

EE 531: ADVANCED VLSI DESIGN

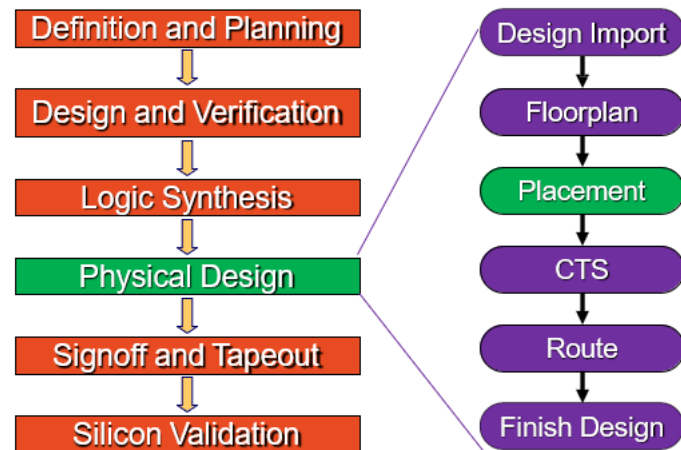
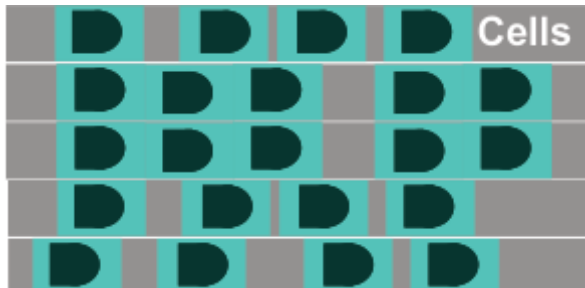
Placement

Nishith N. Chakraborty

February, 2025

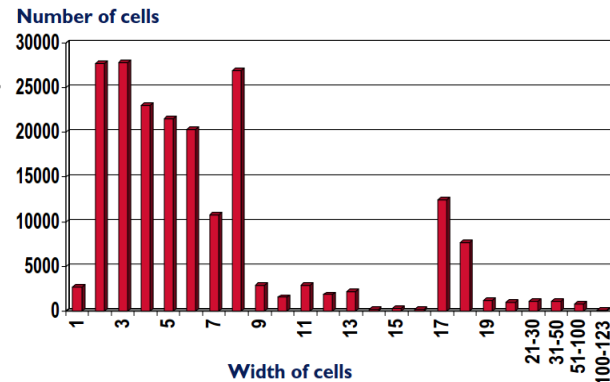
DESIGN FLOW: OUR PROGRESS

- We have reviewed the synthesis of our design into a technology mapped gate-level netlist.
- We have seen how to design a floorplan with pre-placed blocks.
- Now we will move into detailed placement of the standard cells.



CHIP SIZE AND SMALL GATES

- Before we start discussing how to place the standard cells, we would like to make sure we understand how big a problem it is.
 - How big is a “100 Million gate ASIC”?
- In real designs, small cells dominate.
 - Therefore, numbers are usually given as “equivalent small gates”
 - May also consider a hard macro to be many, many small gates.



CHIP SIZE AND SMALL GATES

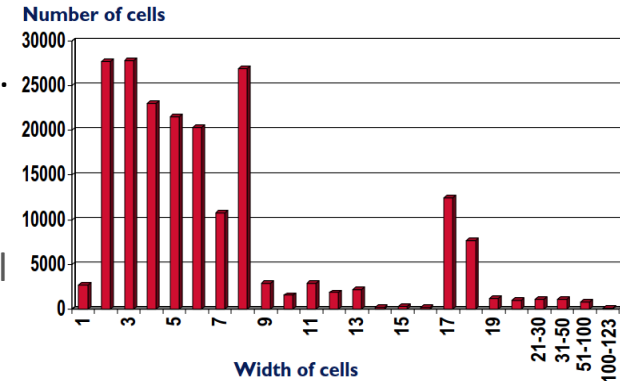
- Before we start discussing how to place the standard cells, we would like to make sure we understand how big a problem it is.

➤ How big is a “100 Million gate ASIC”?

- In real designs, small cells dominate.

➤ Therefore, numbers are usually given as “equivalent small gates”

➤ May also consider a hard macro to be many, many small gates.



- Conclusion:

➤ Gates==Equivalent NAND2 gates

➤ Instances: # of things placed!

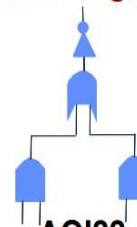
➤ Rule of thumb: $\text{Instances} = \text{Gates} / 4..5$

Size? 1 gate



NAND2

Size? ~4 gates



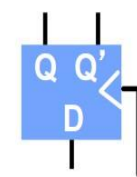
AOI22

Size? ~6 gates



1bit adder

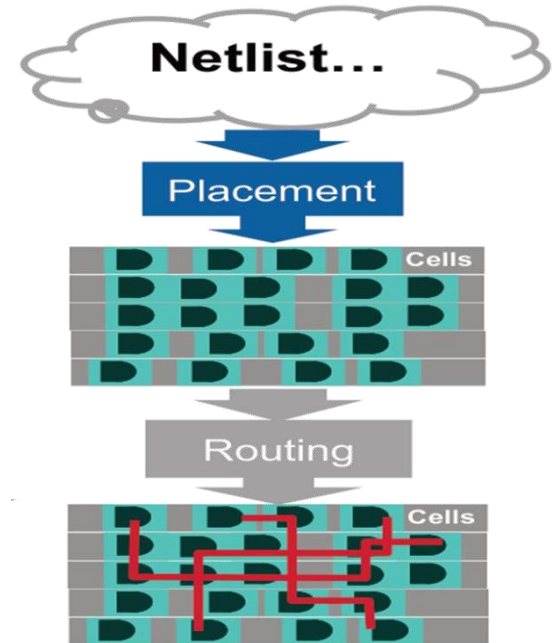
Size? ~10 gates



D Flip Flop

PLACEMENT

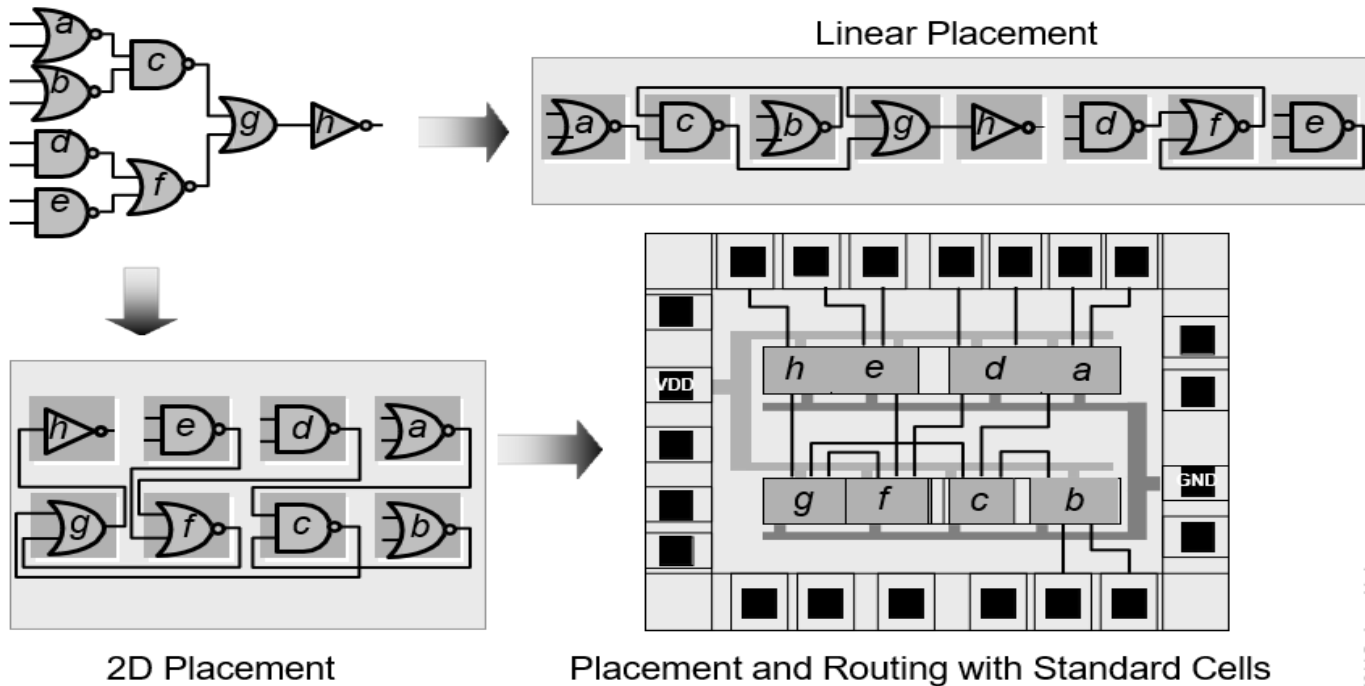
- Placement is the stage of the design flow, during which each instance (standard cell) is given an exact location.
- Inputs:
 - Netlist of gates and wires.
 - Floorplan and Technology constraints
- Output:
 - All cells located in the floorplan.
- Goal
 - Provide legal location of entire netlist
 - Enable detailed route of all nets
 - Meet timing, area, and power targets



PLACEMENT

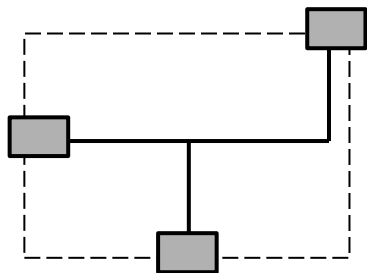
- Key is use of constant height, variable-width standard cells arrayed into rows across the chip
- Can also add application-specific custom blocks
- Typically, there is no separation between std. cell rows as routing occurs over the cells using multiple metal layers
- Placement makes use of LEF input

PLACEMENT EXAMPLE

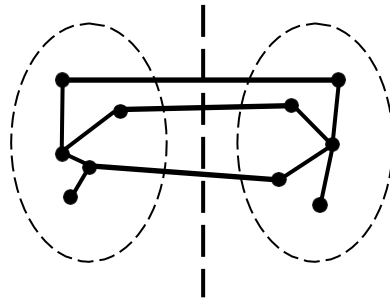


OPTIMIZATION OBJECTIVES

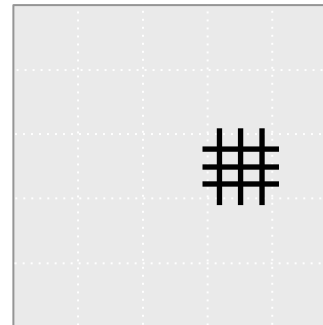
Total
Wirelength



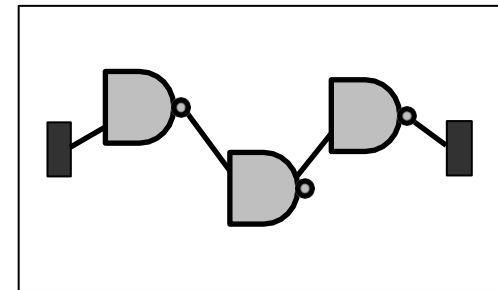
Number of
Cut Nets



Wire
Congestion



Signal
Delay



PLACEMENT FLOW

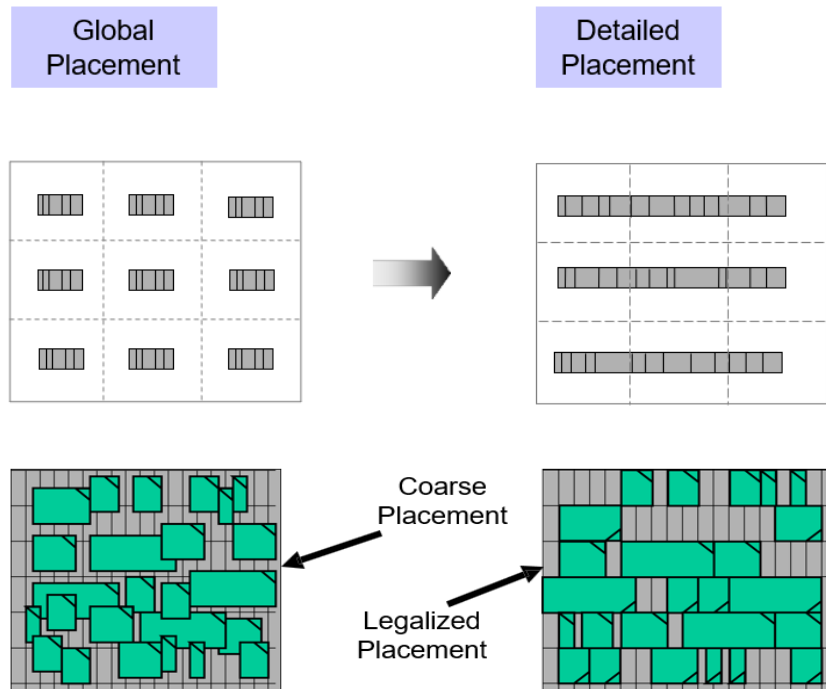
- In general, most tools partition the placement task into two stages:

- Global placement:

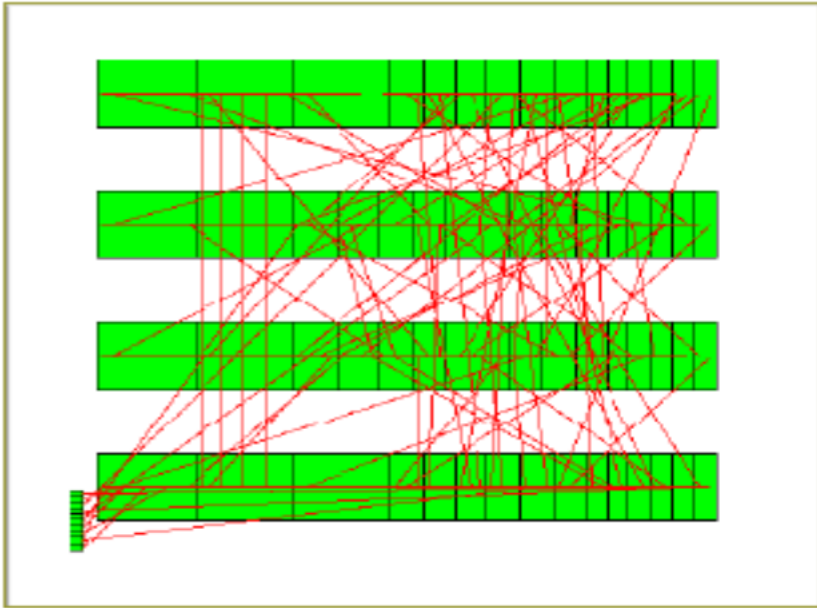
- Quickly divide each cell into “bins” to try and minimize the number of connections between groups.

- Detailed placement:

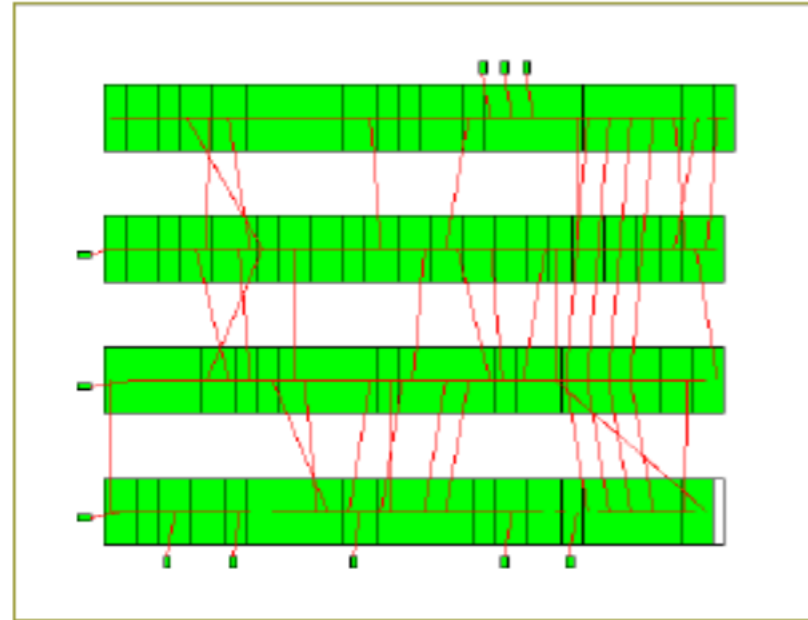
- Provide a legal placement for each instance
 - Try and minimize wirelength (or other cost metrics)
 - Try to finish with uncongested design.



RESULTS OF PLACEMENT



Bad Placement



Good Placement

RESULTS OF PLACEMENT

- Bad placement causes routing congestion:
 - Increases circuit area and cost
 - Longer wires leading to more capacitance
 - Longer delay and higher dynamic power
- Good placement:
 - Circuit area and wiring decreased
 - Shorter wires with less capacitance
 - Shorter delay and less dynamic power

PLACEMENT ALGORITHMS

- Partitioning-based algorithms:
 - The netlist and the layout are divided into smaller sub-netlists and sub-regions, respectively
 - Process is repeated until each sub-netlist and sub-region is small enough to be handled optimally
 - Detailed placement often performed by optimal solvers, facilitating a natural transition from global placement to detailed placement
 - Example: min-cut placement

PLACEMENT ALGORITHMS

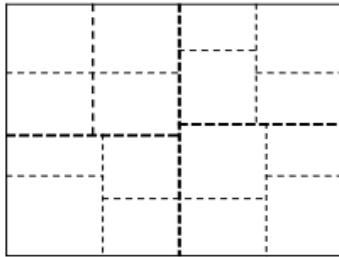
- **Stochastic algorithms:**
 - Randomized moves that allow hill-climbing are used to optimize the cost function
 - Example: simulated annealing
- **Analytic techniques:**
 - Model the placement problem using an objective (cost) function, which can be optimized via numerical analysis
 - Examples: quadratic placement and force-directed placement

PLACEMENT ALGORITHMS

Partitioning-based



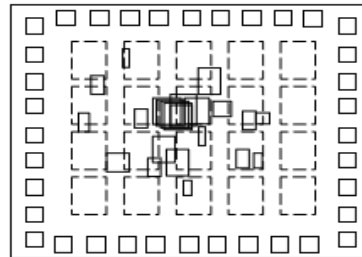
Min-cut
placement



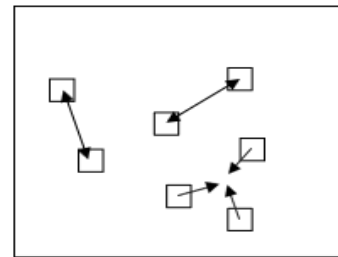
Analytic



Quadratic
placement



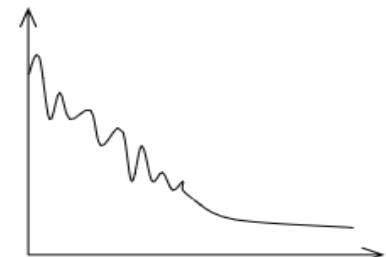
Force-directed
placement



Stochastic



Simulated annealing

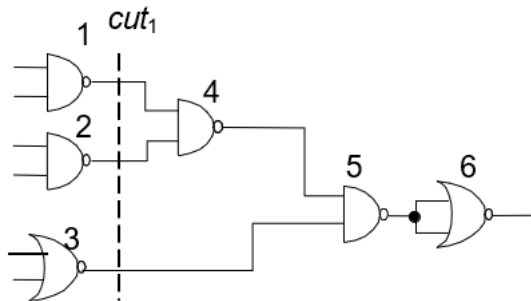


MIN-CUT ALGORITHM

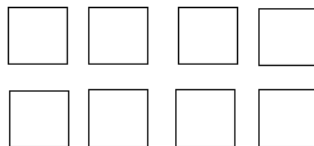
- Uses partitioning algorithms to divide (1) the netlist and (2) the layout region into smaller sub-netlists and sub-regions
- Conceptually, each sub-region is assigned a portion of the original netlist
- Each cut heuristically minimizes the number of cut nets using, for example,
 - Kernighan-Lin (KL) algorithm
 - Fiduccia-Mattheyses (FM) algorithm

MIN-CUT ALGORITHM: EXAMPLE

- Given:

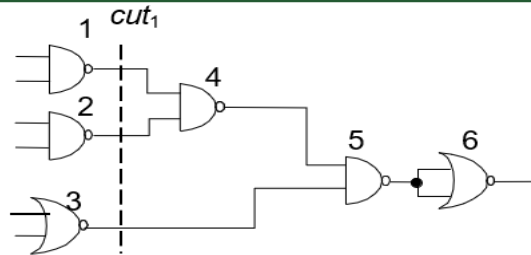


- Task: 4 x 2 placement with minimum wirelength using alternative cutline directions and the KL algorithm

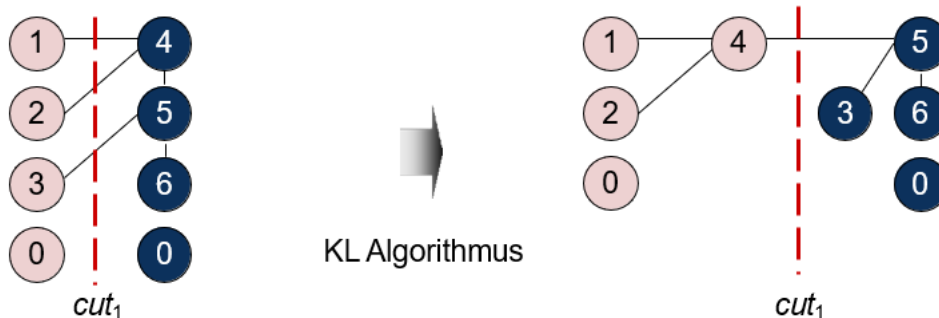


MIN-CUT ALGORITHM: EXAMPLE

- Given:

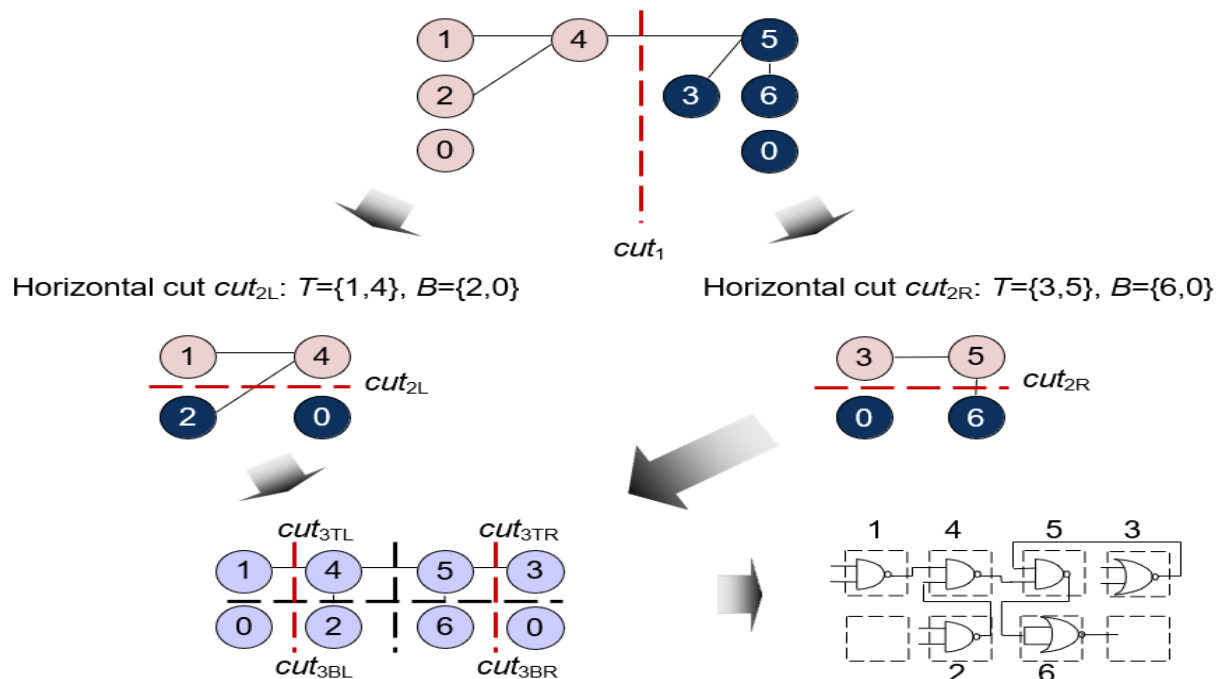


- Vertical cut cut_1 : $L=\{1,2,3\}$, $R=\{4,5,6\}$
- Let's run KL algorithm



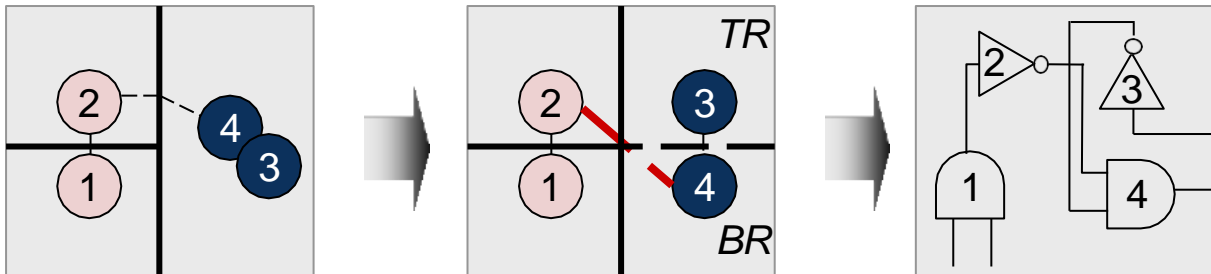
MIN-CUT ALGORITHM: EXAMPLE

- Now partition each partition:



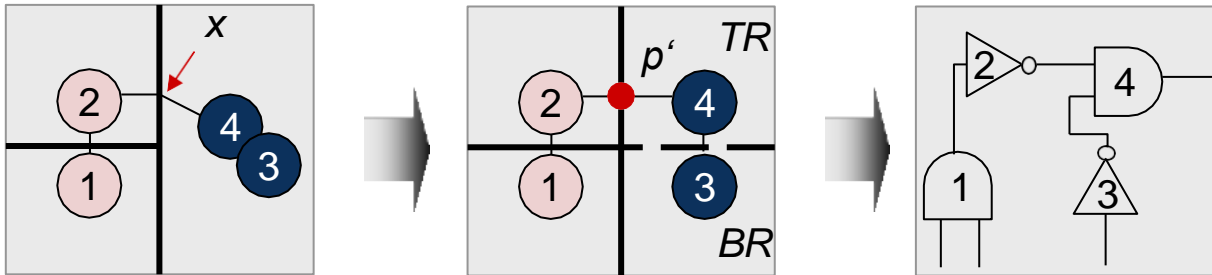
MIN-CUT ALGORITHM: TERMINAL PROPAGATION

- Min-cut didn't take external conditions into account



MIN-CUT ALGORITHM: TERMINAL PROPAGATION

- Min-cut didn't take external conditions into account
- Modified Min-cut to include terminal propagation
 - External connections are represented by artificial connection points on the cutline
 - Dummy nodes in hypergraphs



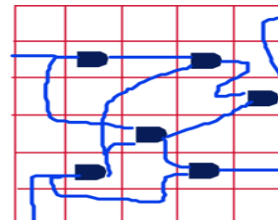
MIN-CUT ALGORITHM: PROS AND CONS

- Advantages:
 - Reasonably fast
 - Objective function can be adjusted, e.g., to perform timing-driven placement
 - Hierarchical strategy applicable to large circuits
- Disadvantages:
 - Randomized, chaotic algorithms – small changes in input lead to large changes in output
 - Optimizing one cutline at a time may result in routing congestion elsewhere

RANDOM PLACEMENT

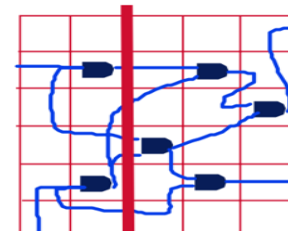
- **Problem Formulation:** Given a netlist, and fixed-shape cells (small, standard cell), find the exact location of the cells to minimize area and wire-length
 - Consistent with the standard-cell design methodology
 - Row-based, no hard-macros
 - Modules
 - Usually fixed, equal height (exception: double height cells)
 - Some fixed (I/O pads)
 - Connected by edges or hyperedges
- Objectives:
 - Cost components: area, wire length
 - Additional cost components: timing, congestion

Wirelength Minimization



Add up the estimated length of all nets and try to minimize

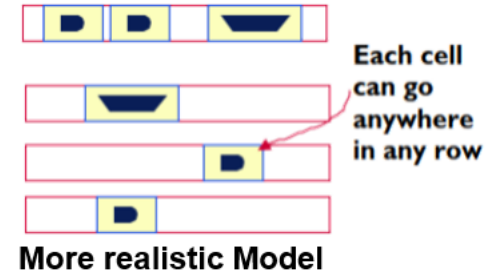
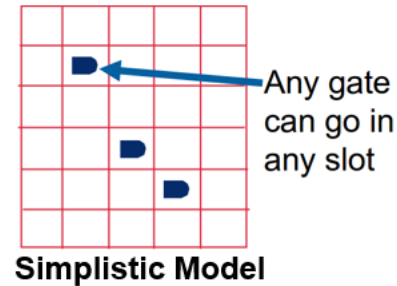
Congestion Minimization



Take any cut through the placement and try to minimize the number of nets that cross it.

SIMPLE PLACER

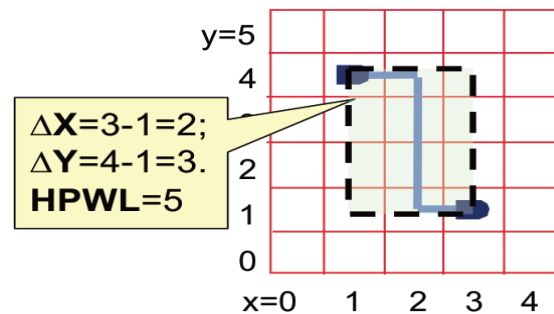
- Assume a very simple chip model:
 - Simple **grid** – cells go in squares
 - **Pins** fixed at edges
- Assume simple gate model:
 - All gates same size
 - Each grid slot can hold one gate.



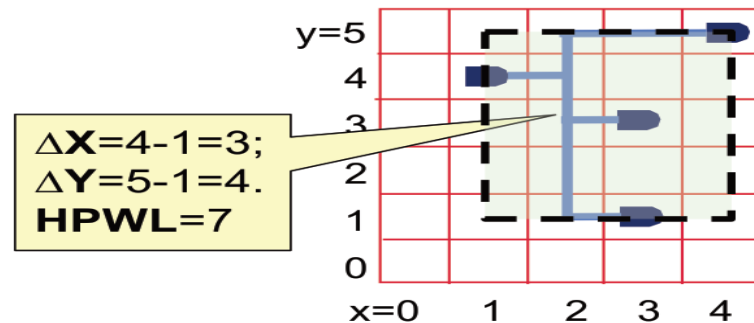
SIMPLE PLACER

- Assume a very simple chip model:
 - Simple **grid** – cells go in squares
 - **Pins** fixed at edges
- Assume simple gate model:
 - All gates same size
 - Each grid slot can hold one gate.
- Simple bounding box wirelength estimator:
 - “**Half-Perimeter Wirelength**” (**HPWL**)
 - Put the smallest box around all gates on net.
 - Measure Width (ΔX) and Height (ΔY) of box.
 - **HPWL = $\Delta X + \Delta Y$**

A “2-point net”



A “4-point net”



SIMPLE PLACER

Let's define a simple algorithm:

- Start with a random placement:
 - Randomly assign each gate to a grid location.
- Apply random iterative improvement:
 - Pick a random pair of gates.
 - Swap their locations and evaluate the change in total wirelength.
 - If wirelength got smaller – accept the swap.
 - If wirelength got bigger – undo the swap.
 - Repeat until wirelength stops improving.

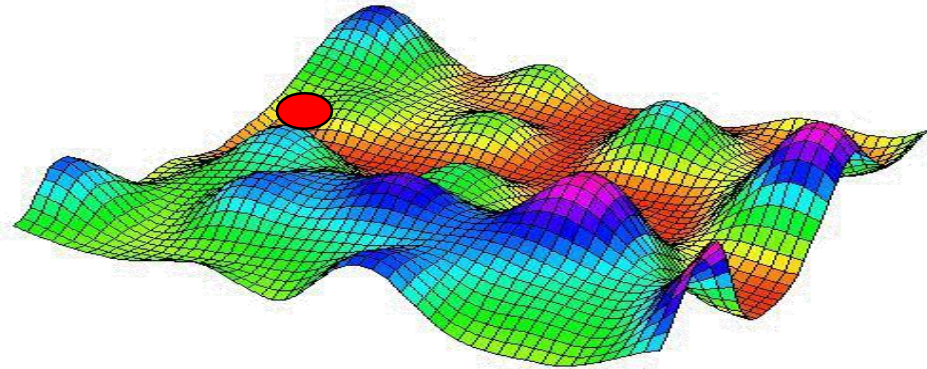
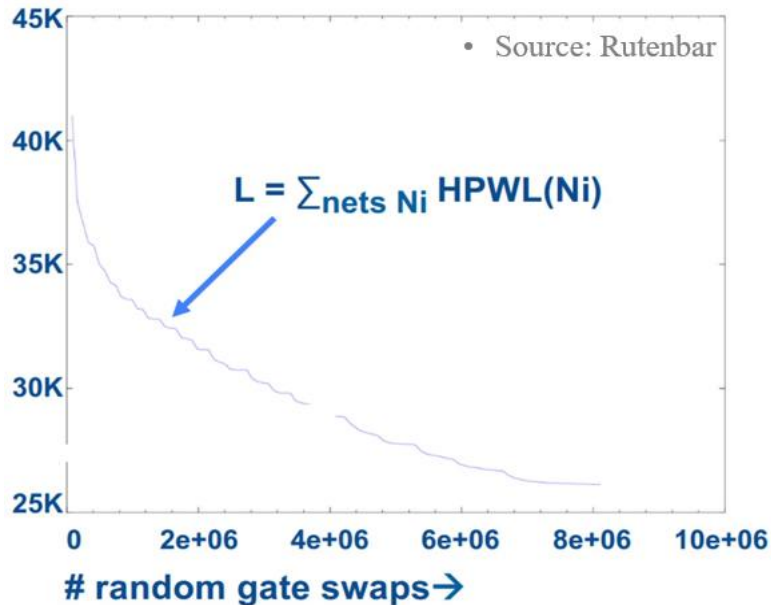
```
// Random initial placement
foreach (gate Gi in netlist)
    place Gi in random (x,y) not occupied.

// calculate initial HPWL
L=0
foreach (net Ni in netlist)
    L = L + HPWL(Ni)

// random iterative improvement
while (overall HPWL is improving)
    pick two random gates Gi, Gj
    swap Gi and Gj
    evaluate ΔL = new HPWL - old HPWL
    if (ΔL < 0) then keep the swap
    if (ΔL > 0) undo the swap
```

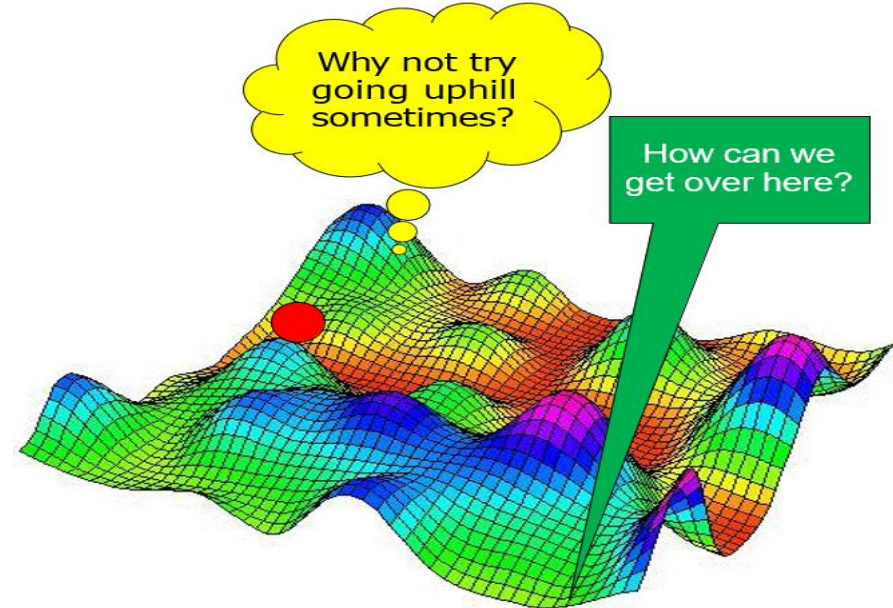
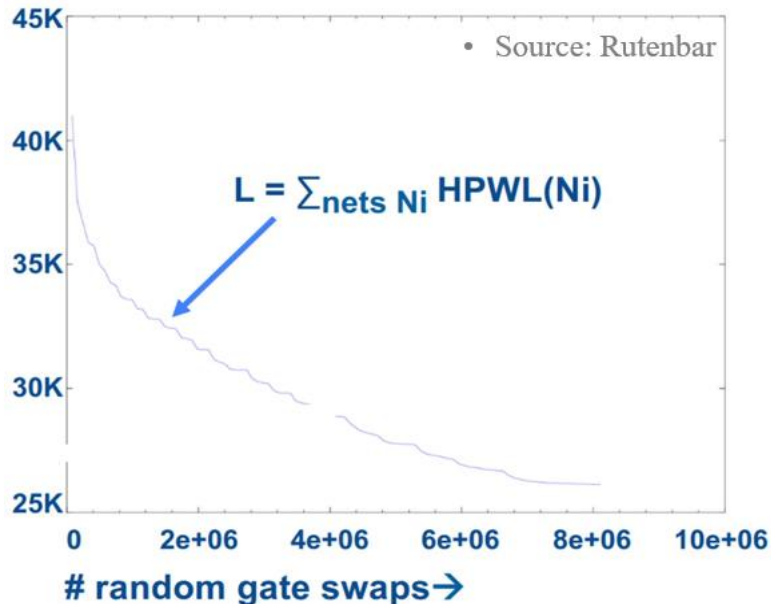
SIMPLE PLACER

- Was this any good?
 - Well, we quickly get stuck in a local minimum.



SIMPLE PLACER

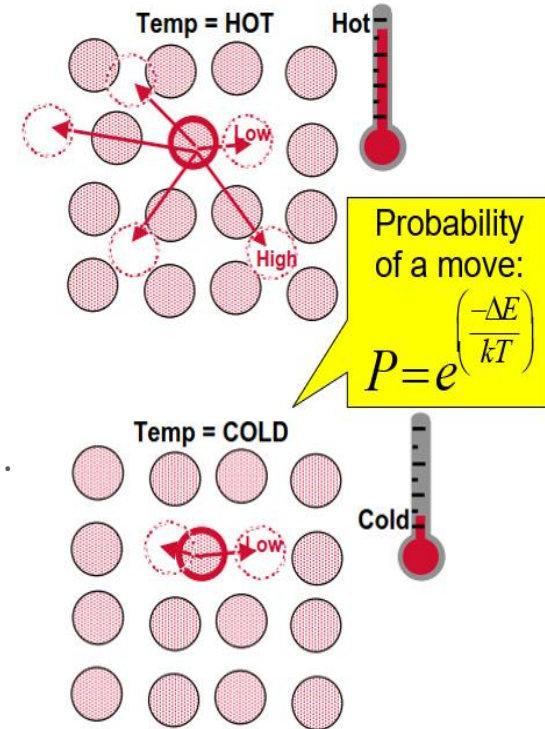
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SIMULATED ANNEALING

In semiconductors, there is “annealing”:

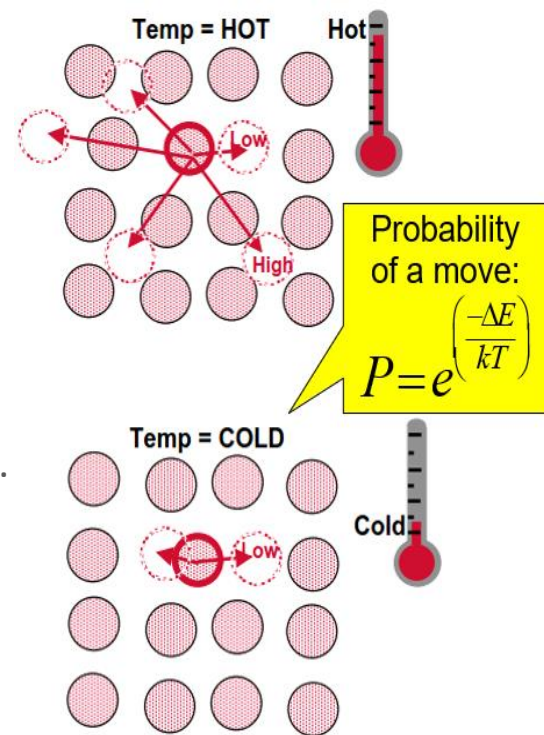
- The **lowest energy state** of a crystal lattice is when all atoms are lined up.
- So if we have a messy crystal:
 - **Heat it up** – give atoms energy to move around.
 - **Cool it slowly** –
 - At first, atoms will move a lot.
 - But as the crystal cools, the movement will be restricted.



SIMULATED ANNEALING

In semiconductors, there is “annealing”:

- The **lowest energy state** of a crystal lattice is when all atoms are lined up.
- So if we have a messy crystal:
 - **Heat it up** – give atoms energy to move around.
 - **Cool it slowly** –
 - At first, atoms will move a lot.
 - But as the crystal cools, the movement will be restricted.
- What if we apply this idea to random hill climbing?
 - At first (“**hot temperature**”) we’ll “climb a lot of hills”.
 - As we progress (“**cool down**”) we will make fewer big jumps.
- This very famous idea is called “**Simulated Annealing**”



SIMULATED ANNEALING ALGORITHM

- Start with the same basic algorithm:
 - Random initial placement
 - Swap two Random gates
 - Evaluate change in HPWL (ΔL)
 - If wirelength improves, accept the change.

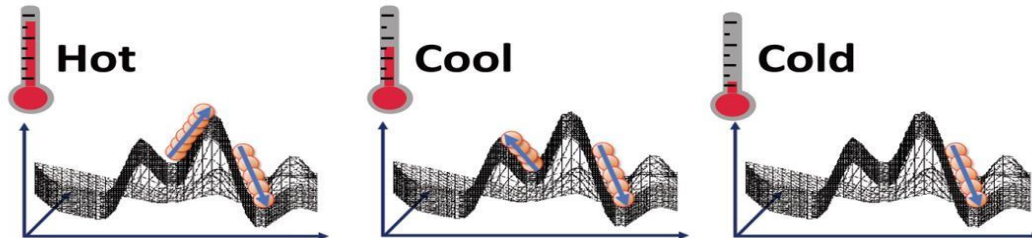
```
T=HOT; frozen = false
while (!frozen)
    swap two random gates Gi, Gj
    evaluate  $\Delta L$ 
    if ( $\Delta L < 0$ ) then
        keep the swap
    else
        if (random() < exp(- $\Delta L/T$ ))
            accept swap
        else
            undo swap
    if (HPWL still decreasing)
        T = 0.9*T
    else
        frozen=true
```

SIMULATED ANNEALING ALGORITHM

- Start with the same basic algorithm:
 - **Random** initial placement
 - **Swap** two Random gates
 - Evaluate change in **HPWL** (ΔL)
 - If wirelength improves, accept the change.
- But what if wirelength increases ($\Delta L > 0$)?
 - Evaluate annealing probability function: $P = \exp\left(\frac{-\Delta L}{T}\right)$
 - Choose a uniform random number (R) between 0 and 1
 - If $R < P$ then keep the swap.
- What is T ?
 - T is the simulated temperature.
 - Start hot. Cool down.**

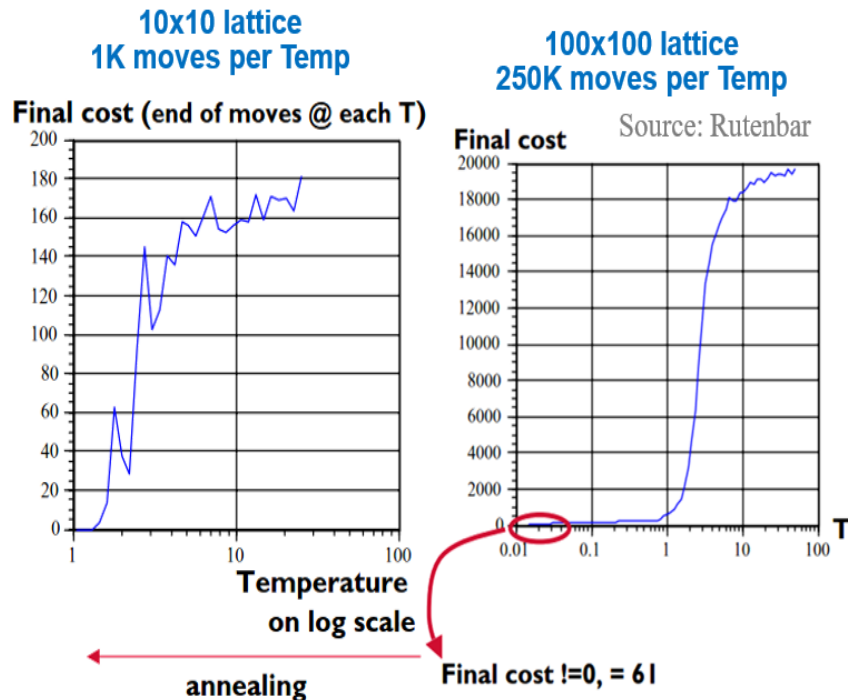
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     $T = 0.9 * T$ 
  else
    frozen=true
  
```



SIMULATED ANNEALING

- How well does this work?
 - Really well!
 - Many EDA algorithms use Simulated Annealing.
- Does it find an **optimal** solution?
 - No. But it's good at avoiding local minima.
- What happens if I run it again?
 - I will get a **different answer** each time!
- **NOT** how placers work today!



ANALYTICAL PLACEMENT APPROACH

- Question:
 - Can we write an equation whose **minimum** is the placement?
 - If we have a **cost function** (such as wirelength) that is a **function of the gate coordinates** (x_i, y_i), i.e.: $L_{\text{wire}} = f(x_1, x_2, \dots, x_N, y_1, y_2, \dots, y_N)$
 - Then we could find the **minimum of f** and this would be our **optimal** placement!

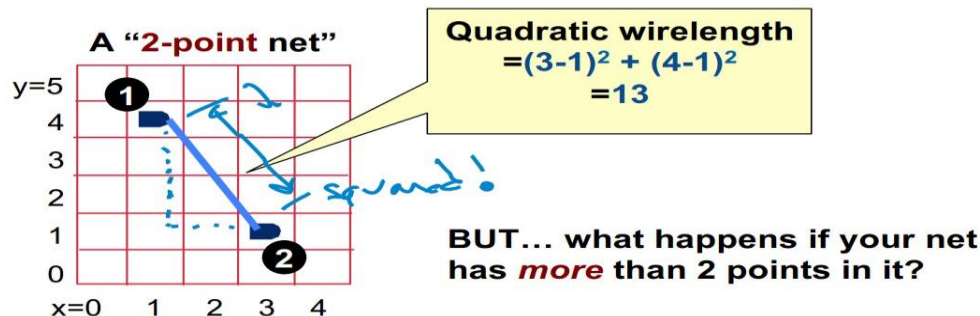
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 - Then we could find the **minimum of f** and this would be our **optimal** placement!
- Sounds crazy, but **the answer is YES!**
 - All modern placers are based on analytical placement.
 - We need to write the cost function in a mathematically friendly way.
 - Then, we can just differentiate and equate to 0!

$$\frac{\partial f}{\partial x} = 0, \frac{\partial f}{\partial y} = 0$$

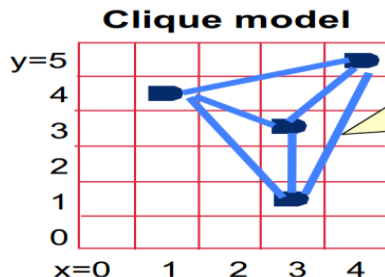
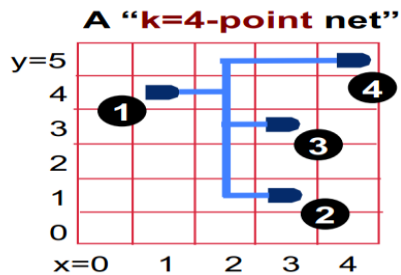
QUADRATIC PLACEMENT COST FUNCTION

- Instead of **HPWL**, let's define a new wirelength model:
 - Quadratic wirelength: $L = (x_1 - x_2)^2 + (y_1 - y_2)^2$



QUADRATIC PLACEMENT COST FUNCTION

- What about a **k-point** net ($k > 2$)?
 - Instead of one “real” net, replace with a **fully connected clique model**.
 - So each gate on the net has a one-to-one connection with the other.
 - Altogether $k(k-1)/2$ nets
 - Compensate by weighting each new net by $1/(k-1)$
- One last point:
 - Assume that gates are **dimensionless** points.



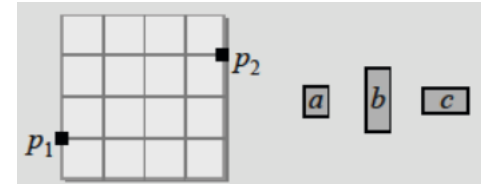
Quadratic estimate:
 $(1/3)[(4-1)^2 + (5-4)^2]$
 $+(1/3)[(4-3)^2 + (5-1)^2]$
 $+(1/3)[(3-1)^2 + (4-1)^2]$
 $+(1/3)[(3-1)^2 + (4-3)^2]$
 $+(1/3)[(4-3)^2 + (5-3)^2]$
 $+(1/3)[(3-3)^2 + (3-1)^2]$
=sum of 6 weighted
2-point lengths

QUADRATIC PLACEMENT CALCULATION

- Example of quadratic wirelength calculation:
 - Each point has an **unknown** (x_i, y_i) coordinate.
 - Each net has a **pre-assigned** weight.

$$L(P) = \sum_{i=1, j=1}^n c(i, j) \left((x_i - x_j)^2 + (y_i - y_j)^2 \right)$$

- Pads are **fixed pins** on the edge.



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- Pads are **fixed pins** on the edge.
- Each dimension can be considered independently:

$$L_x(P) = \sum_{i=1, j=1}^n c(i, j) (x_i - x_j)^2 \quad L_y(P) = \sum_{i=1, j=1}^n c(i, j) (y_i - y_j)^2$$

- Convex quadratic optimization problem: any local minimum solution is also a global minimum
- Optimal x- and y--coordinates can be found by setting the partial derivatives of $L_x(P)$ and $L_y(P)$ to zero

QUADRATIC PLACEMENT CALCULATION

$$L_x(P) = \sum_{i=1, j=1}^n c(i, j)(x_i - x_j)^2$$



$$\frac{\partial L_x(P)}{\partial X} = AX - b_x = 0$$

$$L_y(P) = \sum_{i=1, j=1}^n c(i, j)(y_i - y_j)^2$$



$$\frac{\partial L_y(P)}{\partial Y} = AY - b_y = 0$$

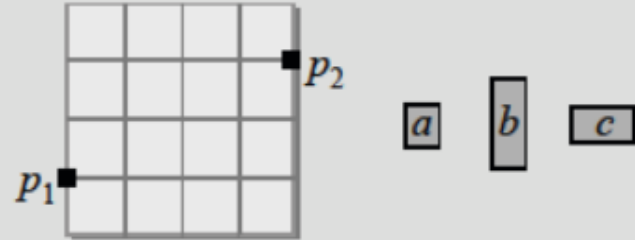
- Where A is a matrix with $A[i][j] = -c(i, j)$ when $i \neq j$, and $A[i][i] =$ the sum of incident connection weights of cell i .
- X is a vector of all the x -coordinates of the non-fixed cells, and b_x is a vector with $b_x[i] =$ the sum of x -coordinates of all fixed cells attached to i .
- Y is a vector of all the y -coordinates of the non-fixed cells, and b_y is a vector with $b_y[i] =$ the sum of y -coordinates of all fixed cells attached to i .

QUADRATIC PLACEMENT EXAMPLE

Example: Quadratic Placement

Given: (1) placement P with two fixed points p_1 (100,175) and p_2 (200,225), (3) three free blocks a - c and (4) nets N_1 - N_4 .

$N_1(P_1, a)$ $N_2(a, b)$ $N_3(b, c)$ $N_4(c, P_2)$



Task: find the coordinates of blocks (x_a, y_a) , (x_b, y_b) and (x_c, y_c) .

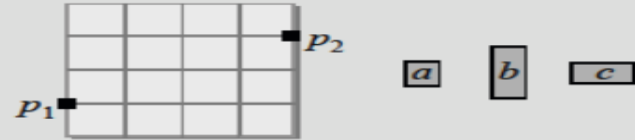
$C_{i,j} = 1$, as no weight specified.

QUADRATIC PLACEMENT EXAMPLE

Example: Quadratic Placement

Given: (1) placement P with two fixed points p_1 (100,175) and p_2 (200,225), (3) three free blocks a - c and (4) nets N_1 - N_4 .

$N_1(P_1, a)$ $N_2(a, b)$ $N_3(b, c)$ $N_4(c, P_2)$



Task: find the coordinates of blocks (x_a, y_a) , (x_b, y_b) and (x_c, y_c) .

Solution:

Solve for x-coordinates.

$$L_x(P) = (100 - x_a)^2 + (x_a - x_b)^2 + (x_b - x_c)^2 + (x_c - 200)^2$$

$$\frac{\partial L_x(P)}{\partial x_a} =$$

$$x_a$$

$$\frac{\partial L_x(P)}{\partial x_b} =$$

$$x_b$$

$$\frac{\partial L_x(P)}{\partial x_c} =$$

$$x_c$$

Solve for y-coordinates.

$$L_y(P) = (175 - y_a)^2 + (y_a - y_b)^2 + (y_b - y_c)^2 + (y_c - 225)^2$$

$$\frac{\partial L_y(P)}{\partial y_a} =$$

$$y_a$$

$$\frac{\partial L_y(P)}{\partial y_b} =$$

$$y_b$$

$$\frac{\partial L_y(P)}{\partial y_c} =$$

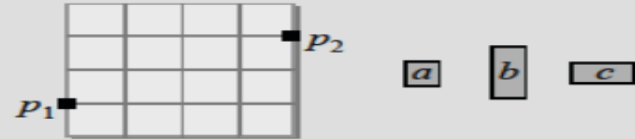
$$y_c$$

QUADRATIC PLACEMENT EXAMPLE

Example: Quadratic Placement

Given: (1) placement P with two fixed points p_1 (100,175) and p_2 (200,225), (3) three free blocks a - c and (4) nets N_1 - N_4 .

$N_1(P_1, a)$ $N_2(a, b)$ $N_3(b, c)$ $N_4(c, P_2)$



Task: find the coordinates of blocks (x_a, y_a) , (x_b, y_b) and (x_c, y_c) .

Solution:

Solve for x-coordinates.

$$L_x(P) = (100 - x_a)^2 + (x_a - x_b)^2 + (x_b - x_c)^2 + (x_c - 200)^2$$

$$\frac{\partial L_x(P)}{\partial x_a} = -2(100 - x_a) + 2(x_a - x_b) = 4x_a - 2x_b - 200 = 0$$

$$\frac{\partial L_x(P)}{\partial x_b} = -2(x_a - x_b) + 2(x_b - x_c) = -2x_a + 4x_b - 2x_c = 0$$

$$\frac{\partial L_x(P)}{\partial x_c} = -2(x_b - x_c) + 2(x_c - 200) = -2x_b + 4x_c - 400 = 0$$

Solve for y-coordinates.

$$L_y(P) = (175 - y_a)^2 + (y_a - y_b)^2 + (y_b - y_c)^2 + (y_c - 225)^2$$

$$\frac{\partial L_y(P)}{\partial y_a} = -2(175 - y_a) + 2(y_a - y_b) = 4y_a - 2y_b - 350 = 0$$

$$\frac{\partial L_y(P)}{\partial y_b} = -2(y_a - y_b) + 2(y_b - y_c) = -2y_a + 4y_b - 2y_c = 0$$

$$\frac{\partial L_y(P)}{\partial y_c} = -2(y_b - y_c) + 2(y_c - 225) = -2y_b + 4y_c - 450 = 0$$

QUADRATIC PLACEMENT EXAMPLE

Solution:

Solve for x-coordinates.

$$L_x(P) = (100 - x_a)^2 + (x_a - x_b)^2 + (x_b - x_c)^2 + (x_c - 200)^2$$

$$\frac{\partial L_x(P)}{\partial x_a} = -2(100 - x_a) + 2(x_a - x_b) = 4x_a - 2x_b - 200 = 0$$

$$\frac{\partial L_x(P)}{\partial x_b} = -2(x_a - x_b) + 2(x_b - x_c) = -2x_a + 4x_b - 2x_c = 0$$

$$\frac{\partial L_x(P)}{\partial x_c} = -2(x_b - x_c) + 2(x_c - 200) = -2x_b + 4x_c - 400 = 0$$



Put in matrix form $AX = b_x$.

$$\begin{bmatrix} 4 & -2 & 0 \\ -2 & 4 & -2 \\ 0 & -2 & 4 \end{bmatrix} \begin{bmatrix} x_a \\ x_b \\ x_c \end{bmatrix} = \begin{bmatrix} 200 \\ 0 \\ 400 \end{bmatrix} \rightarrow \begin{bmatrix} 2 & -1 & 0 \\ -1 & 2 & -1 \\ 0 & -1 & 2 \end{bmatrix} \begin{bmatrix} x_a \\ x_b \\ x_c \end{bmatrix} = \begin{bmatrix} 100 \\ 0 \\ 200 \end{bmatrix}$$

Solve for X: $x_a = 125$, $x_b = 150$, $x_c = 175$.

Solve for y-coordinates.

$$L_y(P) = (175 - y_a)^2 + (y_a - y_b)^2 + (y_b - y_c)^2 + (y_c - 225)^2$$

$$\frac{\partial L_y(P)}{\partial y_a} = -2(175 - y_a) + 2(y_a - y_b) = 4y_a - 2y_b - 350 = 0$$

$$\frac{\partial L_y(P)}{\partial y_b} = -2(y_a - y_b) + 2(y_b - y_c) = -2y_a + 4y_b - 2y_c = 0$$

$$\frac{\partial L_y(P)}{\partial y_c} = -2(y_b - y_c) + 2(y_c - 225) = -2y_b + 4y_c - 450 = 0$$



Put in matrix form $AY = b_y$.

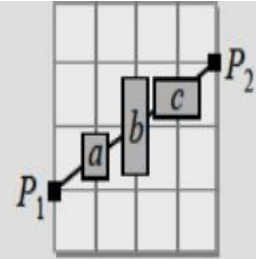
$$\begin{bmatrix} 4 & -2 & 0 \\ -2 & 4 & -2 \\ 0 & -2 & 4 \end{bmatrix} \begin{bmatrix} y_a \\ y_b \\ y_c \end{bmatrix} = \begin{bmatrix} 350 \\ 0 \\ 450 \end{bmatrix} \rightarrow \begin{bmatrix} 2 & -1 & 0 \\ -1 & 2 & -1 \\ 0 & -1 & 2 \end{bmatrix} \begin{bmatrix} y_a \\ y_b \\ y_c \end{bmatrix} = \begin{bmatrix} 175 \\ 0 \\ 225 \end{bmatrix}$$

Solve for Y: $y_a = 187.5$, $y_b = 200$, $y_c = 212.5$.

QUADRATIC PLACEMENT EXAMPLE

- Final Solution:

Final solution: a (125,187.5), b (150,200) and c (175,212.5).



BUILDING ANALYTICAL NETWORK

Recipe for success

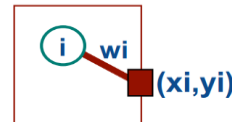
- Build connectivity matrix (C) as follows.
 - $C(i,j)=C(j,i)=w$ for a net with weight w connected between gates i and j .
 - If no net connects gates i and j , $C(i,j)=0$.
- Build A matrix:
 - Off diagonal, $A(i,j) = -C(i,j)$
 - $A(i,i)$ is sum of row i + weight of net from i to pad.
- Build b vectors:
 - If gate i connects to a pad at (x_i, y_i) with weight w_i then
 $b_x(i)=w_i \cdot x_i$, $b_y(i)=w_i \cdot y_i$.

$$C_{i,j} = C_{j,i} = \begin{cases} 0 & i = j \\ 0 & \text{no net}_{i,j} \\ w_{i,j} & \text{net}_{i,j} \end{cases}$$

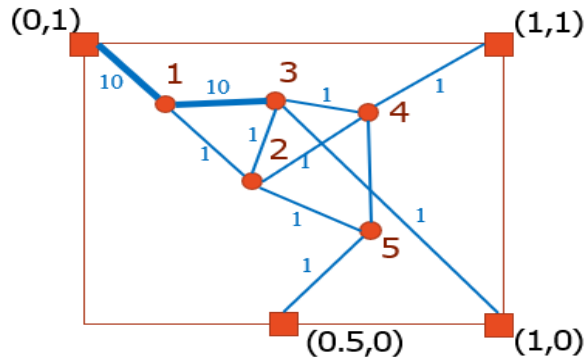
$$A_{i,j} = \begin{cases} -C_{i,j} & i \neq j \\ \sum_{j=1}^N C_{i,j} + w_{j,\text{pads}} & i = j \end{cases}$$

$$b_{x,i} = \begin{cases} 0 & \text{no pad} \\ w_i \cdot x_i & \text{pad } (x_i, y_i, w_i) \end{cases}$$

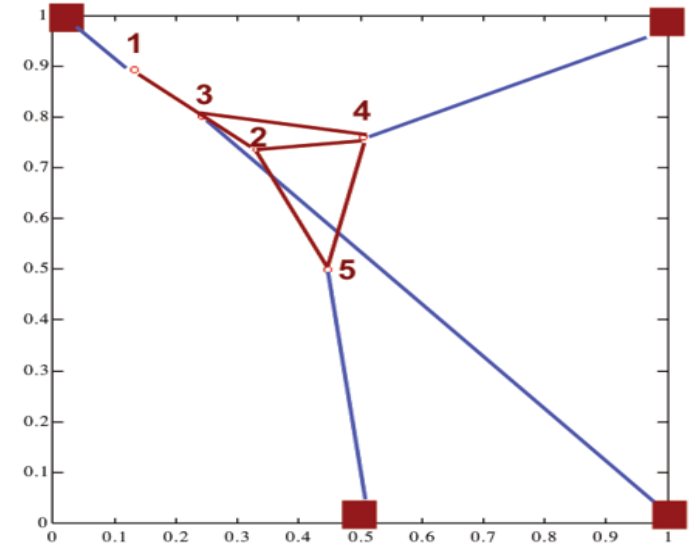
$$b_{y,i} = \begin{cases} 0 & \text{no pad} \\ w_i \cdot y_i & \text{pad } (x_i, y_i, w_i) \end{cases}$$



FIVE GATE EXAMPLE

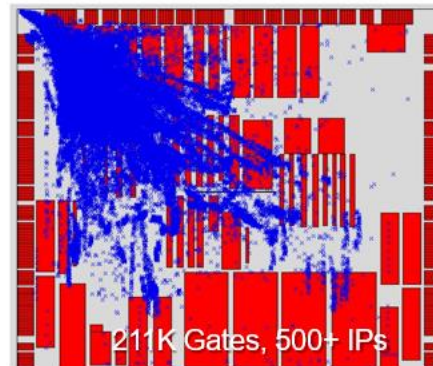
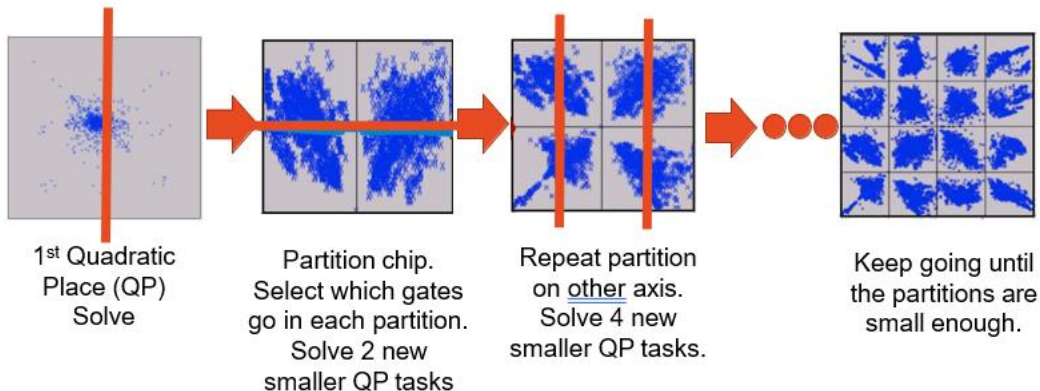
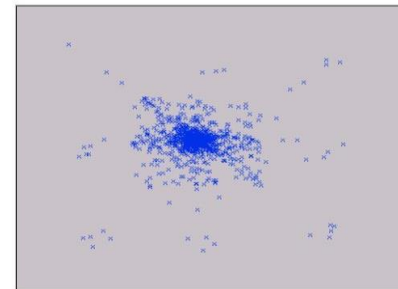


$$C = \begin{bmatrix} 0 & 1 & 10 & 0 & 0 \\ 1 & 0 & 1 & 1 & 1 \\ 10 & 1 & 0 & 1 & 0 \\ 0 & 1 & 1 & 0 & 1 \\ 0 & 1 & 0 & 1 & 0 \end{bmatrix} \quad A = \begin{bmatrix} 21 & -1 & -10 & 0 & 0 \\ -1 & 4 & -1 & -1 & -1 \\ -10 & -1 & 13 & -1 & 0 \\ 0 & -1 & -1 & 4 & -1 \\ 0 & -1 & 0 & -1 & 3 \end{bmatrix} \quad b_x = \begin{bmatrix} 0 \\ 0 \\ 1 \\ 1 \\ 0.5 \end{bmatrix} \quad b_y = \begin{bmatrix} 10 \\ 0 \\ 0 \\ 1 \\ 0 \end{bmatrix}$$



PROBLEM – GATE CLUSTERING

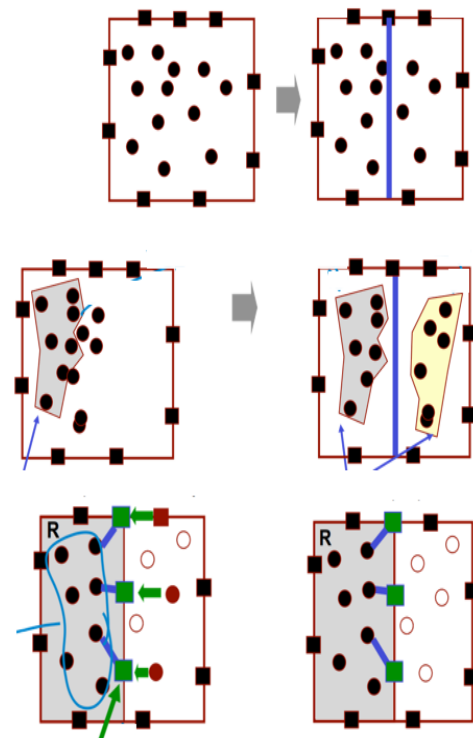
- What does a real quadratic placement look like?
 - All the gates want to be in the same place!
- How can we solve this?
 - Recursive Partitioning!



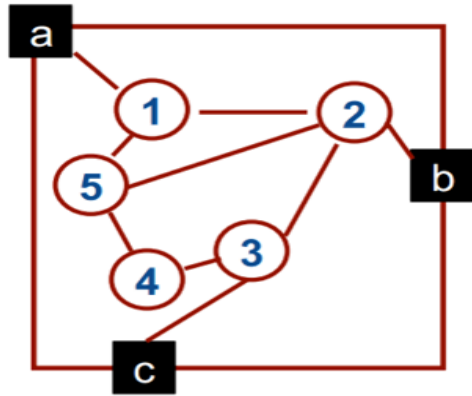
Source: Rutenbar, IBM

RECURSIVE PARTITIONING

- Partition
 - Divide the chip into new, smaller placement tasks.
 - **Divide it in half!**
- Assignment
 - Assign gates into new, smaller region.
 - **Sort the gates** and distribute to each half.
- Containment
 - Formulate new **QP matrix** that keeps gates in new regions.
 - Create “**pseudo pads**” –
 - Every gate and pad NOT inside the partition R is modeled as a pad on the boundary of R.
 - Propagate the pseudo pads to their nearest point on R.



RECURSIVE PARTITIONING EXAMPLE

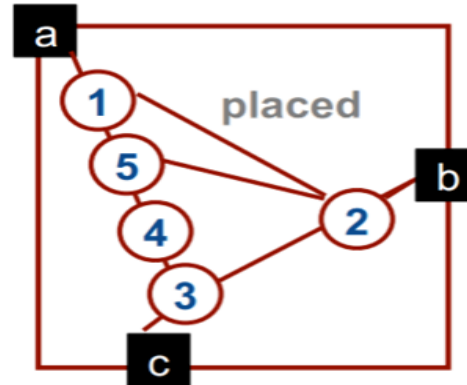


1. Initial netlist

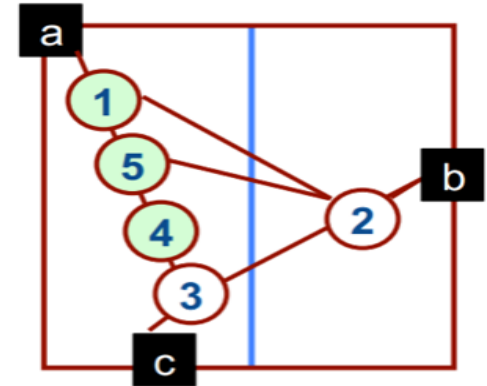
5 gates (1,2,3,4,5)

9 wires

3 pads (a,b,c)



2. Initial QP



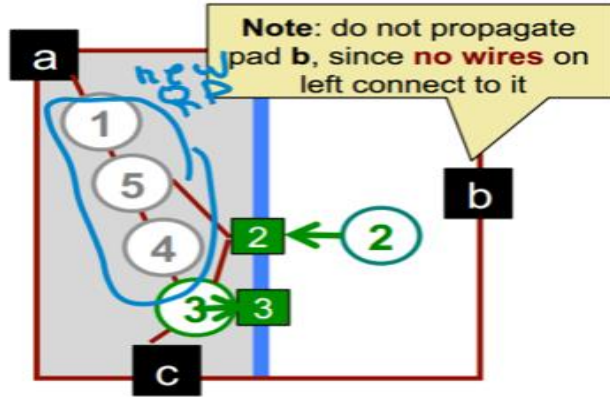
3. First partition

Sort on X:

Gate order 1 5 4 3 2

Pick: 1 5 4 on left

RECURSIVE PARTITIONING EXAMPLE

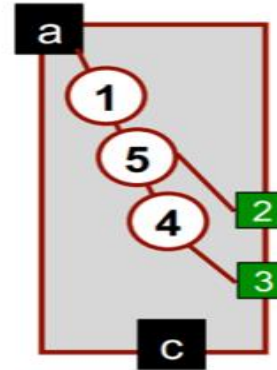


4. Propagate gates/pads

Right-side gates: 2,3

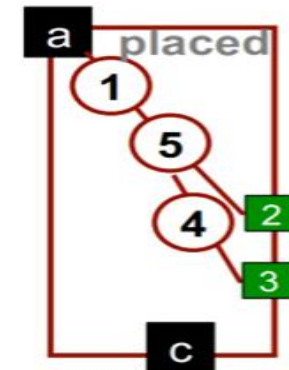
Right-side pads: b

Push to cut, using
y coordinates



5. 2nd QP input

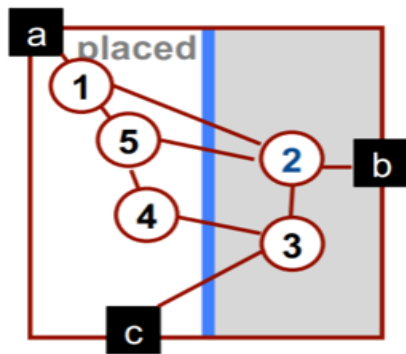
This is set up for
this new smaller
placement



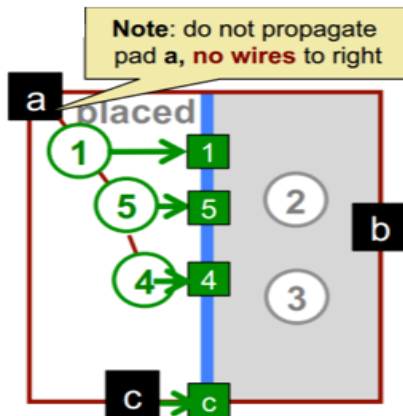
6. 2nd QP solved

New placement

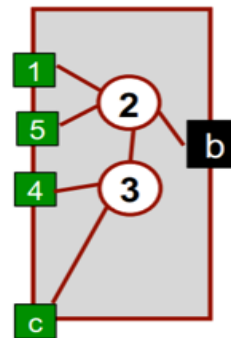
RECURSIVE PARTITIONING EXAMPLE



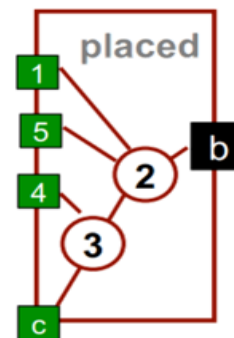
7. Left side placed.
Now, re-place
right-side gates.



8. Propagate gates/pads
This is set up for
next, new smaller
placement



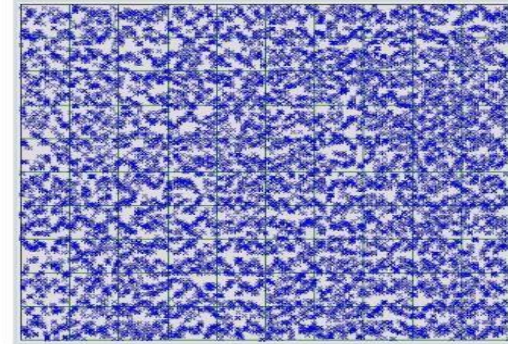
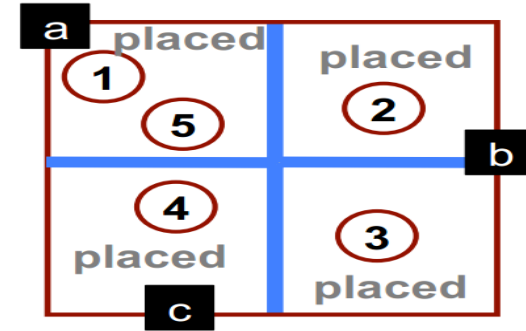
9. 3rd QP input
This is set up for
this new smaller
placement



**10. 3rd QP
solve**

PLACEMENT LEGALIZATION

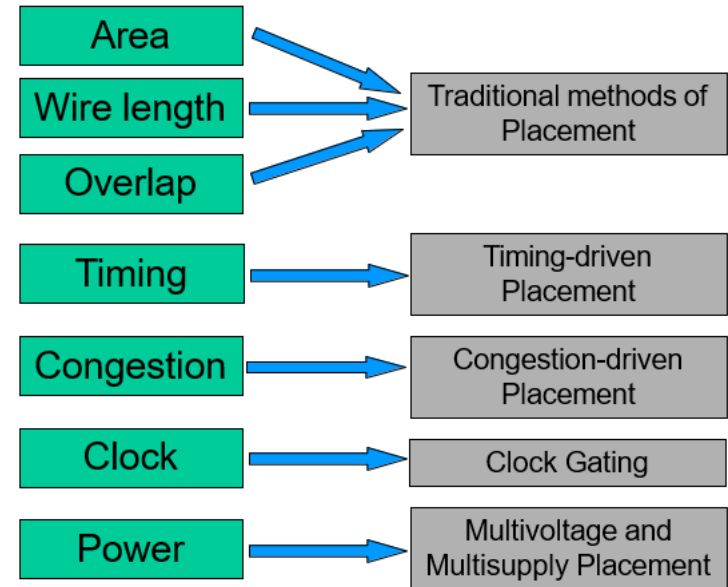
- Keep recursively partitioning...
 - Usually, continue until you have a “small” number of gates in each region (i.e., 10-100 gates)
 - In these regions we will still have overlaps
- Still need to force gates in precise rows for final result
 - This is known as “**legalization**”
 - One easy way to do this is simulated annealing!
 - Just use a low temperature to start with, so you don’t make drastic moves.



Placement in Practice

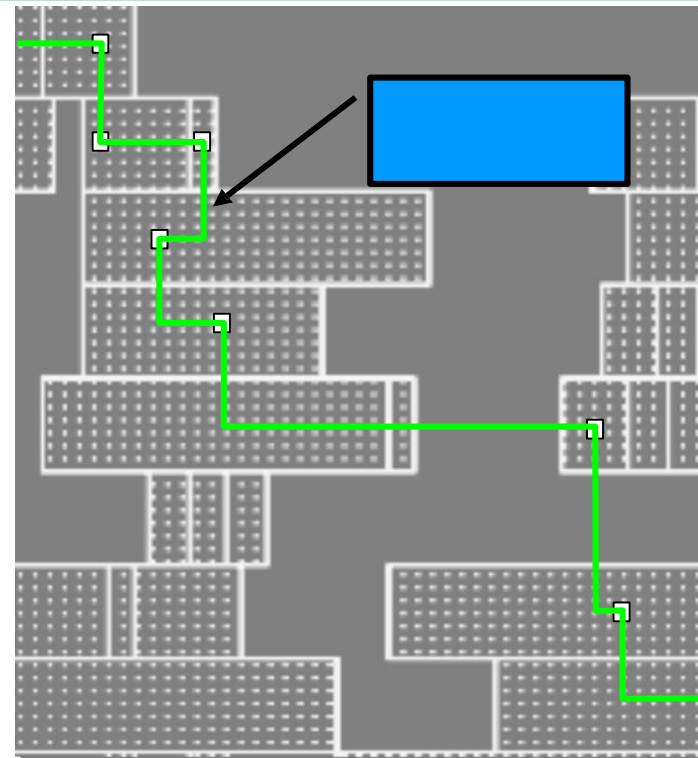
PLACEMENT STRATEGIES

- In addition to wire-length minimization, placement can be driven by two additional primary targets:
 - Timing Optimization (Timing-driven placement)
 - Congestion Minimization (Congestion-driven placement)
- Further targets include clock tree and power optimizations

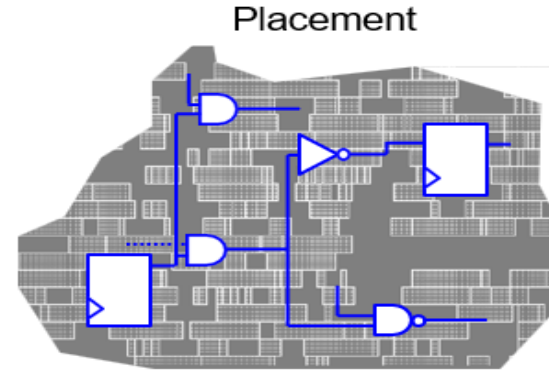
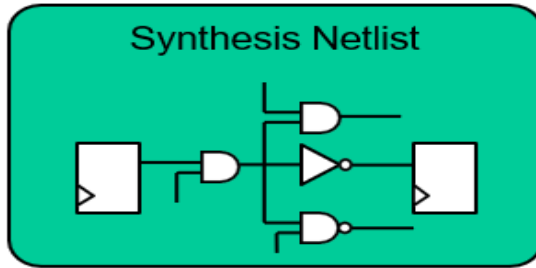


TIMING-DRIVEN PLACEMENT

- Timing-driven placement tries to place critical path cells close together to reduce net RCs and to meet setup timing
- RCs are based on Virtual Route (VR)
 - Layers are not taken into consideration
- Timing-driven placement based on Virtual Route
 - Tries to place cells along timing-critical paths close together to reduce net RCs and meet setup timing
 - Net RCs are based on Virtual Routing estimates



TIMING-DRIVEN PLACEMENT

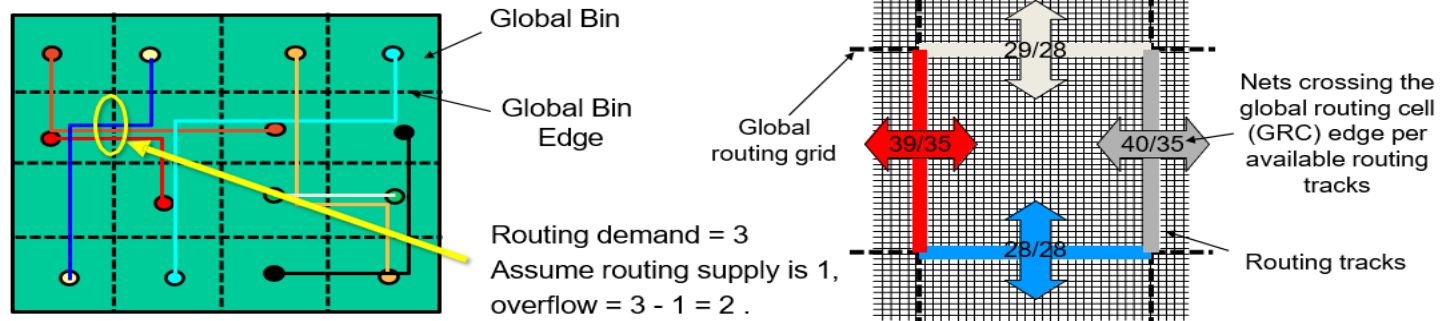


Statistically Based
Wire Load Model (WLM)

| Net Fanout | Resistance K Ω | Capacitance pF |
|---------------|--------------------------|-------------------|
| 1 | 0.0498 | 0.045 |
| 2 | 0.1295 | 0.0812 |
| 3 | 0.2092 | 0.1312 |
| 4 | 0.2888 | 0.1811 |

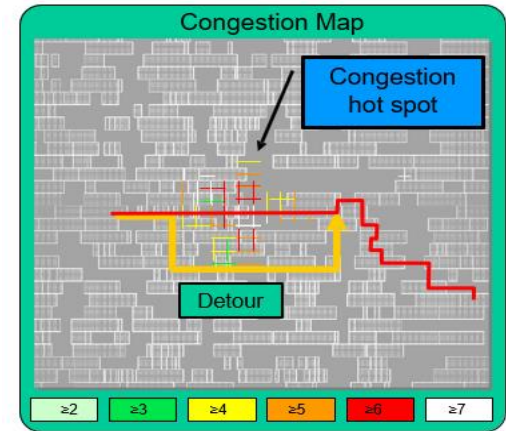
CONGESTION

- Congestion occurs when the number of required routing tracks exceeds the number of available tracks.
 - Congestion can be estimated from the results of a quick global route.
 - Global bins with routing overflow can be identified.



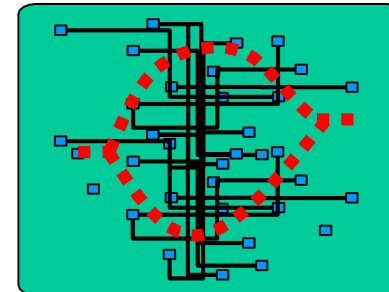
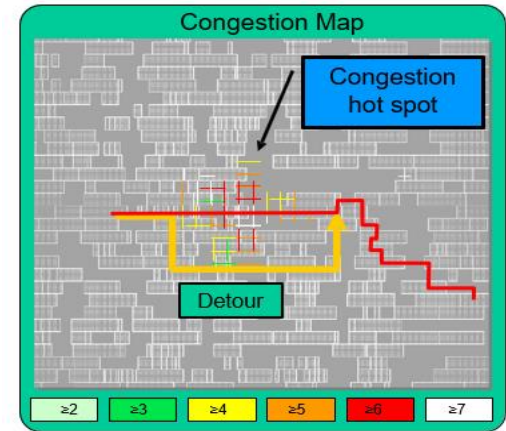
CONGESTION

- Issues with Congestion
 - If congestion is not too severe, the actual route can be detoured around the congested area
 - The detoured nets will have worse RC delay compared to the VR estimates
 - In highly congested areas, delay estimates during placement will be optimistic.



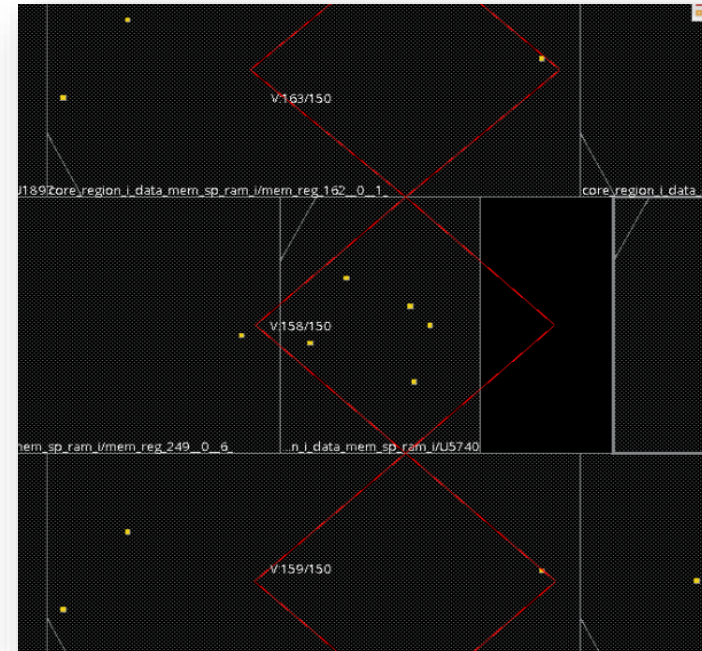
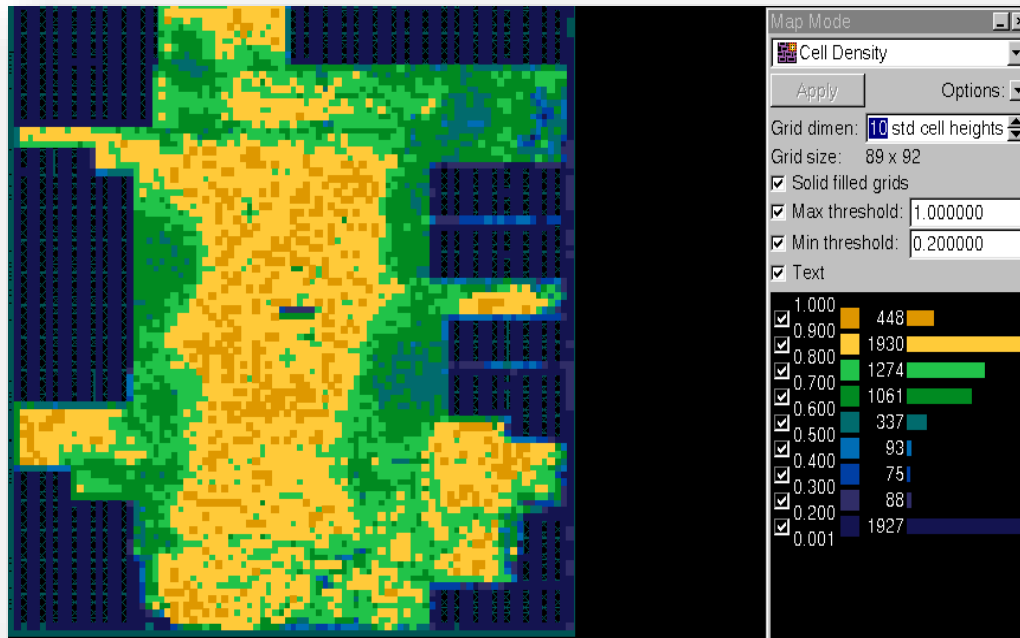
CONGESTION

- Issues with Congestion
 - If congestion is not too severe, the actual route can be detoured around the congested area
 - The detoured nets will have worse RC delay compared to the VR estimates
 - In highly congested areas, delay estimates during placement will be optimistic.
- Not routable or severely congested design
 - It is important to minimize or eliminate congestion before continuing
 - Severe congestion can cause a design to be unroutable



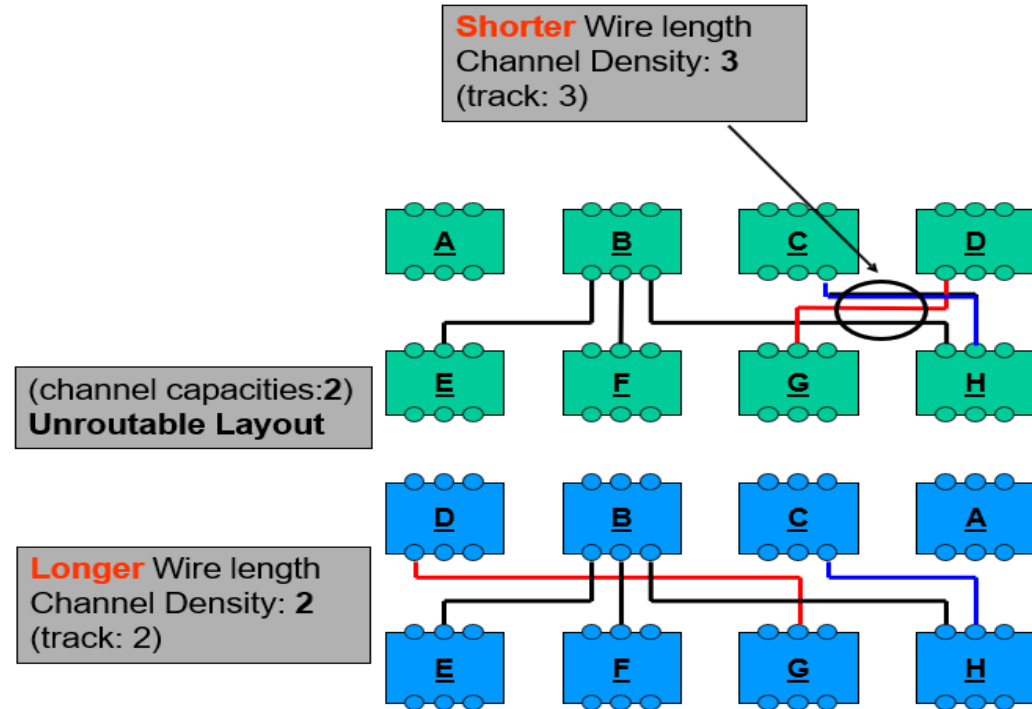
CONGESTION MAPS

- Congestion maps are displayed by the backend tool to help us evaluate the total congestion, identify and fix congestion hot spots.



CONGESTION-DRIVEN PLACEMENT

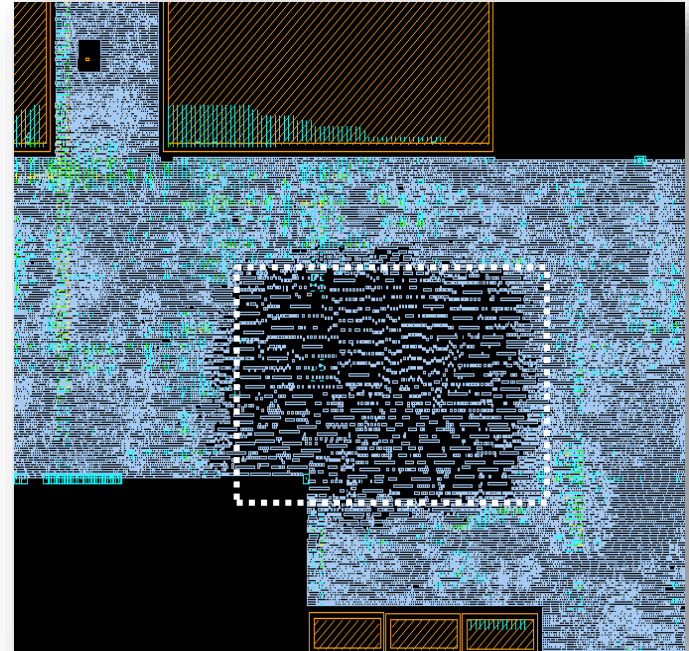
- Congestion Reduction
 - The tool tries to evaluate congestion hotspots and spread the cells (lower utilization) in the area to reduce congestion.
 - The tool can also choose cell location based on congestion, rather than wire-length.



STRATEGIES TO FIX CONGESTION

Modify the floorplan:

- Mark areas for low utilization.
- Top-level ports
 - Changing to a different metal layer
 - Spreading them out, re-ordering or moving to other sides
- Macro location or orientation
 - Alignment of bus signal pins
 - Increase of spacing between macros
 - Add blockages and halos



STRATEGIES TO FIX CONGESTION

Modify the floorplan:

- Core aspect ratio and size
 - Making block taller to add more horizontal routing resources
 - Increase of the block size to reduce overall congestion
- Power grid
 - Fixing any routed or non-preferred layers

Thank you!