

## Step-1

The relation between  $F_{-k}$  and  $F_k$  is as follows:  $F_{-k} = (-1)^{k+1} F_k$ .

## Step-2

Since the difference equation of the Fibonacci series is  $F_{k+2} = F_{k+1} + F_k$ , we can write  $F_k = F_{k+2} - F_{k+1}$ . Thus, we get

$$\begin{aligned} F_0 &= F_2 - F_1 \\ &= 0 \end{aligned}$$

$$\begin{aligned} F_{-1} &= F_1 - F_0 \\ &= 1 \end{aligned}$$

$$\begin{aligned} F_{-2} &= F_0 - F_{-1} \\ &= -1 \end{aligned}$$

$$\begin{aligned} F_{-3} &= F_{-1} - F_{-2} \\ &= 2 \end{aligned}$$

## Step-3

Thus, we can obtain the further terms of the Fibonacci series. It is as follows:

0, 1, 1, 2, 3, 5, 8, 13, 21, 34, 55, 89,...

Thus, the numerical values of the terms remain the same and the terms are alternately positive and negative.

Thus, note the following:

$$F_{-1} = F_1$$

$$F_{-2} = -F_2$$

$$F_{-3} = F_3$$

$$F_{-4} = -F_4$$

And so on!