

Step-1

We want that there should be maximum possible flow of the fluid towards the sink. The final flow can be understood by imagining an edge from node 6 to 1. The edge has tremendous capacity. Let $c_{61} = 100$. This edge fictitiously sends all the fluid, received in the sink, to the source. We want x_{61} to be as large as possible.

Thus, we can write the maximal flow problem as a linear programming problem as follows:

Maximize: x_{61}

Subject to:

$$x_{12} \leq 4$$

$$x_{13} \leq 5$$

$$x_{24} \leq 2$$

$$x_{35} \leq 4$$

$$x_{46} \leq 6$$

$$x_{56} \leq 1$$

$$x_{25} \leq 5$$

$$x_{34} \leq 3$$

$$x_{ij} \geq 0 \text{ for each } i, j.$$

Step-2

Suppose we introduce the slack variables w_{ij} , such that $w_{ij} = c_{ij} - x_{ij}$, then the same problem can be written as follows:

Maximize: x_{61}

Subject to:

$$x_{12} + w_{12} = 4$$

$$x_{13} + w_{13} = 5$$

$$x_{24} + w_{24} = 2$$

$$x_{35} + w_{35} = 4$$

$$x_{46} + w_{46} = 6$$

$$x_{56} + w_{56} = 1$$

$$x_{25} + w_{25} = 5$$

$$x_{34} + w_{34} = 3$$

$$x_{ij} \geq 0 \text{ and } w_{ij} \geq 0 \text{ for each } i, j.$$

