

# 1.2 — Budget Constraint

ECON 306 • Microeconomic Analysis • Spring 2022

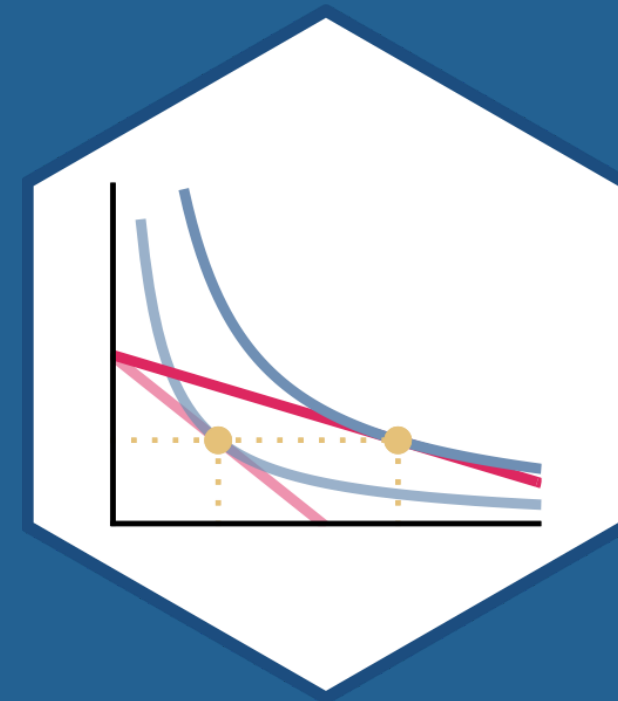
Ryan Safner

Assistant Professor of Economics

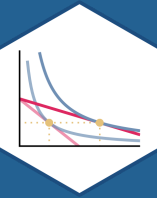
✉ [safner@hood.edu](mailto:safner@hood.edu)

🔗 [ryansafner/microS22](https://ryansafner/microS22)

🌐 [microSs22.classes.ryansafner.com](https://microSs22.classes.ryansafner.com)



# Outline



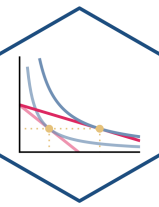
Rational Choice Theory

The Budget Constraint

Opportunity Cost

Changes in Market Conditions

# The Two Major Models of Economics as a “Science”

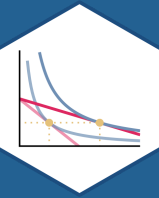


## Optimization

- Agents have **objectives** they value
- Agents face **constraints**
- Make **tradeoffs** to maximize objectives within constraints

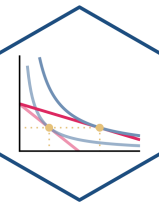
## Equilibrium

- Agents **compete** with others over **scarce** resources
- Agents **adjust** behaviors based on prices
- **Stable outcomes** when adjustments stop



# Rational Choice Theory

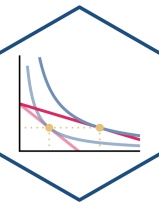
# The Logic of Choice: Ends and Means



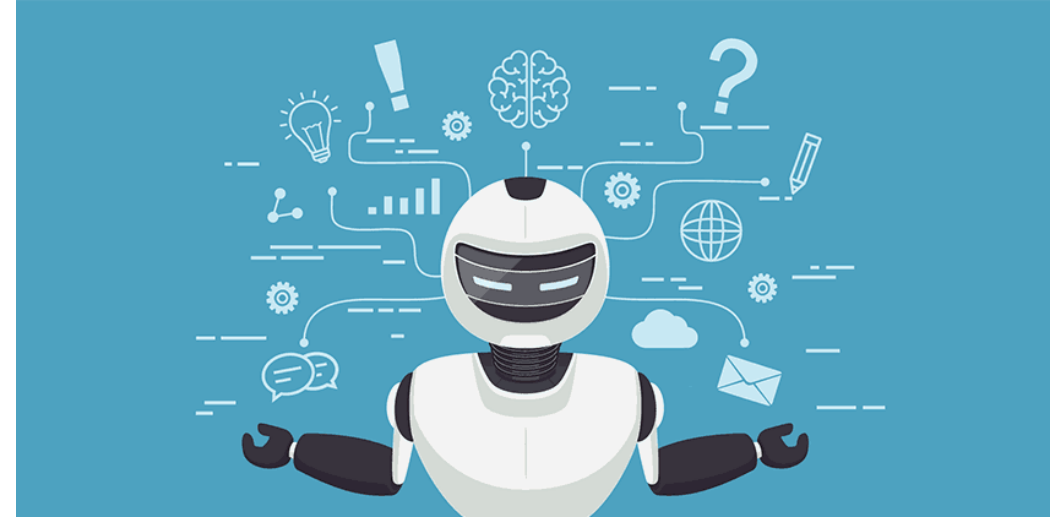
- Each of us acts **purposefully**
- We have **ends**, goals, desires, objectives
  - *Anything* you value!
- We use **means** in the world that we *believe* will achieve our ends
  - **“utility”** when we **consume** services, or
  - if scarce physical object: **“economic good”** or **resource**



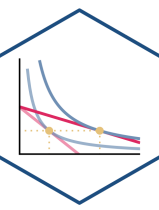
# The Logic of Choice: Purpose



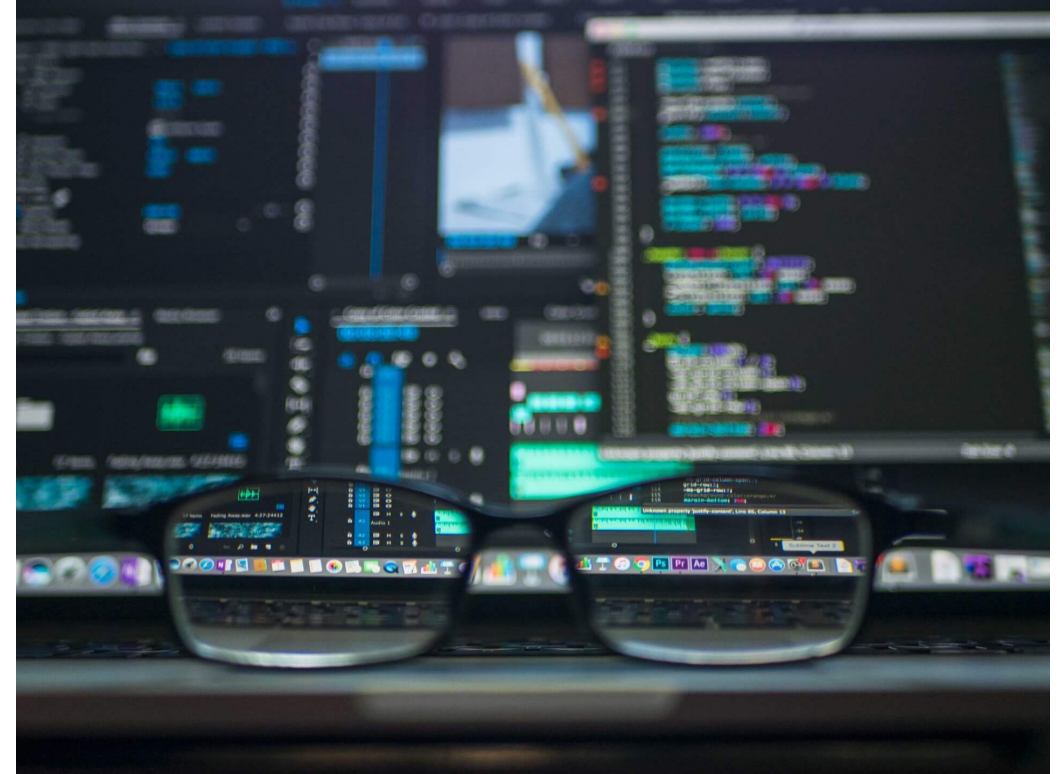
- Acting with **purpose** distinguishes humans from everything else in the universe
- Artificial intelligence researchers face **“the frame problem”**
  - Perception requires motivational goals to determine how to filter reality



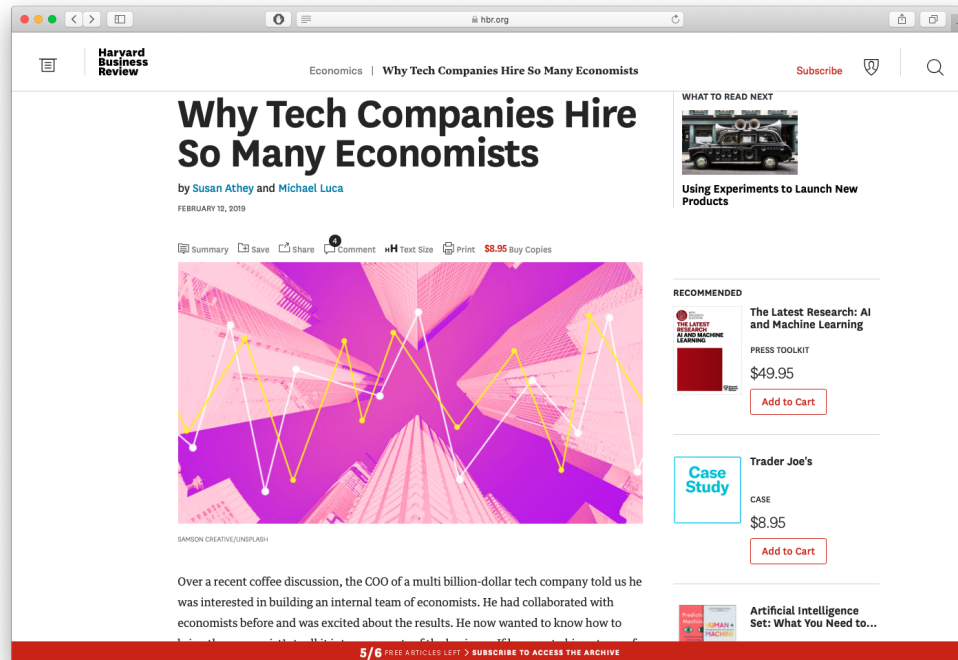
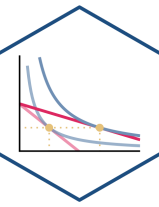
# Causal Inference I



- Machine learning and artificial intelligence are “dumb”
  - Data can never “speak for itself!”
- With the right models and research designs, we *can* say “X causes Y” and quantify it!
- Economists are in a unique position to make *causal* claims that mere statistics cannot



# Causal Inference II

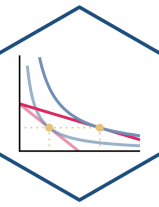


## Harvard Business Review

“First, the field of economics has spent decades developing a toolkit aimed at investigating empirical relationships, focusing on techniques to help understand which correlations speak to a causal relationship and which do not. This comes up all the time — does Uber Express Pool grow the full Uber user base, or simply draw in users from other Uber products? Should eBay advertise on Google, or does this simply syphon off people who would have come through organic search anyway? Are African-American Airbnb users rejected on the basis of their race? These are just a few of the countless questions that tech companies are grappling with, investing heavily in understanding the extent of a causal relationship.”



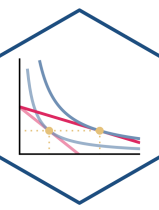
# The Law of Demand



- Perhaps the most fundamental economic “law” is the **law of demand**:
  - **inverse relationship between price and quantity consumed**
  - i.e. demand curves slope downwards
- We investigate its source, and derive more useful properties
- First, we will need to develop a more rigorous framework



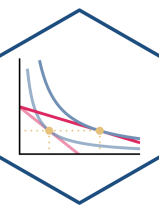
# Rational Choice Theory



- How do people decide:
  - which products to buy
  - which activities to dedicate their time to
  - how to save or invest/plan for the future
- **Rational choice theory**: assume that they **optimize** within constraints
- A model of behavior we can extend to most scenarios



# Rational Choice Theory: Beyond Consumers

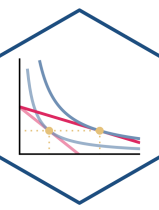


- Often called “**Consumer Theory**” in textbooks, but realize:
- *Everyone* is “a consumer”
  - "Goods and services" aren't just food, clothing, etc, but *anything* that you value! (free time, friendship, reputation, etc.)
  - Producers demand productive inputs
- We are really modeling how **individuals** make choices in almost *any* context!





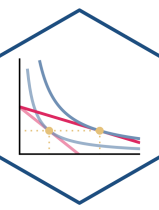
# Consumption Bundles



- Imagine a (very strange) supermarket sells  $x$  and  $y$
- Your choices: amounts of  $\{x, y\}$  to consume as a **bundle**



# Consumption Bundles: Graphically

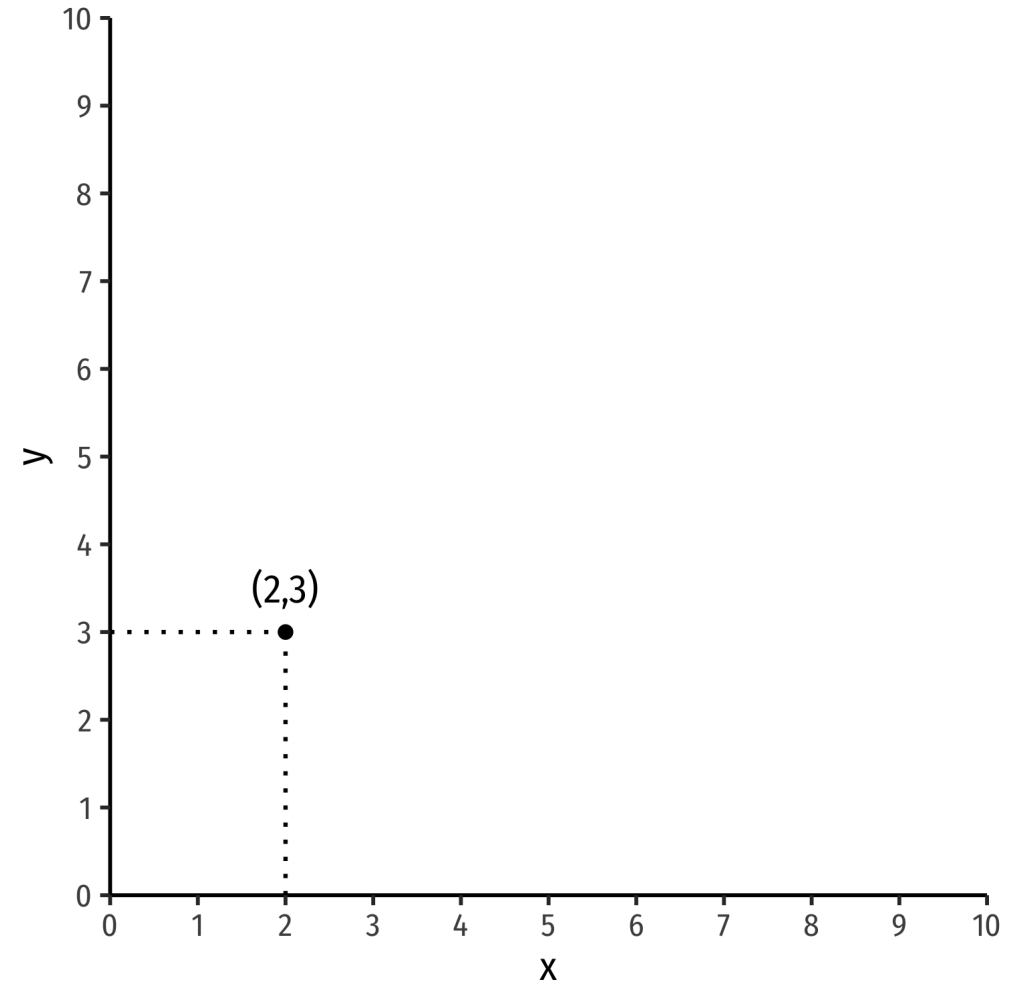


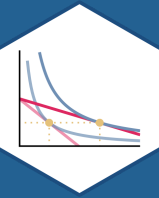
- We can represent bundles graphically
- We'll stick with 2 goods  $(x, y)$  in 2-dimensions<sup>†</sup>

## Example:

- $x$ : 2 units
- $y$ : 3 units

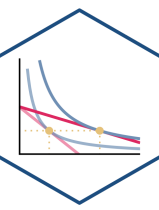
<sup>†</sup> See [appendix](#) in today's class page to extend to  $n$  goods!





# The Budget Constraint

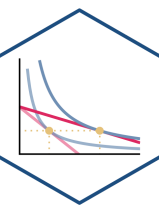
# Affordability



- If you had \$100 to spend, what bundles of goods  $\{x, y\}$  would you buy?
- Only those bundles that are **affordable**
- Denote prices of each good as  $\{p_x, p_y\}$
- Let  $m$  be the amount of income a person has



# Affordability



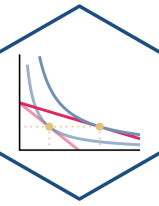
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- Denote prices of each good as  $\{p_x, p_y\}$
- Let  $m$  be the amount of income a person has
- A bundle  $\{x, y\}$  is **affordable** at given prices  $\{p_x, p_y\}$  when:

$$p_x x + p_y y \leq m$$





# The Budget Set

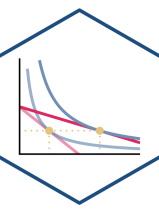


- The set of *all* affordable bundles that a consumer can choose is called the **budget set** or **choice set**

$$p_x x + p_y y \leq m$$



# The Budget Set & the Budget Constraint



- The set of *all* affordable bundles that a consumer can choose is called the **budget set** or **choice set**

$$p_x x + p_y y \leq m$$

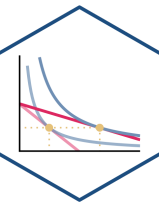
- The **budget constraint** is the set of all bundles that spend *all income*  $m$ :<sup>†</sup>

$$p_x x + p_y y = m$$



<sup>†</sup> Note the difference (the in/equality): budget *constraint* is the **subset** of the *budget set* that *spends all income*.

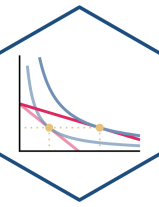
# The Budget Constraint, Graphically



- For 2 goods,  $(x, y)$

$$p_x x + p_y y = m$$

# The Budget Constraint, Graphically

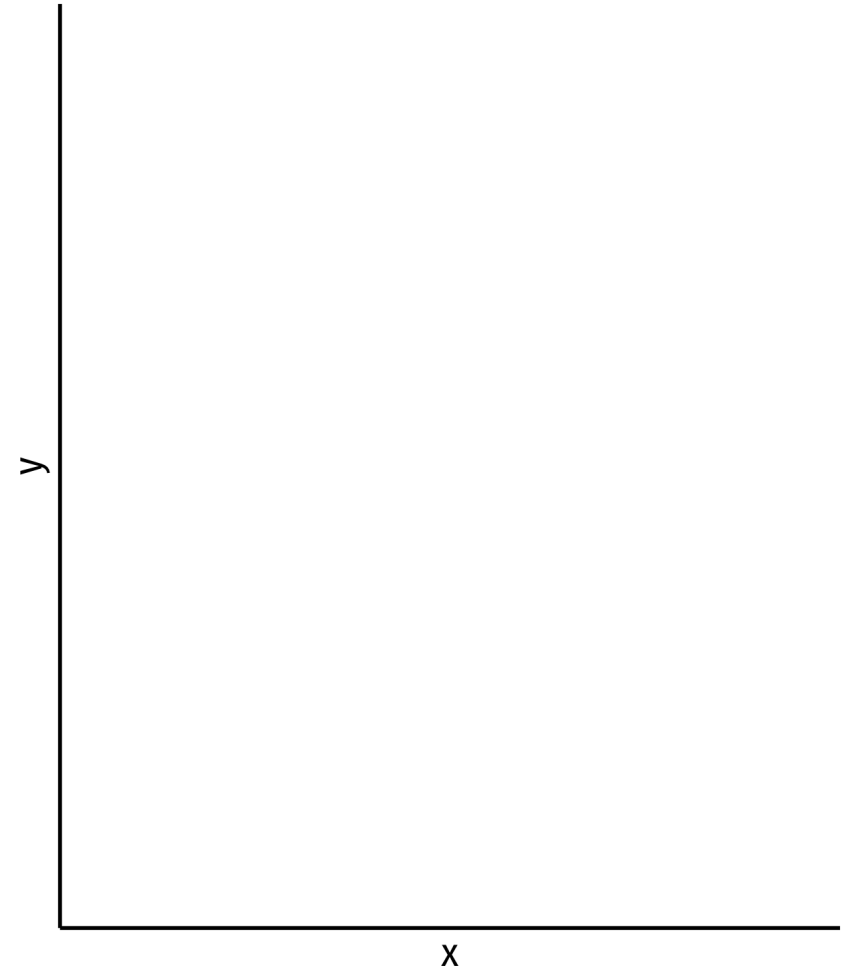


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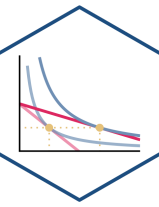
$$p_x x + p_y y = m$$

- Solve for  $y$  to graph

$$y = \frac{m}{p_y} - \frac{p_x}{p_y} x$$



# The Budget Constraint, Graphically



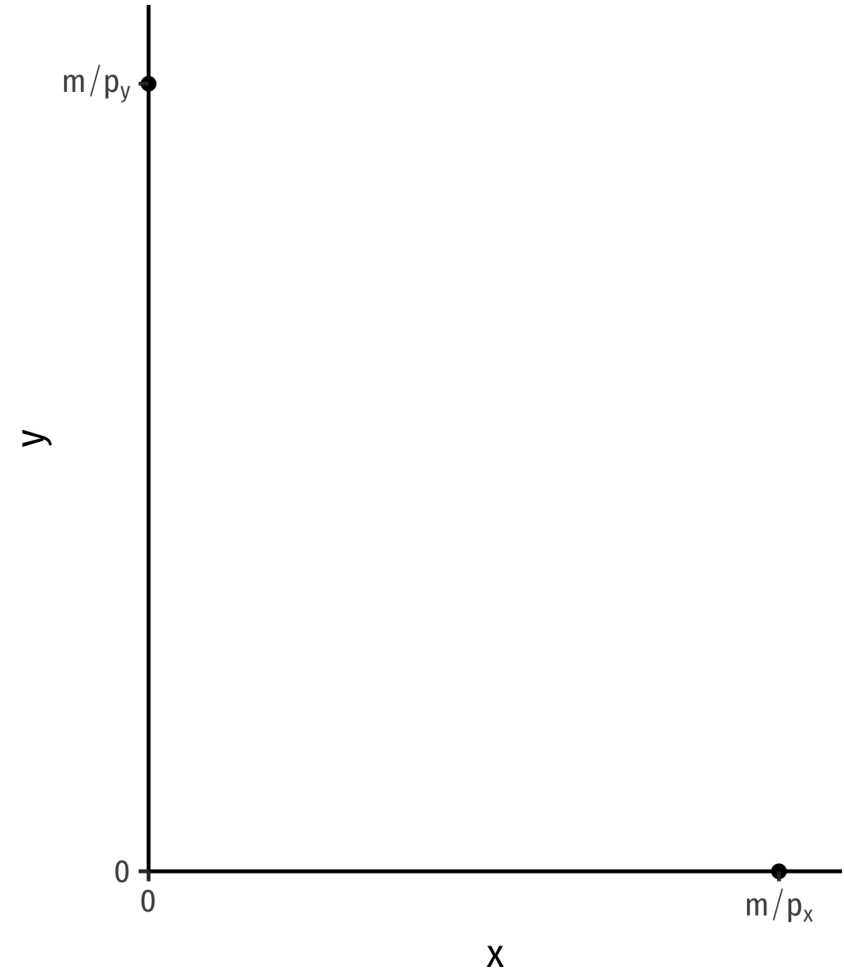
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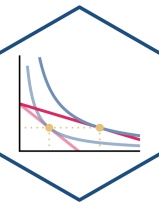
- Solve for  $y$  to graph

$$y = \frac{m}{p_y} - \frac{p_x}{p_y} x$$

- $y$ -intercept:  $\frac{m}{p_y}$
- $x$ -intercept:  $\frac{m}{p_x}$



# The Budget Constraint, Graphically



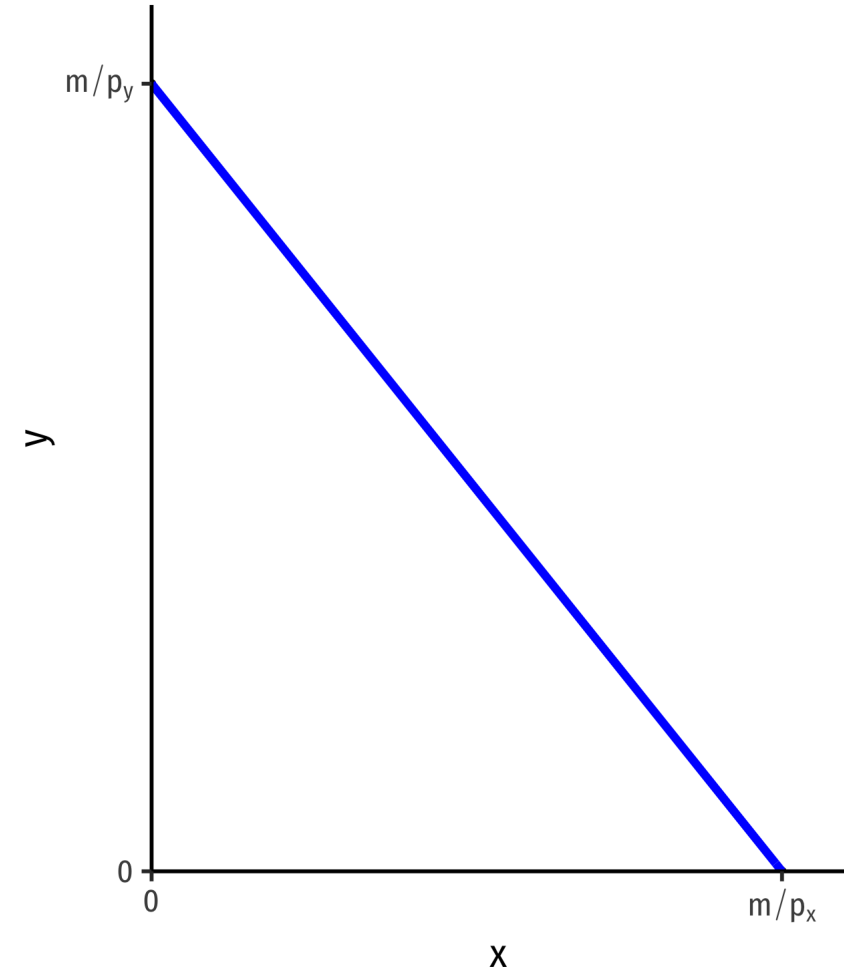
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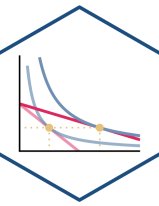
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- $y$ -intercept:  $\frac{m}{p_y}$
- $x$ -intercept:  $\frac{m}{p_x}$
- slope:  $-\frac{p_x}{p_y}$



# The Budget Constraint, Graphically



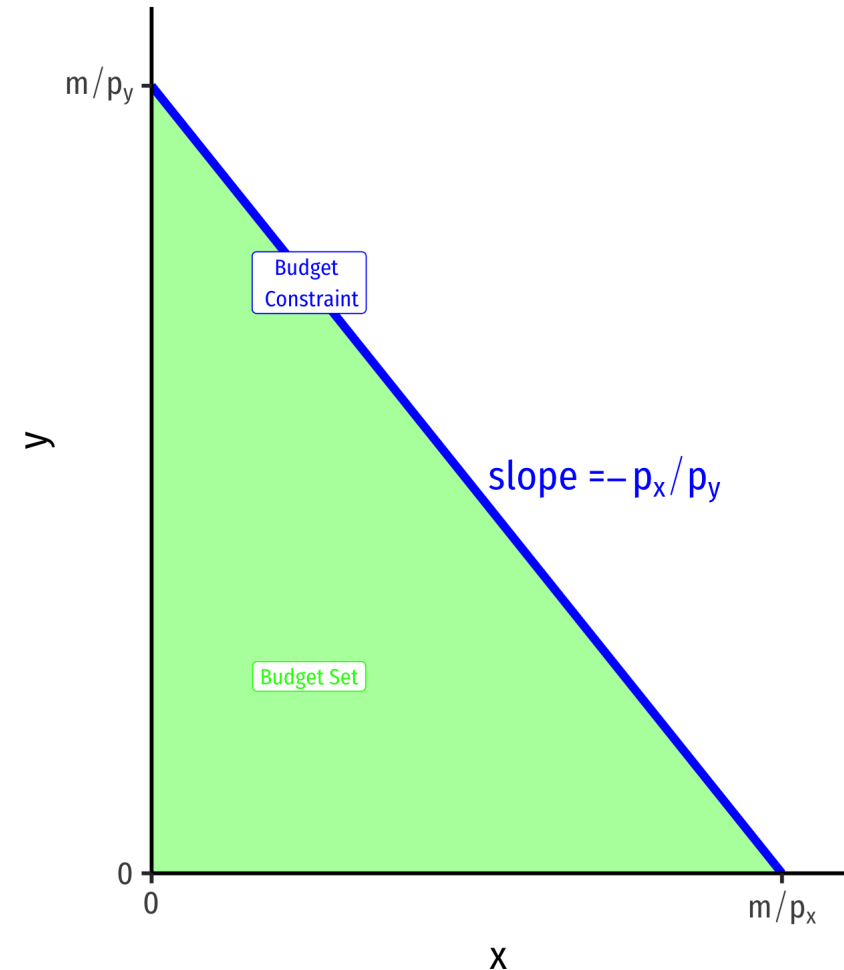
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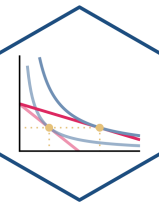
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# The Budget Constraint: Example



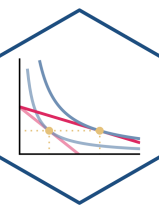
**Example:** Suppose you have an income of \$50 to spend on lattes ( $l$ ) and burritos ( $b$ ). The price of lattes is \$5 and the price of burritos is \$10.

Let  $l$  be on the horizontal axis and  $b$  be on the vertical axis.

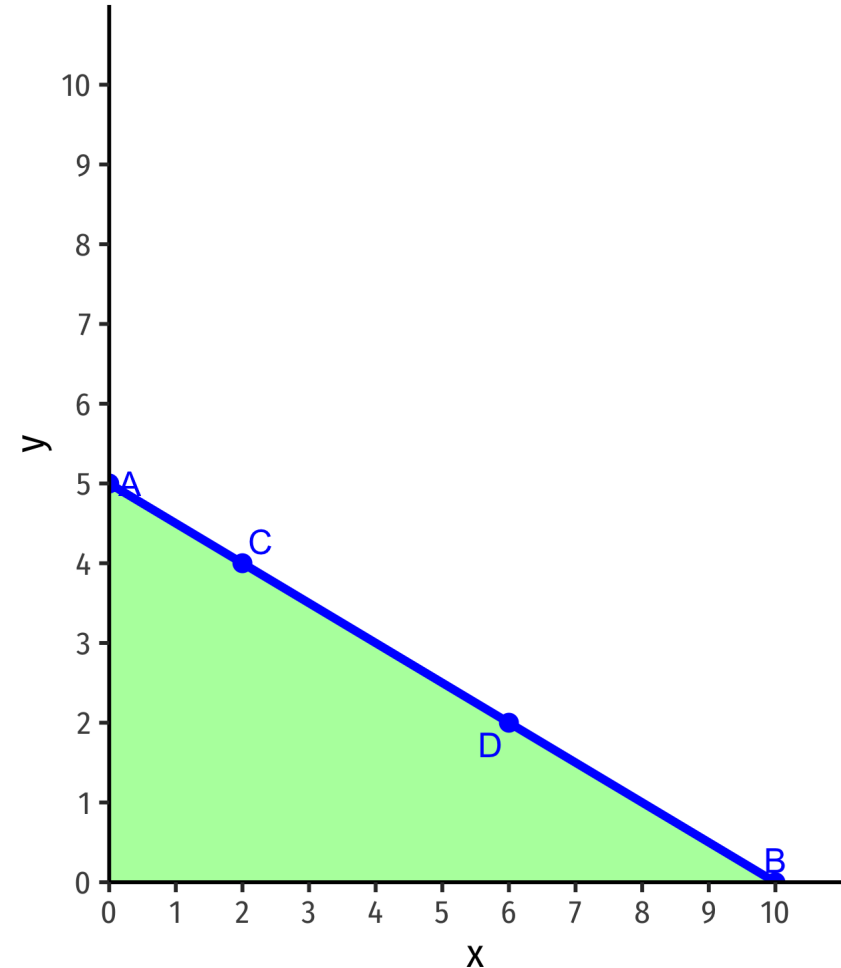
1. Write an equation for the budget constraint (in graphable form).
2. Graph the budget constraint.



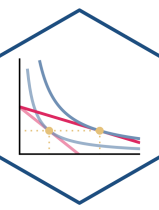
# Interpreting the Budget Constraint



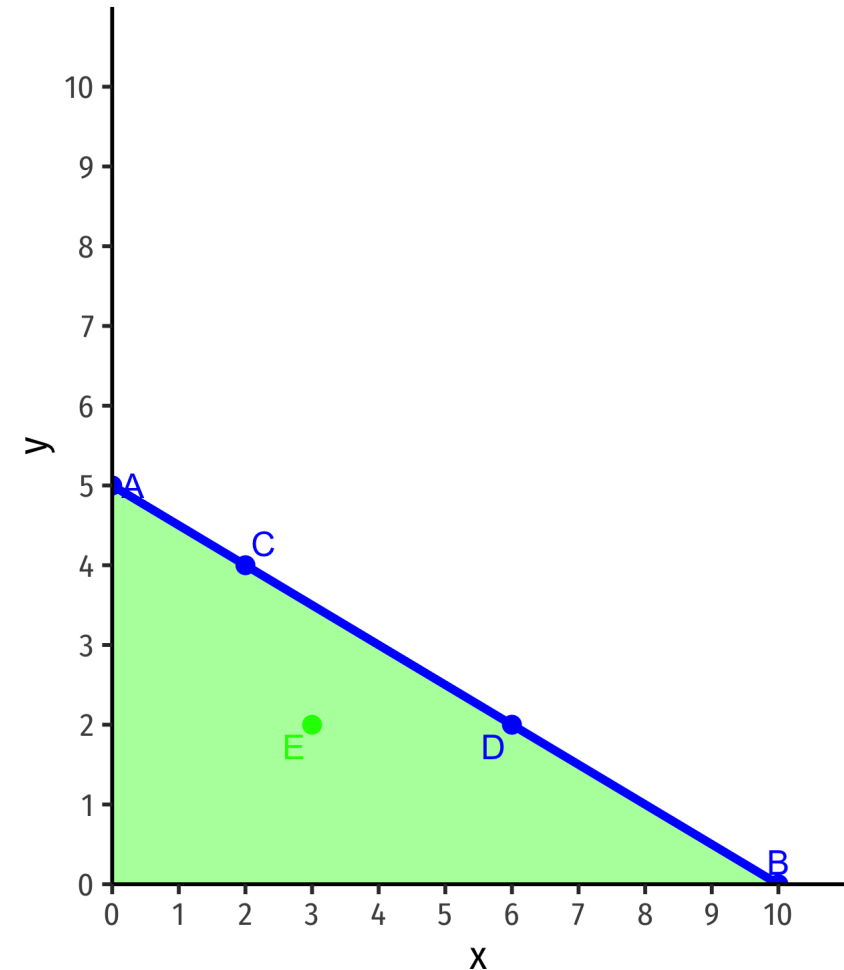
- Points **on the line** spend all income
  - A:  $\$5(0x) + \$10(5y) = \$50$
  - B:  $\$5(10x) + \$10(0y) = \$50$
  - C:  $\$5(2x) + \$10(4y) = \$50$
  - D:  $\$5(6x) + \$10(2y) = \$50$



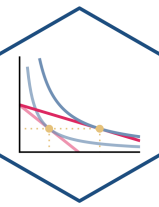
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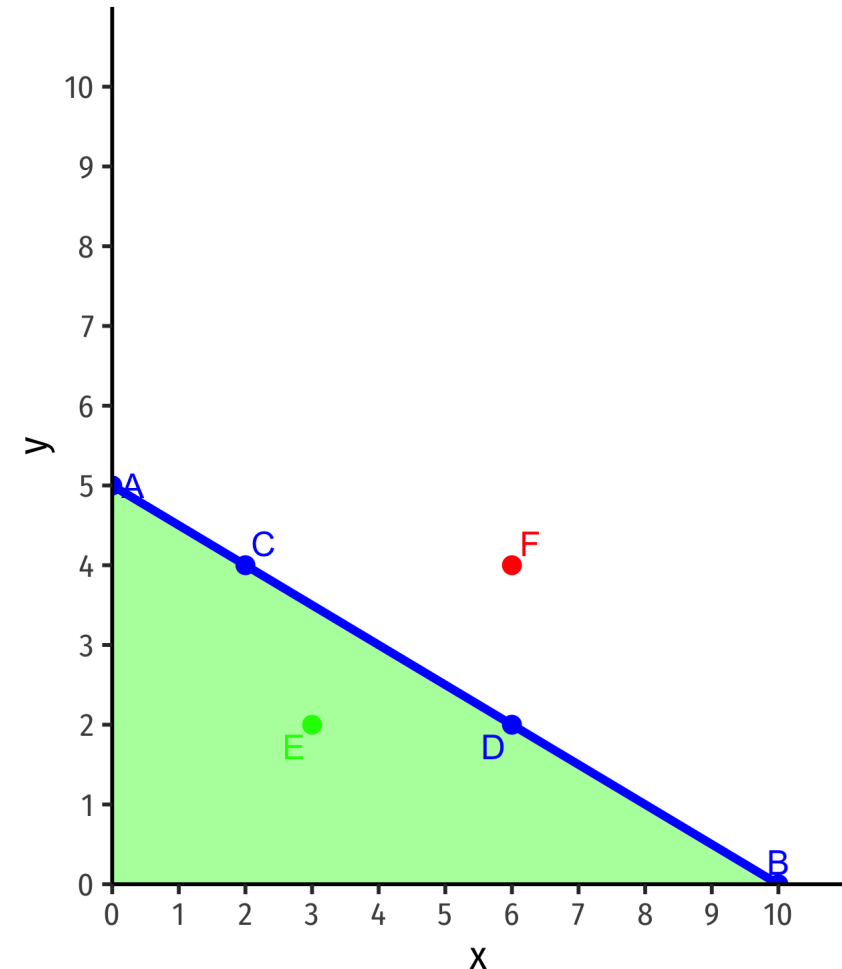
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  - D:  $\$5(6x) + \$10(2y) = \$50$
- Points **beneath** the line are **affordable** but don't use all income
  - E:  $\$5(3x) + \$10(2y) = \$35$

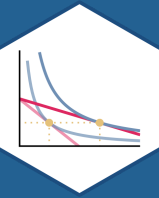


# Interpreting the Budget Constraint



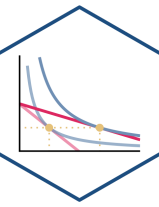
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- Points **beneath** the line are **affordable** but don't use all income
  - E:  $\$5(3x) + \$10(2y) = \$35$
- Points **above** the line are **unaffordable** (at current income and prices)





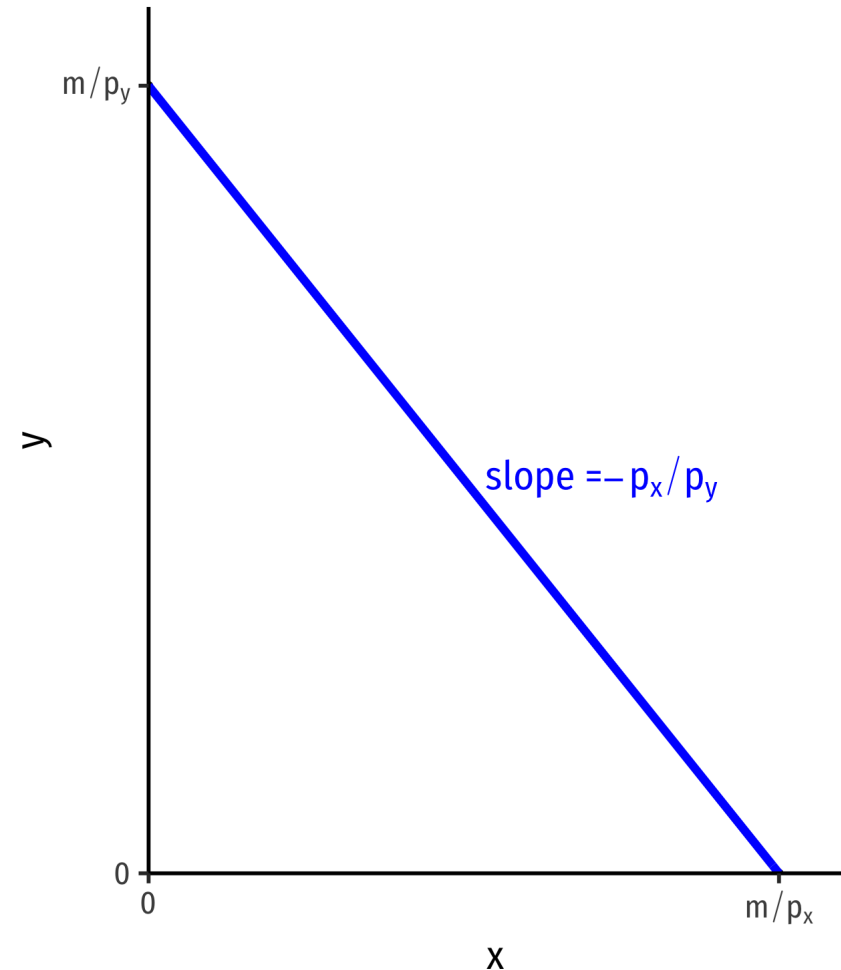
# Opportunity Cost

# Interpreting the Slope

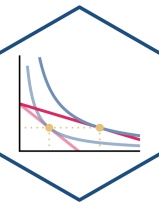


- **Slope:** **tradeoff** between  $x$  and  $y$  at market prices
  - Market **“exchange rate”** between  $x$  and  $y$ :  $\frac{p_x}{p_y}y : 1x$
- **Relative price** of  $x$ , or the **opportunity cost** of  $x$ :

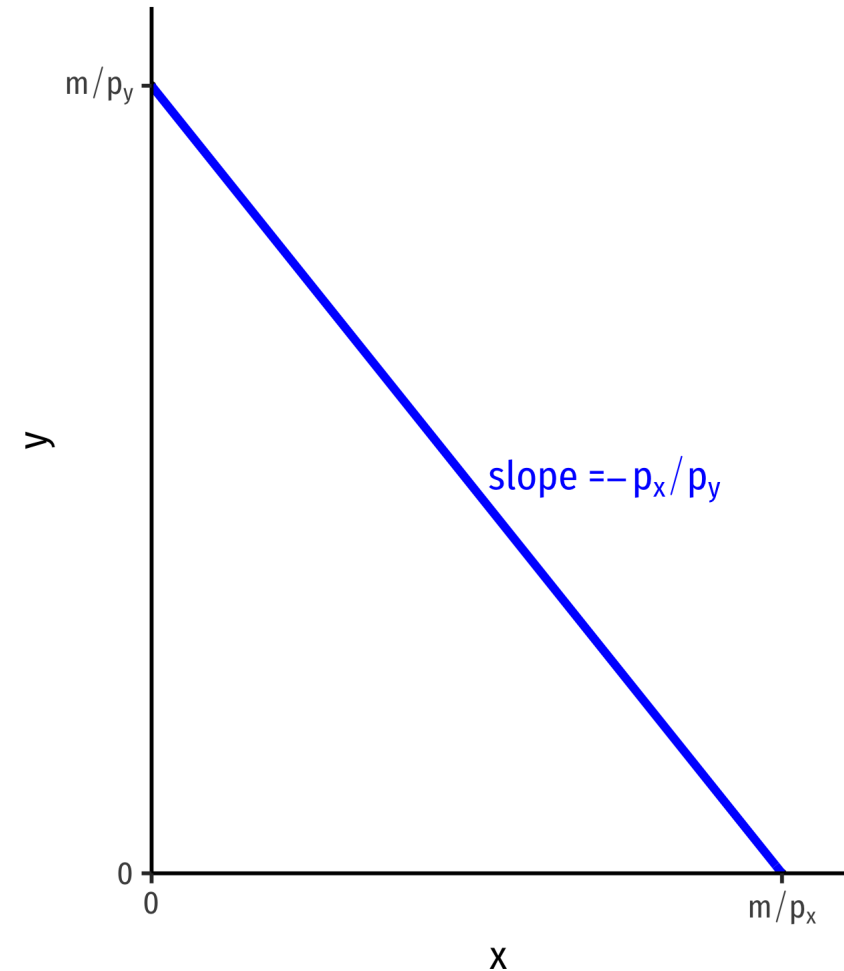
Consuming 1 more unit of  $x$   
requires giving up  $\frac{p_x}{p_y}$  units of  $y$



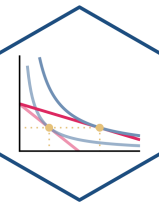
# Opportunity Cost



- **Opportunity cost:** value of next best foregone opportunity
- Even though we use money for prices, when you consume  $x$ , you're really giving up **the opportunity to consume  $y$** !



# The Parable of the Broken Window

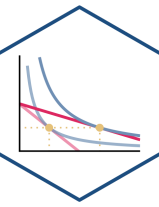


- *That Which is Seen and That Which is Not Seen*

Frederic Bastiat

1801-1850

# The Parable of the Broken Window



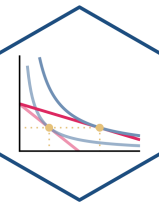
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1801-1850

- *That Which is Seen and That Which is Not Seen*
- “That which is seen”
  - The broken window
  - Resources diverted into glassmaking



# The Parable of the Broken Window

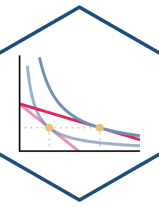


Frederic Bastiat

1801-1850

- *That Which is Seen and That Which is Not Seen*
- “That which is seen”
  - The broken window
  - Resources diverted into glassmaking
- “That which is not seen”
  - Opportunity cost of fixing the window
  - Resources diverted *away* from other opportunities

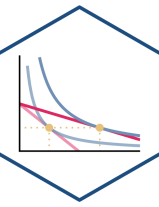
# Applying the Parable of the Broken Window



- What does it mean to say that “**spending money 'stimulates' the economy**”?

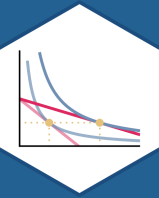


# Applying the Parable of the Broken Window



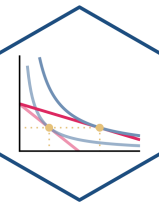
- What does it mean to say that “**spending money 'stimulates' the economy**”?
- Scarce resources used in one industry can **not** be used in other industries
- **Every (visible) decision to spend on X yields more X, and destroys an (invisible) opportunity to spend on Y**





# Changes in Market Conditions

# Changes in Market Conditions

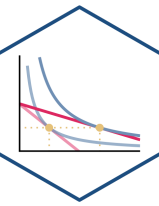


$$m = p_x x + p_y y$$
$$y = \frac{m}{p_y} - \frac{p_x}{p_y} x$$

- Budget constraint is a function of specific **parameters**
  - $m$ : income
  - $p_x, p_y$ : market prices
- Economic analysis: **how changes in constraints affect people's choices**
  - “incentives”



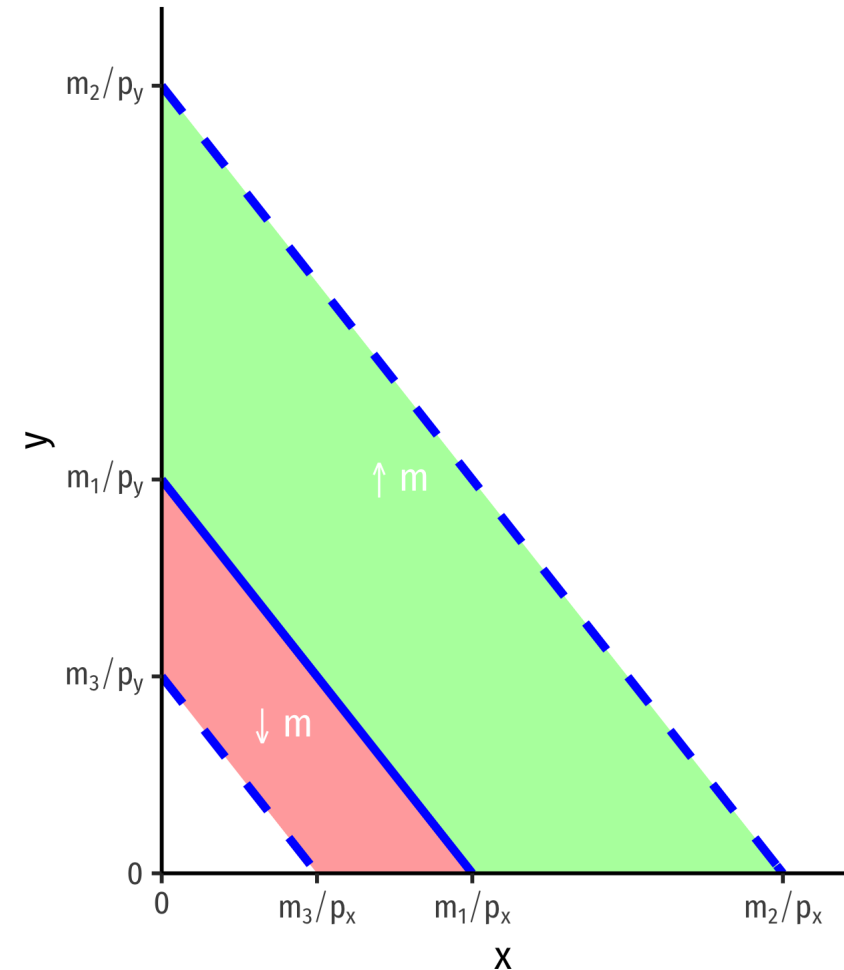
# Changes in Income, $m$



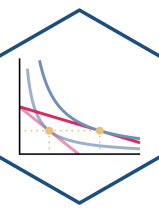
- Changes in **income** shift the budget constraint

## Example:

- Income **increases**  $m_1 \rightarrow m_2$
  - Income **decreases**  $m_1 \rightarrow m_3$
- 
- Slope unchanged (no change in prices!)
  - **Gain/loss** of affordable bundles



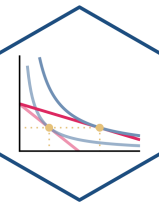
# Changes in Income, $m$ : Example



**Example:** Continuing the lattes and burritos example, (income is \$50, lattes are \$5, burritos are \$10), suppose your income doubles to \$100.

1. Find the equation of the new budget constraint (in graphable form).
2. Graph the new budget constraint.

# Changes in Relative Prices, $p_x$ or $p_y$



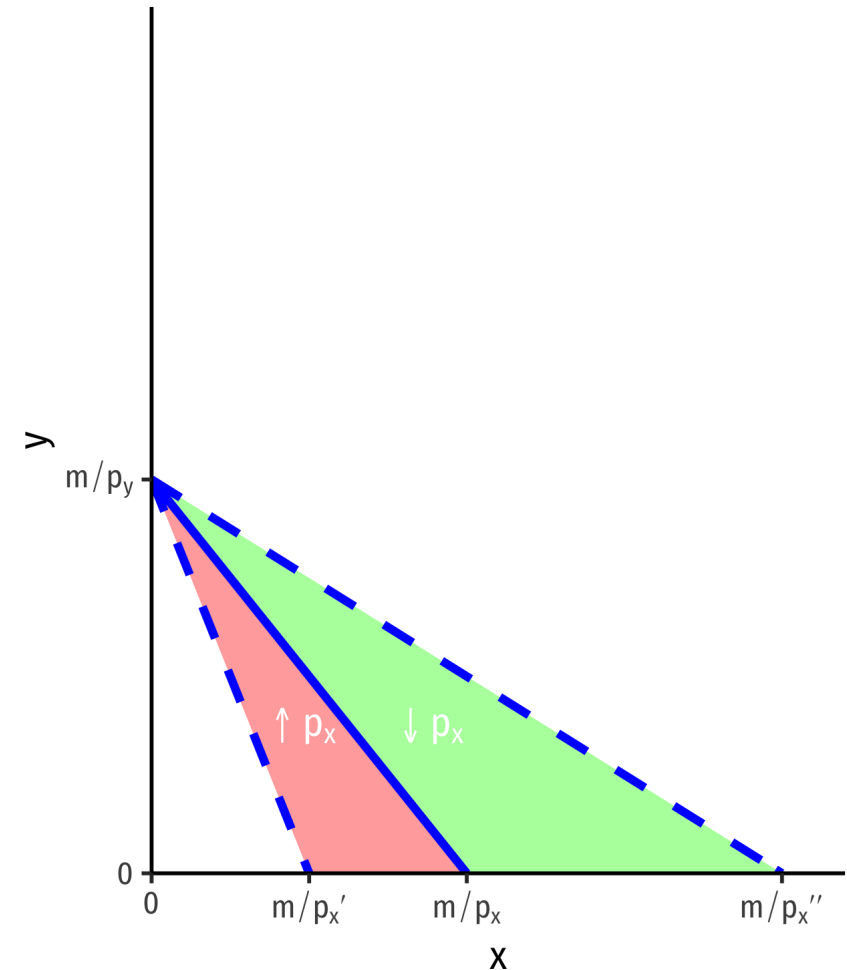
- Change in *relative prices* rotate the budget constraint

## Example:

- Price of  $x$  **increases**  $p_x \rightarrow p'_x$
- Price of  $x$  **decreases**  $p_x \rightarrow p''_x$

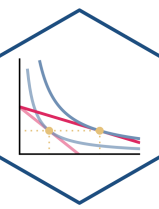
- Change in slope:  $-\frac{p'_x}{p_y}$ ,  $-\frac{p''_x}{p_y}$

- Gain/loss** of affordable bundles





# Changes in Relative Prices, $p_x$ or $p_y$



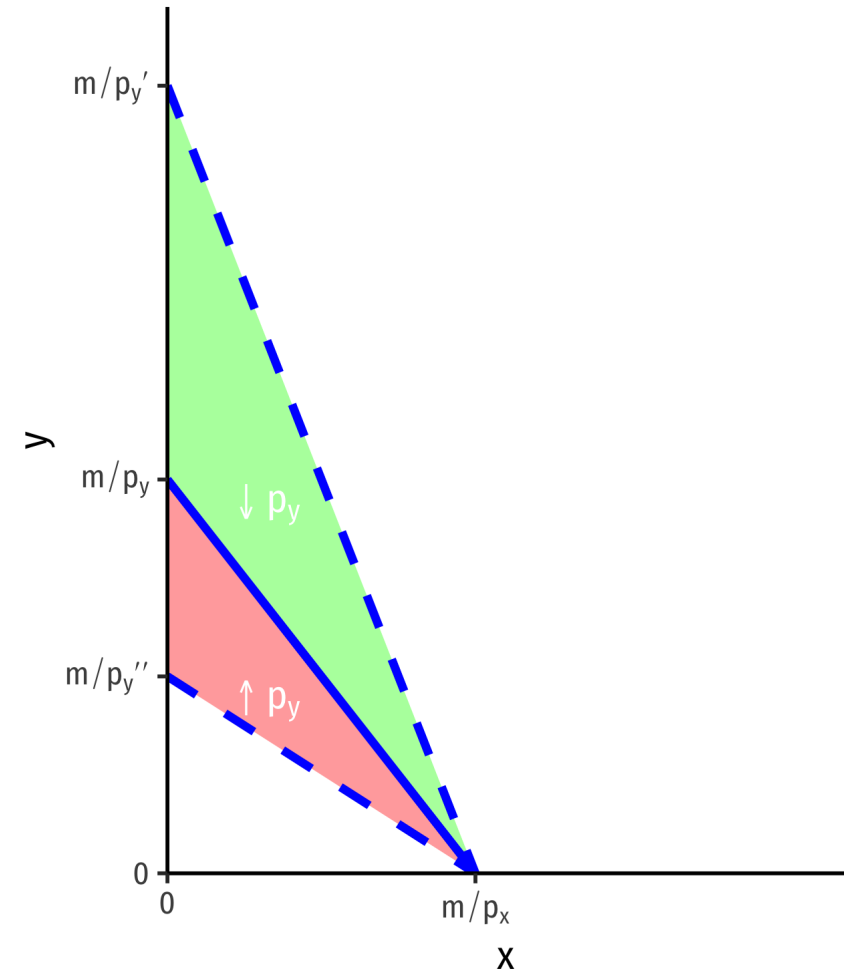
- Change in **relative prices** rotate the budget constraint

## Example:

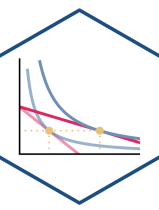
- Price of  $y$  **increases**  $p_y \rightarrow p'_y$
- Price of  $y$  **decreases**  $p_y \rightarrow p''_y$

- Change in slope:  $-\frac{p_x}{p'_y}$ ,  $-\frac{p_x}{p''_y}$

- Gain/loss** of affordable bundles



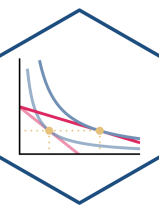
# Economics is About (Changes in) *Relative* Prices



- Economic analysis is about (changes in) *relative* prices
- Budget constraint slope (opportunity cost of  $x$ ) is  $-\frac{p_x}{p_y}$
- Only “**real**” changes in relative prices (from changes in market conditions) change consumer constraints (and alter behavior)
- i.e. not “the price of  $x$ ,” its about “the price of  $x$  *relative to the price of  $y$* ”!



# Economics is About (Changes in) *Relative* Prices

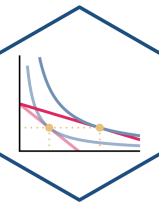


- “**Nominal**” prices are often meaningless!
  - Need to make *comparisons* between prices of different goods

**Example:** Imagine yourself in a strange country. All you know is that the price of bread, in local currency, is “6”...



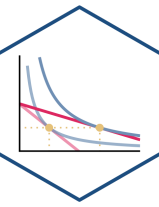
# Changes in Relative Prices: Example



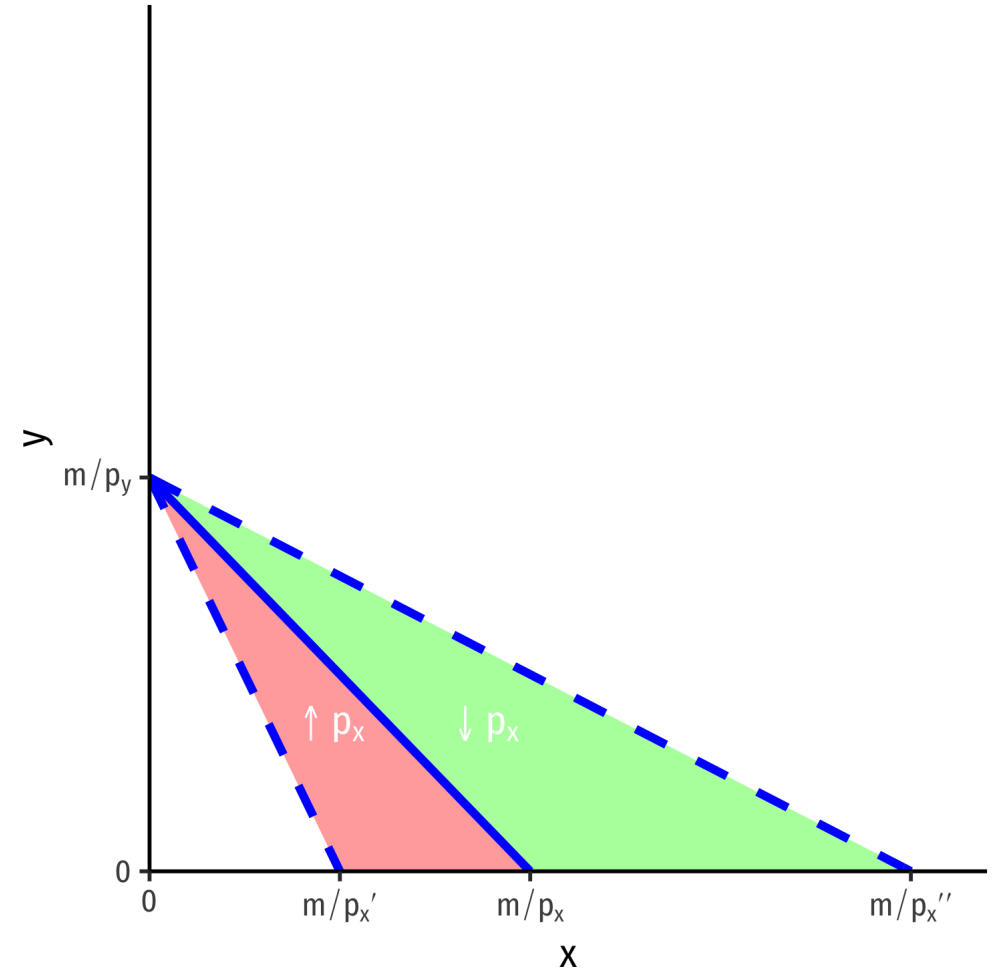
**Example:** Continuing the lattes and burritos example (income is \$50, lattes are \$5, burritos are \$10).

1. Suppose the price of lattes doubles from \$5 to \$10. Find the equation of the new budget constraint and graph it.
2. Return to the original price of lattes (\$5) and suppose the price of burritos falls from \$10 to \$5. Find the equation of the new budget constraint and graph it.

# Budget Constraint and the Law of Demand



- Recall the **law of demand**
- We can derive it right off the budget constraint!
  - As  $\uparrow p_x$ , person can consume less  $x$
  - As  $\downarrow p_x$ , person can consume more  $x$
- Notice I have made **no assumptions** about rationality, preferences, utility, etc to get this!



A graph illustrating the concept of a supporting hyperplane. It shows a convex function (blue curve) and a supporting hyperplane (red line) that touches the function at a point (yellow dot). The hyperplane is tangent to the function at that point, and the function lies entirely above the hyperplane. The graph is enclosed in a blue hexagonal frame.

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