

$$D = \begin{bmatrix} I_{22,1} \\ 0 \\ 0 \end{bmatrix}$$

$$(I_{xy}, s^2 y_1, s^2 y_2 + I_{xy,2} c^2 y_1 + I_{zz,2} s^2 y_1, s^2 y_2)$$

$$\begin{bmatrix} I_{xy,2} s^2 y_1 (c^2 (y_2 + y_3) - 2c(y_2 + y_3) s(y_2 + y_3)) + \\ s^2 (y_2 + y_3) + I_{xy,2} c^2 y_1 + I_{zz,2} s^2 y_1, ( \\ c^2 y_2 s^2 y_3 + 2c y_2 c y_3 s y_3 + s^2 y_2 c^2 y_3) \end{bmatrix}$$

$$\begin{bmatrix} y_1 \\ y_2 \\ y_3 \end{bmatrix}$$

$G$  is  $3 \times 1$

$$G =$$

$$\begin{bmatrix} 0 & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & 0 \end{bmatrix}$$

$$G(y) = \begin{bmatrix} 0 \\ -mg \frac{L^2}{2} s y_2 + mg L_2 (s y_2 c y_3 + c y_2 s y_3) \\ mg \frac{L^2}{2} (-c y_2 s y_3 - s y_2 c y_3) \end{bmatrix}$$

$$\mathcal{L} = \begin{pmatrix} \dot{q}_1 \\ \dot{q}_2 \end{pmatrix}$$

$$\frac{1}{2} \dot{q}_2 (I_{xx,2} \dot{q}_1^2 \dot{q}_2 - I_{xy,2} \dot{q}_1 \dot{q}_2 + I_{zz,2} \dot{q}_1 \dot{q}_2^2)$$

$$\begin{pmatrix} \dot{q}_1 \\ \dot{q}_2 \\ \dot{q}_3 \end{pmatrix}$$

$$\begin{aligned} & \frac{1}{2} \dot{q}_3 [I_{xx,3} \dot{q}_1^2 \dot{q}_3 - 2 \dot{q}_1 \dot{q}_2 \dot{q}_3 + I_{zz,3} \dot{q}_1^2 \dot{q}_3 + I_{yy,3} \dot{q}_2^2 \dot{q}_3 + I_{zz,3} \dot{q}_2^2 \dot{q}_3 + I_{zz,3} \dot{q}_3^2 \dot{q}_3] \\ & \dot{q}_2 \dot{q}_3 + \dot{q}_2^2 \dot{q}_3 \end{aligned}$$

$$\frac{1}{2} \dot{q}_2 (-I_{xx,2} \dot{q}_1^2 \dot{q}_2 + I_{zz,2} \dot{q}_1^2 \dot{q}_2^2)$$

$$\begin{aligned} & \frac{1}{2} \dot{q}_3 [I_{xx,3} \dot{q}_1^2 \dot{q}_3 - 2 \dot{q}_1 \dot{q}_2 \dot{q}_3 + I_{zz,3} \dot{q}_1^2 \dot{q}_3 + I_{yy,3} \dot{q}_2^2 \dot{q}_3 + I_{zz,3} \dot{q}_2^2 \dot{q}_3 + I_{zz,3} \dot{q}_3^2 \dot{q}_3] \\ & \dot{q}_2 \dot{q}_3 + \dot{q}_2^2 \dot{q}_3 \end{aligned}$$

$$\begin{aligned} & \frac{1}{2} \dot{q}_3 [I_{xx,3} \dot{q}_1^2 \dot{q}_3 - 2 \dot{q}_1 \dot{q}_2 \dot{q}_3 + I_{zz,3} \dot{q}_1^2 \dot{q}_3 + I_{yy,3} \dot{q}_2^2 \dot{q}_3 + I_{zz,3} \dot{q}_2^2 \dot{q}_3 + I_{zz,3} \dot{q}_3^2 \dot{q}_3] \\ & \dot{q}_2 \dot{q}_3 + \dot{q}_2^2 \dot{q}_3 \end{aligned}$$