

## Step-1

In every week the chemistry course taught in section  $A$  is  $\frac{1}{4}$  course and in section  $B$ , it is  $\frac{1}{3}$  course and  $\frac{1}{6}$  of each section transfer to the other section.

Let  $T$  be the transition matrix.

In a markov transition matrix, each column adds to 1 and it has no negative entries.

## Step-2

Let  $x_0$  be the total number of students in section  $A \rightarrow x$

Let  $y_0$  be the total number of students in section  $B \rightarrow y$

Let  $z_0$  be the total number of students, who are in neither section (drop outs)  $\rightarrow z$

The number of students in section  $A$  is given as,

$$x = x_0 - \underbrace{\frac{x_0}{6}}_{\text{transferring}} - \underbrace{\frac{x_0}{4}}_{\text{dropping}} + \underbrace{\frac{y_0}{6}}_{\text{transferring from } B}$$

$$= \frac{7x_0}{12} + \frac{y_0}{6} + 0 \cdot z_0$$

The number of students in section  $B$  is given as,

$$y = y_0 - \underbrace{\frac{y_0}{3}}_{\text{dropping}} - \underbrace{\frac{y_0}{6}}_{\text{transferring}} + \underbrace{\frac{x_0}{6}}_{\text{transferring from } A}$$

$$= \frac{x_0}{6} + \frac{y_0}{2} + 0 \cdot z_0$$

The number of students neither in in section  $A$  nor  $B$  is given as,

$$z = \underbrace{\frac{x_0}{4}}_{\text{transferring from } A} + \underbrace{\frac{y_0}{3}}_{\text{transferring from } B} + z_0$$

$$T = \begin{bmatrix} \frac{7}{12} & \frac{1}{6} & 0 \\ \frac{1}{6} & \frac{1}{2} & 0 \\ \frac{1}{4} & \frac{1}{3} & 1 \end{bmatrix}$$

Therefore, the transition matrix for a chemistry course that is taught in section  $A$  and Section  $B$  is

