

Step-1

Complex inner product: $\mathbf{u}^H \mathbf{v} = \overline{u_1} v_1 + \cdots + \overline{u_n} v_n$.

Step-2

Consider the following orthonormal Eigen vectors form of matrix A .

$$\begin{aligned} A &= U \Lambda U^{-1} \\ &= U \Lambda U^H \end{aligned}$$

Prove the following:

$$AA^H = A^H A$$

Step-3

Calculate the following:

$$\begin{aligned} AA^H &= (U \Lambda U^H) (U \Lambda U^H)^H \\ &= (U \Lambda U^H) ((U^H)^H \Lambda U^H) \\ &= U \Lambda U^H U \Lambda U^H \\ &= ((U^H)^H \Lambda U^H) (U \Lambda U^H) \end{aligned}$$

$$AA^H = A^H A$$

Step-4

Therefore, $\boxed{AA^H = A^H A}$. These are exactly the normal matrices