

## Step-1

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Given that producing  $x_1$  trucks and  $x_2$  planes requires  $x_1 + 50x_2$  tons of steel,  $40x_1 + 1000x_2$  pounds of rubber, and  $2x_1 + 50x_2$  months of labor.

Suppose the unit costs  $y_1, y_2, y_3$  are \$700 per ton, \$3 per pound and \$3000 per month.

Given that  $Ax$  gives the amounts of steel, rubber, and labor to produce  $x$ .

We have to find  $A$ .

## Step-2

From the given data, we get

$$Ax = \begin{bmatrix} x_1 + 50x_2 \\ 40x_1 + 1000x_2 \\ 2x_1 + 50x_2 \end{bmatrix}$$
$$= \begin{bmatrix} 1 & 50 \\ 40 & 1000 \\ 2 & 50 \end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \end{bmatrix}$$

Therefore,  $A = \begin{bmatrix} 1 & 50 \\ 40 & 1000 \\ 2 & 50 \end{bmatrix}$

## Step-3

Here  $(Ax)^T y$  is the cost of inputs while  $x^T (A^T y)$  is the value of outputs.