Step-1

We have to show that the following modified Gram-Schmidt steps produce the same

$$C = c - (q_1^T c)q_1 - (q_2^T c)q_2$$
 of Gram-Schmidt Process.

$$C^* = c - (q_1^T c) q_1$$
 and $C = C^* - (q_2^T C^*) q_2$

Step-2

$$C = C^* - (q_2^T C^*) q_2$$

$$= c - (q_1^T c) q_1 - (q_2^T [c - (q_1^T c) q_1]) q_2$$

$$= c - (q_1^T c) q_1 - (q_2^T c) q_2 + q_2^T (q_1^T c) q_1.q_2$$

$$= c - (q_1^T c) q_1 - (q_2^T c) q_2 + 0$$

$$= c - (q_1^T c) q_1 - (q_2^T c) q_2$$

Because q_1, q_2 are orthonormal columns, that is, $q_1q_2 = 0$

Therefore
$$C = c - (q_1^T c)q_1 - (q_2^T c)q_2$$

Hence the required result is proved.