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Problem 1

Points:

“I did not work in a group.”

“I did not consult anyone except my group members”.

non-class material: <https://www.geeksforgeeks.org/merge-two-sorted-arrays/>

Problem 2

Points:

1. $\Theta(n^3 \log n)$
2. $\Theta(n^3.5)$
3. $\Theta(n^4)$
4. $\Theta(n \log^2 n)$
5. $\Theta(n^{3.5} \log^3 n)$

Problem 3

Points:

1. the first time merging first two arrays will cost $n+n$ time and total length will be $2n$

the merging of third in to the first two will cost $2n+n$ time and total length will be $3n$

so until the last, it will cost $(m-1)*n+n$ time and total length will be mn

if we add them together, it will cost $O(n * m^2)$

2. if we use divide and conquer which introduced in class, we split the array in to half every time it will be near linear $O(m \log m)$, and total will cost $O(n * m \log m)$

Problem 4

Points:

for the pivot function here, we first divided into $n/3$ and calculate the medians, then divided in to $n/9$ and return selections

total run time is $\Theta(n) + \Theta(n/3 * \log 3) + \Theta(n) + \Theta(n/9 * \log 9)$

for $n/3$:

$$M = n/3$$

$$A1 > M/2 + M/2 = 2 * M/2 = M = n/3$$

$$A2 > M/2 + M/2 = 2 * M/2 = M = n/3$$

$$a = 1/3b = 2/3a + b = 1$$

$$T(n) = \Theta(n \log n)$$

for $n/9$:

$$M = n/9$$

$$A1 > M/2 + 4 * M/2 = 5 * M/2 = M = 5n/18$$

$$A2 > M/2 + 4 * M/2 = 5 * M/2 = M = 5n/18$$

$$a = 1/9b = 13/18a + b < 1$$

$$T(n) = \Theta(n)$$

and use master theorem to have $T(n) = \Theta(n^3 \log n)$

Problem 5

Points:

no idea