

## Step-1

Given system is  $2x + 3y = 1$

$$10x + 9y = 11$$

Given system can be written matrix form as

$$\begin{pmatrix} 2 & 3 \\ 10 & 9 \end{pmatrix} \begin{pmatrix} x \\ y \end{pmatrix} = \begin{pmatrix} 1 \\ 11 \end{pmatrix}$$

The augmented matrix is

$$\begin{pmatrix} 2 & 3 & 1 \\ 10 & 9 & 11 \end{pmatrix}$$

## Step-2

Subtract  $\frac{10}{2} = 5$  times the first row from the second row to get  $\begin{pmatrix} 2 & 3 & 1 \\ 0 & -6 & 6 \end{pmatrix}$  which is an upper triangular system

$$2x + 3y = 1$$

$$-6y = 6$$

By back-substitution  $-6y = 6$

$$\Rightarrow y = -1$$

And  $2x + 3(-1) = 1$

$$\Rightarrow x = 2$$

Hence the solution is  $\boxed{(2, -1)}$

## Step-3

Verification:-

Put  $x = 2, y = -1$  in the given system

$$2x + 3y = 2(2) + 3(-1)$$

$$= 1$$

$$10x + 9y = 10(2) + 9(-1) \\ = 11$$

Hence  $x$  times  $(2, 10)$  plus  $y$  times  $(3, 9)$  equals  $(1, 11)$ .

## Step-4

If right-hand side changes to  $(4, 44)$ , then the augmented matrix is

$$\begin{pmatrix} 2 & 3 & 4 \\ 10 & 9 & 44 \end{pmatrix}$$

Subtract  $5$  times the first row from the second row

$$\begin{pmatrix} 2 & 3 & 4 \\ 0 & -6 & 24 \end{pmatrix}$$

which is upper triangular system  $2x + 3y = 4$

$$-6y = 24$$

By back-substitution, we have  $-6y = 24$

$$\Rightarrow y = -4$$

And  $2x + 3(-4) = 4$

$$\Rightarrow x = 8$$

Hence the solution is  $(8, -4)$