

Step-1

To check the product of 5 reflections and 8 rotations of the x - y plane produce.

Reflection yields; $(x, y) \xrightarrow{\text{Re}} (y, x)$

Rotation yields; $(x, y) \xrightarrow{\text{Ro}} (y, -x)$

Step-2

Let (x, y) be vector.

Re denote reflection, Ro denotes rotations

Now the product of 5 reflections and 8 rotations is as shown below. $(x, y) \xrightarrow{\text{Re}} (y, x) \xrightarrow{\text{Re}} (y, x) \xrightarrow{\text{Re}} (y, x) \xrightarrow{\text{Re}} (y, x) \xrightarrow{\text{Re}} (x, y)$

$$\xrightarrow{\text{Re}} (y, x) \xrightarrow{\text{Ro}} (-x, y) \xrightarrow{\text{Ro}} (-y, -x) \xrightarrow{\text{Ro}} (x, -y)$$

$$\xrightarrow{\text{Ro}} (y, x) \xrightarrow{\text{Ro}} (-x, y) \xrightarrow{\text{Ro}} (-y, -x) \xrightarrow{\text{Ro}} (x, -y)$$

$$\xrightarrow{\text{Ro}} (y, x)$$

Hence the product of 5 reflections and 8 rotations of x - y plane produce a reflection.