

## Step-1

Consider the following matrices:

$$A_1 = \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix}$$

$$A_2 = \begin{bmatrix} 0 & 1 \\ 1 & 0 \end{bmatrix}$$

$$A_3 = \begin{bmatrix} 1 & 1 \\ 0 & 0 \end{bmatrix}$$

$$A_4 = \begin{bmatrix} 0 & 0 \\ 1 & 1 \end{bmatrix}$$

$$A_5 = \begin{bmatrix} 1 & 0 \\ 1 & 0 \end{bmatrix}$$

$$A_6 = \begin{bmatrix} 0 & 1 \\ 0 & 1 \end{bmatrix}$$

## Step-2

Determine the matrices which are similar.

## Step-3

Recall that similar matrices have same Eigen values. Calculate the Eigen values of all the matrices. Matrix  $A_1$  is triangular matrix so Eigen values of matrix  $A_1$  will be  $\lambda_1 = (1,1)$ . Similarly Eigen values of matrices  $A_3$  and  $A_6$  are :

$$\lambda_3 = (1,0)$$

$$\lambda_6 = (0,1)$$

Therefore,  $\boxed{A_3, A_6}$  are similar matrices.

## Step-4

Calculate Eigen values of matrix  $A_2$ ;

$$A_2 - \lambda I = \begin{bmatrix} 0 - \lambda & 1 \\ 1 & 0 - \lambda \end{bmatrix}$$

$$\det(A_2 - \lambda I) = 0$$

$$(-\lambda)(-\lambda) - 1 = 0$$

$$\lambda^2 - 1 = 0$$

On solving above equation following Eigen values are obtained:

$$\lambda_2 = (1, -1)$$

## Step-5

Eigen values of matrix  $A_4$  will be:

$$A_4 - \lambda I = \begin{bmatrix} 0 - \lambda & 0 \\ 1 & 1 - \lambda \end{bmatrix}$$

$$\det(A_4 - \lambda I) = 0$$

$$(-\lambda)(1 - \lambda) = 0$$

$$\lambda^2 - \lambda = 0$$

On solving above equation following Eigen values are obtained:

$$\lambda_4 = (1, 0)$$

## Step-6

Similarly, Eigen values of matrix  $A_5$  will be  $\lambda_5 = (1, 0)$ .

## Step-7

Therefore, following matrices are similar:

$$\boxed{\begin{bmatrix} 0 & 0 \\ 1 & 1 \end{bmatrix}, \begin{bmatrix} 1 & 1 \\ 0 & 0 \end{bmatrix}, \begin{bmatrix} 1 & 0 \\ 1 & 0 \end{bmatrix}, \begin{bmatrix} 0 & 1 \\ 0 & 1 \end{bmatrix}}$$

Matrix  $A_1$  and  $A_2$  are similar to themselves.