

Step-1

Suppose $AA^T = A^T A$ (1)

The length of Ax is $\|Ax\|$ where the norm is a non negative quantity. (2)

By definition, we have $\|Ax\|^2 = (Ax)^T (Ax)$

$$= x^T (A^T A) x$$

$$= x^T AA^T x \text{ By (1)}$$

$$= (A^T x)^T (A^T x)$$

$$= \|A^T x\|^2$$

In view of (2), we can write this equation as $\|Ax\| = \|A^T x\|$

In other words, the length of Ax = length of $A^T x$ when $AA^T = A^T A$