

Step-1

Identity Transformation: When the outputs of linear transformation $T(v_j) = v_j$ are combinations of $\sum_{i=1}^n m_{ij} w_i$ then the change of basis matrix is M . Matrix M represents the identity transformation.

Step-2

Consider an identity transformation that takes each vector to itself.

$$Tx = x$$

Let the first basis is:

$$v_1 = (1, 2)$$

$$v_2 = (3, 4)$$

Second basis is:

$$w_1 = (1, 0)$$

$$w_2 = (0, 1)$$

This basis does not represent an identity matrix. Find the corresponding matrix that represents the identity transformation.

Step-3

The input basis are $v_1 = (1, 2)$ and $v_2 = (3, 4)$. In the identity transformation first input is the output itself. So, output can be expressed as $1w_1 + 2w_2$. Hence, the first column of the matrix M contains 1 and 2.

Similarly, second column will contain 3 and 4.

Step-4

Therefore the matrix M is :

$$M = \begin{bmatrix} 1 & 3 \\ 2 & 4 \end{bmatrix}$$