

## Step-1

Given that

$$\det(I + M) = \begin{vmatrix} 1+a & b & c & d \\ a & 1+b & c & d \\ a & b & 1+c & d \\ a & b & c & 1+d \end{vmatrix}$$
$$= \begin{vmatrix} 1+a+b+c+d & b & c & d \\ 1+a+b+c+d & 1+b & c & d \\ 1+a+b+c+d & b & 1+c & d \\ 1+a+b+c+d & b & c & 1+d \end{vmatrix}$$

(Adding second, third, fourth columns to the first column)

## Step-2

$$= (1+a+b+c+d) \begin{vmatrix} 1 & b & c & d \\ 1 & 1+b & c & d \\ 1 & b & 1+c & d \\ 1 & b & c & 1+d \end{vmatrix}$$
$$= (1+a+b+c+d) \begin{vmatrix} 1 & b & c & d \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{vmatrix}$$

## Step-3

(Adding  $\hat{a}^{\text{c}} \cdot 1$  time the first row to the second, third and fourth rows)

$$= (1a + a + b + c + d)$$

When  $a = b = c = d = 1$ ,

$$\det(I + M) = 1 + 1 + 1 + 1 + 1$$

$$= \boxed{5}$$