Step-1

a)

The four vectors are dependent.

Because, the four vectors are columns of a 3 by 4 matrix. A with at least one free variable. So Ax = 0

Step-2

b)

The two vectors v_1 and v_2 will be dependent if $v_1 v_2$ matrix has rank 0 or 1 but not 2.

Or

The two vectors v_1 and v_2 will be dependent if $v_1 = tv_2$ for some non-zero scalar t.

Step-3

c)

The vectors v_1 and (0,0,0) are dependent because $(-2)(0,0,0)+(0)v_1=0$