De La Salle ICPC Team Notebook (2018-19)

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1 Advanced Data Structures Without Libraries

1.1 Union Find Disjoint Set

#include <vector>

1.2 Segment Tree

```
#include <vector>
using namespace std;
typedef vector<int> vi;
* Segment tree for Range Maximum Queries
class SegmentTree {
         public:
         vi st, A;
         SegmentTree(const vi &_A) {
                 A = _A;
                  n = (int)A.size();
                  st.assign(4 * n, 0);
                  build(1, 0, n - 1);
        int left(int p) { return 1 << p; }
int right(int p) { return (1 << p) + 1; }</pre>
         void build(int p, int 1, int r) {
                 if(1 == r) {
                          st[p] = 1;
                  } else {
                           int m = 1 + (r - 1) / 2;
                           build(left(p),1,m);
                           build(right(p),m + 1,r);
                           int 1 = st[left(p)];
                           int r = st[right(p)];
                           st[p] = A[1] >= A[r] ? 1 : r;
         int rmq(int i, int j) {
                  return rmq(1,0,n-1,i,j);
         int rmq(int p, int 1, int r, int i, int j) {
   if(1 > j | | r < i) { return -1; }</pre>
                  else if(1 >= i && r <= j) { return st[p]; }</pre>
                           int m = 1 + (r - 1) / 2;
                           int s1 = rmq(left(p), l, m, i, j);
                           int s2 = rmq(right(p), m + 1, r, i, j);
                           if(s1 == -1) {return s2;}
                           else if(s2 == -1) {return s1;}
else {return A[1] >= A[r] ? 1 : r; }
         void pointUpdate(int i, int val) {
                  pointUpdate(1,0,n-1,i,val);
         void pointUpdate(int p, int 1, int r,int i, int val) {
                  if(1 == r) {
                           A[i] = val;
                           int m = 1 + (r - 1) / 2;
                           if(i >= 1 && i <= m) {
                                    pointUpdate(left(p),1,m,i,val);
                                    pointUpdate(right(p),m + 1,r,i,val);
                           int 1 = st[left(p)];
int r = st[right(p)];
                           st[p] = A[1] >= A[r] ? 1 : r;
```

1.3 Fenwick Tree/Binary Indexed Tree

```
#include <vector>
using namespace std;
typedef vector<int> vi;
class FenwickTree (
        public:
        vi ft;
        int n:
        FenwickTree(int n) {
                n = n:
                ft.assign(n + 1,0);
        void update(int index, int increment) {
                while(index <= n) {</pre>
                         ft[index] += increment;
                         index += (index & (-index));
        int rmq(int end) {
                int res = 0:
                while (end) {
                        res += ft[end];
                         end -= (end & (-end));
                return res;
        int rmq(int i, int j) {
                if(i > j) { return 0; }
                else if(i <= 0) { return rmq(j); }</pre>
                else {return rmq(j) - rmq(i - 1)}
};
```

2 Problem Solving Paradigms

2.1 Maximum 1D/2D Range Sum

```
#include <vector>
using namespace std;
typedef vector<int> vi;
int max1DRangeSum(const vi &arr) {
        int ans = 0;
        int cur = 0;
        for(int i = 0; i < (int)arr.size(); i++) {</pre>
                 cur += arr[i];
                 if(cur < 0) cur = 0;
                 ans = max(ans,cur);
        return ans;
int max2DRangeSum(const vector<vi> &arr) {
        vi rowSums(arr.size(),0);
        for(int i = 0; i < (int)arr.size(); i++) {</pre>
                 for(int j = 0; j < (int)arr[i].size(); j++) {
    rowSums[i] += arr[i][j];</pre>
        int ans = 0;
        for(int leftCol = 0; leftCol < (int)arr[0].size(); leftCol++) {</pre>
                 for(int rightCol = leftCol; rightCol < (int)arr[0].size(); rightCol++) {</pre>
                          vi arr2(arr.size(),0);
                          for(int i = 0; i < (int)arr.size(); i++) {</pre>
                                  arr2[i] = leftCol == 0 ? rowSums[rightCol] :
                                                                              (rowSums[rightCol] - rowSums[
                                                                                    leftCol = 11):
                          int temp = max1DRangeSum(arr2);
                          ans = max(ans,temp);
```

return ans;

2.2 Longest Increasing Subsequence

```
#include <algorithm>
#include <vector>
using namespace std;
typedef vector<int> vi;
int lisSlow(const vi &arr) {
        vi memo(arr.size(),1);
        int ans = 1;
for(int i = 1; i < (int)arr.size(); i++) {</pre>
                 for(int j = 0; j < i; j++) {
    if(arr[i] > arr[j]) {
                                   memo[i] = max(memo[i], memo[j] + 1);
                  ans = max(ans.memo[i]);
        return ans:
int lisNLogN(const vi &arr) {
        for(int i = 0; i < (int)arr.size(); i++) {</pre>
                  vi::iterator itr = lower_bound(memo.begin(),memo.end(),arr[i]);
                  if(itr == memo.end()) {
                          memo.push_back(arr[i]);
                  } else {
                          *itr = arr[i];
        return (int) memo.size();
```

$2.3 \quad 0/1 \text{ Knapsack}$

```
#include <vector>
using namespace std;
typedef pair<int, int> ii;
typedef vector<int> vi;
typedef vector<ii> vii;
* item.first - weight of item
 * item.second - value of item
int zeroOneKnapsack(const vii &items, int maxWeight) {
        vector<vi> memo(items.size(),vi(maxWeight + 1,0));
        for(int i = 0; i < (int)items.size(); i++ )</pre>
                for(int j = 0; j <= maxWeight; j++) {</pre>
                        if(i == 0) {
                                 memo[i][j] = j \ge items[0].first ? items[0].second : 0;
                        } else {
                                 memo[i][j] = memo[i - 1][j];
                                if(j >= items[i].first) {
                                         memo[i][j] = max(memo[i][j],
                                                 memo[i - 1][j - items[i].first] + items[i].second);
        return memo[(int)items.size() - 1][maxWeight];
```

2.4 Coin Change

```
#include <vector>
using namespace std;
```

```
typedef pair<int,int> ii;
typedef vector<int> vi;
* returns minimum coins
int coinChangeV1(const vi &denoms, int total) {
        vi memo(total + 1,1 << 29);</pre>
        memo[0] = 0;
for(int i = 1; i <= total; i++) {
                for (int j = 0; j < (int) denoms.size(); j++) {</pre>
                         if(i - denoms[j] >= 0) {
                                  memo[i] = min(memo[i], memo[i - denoms[j]] + 1);
        return memo[total];
 * returns number of ways to give change
int coinChangeV2(const vi &denoms, int total) {
        vector < vi > memo(denoms.size(), vi(total + 1,0));
        for(int i = 0; i < (int)denoms.size(); i++) {</pre>
                for(int j = 0; j <= total; j++) {
    if(i == 0) {</pre>
                                 memo[i][j] = j % denoms[0] ? 1 : 0;
                          } else {
                                  memo[i][j] = 0;
                                  int count = 0;
                                  while(j - count * denoms[i] >= 0) {
                                           memo[i][j] += memo[i - 1][j - count * denoms[i]];
                                           count++;
        return memo[(int)denoms.size() - 1][total];
```

2.5 Traveling Salesman Problem

```
#include <vector>
using namespace std;
typedef vector<int> vi;
int n; // number of nodes
int start; //start node
vector < vi > memo(n, vi(1 << n, -1));
vector<vi> dists; // 2D distance matrix
int tsp(int pos, int mask) {
        if (mask == (1 << n) - 1) {
                return dists[pos][start];
        } else if(memo[pos][mask] != -1) {
                return memo[pos][mask];
                int &res = memo[pos][mask];
                for(int i = 0; i < n; i++) {
                        if((mask & (1 << i)) == 0) {
                                res = min(res, dists[pos][i] + tsp(i, mask | (1 << i)));
                return res:
```

3 Graphs

3.1 Depth First Search

```
#include <vector>
#include <utility>
using namespace std;
```

3.2 Breadth First Search

```
#include <vector>
#include <utility>
#include <queue>
#include <bitset>
using namespace std;
#define MAX_N 1000
typedef pair<int, int> ii;
typedef vector<int> vi;
typedef vector<ii> vii;
vector<vii> adjList;
void bfs(int s) {
       bitset<MAX_N> visited;
        queue<int> q;
        q.push(s);
        visited.set(s);
        while(!q.empty()) {
                int u = q.front(); q.pop();
                for(int i = 0; i < (int)adjList[u].size(); i++) {</pre>
                        ii v = adjList[u][i];
                        if(!visited.test(v.first)) {
                                visited.set(v.first);
                                q.push(v.first);
```

3.3 Connected Components

```
#include <vector>
#include <utility>
using namespace std;
#define UNVISITED 1
#define VISITED 2
typedef pair<int, int> ii;
typedef vector<int> vi;
typedef vector<ii> vii;
vector<vii> adjList;
vi dfs_num;
int V;
void dfs(int u) {
        dfs_num[u] = VISITED;
        for(int i = 0; i < (int)adjList[u].size(); i++) {</pre>
                ii v = adjList[u][i];
                if(dfs_num[v.first] == UNVISITED) {
                        dfs(v.first);
```

3.4 Flood Fill

```
#include <vector>
#include <utility>
#include <queue>
using namespace std;
#define MAX_R 1000
#define MAX_C 1000
typedef pair<int, int> ii;
typedef vector<int> vi;
typedef vector<ii> vii;
int grid[MAX_R][MAX_C];
int dr[] = \{-1, -1, -1, 0, 0, 1, 1, 1\};
int dc[] = \{-1, 0, 1, -1, 1, -1, 0, 1\};
int iterativeFloodFill(int r, int c, int v1, int v2){
        if(r >= 0 \&\& r < MAX_R \&\& c >= 0 \&\& c < MAX_C \&\& grid[r][c] == v1) {
                 queue<int> q;
                 q.push(r * MAX_C + c);
                 int area = 0;
                 while(!q.empty()) {
                         int u = q.front(); q.pop();
int inR = u / MAX_C;
int inC = u % MAX_C;
                          grid[inR][inC] = v2;
                          area++:
                          for(int i = 0; i < 4; i++) {
                                  int nr = inR + dr[i];
                                  int nc = inC + dc[i];
                                  if (nr >= 0 && nr < MAX_R && nc >= 0 && nc < MAX_C &&
                                          grid[nr][nc] == v1) {
                                           q.push(nr * MAX_C + nc);
                 return area;
        return 0;
int recursiveFloodFill(int r, int c, int v1, int v2) {
        if(r >= 0 && r < MAX_R && c >= 0 && c < MAX_C && grid[r][c] == v1) {</pre>
                 grid[r][c] = v2;
                 int area = 1;
                 for(int i = 0; i < 4; i++) {
                         int nr = r + dr[i];
                         int nc = c + dc[i];
                          area += recursiveFloodFill(nr,nc,v1,v2);
                 return area:
        else
                 return 0:
```

3.5 Bipartite Graph Check

```
#include <vector>
#include <queue>
#include <queue>
#include <br/>
#include
```

```
typedef vector<int> vi;
typedef vector<ii> vii;
vector<vii> adjList;
bool isBipartite(int s) {
         queue<int> q;
         q.push(s);
         vi color(V, NO_COLOR);
         color[s] = 0;
         bool isBipartite = true;
         while(!q.empty() && isBipartite) {
                  int u = q.front(); q.pop();
for(int i = 0; i < (int)adjList[u].size(); i++) {
    ii v = adjList[u][i];</pre>
                           if(color[v.first] == NO_COLOR) {
                                    color[v.first] = 1 - color[u];
                                     q.push(v.first);
                            } else if(color[v.first] == color[u]) {
                                    isBipartite = false;
         return isBipartite;
```

3.6 Edge Property Check

```
#include <cstdio>
#include <vector>
#include <utility>
using namespace std:
#define UNVISITED 1
#define VISITED 2
#define EXPLORED 3
typedef pair<int, int> ii;
typedef vector<int> vi;
typedef vector<ii> vii;
vector<vii> adjList;
vi dfs_parent;
vi dfs num;
void dfs(int u) {
        dfs num[u] = VISITED;
        for(int i = 0; i < (int)adjList[u].size(); i++) {</pre>
                ii v = adjList[u][i];
                if(dfs_num[v.first] == UNVISITED) {
                        printf("Edge (%d,%d): Tree Edge\n",u,v.first);
                        dfs_parent[v.first] = u;
                        dfs(v.first);
                } else if(dfs_num[v.first] == VISITED) {
                        if(v.first == dfs_parent[u]) {
                                printf("Edge (%d,%d): Two-Way Edge\n",u,v.first);
                                printf("Edge (%d,%d): Back Edge\n",u,v.first);
                else
                        printf("Edge (%d,%d): Forward/Cross Edge\n",u,v.first);
        dfs_num[u] = EXPLORED;
```

3.7 Finding Articulation Points And Bridges

```
#include <vector>
#include <tutility>
#include <bitset>
using namespace std;
#define MAX_N 1000

typedef pair<int,int> ii;
typedef vector<int> vi;
typedef vector<ii> vii;
vector<vii> adjList;
```

```
vi dfs_num, dfs_low, dfs_parent;
bitset<MAX_N> isArticulationPoint;
int dfsCtr = 0, V, children, dfsRoot;
void dfs(int u,vii &bridges) {
        dfs_num[u] = dfs_low[u] = dfsCtr++;
        for(int i = 0; i < (int)adjList[u].size(); i++) {</pre>
                ii v = adjList[u][i];
                if(dfs_num[v.first] == -1) {
                        dfs_parent[v.first] = u;
                         dfs(v.first,bridges);
                        if(u == dfsRoot) {
                                 children++;
                         dfs_low[u] = min(dfs_low[u],dfs_low[v.first]);
                         if(dfs_num[u] <= dfs_low[v.first]) {</pre>
                                 isArticulationPoint.set(u);
                         if(dfs_num[u] < dfs_low[v.first]) {</pre>
                                 bridges.push_back(ii(u,v.first));
                } else if(v.first != dfs_parent[u]) {
                         dfs_low[u] = min(dfs_low[u],dfs_num[v.first]);
pair<vi,vii> findArticulationPointsAndBridges() {
        vii bridges:
        isArticulationPoint.reset();
        dfs_num.assign(V,-1);
        dfs_low.assign(V,-1);
        dfs_parent.assign(V,-1);
        for (int i = 0; i < V; i++) {</pre>
                if(dfs_num[i] == -1) {
                         children = 0;
                        dfsRoot = i;
                        dfs(i,bridges);
                         if(children > 1) {
                                 isArticulationPoint.set(i);
                         } else {
                                 isArticulationPoint.reset(i);
        vi artPoints;
        for (int i = 0; i < V; i++) {
                if(isArticulationPoint.test(i)) {
                         artPoints.push_back(i);
        return pair<vi, vii>(artPoints, bridges);
```

3.8 Finding Strongly Connected Components

```
#include <vector>
#include <utility>
#include <bitset>
#include <stack>
using namespace std;
#define MAX N 1000
typedef pair<int, int> ii;
typedef vector<int> vi;
typedef vector<ii> vii;
vector<vii> adjList;
vi dfs_num, dfs_low;
bitset<MAX_N> visited;
int dfsCtr = 0, V, scc;
void tarjan(int u,stack<int> &s){
          // printf("Tarjan(%d)\n",u);
         dfs_num[u] = dfs_low[u] = dfsCtr++;
         s.push(u);
        for(int i = 0; i < (int) adjList[u].size(); i++) {
    ii v = adjList[u][i];
    if(dfs_num[v.first] == -1) {</pre>
                           tarjan(v.first,s);
```

```
if(visited.test(u)) {
                      dfs_low[u] = min(dfs_low[u], dfs_low[v.first]);
       if(dfs_low[u] == dfs_num[u]) {
              printf("SCC #%d:",++scc);
              while(s.top() != u) {
                     int temp = s.top();
printf(" %d",temp);
              printf(" %d\n",s.top());
              s.pop();
int printAndCountSCCs() {
       stack<int> s;
       dfs_num.assign(V,-1);
       dfs_low.assign(V,-1);
       if(dfs_num[i] == -1) {
                      tarjan(i,s);
       return scc:
```

3.9 Single Source Shortest Path using Dijkstra's Algorithm

```
#include <vector>
#include <utility>
#include <queue>
using namespace std;
typedef pair<int, int> ii;
typedef vector<int> vi;
typedef vector<ii> vii;
#define TNF 1000000000
int V:
vector<vii> adjList;
vi dijkstras(int s) {
        vi dist(V, INF);
        priority_queue<ii, vii, greater<ii>> q;
        q.push(s);
         dist[s] = 0;
        while(!q.empty()) {
                  ii u = q.top(); q.pop();
                  if(u.first > dist[u.second]) {
                          continue:
                  for(int i = 0; i < (int)adjList[u.second].size(); i++) {</pre>
                          ii v = adjList[u.second][i];
                          if(dist[v.first] > dist[u.second] + v.second) {
    dist[v.first] = dist[u.second] + v.second;
        return dist;
```

3.10 All Pairs Shortest Path using Floyd Warshall's Algorithm

```
#include <vector>
using namespace std;
typedef vector<int> vi;
#define INF 1000000000
int V;
vector<vi> adjMat;
vector<vi> dijkstras(int s) {
```

3.11 Max Flow with Edmonds Karp Algorithm

#include <vector>

```
#include <bitset>
#include <queue>
using namespace std;
#define MAX_N 1000
#define INF 1000000000
typedef vector<int> vi;
class Edge {
        public:
        int u, v, cap, rem;
        Edge(int _u, int _v, int _cap) : u(_u), v(_v), cap(_cap), rem(_cap) {}
};
int V, f, s, t;
vi p;
vector<vector<Edge *> > adjList;
Edge *res[MAX_N][MAX_N];
void augment(int v, int minEdge) {
         // printf("augmenting %d\n",v);
        if(v == s) {
                f = minEdge:
        } else if(p[v] != -1) {
                augment(p[v],min(minEdge,res[p[v]][v]->rem));
                res[p[v]][v]->rem -= f;
res[v][p[v]]->rem += f;
int edmondsKarp(int source, int sink) {
        int mf = 0;
        s = source;
        t = sink;
        while(true) {
                bitset<MAX_N> visited;
                queue<int> q;
                q.push(s);
                p.assign(V,-1);
                 visited.set(s);
                while(!q.empty()) {
                         int u = q.front(); q.pop();
// printf("exploring %d\n",u);
                         if(u == t) {
                                 break;
                         } else {
                                  for(int i = 0; i < (int)adjList[u].size(); i++) {</pre>
                                          Edge *e = adjList[u][i];
                                          if(e->rem > 0 && !visited.test(e->v)){
                                                  p[e->v] = u;
                                                   visited set (e->v);
                                                   q.push(e->v);
                 augment(t,INF);
                if( f == 0) {
                         break;
                mf += f;
        return mf;
typedef pair<int.int> ii:
typedef pair<int,ii> iii;
int main() {
        V = 7;
        adjList.assign(V, vector<Edge*>());
```

```
* This is a sample graph.
vector<iii> edges;
edges.push_back(iii(0,ii(1,10)));
edges.push_back(iii(0,ii(4,10)));
edges.push_back(iii(1,ii(2,20)));
edges.push_back(iii(2,ii(3,10)));
edges.push_back(iii(4,ii(1,10)));
edges.push_back(iii(2,ii(5,5)));
edges.push_back(iii(3,ii(6,10)));
edges.push_back(iii(5,ii(6,10)));
for(int i = 0; i < (int)edges.size(); i++) {</pre>
         * This is how to add an edge.
        iii cur = edges[i];
        Edge *e = new Edge(cur.first,cur.second.first,cur.second.second);
        Edge *eRev = new Edge(cur.second.first,cur.first,0);
        adjList[cur.first].push_back(e);
        adjList[cur.second.first].push_back(eRev);
        res[cur.first][cur.second.first] = e;
res[cur.second.first][cur.first] = eRev;
printf("maxflow: %d\n",edmondsKarp(0,6));
return 0:
```

3.12 Max Flow with Dinic's Algorithm

```
#include <vector>
#include <bitset>
#include <queue>
using namespace std;
#define MAX N 1000
#define INF 1000000000
typedef vector<int> vi;
class Edge {
        public:
        int u. v. cap. rem:
        Edge(int _u, int _v, int _cap) : u(_u), v(_v), cap(_cap), rem(_cap) {}
int V, f, s, t;
vector<vector<Edge *> > adjList;
Edge *res[MAX_N][MAX_N];
void augment(int v, int minEdge) {
        // printf("augmenting %d\n",v);
        if(v == s) {
                 f = minEdge;
        } else if(p[v] != -1) {
                augment (p[v], min (minEdge, res[p[v]][v]->rem));
res[p[v]][v]->rem -= f;
                 res[v][p[v]]->rem += f;
int dinicsMaxFlow(int source, int sink) {
        int mf = 0;
        s = source;
t = sink;
        bool hasFlow = true:
        while (hasFlow) {
                vi dist(V, INF);
                 queue<int> q;
                 q.push(s);
                 while(!q.empty()) {
                          int u = q.front(); q.pop();
                          // printf("exploring %d\n",u);
                          if(u == t) {
                                  break;
                          else
                                   for(int i = 0; i < (int)adjList[u].size(); i++) {</pre>
                                           Edge *e = adjList[u][i];
                                           if(e->rem > 0 && dist[e->v] == INF){
    dist[e->v] = dist[u] + 1;
                                                    q.push(e->v);
```

```
hasFlow = false;
              while (true) {
                      bitset<MAX_N> visited;
                      q = queue<int>();
                      q.push(s);
                      p.assign(V,-1);
                      visited.set(s);
                      while(!q.empty()) {
    int u = q.front(); q.pop();
    if(u == t) {
                                    break;
                             } else {
                                    dist[u] + 1) {
                                                   visited.set(e->v);
                                                   q.push(e->v);
                      augment (t, INF);
                      if( f == 0) {
                             break:
                      mf += f;
                      hasFlow = true;
       return mf;
typedef pair<int, int> ii;
typedef pair<int, ii> iii;
adjList.assign(V, vector<Edge*>());
        * This is a sample graph.
       vector<iii> edges;
```

edges.push_back(iii(0,ii(1,10)));

- 4 Combinatorics
- 5 Number Theory
- 6 Miscellaneous Mathematics
- 7 String Processing
- 8 Computational Geometry