(\omega_1 t) + B\sin(\omega_2 t) \tag{3.8}$$

The amplitude of the signal, A, can be determined by multiplying the signal, y, by a reference signal with the same frequency as ω_1 and filtering:

$$y \cdot \sin(\omega_1 t) = [A \sin(\omega_1 t) + B \sin(\omega_2 t)] \sin(\omega_1 t)$$
(3.9)

$$= A \sin^2(\omega_1 t) + B \sin(\omega_1 t) \sin(\omega_2 t)$$
(3.10)

$$= A\left(\frac{1}{2} - \frac{1}{2}\cos(2\omega_1 t)\right) + B\sin(\omega_1 t)\sin(\omega_2 t)$$
 (3.11)

Note that Equation 3.9 resembles the imaginary part of the standard DFT equation (Equation 3.3), where the input signal is multiplied by a sine wave at a set reference frequency.

A filter is applied to Equation 3.11 (similar to the summation filter used in Equation 3.3), with a cutoff frequency that is smaller than ω_1 . This results in all terms approaching zero, except for $\frac{A}{2}$, which can be calculated and solved for A to achieve the magnitude of the frequency component at ω_1 . To calculate the magnitude and phase of the signal y, it must be multiplied by a reference sine signal (as in Equation 3.9) and a reference cosine signal. The following equation shows the result of the mixing step (phase-sensitive detection) in the lock-in amplifier:

$$Y = X\cos(\omega t) + jX\sin(\omega t) \tag{3.12}$$

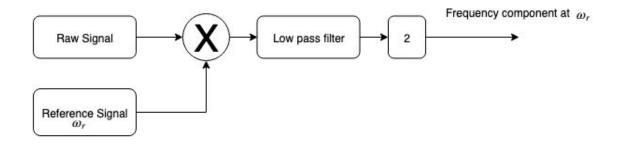


Figure 3.4: A block diagram showing the details of a lock-in amplifier [2]. This figure was created with Draw.io.

where X is the noisy AC signal and Y is the signal that is fed into a filter to remove any unwanted frequency components at ω_1 and $2\omega_1$ and produce a signal, $Y_{filtered}$ that only contains the DC component:

$$Y_{filtered} = \frac{A_{real}}{2} + j \frac{A_{imaginary}}{2} \tag{3.13}$$

Using the lock in amplifier tuned to a constant frequency, Figure 3.5 shows the resulting output. This shows that an imbalance can be detected by measuring the output of a lock-in amplifier that is tuned to the frequency of the turbine rotor. When the acceleration data is treated as an AM signal, with the carrier frequency equal to the rotor frequency, the acceleration due to the rotation of the blades can be identified. This acceleration is directly related to the mass at the end of the blade, and should be a constant value (as long as the rotor frequency is accurately known).

Lock-in amplifiers are typically used when the frequency is relatively stable and the signal-to-noise ratio is low. For this application, the rotor frequency can change, which may not give the LIA filters enough time to settle. If there is a very stable and accurate rotor speed controller, this method would be ideal because it extracts the signal of interest despite the high noise and distortions in the measurement.

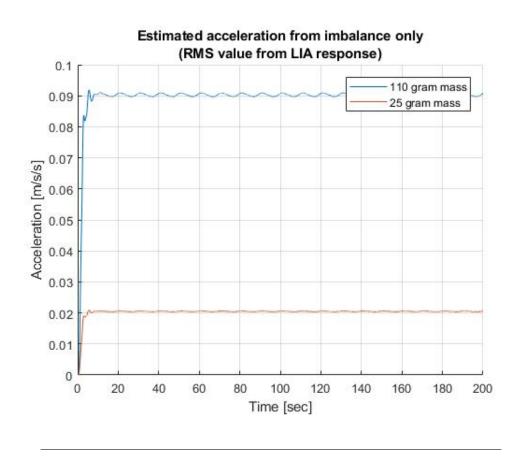


Figure 3.5: The output of the lock-in amplifier from the simulated data shown in Figure 3.2

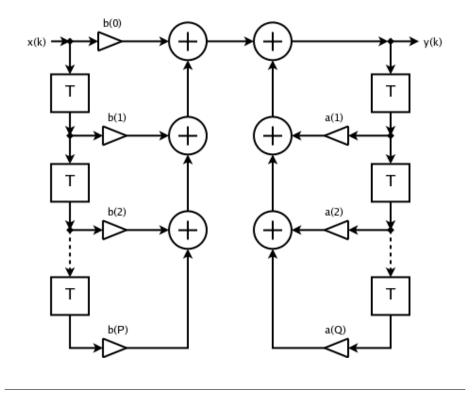


Figure 3.6: A block diagram of a standard IIR filter. [6]

3.2.2.1 Types of low-pass filters

The filter choice is very important for a lock-in amplifier. Some of the common options are finite impulse response (FIR) filters, and infinite impulse response (IIR) filters, and the Savitzky-Golay (SG) filter.

The IIR filter is shown in Figure ??, which significantly smooths the data, but at the cost of some time-domain distortion. An IIR filter uses past states in the output calculation, meaning an impulse input signal will affect the filter output forever (*infinite* impulse response filter). This results in a transfer function as follows:

$$T(z) = \frac{b(z)}{a(z)} \tag{3.14}$$

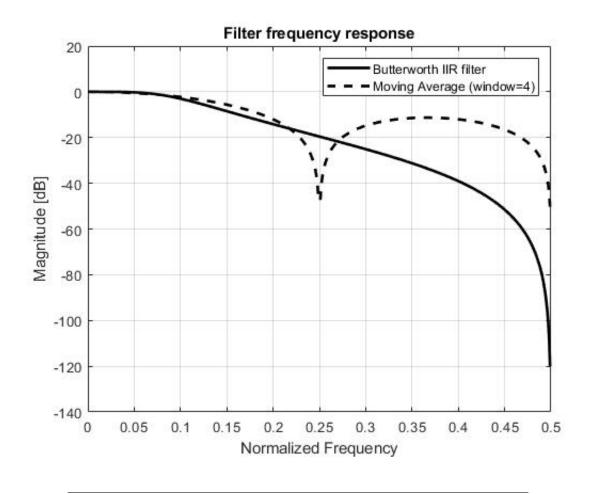


Figure 3.7: The filter response of the Butterworth IIR filter (Equation ??) compared to a moving average filter with a window size of 4. This figure was created in MATLAB with 2 simulated filter designs.

Figure 3.7 shows the result of a Butterworth IIR filter compared to a moving average filter. This shows that a customized filter is much more effective than standard moving average methods of smoothing data.

Another filter alternative is the FIR filter, which does not rely on past states to calculate the filter output. This results in a finite response to an impulse input and a linear phase. A common FIR filter that is used for smoothing data is a moving average (where all of the filter coefficients are identical). To achieve a more customized filter for this data, a FIR filter is designed using the Window method, which designs a FIR

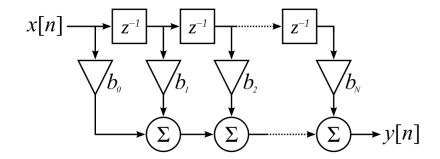


Figure 3.8: A block diagram of a standard FIR filter. [5]

filter using a specified window. Figure 3.8 shows a block diagram of a FIR filter. One of the most common uses of FIR filters is to decimate a signal (not having to calculate previous states allows for some significant optimizations when decimation is involved). Because the past states are not used, the transfer function has a denominator of 1:

$$T(z) = \frac{b(z)}{1} \tag{3.15}$$

Another filter option for this data is the Savitzky-Golay (SG) filter, which increases the signal-to-noise ratio with out significantly distorting the signal. The SG filter uses convolution to fit a polynomial on a sliding window to the data. The output of this filter can be calculated using the following equation [18]:

$$Y_j = (\mathbf{C} \otimes y)_j = \sum_{i = -\frac{m-1}{2}}^{\frac{m-1}{2}} C_i y_{j+i}$$
 (3.16)

 C_i are the convolution coefficients (m total coefficients), y is the sampled data point, and j is the index of the data point.

The convolution coefficients can be selected from a table, but it is much more robust

to calculate them prior to performing any filtering. The convolution coefficients, \mathbf{C} , are calculated using a variable change. The time vector for a given window, \vec{x} , is converted to \vec{z} using the time step (Δt) with the following equation:

$$z = \frac{\vec{x} - \bar{x}}{\Delta t} \tag{3.17}$$

 \bar{x} is the time value at the central point of the window. \vec{z} is used to calculate the matrix \mathbf{J} , where each i—throw of \mathbf{J} has the values $1, z_i, z_i^2, z_i^3, ..., z_i^n$. After \mathbf{J} has been created, the convolution coefficients can be calculated as follows:

$$\mathbf{C} = \left(\mathbf{J}^{\mathbf{T}}\mathbf{J}\right)^{-1}\mathbf{J}^{\mathbf{T}} \tag{3.18}$$

The filtered data can then be calculated as the convolution of \mathbf{C} and the unfiltered data (Equation 3.16).

3.2.3 Identifying the rotor frequency from the tower accelerations

If the rotor frequency cannot be measured directly it is possible to obtain the frequency indirectly from the acceleration data. A phase-locked loop is a control system that minimizes the phase between to signals. As the phase error is driven to zero, the output signal frequency approaches the input signal's frequency. Phase-locked loops (PLLs) are commonly used in telecommunications where the frequency of a noisy signal can be recreated with an internal oscillator that locks on to the frequency of the noisy signal. Figure 3.9 shows a block diagram of the PLL implementation with tower acceleration data as the input.

The first stage of the frequency detection is a narrow bandpass filter to get rid of high

frequency noise and natural frequency resonance of the tower. This is multiplied by an internal oscillator that starts at an arbitrary frequency (a guess that is close to the actual frequency, but not necessarily accurate). This signal is passed through a lowpass filter to provide a steady phase error. The phase error is driven to 0 using a PID controller. This outputs the correct frequency of the signal that is then fed back and multiplied with the input signal.

One of the problems with a phase-locked loop is the PID controller gains depend on the amplitude of the signal, which changes depending on the amount of imbalance and rotor frequency. The simplest approach to this would be to normalize the accelerations with the expected frequency. This, however, is not perfect and doesn't account for the acceleration variation due to different eccentric masses. A better solution would be to use a simple envelope detector to determine the amplitude of signal. The accelerations can be divided by the output of the envelope detector to normalize the signal. Figure 3.11 shows an example of a simple envelope detector[4]. The low-pass filter in the envelope detector can be designed based on the desired accuracy. For high computational efficiency, an averaging filter can be used because it minimizes the amount of multiply operations, and reduces the filter calculation to summations only.

3.2.4 Zoom FFT

A very powerful method for reducing the computational cost of the FFT calculation is to use a Zoom FFT. If the imbalance detection device contains a low-power processor, it will be able to run for a long time off of a battery. This also means that the processor could be much slower than an alternative high-power processor. A Zoom FFT will significantly reduce the computational load on the processor, allowing the low-power processor to sufficiently calculate the frequency spectrum of the input signal.

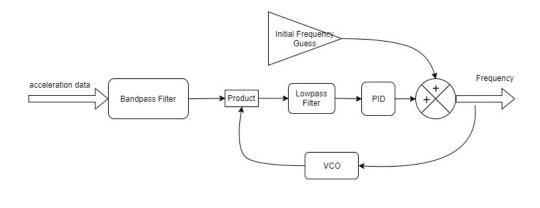


Figure 3.9: The block diagram of a phase-locked loop implementation when detecting rotor frequencies from acceleration measurements [14]. This diagram was created with Draw.io [?].

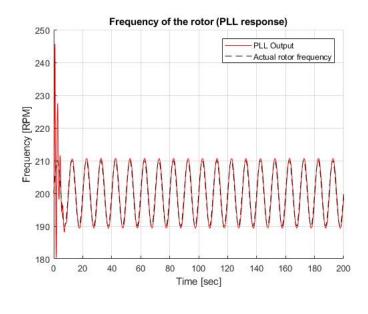


Figure 3.10: The output of the PLL when detecting frequency from the data shown in Figure 3.2. The frequency of the input data oscillates from 190 RPM to 210 RPM to simulate a real turbine controller that may oscillate between frequencies.

Envelope Detector u^2 Low pass filter 2 \sqrt{u}

Figure 3.11: A block diagram for a simple envelope detector. The signal is first squared and multiplied by a gain of 2. This signal (which should be entirely positive) is sent through a lowpass filter to remove the high frequency information. The lowpass filter needs to reject 2f, which is the resulting frequency when a signal with frequency, f is squared. The square root of the resulting signal produces the the amplitude of the signal. This figure was created with Draw.io.

One of the main tradeoffs for the reduced computational load, is a reduced frequency spectrum range. For example, a set of 1024 data points sampled at F_s , will produce a frequency spectrum from 0 to $F_s/2$ using the standard FFT. A zoom FFT with a decimation rate of D=10 can produce a frequency spectrum with a range of $F_s/20$ at 1/10th the computational cost.

If the frequency of the rotor is not precisely known, then a lock-in amplifier is difficult to implement. In order to detect excitation at the rotor frequency, the time-domain data can be transformed into the frequency domain. A discrete Fourier transform (DFT) is the frequency domain representation of a sampled signal; however, can be slow and difficult to calculate on a microcontroller.

To efficiently calculate the Fourier transform, the DFT matrix can be factored and the complexity reduced from $O(n^2)$ to $O(n \log n)$. This efficient algorithm is called the fast Fourier transform (FFT). Despite being much more efficient than the standard DFT, a generic FFT is still inefficient for this application because most of the frequency data occurs outside the bandwidth of interest and is thrown away. This can be fixed by applying a zoom FFT algorithm.

The zoom FFT consists of 4 main steps. First the data is convoluted with a reference signal in the time domain (translated in the frequency domain) to shift a center frequency, F_c , to 0 Hz. Second, a lowpass filter prevents aliasing when sampling at a lower sample rate. An infinite impulse response (IIR) filter can be used for simplicity; however, the phase information of the signal is lost. To solve this, a finite impulse response (FIR) filter can be used. FIR filters are more complicated but most have a flat phase response, ensuring the filter output retains the original phase information. Typically, discrete FIR filters are applied in various 2-stage filters for simplicity. Third, the data is decimated (re-sampled at a lower rate). Finally, the decimated data is passed through a FFT algorithm that produces a frequency spectrum in the specified bandwidth. Since the frequency range of the zoom FFT is much smaller, the resolution can be much higher for a FFT length. Alternatively, a much smaller FFT length can be used to produce the same resolution.

For a microcontroller sampling the acceleration of the turbine tower at 100 Hz, Figure 3.12 shows a block diagram of a zoom FFT implementation for detecting an imbalance. Point A represents the raw input signal, which is the acceleration of the tower sampled at $F_s = 100$ Hz in this case. The frequency translation is performed by mixing the input signal with a reference signal at F_c . The goal of a Zoom FFT is to reduce the amount of data by decimating the original signal and reducing the sampling rate. Just performing a sampling rate reduction would result in aliasing, so there needs to be a digital anti-aliasing filter that prepares the signal for the decimation step. This digital filter is a low pass FIR filter that produces a filtered signal at Point C, which can then be decimated without aliasing to achieve Point D. This new set of data is sampled at $F_{s,new} = \frac{F_s}{D}$, which means the frequency spectrum spans a much smaller range.

Zoom FFTs [8] contain the following parameters:

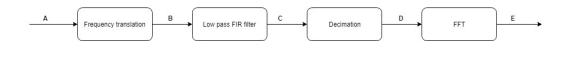


Figure 3.12: A block diagram showing the zoom FFT algorithm. This figure was created with Draw.io.

 F_c : The frequency center (shifted to 0 Hz by the zoom FFT)

BW: The bandwidth of interest

 F_s : The sampling rate

N: The length of the FFT

The decimation factor, D, is calculated as follows:

$$D = floor\left(\frac{F_s}{BW}\right)$$

Where the length, L, of the initial buffer into the decimator is:

$$L = D \cdot N$$

The computational reduction for a Zoom FFT is shown in Figure 3.13. However, it is important to note that a stronger filter is required for higher decimation factors, D. This means there is a trade-off between FFT computational load and filter computational load. A zoom FFT is just the name of a method of frequency transformation where the data is decimated before applying the FFT algorithm. The computational savings occur when a well-designed lowpass filter does not negate the workload reduction caused by the FFT. Essentially, this is a much more flexible FFT where different aspects can be modified to optimize for the application. In this case, the Zoom FFT can provide a much higher resolution frequency analysis because the frequencies of interest are much smaller than the sampling rate.

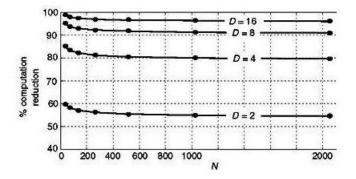


Figure 3.13: A diagram showing the percent computational workload reduction of a $\frac{N}{D}$ -point Zoom FFT relative to a standard *n*-points FFT [14].

3.2.4.1 Frequency translation

Shifting data in the frequency domain is a common technique used in AM radio signals. Audio frequencies are typically mixed with a high frequency carrier that, according to the Nyquist criteria, would require an extremely high sample rate to capture the signal.

If ω is the rotor frequency, multiplying the time domain signal by $\cos(-\omega t)$ is the same as convolving the data in the frequency domain. Since the frequency spectra for $\cos(-\omega t)$ is symmetric across the y-axis, the time-domain must be multiplied by an imaginary wave.

The equation for the frequency-shifted time-domain data is:

$$Y = Xe^{-i(\omega t)} (3.19)$$

where Y is the shifted data, X is the original data, ω is the rotor frequency, and t is the time. Based on Equation 3.19, the real and imaginary parts of the shifted signal

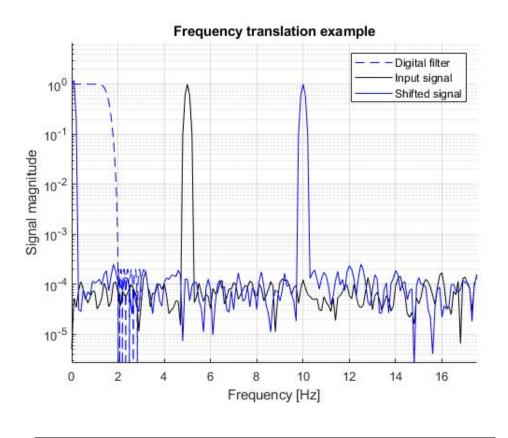


Figure 3.14: This figure shows an example of frequency translation. The black signal is the frequency spectrum of some input signal that has a strong component at 5 Hz. The blue signal shows the frequency shifted spectrum that results from multiplying the input signal by a reference signal with a frequency of 5 Hz (as shown in Equation 3.21). The dotted blue line shows the digital filter response. This figure was generated with MATLAB.

are shown below [8]:

$$Y_{real} = X \cos(\omega t) \tag{3.20}$$

$$Y_{imaginary} = -X\sin\left(\omega t\right) \tag{3.21}$$

An example of frequency translation is shown in Figure 3.14. The blue signal is the frequency-shifted signal, which has a higher frequency at 2 times the original signal frequency. In order to remove the extra component at 10 Hz, the digital filter (shown with a dotted blue line) must be applied to the shifted signal.

3.2.4.2 Decimation/downsampling

Decimation is the process of reducing the sample rate of a signal. Before the data is downsampled, the high frequency components are reduced with a lowpass filter. This filter is also called an anti-aliasing filter because it prevents high frequency data from being misinterpreted at a different sample rate. Equation 3.22 shows the equation used for calculating the output of a FIR decimator, where x is the input data, h is the impulse response, K is the length, and D is the decimation factor [13].

$$y[n] = \sum_{k=0}^{K-1} x[nD - k] \cdot h[k]$$
 (3.22)

Figure 3.14 shows a visual representation of the decimation process and anti-aliasing filter. The shifted signal (blue) contains important frequency information in the range 0 - 2 Hz. Any higher frequencies have been significantly attenuated by the digital filter (dotted blue line). This means the blue data can be decimated to a new sampling rate of 4 Hz, without any aliasing effects (because the digital filter ensures there are no strong components above 2 Hz).

3.2.4.3 An optimized Zoom FFT implementation

Table 3.1 shows the parameters for the Zoom FFT. These values have been strategically picked to make the optimization process easier. In general, some nice optimizations can be achieved if the number of filter coefficients (N_b+1) is an integer multiple of the sampling rate (F_s) .

In Table 3.1, the FFT length is the number of samples in the buffer used as the input to the FFT. An FFT length of 1024 means that 1024 samples are used as an input to the FFT algorithm. The FIR filter order is 255, which is high because it needs to strongly attenuate higher frequencies with a narrow pass band. Despite having

Table 3.1: Zoom FFT parameters

Variable	Value	Description	
F_{min}	2 Hz	The minimum frequency for the Zoom FFT calculation	
F_s	128 Hz	The original sampling rate	
F_r	4 Hz	The frequency range of the Zoom FFT	
N_{fft}	128	FFT length (buffer length used in the FFT calculation)	
N_b	255	FIR filter order	
D	$\frac{F_s}{2F_r} = 16$	Decimation rate	

an extremely large order, the FIR filter is simple and computationally inexpensive to implement (this will be shown later in this section). An order of $N_b = 255$ means the filter order will have $256 \ (N_B + 1)$ coefficients. F_{min} and F_r define the frequency range that the Zoom FFT is targeting. More specifically, the Zoom FFT will calculate the frequency spectrum of the input signal only from F_{min} to F_r . The filter design is highly motivated by the frequency range because it needs to attenuate the original signal sufficiently (to prevent aliasing at the decimation step) at the edge of the frequency range.

The reference signal for the Zoom FFT is created at the minimum frequency, F_{min} shown in Table 3.1 and is shown in Equation 3.23.

$$y_{ref} = \sin\left(F_{min} \cdot 2\pi \cdot time\right) \tag{3.23}$$

Note that there are only 64 unique values in a reference signal with the specified F_{min} . This means that all of these values can be precomputed at initialization and stored in memory. This removes the sin () operations from the real-time calculations, which reduces the computational time, since trig functions are one of the slowest floating-point operations (they are typically about 15X slower than a floating-point addition

operation) [?].

One of the benefits for using a finite impulse response (FIR) filter is that there are no recursive calculations. This produces a very important property of FIR filters, which is that not all the outputs need to be calculated. Assuming there are $(N_b + 1)$ filter coefficients, a random window of $(N_b + 1)$ samples can be properly filtered at any time during operation. If we are decimating the input signal, this means we do not have to calculate the filter outputs for samples that are removed due to the decimation step.

The down-sampled data, y_{ds} , can be calculated as follows (\odot is the element-wise multiplication operator):

$$y_{ds} = \vec{y}^T \cdot \left(\vec{y}_{ref} \odot 2\vec{b} \right) \tag{3.24}$$

In Equation 3.24, y_{ds} is the value at the decimated sampling rate. \vec{y} is a sliding buffer of the original input data, which is a vector of $(N_b + 1)$ values. \vec{y}_{ref} is the vector of the reference signal values, which also has a length of $(N_b + 1)$. \vec{b} is the vector of FIR filter coefficients. The factor of 2 in this equation is a result of the derivation of the frequency-shift process. Equation 3.24 is calculated at the decimated sampling rate (F_{sD}) , which is shown in Equation 3.25.

$$F_{sD} = \frac{F_s}{D} \tag{3.25}$$

Equation 3.24 can also be used with larger filter orders. Effectively, this means that the filtering and decimation part of the Zoom FFT can be performed with just a single dot product and an element-wise vector multiplication. Using the values in Table 3.1, the following steps can be followed to create a Zoom FFT algorithm:

- 1. Precompute the unique values of the reference signal during initialization.
- 2. Design a FIR filter with an appropriate cutoff frequency and filter order. The

cutoff frequency (F_{cutoff}) is equal to the frequency range (F_r) of the Zoom FFT. The coefficients of this filter are stored in \vec{b} .

- 3. Generate a sliding buffer of data with a window size of $(N_b + 1)$ and an overlap of $(N_b + 1 \frac{F_s}{D})$, which is stored in \vec{y} .
- 4. Perform the calculation shown in Equation 3.24.
- 5. Calculate the FFT of the newly decimated data.

Figure 3.15 shows the results of a MATLAB simulation using the Zoom FFT to calculate the frequency spectrum. In this simulation, the standard FFT uses an FFT length of 2048, while the Zoom FFT only has a length of $N_{fft} = 128$. This is a significant reduction in computation for the same frequency resolution in the target Zoom FFT range. Both a standard FFT and a Zoom FFT use the same FFT algorithm, so the difference in performance comes from the lower sampling rate, and therefore smaller frequency range.

3.2.4.4 Estimating processor performance

Comparing the computational time of different algorithms is difficult because the dominant factor is usually memory access, rather than actual floating-point operations [?]. Evaluating the computational cost due to memory access patterns in complicated, so this analysis will only consider the computational cost of the floating-point operations (FLOPs). To minimize the cost from memory access patterns, the algorithms will be vectorized and converted to matrix form. Most processors have highly optimized matrix operation functions, which should hopefully make arithmetic the dominant factor when determining the computational cost.

For this analysis, a STM32 processor is used as the baseline for estimating cycle

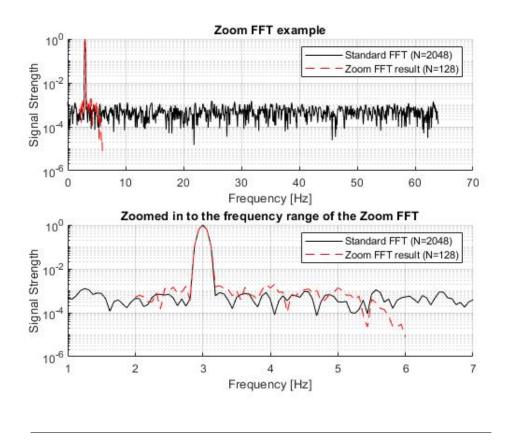


Figure 3.15: This figure shows the results of a Zoom FFT using the parameters listed in Table 3.1. The top plot shows the frequency spectrum from a standard FFT (black) and a Zoom FFT (red). The bottom plot shows the same data as the top plot, but zoomed into a narrow frequency range. The standard FFT has a length of 2048, while the Zoom FFT has a length of 128. This figure was created with MATLAB.

Table 3.2: Cycle counts for a STM32 floating-point processor. The exponential* operation is estimated from a floating-point performance analysis [?] because it is not stated in the STM32 datasheet.

Operation	Cycles
Absolute value	1
Negate of a float	1
Addition/subtraction	1
Multiply	3
Multiply and accumulate/subtract	3
Divide	14
Square Root	14
Exponential	20*

counts because it is the unit used to prototype the LifeLine data acquisition device that collects experimental acceleration data from the turbine. The STM32 has its own single precision register set to handle floating-point operations with hardware (rather than using compiled C libraries to perform the floating-point operations in many complex steps). The floating-point unit (FPU) in the STM32 offers arithmetic instructions for the operations listed in Table 3.2 [?].

Many FPUs (like the one in Table 3.2), have multiply/accumulate arithmetic instructions, which means they can perform a multiplication and addition all in one step. Additionally, division operations are much more expensive than multiplication operations and should be avoided as much as possible when designing algorithms.

3.2.5 Goertzel Algorithm

The Goertzel algorithm is a method for calculating individual bins of a discrete Fourier transform (DFT) without calculating all of the bins. Since imbalance detection depends on the strength of the rotor frequency, this algorithm produces the particular rotor frequency bin value without calculating the entire DFT. Fundamentally, this algorithm operates similarly to the Zoom FFT previously described, and is often called a Goertzel filter because the algorithm takes the form of a digital filter. This algorithm applies 2 stages of filtering, where the first stage is an infinite impulse response (IIR) filter, and the second stage is a finite impulse response (FIR) filter.

For the first stage of the Goertzel algorithm, a 2nd order IIR filter is applied to x:

$$s[n] = x[n] + 2\cos(\omega_0)s[n-1] - s[n-2]$$
(3.26)

This IIR filter follows a Direct Form II structure, where 2 state variables are required for a 2nd order filter. ω_0 is defined as the normalized frequency to be analyzed.

The second stage of the algorithm is a FIR filter, which is known for its linear phase, and lack of feedback. This means that the filter output does not depends on any previous outputs.

$$y[n] = s[n] - e^{-j\omega_0} s[n-1]$$
(3.27)

Equation 3.27 shows the output of the Goertzel equation, y[n].

There is an optimized version of the Goertzel algorithm that is even faster than the general form, but it produces squared magnitude components at each frequency instead of real/imaginary pairs [7]. The phase of the frequency component is not used in the imbalance detection algorithm, so the optimized Goertzel algorithm is well suited for this application. One of the benefits of the Goertzel algorithm is the

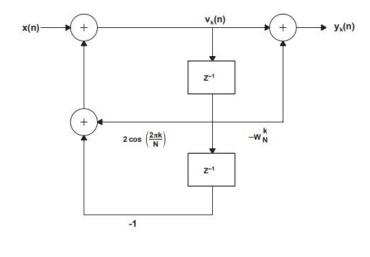


Figure 3.16: The direct-form realization of the Goertzel Algorithm[12].

buffer lengths do not need to be a power of 2. An overview of the algorithm in a block diagram form is shown in Figure 3.16.

The Goertzel algorithm is simulated with MATLAB and the results are shown in Figure 3.17. The Goertzel algorithm calculates individual frequency components of the DFT, which are identical to the values calculated with a standard FFT algorithm.

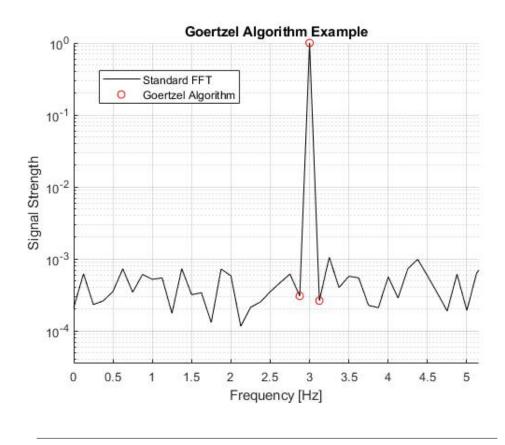


Figure 3.17: This figure shows the frequency spectrum calculated with a standard FFT (black) and a few points calculated with the Goertzel algorithm (red). This figure was created in MATLAB.

Chapter 4

IMBALANCE DETECTION ALGORITHM

TODO: describe LifeLine system.

4.1 Overview

A rotor imbalance can cause problems and failures with the turbine, so it is important

to detect the "state" of the turbine using some measured input. Turbine dynamics are

complicated, vary between different systems and can be dependent on many variables.

An effective way to develop a model that is optimized for each different turbine is to

use machine learning (ML). Machine learning is the study of algorithms that build

mathematical models to perform specific tasks without explicit instructions.

4.1.1 Machine learning background

The 2 main types of machine learning algorithms are supervised and unsupervised

learning. Supervised algorithms assume that each data set is assigned an output,

while unsupervised algorithms take a data set of only inputs and attempt to cre-

ate groups and classes from the input data. For this application, each measurement

data set from the turbine will be manually labeled as "good" or "bad" (or as "bal-

anced"/"unbalanced"), which is a type of supervised learning.

Machine learning algorithms also fall into the "regression" or "classification" cate-

gories. Regression algorithms are used if the output is a continuous function, while

classification algorithms are used if the output falls into distinct classes. The output

49

for the turbine detection algorithm is the state of the turbine (balanced/imbalanced), which is a discrete classification.

Knowing that the ML algorithm must be a classification, supervised model, the specific algorithm choice can be narrowed down. Some of the common algorithms are logistic regression (this can be used as a classification algorithm even though it is called "regression"), k-nearest neighbor, and neural networks. This paper will analyze each of these models and apply them to the experimental turbine data.

4.2 The training data

Typically, it is common for machine learning algorithms to split the data into test and training sub groups. This allows the accuracy of the models to be trained and evaluated on different data sets. The input data for the turbine is a 256-point frequency spectrum of the acceleration data at the top of the tower. Figure 4.1 shows a spectrogram of the measured acceleration data. A spectrogram is a way to visualize frequency data over time in a 2-dimensional figure, where the magnitudes of each frequency component are represented by a different color. The spectrogram shows that there is a strong frequency component at about 2.4 Hz (the rotor frequency) that is constant throughout most of the operation.

Currently, only a single set of about 100 training examples exists. The data can be separated into 2 classes; however, there is no information about which is the *balanced* and *imbalanced* classes. To properly train the machine learning models, more data is required. Despite the lack of available data, this paper will discuss the methods and implementations of each algorithm using the limited data set.

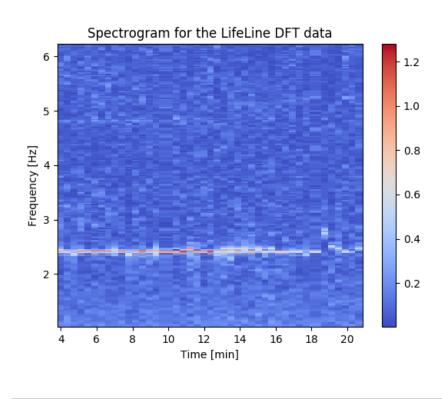


Figure 4.1: This figure shows the spectrogram of the tower accelerations.

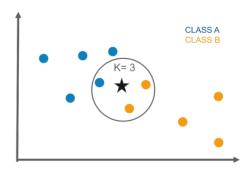


Figure 4.2: A visualization of the KNN algorithm [?]. The training data for a 2-class problem with 2 inputs is shown as blue and orange dots. For K=3, a circle is drawn around the new point (star) until 3 training data points fall within the circle. The classification of the new point is then determined by the majority of the points inside the circle. In this case, there are more $Class\ B$ points than $Class\ A$ points, so the new point (star) will be classified as $Class\ B$.

4.3 K-Nearest Neighbor algorithm

4.4 About the algorithm

The k-nearest neighbor (KNN) algorithm is one of the simplest models, but can be the most accurate and powerful when dealing with fairly small data sets. This model essentially "memorizes" the training data and plots the points in *n*-dimensional space. The classification of a new point is calculated based on the distances between the new point and the training points. For example, Figure 4.2 shows a visualization of the classification process for a 2-class system. Since this algorithm uses all of the training data in memory, it becomes very slow with many inputs, and many training data sets. The example in Figure 4.2 is a 2-dimensional problem (only 2 inputs) with only a few data points, so the KNN algorithm works very well.

The K-NN algorithm uses a "majority voting" method where the Euclidian distance between all the training data points and the test data is calculated. This model assumes there is a relatively equal amount of balanced rotor experimental data and imbalanced experimental rotor data, which means the sample weighting can be uniform. If there is a much higher frequency class (for example, much more balanced experimental data), this class will tend to dominate the calculations regardless of the actual class of the test data.

The number of neighbors, k, is chosen to be 5 for this algorithm (using trial and error). A larger value of k will reduce the classification noise, but the boundaries are much more general and not as tuned to the training data. A lower value of k will match the model very closely to the training data, but may add noise into the classification process.

The Euclidean distance is simply the distance between the data points. This equation is shown below:

$$d = \sqrt{\sum (x_{i,a} - x_{j,a})^2}$$
 (4.1)

4.4.1 Choosing the data

The KNN algorithm works well on small data sets, so the DFT data should be preprocessed and cut down to a smaller, 2-dimensional data set. Based on a simplified dynamic model of the turbine tower, a rotor imbalance will cause a high frequency excitation at the rotor frequency. Using the maximum frequency component of the experimental DFT data and the corresponding frequency is a good way to capture enough information about the tower, while also reducing the data set from 256 input points to only 2 input points.

Figure 4.3 shows the frequency spectrum from a single DFT calculation. To convert

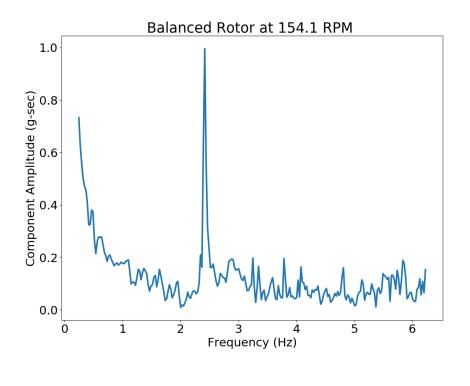


Figure 4.3: This figure shows a single DFT result (a single column from Figure 4.1).

this data into 2-dimensional data for the KNN algorithm, the peak value and corresponding frequency are extracted from this data. For example, Figure 4.3 would produce a 2-dimensional data set as shown in Equation 4.2.

$$[frequency, amplitude, class] = [2.3, 1.0, Class A]$$
 (4.2)

By converting the entire data set for all training examples into 2-dimensional data, the data in Figure 4.1 can be represented as the data in Figure 4.4.

4.4.2 Algorithm Results

To apply the algorithm, the data is converted into short lists containing a maximum amplitude, a corresponding frequency value, and the known class (Equation 4.2). For

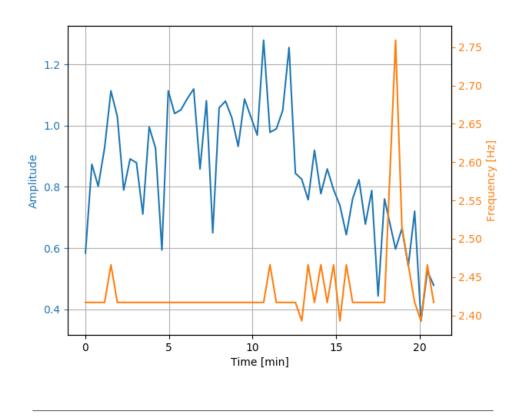


Figure 4.4: This figure shows a the 2-dimensional data used as an input to the KNN classification algorithm.

Table 4.1: An example of the terminology for the confusion matrix in Equation 4.3. Class A and Class B represent the different classes of data. These can be related to a balanced and imbalanced rotor with proper data set labels.

	Predicted Class A	Predicted Class B
Actual Class A	12	1
Actual Class B	3	6

this test, there are 55 experimental DFT results for $Class\ A$ and 55 experimental DFT results for $Class\ B$.

Training the KNN model is extremely fast and only involves storing all of the training data in memory. When the algorithm is applied to new test examples, the results can be visualized in a confusion matrix [?] as shown in Equation 4.3. A confusion matrix is a common tool used to describe the performance of a classification algorithm. This is an n by n matrix (where n is the number of classes) that essentially shows the amount of correct and incorrect guesses for each class. Table 4.1 shows a labeled version of the confusion matrix shown in Equation 4.3.

$$C_{confusion} = \begin{bmatrix} 12 & 1\\ 3 & 6 \end{bmatrix} \tag{4.3}$$

A nice way to visualize the results of the classification algorithm with 2-dimensional inputs is to create a decision boundary plot. A decision boundary is the area in space where the algorithm switches to a different classification. Figure 4.5 shows the classification boundary for the KNN algorithm with K=3.

Initially, the balanced and imbalanced classes were expected to be easily distinguish-

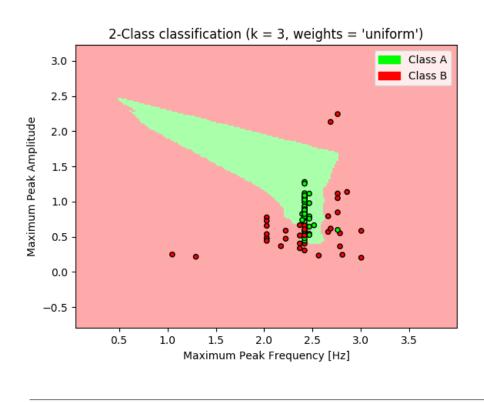


Figure 4.5: This figure shows the classification boundary for the KNN algorithm with K=3 for all of the training data.

able from each other. Despite not having accurate labels of the experimental data, the imbalanced rotor data was expected to have much higher amplitudes at the rotor frequency; however, from Figure 4.5, there isn't a significant difference between the amplitudes of the 2 data classes.

One observation that can be made from the data shown in Figure 4.5 is that the Class A data seems to have more frequency stability. The Class A data has a constant frequency of about 2.5 Hz, while the Class B data has varying frequencies. There is not enough data to make any hard conclusions, but this variance could be caused by either wind speed fluctuations or an actual property of the imbalance. It is possible that an imbalance in the rotor could cause more variations in rotor speed, despite not having significant amplitude differences. However, until the data can be accurately labeled, or more experimental data is collected, these classes should remain Class A and Class B to avoid any incorrect assumptions about the rotor imbalance.

4.5 Logistic Regression

4.5.1 About the algorithm

Logistic regression (LR) is a modified version of linear regression that is adapted for classification problems. Logistic regression minimizes the squared error of a linear combination of the input parameters when passed through a sigmoid function. To fully understand logistic regression, a brief background of linear regression is required.

Linear regression is the process of minimizing the least squares cost of a data set with a linear function. This is a commonly utilized method in curve fitting, but can also be applied to very high order systems. Mathematically, this means minimizing the cost function shown in Equation 4.4. The hypothesis is the linear curve fit shown in

Equation 4.5.

$$J(\vec{\theta}) = \frac{1}{2m} \sum_{i=1}^{m} (h_{\theta}(x_i) - y_i)^2$$
 (4.4)

$$h_{\theta}(x) = \mathbf{x} \cdot \vec{\theta}^{T} \tag{4.5}$$

$$\vec{\theta} = [\theta_1, \theta_2, \theta_3, \dots, \theta_n] \tag{4.6}$$

n is the number of parameters (or features) in the input, \mathbf{x} . m is the number of training examples, which means \mathbf{x} is of size [m, n] and $\vec{\theta}$ is a vector with n elements.

In order to apply linear regression to classification problems, the sigmoid function is applied to the linear regression hypothesis (h_{θ}) . The sigmoid function is defined in Equation 4.7 and is visually shown in Figure 4.6. The sigmoid function is designed to map an input to a value between 0 and 1, which represents the probability that the input is of a certain class. This sigmoid function is what enables logistic regression to calculate binary outputs.

$$g(z) = \frac{1}{1 + e^{-z}} \tag{4.7}$$

This new hypothesis function (Equation 4.9) produces a new cost function, shown in Equation 4.8.

$$J(\theta) = \frac{1}{m} \sum_{i=1}^{m} \left[y_i \ln(h_{\theta}(x_i)) + (1 - y_i) \ln(1 - h_{\theta}) \right]$$
 (4.8)

$$h_{\theta} = g(\mathbf{x} \cdot \vec{\theta}^T) = \frac{1}{1 + e^{-(\mathbf{x} \cdot \vec{\theta}^T)}}$$
(4.9)

The goal of logistic regression is to create a model that best fits the experimental training data by optimizing the parameters $\vec{\theta}$ to minimize the cost function, $J(\theta)$. To do this, the gradient descent method is used [?]. To perform gradient descent, both the cost function and the gradient function of $\vec{\theta}$ are required. The gradient can be numerically calculated using the finite difference method [?]; however, this is much

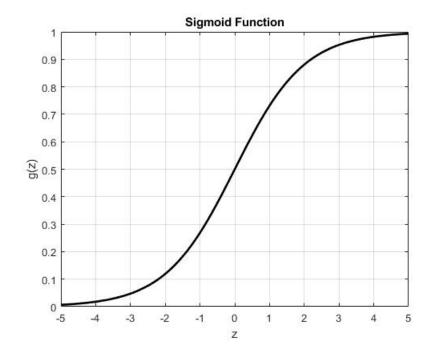


Figure 4.6: This figure shows the sigmoid function plot.

more computationally intensive than directly calculating the gradient analytically. The derivative of the sigmoid function is shown in Equation 4.10. This produces a simple equation for the gradient of the cost function, which is shown in Equation 4.11.

$$g'(z) = g(z)(1 - g(z)) \tag{4.10}$$

$$\frac{\partial J(\theta)}{\partial \theta_j} = \frac{1}{m} \sum_{i=1}^m \left(h_{\theta}(x_i) - y(i) \right) x_{j,i} \tag{4.11}$$

 h_{θ} is defined in Equation 4.9 and g(z) is defined in Equation 4.8. In other words, Equation 4.11 represents an average of (h-y)x for every training example and calculated with respect to each θ parameter (j is the number of parameters in the model).

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