

Step-1

We have to find that which of the following rules give a correct definition of the rank of A .

Let R be the row reduced echelon form of the matrix ' A '

a) The number of non zero rows in R .

The above definition gives the correct definition for the rank of A .

Step-2

b) The number of columns minus the total number of rows.

The above definition does not give the correct definition for the rank of A .

For example, $A = \begin{bmatrix} 1 & 0 \\ 0 & 0 \end{bmatrix}$ has rank 1.

But number of columns minus the total number of rows = 0

Step-3

c) The number of columns minus the number of free columns.

The above definition gives the correct definition for the rank of A .

Step-4

d) The number 1s in R .

The above definition does not give the correct definition for the rank of A .

For example, if $A = \begin{bmatrix} 1 & 1 & 1 & 1 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \end{bmatrix}$, rank of $A = 1$ but A has four 1's.