

## Step-1

Now consider the following:

$$\begin{aligned}(FEF^{-1})x &= (FE)(F^{-1}x) \\ &= F(E(F^{-1}x))\end{aligned}$$

We know that when the product of either  $F$  or  $F^{-1}$  with  $x$  is carried out, a total of  $\frac{1}{2}n \log_2 n$  multiplications are required.

## Step-2

Thus, to obtain  $F^{-1}x$ , we need  $\frac{1}{2}n \log_2 n$  number of multiplications. After that, we have to calculate  $E(F^{-1}x)$ . Now  $E$  is an  $n$  by  $n$  diagonal matrix. Thus,  $E(F^{-1}x)$  needs  $n$  more multiplications. Finally, we carry out  $F(E(F^{-1}x))$ , which further requires  $\frac{1}{2}n \log_2 n$  number of multiplications.

Therefore, in total, we require  $\frac{1}{2}n \log_2 n + n + \frac{1}{2}n \log_2 n = n \log_2 n + n$  number of multiplications.

## Step-3

Out of these,  $\frac{1}{2}n \log_2 n$  multiplications come from each  $F$  and  $F^{-1}$  and the remaining  $n$  multiplications come from  $E$ .