

# 1.2 – Technology and Cost

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 [ios23.classes.ryansafner.com](https://ios23.classes.ryansafner.com)



# Outline



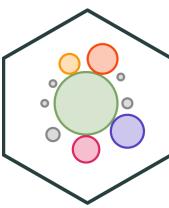
Short Run Production Concepts

Costs in the Short Run

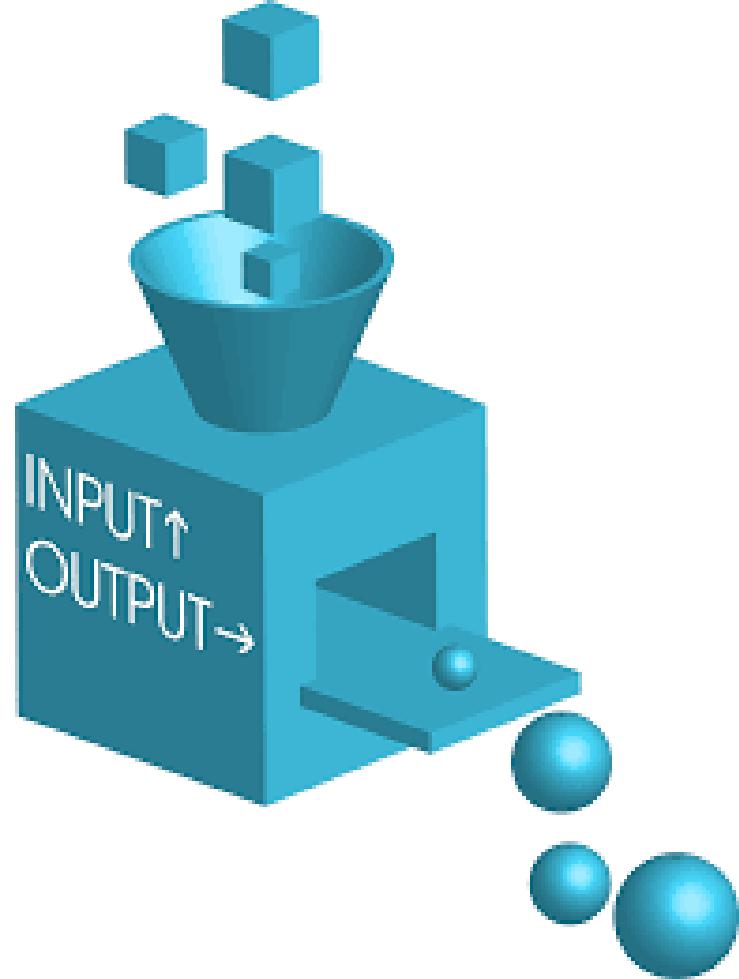
Costs in the Long Run

Revenues

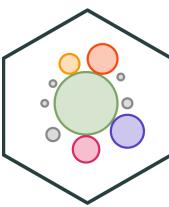
# This Black Box We Call "Firms"



- Firm is a mere production process:
  - a bundle of technology, physical assets, and individuals
- Synonymous with production function
- Fully replicable
- We'll explore (and explode) this much later



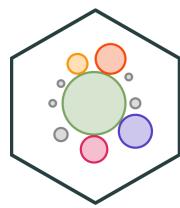
# What Do Firms Do? I



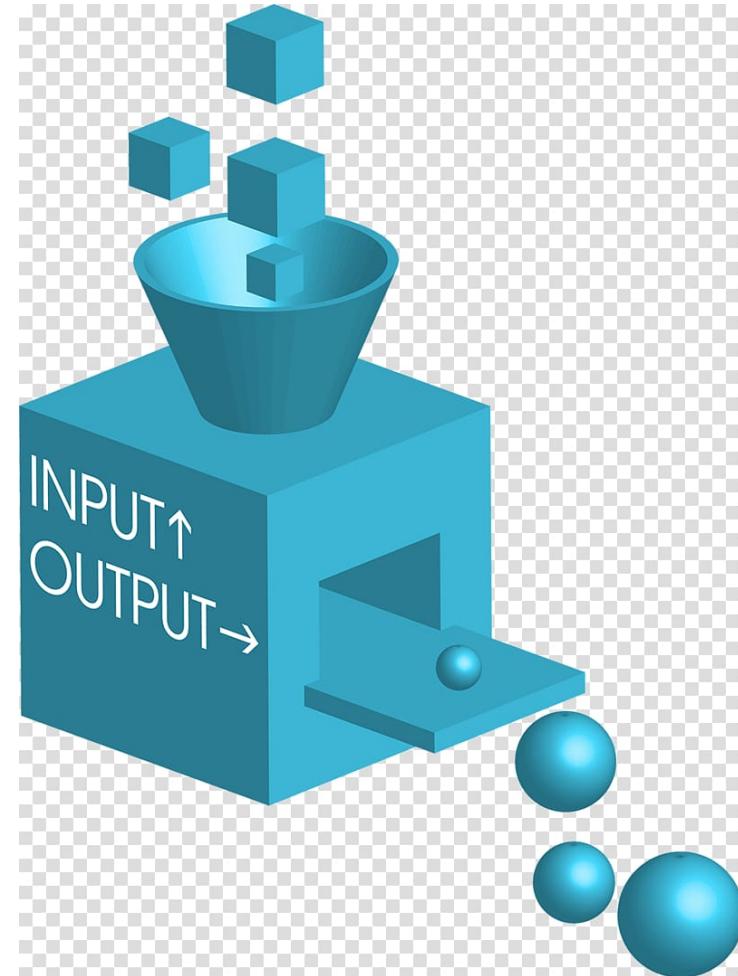
- We'll assume “the firm” is the agent to model:
- So what do firms do?
- How would we set up an optimization model:
  1. **Choose:** < some alternative >
  2. **In order to maximize:** < some objective >
  3. **Subject to:** < some constraints >



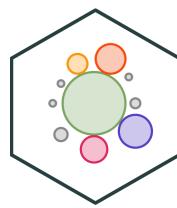
# What Do Firms Do? II



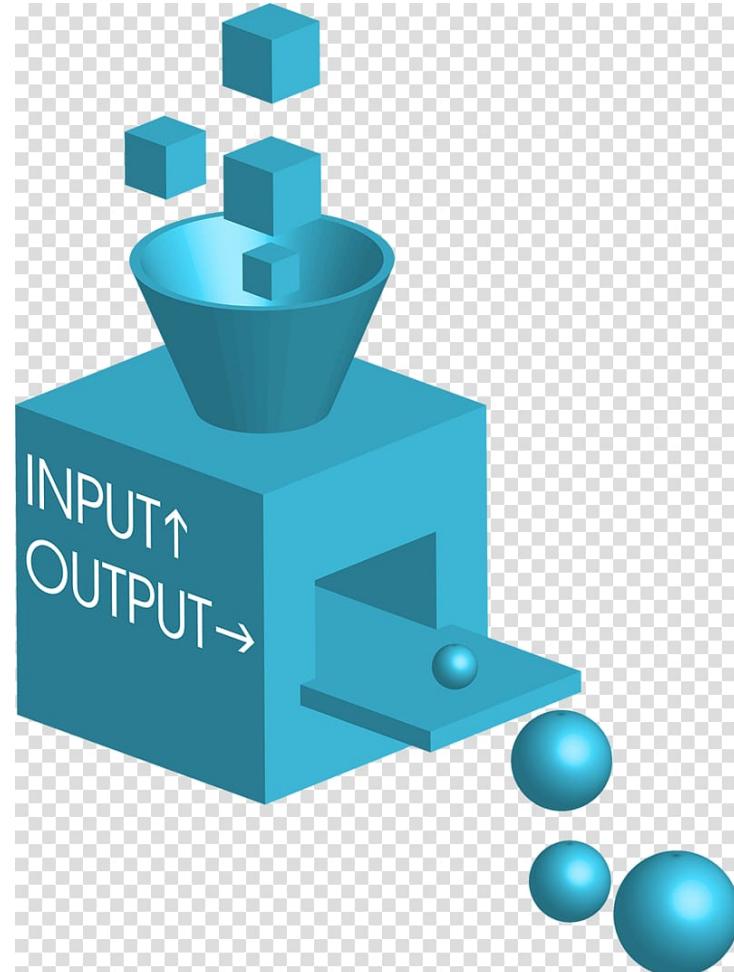
- Firms convert some goods to other goods:



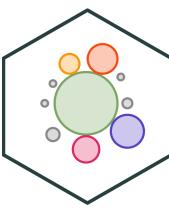
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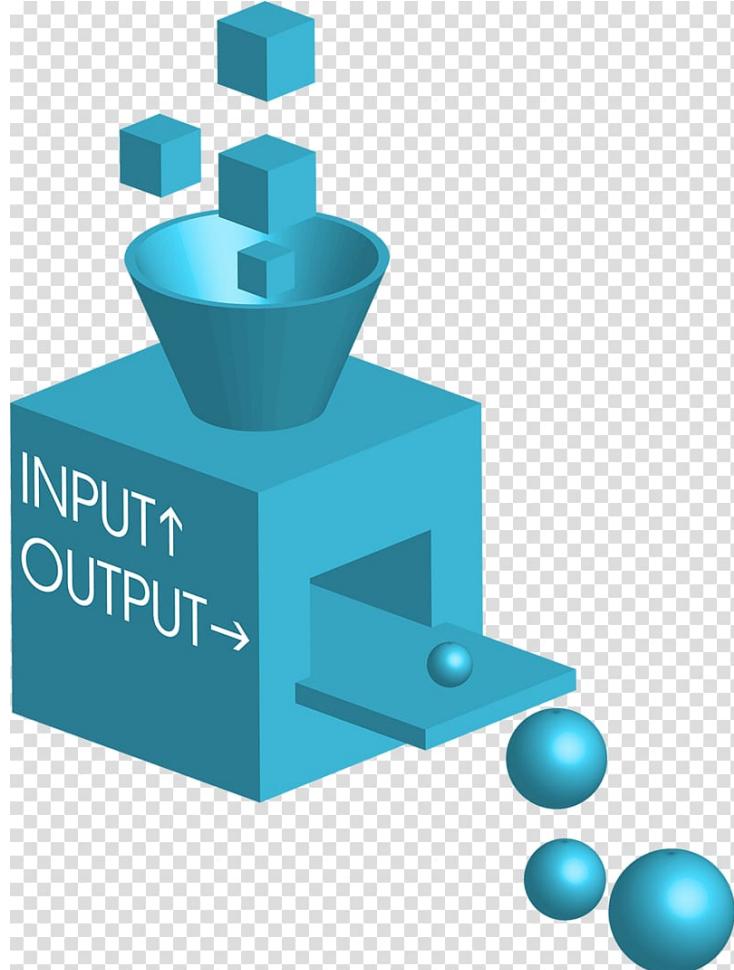
- Firms convert some goods to other goods:
- **Inputs:**  $x_1, x_2, \dots, x_n$ 
  - **Examples:** worker efforts, warehouse space, electricity, loans, oil, cardboard, fertilizer, computers, software programs, etc



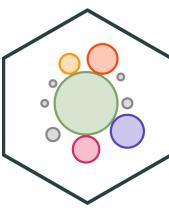
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- Firms convert some goods to other goods:
- **Inputs:**  $x_1, x_2, \dots, x_n$ 
  - **Examples:** worker efforts, warehouse space, electricity, loans, oil, cardboard, fertilizer, computers, software programs, etc
- **Output:**  $q$ 
  - **Examples:** gas, cars, legal services, mobile apps, vegetables, consulting advice, financial reports, etc

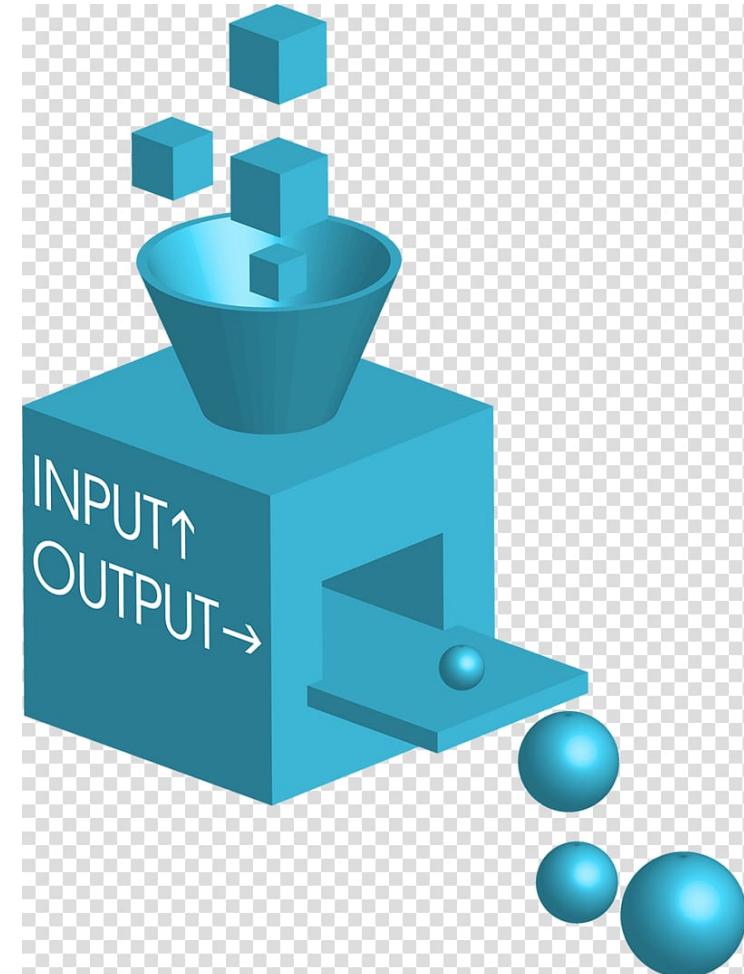


# What Do Firms Do? III

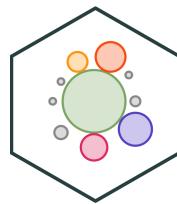


- **Technology** or a **production function**:  
rate at which firm can convert specified  
**inputs** ( $x_1, x_2, \dots, x_n$ ) into **output**  
( $q$ )

$$q = f(x_1, x_2, \dots, x_n)$$



# Production Function as Recipe



## The production function

READY IN: 1hr 20mins

YIELD: 2 loaves

UNITS: US

### INGREDIENTS

#### Nutrition

5 cups all-purpose  
white flour

2 tablespoons yeast (or  
2 x 7g pkts)

2 teaspoons sugar

1 teaspoon salt

2 cups warm-hot water

$\frac{1}{4}$  cup cooking oil

## The production algorithm

### DIRECTIONS

Put 4 cups of the flour, yeast, sugar and salt into large bowl.

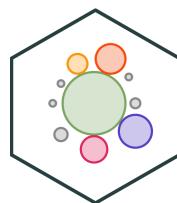
Pour in hot water and oil and mix until combined- it will be sticky.

Add the remaining flour in increments until dough is no longer sticky.

Knead for about 5 minutes until dough is elastic and smooth.

Place dough back into bowl and cover with a damp teatowel and let it rise until double its size- about 1/2 hour.

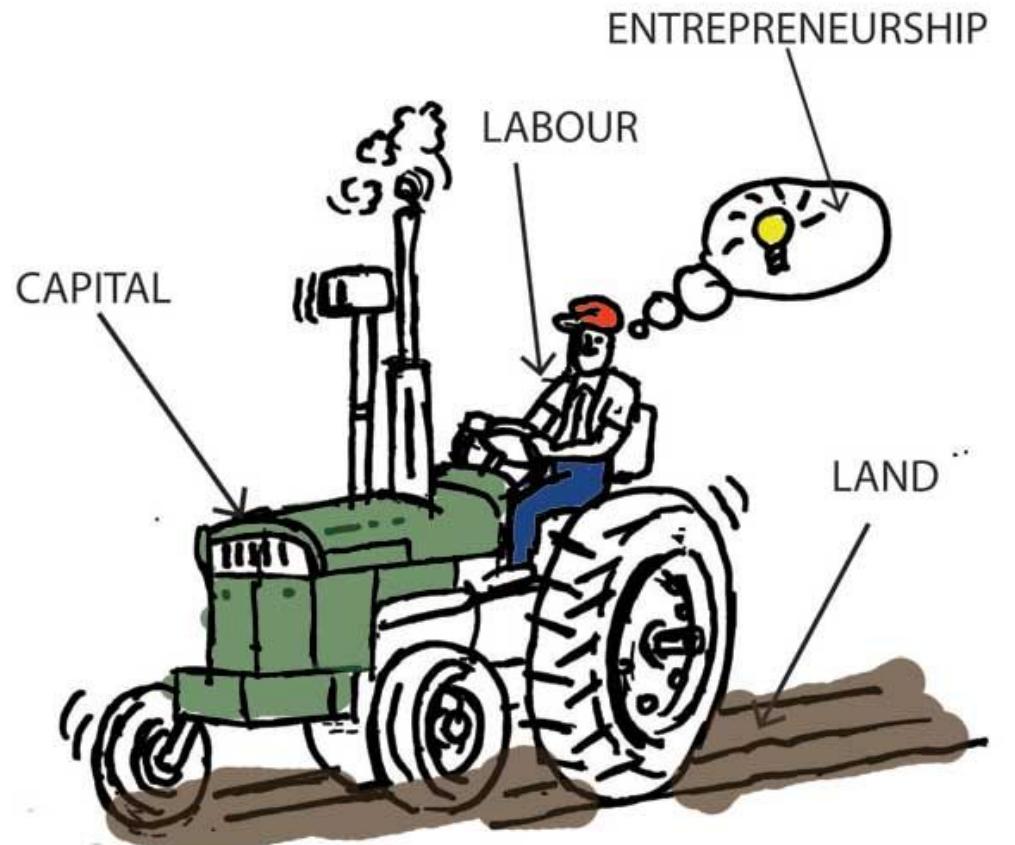
# Factors of Production I



$$q = A f(t, l, k)$$

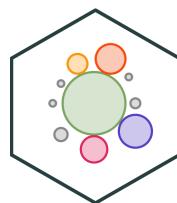
- Economists typically classify inputs, called the **“factors of production” (FOP)**:

Factor	Owned By	Earns
Land (t)	Landowners	Rent
Labor (l)	Laborers	Wages
Capital (k)	Capitalists	Interest



- $A$ : "total factor productivity"  
(ideas/knowledge/institutions)

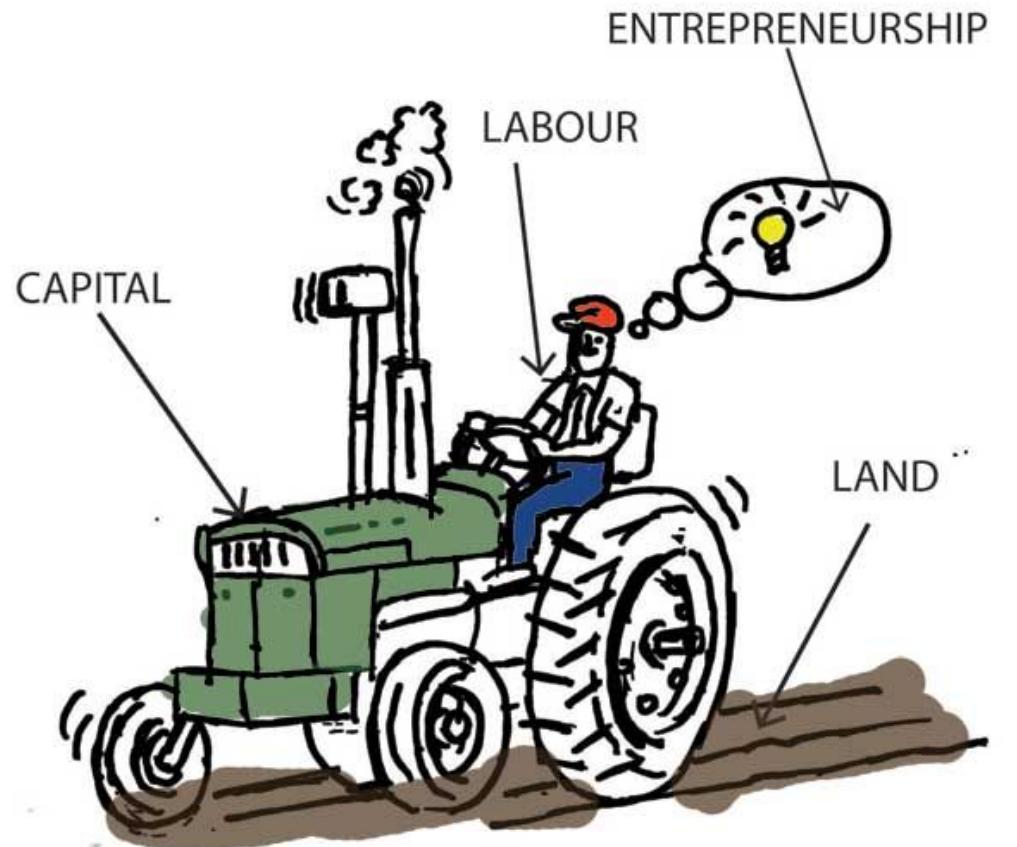
# Factors of Production II



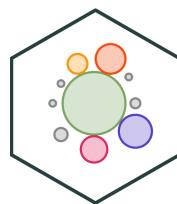
$$q = f(l, k)$$

- We will assume just two inputs: labor  $l$  and capital  $k$

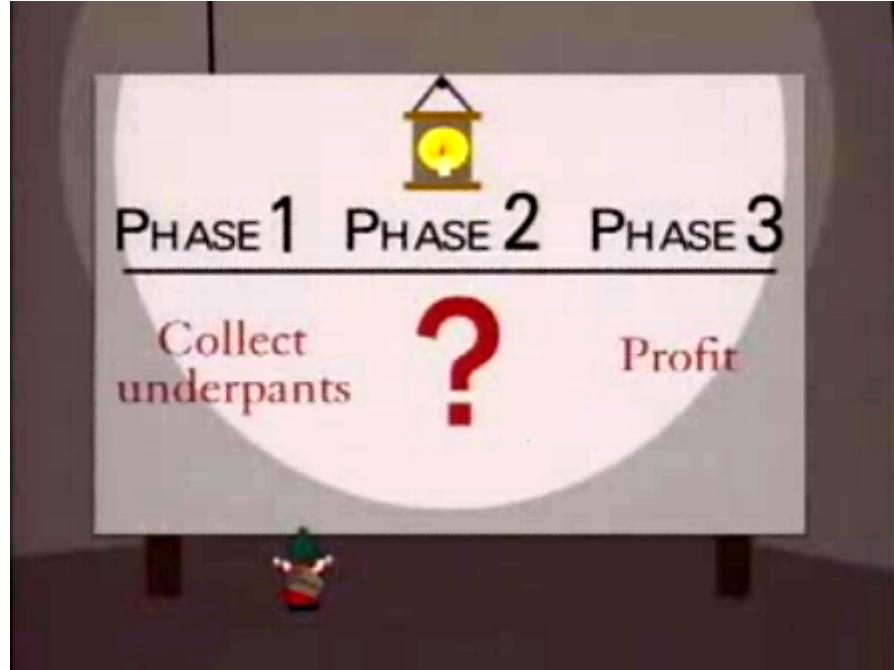
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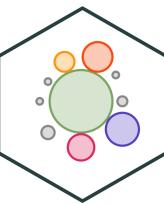
# What Does a Firm Maximize?



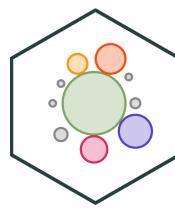
- We assume firms **maximize profit** ( $\pi$ )
- Not true for all firms
  - **Examples:** non-profits, charities, civic associations, government agencies, criminal organizations, etc
- Even profit-seeking firms may also want to maximize *additional* things
  - **Examples:** goodwill, sustainability, social responsibility, etc



# Profits Have a Bad Rap These Days



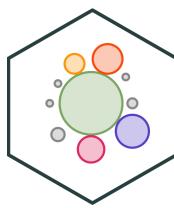
# What is Profit?



- In economics, **profit** is simply **benefits minus (opportunity) costs**



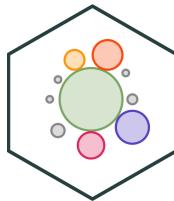
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- Suppose firm sells **output  $q$**  at price  $p$



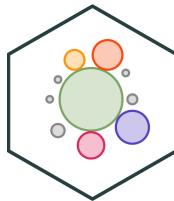
# What is Profit?



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- Suppose firm sells **output**  $q$  at price  $p$
- It can buy each **input**  $x_i$  at an associated price  $p_i$ , i.e.
  - labor  $l$  at wage rate  $w$
  - capital  $k$  at rental rate  $r$



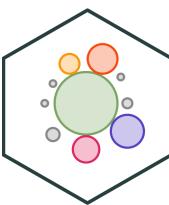
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  - labor  $l$  at wage rate  $w$
  - capital  $k$  at rental rate  $r$
- The profit of selling  $q$  units and using inputs  $l, k$  is:



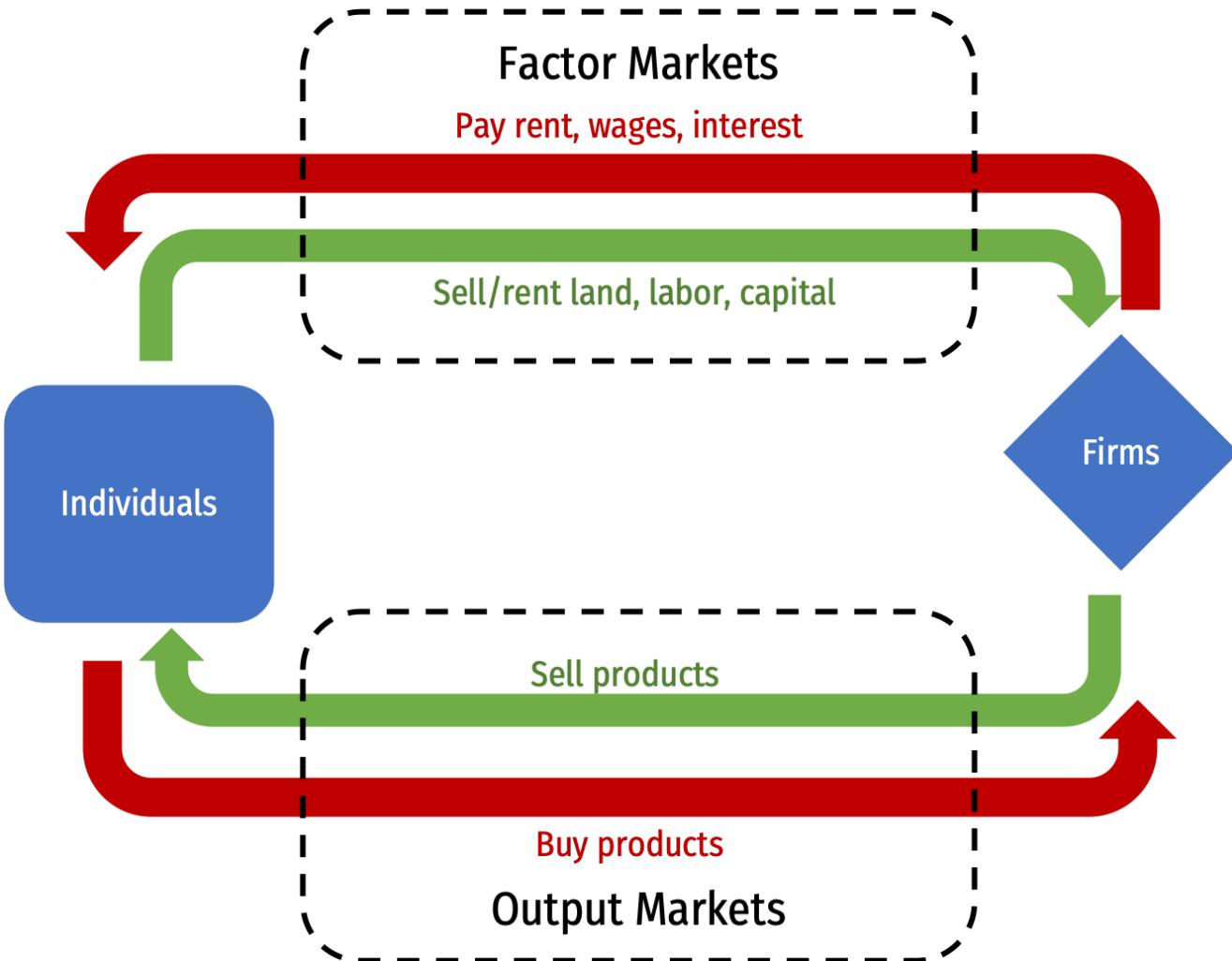
# Who Gets the Profits? I



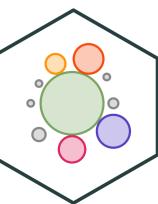
$$\pi = \underbrace{pq}_{revenues} - \underbrace{(wl + rk)}_{costs}$$



# Reminder from Macroeconomics: “The Circular Flow”



# Who Gets the Profits? I

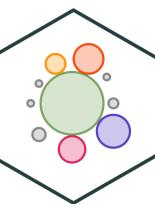


$$\pi = \underbrace{pq}_{revenues} - \underbrace{(wl + rk)}_{costs}$$

- The firm's costs are all of the factor-owner's incomes!
  - Landowners, laborers, creditors are all paid rent, wages, and interest, respectively



# Who Gets the Profits? I

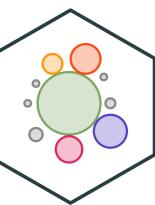


$$\pi = \underbrace{pq}_{\text{revenues}} - \underbrace{(wl + rk)}_{\text{costs}}$$

- Profits are the **residual value** leftover after paying all factors
- Profits are income for the **residual claimant(s)** of the production process (i.e. **owner(s)** of a firm):
  - Entrepreneurs
  - Shareholders



# Who Gets the Profits? II

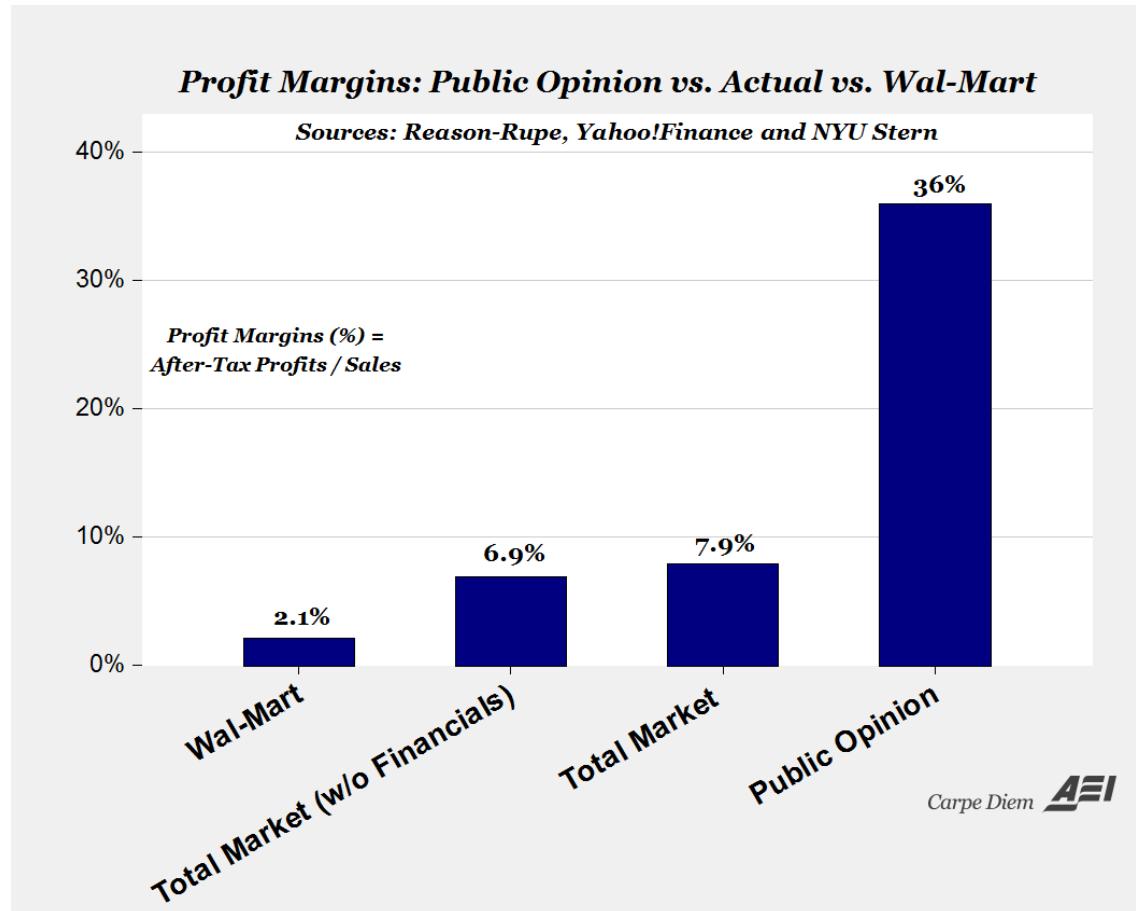
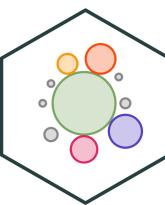


$$\pi = \underbrace{pq}_{\text{revenues}} - \underbrace{(wl + rk)}_{\text{costs}}$$

- Residual claimants have incentives to maximize firm's profits, as this *maximizes their own income*
- Entrepreneurs and shareholders are the only participants in production that are *not* guaranteed an income!
  - Starting and owning a firm is inherently **risky**!

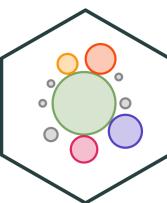


# People Overestimate Profits



Source: [American Enterprise Institute](#)

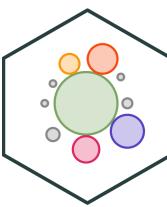
# Profits and Entrepreneurship: A Preview



- In markets, production must face the **profit test**:
  - Is consumer's willingness to pay > opportunity cost of inputs?
- Profits are an indication that **value is being created for society**
- Losses are an indication that **value is being destroyed for society**
- Survival in markets *requires* firms continually create value & earn profits



# The Firm's Optimization Problem I



- So what do firms do?

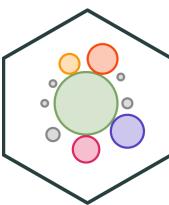
1. **Choose:** <some alternative>
2. **In order to maximize:** <profits>

3. **Subject to:** <technology>

- We've so far assumed they maximize profits and they are limited by their technology



# The Firm's Optimization Problem II



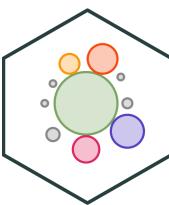
- What do firms **choose**? (Not an easy answer)
- Prices?
  - Depends on the market the firm is operating in!
  - Study of **industrial organization**
- Essential question: **how competitive is a market?** This will influence what firms (can) do



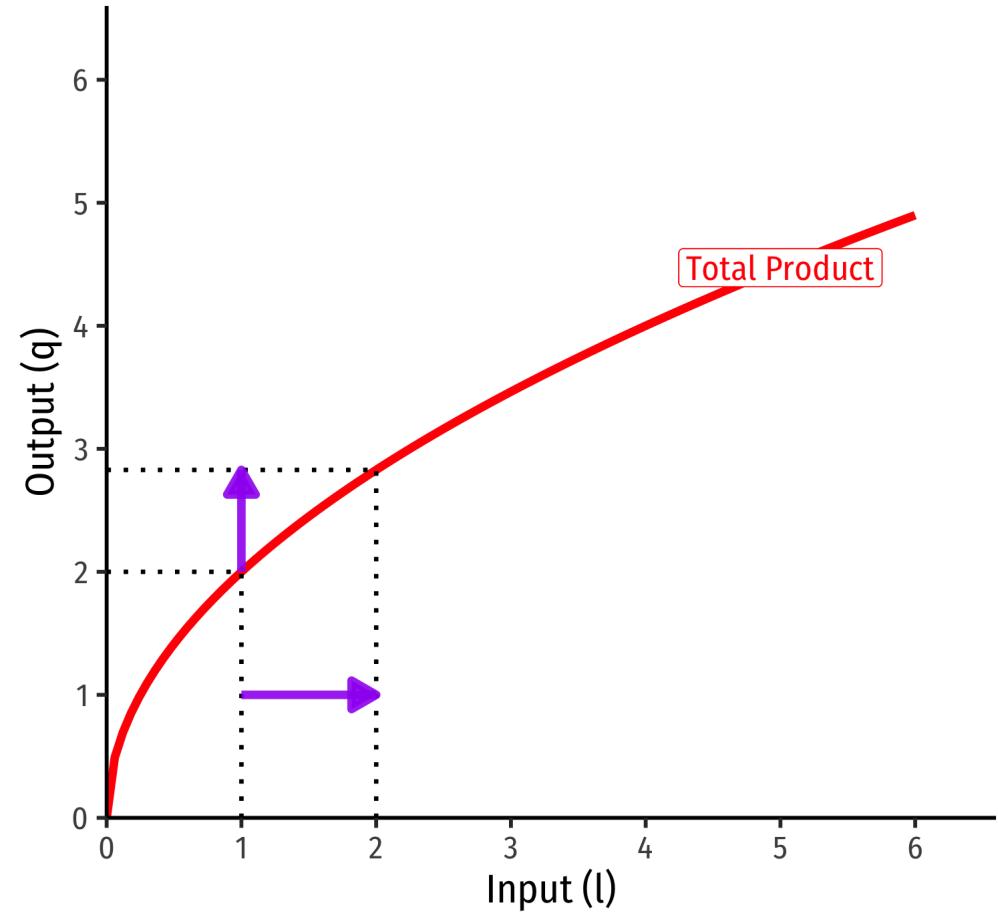


# Short-Run Production Concepts

# Marginal Products

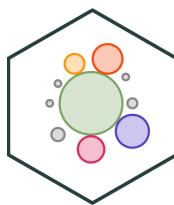


- The **marginal product** of an input is the *additional output produced by one more unit of that input (holding all other inputs constant)*
- Like marginal utility
- Similar to marginal utilities, I will give you the marginal product equations



$$\text{Technology: } q(l, \bar{k}) = 2\sqrt{l}$$

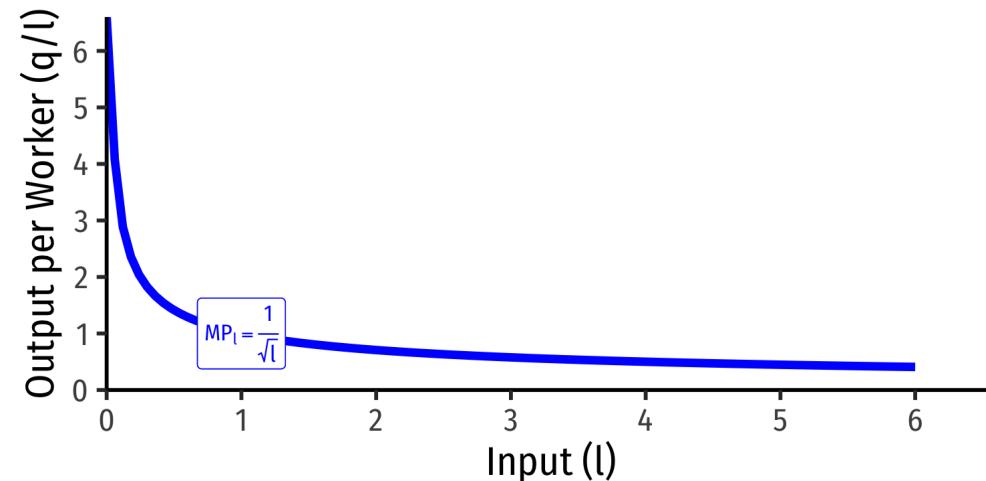
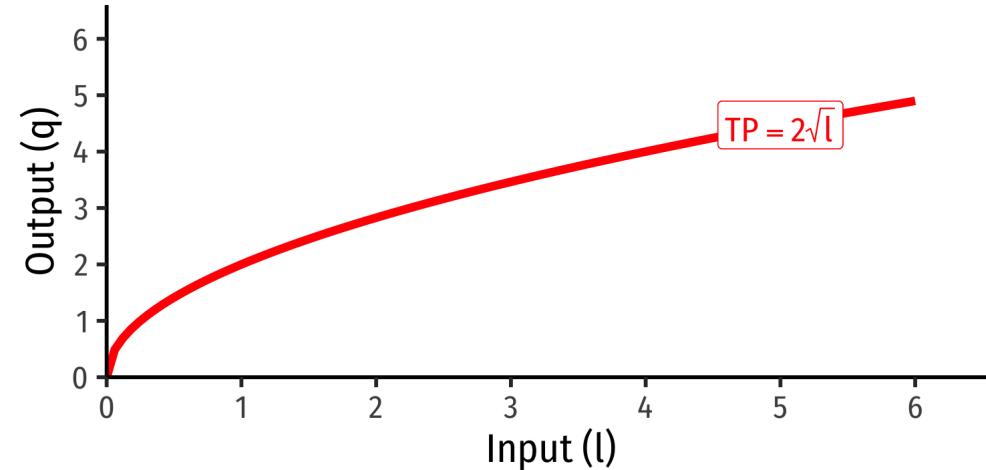
# Marginal Product of Labor



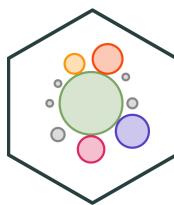
- Marginal product of labor ( $MP_l$ ):  
additional output produced by adding  
one more unit of labor (holding  $k$   
constant)

$$MP_l = \frac{\Delta q}{\Delta l}$$

- $MP_l$  is slope of  $TP$  at each value of  $l$ !
  - Note: via calculus:  $\frac{\partial q}{\partial l}$



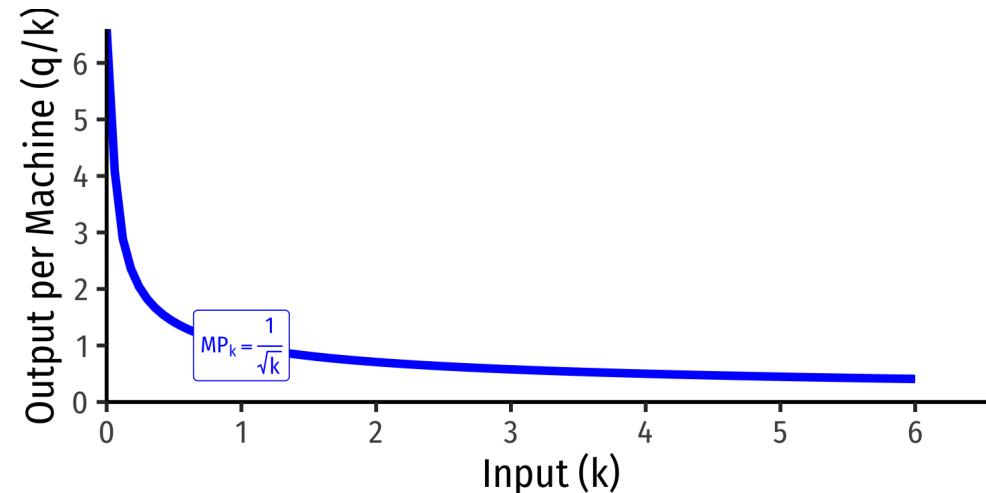
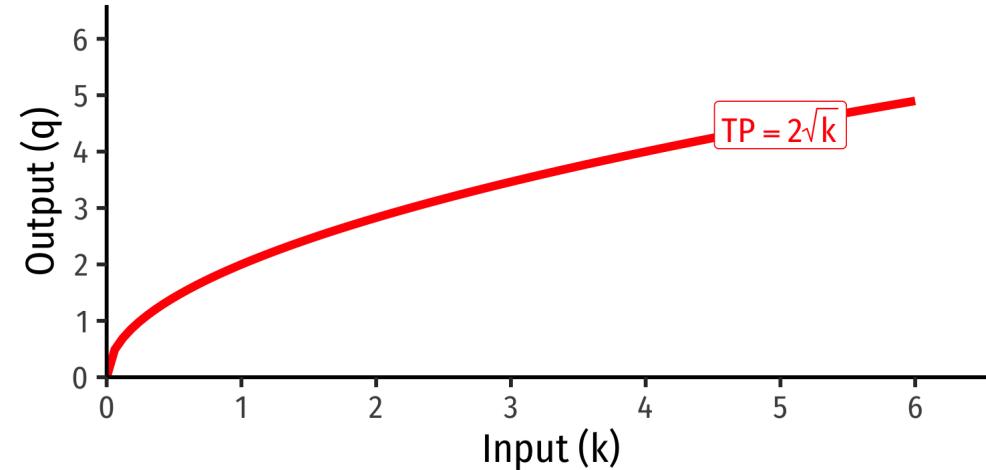
# Marginal Product of Capital



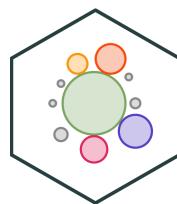
- **Marginal product of capital ( $MP_k$ ):** additional output produced by adding one more unit of capital (holding  $l$  constant)

$$MP_k = \frac{\Delta q}{\Delta k}$$

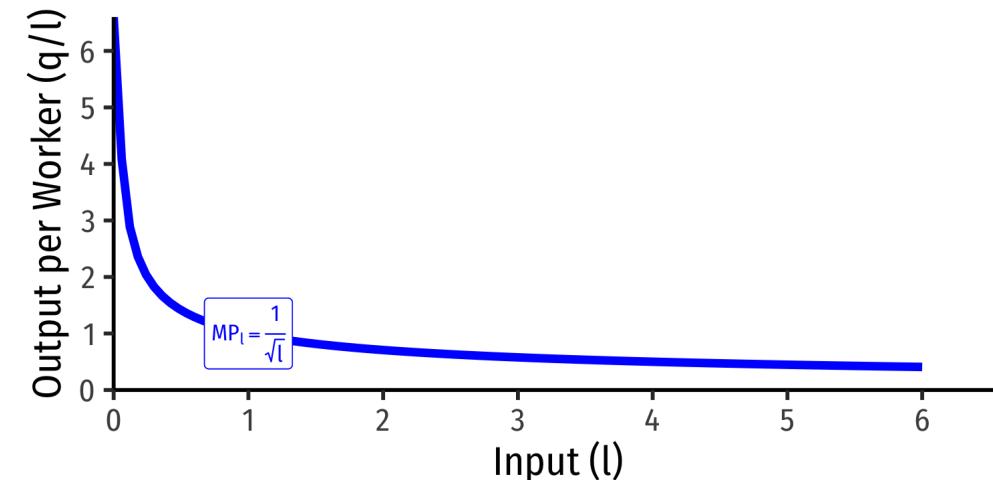
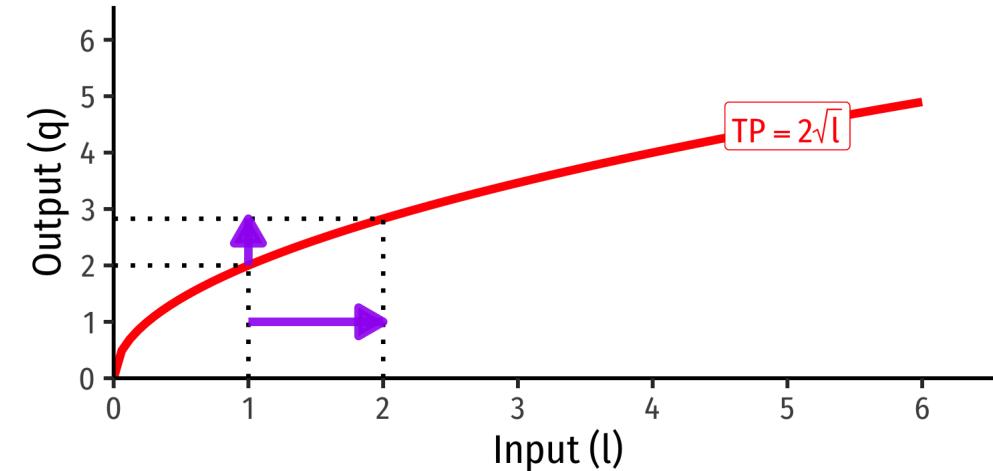
- $MP_k$  is slope of  $TP$  at each value of  $k$ !
  - Note: via calculus:  $\frac{\partial q}{\partial k}$
- Note we don't consider capital in the short run!



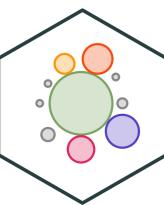
# Diminishing Returns



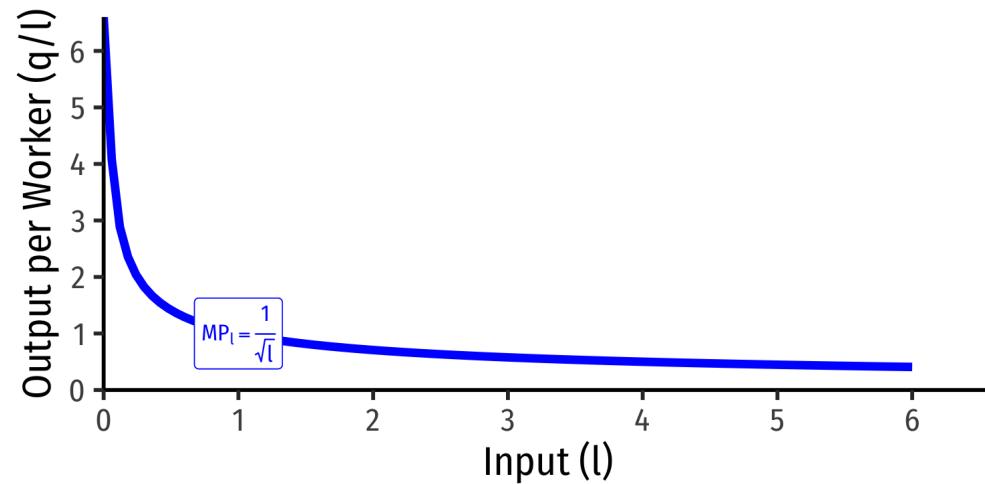
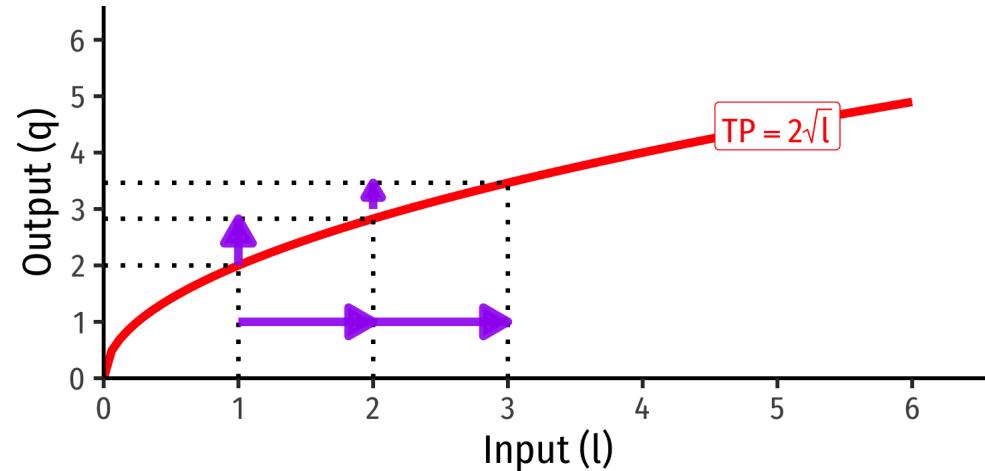
- **Law of Diminishing Returns:** adding more of one factor of production **holding all others constant** will result in successively lower increases in output
- In order to increase output, firm will need to increase *all* factors!



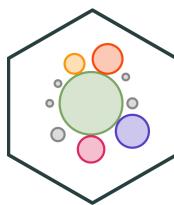
# Diminishing Returns



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# Average Product of Labor (and Capital)

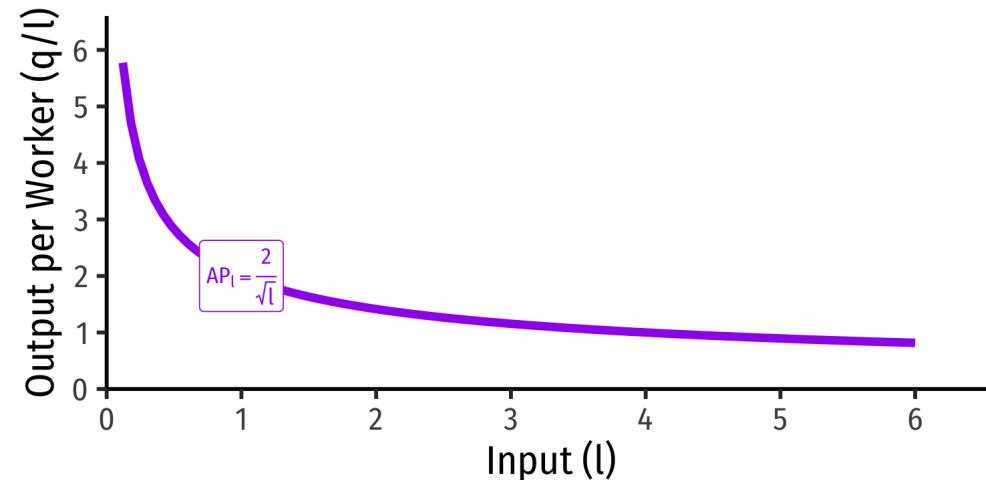
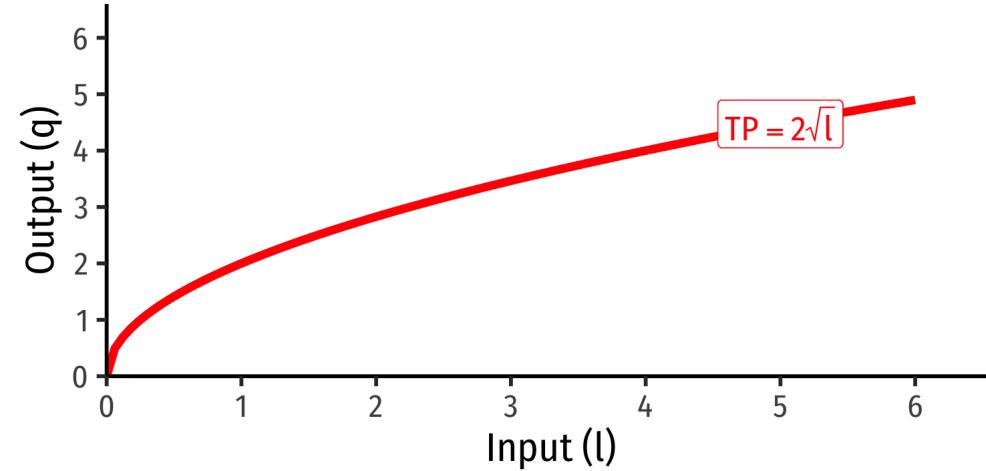


- **Average product of labor ( $AP_l$ )**: total output per worker

$$AP_l = \frac{q}{l}$$

- A measure of *labor productivity*
- **Average product of capital ( $AP_k$ )**: total output per unit of capital

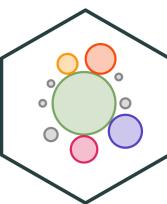
$$AP_k = \frac{q}{k}$$





# The Firm's Problem: Long Run

# The Long Run



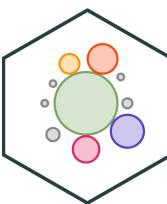
- In the long run, *all* factors of production are **variable**

$$q = f(k, l)$$

- Can build more factories, open more storefronts, rent more space, invest in machines, etc.
- So the firm can choose both *l and k*



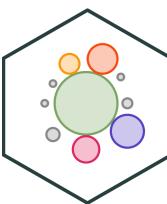
# Production Costs are Opportunity Costs



- Remember, **economic costs** are broader than the common conception of “cost”
  - **Accounting cost:** monetary cost
  - **Economic cost:** value of next best alternative use of resources given up (i.e. **opportunity cost**)



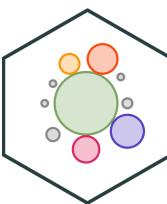
# Production Costs are Opportunity Costs



- This leads to the difference between:
  - **Accounting profit:** revenues minus accounting costs
  - **Economic profit:** revenues minus accounting + opportunity costs
- A really difficult concept to think about!



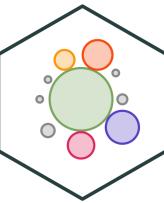
# Production Costs are Opportunity Costs



- Another helpful perspective:
  - **Accounting cost:** what you **historically** paid for a resource
  - **Economic cost:** what you can **currently** get in the market for a selling a resource (it's value in *alternative uses*)



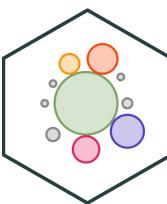
# A Reminder: It's Demand all the Way Down!



- **Supply** is actually **Demand** in disguise!
- An **(opportunity) cost** to buy (scarce) inputs for production because **other people demand** those same inputs to consume or produce **other valuable things!**
  - Price necessary to **pull them out of other valuable productive uses** in the economy!



# Production Costs are Opportunity Costs



- Because resources are scarce, and have rivalrous uses, **how do we know we are using resources efficiently??**
- In functioning markets, **the market price measures the opportunity cost of using a resource for an alternative use**
- Firms not only pay for direct use of a resource, but also indirectly compensate society for “*pulling the resource out*” of alternate uses in the economy!



# Production Costs are Opportunity Costs



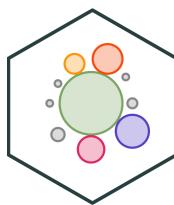
- Every choice incurs an opportunity cost

## Examples:

- If you start a business, you may give up your salary at your current job
- If you invest in a factory, you give up other investment opportunities
- If you use an office building you own, you cannot rent it to other people
- If you hire a skilled worker, you must pay them a high enough salary to deter them from working for other firms



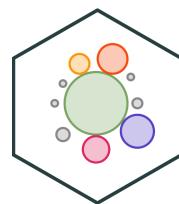
# Opportunity Costs vs. Sunk Costs



- Opportunity cost is a *forward-looking* concept
- Choices made in the *past* with *non-recoverable* costs are called **sunk costs**
- Sunk costs *should not* enter into future decisions
- Many people have difficulty letting go of unchangeable past decisions: **sunk cost fallacy**



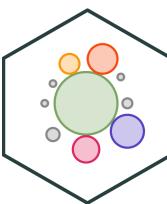
# Common Sunk Costs in Business



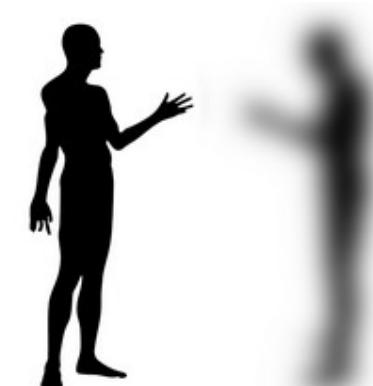
- Licensing fees, long-term lease contracts
- Specific capital (with no alternative use): uniforms, menus, signs
- Research & Development spending
- Advertising spending



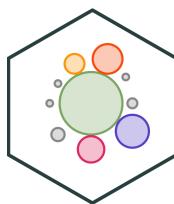
# The Accounting vs. Economic Point of View I



- Helpful to consider two points of view:
  1. **“Accounting point of view”**: are you taking in more cash than you are spending?
  2. **“Economic point of view”**: is your product you making the *best social* use of your resources
    - i.e. are there higher-valued uses of your resources you are keeping them out of?



# The Accounting vs. Economic Point of View II



- **Implications for society:** are consumers *best off* with you using scarce resources (with alternative uses!) to produce your current product?
- Remember: **this is an *economics* course, not a *business* course!**
  - Economists are pro-market, *not* pro-business!
  - What might be good/bad for **one** business might have bad/good *consequences* for society!





# Costs in the Short Run

# Costs in the Short Run



- **Total cost function,  $C(q)$**  relates output  $q$  to the total cost of production  $C^t$

$$C(q) = f + VC(q)$$

- Two kinds of short run costs:

**1. Fixed costs,  $f$**  are costs that do not vary with output

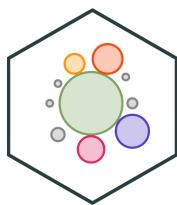
- Only true in the short run! (Consider this the cost of maintaining your capital)

**2. Variable costs,  $VC(q)$**  are costs that vary with output (notice the variable in them!)

- Typically, the more production of  $q$ , the higher the cost
- e.g. firm is hiring *additional* labor

<sup>t</sup> Assuming that (i) firms are always choosing input combinations that minimize total cost and (ii) input prices are constant. See more in [today's appendix](#).

# Fixed vs. Variable costs: Examples

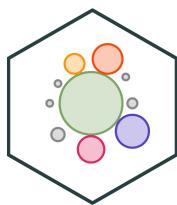


## Example: Airlines

**Fixed costs:** the aircraft, regulatory approval

**Variable costs:** providing one more flight

# Fixed vs. Variable costs: Examples

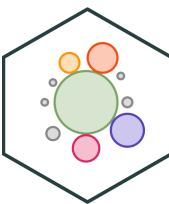


**Example:** Car Factory

**Fixed costs:** the factory, machines in the factory

**Variable costs:** producing one more car

# Fixed vs. Variable costs: Examples

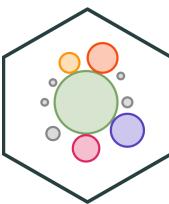


## Example: Starbucks

**Fixed costs:** the retail space, espresso machines

**Variable costs:** selling one more cup of coffee

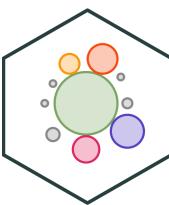
# Fixed vs. Sunk costs



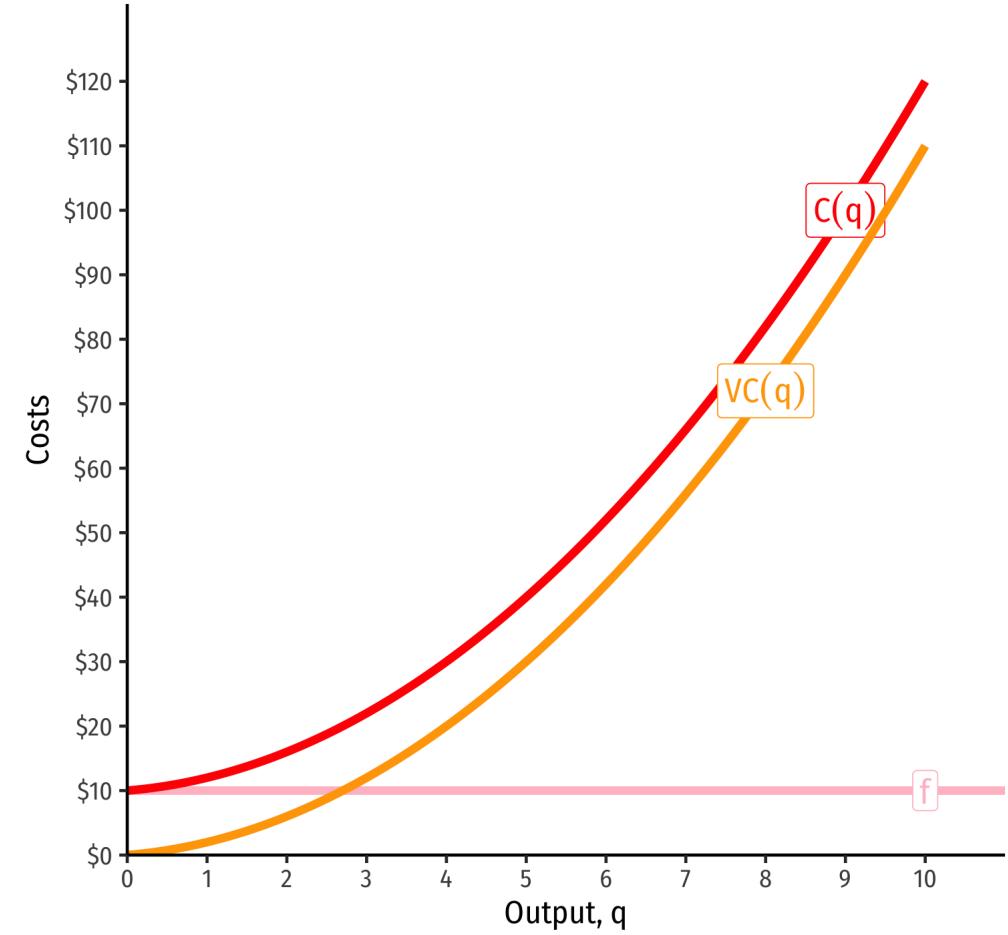
- Diff. between **fixed** vs. **sunk** costs?
- **Sunk costs** are a *type* of **fixed cost** that are *not* avoidable or recoverable
- Many **fixed costs** can be avoided or changed in the long run
- Common **fixed**, but *not sunk*, costs:
  - rent for office space, durable equipment, operating permits (that are renewed)
- When deciding to *stay* in business, **fixed costs** matter, **sunk costs** do not!



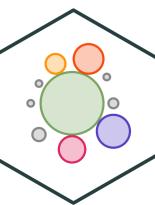
# Cost Functions: Example, Visualized



$q$	$f$	$VC(q)$	$C(q)$
0	10	0	10
1	10	2	12
2	10	6	16
3	10	12	22
4	10	20	30
5	10	30	40
6	10	42	52
7	10	56	66
8	10	72	82
9	10	90	100
10	10	110	120



# Average Costs



- **Average Fixed Cost:** fixed cost per unit of output:

$$AFC(q) = \frac{f}{q}$$

- **Average Variable Cost:** variable cost per unit of output:

$$AVC(q) = \frac{VC(q)}{q}$$

- **Average (Total) Cost:** (total) cost per unit of output:

$$AC(q) = \frac{C(q)}{q}$$

# Marginal Cost

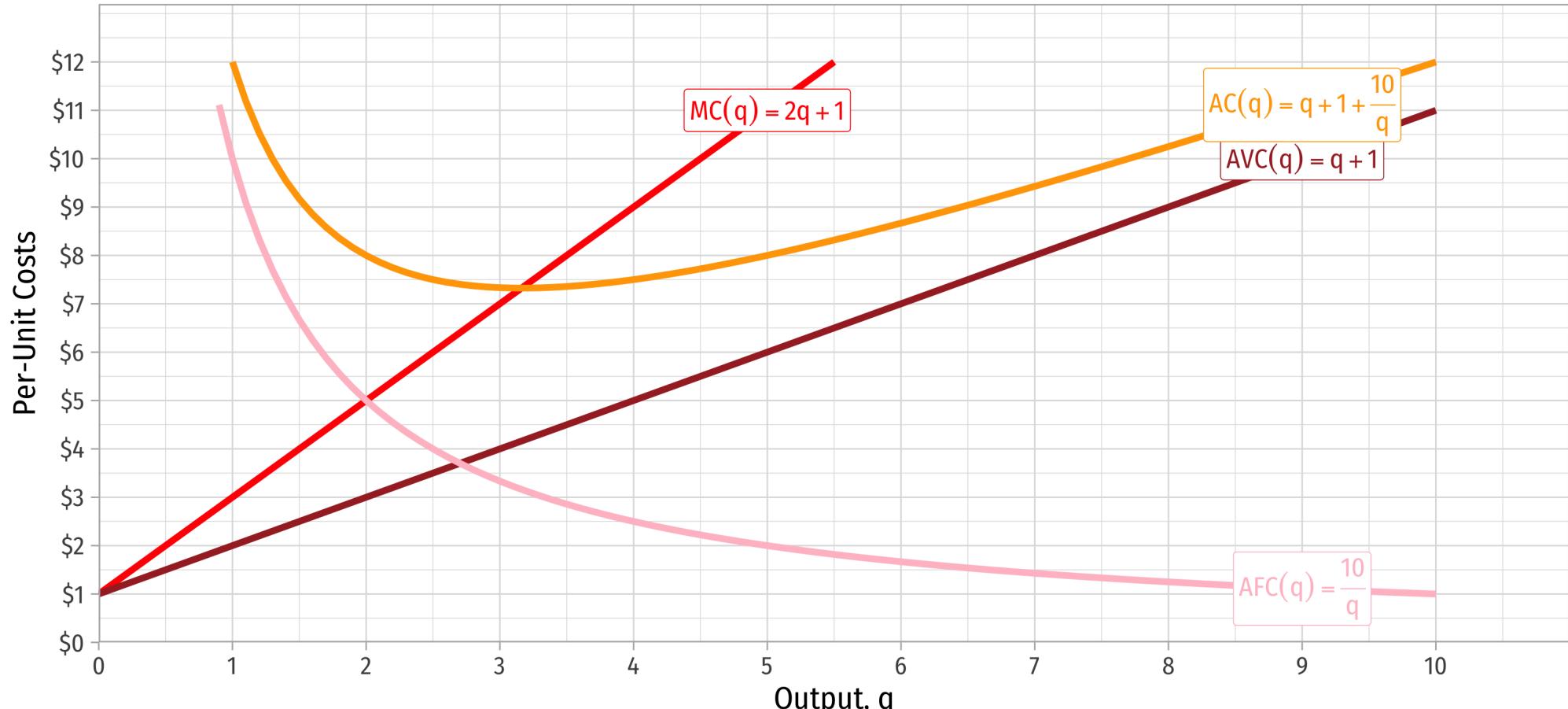
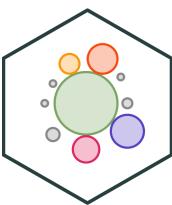


- **Marginal Cost** is the change in total cost for each additional unit of output produced:

$$MC(q) = \frac{\Delta C(q)}{\Delta q}$$

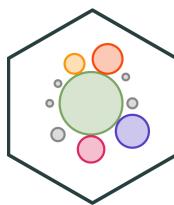
- Calculus: first derivative of the cost function
- **Marginal cost is the *primary* cost that matters in making decisions**
  - All other costs are driven by marginal costs
  - This is the main cost that firms can “see”

# Average and Marginal Costs: Visualized

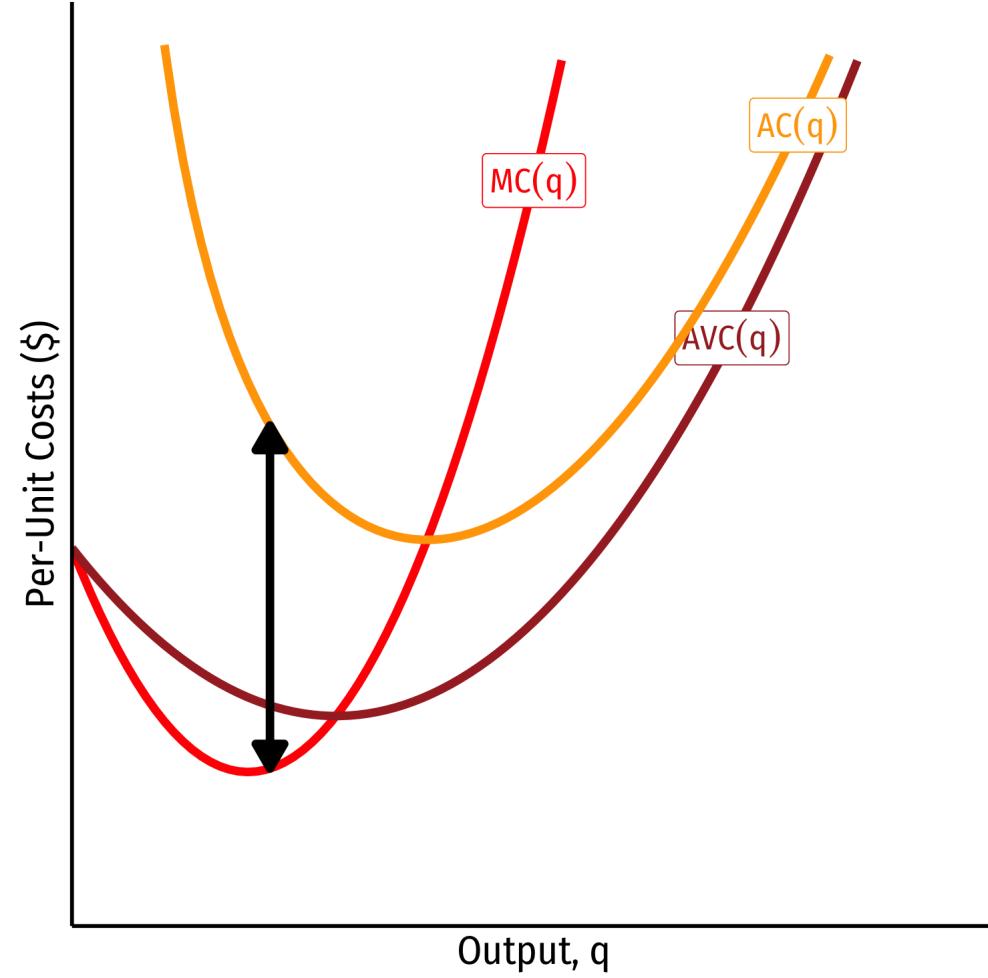


$$C(q) = q^2 + q + 10$$

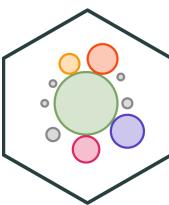
# Relationship Between Marginal and Average



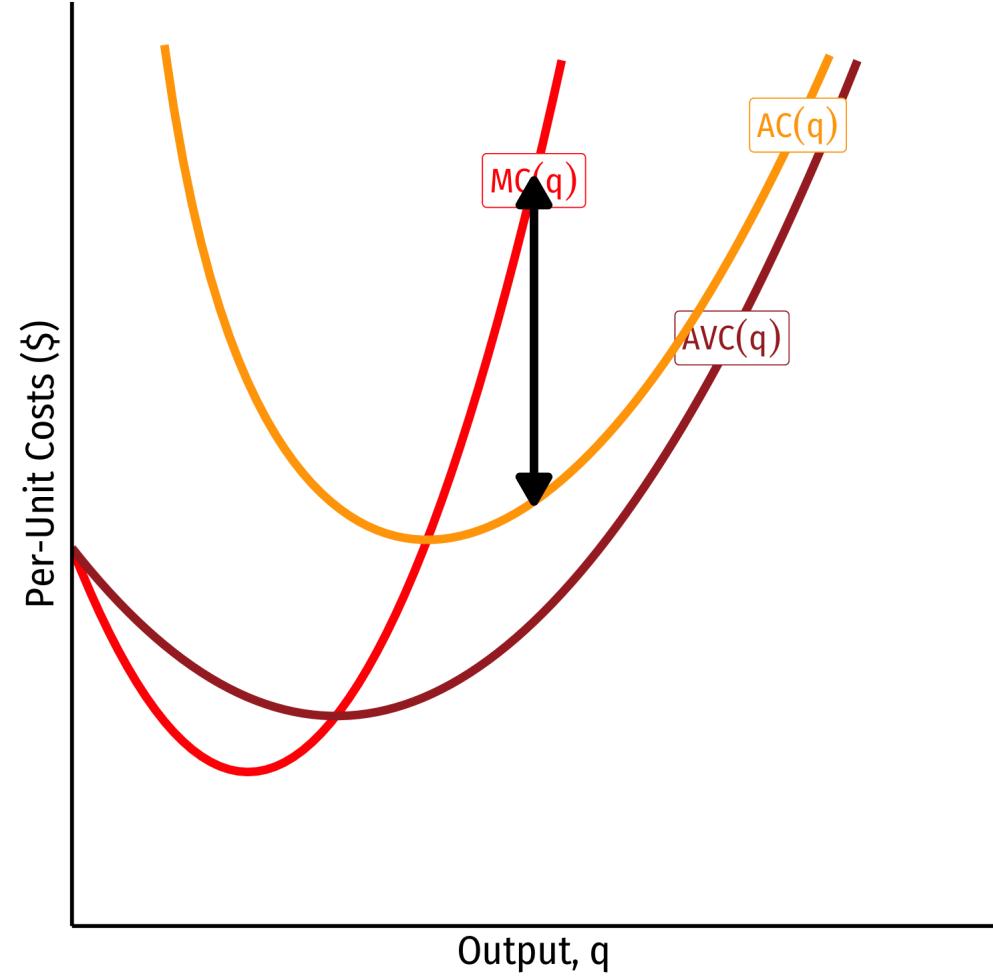
- Mathematical relationship between a marginal & an average value
- If **marginal** < **average**, then **average** ↓



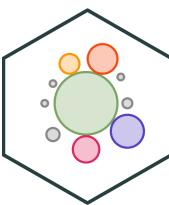
# Relationship Between Marginal and Average



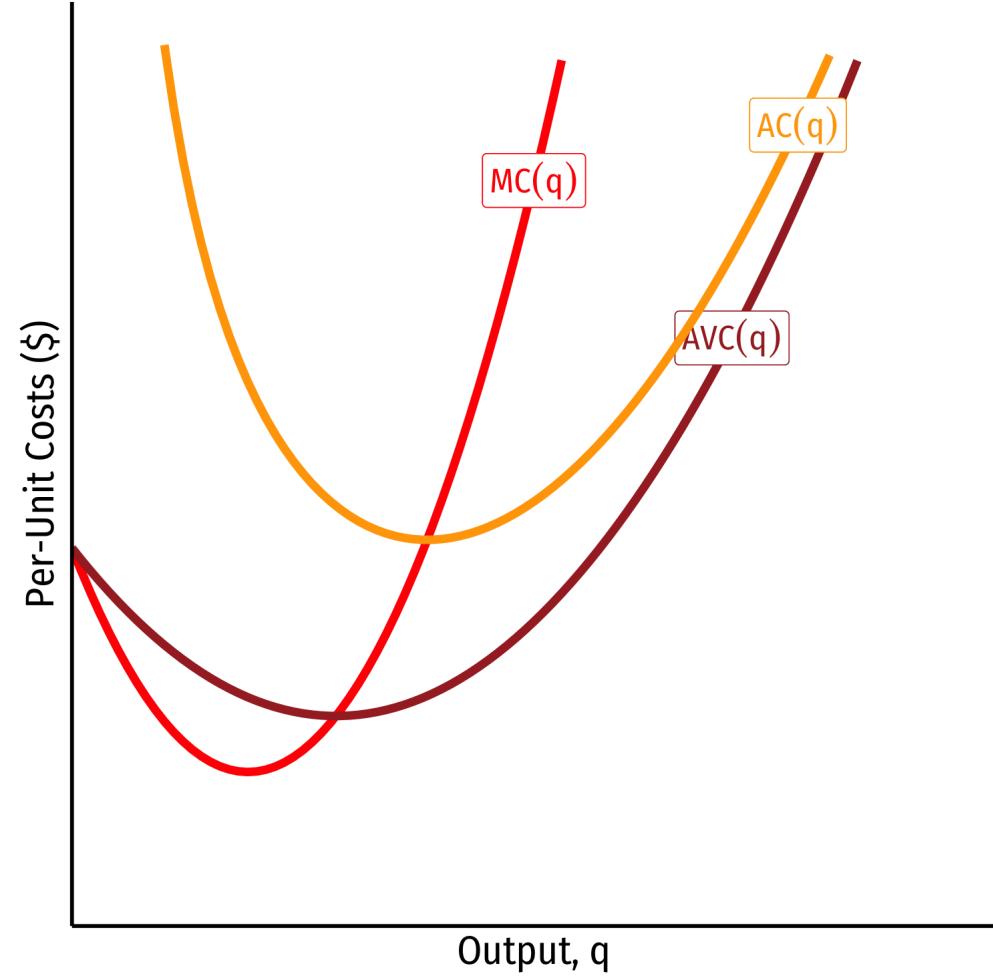
- Mathematical relationship between a marginal & an average value
- If marginal < average, then average ↓
- If marginal > average, then average ↑



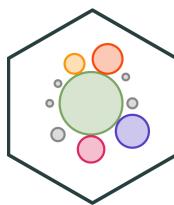
# Relationship Between Marginal and Average



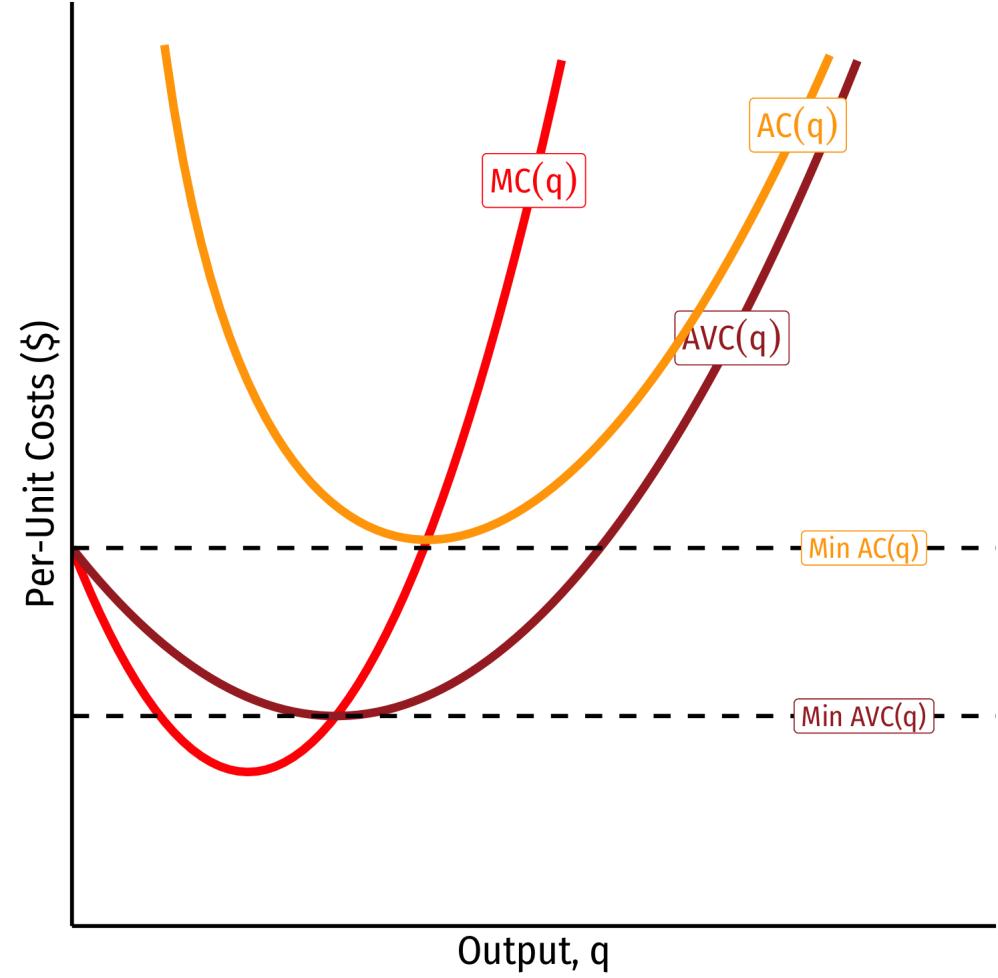
- Mathematical relationship between a marginal & an average value
- If marginal < average, then average ↓
- If marginal > average, then average ↑
- When marginal = average, average is **maximized/minimized**



# Relationship Between Marginal and Average



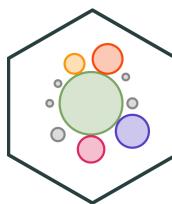
- Mathematical relationship between a marginal & an average value
- If marginal < average, then average ↓
- If marginal > average, then average ↑
- When marginal = average, average is **maximized/minimized**
  - When  $MC(q)=AC(q)$ ,  $AC(q)$  is at a *minimum* (break-even price)
  - When  $MC(q)=AVC(q)$ ,  $AVC(q)$  is at a *minimum* (shut-down price)





# Costs in the Long Run

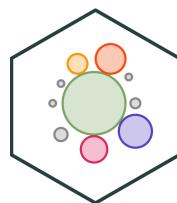
# Costs in the Long Run



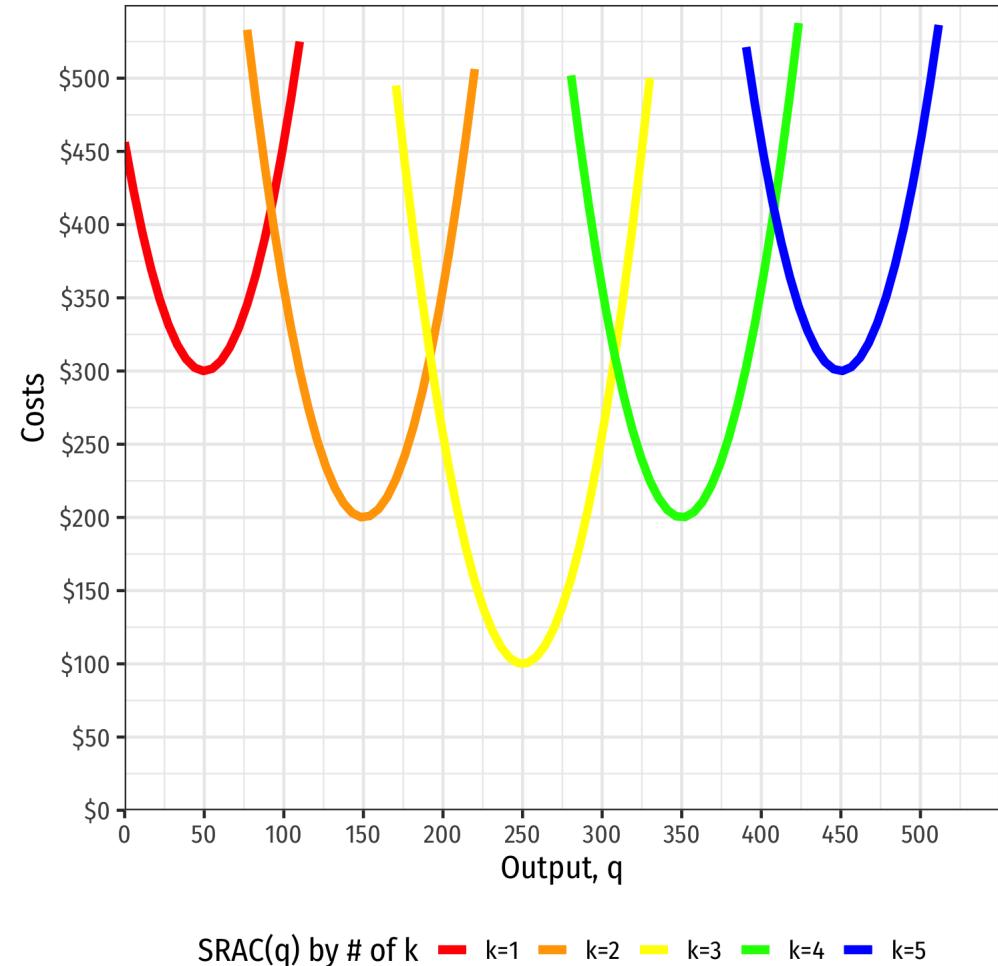
- **Long run:** firm can change all factors of production & vary scale of production
- **Long run average cost,  $LRAC(q)$ :** cost per unit of output when the firm can change *both l and k* to make more  $q$
- **Long run marginal cost,  $LRMC(q)$ :** change in long run total cost as the firm produce an additional unit of  $q$  (by changing *both l and/or k*)



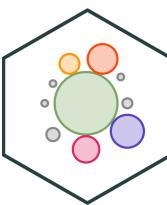
# Average Cost in the Long Run



- **Long run:** firm can choose  $k$  (factories, locations, etc)
- Separate short run average cost (SRAC) curves for each amount of  $k$  potentially chosen

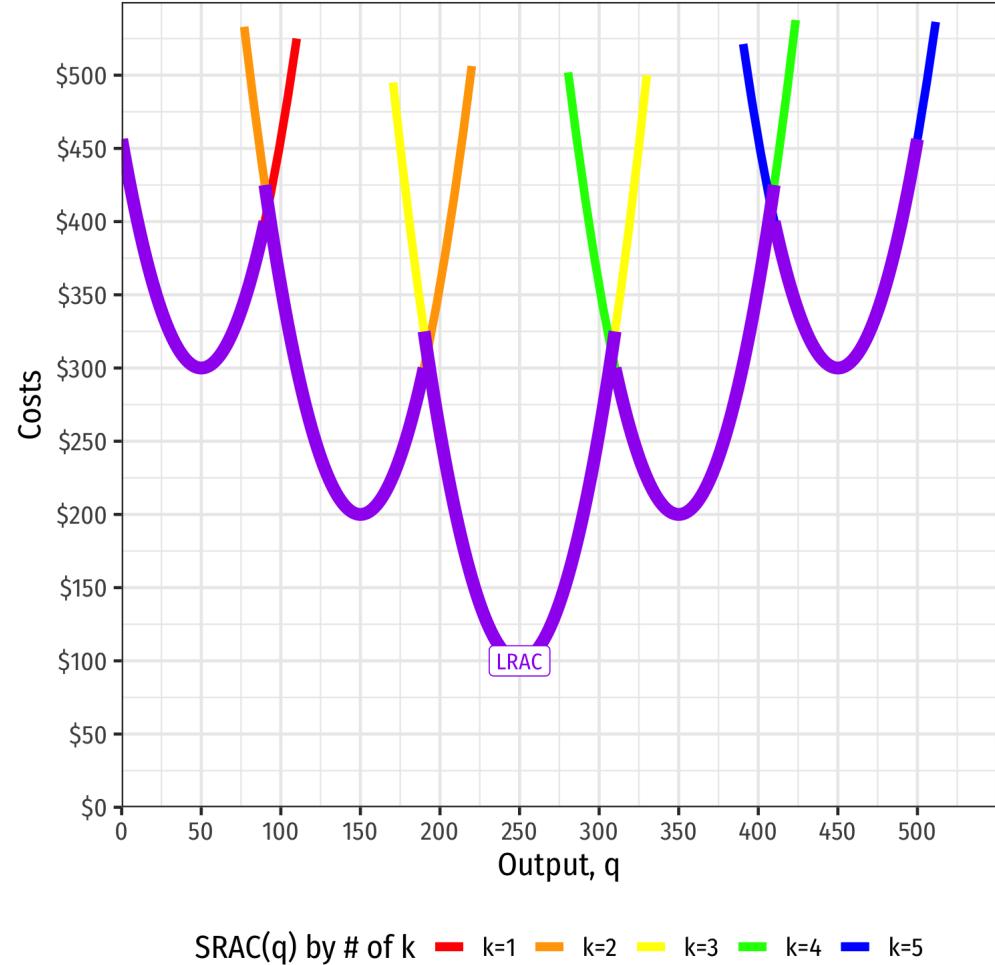


# Average Cost in the Long Run

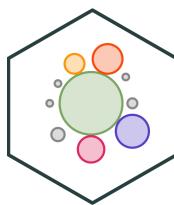


- **Long run:** firm can choose  $k$  (factories, locations, etc)
- Separate short run average cost (SRAC) curves for each amount of  $k$  potentially chosen
- **Long run average cost (LRAC)** curve “envelopes” the lowest (optimal) regions of all the SRAC curves!

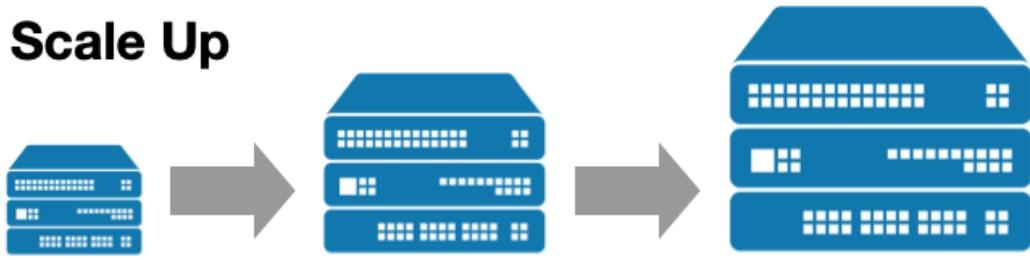
“Subject to producing the optimal amount of output, choose  $l$  and  $k$  to minimize cost”



# Long Run Costs & Scale Economies I

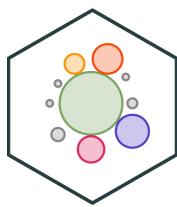


## Scale Up

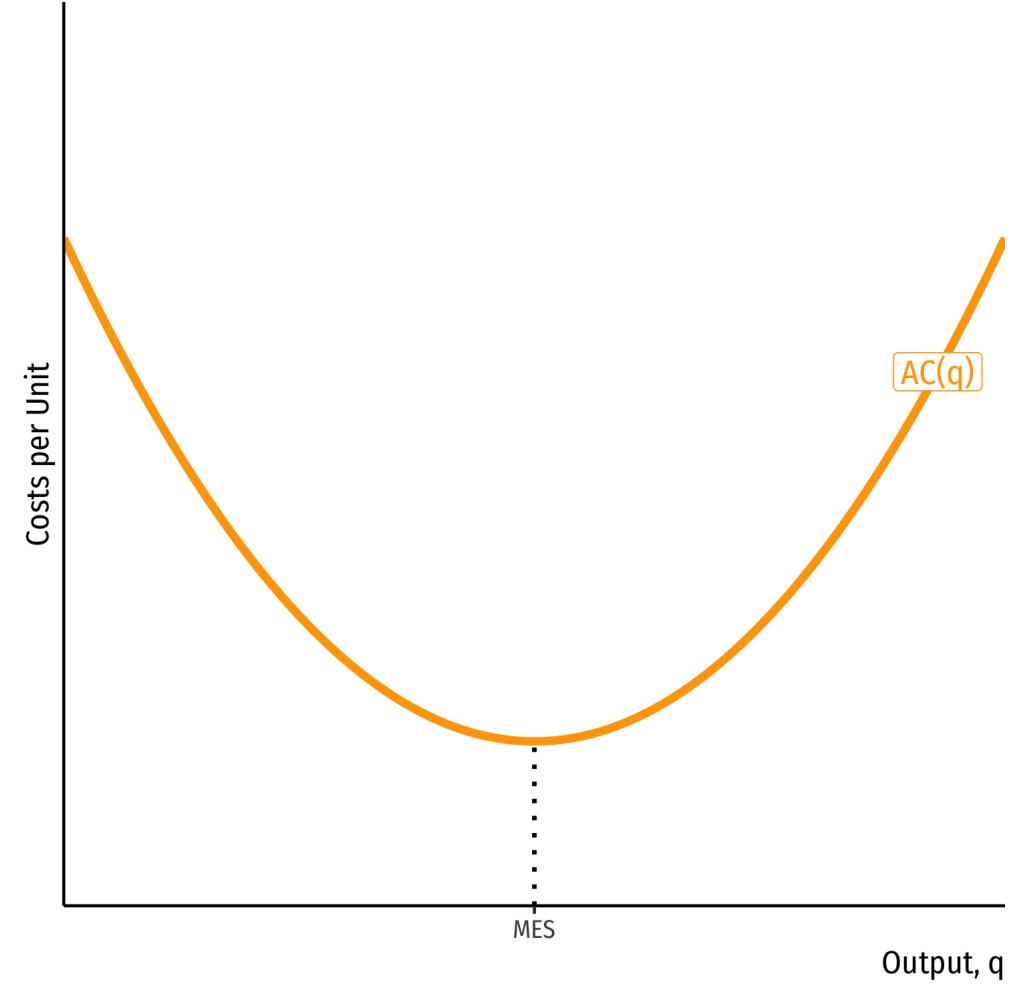


- Further important properties about costs based on **scale economies** of production: change in **average costs** when output is increased (scaled)
- **Economies of scale:** average costs **fall** with more output
  - High fixed costs  $AFC > AVC(q)$  low variable costs
- **Diseconomies of scale:** average costs **rise** with more output
  - Low fixed costs  $AFC < AVC(q)$  high variable costs
- **Constant economies of scale:** average costs **don't change** with more output
  - Firm at minimum average cost (optimal plant size), called **minimum efficient scale (MES)**

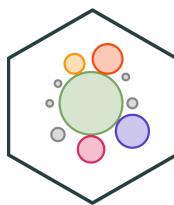
# Long Run Costs & Scale Economies II



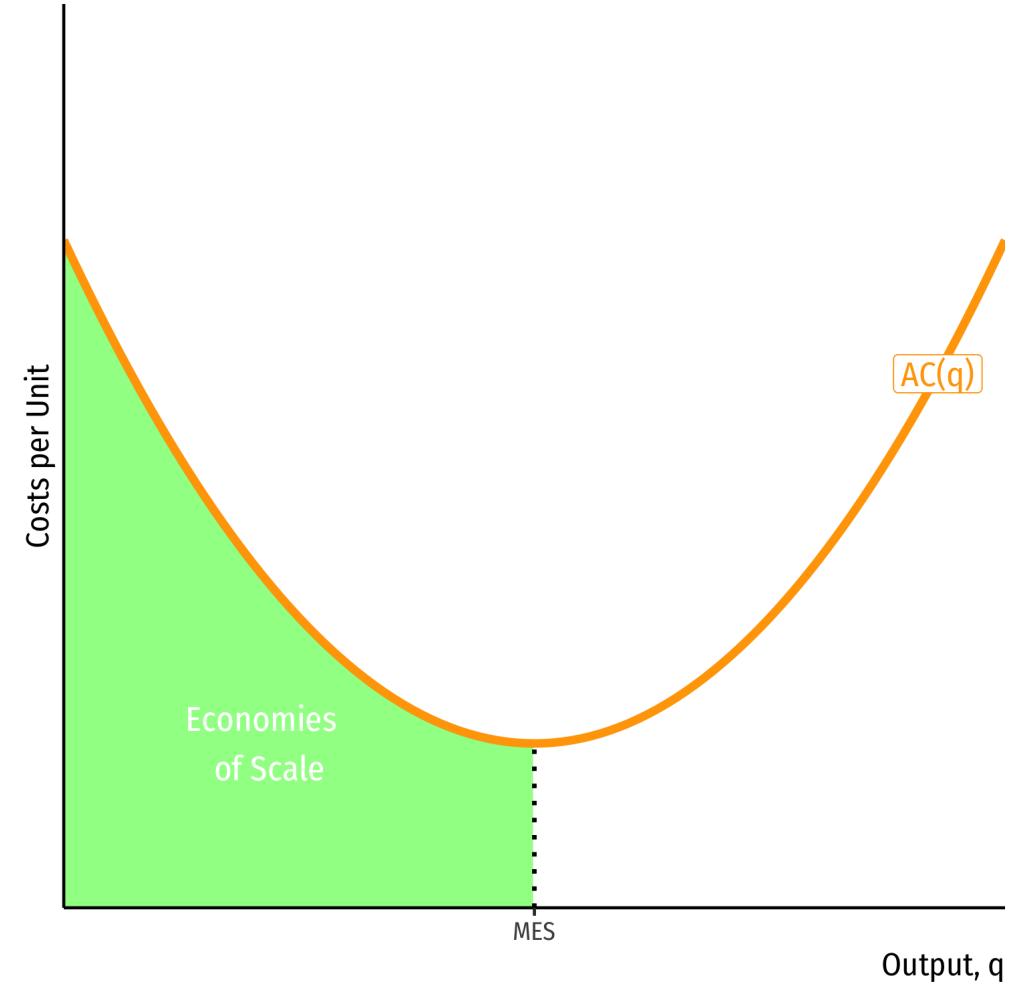
- **Minimum Efficient Scale:**  $q$  with the lowest  $AC(q)$ 
  - “optimal firm size”



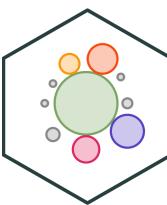
# Long Run Costs & Scale Economies II



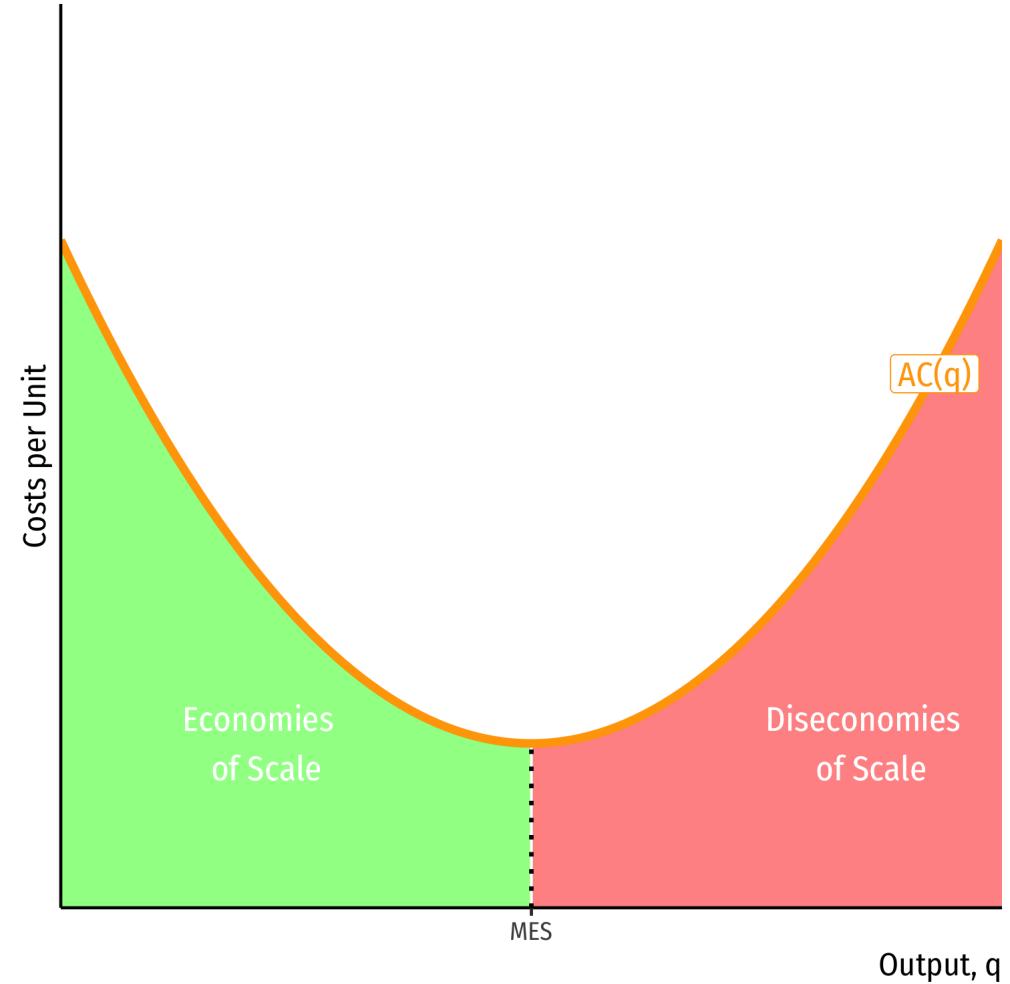
- **Minimum Efficient Scale:**  $q$  with the lowest  $AC(q)$ 
  - “optimal firm size”
- **Economies of Scale:**  $\uparrow q, \downarrow AC(q)$



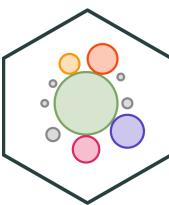
# Long Run Costs & Scale Economies II



- **Minimum Efficient Scale:**  $q$  with the lowest  $AC(q)$ 
  - “optimal firm size”
- **Economies of Scale:**  $\uparrow q, \downarrow AC(q)$
- **Diseconomies of Scale:**  $\uparrow q, \uparrow AC(q)$



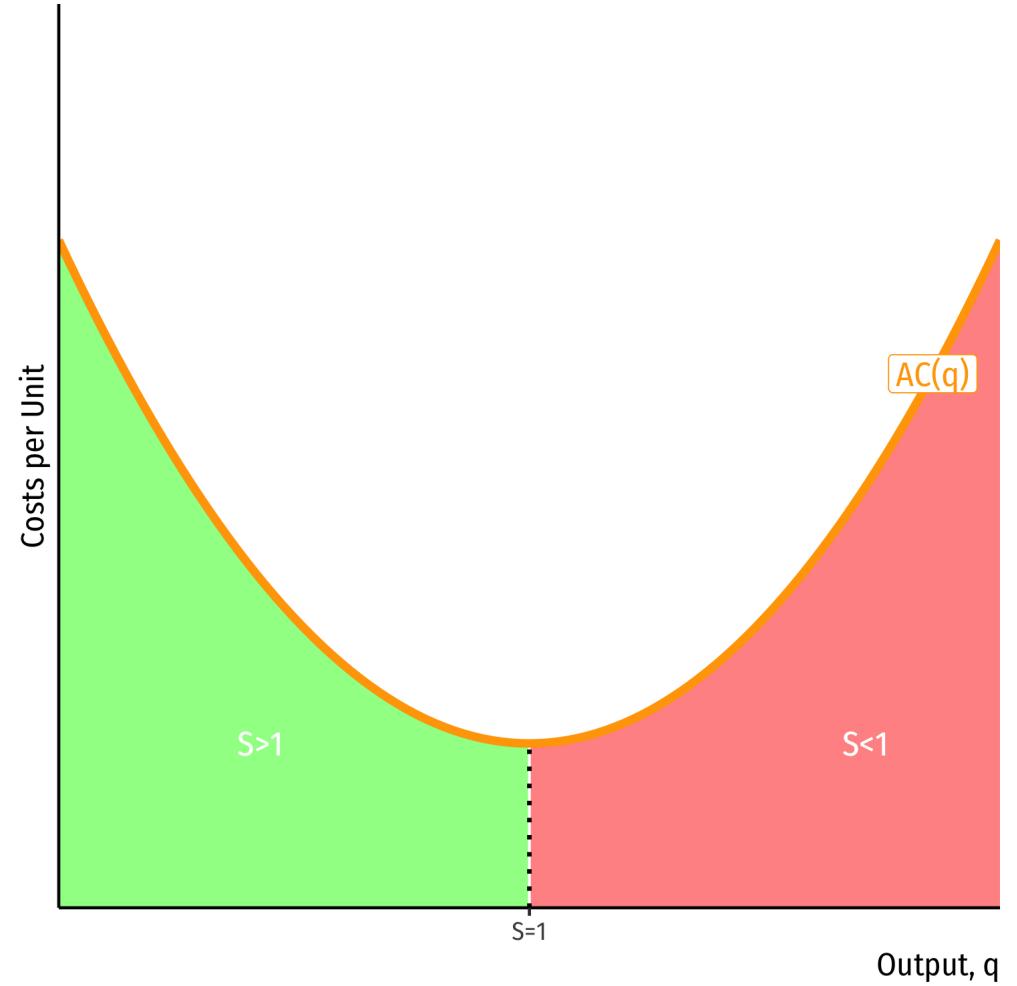
# Long Run Costs & Scale Economies III



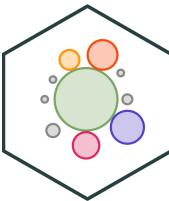
- Can measure economies of scale ( $S$ ):

$$S(q) = \frac{AC(q)}{MC(q)}$$

- $S > 1$ : economies of scale at  $q$
- $S < 1$ : diseconomies of scale at  $q$
- $S = 1$ : minimum efficient scale at  $q$



# Economies of Scope



- We often assume **single-product plants/firms**, but in reality most firms/plants are **multi-product**
- **Economies of Scope**: cost of producing multiple products (e.g.  $q_1$  and  $q_2$ ) in a single plant exceeds costs of producing a single product in each plant

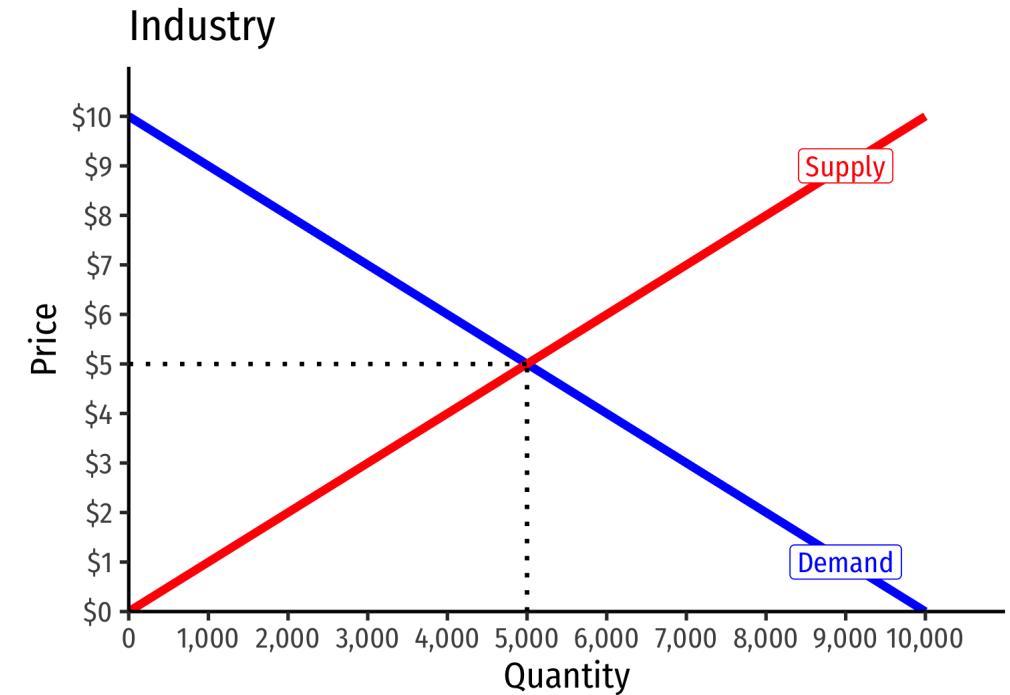
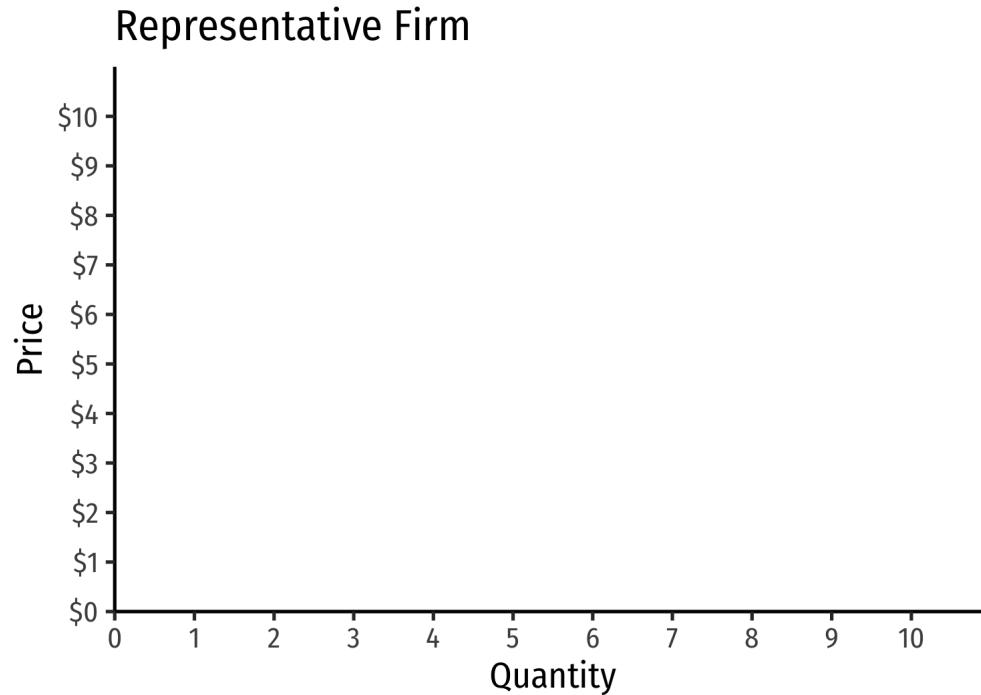
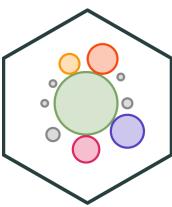
$$C(q_1, q_2) < C(q_1, 0) + C(0, q_2)$$



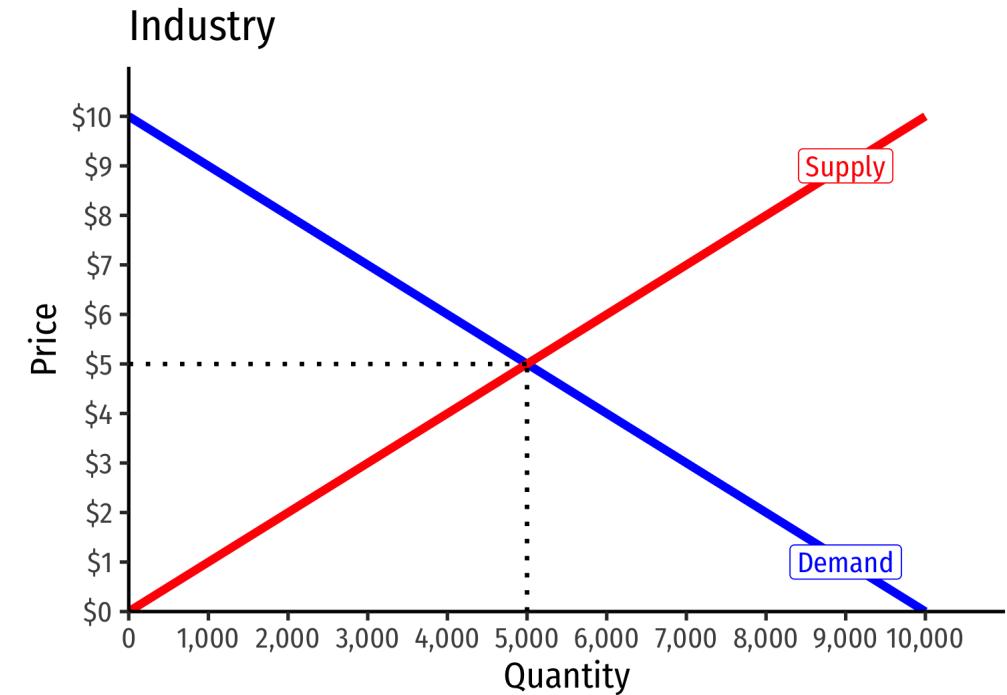
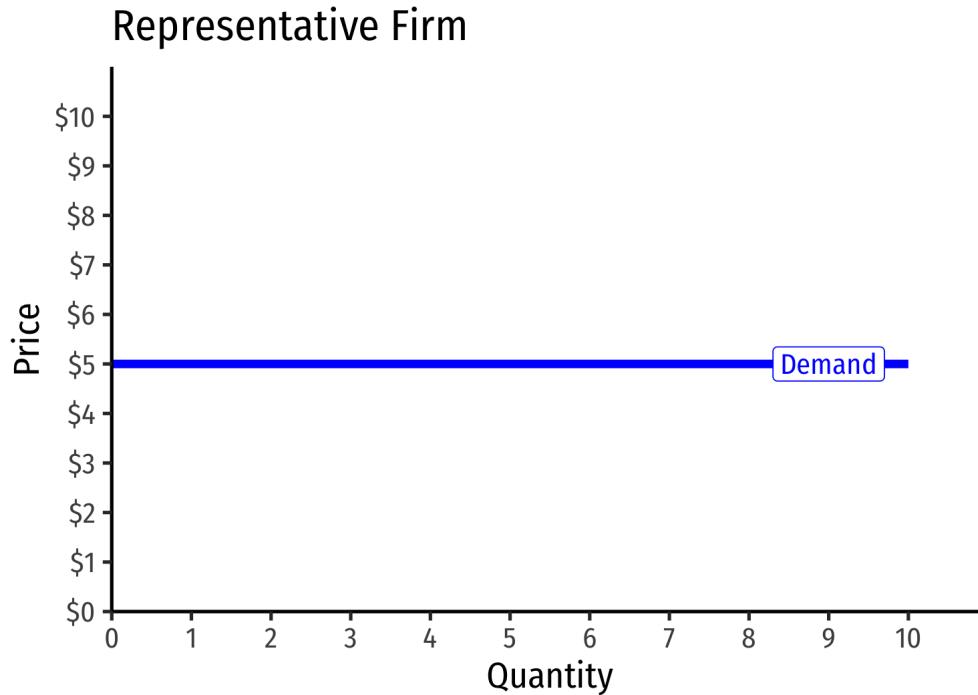
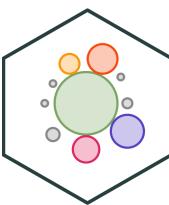


# Revenues

# Revenues for Firms in *Competitive* Industries I

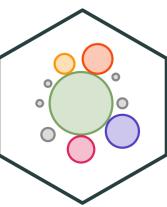


# Revenues for Firms in *Competitive* Industries I

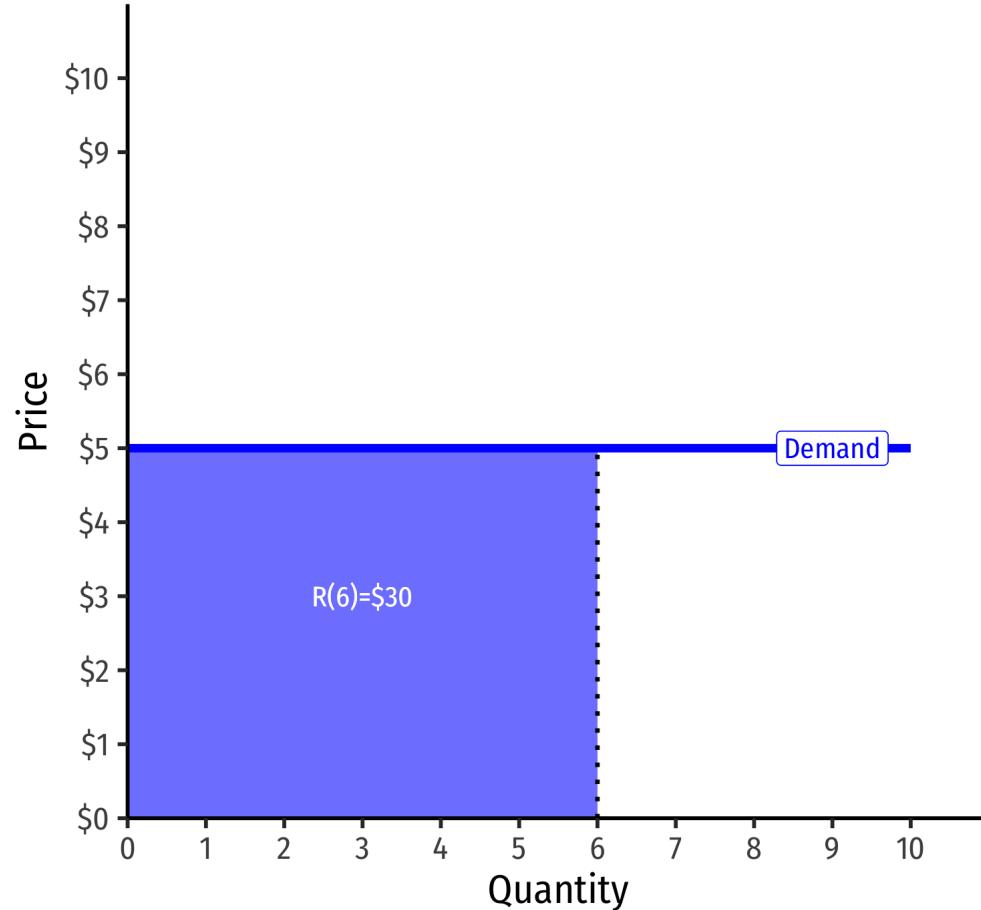


- Demand for a firm's product is **perfectly elastic** at the market price
- Where did the **supply curve** come from? You'll know today

# Revenues for Firms in *Competitive* Industries II

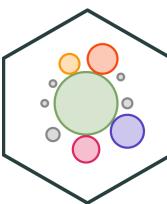


Representative Firm



- **Total Revenue**  $R(q) = pq$

# Average and Marginal Revenues



- **Average Revenue:** revenue per unit of output

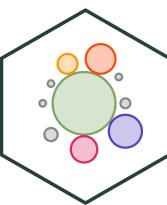
$$AR(q) = \frac{R}{q}$$

- $AR(q)$  is **by definition** equal to the price! (Why?)
- **Marginal Revenue:** change in revenues for each additional unit of output sold:

$$MR(q) = \frac{\Delta R(q)}{\Delta q}$$

- Calculus: first derivative of the revenues function
- **For a competitive firm (only),  $MR(q) = p$ , i.e. the price!**

# Average and Marginal Revenues: Example



**Example:** A firm sells bushels of wheat in a very competitive market. The current market price is \$10/bushel.

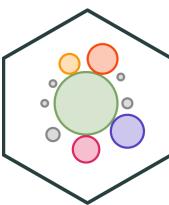
For the 1<sup>st</sup> bushel sold:

- What is the total revenue?
- What is the average revenue?

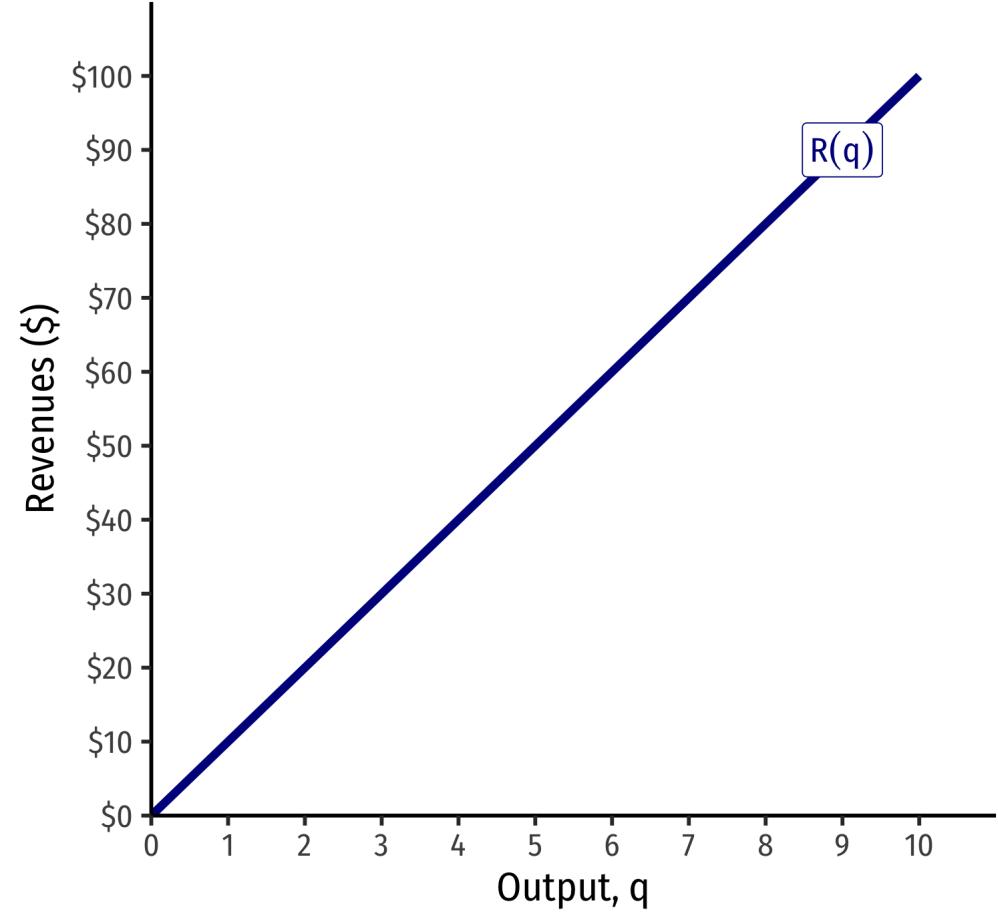
For the 2<sup>nd</sup> bushel sold:

- What is the total revenue?
- What is the average revenue?
- What is the marginal revenue?

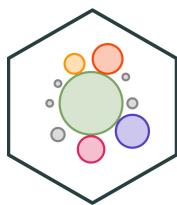
# Total Revenue, Example: Visualized



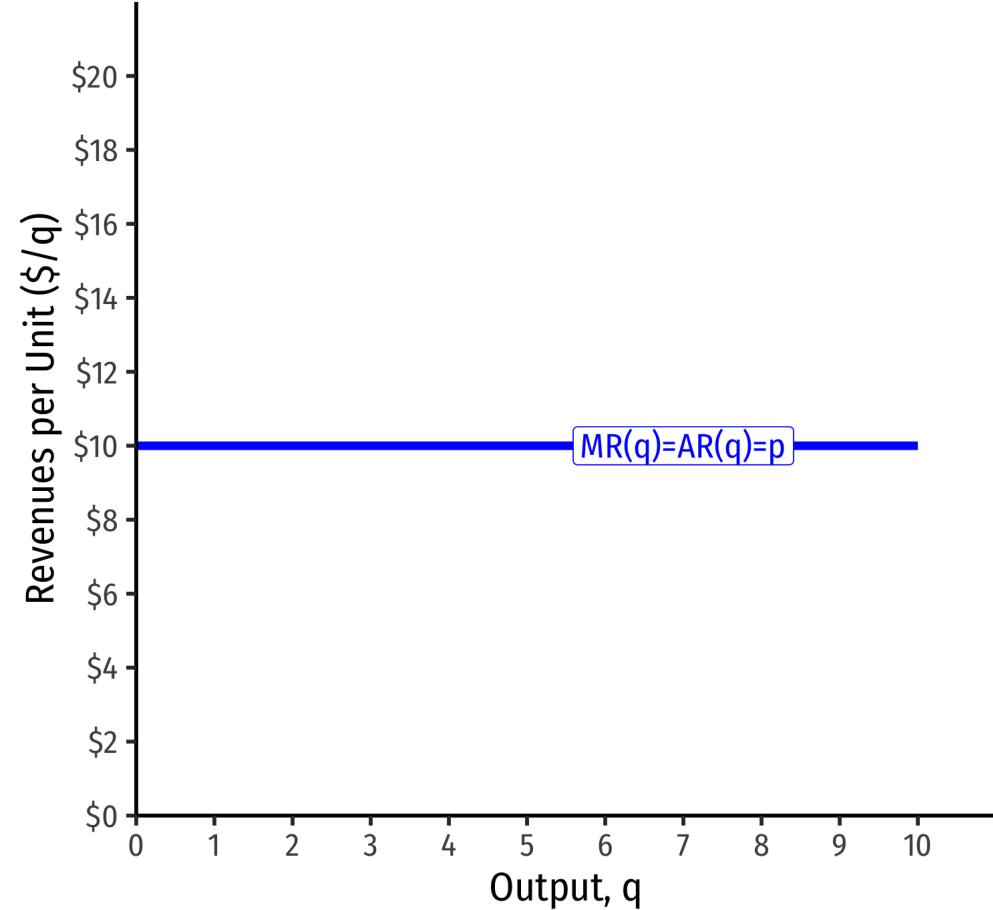
$q$	$R(q)$
0	0
1	10
2	20
3	30
4	40
5	50
6	60
7	70
8	80
9	90
10	100



# Average and Marginal Revenue, Example: Visualized



$q$	$R(q)$	$AR(q)$	$MR(q)$
0	0	—	—
1	10	10	10
2	20	10	10
3	30	10	10
4	40	10	10
5	50	10	10
6	60	10	10
7	70	10	10
8	80	10	10
9	90	10	10
10	100	10	10



$$R(q) = 10q$$