

Step-1

a) Area of parallelogram with edges $v = (3, 2)$ and $w = (1, 4)$ is

$$\begin{aligned} \begin{vmatrix} u \\ v \end{vmatrix} &= \begin{vmatrix} 3 & 2 \\ 1 & 4 \end{vmatrix} \\ &= 12 - 2 \\ &= 10 \text{ sq.units} \end{aligned}$$

Step-2

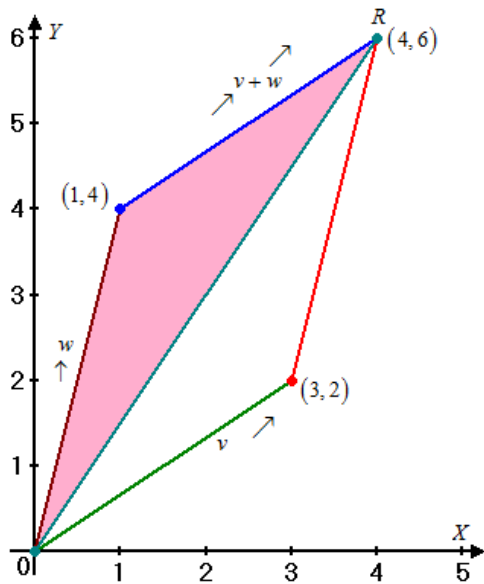
(b) The area of the triangle with sides $v, w, v + w$ is half the area of the parallelogram with the adjacent edges v, w

$$\begin{aligned} &= \frac{10}{2} \\ &= 5 \text{ sq.units} \end{aligned}$$

We draw the vectors $v = (3, 2)$ and $w = (1, 4)$ starting from the origin $(0, 0)$.

We extend a line from v parallel to w whose length is equal to that of w in the positive direction of w with the end point R .

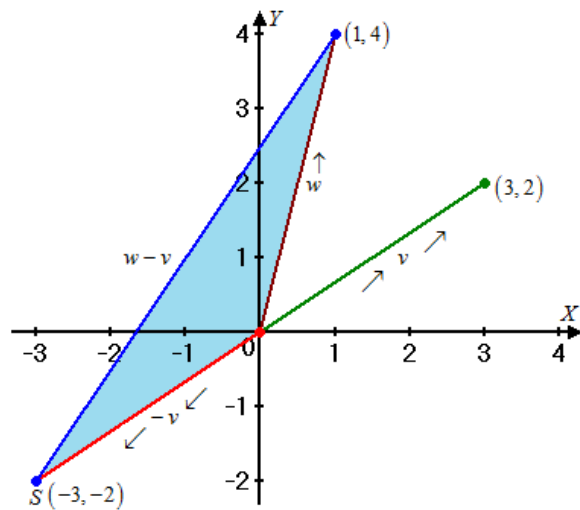
We join OR to get the vector $v + w$.



Step-3

c) Observe that $-v$ is the vector in the negative direction of v and with the same magnitude that of v .

Also, the vector $w - v$ is a vector that joins O to S where S is the end point of the vector drawn from w in the negative direction of v and is parallel to v of magnitude v .



Step-4

The area of the triangle with sides $v, w, w-v$ is also equal to half the area of the parallelogram with adjacent edges v and w .

Therefore, the required area is 5 sq.units