## Step-1

Consider the following system,

$$3x + 2y = 10$$

$$6x + 4y =$$
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The objective is to choose a right-hand side which gives no solution, and another right hand-side which gives infinitely many solutions, and find two of those solutions.

## Step-2

Write the 6x + 4y as follows,

$$6x + 4y = 2(3x + 2y)$$

Therefore, the system of equations can be expressed as,

$$3x + 2y = 10$$

$$2(3x+2y) = _{-}$$

If the right hand side of the second equation is not 2(10) = 20, then the second equation becomes,

$$3x + 2y \neq 10$$

Then, the given system becomes as follows:

$$3x + 2y = 10$$

$$3x + 2y \neq 10$$

So, this is impossible.

Therefore, the system has no solution if the right hand side of the 2<sup>nd</sup> equation is a real number which is not 20.

## Step-3

If the right hand side of the 2<sup>nd</sup> equation is 20, then the system reduced as follows,

$$3x + 2y = 10$$

$$2(3x+2y)=20$$

This implies,

$$3x + 2y = 10$$

$$3x + 2y = 10$$

So, there is only one equation 3x + 2y = 10 to solve. This is a straight line, so it has infinitely many points.

That is, the system has infinitely many solutions if the right side of the 2<sup>nd</sup> equation is 20.

## Step-4

If x = 0, then from the equation 3x + 2y = 10,

$$3(0) + 2y = 10$$
$$y = 5$$

Then, a solution of the system is (0,5).

If x = 4, then from the equation 3x + 2y = 10,

$$3(4)+2y=10$$
$$2y=10-12$$
$$2y=-2$$
$$y=-1$$

Then, a solution of the system is (4,-1).

Hence, the two solutions of the system are (0,5) and (4,-1).