## Step-1

We have the projection matrix *P* upon to a line *a* is  $P = \frac{a^T a}{a^T a}$ 

$$P^{2} = \left(\frac{aa^{T}}{a^{T}a}\right) \left(\frac{aa^{T}}{a^{T}a}\right)$$
$$= \frac{\left(aa^{T}\right)\left(aa^{T}\right)}{\left(a^{T}a\right)\left(a^{T}a\right)}$$

$$=\frac{a(a^Ta)a^T}{(a^Ta)(a^Ta)}$$

$$= \frac{aa^{T}}{a^{T}a}$$
 Since  $a^{T}a$  is a scalar, we cancelled it.

=P

Therefore,  $P^2 = P$  when *P* is a projection matrix.