

Step-1

We know that a positive definite matrix cannot have a zero on its diagonal.

So a diagonal entry a_{jj} of a symmetric matrix cannot be smaller than all the λ 's.

If it were, then $A - a_{jj}I$ would have positive Eigen values and would be positive definite. But $A - a_{jj}I$ has a zero on the main diagonal.