

Step-1

$$A = \begin{pmatrix} 2 & 2 & 0 \\ 2 & 5 & 3 \\ 0 & 3 & 8 \end{pmatrix}.$$

Given matrix is

Now the upper left determinants are

$$A_1 = 2,$$

$$A_2 = \begin{vmatrix} 2 & 2 \\ 2 & 5 \end{vmatrix} = 6,$$

$$\begin{aligned} A_3 &= |A| \\ &= 2(40 - 9) - 2(16) + 0 \\ &= 30 \end{aligned}$$

Therefore, the upper left determinants are $A_1 = 2, A_2 = 6$ and $A_3 = 30$.

Step-2

Now we determine the pivots of A .

$$A = \begin{pmatrix} 2 & 2 & 0 \\ 2 & 5 & 3 \\ 0 & 3 & 8 \end{pmatrix}$$

Apply $R_2 \rightarrow R_2 - R_1$

$$= \begin{pmatrix} 2 & 2 & 0 \\ 0 & 3 & 3 \\ 0 & 3 & 8 \end{pmatrix}$$

Apply $R_3 \rightarrow R_3 - R_2$

$$= \begin{pmatrix} 2 & 2 & 0 \\ 0 & 3 & 3 \\ 0 & 0 & 5 \end{pmatrix}$$

So the pivots of A are $2, 3$ and 5 .

Step-3

Verification,

The pivots are $\frac{A_1}{1}, \frac{A_2}{A_1}$ and $\frac{A_3}{A_2}$.

i.e. $\frac{2}{1}, \frac{6}{2}, \frac{30}{6}$

That is 2,3,5.

Thus pivots are verified.