

Step-1

We have $\det A = 6$ and

$$\det A = \begin{vmatrix} \text{row 1} \\ \text{row 2} \\ \text{row 3} \end{vmatrix} = \begin{vmatrix} \text{row 1} + \text{row 2} \\ \text{row 2} + \text{row 3} \\ \text{row 3} \end{vmatrix}$$

Step-2

$$\det B = \begin{vmatrix} \text{row 1} + \text{row 2} \\ \text{row 2} + \text{row 3} \\ \text{row 3} + \text{row 1} \end{vmatrix}$$

Therefore

$$= \det A + \begin{vmatrix} \text{row 1} + \text{row 2} \\ \text{row 2} + \text{row 3} \\ \text{row 1} \end{vmatrix}$$

Step-3

$$\det B = \det A + \begin{vmatrix} \text{row 2} \\ \text{row 2} + \text{row 3} \\ \text{row 1} \end{vmatrix}$$

$$= \det A + \begin{vmatrix} \text{row 2} \\ \text{row 3} \\ \text{row 1} \end{vmatrix}$$

Step-4

$$\det B = \det A - \begin{vmatrix} \text{row 2} \\ \text{row 1} \\ \text{row 3} \end{vmatrix}$$

$$= \det A + \begin{vmatrix} \text{row 1} \\ \text{row 2} \\ \text{row 3} \end{vmatrix}$$

$$= \det A + \det A$$

$$= 6 + 6$$

$$= \boxed{12}$$