Step-1

The above discussion is shown in the figure below:

The green arrows are showing the action of A^T on the vectors y_c, y_l and the whole y. Note that the only vector common to Row space and Nullspace of $\mathbf{R}^n$ is the zero vector.