

Step-1

Given that put bases for the orthogonal subspaces \mathbf{V} and \mathbf{W} into the columns of matrices V and W , we have explain that why $V^\perp W = \text{zero matrix}$, and we have to match this equation with $v^T w = 0$ for vectors.

Step-2

The matrices V and W contains orthogonal basis vectors as their columns, so we have

$$V^\perp W = \text{zero matrix}.$$

This makes each basis vector for V orthogonal to each basis vector for W .

Thus every v in V is orthogonal to every w in W , so $v^T w = 0$