# Assignment 1

## Part 1: Create an instance

#### ${\bf City Instance}$

cityID	name	country
1	Toronto	Canada
2	Montreal	Canada

#### TripInstance

tripID	startCity	length
1	1	4

#### ${\bf Transport Activity Instance}$

aID	destCity	mode
4	2	train

#### Tour Activity Instance

aID	name	duration	extra
1	ROM	5	False
2	CN Tower	6	False
3	Toronto Zoo	11	False
5	Old Montreal	5	False
6	Mont Royal	6	True

#### It in erary Instance

tripID	day	step	cityID	activityID
1	1	1	1	1
1	1	2	1	2
1	2	1	1	3
1	3	1	1	4
1	4	1	2	5
1	4	2	2	6

#### ${\bf StaffInstance}$

staffID	name	hireDate
1	Me	20240101

#### ${\bf Traveller Instance}$

tID	name	email	citizenship
1	John Doe	a@mail.com	Canada
2	Jane Doe	b@mail.com	Canada
3	Lorem Is	c@mail.com	Canada

#### ${\bf Booking Instance}$

bID	tripID	startDate	traveller	bookedBy	price
1	1	20240131	1	1	500
2	1	20240131	2	1	500
3	1	20240131	3	1	500

#### ExtraBookingInstance

bID	activity	price
3	6	200

## Part 2: Give the output of a query

#### Query Output

duration
5
6
11

# Part 3: Violating a constraint

CityInstance

### ${\bf Trip Instance}$

### ${\bf Staff Required Instance}$

cityID	name	country
1	Toronto	Canada

tripID	startCity	length
1	1	1

activityID	role
1	Guide

Tour Activity Instance

aID	name	duration	extra	
1	CN Tower	6	False	

#### It in erary Instance

tripID	day	step	cityID	activityID
1	1	1	1	1

StaffInstance

staffID	name	hireDate	
1	Me	20240101	

TravellerInstance

tID	name email		citizenship	
1	John Doe	a@mail.com	Canada	

#### ${\bf Booking Instance}$

bID	tripID	startDate	traveller	bookedBy	price
1	1	20240131	1	1	500

### Part 4: Queries

1. – Every country and tripID tuple where the trip visited the country.

 $Countries(country, tripID) := \prod_{country, tripID}(City \bowtie Itinerary)$ 

- Every tripID that has visited at least three countries.

AtLeastThrice(tripID) :=

$$\Pi_{T1.tripID} \left[ \sigma_{T1.tripID=T2.tripID=T3.tripID} \left( \rho_{T1}Countries \times \rho_{T2}Countries \times \rho_{T3}Countries \right) \right]$$

Every tripID that has visited at least four countries.

AtLeastFour(tripID) :=

$$\Pi_{T1.tripID} \begin{bmatrix} \sigma_{T1.tripID=T2.tripID} \\ = T3.tripID=T4.tripID \\ \land \\ T1.country < T2.country \\ < T3.country < T4.country \end{bmatrix} \left( \rho_{T1}Countries \times \rho_{T2}Countries \times \rho_{T3}Countries \times \rho_{T4}Countries \right) \end{bmatrix}$$

- Every tripID that has visited exactly three countries.

ExactlyThree(tripID) := AtLeastThrice - AtLeastFour

- The tripID and day of every day in any trip.

 $TripDays(tripID, day) := \Pi_{tripID, day}Itinerary$ 

- The tripID and day of every day that is not the last day in a trip.

$$NotLastDays(tripID, day) := \underset{\text{T1.day}}{\Pi_{\text{T1.tripID}}}, (\sigma_{\text{T1.tripID}} = \underset{\text{T2.tripID}}{\text{T2.tripID}} (\rho_{\text{T1}} \text{TripDays} \times \rho_{\text{T2}} \text{TripDays}))$$

- The tripID and day of every day that is the last day in a trip.

LastDay(tripID, day) := TripDays - NotLastDays

- The tripID and step of every step on the last day of any trip.

 $LastDaySteps(tripID, day, step) := \Pi_{tripID, day, step}(LastDay \bowtie Itinerary)$ 

- The tripID and step of every step that is not the last step on the last day in a trip.

$$NotLastStep(tripID, day, step) := \prod_{\substack{\text{T1.tripID}, \\ \text{T1.step} \\ \text{T1.step}}} (\sigma_{\text{T1.tripID}} = \max_{\substack{\text{T2.tripID} \\ \text{T1.step} \\ \text{T2.step}}} (\rho_{\text{T1}} \text{LastDaySteps} \times \rho_{\text{T2}} \text{LastDaySteps}))$$

- The tripID and step of every last step on the last day in a trip.

LastStep(tripID, day, step) := LastDaySteps - NotLastStep

- The tripID, citvID, and country of every trip's start city.

 $Renamed(tripID, cityID, country) := \prod_{tripID, cityID, country} (\rho_{T1(tripID, cityID, length)} Trip) \bowtie City$ 

- The tripID, cityID, and country of the start city in a trip that visits exactly three countries.

 $Start(tripID, startCityID, startCountry) := \Pi_{tripID, cityID, country}(Itinerary \bowtie ExactlyThree \bowtie Renamed)$ 

- The tripID, cityID, and country of the end city in a trip that visits exactly three countries.

 $End(tripID, endCityID, endCountry) := \Pi_{tripID, cityID, country}(Itinerary \bowtie ExactlyThree \bowtie LastStep \bowtie City)$ 

 $Start \bowtie End$ 

2. – The cityID of every city which is not part of any trip.

$$NoTrip(cityID) := \Pi_{cityID}City - \Pi_{cityID}Itinerary$$
  
 $\Pi_{name,country}(NoTrip \bowtie City)$ 

- 3. Cannot be expressed.
- 4. Cannot be expressed.
- 5. The bID, activity, and price of every extra booking that is not the most expensive.

NotMax(bID, activity, price) :=

$$\Pi_{T1.bID,T1.activity,T1.price} \left[ \sigma_{T1.bID \neq T2.bID} \left( \rho_{T1}ExtraBooking \times \rho_{T2}ExtraBooking \right) \right]$$

- The bID, activity, and price of every extra booking with the maximum price.

$$Max(bID, activity, price) := ExtraBooking - NotMax$$

- The bID, activity, and price of every extra booking that is that is not the second most expensive.

NotSecond(bID, activity, price) :=

$$\Pi_{T1.bID,T1.activity,T1.price} \left[ \sigma_{T1.bID \neq T2.bID} \left( \rho_{T1} NotMax \times \rho_{T2} NotMax \right) \right]$$

- The bID, activity, and price of every extra booking with the second greatest price.

Second(bID, activity, price) := ExtraBooking - Max - NotSecond

$$\Pi_{tripID,activity,price} \bigg[ \Big( Max \cup Second \Big) \bowtie Booking \bigg]$$

6. – The staffID of every staff hired before 2020.

$$Before2020(staffID) := \prod_{staffID}(\sigma_{hireDate < 20200101}Staff)$$

- The staffID and tripID of every 'guide' assignment to a trip where the staff was hired before 2020.

$$Guide(staffID, tripID) := \Pi_{staffID, tripID} \Big( \sigma_{role='guide'} StaffAssignment \bowtie Before 2020 \Big)$$

- Every possible combination of staffID and tripID where the staff was hired before 2020.

$$EveryPossible(staffID, tripID) := \Pi_{staffID}Before2020 \times \Pi_{tripID}Trip$$

- The staffID of the staff who were not assigned as 'guide' to every trip.

$$Missing(staffID) := \Pi_{staffID}(EveryPossible - Guide)$$

Before 2020 - Missing

7. Note: I solved this before the clarification that returning to a city previously visited at an earlier date counts as visiting a new city.

$$\Pi_{tripID}Itinerary - \Pi_{T1.tripID} \left[ \sigma_{T1.tripID=T2.tripID} \left( \rho_{T1}Itinerary \times \rho_{T2}Itinerary \right) \right]$$

$$T1.dau \stackrel{\wedge}{\sim} T2.dau$$

8. – All bIDs and tripIDs where the booking does not have the earliest start date for the trip.

$$NotEarliestBooking(bID, tripID) := \Pi_{T2.bID, T2.tripID} \begin{bmatrix} \sigma & _{T1.tripID=T2.tripID} & \left( \rho_{T1}Booking \times \rho_{T2}Booking \right) \\ \sigma & _{T1.startDate}^{\land} & \sigma & \sigma & \sigma \\ \sigma & _{T1.startDate}^{\land} & \sigma & \sigma & \sigma \\ \sigma & _{T2.startDate}^{\land} & \sigma & \sigma & \sigma \\ \sigma & _{T2.startDate}^{\land} & \sigma & \sigma & \sigma \\ \sigma & _{T3.tripID=T2.tripID}^{\land} & \sigma & \sigma & \sigma \\ \sigma & _{T3.tripID=T2.tripID}^{\land} & \sigma & \sigma & \sigma \\ \sigma & _{T3.tripID=T2.tripID}^{\land} & \sigma & \sigma & \sigma \\ \sigma & _{T3.tripID=T2.tripID}^{\land} & \sigma & \sigma & \sigma \\ \sigma & _{T3.tripID=T2.tripID}^{\land} & \sigma \\ \sigma & _{T3.tripID=T2.tripID=T2.tripID}^{\land} & \sigma \\ \sigma & _{T3.tripID=T2.tripID=T2.tripID=T2.tripID=T2.tripID=T2.tripID=T2.tripID=T2.tripID=T2.tripID=T2.tripID=T2.tripID=T2.tripID=T2.tripID=T2.tripID=T2.tripID=T2.tripID=T2.tripID=T2.tripID=T2.tr$$

– All bIDs and tripIDs where the booking has the earliest start date for the trip.

 $EarliestBookings(bID, tripID) := \Pi_{bID, trivID}Booking - NotEarliestBooking$ 

- The bIDs of all earliest bookings where their trips are booked by at least two other travellers at later start dates.

 $AtLeastThreePeople(bID) := \Pi_{bID}EarliestBookings \cap$ 

$$astThreePeople(bID) := \Pi_{bID}EarliestBookings \cap$$

$$\Pi_{T1.bID} \begin{bmatrix} \sigma & _{T1.tripID=T2.tripID=T3.tripID} & \left(\rho_{T1}Booking \times \rho_{T2}Booking \times \rho_{T3}Booking\right) \end{bmatrix}$$

$$T1.startDate < T2.startDate$$

$$T1.startDate < T3.startDate < T3.traveller < T3.traveller$$

– All travellers who are not influencers.

 $NotInfluencers(traveller) := \Pi_{traveller}(\Pi_{traveller,bID}Booking - (\Pi_{traveller}Booking \times AtLeastThreePeople))$ 

 $\Pi_{name.email}((\Pi_{traveller}Booking - NotInfluencers) \bowtie Traveller)$ 

- 9. Cannot be expressed.
- 10.  $\Pi_{T1.staffID,T2.staffID} \left[ \sigma_{T1.staffID < T2.staffID} \left( \rho_{T1}StaffAssignment \times \rho_{T2}StaffAssignment \right) \right]$   $T1.tripID \stackrel{\wedge}{=} T2.tripID$ T1.startDate = T2.startDate

## Part 5: Additional integrity constraints

1. – The tripID and day of every first day of a trip listed in Itinerary.

$$FirstDay(tripID, day) := \Pi_{tripID, day}Itinerary -$$

$$\Pi_{T2.tripID,T2.day} \left[ \sigma_{T1.tripID=T2.tripID} \left( \rho_{T1}Itinerary \times \rho_{T2}Itinerary \right) \right]$$

$$\Pi_{tripID}(\sigma_{day>1}FirstDay) \cup \Pi_{tripID}\Bigg(\Pi_{tripID,day}Itinerary - \Pi_{tripID,day}(\sigma_{day=1}Itinerary) - \Pi_{tripID,day$$

$$\Pi_{T2.tripID,T2.day} \left[ \sigma_{T1.tripID=T2.tripID} \left( \rho_{T1}Itinerary \times \rho_{T2}Itinerary \right) \right] \right) = \emptyset$$

- 2.  $\rho_{T1(activityID)}(\Pi_{activity}ExtraBooking) \Pi_{activityID}Itinerary = \emptyset$
- 3.  $\Pi_{traveller,country}[Booking \bowtie Itinerary \bowtie City] -$

$$\rho_{T2(traveller,country)}(\Pi_{tID,citizenship}Traveller) - \Pi_{traveller,country}(\sigma_{expiry>startDate}(Visa \bowtie Booking)) = \emptyset$$

4. 
$$\Pi_{T1.tripID} \begin{bmatrix} \sigma & T1.tripID=T2.tripID=T3.tripID \\ T1.day=T2.day=T3.day \\ & & & & & & & & \\ T1.country$$

$$\left(\rho_{T1}(City\bowtie Itinerary)\times\rho_{T2}(City\bowtie Itinerary)\times\rho_{T3}(City\bowtie Itinerary)\right)\right]=\emptyset$$

5. – The tripID, day, and step of every transport activity in the itinerary.

TransportItinerary(tripID, day, step) :=

$$\Pi_{tripID,day,step,activityID}(Itinerary\bowtie(\rho_{R1(activityID)}\Pi_{aID}TransportActivity))$$

– The tripID, day, and step of every transport activity that is the last step of a day in a trip.

LastStepTransport(tripID, day, step) := TransportItinerary - Transport

$$\Pi_{T1.tripID,T1.day,T1.step} \left[ \sigma_{T1.tripID=T2.tripID} \left( \rho_{T1}Itinerary \times \rho_{T2}Itinerary \right) \right]$$

$$\uparrow T1.day = T2.day$$

$$\uparrow T1.step < T2.step$$

$$\Pi_{T1.tripID} \left[ \sigma_{T1.tripID=T2.tripID} \left( \rho_{T1} TransportItinerary \times \rho_{T2} TransportItinerary \right) \right] \cup \prod_{\substack{T1.day = T2.day \\ T1.step+1=T2.step}} \left( \rho_{T1} TransportItinerary \times \rho_{T2} TransportItinerary \right) \right]$$

$$\Pi_{T3.tripID} \left[ \sigma_{T3.tripID=T4.tripID} \left( \rho_{T3} (\Pi_{tripID,day} LastStepTransport) \times \rho_{T4} (\sigma_{step=1} TransportItinerary)) \right) - \emptyset$$

6. Cannot be expressed.