# Session 2

May 16, 2020

### 1 Session 2

## 1.1 Implementing a 2D simulation of Active Brownian Particles (ABP) in C++

In the second session of this tutorial we port the Python code developed in Session 1 to C++. We keep the structure and naming the same as in the Python version and only make changes where necessary to set the sage for the GPU implementation in Session 3.

### 1.1.1 Brief overview of the design layout

The image below show key components of a particle based simulation code and how they interact with each other:

Let us briefly focus on the *Evolver* class. Its task is to evolve the system by a single time step, i.e., to propagate the dynamics for  $\delta t$ . In particular, its task is to:

- 1. Ensure that the neighbor list is up to date;
- 2. Perform the integration pre-step;
- 3. Compute all forces and torques on each particle;
- 4. Perform the integration post-step;
- 5. Apply periodic boundary conditions.

In our design, one can have multiple force and torque laws apply in the system. In addition, multiple integrators can act in the same system.

Here we focus on the item number 3, and in particular the fact that in a given system one could have multiple types of interactions.

For example, in our case, we apply the self-propulsion force  $\mathbf{F}_i^{\mathrm{sp}} = \alpha \mathbf{n}_i$  on each particle. In addition, each particle experiences soft-core repulsion due to overlaps with its neighbors, i.e.  $\mathbf{F}_i^{\mathrm{elastic}} = \sum_j k \left(2a - r_{ij}\right) \hat{\mathbf{r}}_{ij}$  for  $r_{ij} \leq 2a$ , with the same meaning of parameters as used in Session 1. In our implementation, each term in the total force is implemented as a separate class. The self-propulsion term is handled by the SelfPropulsion class, while the soft-core repulsion is implemented in the HarmonicForce class.

The *Evolver* class has member variable called *force\_computes* that is a Python list that stores all different types of interactions used in a given simulation. To be a bit more technical, if we want to add self-propulsion and soft-core repulsion to our system, we simply create two objects (instances), one for each of the two ""force type" classes and append them to the *force\_computes* list of the *Evolver* class.

The *evolve* function of the *Evolver* class then **simply** iterates over all elements of the *force\_computes* list and calls the appropriate *compute* function for each of element.

It is not a coincidence that we put the word **simply** in bold. Due to Python's expressive and powerful data structure this was all we needed to do. However, a lot of things are happening under the hood here, which we need to understand if we are to switch to C++. Code written in C++ is in general much faster than the same code written in Python. This, however, comes at the expense of lot of things that, colloquially put, just work in Python, need to be explicitly implemented in C++.

In order to understand how to port to C++ the same functionality that allows us to split different types of forces into separate classes, we need to introduce the concepts of *class inheritance* and *smart pointers*.

#### 1.1.2 Classes

Class is the central language feature of C++. It is a user-defined type that represents a concept in the code. An instance of a class is called an *object*. A typical class is, therefore, a piece of C++ code that contains some data (called *member data*) and some operations that are performed on that data (called *member functions*). In other words, a class is an abstraction of a set of properties and operations that can be performed on those properties. Note that a class can contain members only (i.e., no member functions) but it also can contain no member data and only member functions. At first, the later example sounds paradoxical but it is of central importance for this discussion.

Concrete classes Let us give several concrete examples of classes.

One of the central entities in our simulation is a particle. It is, therefore, natural to represent it as a class. This is a very simple class that holds basic information such as position, velocity, type, etc. of a particle.

```
struct Particle
{
    int id;
                       // particle id
                       // particle type
    int type;
    real radius;
                       // particle radius
                       // particle position
    real2 r;
                       // particle velocity
    real2 v;
    real2 f;
                       // particle force
                       // particle director
    real2 n;
};
```

Note: In the previous example, real and real2 are user defined types to be discussed later. We also use struct which is essentially a class with all members being public, i.e., accessible by non-member functions.

Finally, our actual implementation includes several other member data, which are here omitted for brevity.

Arguably, *Particle* is not an overly exciting class as it does not do much. A more interesting example is the *System* class. This class hold the list of all particles we would like to simulate and

basic operations on them, such as adding a new particle. In a reduced form, this class could look something like this.

```
class System
public:
   System(Box& box) : _box{box}, _numparticles{0} { _particles.clear(); }
    ~System() { }
    std::vector<Particle>& get(void) { return _particles; }
    void add_particle(const Particle& _particle)
        _particles.push_back(_particle);
        _particles[_numparticles].id = _numparticles;
        _numparticles = _particles.size();
   }
    int size() const { return _numparticles; }
private:
                                         // Simulation box
   Box& _box;
   std::vector<Particle> _particles;
                                         // Standard library vector containing all particles
    int _numparticles;
                                         // Total number of particles in the system
};
```

Again, for future compatibility with the GPU our implementation is slightly different.

Our *System* class is an example of a *concrete* class. It essentially behaves as any built-in type since it contains the data (e.g., an std vector with particles) and some operations on that data (e.g., adding a new particle.

**Abstract classes** What about forces though? We gave several examples of forces (e.g., self-propulsion and soft-core repulsion). These are all, however, specific examples of a force. The question is if there is a way to abstract this notion away and instead define an interface to all possible (within reason!) forces, some of which we may want to implement in the future?

The answer to that is provided by the notion of an abstract class. An abstract class is an interface, i.e., it is impossible to create an object that is an instance of an abstract class. However, it is possible to inherit from it and create a class hierarchy with children classes that share the same interface as the parent class and provide as specific implementation. This allows us to create a robust system that can handle the entire class hierarchy and allows adding new functionality without having to make changes to the code that uses his class hierarchy.

At this point, this all sounds very abstract and overly convoluted. So, the best is to proceed with an example.

Let us create an abstract class called *Force* that will serve as the interface to all forces types (for simplicity, let us restrict to single-particle and pair-wise interactions).

The Force class looks like any other class with several important differences. The first one is that two of its member functions have a prefix **virtual**. This means that these functions will be overwritten by children classes and the precise version of the member function which is executed will be determined at the runtime. We will get back to this point shortly.

In addition, we have this somewhat strange line

```
virtual void compute() = 0;
```

private:

the "=0" notation means that the *compute* function is a pure virtual function, i.e., just a name holder. Any attempts to call *Force::compute()* will result in a compilation error. This just reflects the fact that one cannot simply compute a *force* without knowing what that force is.

Finally, we note that the keyword **protected** means that those data members will be accessible by the children classes.

Class inheritance Let us now implement a specific type of interaction, say, self-propulsion. We will do this by defining a class SelfPropulsionForce that is a child of the abstract class Force.

```
double _alpha; // strength of the self propulsion force
};
In the last example, line
class SelfPropulsionForce : public Force
```

means that the class SelfPropulsionForce is a child of the abstract class Force, i.e., it shares inherits its interface and some of its properties. The keyword **override** tells to C++ that this class "overrides", i.e., implements the actual computation of, in this case, self-propulsion force.

The power of this lies in how we can use the interface to access the children.

Let us look into the relevant part of the *Evolver* class, i.e., the past it stores and computes all forces.

```
class Evolver
public:
    //..
    void add_force(const std::string name, std::unique_ptr<Force> f)
    {
        // ...
        force list[name] = std::move(f); // Move is used here to transfer ownership of the
        // ...
    }
    //...
    void compute_forces()
        for (const auto& force : _force_list)
            force.second->compute();
    }
    // ...
private:
    std::map<std::string, std::unique ptr<Force>> force list; // list of all the pointer t
};
Let us analyze this example. First we note the line
std::map<std::string, std::unique_ptr<Force>> _force_list;
which tells the Evolver class to store all force types into a map (i.e., loosely speaking, a C++ version
```

which tells the *Evolver* class to store all force types into a map (i.e., loosely speaking, a C++ version of Python's dictionary) where keys are stings (i.e., name of the force, such as 'self-propulsion') and the value is a **unique pointer** to the *Force* object.

Reminder: A pointer is a variable that stores the address of another variable (e.g., an object). A raw pointer is dereferenced (i.e., the content of the memory location it points to is accessed) using the '' operator. However, when working with raw\* pointers the programmer has to ensure that the

memory is released back to the OS once the pointer goes out of scope. Otherwise, one can end up with often hard to track memory leaks.

There are two important points in here. A *unique pointer* is a version of a *smart pointer*. A *smart pointer* if a close cousin of the raw pointer with an important difference that it automatically disposes of the object it points to when it goes out of scope. A *unique pointer* is a special type of a smart pointer such that there can be only one copy of it.

The second important point is that we defined a unique pointer to the abstract *Force* class, i.e., this class will serve as the interface to all of its children. Precisely because of this 'place-holder' role we have to use pointers instead of bare types. In other words, a definition such as

```
std::map<std::string, Force> _force_list;
would not work, since it is impossible to create object of the abstract type Force.
In the main code, we would have a sequence like
₹
    // ...
    Evolver e(/* ... */);
    e.add_force("self-propulsion", std::unique_ptr<SelfPropulsionForce>(new SelfPropulsionForce
    e.compute_forces();
    // ...
}
Note an important thing here, although the member function
void add force(const std::string name, std::unique_ptr<Force> f)
of the Evolver class expects
std::unique_ptr<Force>
as it second parameter, in the line
e.add_force("self-propulsion", std::unique_ptr<SelfPropulsionForce>(new SelfPropulsionForce(2.)
```

we passed a unique pointer to the SelfPropulsionForce class instead. While this looks like a mistake, it is actually intended behavior, since the class Force acts as the interface to all implementations of force classes. Since we pass a pointer and not the actual object, the precise implementation of the virtual member functions can be decided at the runtime. Therefore, in this case, Evolver's compute\_force class will call the compute member function defined in the SelfPropulsionForce class.

This mechanics where we can use a base abstract type to refer to a wide range of *derived* (i.e., children) types is called *polymorphism* and is one of the central features of all modern object oriented languages.

Its power lies in the fact that if in the future we decide to implement, say, a *LennardJonesForce* class we do not need to modify the *Evolve* class at all. Instead, all we need to do would be write

```
{
    // ...
e.add_force("lennard-jones", std::unique_ptr<JennardJonesForce>(new LennardJonesForce(2.0,
    // ...
```

```
e.compute_forces();
// ...
}
```

in the main code.

### 1.2 Binding C++ and Python

In this section we briefly describe how to bind c++/CUDA with python. For that propose we are going to use header-only library that exposes C++ types in Python.

#### 1.2.1 Brief overview of the design layout: the interface

The following image below show how the interface with the simulation package.

<b>Note:</b> This is one of many design layouts that can be used. The one chosen here reflects

#### 1.2.2 The interface: pybind11

**pybind11** is a lightweight header-only library that provide a fast development interface to create Python bindings to existent C++ code. Here we supply a brief description on how to do that for our code.

**pybind11** have an excellent documentation so for brevity here we are only focus in how to expose classes and functions. Let us give several concrete examples of how to expose C++ code to Python.

#### 1.2.3 1. Exposing functions

Consider the following C++ function that apply periodic boundary conditions.

```
///<! Ofile: enforce_periodic.hpp
inline double enforce_periodic(const double &r, const double &L)
{
    double _r = r;
    if (box.periodic)
        if (r > 0.5*L)
            _r -= L;
        else if (r < -0.5*L)
            _r.x += L;
    }
    return _r;
}
Now, to expose double enforce_periodic(const double &r, const BoxType &box) into
Python we need a .cpp with the following
///<! Ofile: python_bindings_export.cpp
#include <pybind11/pybind11.h>
                                  ///<!Include the pybind11 library
#include "enforce_periodic.hpp"
                                  ///<!Include enforce_periodic.hpp
```

```
PYBIND11_MODULE(cppmodule, m)
{
    m.doc() = "pybind11 example"; ///<! optional module docstring
    m.def("enforce_periodic", &enforce_periodic, "Enforce periodic boundary conditions");
}</pre>
```

The PYBIND11\_MODULE() macro creates a function that can be called from within Python. The first argument in PYBIND11\_MODULE() is the *module name* (cppmodule( in our case), whereas the second macro m defines a variable of type py::module which is the main interface for creating bindings. Next, module::def() keyword generates binding code that exposes the enforce\_periodic() function to Python. Now from the python side with can do

```
from cppmodule import *
L = 10.0
x = 11.0
#New x
x_periodic = enforce_periodic(x, L)
```

#### 1.2.4 2. Exposing structured types

Structured types are classes that only contain *only* encapsulated data types such our **struct** Particle:

```
///<! Ofile: particle.hpp
/* @brief 1D particle type */
struct Particle
   int id;
                     // particle id
   int type;
                     // particle type
   real radius;
                     // particle radius
   real r;
                     // particle position
                     // particle velocity
   real v;
                      // particle force
   real f;
   real n;
                      // particle director
};
```

The following code show how expose this in python we need to understand first how to bind **classes** with pybind11

```
///<! @file: pybind_export_particle.hpp

#include "particle.hpp"

void export_ParticleType(py::module &m)
{
    py::class_<Particle>(m, "Particle")
        .def(py::init<>())
        .def readwrite("id", &Particle::id, "Particle id")
```

```
.def_readwrite("type", &Particle::type, "Particle material type")
.def_readwrite("radius", &Particle::radius, "Particle radius")
.def_readwrite("r", &Particle::r, "Particle positions")
.def_readonly("v", &Particle::v, "Particle velocity")
.def_readonly("f", &Particle::f, "Particle force");
.def_readwrite("n", &Particle::n, "Particle director");
}
Here the class_ creates bindings for a C++ class or struct-style data structure, and as in python classes, the init() takes the types of a constructor's parameters as template arguments and wraps
```

Here the class\_ creates bindings for a C++ class or struct-style data structure, and as in python classes, the init() takes the types of a constructor's parameters as template arguments and wraps the corresponding class constructor. In our case struct Particle doesn't define any constructor inside of C++ code but by using pybind is possible to extend this without modifying the particle.hpp file

```
///<! Ofile: pybind_export_particle.hpp
//..
{
    py::class_<Particle>(m, "Particle")
        .def(py::init<>()) ///<!default constructor</pre>
        .def("__init__", [](Particle &self, const int& id, const int& type, const real& radius
                    new (&self) Particle();
                    self. = x;
                    self.y = y;
                    self.id = id;
                                                // particle id
                                                // particle type
                    self.type = type;
                    self.radius = radius;
                                                // particle radius
                    self.r = r;
                                                // particle position
                                                // particle director
                    self.n = n
                    self.v = 0.0
                                                // particle velocity
                    self.f = 0.0
                                                // particle force
                })
        //..
}
Finally we need export the Particle type as follows
```

Now from the python side with can do

```
from cppmodule import *

p = Particle() # define an empty particle
p.id = 0
p.type = 0
p.radius = 1.0
p.x = 0.35
p.n = -1.0
p.f = -1.2 # Error read only variable!
# and so on ..
# or simple
p = Particle(0, 0, 1.0, 0.35, 1)
```

### 1.2.5 3. Export any type of class.

To export any type of class with function and variables we need to simple follows the steps 1 and 2 taking in account the following

Pybind in short

```
Type
                                                                        pybind interface
function
                                                     .def("myfunction", &myfunction)
                                                     py::class_<myclass>(py::module,
class
                                                                           "myclass"))
class constructor I
                                                  .def(py::init<var1, ..., varN>()))
class constructor II
                                                  .def("__init__", [](myclass &self,
                                                                     var1, ..., varN))
class read only variable
                                                         .def_readonly("myvariable",
                                                                &myclass::myvariable)
class read and write variable
                                                        .def_readwrite("myvariable",
                                                                &myclass::myvariable)
class function
                                                                   .def("myfunction",
                                                                &myclass::myfunction)
```

For more information visit pybind documentation page!!

As an example consider the SystemClass defined in ABPTutorial/c++/abpcpp/cppmodule/src/system,

```
void export_SytemClass(py::module &m)
{
    py::class_<SystemClass>(m, "System")
        .def(py::init<const BoxType &>())
        .def(py::init<const host::vector<ParticleType> &, const BoxType &>())
        .def("get_particles", &SystemClass::get)
        .def("add", &SystemClass::add_particle)
        .def("apply_periodic", &SystemClass::apply_periodic)
        .def("box", &SystemClass::get_box)
```

```
.def_readonly("Numparticles", &SystemClass::Numparticles)
;
}
```

## 1.3 Working Example

### 1.3.1 Review on particle-based simulation

As before our simulation workflow consists of three steps:

- 1. Creating the initial configuration;
- 2. Executing the simulation;
- 3. Analyzing the results.

Where, the step 1 feeds into step 2, which, in turn feeds into step 3. The step 1 generate the system configuration for our simulation as a single JSON file (see Python/pymd/builder or ABPTutorial/c++/abpcpp/builder).

```
<b>Reminder:</b>
```

To generate configurations we need to do the following.

```
from cppmd.builder import *
phi = 0.4
L = 50
a = 1.0
random_init(phi, L, rcut=a, outfile='init.json')
```

Where,  $\phi$  is the number density, L is the box's size, and a the particle radius.

Let us start with a working example of a full simulation.

We read the initial configuration stored in the file *init.json* with N=4,000 randomly placed particles in a square box of size L=100. We assume that all particles have the same radius a=1. Further, each particle is self-propelled with the active force of magnitude  $\alpha=1$  and experiences translational friction with friction coefficient  $\gamma_t=1$ . Rotational friction is set to  $\gamma_r=1$  and the rotational diffusion constant to  $D_r=0.1$ . Particles within the distance d=2 of each other experience the polar alignment torque of magnitude J=1.

We use the time step  $\delta t = 0.01$  and run the simulation for 1,000 time steps. We record a snapshot of the simulation once every 10 time steps.

```
[]: %matplotlib widget
import matplotlib.pyplot as plt
import cppmd as md

particles, box = md.read_json("initphi=0.4L=100.json")
system = md.System(particles, box)

dump = md.Dump(system)  # Create a dump object
dump.show()  # Plot the particles with matplotlib
```

```
plt.show()
evolver = md.Evolver(system)
                                # Create a system evolver object
#add the forces and torques
# Create pairwise repulsive interactions with the spring contant k = 10 and
\rightarrow range a = 2.0
evolver.add force("Harmonic Force", {"k":10.0, "a":2.0})
# Create self-propulsion, self-propulsion strength alpha = 1.0
evolver.add_force("Self Propulsion", {"alpha":1.0})
# Create pairwise polar alignment with alignment strength J = 1.0 and range a = 1
→2.0
evolver.add_torque("Polar Align", {"k":1.0, "a":2.0})
#add integrators
# Integrator for updating particle position, friction gamma = 1.0, "random"
⇒seed" seed = 10203 and no thermal noise
evolver.add_integrator("Brownian Positions", {"T":0.0, "gamma":1.0, "seed":
→10203})
# Integrator for updating particle orientation, friction gamma = 1.0,,,
\rightarrow "rotation" T = 0.1, D_r = 0.0, "random seed" seed = 10203
evolver.add integrator("Brownian Rotation", {"T":0.1, "gamma":1.0, "seed":
→10203})
evolver.set_time_step(1e-2) # Set the time step for all the integrators
```

#### 1.4 Visualizing results

As before we have save our output files using VTK format. For convenience here we also provide with a paraview state file which will allow you to rapidly plot the results.

#### 1.4.1 Instructions:

- 1. Open paraview.
- 2. Go to File->Load State->paraview\_plotter.py

If you desire to change the names of the output file or the number/snapshoot steps you will need to modify the following lines in paraview\_plotter.py.