Step-1

The objective is to complete the statement, $\hat{a}\in \infty$ Normally 4 $\hat{a}\in \infty$ In four dimensional space meet at a ____ $\hat{a}\in$, and also find the combination of (1,0,0,0),(1,1,0,0),(1,1,1,0) which produce b=(3,3,3,2)

Step-2

Consider the following expression,

$$(1,0,0,0),(1,1,0,0),(1,1,1,0),(1,1,1,1)$$

Produces b = (3, 3, 3, 2)

Normally 4 planes in four-dimension space meet at a **point** (similar to 3 planes meeting in 3 dimension space at a point).

The combination of the 4 column vectors producing b is:

$$1 \begin{pmatrix} 1 \\ 1 \\ 1 \\ 0 \end{pmatrix} + 2 \begin{pmatrix} 1 \\ 1 \\ 1 \\ 1 \end{pmatrix} = \begin{pmatrix} 3 \\ 3 \\ 3 \\ 3 \\ 2 \end{pmatrix}$$

The system of linear equations this is satisfying is

$$x+y+z+t=3$$
$$y+z+t=3$$
$$z+t=3$$
$$t=2$$

The solution of the equation is given as following in matrix format:

 $\begin{bmatrix} 0 \\ 0 \\ 1 \\ 2 \end{bmatrix}$