De La Salle ICPC Team Notebook (2018-19)

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1 Advanced Data Structures Without Libraries

1.1 Union Find Disjoint Set

```
rank.assign(n,0);
                size.assign(n,1);
                for(int i = 0; i < n; i++) { p[i] = i; }
        void unionSet(int i, int j) {
                if(!isSameSet(i,j)) {
                        int x = findSet(i), y = findSet(j);
                        if(rank[x] > rank[y]) {
                                p[y] = x;
                         } else {
                                 p[x] = y;
                                 if(rank[x] == rank[y]) { rank[y]++; }
                        size[x]+=size[y];
size[y] = size[x];
        int findSet(int i) {
                if(p[i] != i) {
                        p[i] = findSet(p[i]);
                return p[i];
        bool isSameSet(int i, int j) { return findSet(i) == findSet(j);}
};
```

1.2 Segment Tree

```
#include <vector>
using namespace std;
typedef vector<int> vi;
 * Segment tree for Range Maximum Queries
class SegmentTree {
        public:
        vi st, A;
        int n;
        SegmentTree(const vi &_A) {
                 n = (int)A.size();
                 st.assign(4 * n, 0);
                 build(1, 0, n - 1);
        int left(int p) { return 1 << p; }</pre>
        int right(int p) { return (1 << p) + 1; }</pre>
        void build(int p, int 1, int r) {
                 if(1 == r) {
                         st[p] = 1;
                 } else {
                          int m = 1 + (r - 1) / 2;
                          build(left(p),1,m);
                          build(right(p),m + 1,r);
                          int 1 = st[left(p)];
                          int r = st[right(p)];
st[p] = A[1] >= A[r] ? 1 : r;
        int rmq(int i, int j) {
                 return rmq(1,0,n-1,i,j);
        int rmq(int p, int 1, int r, int i, int j) {
    if(1 > j | | r < i) { return -1; }</pre>
                 else if(l >= i && r <= j) { return st[p]; }</pre>
                          int m = 1 + (r - 1) / 2;
                          int s1 = rmq(left(p),1,m,i,j);
                          int s2 = rmq(right(p), m + 1, r, i, j);
                          if(s1 == -1) {return s2;}
                          else if(s2 == -1) {return s1;}
                          else {return A[1] >= A[r] ? 1 : r; }
        void pointUpdate(int i, int val) {
                 pointUpdate(1,0,n-1,i,val);
        void pointUpdate(int p, int 1, int r,int i, int val) {
                 if(1 == r) {
                          A[i] = val;
                 } else {
```

1.3 Fenwick Tree/Binary Indexed Tree

```
#include <vector>
using namespace std;
typedef vector<int> vi;
class FenwickTree {
        public:
        vi ft;
        int n:
        FenwickTree(int _n) {
                n = n:
                ft.assign(n + 1,0);
        void update(int index, int increment) {
                while(index <= n) {</pre>
                         ft[index] += increment;
                         index += (index & (-index));
        int rmq(int end) {
                int res = 0:
                while (end) {
                         res += ft[end];
                         end -= (end & (-end));
                return res;
        int rmq(int i, int j) {
                if(i > j) { return 0; }
                 else if(i <= 0) { return rmq(j); }</pre>
                else {return rmq(j) - rmq(i - 1)}
};
```

2 Problem Solving Paradigms

2.1 Maximum 1D/2D Range Sum

```
#include <vector>
using namespace std;

typedef vector<int> vi;

int maxlDRangeSum(const vi &arr) {
    int ans = 0;
    int cur = 0;
    for(int i = 0; i < (int)arr.size(); i++) {
        cur += arr[i];
        if(cur < 0) cur = 0;
        ans = max(ans,cur);
    }
    return ans;
}

int max2DRangeSum(const vector<vi> &arr) {
    vi rowSums(arr.size(),0);
    for(int i = 0; i < (int)arr.size(); i++) {
        for(int j = 0; j < (int)arr[i].size(); j++) {
            rowSums[i] += arr[i][j];
        }
}</pre>
```

2.2 Longest Increasing Subsequence

```
#include <algorithm>
#include <vector>
using namespace std;
typedef vector<int> vi;
int lisSlow(const vi &arr) {
        vi memo(arr.size(),1);
        int ans = 1;
for(int i = 1; i < (int)arr.size(); i++) {</pre>
                 for(int j = 0; j < i; j++) {
    if(arr[i] > arr[j]) {
                                   memo[i] = max(memo[i], memo[j] + 1);
                  ans = max(ans, memo[i]);
        return ans;
int lisNLogN(const vi &arr) {
        vi memo:
        for(int i = 0; i < (int)arr.size(); i++) {</pre>
                  vi::iterator itr = lower_bound(memo.begin(), memo.end(), arr[i]);
                  if(itr == memo.end()) {
                          memo.push_back(arr[i]);
                  } else {
                           *itr = arr[i];
         return (int) memo.size();
```

$2.3 \quad 0/1 \text{ Knapsack}$

```
#include <vector>
using namespace std;
typedef pair<int, int> ii;
typedef vector<int> vi,
typedef vector<ii> vii;
* item.first - weight of item
 * item.second - value of item
int zeroOneKnapsack(const vii &items, int maxWeight) {
        vector<vi> memo(items.size(),vi(maxWeight + 1,0));
        for(int i = 0; i < (int)items.size(); i++ )</pre>
                 for(int j = 0; j <= maxWeight; j++) {</pre>
                         if(i == 0){
                                  memo[i][j] = j >= items[0].first ? items[0].second : 0;
                         } else {
                                  memo[i][j] = memo[i - 1][j];
                                 if(j >= items[i].first) {
    memo[i][j] = max(memo[i][j],
                                                   memo[i - 1][j - items[i].first] + items[i].second);
```

```
return memo[(int)items.size() - 1][maxWeight];
```

2.4 Coin Change

```
#include <vector>
using namespace std;
typedef pair<int,int> ii;
typedef vector<int> vi;
 * returns minimum coins
int coinChangeV1(const vi &denoms, int total) {
       return memo[total];
 * returns number of ways to give change
int coinChangeV2(const vi &denoms, int total) {
       vector<vi> memo(denoms.size(), vi(total + 1,0));
for(int i = 0; i < (int)denoms.size(); i++) {</pre>
               for (int j = 0; j <= total; j++) {
    if (i == 0) {</pre>
                                memo[i][j] = j % denoms[0] ? 1 : 0;
                        } else {
                                memo[i][j] = 0;
                                int count = 0;
                                while(j - count * denoms[i] >= 0) {
                                        memo[i][j] += memo[i - 1][j - count * denoms[i]];
                                        count++;
        return memo[(int)denoms.size() - 1][total];
```

2.5 Traveling Salesman Problem

```
#include <vector>
using namespace std;
typedef vector<int> vi;
int n; // number of nodes
int start; //start node
vector < vi > memo(n, vi(1 << n, -1));
vector<vi> dists; // 2D distance matrix
int tsp(int pos, int mask) {
       if(mask == (1 << n) - 1) {
               return dists[pos][start];
        } else if(memo[pos][mask] != -1) {
               return memo[pos][mask];
        else
                int &res = memo[pos][mask];
                for(int i = 0; i < n; i++) {
                        if((mask & (1 << i)) == 0) {
                                res = min(res, dists[pos][i] + tsp(i, mask | (1 << i)));
                return res;
```

3 Graphs

3.1 Depth First Search

```
#include <vector>
#include <utility>
using namespace std;
#define UNVISITED 1
#define VISITED 2
typedef pair<int, int> ii;
typedef vector<int> vi;
typedef vector<ii> vii;
vector<vii>> adiList:
vi dfs_num;
void dfs(int u) {
        dfs_num[u] = VISITED;
        for(int i = 0; i < (int)adjList[u].size(); i++) {</pre>
                ii v = adjList[u][i];
                if(dfs_num[v.first] == UNVISITED) {
                       dfs(v.first);
```

3.2 Breadth First Search

```
#include <vector>
#include <utility>
#include <queue>
#include <bitset>
using namespace std;
#define MAX N 1000
typedef pair<int, int> ii:
typedef vector<int> vi;
typedef vector<ii> vii;
vector<vii> adjList;
void bfs(int s) {
       bitset<MAX_N> visited;
       queue<int> q;
       q.push(s);
       visited.set(s):
       while(!q.empty()) {
             if(!visited.test(v.first)) {
                            visited.set(v.first);
                            q.push(v.first);
```

3.3 Connected Components

```
#include <vector>
#include <utility>
using namespace std;
#define UNVISITED 1
#define VISITED 2
typedef pair<int, int> ii;
typedef vector<int> vi;
typedef vector<ii> vii;
```

3.4 Flood Fill

```
#include <vector>
#include <utility>
#include <queue>
using namespace std:
#define MAX R 1000
#define MAX_C 1000
typedef pair<int, int> ii;
typedef vector<int> vi;
typedef vector<ii> vii;
int grid[MAX_R][MAX_C];
int dr[] = {-1,-1,-1,0,0,1,1,1};
int dc[] = {-1,0,1,-1,1,-1,0,1};
int iterativeFloodFill(int r, int c, int v1, int v2){
        if(r >= 0 \&\& r < MAX_R \&\& c >= 0 \&\& c < MAX_C \&\& grid[r][c] == v1) {
                 queue<int> q;
                 q.push(r * MAX_C + c);
                 int area = 0;
                 while(!q.empty()) {
                         int u = q.front(); q.pop();
int inR = u / MAX_C;
                          int inC = u % MAX_C;
                          grid[inR][inC] = v2;
                          for (int i = 0; i < 4; i++) {
                                  int nr = inR + dr[i];
                                  int nc = inC + dc[i];
                                  if(nr >= 0 \&\& nr < MAX_R \&\& nc >= 0 \&\& nc < MAX_C \&\&
                                           grid[nr][nc] == v1) {
                                           q.push(nr * MAX_C + nc);
                 return area;
        return 0;
int recursiveFloodFill(int r, int c, int v1, int v2) {
         if(r >= 0 && r < MAX_R && c >= 0 && c < MAX_C && grid[r][c] == v1) {
                 grid[r][c] = v2;
                 int area = 1;
                 for(int i = 0; i < 4; i++) {
                          int nr = r + dr[i];
                          int nc = c + dc[i];
                          area += recursiveFloodFill(nr,nc,v1,v2);
                 return area;
        else
                 return 0;
```

3.5 Bipartite Graph Check

```
#include <vector>
#include <utility>
#include <queue>
#include <bitset>
using namespace std;
#define MAX N 1000
#define NO_COLOR -1
typedef pair<int.int> ii:
typedef vector<int> vi;
typedef vector<ii> vii;
vector<vii> adjList;
bool isBipartite(int s) {
        queue<int> q;
        q.push(s);
        vi color(V,NO_COLOR);
        color[s] = 0;
        bool isBipartite = true:
        while(!q.empty() && isBipartite) {
   int u = q.front(); q.pop();
   for(int i = 0; i < (int)adjList[u].size(); i++) {</pre>
                           ii v = adjList[u][i];
                           if(color[v.first] == NO_COLOR) {
                                   color[v.first] = 1 - color[u];
                                    q.push(v.first);
                           } else if(color[v.first] == color[u]) {
                                   isBipartite = false;
        return isBipartite;
```

3.6 Edge Property Check

```
#include <cstdio>
#include <vector>
#include <utility>
using namespace std:
#define UNVISITED 1
#define VISITED 2
#define EXPLORED 3
typedef pair<int, int> ii;
typedef vector<int> vi;
typedef vector<ii> vii;
vector<vii> adjList;
vi dfs_parent;
vi dfs_num;
void dfs(int u) {
        dfs_num[u] = VISITED;
        for(int i = 0; i < (int)adjList[u].size(); i++) {</pre>
                ii v = adjList[u][i];
if(dfs_num[v.first] == UNVISITED) {
                        printf("Edge (%d,%d): Tree Edge\n",u,v.first);
                         dfs_parent[v.first] = u;
                         dfs(v.first);
                } else if(dfs_num[v.first] == VISITED) {
                         if(v.first == dfs_parent[u]) {
                                 printf("Edge (%d,%d): Two-Way Edge\n",u,v.first);
                         } else
                                 printf("Edge (%d,%d): Back Edge\n",u,v.first);
                } else
                         printf("Edge (%d,%d): Forward/Cross Edge\n",u,v.first);
        dfs_num[u] = EXPLORED;
```

3.7 Finding Articulation Points And Bridges

```
#include <vector>
#include <utility>
#include <bitset>
using namespace std:
#define MAX_N 1000
typedef pair<int, int> ii;
typedef vector<int> vi;
typedef vector<ii> vii;
vector<vii> adjList;
vi dfs_num, dfs_low, dfs_parent,
bitset<MAX_N> isArticulationPoint;
int dfsCtr = 0, V, children, dfsRoot;
void dfs(int u,vii &bridges) {
        dfs_num[u] = dfs_low[u] = dfsCtr++;
for(int i = 0; i < (int)adjList[u].size(); i++) {</pre>
                 ii v = adjList[u][i];
                 if(dfs_num[v.first] == -1) {
                          dfs_parent[v.first] = u;
                          dfs(v.first,bridges);
                          if(u == dfsRoot) {
                                   children++;
                          dfs_low[u] = min(dfs_low[u],dfs_low[v.first]);
                          if(dfs_num[u] <= dfs_low[v.first]) {</pre>
                                   isArticulationPoint.set(u):
                          if(dfs_num[u] < dfs_low[v.first]) {</pre>
                                   bridges.push_back(ii(u,v.first));
                 } else if(v.first != dfs_parent[u]) {
                          dfs_low[u] = min(dfs_low[u],dfs_num[v.first]);
pair<vi,vii> findArticulationPointsAndBridges() {
         vii bridges;
        isArticulationPoint.reset();
        dfs_num.assign(V,-1);
        dfs_low.assign(V,-1);
        dfs_parent.assign(V,-1);
for(int i = 0; i < V; i++)</pre>
                 if(dfs_num[i] == -1) {
                          children = 0;
                          dfsRoot = i;
                          dfs(i,bridges);
                          if(children > 1) {
                                   isArticulationPoint.set(i);
                          } else {
                                   isArticulationPoint.reset(i);
        vi artPoints;
        for(int i = 0; i < V; i++) {
    if(isArticulationPoint.test(i)) {</pre>
                          artPoints.push_back(i);
        return pair<vi, vii>(artPoints, bridges);
```

3.8 Finding Strongly Connected Components

```
#include <vector>
#include <vtility>
#include <bitset>
#include <stack>

using namespace std;
#define MAX_N 1000

typedef pair<int,int> ii;
typedef vector<int> vi;
```

```
typedef vector<ii> vii;
vector<vii> adjList;
vi dfs_num, dfs_low;
bitset<MAX_N> visited;
int dfsCtr = 0, V, scc;
void tarjan(int u, stack<int> &s) {
          // printf("Tarjan(%d)\n",u);
         dfs_num[u] = dfs_low[u] = dfsCtr++;
         s.push(u);
         visited.set(u);
         for(int i = 0; i < (int)adjList[u].size(); i++) {
    ii v = adjList[u][i];
    if(dfs_num[v.first] == -1) {</pre>
                             tarjan(v.first,s);
                   if(visited.test(u)) {
                             dfs_low[u] = min(dfs_low[u],dfs_low[v.first]);
         if(dfs_low[u] == dfs_num[u]) {
    printf("SCC #%d:",++scc);
                   while(s.top() != u) {
                             int temp = s.top();
                                                           s.pop();
                             printf(" %d",temp);
                   printf(" %d\n",s.top());
                   s.pop();
int printAndCountSCCs() {
         visited.reset();
         stack<int> s;
         dfs_num.assign(V,-1);
         dfs_low.assign(V,-1);
         for(int i = 0; i < V; i++) {
    // printf("dfs_num[%d] = %d\n",i,dfs_num[i]);
    if(dfs_num[i] == -1) {</pre>
                             tarjan(i,s);
         return scc;
```

3.9 Minimum Spanning Tree Using Kruskal's Algorithm

```
#include <vector>
#include <utility>
#include <algorithm>
using namespace std;
typedef pair<int, int> ii;
typedef vector<int> vi;
typedef vector<ii> vii;
typedef pair<int, ii> iii;
class UnionFind {
        public:
        vi p, rank;
        UnionFind(int n) {
                 p.assign(n,0);
                 rank.assign(n,0);
for(int i = 0; i < n; i++) { p[i] = i; }</pre>
        void unionSet(int i, int j) {
                 if(!isSameSet(i, j)) {
                         int x = findSet(i), y = findSet(j);
                         if(rank[x] > rank[y]) {
                                 p[y] = x;
                                  if(rank[x] == rank[y]) { rank[y]++; }
        int findSet(int i) {
                 if(p[i] != i) {
                         p[i] = findSet(p[i]);
                 return p[i];
```

3.10 Minimum Spanning Tree Using Prim's Algorithm

```
#include <vector>
#include <utility>
#include <queue>
#include <bitset>
using namespace std;
typedef pair<int, int> ii;
typedef vector<int> vi;
typedef vector<ii> vii;
#define MAX_N 1000
vector<vii> adjList;
int primsMST() {
        bitset<MAX_N> taken;
        priority_queue<ii>> q;
        q.push(ii(0,0));
        int mst = 0;
        while(!q.empty()) {
                ii cur = q.top(); q.pop();
                int u = -cur.second, w = -cur.first;
                if(!taken.test(u)) {
                        taken.set(u);
                        for(int i = 0; i < (int)adjList[u].size(); i++) {</pre>
                                ii v = adjList[u][i];
                                if(!taken.test(v.first)) {
                                        q.push(ii(-v.second,-v.first));
                        mst += w:
        return mst;
```

3.11 Single Source Shortest Path using Dijkstra's Algorithm

```
#include <vector>
#include <utility>
#include <queue>

using namespace std;

typedef pair<int, int> ii;
typedef vector<int> vi;
typedef vector<ii> vii;
#define INF 1000000000
int V;
```

3.12 All Pairs Shortest Path using Floyd Warshall's Algorithm

3.13 Max Flow with Edmonds Karp Algorithm

```
#include <vector>
#include <bitset>
#include <queue>
using namespace std;
#define MAX N 1000
#define INF 1000000000
typedef vector<int> vi;
        Edge(int _u, int _v, int _cap) : u(_u), v(_v), cap(_cap), rem(_cap) {}
};
int V, f, s, t;
vi p;
vector<vector<Edge *> > adjList;
Edge *res[MAX_N][MAX_N];
void augment(int v, int minEdge) {
        // printf("augmenting %d\n",v);
        if(v == s) {
               f = minEdge;
        } else if(p[v] != -1) {
                augment(p[v],min(minEdge,res[p[v]][v]->rem));
                res[p[v]][v]->rem -= f;
                res[v][p[v]]->rem += f;
int edmondsKarp(int source, int sink) {
       int mf = 0;
        s = source;
        t = sink;
```

```
while(true) {
                f = 0;
                bitset<MAX_N> visited;
                queue<int> q;
                q.push(s);
                p.assign(V,-1);
                 visited.set(s);
                while(!q.empty()) {
                         int u = q.front(); q.pop();
                         // printf("exploring %d\n",u);
                        if(u == t) {
                                 break;
                        } else {
                                 for(int i = 0; i < (int)adjList[u].size(); i++) {</pre>
                                         Edge *e = adjList[u][i];
if(e->rem > 0 && !visited.test(e->v)){
                                                 p[e->v] = u;
                                                 visited.set(e->v);
                                                 q.push(e->v);
                 augment (t, INF);
                if( f == 0) {
                        break:
                mf += f;
        return mf;
typedef pair<int, int> ii;
typedef pair<int,ii> iii;
int main() {
        adjList.assign(V, vector<Edge*>());
         * This is a sample graph.
        vector<iii> edges;
        edges.push_back(iii(0,ii(1,10)));
        edges.push_back(iii(0,ii(4,10)));
        edges.push_back(iii(1,ii(2,20)));
        edges.push_back(iii(2,ii(3,10)));
        edges.push_back(iii(4,ii(1,10)));
        edges.push_back(iii(2,ii(5,5)));
        edges.push_back(iii(3,ii(6,10)));
        edges.push_back(iii(5,ii(6,10)));
        for(int i = 0; i < (int)edges.size(); i++) {</pre>
                 * This is how to add an edge.
                iii cur = edges[i];
                Edge *e = new Edge(cur.first,cur.second.first,cur.second.second);
                Edge *eRev = new Edge(cur.second.first,cur.first,0);
                adjList[cur.first].push_back(e);
                adjList[cur.second.first].push_back(eRev);
                res[cur.first][cur.second.first] = e;
                res[cur.second.first][cur.first] = eRev;
        printf("maxflow: %d\n",edmondsKarp(0,6));
        return 0;
```

3.14 Max Flow with Dinic's Algorithm

```
#include <vector>
#include <bitset>
#include <gueue>

using namespace std;

#define MAX_N 1000
#define INF 1000000000

typedef vector<int> vi;

class Edge {
    public:
        int u, v, cap, rem;
        Edge(int _u, int _v, int _cap) : u(_u), v(_v), cap(_cap), rem(_cap) {}
};
```

```
int V, f, s, t;
vi p;
vector<vector<Edge *> > adjList;
Edge *res[MAX_N][MAX_N];
void augment(int v, int minEdge) {
        // printf("augmenting %d\n",v);
        if(v == s) {
               f = minEdge;
        } else if(p[v] != -1) {
                 augment(p[v],min(minEdge,res[p[v]][v]->rem));
                res[p[v]][v]->rem -= f;
res[v][p[v]]->rem += f;
int dinicsMaxFlow(int source, int sink) {
        int mf = 0;
        s = source;
        t = sink;
        bool hasFlow = true:
        while(hasFlow) {
                vi dist(V, INF);
                 queue<int> q;
                 q.push(s);
dist[s] = 0;
                 while(!q.empty()) {
                         int u = q.front(); q.pop();
// printf("exploring %d\n",u);
                         if(u == t) {
                                 break;
                          } else {
                                  for(int i = 0; i < (int)adjList[u].size(); i++) {</pre>
                                          Edge *e = adjList[u][i];
                                          if(e->rem > 0 && dist[e->v] == INF) {
                                                  dist[e->v] = dist[u] + 1;
                                                   q.push(e->v);
                 hasFlow = false;
                 while(true) {
                         bitset<MAX_N> visited;
                         q = queue<int>();
                         q.push(s);
                         p.assign(V,-1);
                          visited.set(s);
                         while(!q.empty()) {
                                  int u = q.front(); q.pop();
                                  if(u == t) {
                                          break:
                                  else
                                          for(int i = 0; i < (int)adjList[u].size(); i++) {</pre>
                                                   Edge *e = adjList[u][i];
                                                   if(e->rem > 0 && !visited.test(e->v) && dist[e->v] ==
                                                         dist[u] + 1) {
                                                           p[e->v] = u;
                                                            visited.set(e->v);
                                                           q.push(e->v);
                          augment(t, INF);
                         if( f == 0) {
                                  break:
                         mf += f;
                         hasFlow = true;
        return mf;
typedef pair<int,int> ii;
typedef pair<int, ii> iii;
int main() {
        adjList.assign(V, vector<Edge*>());
         * This is a sample graph.
        vector<iii> edges;
        edges.push_back(iii(0,ii(1,10)));
        edges.push_back(iii(0,ii(4,10)));
        edges.push_back(iii(1,ii(2,20)));
        edges.push_back(iii(2,ii(3,10)));
```

4 Combinatorics

4.1 Combinatorics

```
public class Combinatorics {
        static int[] fibo(int n)
                int[] f = new int[n];
                f[0] = f[1] = 1;
                for(int i=2; i<n; i++) f[i] = f[i-1]+f[i-2];
                return f:
        // alternatively:
        // nCk = n!/(k!*(n-k)!)
        // nPk = n!/(n-k)!
        // add a memo table if needed to reduce overlaps
        static int binomialCoefficient(int n, int k) {
                if(n==k || k==0) return 1;
                return binomialCoefficient (n-1, k-1) +binomialCoefficient (n-1, k);
        static int[] catalan(int n) {
                int[] cat = new int[n];
                for(int i=1; i<n; i++) cat[i] = ((2*i*(2*i-1)) / ((i+1)*i))*cat[i-1];</pre>
                return cat;
```

5 Number Theory

5.1 NumberTheory

```
import java.util.*;
public class NumberTheory {
        static BitSet sieve; // used for generating primes
        static ArrayList<Integer> primes; // change to long if necessary
        static int[] nDiffPF; // for modified sieve
        static int bound; // array cap, usually 10 7
        static int[] e; // for modified sieve euler phi
        static void generatePrimes() {
                sieve.set(2, bound);
                for(int i=2; i<bound; i++)</pre>
                        if(sieve.get(i)) {
                                 primes.add(i);
                                 for(int j=i+i; i<bound; j+=i) sieve.set(j, false);</pre>
        static boolean isPrime(int n) {
                if(n<bound) return sieve.get(n);</pre>
                for(int i=0; i<primes.size(); i++)</pre>
                         if(n%primes.get(i)==0) return false;
                return true;
```

```
// assumption: a>=b
static int gcd(int a, int b) {
        return b==0 ? a : gcd(b, a%b);
// alternative: get max of powers across all prime factors of a and b
static int lcm(int a, int b) {
        return a*(b/gcd(a, b));
// returns map of format <factor, power>
// convert to TreeMap if you need order
// easy to tweak to count all PF, count distinct PF, sum PF, num Div static HashMap<Integer, Integer> getPrimeFactors(int n) {
         HashMap<Integer, Integer> factors = new HashMap<>();
         int pIndex = 0, p = primes.get(pIndex);
         while (p*p<=n) {
                 while (n%p==0) {
                          factors.put(p, factors.containsKey(p) ? factors.get(p)+1 : 1);
                 p = factors.get(++pIndex);
         if(n!=1) factors.put(n, factors.containsKey(n) ? factors.get(n)+1 : 1);
         return factors:
static int eulerPhi(int n) {
        int pIndex = 0, p = primes.get(pIndex), ans = n;
         while (p*p<=n) {
                 if(n%p==0) ans-=ans/p;
                 while (n%p==0) n/=p;
                 p = primes.get(++pIndex);
         if(n!=1) ans-=ans/n;
         return ans;
// more efficient way to count num of different PF of many numbers
static void modifiedSieve() {
        nDiffPF = new int[bound];
for(int i=2; i<bound; i++)</pre>
                 if(nDiffPF[i]==0) for(int j=i; j<bound; j+=i) nDiffPF[j]++;</pre>
static void modifiedEulerPhi() {
         e = new int[bound];
         for(int i=1; i<bound; i++) e[i] = i;</pre>
         for(int i=2; i<bound; i++)</pre>
                 if(e[i]==i) for(int j=i; j<bound; j+=i) e[j] = (e[j]/i)*(i-1);
```

6 Miscellaneous Mathematics

- 7 String Processing
- 8 Computational Geometry
- 8.1 One Dimensional Objects

```
#include <cmath>

class Point{
    public:
        double x, y;
        Point() { x = y = 0; }
        Point (double _x, double _y) : x(_x), y(_y) {}

        bool operator<(const Point &p) const {
            if(fabs(x - p.x) > 1e-10) {
                 return x < p.x;
            } else {
                 return y < p.y;
            }
        }
}</pre>
```

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```
bool operator==(const Point &p) const {
                return (fabs(x - p.x) < 1e-10 && fabs(y - p.y) < 1e-10);
         * theta in radians
        Point rotate(double theta) {
                return Point(cos(theta) * x - sin(theta) * y,
                                                sin(theta) * x + cos(theta) * y);
        double dist(const Point &p) const {
                return hypot(x - p.x, y - p.y);
};
        public:
        double a, b, c;
        Line(Point from, Point to) {
                if(fabs(from.x - to.x) < 1e-10) {
                        a = 1:
                        b = 0;
                        c = -from.x:
                else (
                        a = (to.y - from.y) / (to.x - from.x);
                        b = 1;
                        c = -(a * from.x) - from.y;
        bool areParallel(const Line &12) const {
                return (fabs(a - 12.a) < 1e-10 && fabs(b - 12.b) < 1e-10);
        bool areSame(const Line &12) const {
                return areParallel(12) && fabs(c - 12.c) < 1e-10;
        bool areIntersect(const Line &12, Point &p) {
                if(areParallel(12)) {
                        return false;
                p.x = (12.b * c - b * 12.c) / (12.a * b - a * 12.b);
                if(fabs(b) > 1e-10) {
                p.y = -(a * p.x + c);
} else {
                        p.y = -(12.a * p.x + 12.c);
                return true:
1:
class Vector (
        public:
        double x, v;
        Vector(double _x, double _y) : x(_x), y(_y) {}
        Vector (Point src, Point dest) {
                x = dest.x - src.x;
                y = dest.y - src.y;
        Vector scale (double c) {
                return Vector(x * c, y * c);
        Point translate(Point p) {
                return Point(p.x + x,p.y + y);
        double dot(const Vector &b) const {
                return x * b.x + y * b.y;
        double norm() const {
                return x * x + y * y;
};
* distance of point p from line AB
double distToLine(Point p, Point a, Point b, Point &c) {
       Vector ap = Vector(a,p), ab = Vector(a,b);
double u = ap.dot(ab) / ab.norm();
        ab.scale(u).translate(a);
        return p.dist(c);
```

8.2 Circles

```
#include <cmath>
 \star Checks if p is in circle with center c and radius r.
 * Returns 0 if inside, 1 if on border, and 2 if outside.
int insideCircle(Point p, Point c, double r) {
        double dx = p.x - c.x, dy = p.y - c.y;
double dist = hypot(dx,dy);
        return dist < r - 1e-10 ? 0 : (dist < r + 1e-10 ? 1 : 2);
double getPI() {
        return acos(-1.0);
 * returns area of circle with radius r
double circleArea(double r) {
        return getPI() * r * r;
* returns arc length of circle with radius r and vertex angle theta (in radians)
double arcLength(double r, double theta) {
        return theta * r;
 * returns chord length of circle with radius r and vertex angle theta (in radians)
double chordLength(double r, double theta) {
        return sqrt (2 * r * r * (1 - cos(theta)));
* returns area of sector of circle with radius r and vertex angle theta (in radians)
double sectorArea(double r, double theta) {
        return r * r * theta / 2;
 * returns area of segment of circle with radius r and vertex angle theta (in radians)
 * segment is section between chord and arc
double segmentArea(double r, double theta) {
        return sectorArea(r,theta) - r * cos(theta / 2.0) * r * sin(theta / 2.0);
\star given two points p1 and p2, find the center of circles, c, with radius r.
bool circle2PtsRad(Point p1, Point p2, double r, Point &c) {
        double d2 = (p1.x - p2.x) * (p1.x - p2.x) +
        (p1.y - p2.y) * (p1.y - p2.y);

double det = r * r / d2 - 0.25;
        if (det < 0.0) return false;</pre>
        double h = sqrt(det);
        c.x = (p1.x + p2.x) * 0.5 + (p1.y - p2.y) * h;
        c.y = (p1.y + p2.y) * 0.5 + (p2.x - p1.x) * h;
        return true:
```

8.3 Triangles

```
#include <cmath>
#include "OneDim.cpp"

/**
    * returns area of triangle with base b and height h.
    */
double area(double b, double h) {
        return b * h * 0.5;
}

/**
    * returns perimeter of triangle with sides a, b, and c.
    */
double perimeter(double a, double b, double c) {
```

```
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```

```
return a + b + c;
}

/**

* returns semiperimeter of triangle with sides a, b, and c.

*/
double semiperimeter(double a, double b, double c) {
        return (a + b + c) / 2.0;
}

/**

* returns area of triangle with sides a, b, and c.

*/
double area(double a, double b, double c) {
        double s = semiperimeter(a,b,c);
        return sqrt(s * (s - a) * (s - b) * (s - c));
}

/**

* returns radius of incircle of triangle with sides a, b, and c.

*/
double incircleradius(double a, double b, double c) {
        return area(a,b,c) / semiperimeter(a,b,c);
}

/**

* returns radius of incircle of triangle with sides a, b, and c.

*/
double incircleradius of incircle of triangle with sides a, b, and c.

*/
double rinCircle(Point pl, Point p2, Point p3) {
        return incircleradius(p1.dist(p2),p2.dist(p3),p3.dist(p1));
}

// assumption: the required points/lines functions have been written
// returns 1 if there is an incircle center, returns 0 otherwise
```

```
// if this function returns 1, ctr will be the inCircle center
// and r is the same as rInCircle
int inCircle(Point p1, Point p2, Point p3, Point &ctr, double &r) {
        r = rInCircle(p1, p2, p3);
        if (fabs(r) < 1e-10)
                return 0; // no inCircle center
         double ratio = p1.dist(p2) / p1.dist(p3);
         Vector p2p3(p2, p3);
         Point p = p2p3.scale(ratio / (1 + ratio)).translate(p2);
         Line 11(p1,p);
         ratio = p2.dist(p1) / p2.dist(p3);
         Vector p1p3(p2, p3);
         p = plp3.scale(ratio / (1 + ratio)).translate(pl);
        Line 12(p2, p);
11.areIntersect(12, ctr); // get their intersection point
         return 1;
 \star returns radius of circumcircle of triangle with sides a, b, and c.
double circumcircleradius(double a, double b, double c) {
         return a * b * c / 4 * area(a,b,c);
 * returns radius of incircle of triangle with sides a, b, and c.
double rCircumCircle(Point p1, Point p2, Point p3) {
    return circumcircleradius(p1.dist(p2),p2.dist(p3),p3.dist(p1));
```