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CIS 457

## Homework 2

Questions 1 and 2:

**Question 1:**  $A = \begin{bmatrix} a_{11} & a_{12} \\ a_{21} & a_{22} \end{bmatrix}$   $A^{-1} = \begin{bmatrix} a_{22}/D & -a_{12}/D \\ -a_{21}/D & a_{11}/D \end{bmatrix}$   
 $D = a_{11}a_{22} - a_{12}a_{21}$

$AA^{-1} = \begin{bmatrix} \frac{a_{11}(a_{22})}{D} + (-\frac{a_{12}a_{21}}{D}), & -\frac{a_{11}(a_{12})}{D} + \frac{a_{12}a_{11}}{D} \\ \frac{a_{21}a_{22}}{D} - \frac{a_{21}a_{22}}{D}, & -\frac{a_{21}a_{12}}{D} + \frac{a_{11}a_{22}}{D} \end{bmatrix}$

$\begin{bmatrix} \frac{D}{D} & 0 \\ 0 & \frac{D}{D} \end{bmatrix} = \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix} = I \checkmark$

**Question 2)**

**Pt in Triangle**  
 Draw a line from each vertex of the triangle ( $PA, PB, PC$ )  
 Determine the orientation of triangle formed by the lines ( $ABP, BCP, CAP$ )  
 If all orientations are the same the point is in the triangle else it is outside of the triangle.

**Pt in Polygon**  
 Draw a line to the right extending out of the polygon.  
 Count the edges that intersect the line.  
 If odd # of edges Pt is inside polygon, even # of edges Pt is outside.

Question 3:

### 3) Tools 2D, area 2

uses the cross product of 2 vectors to determine the double the area in between the vectors.

area 2 is generalized for any polygon by  $\sum_{i=0}^{n-1} (x_i y_{i+1} - y_i x_{i+1})$

Area 2 is used to find if a point is in a polygon/triangle, if a point can be projected on a line, and if a point is on a line.

#### Question 4:

```
import java.awt.*;
import java.awt.event.MouseAdapter;
import java.awt.event.MouseEvent;
import java.awt.event.WindowAdapter;
import java.awt.event.WindowEvent;
import java.util.Vector;

public class Question4 extends Frame {

    public static void main(String[] args)

    {new Question4();}
    Question4()
    {

        super("Define vertices by clicking");
```

```

        addWindowListener(new WindowAdapter()
        { public void windowClosing(WindowEvent e)
        { System.exit(0);}
        });

        setSize (500, 300);
        add("Center", new Lines());
        setCursor(Cursor.getPredefinedCursor(Cursor.CROSSHAIR_CURSOR));
        show();
    }
}

```

```

class Lines extends Canvas {

```

```

    Vector v = new Vector();

```

```

    Point2D a, b, c, d;
    float x0, y0, rWidth = 10.0F, rHeight = 7.5F, pixelSize, xI,yI;
    boolean ready = true;
    int centerX, centerY;
    int clickCounter = 0;

```

```

    Lines() {
        addMouseListener(new MouseAdapter() {
            public void mousePressed(MouseEvent evt) {
                float xA = fx(evt.getX()), yA = fy(evt.getY());
                float dx = xA - x0, dy = yA - y0;
                if (clickCounter < 4) {
                    v.addElement(new Point2D(xA, yA));
                    clickCounter = clickCounter + 1;
                    repaint();
                    ready = true;
                } else if (clickCounter == 4) {
                    ready = false;
                    v.addElement(new Point2D(xA, yA));
                }
            }
        });
    }
}

```

```

    public void paint(Graphics g) {

```

```

        g.drawString("Click Four Points to create two lines.", 5, 20);

```

```

        g.setColor(Color.white);

```

```

        selection();
        int left = iX(-rWidth / 2), right = iX(rWidth / 2),
            bottom = iY(-rHeight / 2), top = iY(rHeight / 2) + 60;
        g.drawRect(left, top - 15, right - left, bottom - top);
        g.fillRect(left, top - 15, right - left, bottom - top);
        g.setColor(Color.red);

```

```

        int n = 4;
        if (n == 0) return;
        a = (Point2D) (v.elementAt(0));
        g.fillOval(iX(a.x) - 2, iY(a.y) - 2, 4, 4);

```

```

for (int i = 1; i<n; i++) {
    if (i == (4) && !ready) {
        break;
    }

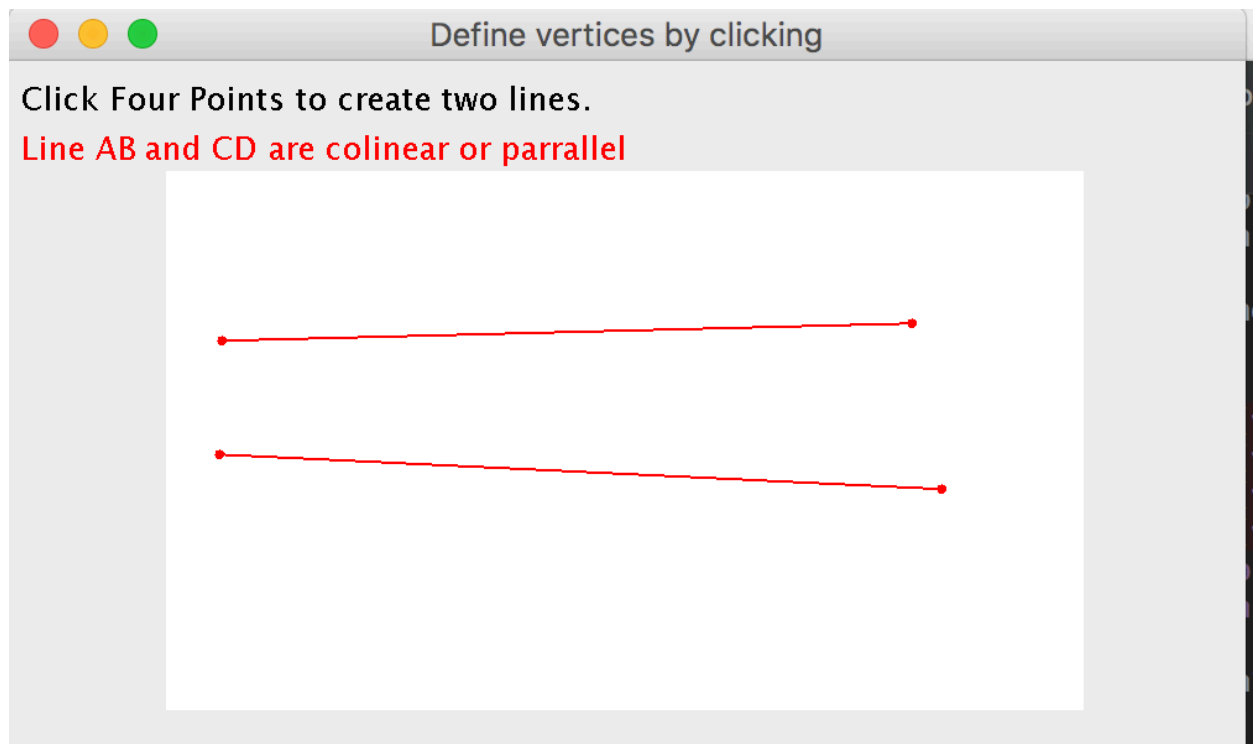
    Point2D b = (Point2D) (v.elementAt(i % n));
    g.fillOval(iX(b.x) - 2, iY(b.y) - 2, 4, 4);
    if(i!=2)
        g.drawLine(iX(a.x), iY(a.y), iX(b.x), iY(b.y));
    a = b;
}
a=(Point2D) (v.elementAt(0));
b=(Point2D) (v.elementAt(1));
c=(Point2D) (v.elementAt(2));
d=(Point2D) (v.elementAt(3));
double a1 = b.y - a.y;
double b1 = a.x - b.x;

double c1 = a1*(a.x) + b1*(a.y);

// Line CD represented as a2x + b2y = c2
double a2 = d.y - c.y;
double b2 = d.x - c.x;
double c2 = a2*(c.x)+ b2*(c.y);

double determinant = a1*b2 - a2*b1;
double epsilon=(Math.pow(10.0,-
3.0)*(Math.pow(b1,2)+Math.pow(a1,2)+Math.pow(d.x-c.x,2)+Math.pow(a2,2)));
if (determinant<=epsilon)
{
    g.drawString("Line AB and CD are colinear or parrallel", 5, 40);
}
else
{
    double x = (b2*c1 - b1*c2)/determinant;
    double y = (a1*c2 - a2*c1)/determinant;
    g.drawOval(iX((float)x)-5, iY((float)y)-5, 10, 10);
}

```



Question 5:

```
import java.awt.*;
import java.awt.event.*;
import java.util.*;
import java.awt.Graphics;

public class Question5 extends Frame {

    public static void main(String[] args)

    {new Question5();}
    Question5()
    {

        super("Define vertices by clicking");
        addWindowListener(new WindowAdapter()
        { public void windowClosing(WindowEvent e)
        { System.exit(0);}
        });

        setSize (500, 300);
        add("Center", new Poly());
        setCursor(Cursor.getPredefinedCursor(Cursor.CROSSHAIR_CURSOR));
        show();
    }
}
class Tools2D
{
```



```

static float area2(Point2D a, Point2D b, Point2D c)
{ return (a.x - c.x) * (b.y - c.y) - (a.y - c.y) * (b.x - c.x); }

static boolean onSegment(Point2D a, Point2D b, Point2D p)
{ double dx = b.x - a.x, dy = b.y - a.y,
  eps = 0.001 * (dx * dx + dy * dy);
  return
    (a.x != b.x &&
     (a.x <= p.x && p.x <= b.x || b.x <= p.x && p.x <= a.x)
     || a.x == b.x &&
     (a.y <= p.y && p.y <= b.y || b.y <= p.y && p.y <= a.y))
     && Math.abs(Tools2D.area2(a, b, p)) < eps; }

static boolean ccw(Point2D[] p)
{ int n = p.length, k=0;
  for (int i=1; i<n; i++)
    if (p[i].x <= p[k].x && (p[i].x < p[k].x || p[i].y <
      p[k].y))
      k=i;
  int prev = k - 1, next = k + 1;
  if (prev == -1) prev = n - 1;
  if (next == n) next = 0;
  return Tools2D.area2(p[prev], p[k], p[next]) > 0; }

static boolean insideTriangle(Point2D a, Point2D b, Point2D c, Point2D p)
{ return
  Tools2D.area2(a, b, p) >= 0 &&
  Tools2D.area2(b, c, p) >= 0 &&
  Tools2D.area2(c, a, p) >= 0; }
}

class Poly extends Canvas {

  Vector v = new Vector();
  Vector p = new Vector();
  Point2D aa, bb, cc, pp;
  float x0, y0, rWidth = 10.0F, rHeight = 7.5F, pixelSize;
  boolean ready = true;
  int centerX, centerY;
  int clickCounter = 0;

  Poly() {
    addMouseListener(new MouseAdapter() {
      public void mousePressed(MouseEvent evt) {
        float xA = fx(evt.getX()), yA = fy(evt.getY());
        float dx = xA - x0, dy = yA - y0;
        if (clickCounter < 4) {
          v.addElement(new Point2D(xA, yA));
          clickCounter = clickCounter + 1;
          repaint();
          ready = true;
        } else if (clickCounter == 4) {
          ready = false;
          v.addElement(new Point2D(xA, yA));
        }
      }
    })
  }
}

```

```

});
}

public void paint(Graphics g) {
    Tools2D tools2D = new Tools2D();
    g.drawString("Click Three Points to paint a Triangle.", 5, 20);
    g.drawString("Click a Fourth Point to Select Point P.", 5, 40);
    g.setColor(Color.white);

    selection();
    int left = iX(-rWidth / 2), right = iX(rWidth / 2),
        bottom = iY(-rHeight / 2), top = iY(rHeight / 2) + 60;
    g.drawRect(left, top - 15, right - left, bottom - top);
    g.fillRect(left, top - 15, right - left, bottom - top);
    g.setColor(Color.red);

    int n = 3;
    if (n == 0) return;
    Point2D a = (Point2D) (v.elementAt(0));
    g.fillOval(iX(a.x) - 2, iY(a.y) - 2, 4, 4);

    for (int i = 1; i <= n; i++) {
        if (i == (n) && !ready) {
            break;
        }
        Point2D b = (Point2D) (v.elementAt(i % n));
        g.fillOval(iX(b.x) - 2, iY(b.y) - 2, 4, 4);
        g.drawLine(iX(a.x), iY(a.y), iX(b.x), iY(b.y));
        a = b;
    }

    //Draws x on fourth point p as an X:
    g.setColor(Color.blue);
    Point2D p = (Point2D) (v.elementAt(3));
    float pX = p.x, pY = p.y;
    g.drawLine(iX(pX) - 3, iY(pY) + 3, iX(pX) + 3, iY(pY) - 3);
    g.drawLine(iX(pX) - 3, iY(pY) - 3, iX(pX) + 3, iY(pY) + 3);
    Point2D[] pointsArray = new Point2D[4];
    int k = 0;
    for (k = 0; k < pointsArray.length; k++) {
        pointsArray[k] = (Point2D) (v.elementAt(k));
    }

    if (Tools2D.onSegment(pointsArray[2], pointsArray[0], pointsArray[3]) == true
        || Tools2D.onSegment(pointsArray[0], pointsArray[1], pointsArray[3])
== true
        || Tools2D.onSegment(pointsArray[1], pointsArray[2], pointsArray[3])
== true) {
        g.drawString("Point P lies on an edge of triangle ABC.", 5, 230);
    } else {
        //Test if Triangle orientation is ccw
        if (Tools2D.ccw(pointsArray)) {
            if (Tools2D.insideTriangle(pointsArray[0], pointsArray[1],
pointsArray[2], pointsArray[3])) {
                g.drawString("Point P lies inside of triangle ABC", 5, 230);
            } else {
                g.drawString("Point P lies outside of triangle ABC", 5, 230);
            }
        } else
    }
}

```

```

        {
            if (tools2D.insideTriangle(pointsArray[2], pointsArray[1],
pointsArray[0], pointsArray[3])) {
                g.drawString("Point P lies inside of triangle ABC", 5, 230);
            } else {
                g.drawString("Point P lies outside of triangle ABC", 5, 230);
            }
        }
    }
}

void selection() {
    Dimension d = getSize();
    int maxX = d.width - 1, maxY = d.height - 1;
    pixelSize = Math.max(rWidth / maxX, rHeight / maxY);
    centerX = maxX / 2;
    centerY = maxY / 2;
}

int iX(float x) {
    return Math.round(centerX + x / pixelSize);
}

int iY(float y) {
    return Math.round(centerY - y / pixelSize);
}

float fx(int x) {
    return (x - centerX) * pixelSize;
}

float fy(int y) {
    return (centerY - y) * pixelSize;
}
}

class Point2D {
    float x, y;
    Point2D(float x, float y){this.x = x; this.y = y;}}

```



