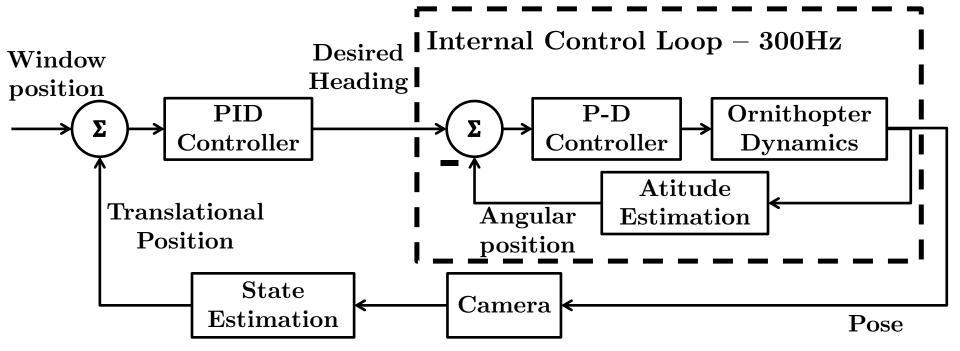
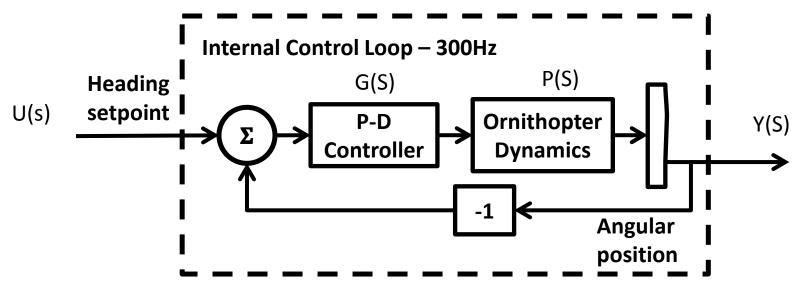
#### External Control Loop – 10Hz



#### Internal control loop



Yaw dynamics

$$\begin{bmatrix} \dot{\theta} \\ \dot{\omega} \end{bmatrix} = \begin{bmatrix} 0 & 1 \\ 0 & 0 \end{bmatrix} \begin{bmatrix} \theta \\ \omega \end{bmatrix} + \begin{bmatrix} 0 \\ \frac{r}{I_{zz}} \end{bmatrix} u$$

$$G(s) = \frac{K_D s^2 + K_P s + K_I}{s} = \frac{0.2s^2 + 2.0s}{s}$$

$$P(s) = \frac{I_{ZZ}}{S^2} \qquad M = \frac{r}{I_{ZZ}}$$

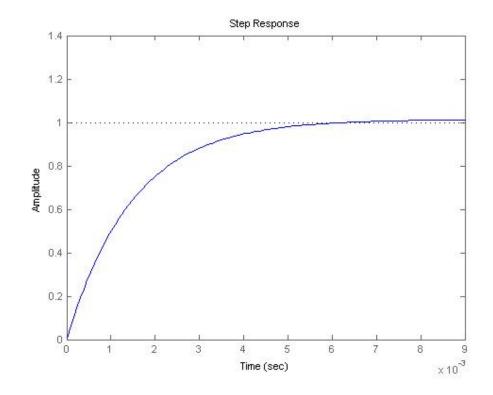
$$\frac{Y(s)}{U(s)} = \frac{G(s)P(s)}{G(s)P(S) + 1} = \frac{M(K_D s^2 + K_P s + K_I)}{s^3 + M(K_D s^2 + K_P s + K_I)}$$

## **Using Aforementioned Dynamics**

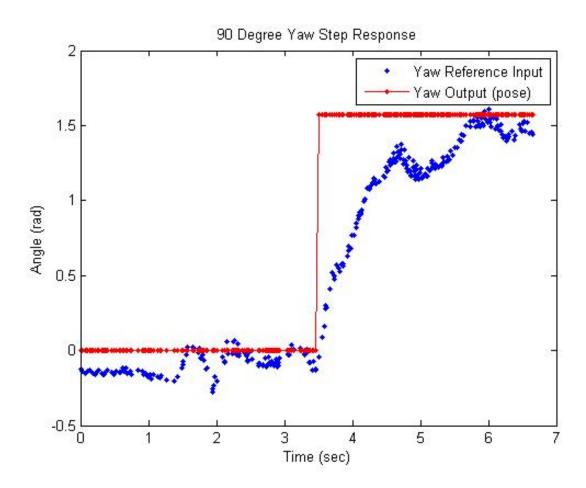
M = 3426

$$\frac{Y(s)}{U(s)} = \frac{G(s)P(s)}{G(s)P(S)+1} = \frac{M(K_Ds^2 + K_Ps + K_I)}{s^3 + M(K_Ds^2 + K_Ps + K_I)} = \frac{685.2s^2 + 6852s}{s^3 + 685.2s^2 + 6852s}$$
$$= \frac{685.2s + 6852}{s^2 + 685.2s + 6852}$$

step response way too fast (obvious from large coefficients)

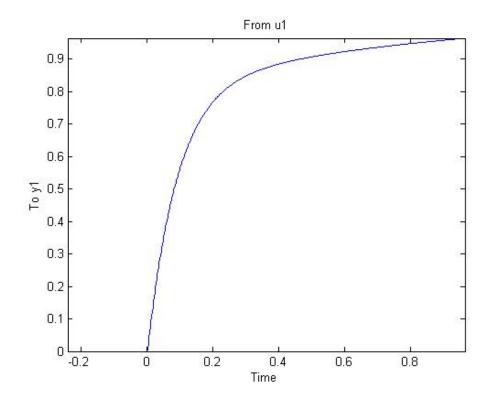


Now estimating transfer function (using MATLAB) since I know its order (more or less) and I have the step response below form experimentation (3 poles, 1 zero)



### **Estimated Transfer Function**

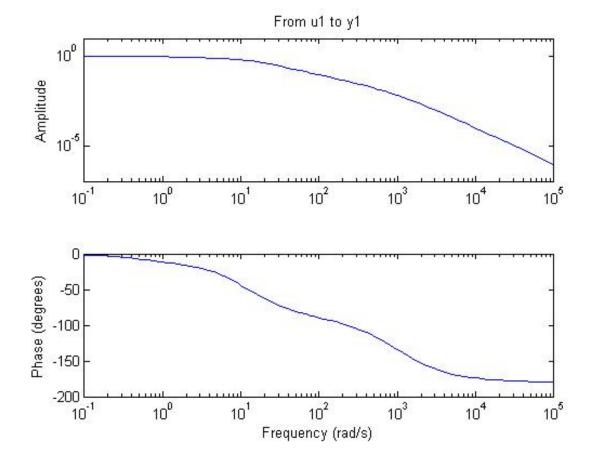
$$G(s) = \frac{1.049(1 + 0.7534s)}{(1 + 0.09019s)(1 + 0.94577s)(1 + 0.001s)}$$



# Freq/Stability

Zeros: -1.3273

Poles: -1000, -11.0877, -1.0573



- Visio
- Cmu serif
- 2<sup>nd</sup> order fit