

Step-1

We have to fill in the following blanks.

Suppose \mathbf{L} is a one dimensional subspace (a line) \mathbf{R}^3 . Its orthogonal complement \mathbf{L}^\perp is the _____ perpendicular to \mathbf{L} . Then $(\mathbf{L}^\perp)^\perp$ is a _____ perpendicular to \mathbf{L}^\perp . In fact $(\mathbf{L}^\perp)^\perp$ is the same as _____.

Step-2

Suppose \mathbf{L} is a one dimensional subspace (a line) \mathbf{R}^3 . Its orthogonal complement \mathbf{L}^\perp is the two- dimensional subspace (a plane) in R^3 perpendicular to \mathbf{L} . then $(\mathbf{L}^\perp)^\perp$ is a one-dimensional subspace (a line) perpendicular to \mathbf{L}^\perp . In fact $(\mathbf{L}^\perp)^\perp$ is the same as \mathbf{L} .