

## Report

### Time Complexities:

(for all of these,  $n$  represents the number of nodes in the tree)

Insert:  $O(\log(n))$  because you only compare ID at each level of the tree to find where it fits, which takes  $\log(n)$  time. Then you rebalance your way back up the tree, also taking up to  $\log(n)$ , but these added together just gives you  $2\log(n)$  and the constant can be dropped.

remove:  $O(\log(n))$  It first calls the search-with-ID function in order to make sure the node exists, which takes  $\log(n)$  (see below), then you have to delete which is  $O(1)$ , and then trace your way back up the tree recalculating the heights, which also takes  $\log(n)$ . So, reducing  $(O(2\log(n) + 1))$  gives  $O(\log(n))$

search with ID:  $O(\log(n))$  because you only compare at each level of the balanced tree until you find it

search with Name:  $O(n)$  because it searches in a preorder traversal, and worst case it could be the farthest right node, thus having to hit every node before it.

printPreorder, printPostorder, printInorder:  $O(n)$ . They have to visit every node in the tree in order to print them.

removeInorder:  $O(n)$ . Worst case, if the last index is called, it would have to traverse through every node in order, which is an  $O(n)$  operation. It also rebalances which is  $O(\log(n))$

printLevelCount:  $O(n)$ , it goes through level by level hitting each node, queueing up each node's children, and tracking when it goes down a level. Therefore since it hits every node it is  $O(n)$

I learned a ton about practical implementation of an AVL tree. I learned things like how to implement several different kinds of traversals, and the use cases for each. I thought it was really cool how easy it is to do a level order traversal with the queue, as well as the other traversals with very simple recursion. The most interesting things I learned were the remove and insert methods. These were the most challenging tasks for me, as I struggled to conceptualize what was happening and trace the recursion stack of which nodes ended up pointing where when I tried to do rotations. If I could go back, I would have spent more time beforehand understanding the rotations and how and why they work. I had a weak grasp of the concept going into the project, and I ended up paying for it by spending a lot of time debugging those functions.