

## Step-1

Given that columns of a matrix  $A$  are  $n$  vectors from the set  $\mathbb{R}^m$ .

To find the rank of matrix  $A$  if they are linearly independent.

## Step-2

Rank of a matrix is the number of maximum independent rows = number of maximum independent columns.

Now, if columns of  $A$  are  $n$  vectors and they all are linearly independent then number of maximum independent columns is  $n$ .

Hence, rank of  $A$  will be  $n$ .

## Step-3

Given that columns of a matrix  $A$  are  $n$  vectors from the set  $\mathbb{R}^m$ .

To find the rank of matrix  $A$  if they span  $\mathbb{R}^m$ .

## Step-4

Rank of a matrix is the number of maximum independent rows = number of maximum independent columns.

As the columns of matrix are vector from  $\mathbb{R}^m$  and they span  $\mathbb{R}^m$  so maximum independent columns is  $m$ .

Hence, rank of  $A$  will be  $m$ .

## Step-5

Given that columns of a matrix  $A$  are  $n$  vectors from the set  $\mathbb{R}^m$ .

To find the rank of matrix  $A$  if they are a basis for  $\mathbb{R}^m$ .

## Step-6

Rank of a matrix is the number of maximum independent rows = number of maximum independent columns.

As the columns of matrix are vector from  $\mathbb{R}^m$  and they span (basis is the independent set of vectors spanning a vector space)  $\mathbb{R}^m$  so independent columns is  $m$ .

Hence, rank of  $A$  will be  $m$ .