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#include <iostream>
#include <cmath>
#include <vector>
#include<stdlib.h>
#include<algorithm>
#include "Point.h"
using namespace std;
bool sortByX (Point a, Point b) {
            return (a.getY() < b.getY());
bool sortByY (Point a, Point b) {
            return (a.getX() \le b.getX());
void printToPPM (int sizeGrid, int numPoints, vector<Point> scaled, Point firstPointScaled, Point
secondPointScaled){
            int grid [sizeGrid][sizeGrid];
            for (int row = 0; row < sizeGrid; row++){
                        for (int col = 0; col \leq sizeGrid; col++){
                                     grid[row][col] = 1;
            for (int index = 0; index < numPoints; index++){
                        grid[int(scaled[index].getX())][int(scaled[index].getY())] = 0;
            for (int x = firstPointScaled.getX()-1; x \le firstPointScaled.getX()+1; x++){
                        for(int y = firstPointScaled.getY()-1; y \le firstPointScaled.getY()+1; y++){
                                     grid[x][y]=2;
            for (int x = \text{secondPointScaled.getX}()-1; x \le \text{secondPointScaled.getX}()+1; x++){
                        for(int y = \text{secondPointScaled.getY}()-1; y \le \text{secondPointScaled.getY}()+1; y++){
                                     grid[x][y]=2;
            sort (scaled.begin(), scaled.end(), sortByX);
            cout << "P3" << sizeGrid << "" << sizeGrid << "1" << endl;
            for (int row = 0; row \leq sizeGrid; row++){
                        for (int col = 0; col \leq sizeGrid; col++){
                                     if (grid[row][col] == 1)
                                                 cout << "1 1 1 "; //white
                                     else if (grid[row][col] == 0)
                                                 cout << "0 0 0 "; //black
                                     else if (grid[row][col] == 2)
                                                 cout << "0 0 1 "; //blue
                        cout << endl;
double calculateDistance(Point first, Point second){
            double distance = sqrt(pow(second.getX()-first.getX(),2) + pow(second.getY()-first.getY(),2));
            return (distance);
```

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vector<Point> bruteForce(vector<Point> points){
           int numPoints = points.size();
            double minDistance = 2.0;
            Point firstPoint = Point();
            Point secondPoint = Point();
            for (int first = 0; first < numPoints-1; first++){
                        for (int second = first+1; second < numPoints; second++){
                                    double distance = calculateDistance(points[first], points[second]);
                                    if (distance < minDistance){</pre>
                                                firstPoint = points[first];
                                                secondPoint = points[second];
                                                minDistance = distance;
            vector<Point> firstAndSecond;
            firstAndSecond.push back(firstPoint);
            firstAndSecond.push_back(secondPoint);
            return (firstAndSecond);
vector<Point> recursiveDivide(vector<Point> points){
            int pointsLength = points.size();
            if (pointsLength==3){
                        return (bruteForce(points));
            if (pointsLength==2){
                        return points;
            int midpoint = int(pointsLength/2);
            vector<Point> leftpoints;
            vector<Point> rightpoints;
            for (int index = 0; index < midpoint; index++){
                        leftpoints.push back(points[index]);
            for (int index = midpoint; index < pointsLength; index++){
                        rightpoints.push back(points[index]);
            vector<Point> leftpair = recursiveDivide(leftpoints);
            vector<Point> rightpair = recursiveDivide(rightpoints);
            vector<Point> smallerpair;
            double leftdistance = calculateDistance(leftpair[0], leftpair[1]);
            double rightdistance = calculateDistance(rightpair[0], rightpair[1]);
            double mindistance = 2;
            if (leftdistance < rightdistance){</pre>
                        smallerpair = leftpair;
                        mindistance = leftdistance;
            else{
                        smallerpair = rightpair;
                        mindistance = rightdistance;
            vector<Point> straddling;
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for (int index = 0; index < pointsLength; index++){
                       if (abs(points[index].getX()-points[midpoint].getX())<mindistance){
                                   straddling.push back(points[index]);
            if (straddling.size()>2){
                       vector<Point> straddlingpair = bruteForce(straddling);
                       if (calculateDistance(straddlingpair[0], straddlingpair[1]) < mindistance)
                                   return (straddlingpair);
            if (straddling.size()==2){
                       if (calculateDistance(straddling[0], straddling[1]) < mindistance)
                                   return (straddling);
           return (smallerpair);
class HashEntry {
private:
            vector<Point> key;
            double value;
public:
           HashEntry(vector<Point> key, double value) {
                       this->key = key;
                       this->value = value;
            vector<Point> getKey() {
                       return key;
            double getValue() {
                       return value;
};
const int tableSize = 128;
class HashMap {
private:
           HashEntry **table;
public:
           HashMap() {
                       table = new HashEntry*[tableSize];
                       for (int i=0; i<tableSize; i++){
                                   table[i] = NULL;
            double get(vector<Point> key) {
                       int hash = (key % tableSize);
                       while (table[hash] != NULL && table[hash]->getKey() != key)
                                   hash = (hash+1)\%tableSize;
                       if(table[hash] == NULL)
                                   return -1;
                       else
                                   return table[hash]->getValue();
            void put(vector<Point> key, double value) {
                       int hash = (key%tableSize);
                       while(table[hash] != NULL && table[hash]->getKey() != key)
                                   hash = (hash+1)\%tableSize;
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if (table[hash] != NULL)
                                   delete table[hash]:
                       table[hash] = new HashEntry(key,value);
           ~HashMap() {
                       for(int i=0; i<tableSize; i++){
                                   if (table[i] != NULL)
                                              delete table[i];
};
vector<Point> sieveAlgorithm(vector<Point> points){
                       Go through all points
                                   pick randpoint, store dist to each point
                                  min distance is D
                       take D, D/3 -> size of mesh
                                   divide unit square into D/3
                                   loop through points, where point goes into map
                                              which box it goes in, store where that goes in
                       once you have hashtable
                                   with every box label points to all points in box
                                   go through hash, if all boxes around it are empty and that box just has box
                       Recur until subset becomes 0
                                   look at D you used
                                              last seive algorithm
                                                          build new hash table
                                                          go through each point, find points
                                                          find points in neighborhood, brute force
                                              compare min distances
           //std::map <int,int> pointDistDict;
           int pointsLength = points.size();
           if (pointsLength==3){
                       return (bruteForce(points));
           if (pointsLength==2){
                       return points;
           HashMap randPointHashDict = new HashMap();
           double D = 2.0;
           srand (time(NULL));
           for (int index=0; index<pointsLength; index++)
                       double xValue = (double(rand()) / double(RAND MAX));
                       double yValue = (double(rand()) / double(RAND MAX));
                       vector<Point> randPoint = Point(xValue, yValue);
                       double distBet = calculateDistance(points[index],randPoint);
                       randPointHashDict.put(points[index],distBet);
                       if(distBet<D){
                         D = distBet;
           double miniD = D/3.0;
           /*vector<Point> newLeftPointsX(pointsLength);
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vector<Point> newMidPointsX(pointsLength);
vector<Point> newRightPointsX(pointsLength);
for(int index=0; index<pointsLength; index++){</pre>
  oldXVal = points[index].getX();
  oldYVal = points[index].getY();
  if(oldXVal < miniD){</pre>
    newLeftPointsX[index] = points[index];
  else if(oldXVal > miniD && oldXVal < miniD*2){
    newMidPointsX[index] = points[index];
  else {
    newRightPointsX[index] = points[index];
vector<Point> newBottomPointY(pointsLength);
vector<Point> newMidPointsY(pointsLength);
vector<Point> newTopPointsY(pointsLength);
for(int index=0; index<pointsLength; index++){
  oldXVal = points[index].getX();
  oldYVal = points[index].getY();
  if(oldYVal < miniD){
    newBottomPointsY[index] = points[index];
  else if(oldYVal > miniD && oldYVal < miniD*2){
    newMidPointsY[index] = points[index];
  else {
    newTopPointsY[index] = points[index];
vector<Point> newTopLeftPoints(pointsLength);
vector<Point> newTopMidPoints(pointsLength);
vector<Point> newTopRightPoints(pointsLength);
vector<Point> newMidLeftPoints(pointsLength);
vector<Point> newCenterPoints(pointsLength);
vector<Point> newMidRightPoints(pointsLength);
vector<Point> newBottomLeftPoints(pointsLength);
vector<Point> newBottomMidPoints(pointsLength);
vector<Point> newBottomRightPoints(pointsLength);
for(int index=0; index<pointsLength; index++){
  oldXVal = points[index].getX();
  oldYVal = points[index].getY();
  if(oldXVal<0.5-miniD){
    if(oldYVal<0.5-miniD){
       newTopLeftPoints[index] = points[index];
    else if(oldYVal>0.5+miniD){
       newBottomLeftPoints[index] = points[index];
    else{
       newMidLeftPoints[index] = points[index];
  else if(oldXVal>0.5+miniD){
    if(oldYVal<0.5-miniD){
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newTopRightPoints[index] = points[index];
       else if(oldYVal>0.5+miniD){
         newBottomRightPoints[index] = points[index];
       else{
         newMidRightPoints[index] = points[index];
    else {
       if(oldYVal<0.5-miniD){
         newTopMidPoints[index] = points[index];
       else if(oldYVal>0.5+miniD){
         newBottomMidPoints[index] = points[index];
      else{
         newCenterPoints[index] = points[index];
  for(int index=0; index<pointsLength; index++){
    randPointHashDict.get(points[index]);
    centerLength = newCenterPoints.size();
    if(newTopLeftPoints.size()==0 && newTopMidPoints.size()==0 && newTopRightPoints.size()==0 &&
newMidLeftPoints.size()==0 && newMidRightPoints.size()==0 && newBottomLeftPoints.size()==0 &&
newBottomMidtPoints.size()==0 && newBottomRightPoints.size()==0){
                                  for(int i=0; i<centerLength; i++){
                                             vector<Point> brutePoints(centerLength);
                                             brutePoints[i] = newCenterPoints[i];
                                  return bruteForce(brutePoints);
                      else{
                                  return sieveAlgorithm(newCenterPoints);
int main(void) {
           int numPoints = 3;
           while (true) {
                      vector<Point> values(numPoints);
                      sort (values.begin(), values.end(), sortByX);
                      srand (time(NULL));
                      for (int point = 0; point < numPoints; point++){
                                  double xValue = (double(rand()) / double(RAND MAX));
                                  double yValue = (double(rand()) / double(RAND MAX));
                                  values[point] = Point(xValue, yValue);
                      vector<Point> pairBrute;
                      vector<Point> pairRecursive;
                      vector<Point> pairSieve;
                      cout << numPoints << "\t";</pre>
                      const clock t initialTime = clock();
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pairBrute = bruteForce(values):
                       cout << float (clock () - initialTime ) / CLOCKS PER SEC << "\t\t";
                       const clock t initialTime2 = clock();
                       pairRecursive = recursiveDivide(values);
                       cout << float( clock () - initialTime2 ) / CLOCKS PER SEC << "\t\t";</pre>
     const clock t initialTime3 = clock();
                       pairSieve = sieveAlgorithm(values);
                       cout << float( clock () - initialTime3 ) / CLOCKS PER SEC << endl;</pre>
                       if (numPoints > 10000)
                                   numPoints *= 1.25:
                       else if (numPoints > 5000)
                                   numPoints *= 1.5;
                       else
                                   numPoints *= 2;
                       Point firstBrute = pairBrute[0];
                       Point secondBrute = pairBrute[1];
                       Point firstRecursive = pairRecursive[0];
                       Point secondRecursive = pairRecursive[1];
                       int sizeGrid = 500;
                       vector<Point> scaled(numPoints);
                       for (int index = 0; index < numPoints; index++) {
                                   Point unscaled = values[index];
                                   scaled[index] = Point(double(int(unscaled.getX()*sizeGrid)),
double(int(unscaled.getY()*sizeGrid)));
                       Point firstBruteScaled = Point(double(int(firstBrute.getX()*sizeGrid)),
double(int(firstBrute.getY()*sizeGrid)));
                       Point secondBruteScaled = Point(double(int(secondBrute.getX()*sizeGrid)),
double(int(secondBrute.getY()*sizeGrid)));
                       Point firstRecursiveScaled = Point(double(int(firstRecursive.getX()*sizeGrid)),
double(int(firstRecursive.getY()*sizeGrid)));
                       Point secondRecursiveScaled = Point(double(int(secondRecursive.getX()*sizeGrid)),
double(int(secondRecursive.getY()*sizeGrid)));
                       cout << "Brute:" << endl;
                       cout << firstBruteScaled << endl;</pre>
                       cout << secondBruteScaled << endl;</pre>
                       cout << "Recursive:" << endl;
                       cout << firstRecursiveScaled << endl;</pre>
                       cout << secondRecursiveScaled << endl;</pre>
                       //printToPPM(sizeGrid, numPoints, scaled, firstRecursiveScaled, secondRecursiveScaled);
            }
}
```