

Step-1

(a)

To find the first column of 3×3 matrix, consider the following vector:

$$\begin{bmatrix} 1 \\ 0 \\ 0 \end{bmatrix}$$

Project the vector $\begin{bmatrix} 1 \\ 0 \\ 0 \end{bmatrix}$ onto x - y plane, and get the vector $\begin{bmatrix} 1 \\ 0 \\ 0 \end{bmatrix}$.

Step-2

To find the second and third column of 3×3 matrix, consider the following vectors:

$$\begin{bmatrix} 0 \\ 1 \\ 0 \end{bmatrix} \text{ And } \begin{bmatrix} 0 \\ 0 \\ 1 \end{bmatrix}$$

Project the vector $\begin{bmatrix} 0 \\ 1 \\ 0 \end{bmatrix}$ onto x - y plane, and get the vector $\begin{bmatrix} 0 \\ 1 \\ 0 \end{bmatrix}$.

Now, project the vector $\begin{bmatrix} 0 \\ 0 \\ 1 \end{bmatrix}$ onto x - y plane, and get the vector $\begin{bmatrix} 0 \\ 0 \\ 0 \end{bmatrix}$.

Step-3

$$\begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 0 \end{bmatrix}$$

Therefore, the matrix transformation by projecting every vector onto the x - y plane is given by $\begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 0 \end{bmatrix}$.

Step-4

(b)

To find the first column of 3×3 matrix, consider the following vector:

$$\begin{bmatrix} 1 \\ 0 \\ 0 \end{bmatrix}$$

Reflect the vector $\begin{bmatrix} 1 \\ 0 \\ 0 \end{bmatrix}$ through the x - y plane, we get the vector $\begin{bmatrix} 1 \\ 0 \\ 0 \end{bmatrix}$.

Step-5

To find the second and third column of 3×3 matrix, consider the following vectors:

$$\begin{bmatrix} 0 \\ 1 \\ 0 \end{bmatrix} \text{ And } \begin{bmatrix} 0 \\ 0 \\ 1 \end{bmatrix}$$

Reflect the vector $\begin{bmatrix} 0 \\ 1 \\ 0 \end{bmatrix}$ through the xy -plane, and get the vector $\begin{bmatrix} 0 \\ 1 \\ 0 \end{bmatrix}$.

Now, reflect the vector $\begin{bmatrix} 0 \\ 0 \\ 1 \end{bmatrix}$ through the xy -plane, and get the vector $\begin{bmatrix} 0 \\ 0 \\ -1 \end{bmatrix}$.

Step-6

$$\begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & -1 \end{bmatrix}$$

Therefore, the matrix of transformation by reflecting every vector through the x - y plane is given by $\begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & -1 \end{bmatrix}$.

Step-7

(c)

To find the first column of 3×3 matrix, consider the following vector:

$$\begin{bmatrix} 1 \\ 0 \\ 0 \end{bmatrix}$$

Rotate the vector $\begin{bmatrix} 1 \\ 0 \\ 0 \end{bmatrix}$ in the x - y plane by 90° , and get the vector $\begin{bmatrix} 0 \\ 1 \\ 0 \end{bmatrix}$.

To find the second and third column of 3×3 matrix, consider the following vectors:

$$\begin{bmatrix} 0 \\ 1 \\ 0 \end{bmatrix} \text{ And } \begin{bmatrix} 0 \\ 0 \\ 1 \end{bmatrix}$$

Rotate the vector $\begin{bmatrix} 0 \\ 1 \\ 0 \end{bmatrix}$ in the x - y plane by 90° , and get vector $\begin{bmatrix} -1 \\ 0 \\ 0 \end{bmatrix}$.

Rotate the vector $\begin{bmatrix} 0 \\ 0 \\ 1 \end{bmatrix}$ in the x - y plane by 90° , and get the vector $\begin{bmatrix} 0 \\ 0 \\ 1 \end{bmatrix}$.

Step-8

$$\begin{bmatrix} 0 & -1 & 0 \\ 1 & 0 & 0 \\ 0 & 0 & 1 \end{bmatrix}$$

Therefore, the matrix of transformation by rotating the x - y plane through 90° , leaving the z -axis alone is given by $\begin{bmatrix} 0 & -1 & 0 \\ 1 & 0 & 0 \\ 0 & 0 & 1 \end{bmatrix}$.

Step-9

(d)

To find the first column of 3×3 matrix, consider the following vector:

$$\begin{bmatrix} 1 \\ 0 \\ 0 \end{bmatrix}$$

Rotate the vector $\begin{bmatrix} 1 \\ 0 \\ 0 \end{bmatrix}$ in the x - y plane by 90° , and get vector $\begin{bmatrix} 0 \\ 1 \\ 0 \end{bmatrix}$.

Rotate the vector $\begin{bmatrix} 0 \\ 1 \\ 0 \end{bmatrix}$ in x - z plane by 90° , and get vector $\begin{bmatrix} 0 \\ 1 \\ 0 \end{bmatrix}$.

Rotate the vector $\begin{bmatrix} 0 \\ 1 \\ 0 \end{bmatrix}$ in y - z plane by 90° , we get vector $\begin{bmatrix} 0 \\ 0 \\ 1 \end{bmatrix}$.

Step-10

To find the second column of 3×3 matrix, consider the following vectors:

$$\begin{bmatrix} 0 \\ 1 \\ 0 \end{bmatrix}$$

Rotate the vector $\begin{bmatrix} 0 \\ 1 \\ 0 \end{bmatrix}$ in the x - y plane by 90° , and get vector $\begin{bmatrix} 0 \\ -1 \\ 0 \end{bmatrix}$.

Rotate the vector $\begin{bmatrix} 0 \\ -1 \\ 0 \end{bmatrix}$ in x - z plane by 90° , and get vector $\begin{bmatrix} 0 \\ 0 \\ -1 \end{bmatrix}$.

Rotate the vector $\begin{bmatrix} 0 \\ 0 \\ -1 \end{bmatrix}$ in y - z plane by 90° , and get vector $\begin{bmatrix} 0 \\ 1 \\ 0 \end{bmatrix}$.

Step-11

To find the third column of 3×3 matrix, consider the following vector:

$$\begin{bmatrix} 0 \\ 0 \\ 1 \end{bmatrix}$$

Rotate the vector $\begin{bmatrix} 0 \\ 0 \\ 1 \end{bmatrix}$ in the x - y plane by 90° , and get vector $\begin{bmatrix} 0 \\ 0 \\ 1 \end{bmatrix}$.

Rotate the vector $\begin{bmatrix} 0 \\ 0 \\ 1 \end{bmatrix}$ in x - z plane by 90° , and get vector $\begin{bmatrix} -1 \\ 0 \\ 0 \end{bmatrix}$.

Rotate the vector $\begin{bmatrix} -1 \\ 0 \\ 0 \end{bmatrix}$ in y - z plane by 90° , and get vector $\begin{bmatrix} -1 \\ 0 \\ 0 \end{bmatrix}$.

Therefore, the matrix transformation by rotating the x - y plane, then x - z plane and then y - z through 90° , is given by $\begin{bmatrix} 0 & 0 & -1 \\ 0 & 1 & 0 \\ 1 & 0 & 0 \end{bmatrix}$.

Step-12

(e)

To find the first column of 3×3 matrix, consider the following vector:

$$\begin{bmatrix} 1 \\ 0 \\ 0 \end{bmatrix}$$

Step-13

Rotate the vector $\begin{bmatrix} 1 \\ 0 \\ 0 \end{bmatrix}$ in the x - y plane by 180° , and get vector $\begin{bmatrix} -1 \\ 0 \\ 0 \end{bmatrix}$.

Rotate the vector $\begin{bmatrix} -1 \\ 0 \\ 0 \end{bmatrix}$ in x - z plane by 180° , and get vector $\begin{bmatrix} 1 \\ 0 \\ 0 \end{bmatrix}$.

Rotate the vector $\begin{bmatrix} 1 \\ 0 \\ 0 \end{bmatrix}$ in y - z plane by 180° , and get vector $\begin{bmatrix} 1 \\ 0 \\ 0 \end{bmatrix}$.

Step-14

To find the second column of 3×3 matrix, consider the following vector:

$$\begin{bmatrix} 0 \\ 1 \\ 0 \end{bmatrix}$$

Rotate the vector $\begin{bmatrix} 0 \\ 1 \\ 0 \end{bmatrix}$ in the x - y plane by 180° , and get vector $\begin{bmatrix} 0 \\ -1 \\ 0 \end{bmatrix}$.

Rotate the vector $\begin{bmatrix} 0 \\ -1 \\ 0 \end{bmatrix}$ in x - z plane by 180° , and get vector $\begin{bmatrix} 0 \\ -1 \\ 0 \end{bmatrix}$.

Rotate the vector $\begin{bmatrix} 0 \\ -1 \\ 0 \end{bmatrix}$ in y - z plane by 180° , and get vector $\begin{bmatrix} 0 \\ 1 \\ 0 \end{bmatrix}$.

Step-15

To find the third column of 3×3 matrix, consider the following vector:

$$\begin{bmatrix} 0 \\ 0 \\ 1 \end{bmatrix}$$

Rotate the vector $\begin{bmatrix} 0 \\ 0 \\ 1 \end{bmatrix}$ in the x - y plane by 180° , and get vector $\begin{bmatrix} 0 \\ 0 \\ 1 \end{bmatrix}$.

Rotate the vector $\begin{bmatrix} 0 \\ 0 \\ 1 \end{bmatrix}$ in x - z plane by 180° , and get vector $\begin{bmatrix} 0 \\ 0 \\ -1 \end{bmatrix}$.

Rotate the vector $\begin{bmatrix} 0 \\ 0 \\ -1 \end{bmatrix}$ in y - z plane by 180° , and get vector $\begin{bmatrix} 0 \\ 0 \\ 1 \end{bmatrix}$.

Step-16

Therefore, the matrix of transformation by rotating the x - y plane, then x - z plane and then y - z by 180° , is given by $\begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix}$.