

# Work, wellbeing, and scarcity

Sessions 5–6

PMAP 8141: Microeconomics for Public Policy  
Andrew Young School of Policy Studies

# Plan for today

Incentives

Elasticity

Preferences, constraints, and tradeoffs

Utility and indifference

Calculus party!!!

Maximizing utility

# Incentives

# Why do people do what they do?

**People get utility from doing stuff**

Extrinsic rewards

Intrinsic rewards

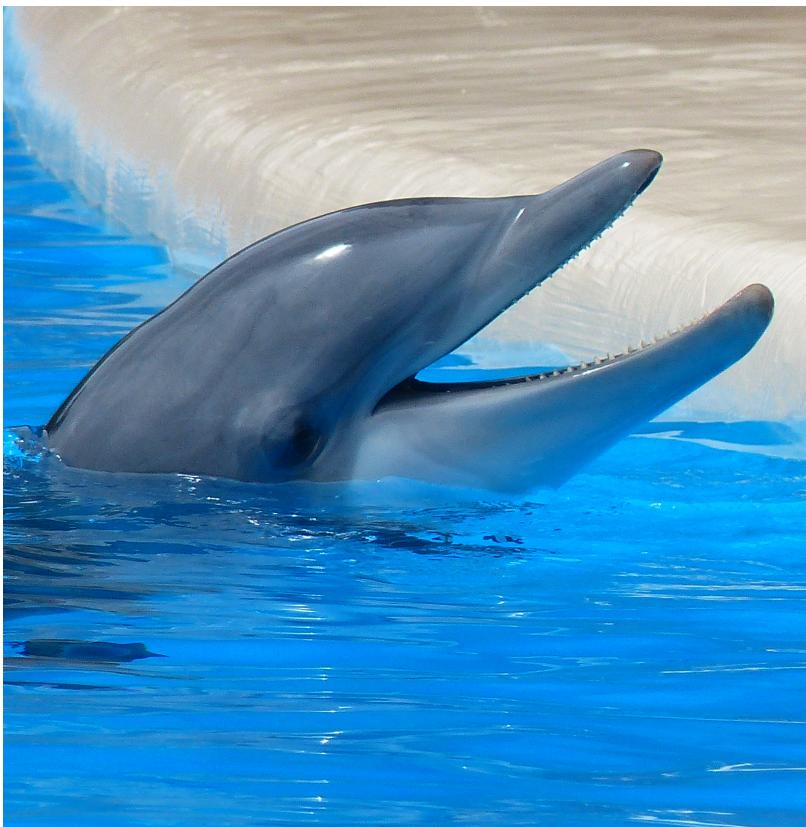
**These can get distorted  
and crowded out!**

# Why care as an MPA/MPP?

Good policy uses incentives to channel behavior toward some desired outcome. Bad policy either ignores incentives or fails to anticipate how rational individuals might change their behavior to avoid being penalized.

*Naked Economics*, p. 39

# Perverse incentives



# Importance of incentives

People respond to  
what you signal

You get what you measure

Daycares and late pickups

Blood donors

Taxes

Favors

Thanksgiving

Playgroups and daycares

MLMs

NED and democracy promotion

**Extrinsic rewards can crowd  
out intrinsic motivations**

**Don't violate important social  
relationships by reducing services  
to a market transaction**

**Pay enough or don't pay at all**

# Elasticity

# Elasticity

**How responsive people are  
to changes in prices**

“If the price changes, how much  
does the quantity change?”

# Elasticity and responsiveness

$$\varepsilon = -\frac{\% \text{ change in demand}}{\% \text{ change in price}}$$

$$\varepsilon = -\frac{\Delta Q}{\Delta P} \times \frac{P}{Q}$$

**% change in demand that follows a 1% change in price**

Q ↑ P ↓  
or  
Q ↓ P ↑

$\varepsilon = 2$ : "If price increases by 10%, quantity decreases by 20%"

$\varepsilon = 0.5$ : "If price increases by 10%, quantity decreases by 5%"

# $\epsilon = \infty$ = Perfectly elastic

Any change in price moves quantity to 0

Identical goods  
*Two vending machines*

# $\epsilon > 1$ = Elastic

Changes in price change the quantity a lot

Goods with substitutes  
*Diet Coke*

# $\epsilon = 1$ = Unit elastic

Changes in price change the quantity the same

# $\epsilon < 1$ = Inelastic

Changes in price change the quantity a little

Goods with few substitutes  
*AIDS medicine*

# $\epsilon = 0$ = Perfectly inelastic

Changes in price do nothing to the quantity

Survival goods  
*Water in the desert*

# $\epsilon$ , taxes, and preferences

Taxing things changes their prices

Changing prices changes  
quantities demanded

Taxing elastic goods will make quantities go down a lot and decrease tax revenues

Taxing inelastic goods will make quantities go down slightly and not hurt revenues

Category	Type	Calories per serving	Price per 100 g (\$)	Typical spending per week (\$)	Price elasticity of demand
1	Fruit and vegetables	660	0.38	2.00	1.128
2	Fruit and vegetables	140	0.36	3.44	0.830
15	Grain, pasta, bread	1,540	0.38	2.96	0.854
17	Grain, pasta, bread	960	0.53	2.64	0.292
28	Snacks, candy	433	1.13	4.88	0.270
29	Snacks, candy	1,727	0.68	7.60	0.295
30	Milk	2,052	0.09	2.32	1.1793
31	Milk	874	0.15	1.44	1.972

If P↑ by 10%, Q↓ ...

8.3%

2.7%

19.72%

# General tax guidance

**Tax inelastic products unless you're  
tying to change consumption**

Soda?

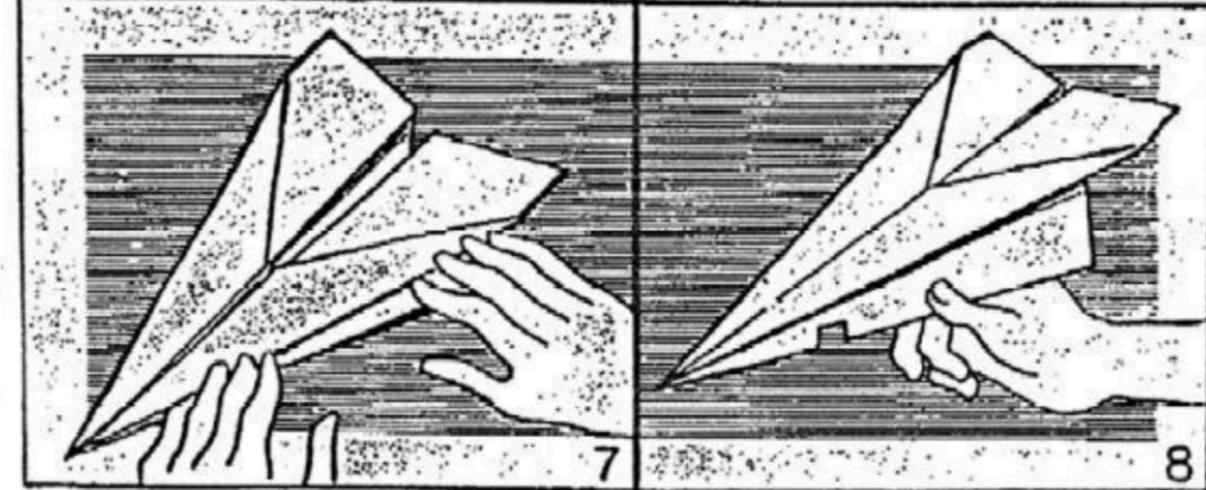
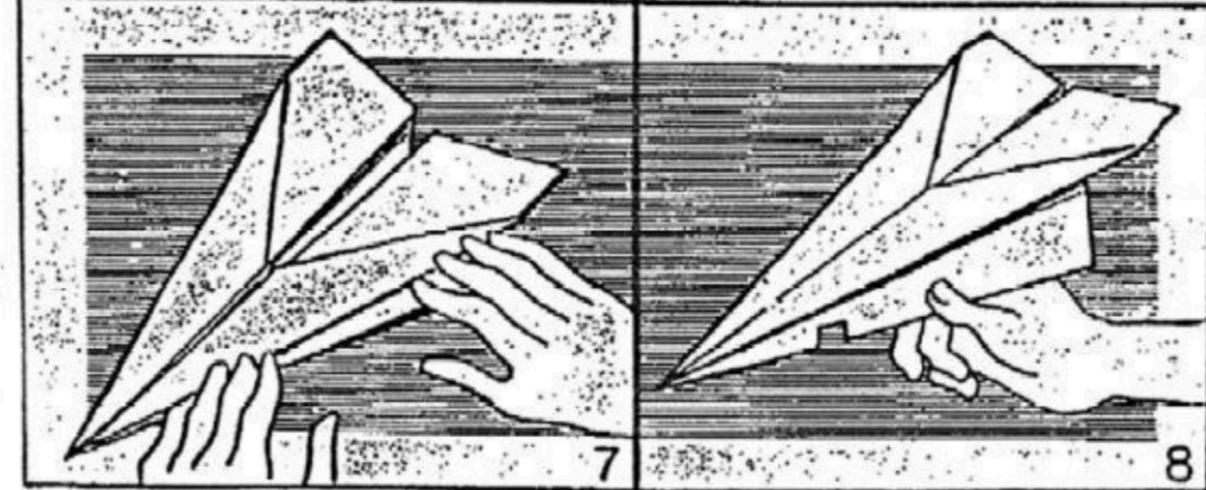
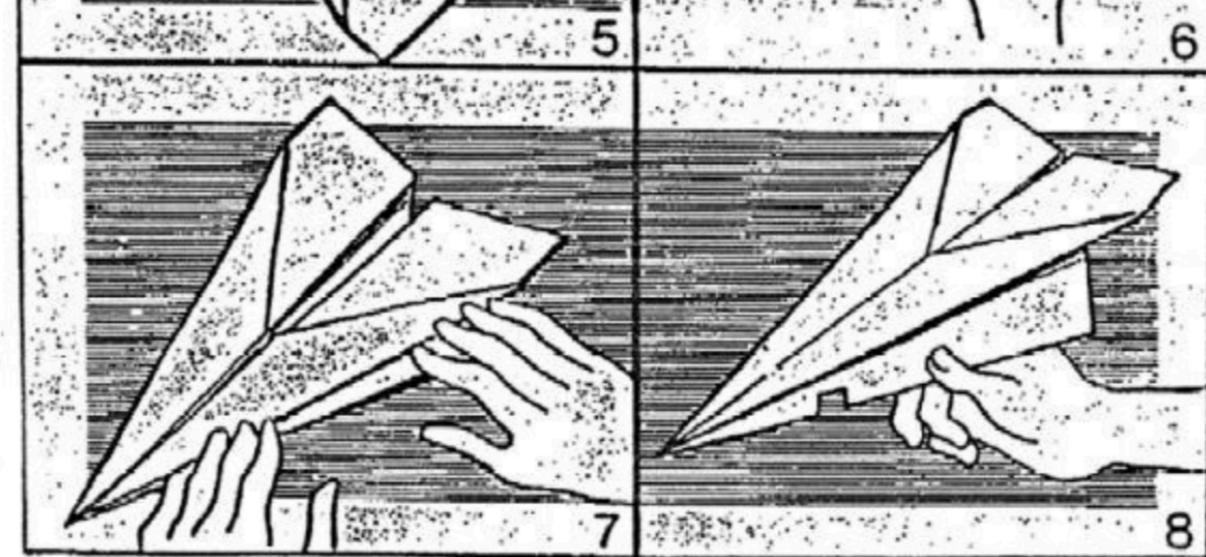
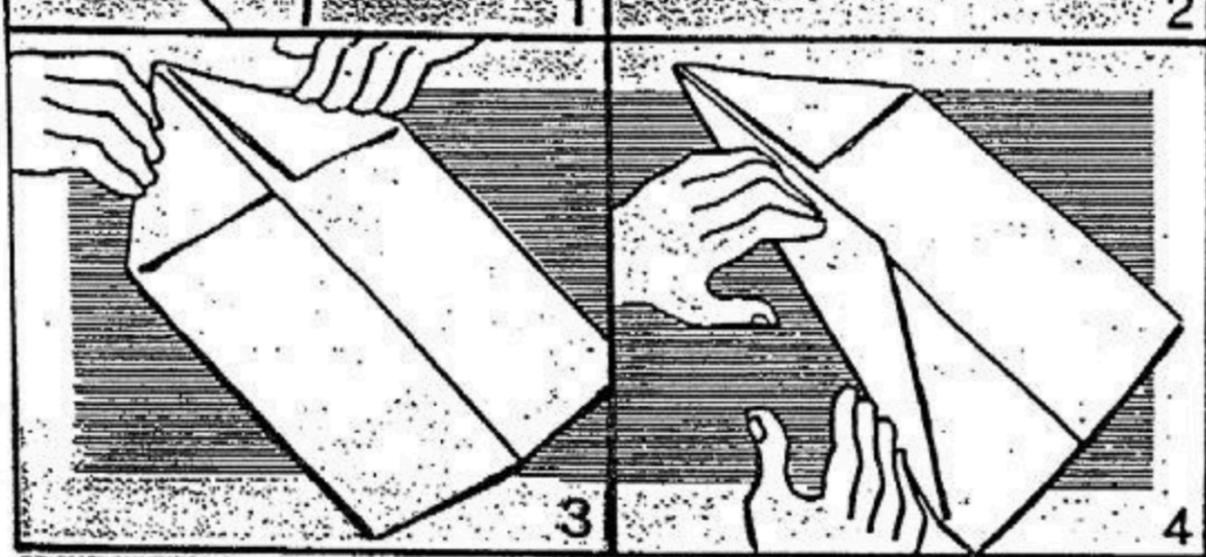
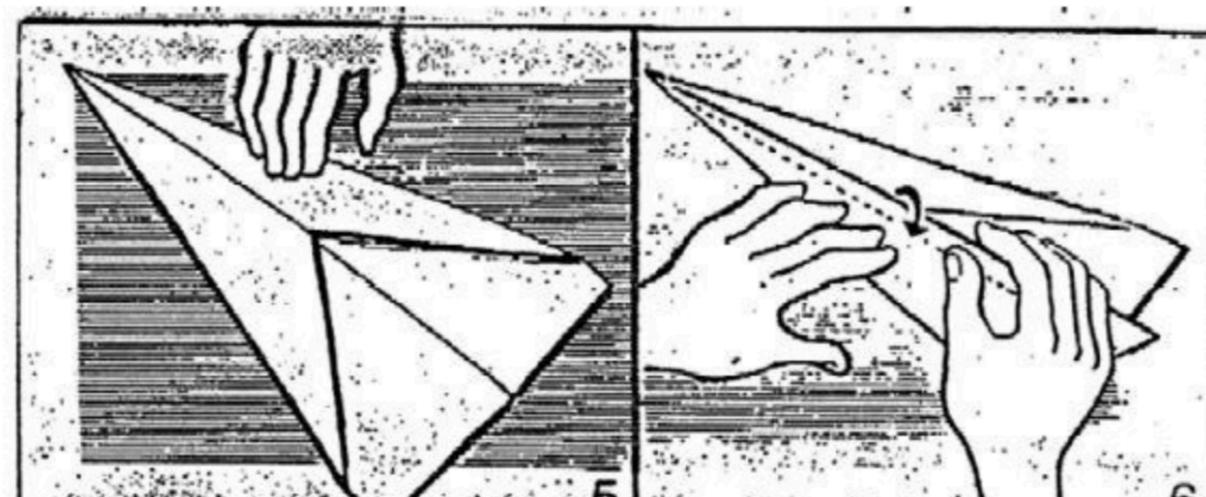
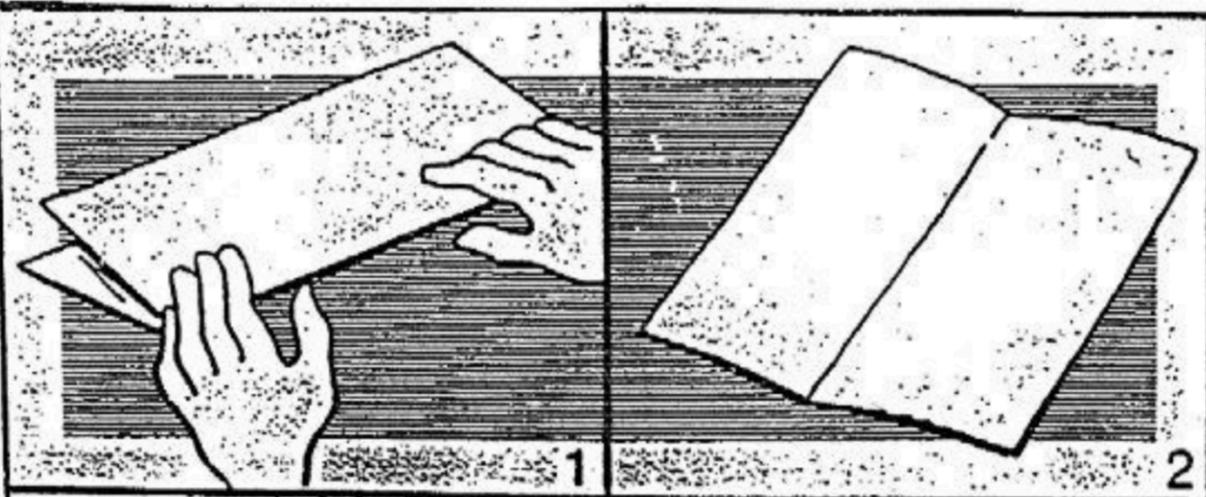
Cigarettes?

Alcohol?

Property?

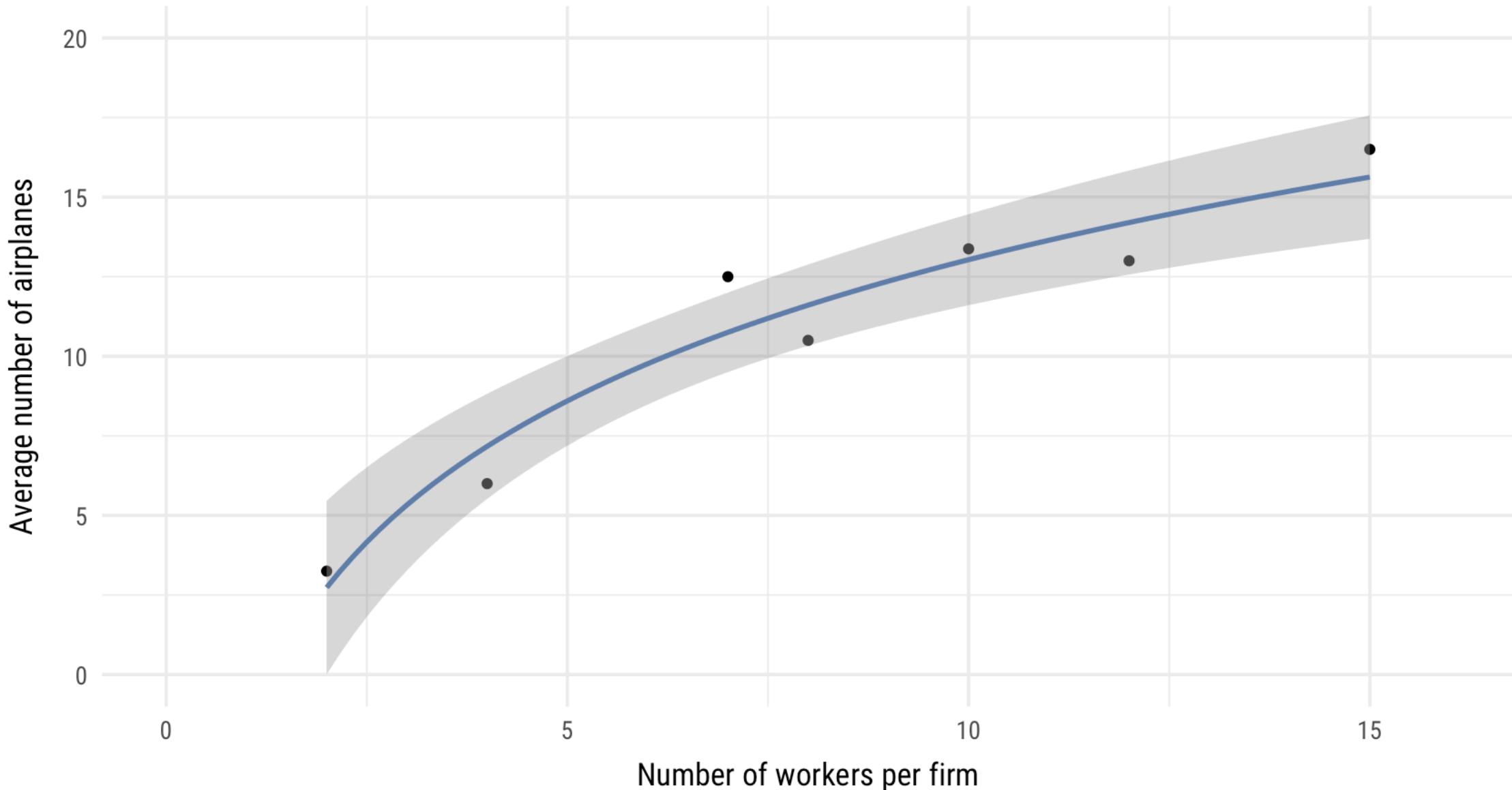
**Those who can afford to avoid  
taxes will try to avoid them**

Preferences,  
constraints, and tradeoffs



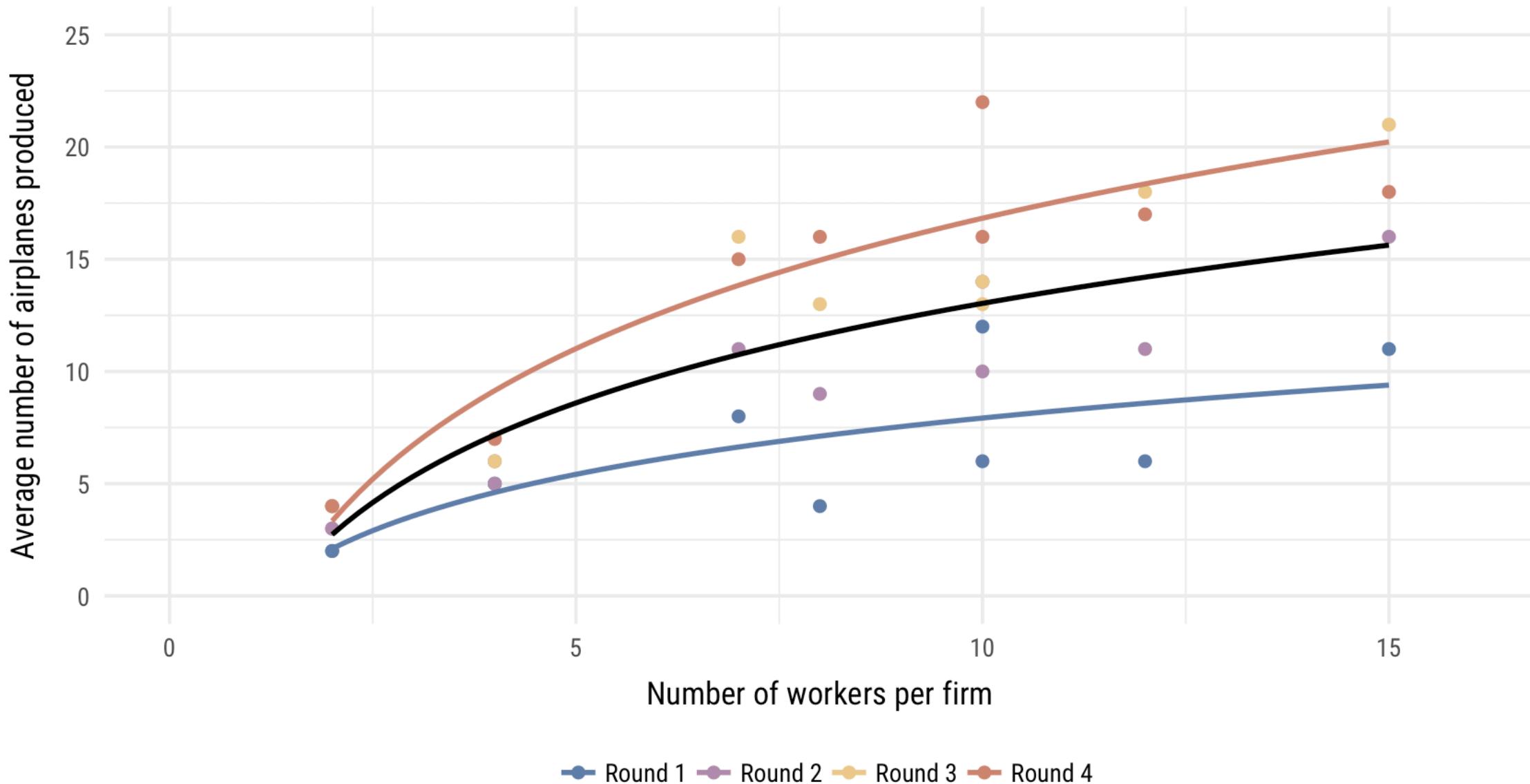
# Average number of airplanes produced by 10 firms

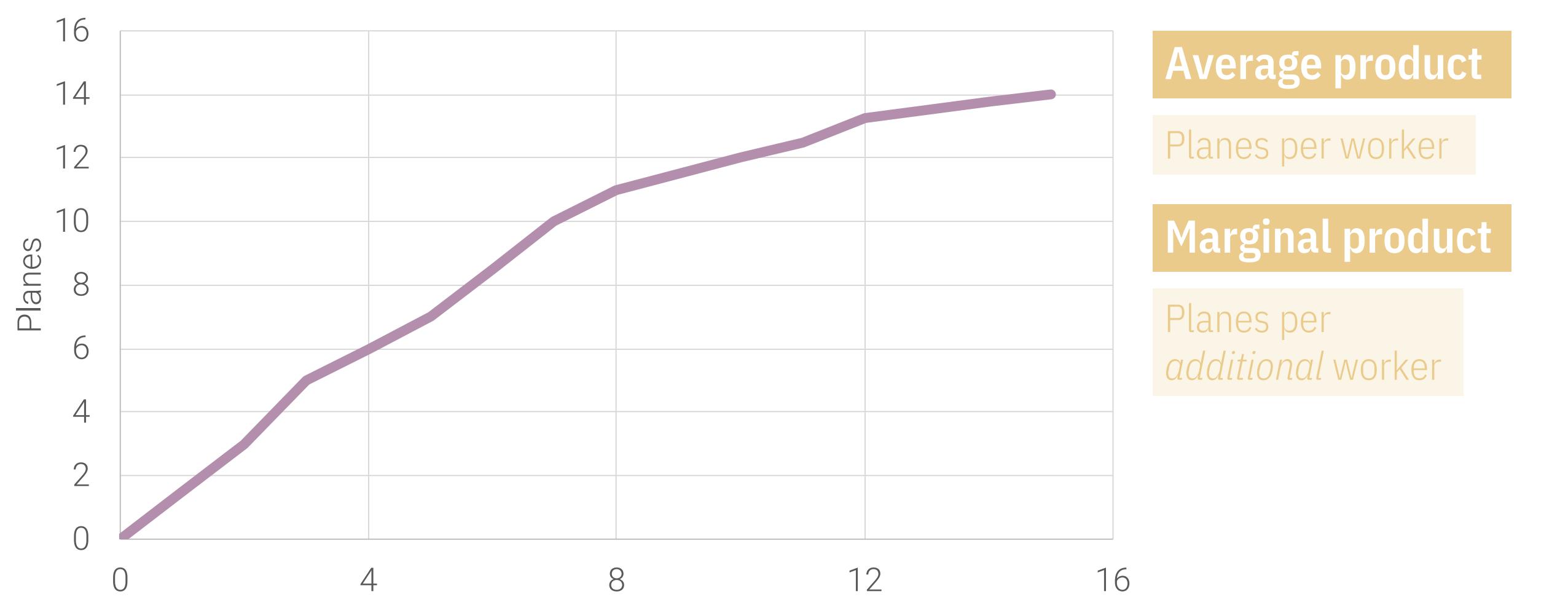
Averaged over 4 rounds; firms varied in size



# Number of airplanes produced by 10 firms

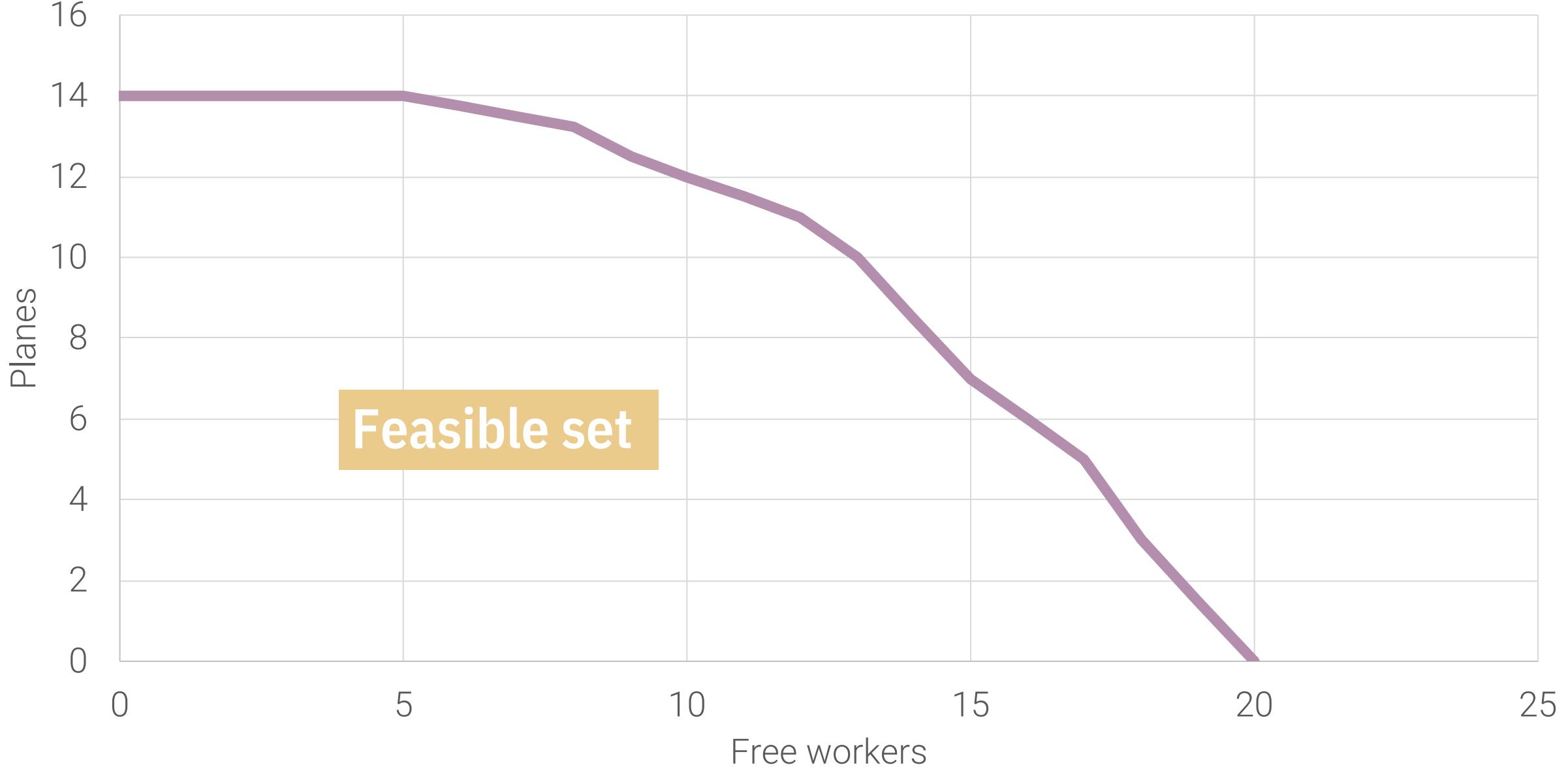
Firms varied in size

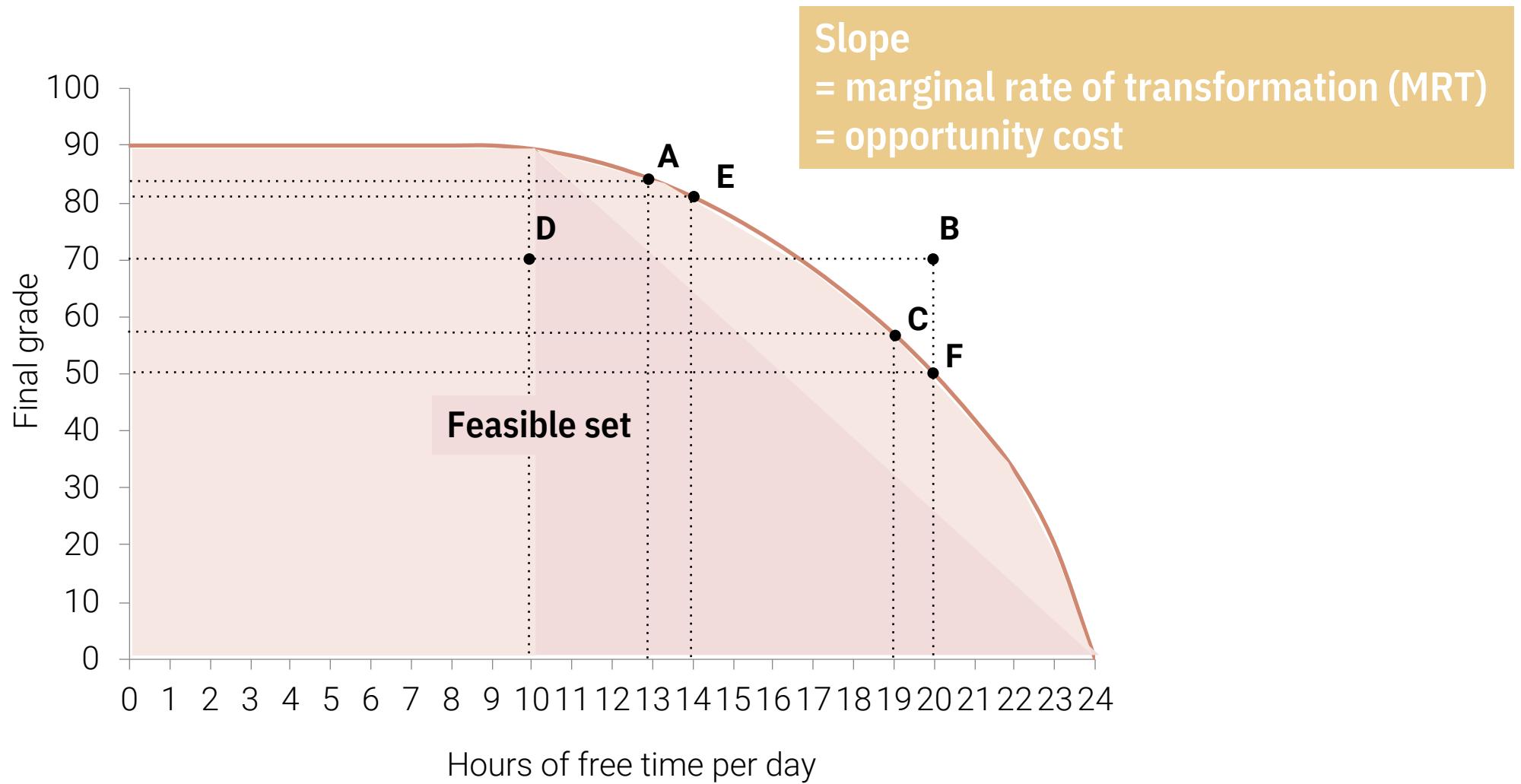




Workers	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
Planes	0	1.5	3	5	6	7	8.5	10	11	11.5	12	12.5	13.25	13.5	13.75	14

Does marginal product  
always diminish?





	A	E	C	F
Free time	13	14	19	20
Grade	84	81	57	50
Opportunity cost		3		7

WHY ARE YOU GOING HERE?  
GAS IS TEN CENTS A GALLON CHEAPER AT  
THE STATION FIVE MINUTES THAT WAY.



IF YOU SPEND NINE MINUTES OF YOUR  
TIME TO SAVE A DOLLAR, YOU'RE WORKING  
FOR LESS THAN MINIMUM WAGE.

# Opportunity cost

The value of the thing you can't  
do because of a decision

The value of the forgone option



# Opportunity cost

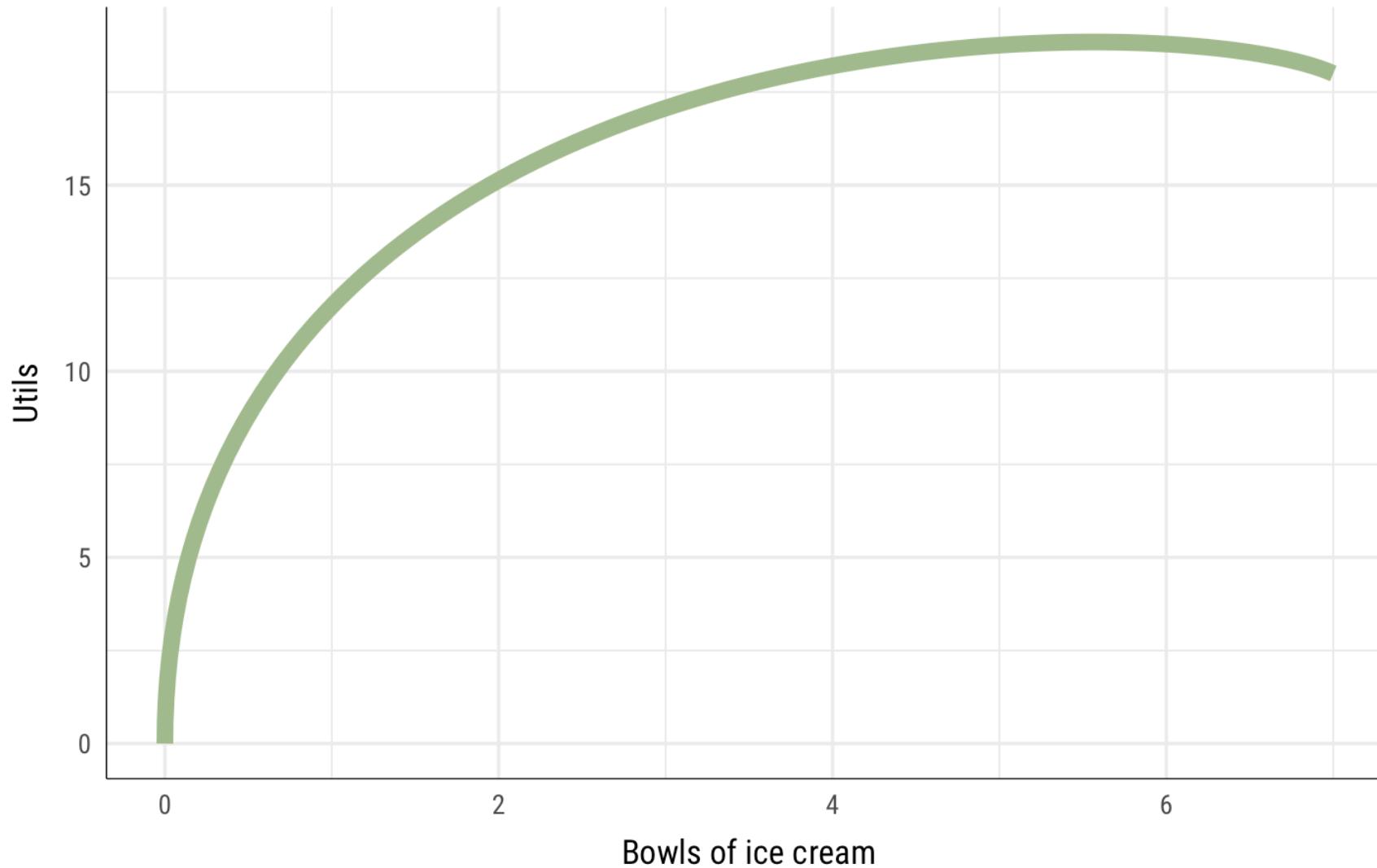
Cost for theater concert	\$25	
Value of park concert to you	\$15	
Economic cost of theater	\$40	
Value of theater concert to you	\$50	\$35
Your choice	Theater	Park

# Utility

## Happiness points



# Diminishing marginal utility



# Utility and indifference

# Utility bundles

Theoretical combination of goods  
that provide same level of utility

$$u(x_1, x_2)$$

$$u(x_1, x_2) = x_1 x_2$$

# Utility bundles

$$u(x_1, x_2) = x_1 x_2$$

$$u(1, 2)$$
 2

$$u(100, 3)$$
 300

$$u(4, 1)$$
 4

# Utility bundles

$$u = xy$$

x and y give same utility

$$u = \sqrt{xy}$$

x and y give same utility

$$u = x^2y^2$$

x and y give same utility

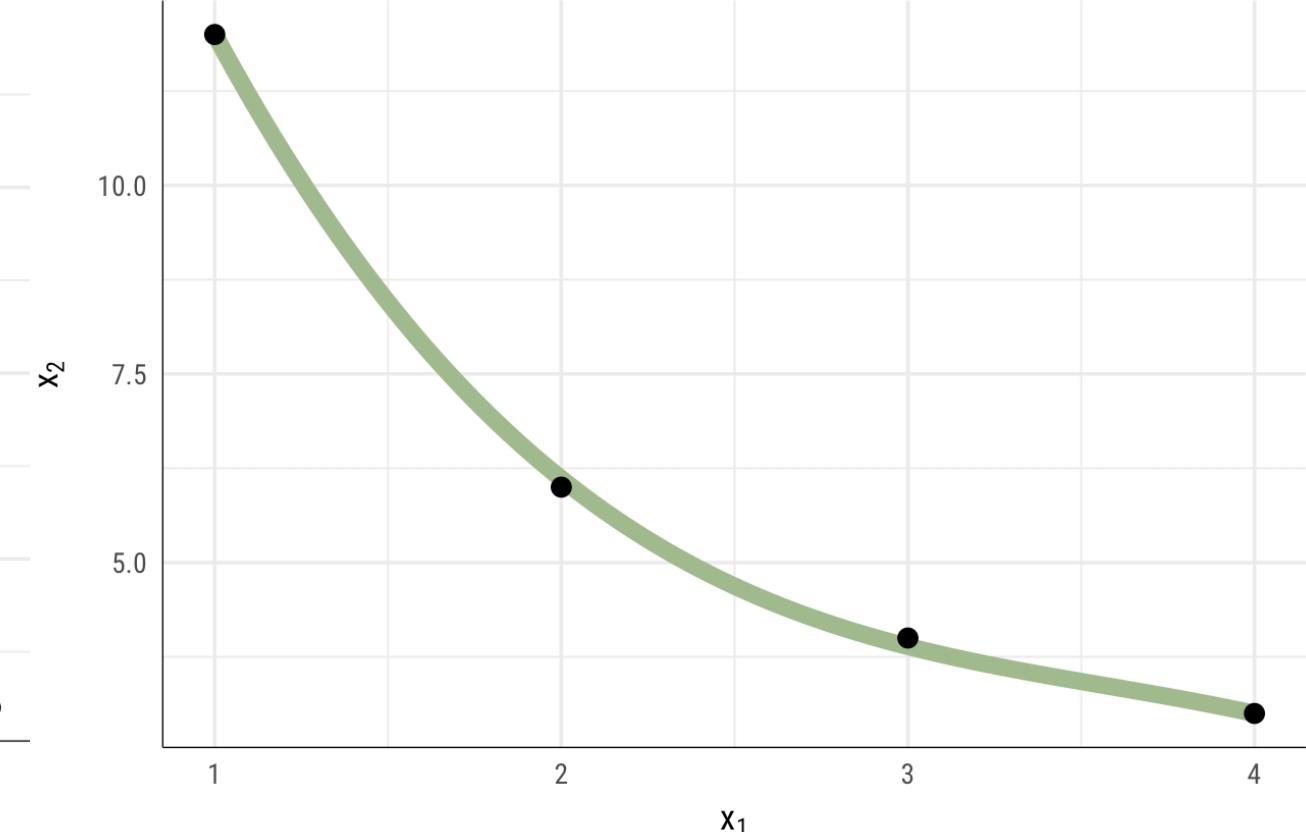
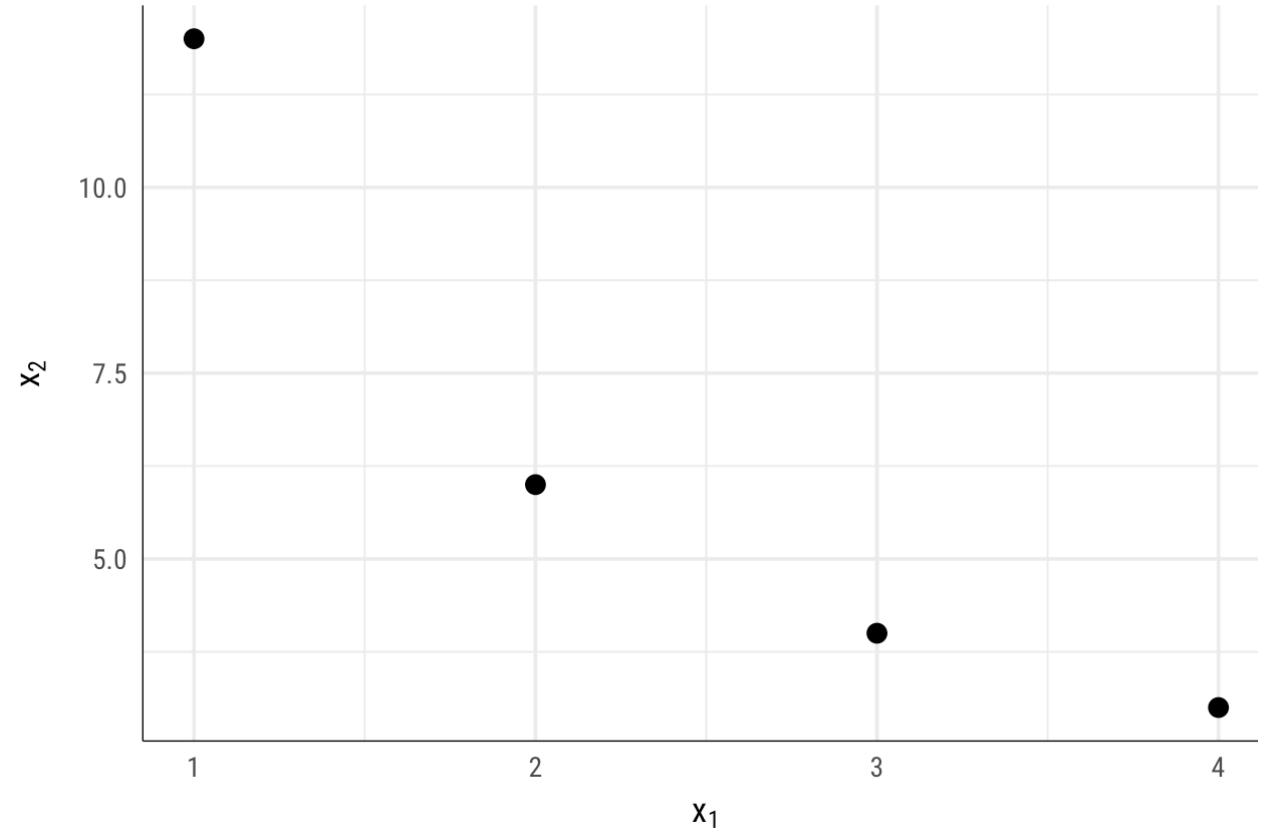
$$u = x^2y$$

x gives more utility than y

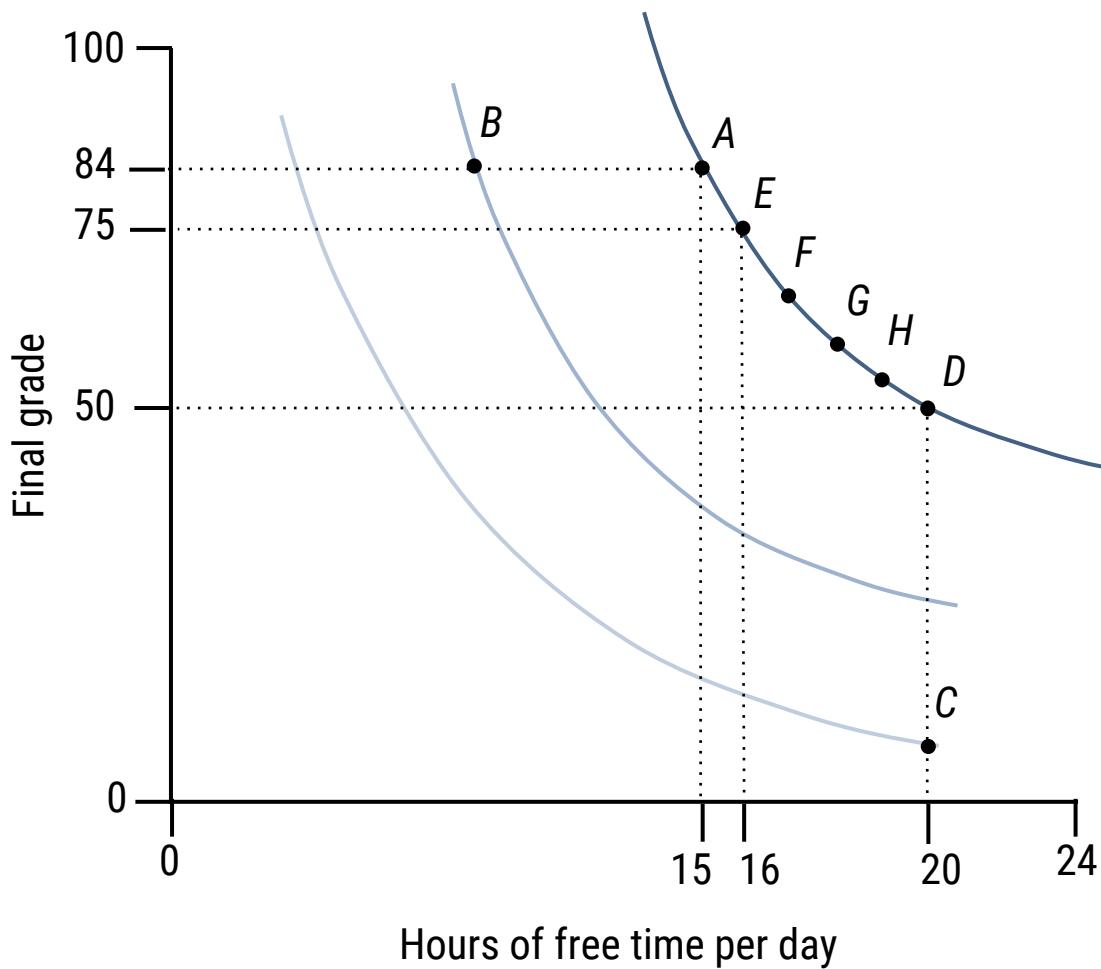
What combinations of inputs will produce 12 utils?

$$u(x_1, x_2) = x_1 x_2$$

$$u(x_1, x_2) = x_1 x_2$$



# Indifference curves



# Indifference curves

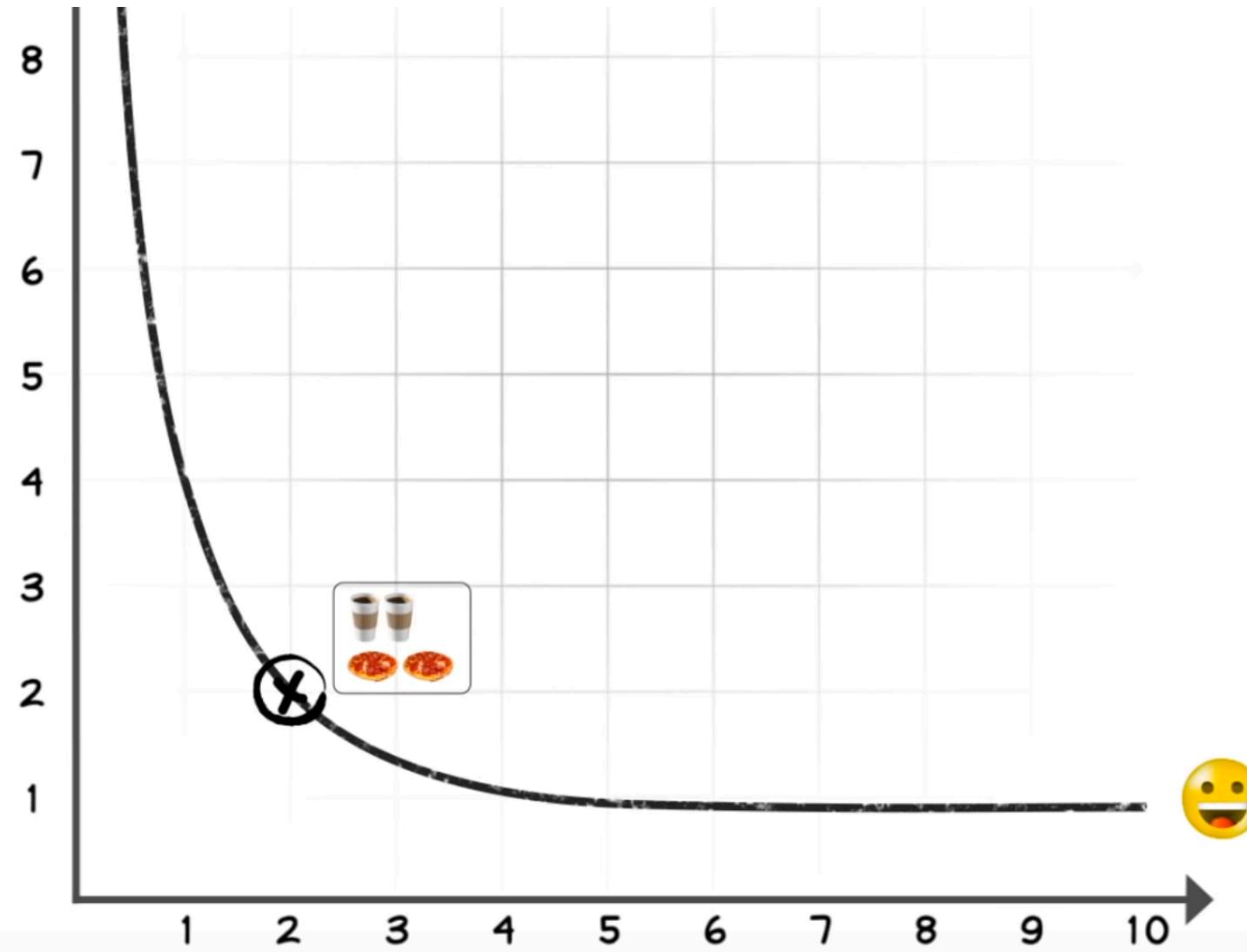
Theoretical points where we're  
equally happy with a mix of goods

Measured in utility  
(or “utils”, or happiness points)

Higher curves = more utils



CUPS OF  
COFFEE  
PER WEEK



# OF PIZZAS PER WEEK

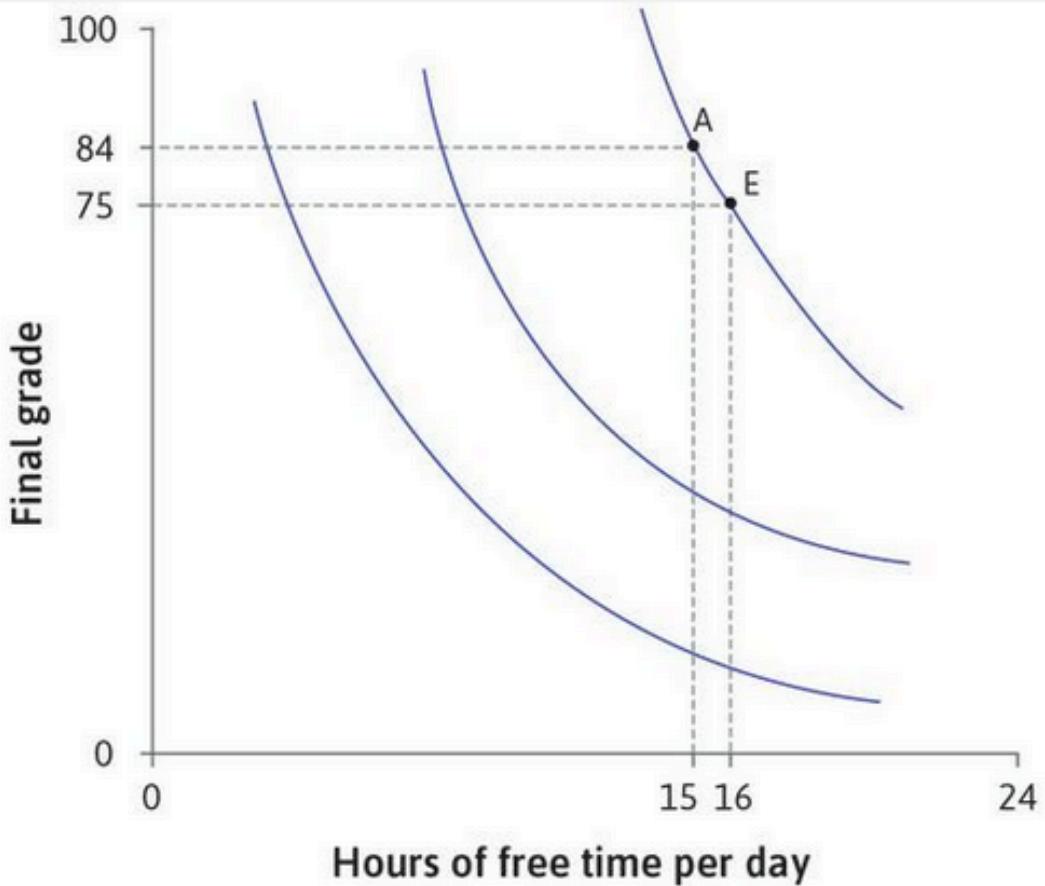


2:51 / 8:27

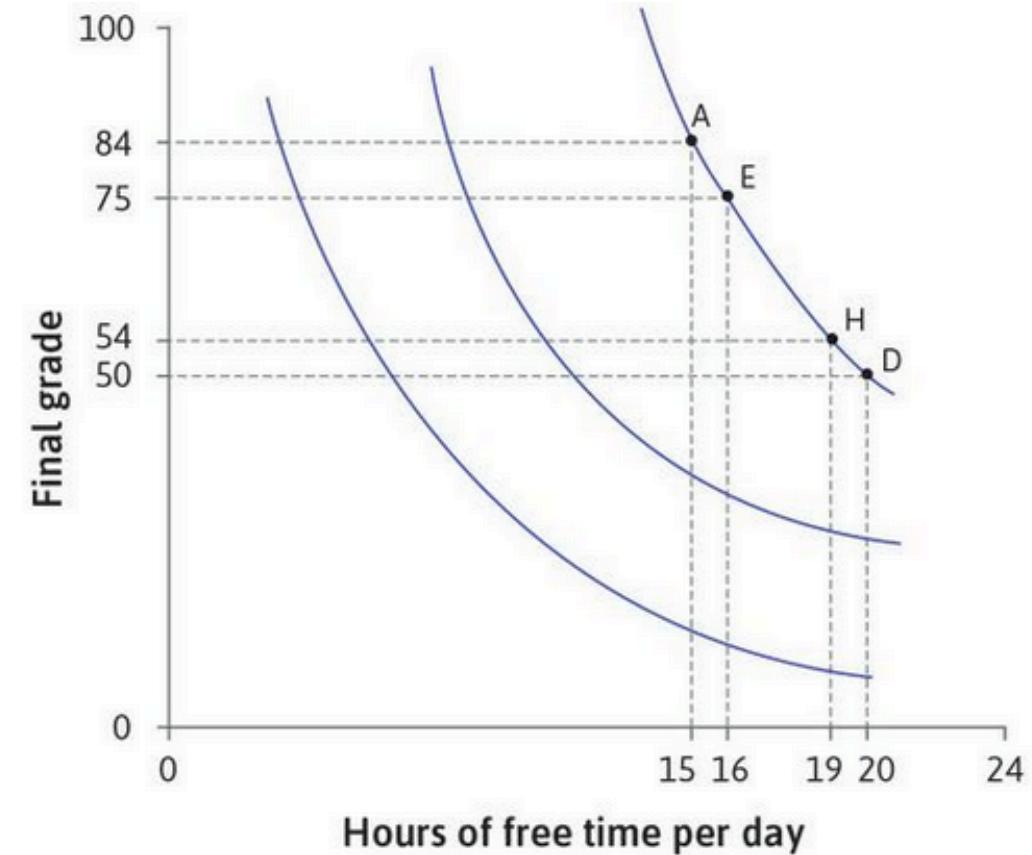
<https://www.youtube.com/watch?v=iOmDo5jLfw8>



# Slope of indifference curve = marginal rate of substitution (MRS)



MRS at A = 9



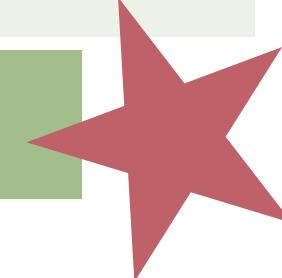
MRS at H = 4

# Calculus party!!!

# Two reasons for calculus

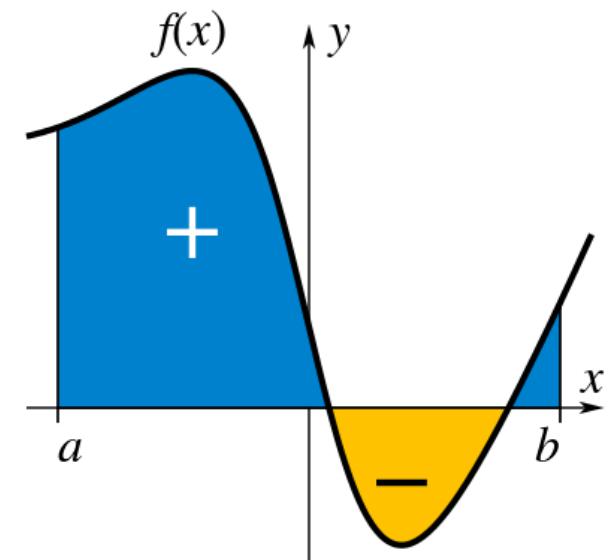
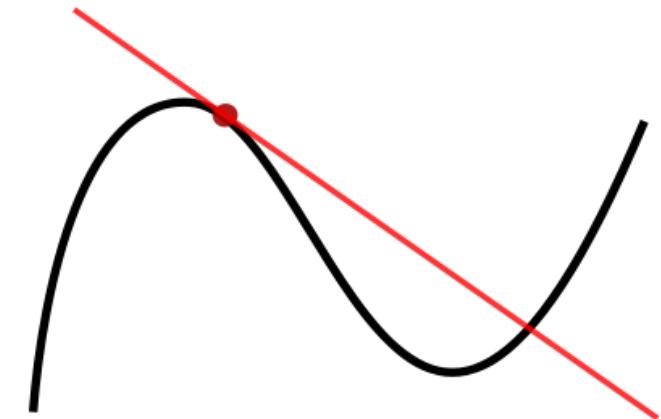
Find the slope of a line

Differential calculus



Find the area under a line

Integral calculus



# Drawing lines with math

$$y = mx + b$$

y

A number

x

A number

m

Slope

$\frac{\text{rise}}{\text{run}}$

b

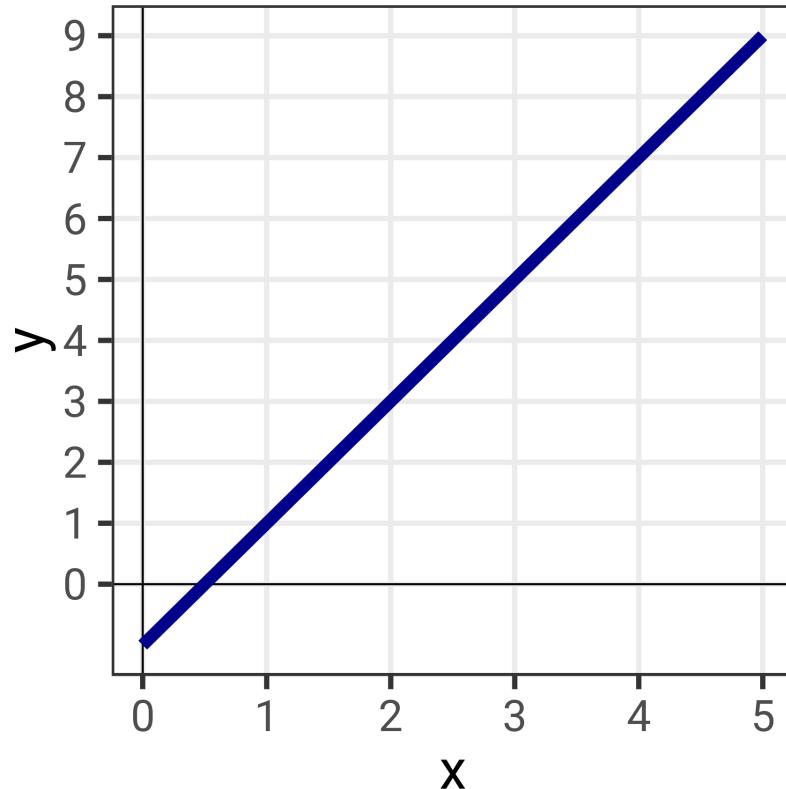
y intercept

# Slope

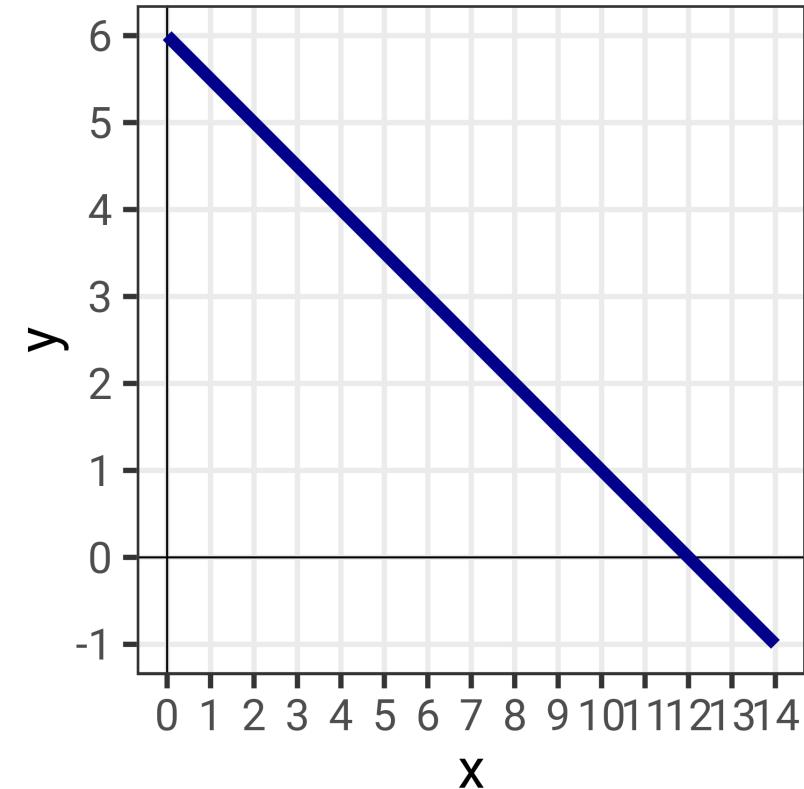
Slope = rise/run =  
how y changes  
as you change x

# Slopes and intercepts

$$y = 2x - 1$$



$$y = -0.5x + 6$$



# Graph these

desmos.com

$$y = 5x + 2$$

$$y = x - 1$$

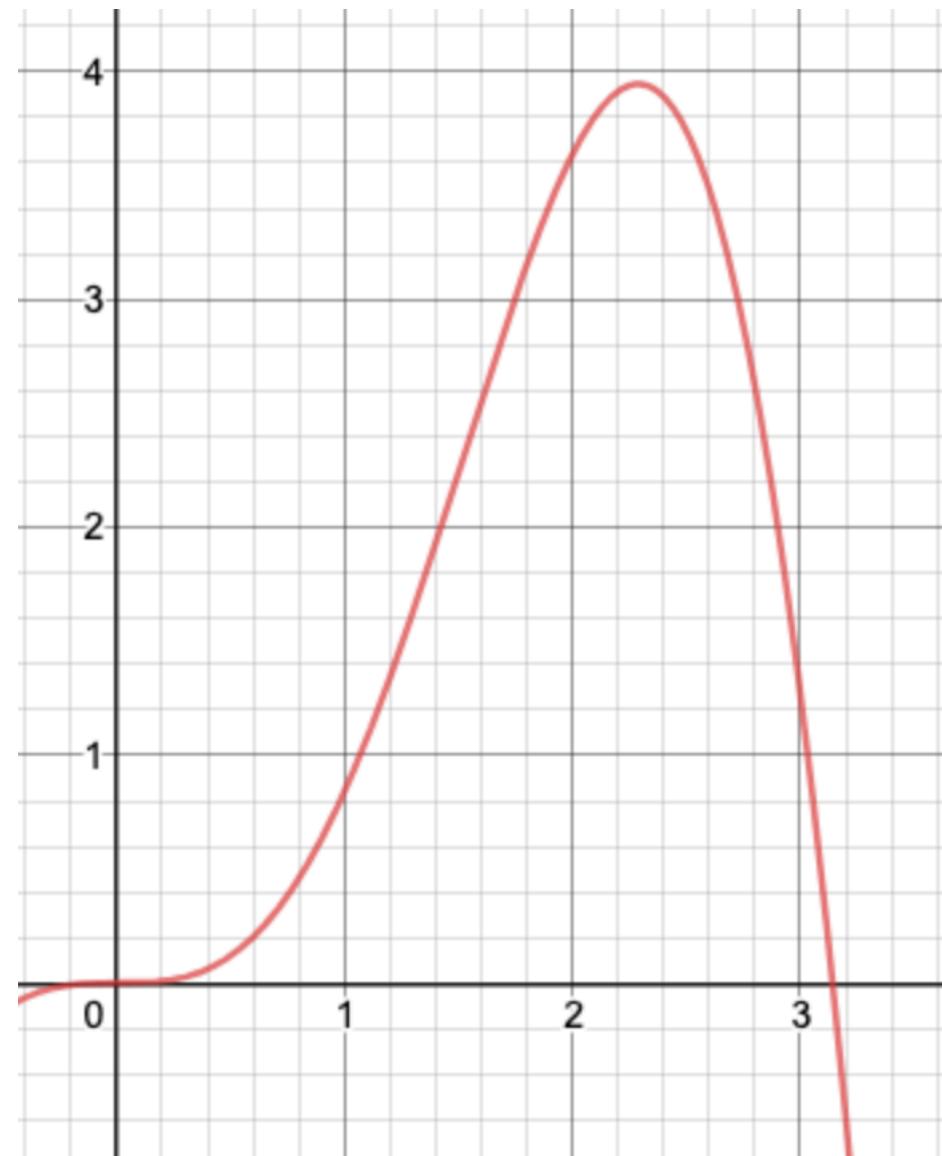
$$y = -2x + 11$$

$$y = 6 - 2x$$

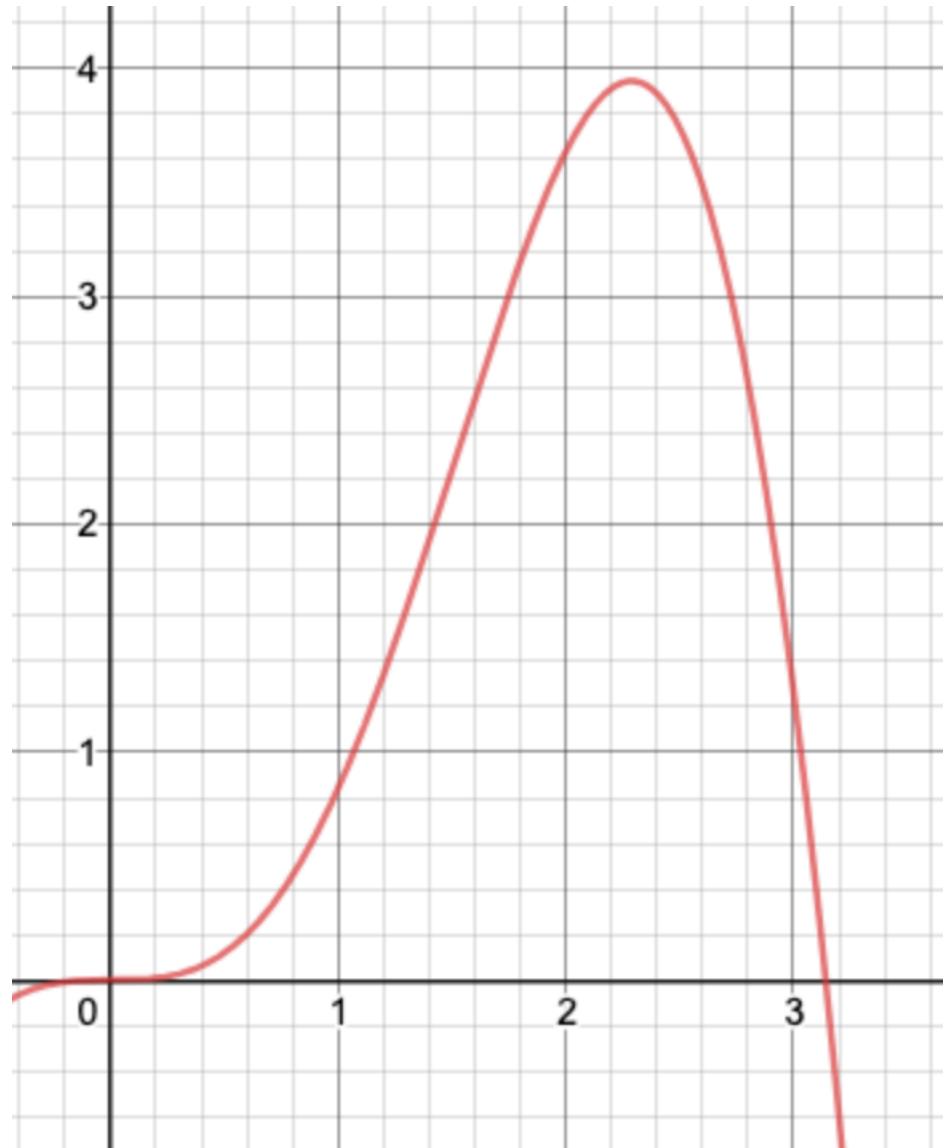
$$y = 0.33x - 1$$

$$y = 0.75x - 3$$

# What about curvy lines?



# No single slope!

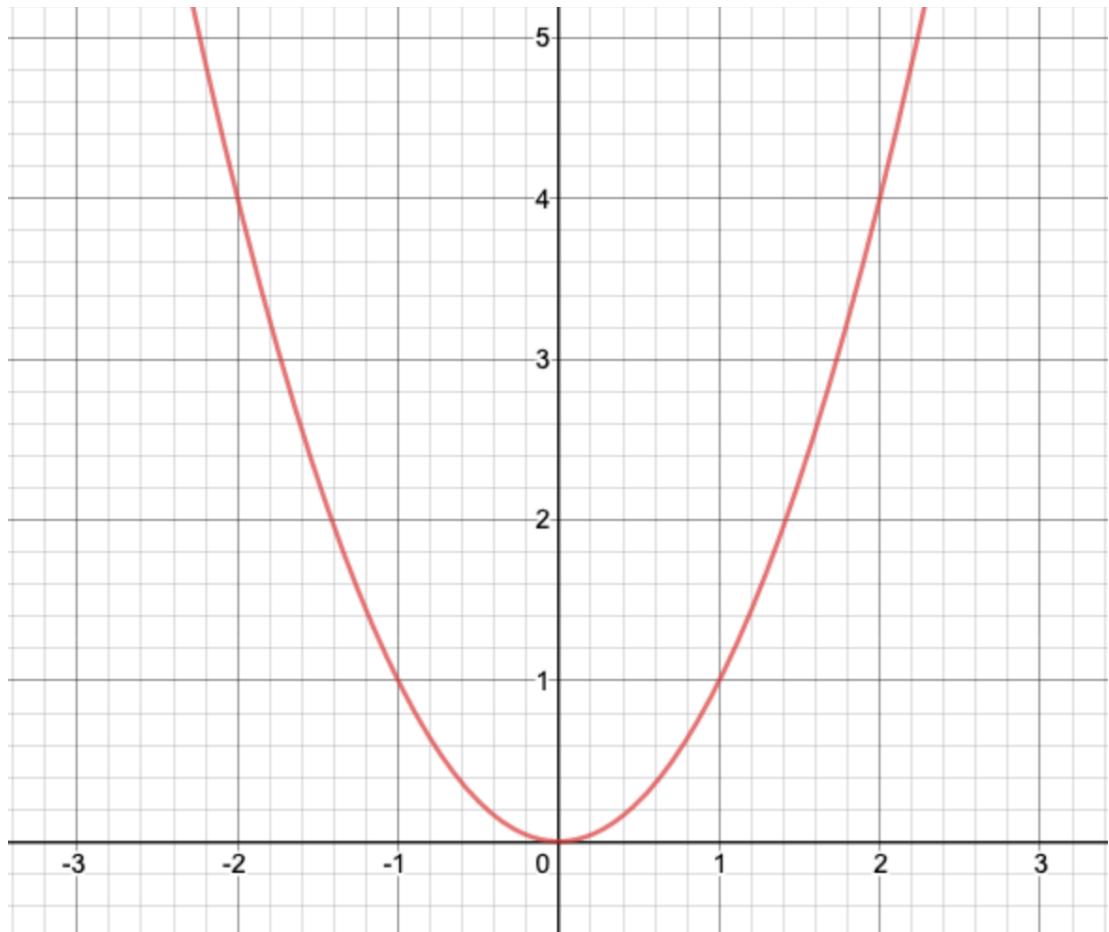


Slope is different  
at every  $x$

Slope will be a  
*formula*, not a  
single number

Derivative

# Basic derivatives



$$y = x^2$$

**Power rule**

Move exponent down to  
coefficient, reduce  
exponent by 1

$$y' = 2x$$

$$y = 3x^3 - 4x^2 + 6x - 1$$

$$y' = 9x^2 - 8x^1 + 6$$

$$y = 5x + 2$$

$$y' = 5$$

# Your turn

$$y = 3x^2 - 4x + 8$$

$$y = -2x^4 - 2x + 100$$

$$y = 7x + 2$$

wolframalpha.com  
"derivative 3x^2 - 4x + 8"

# Partial derivatives

**Power rule only  
works with 1 variable**

$$u = xy$$

That means you can't figure  
out the derivative here!  
It has  $x$  and  $y$ .

# Partial derivatives

Do the x part first,  
then do the y part

x part / y part

$$u = xy \quad u' = \frac{y}{x}$$

# Maximizing utility

# Marginal rate of substitution (MRS)

**Theoretical** tradeoff between inputs

Slope of indifference curve

$$MRS = \frac{dy}{dx} = \frac{\Delta y}{\Delta x} = \frac{P_x}{P_y} = \frac{MU_x}{MU_y} = \frac{\partial u/\partial x}{\partial u/\partial y}$$

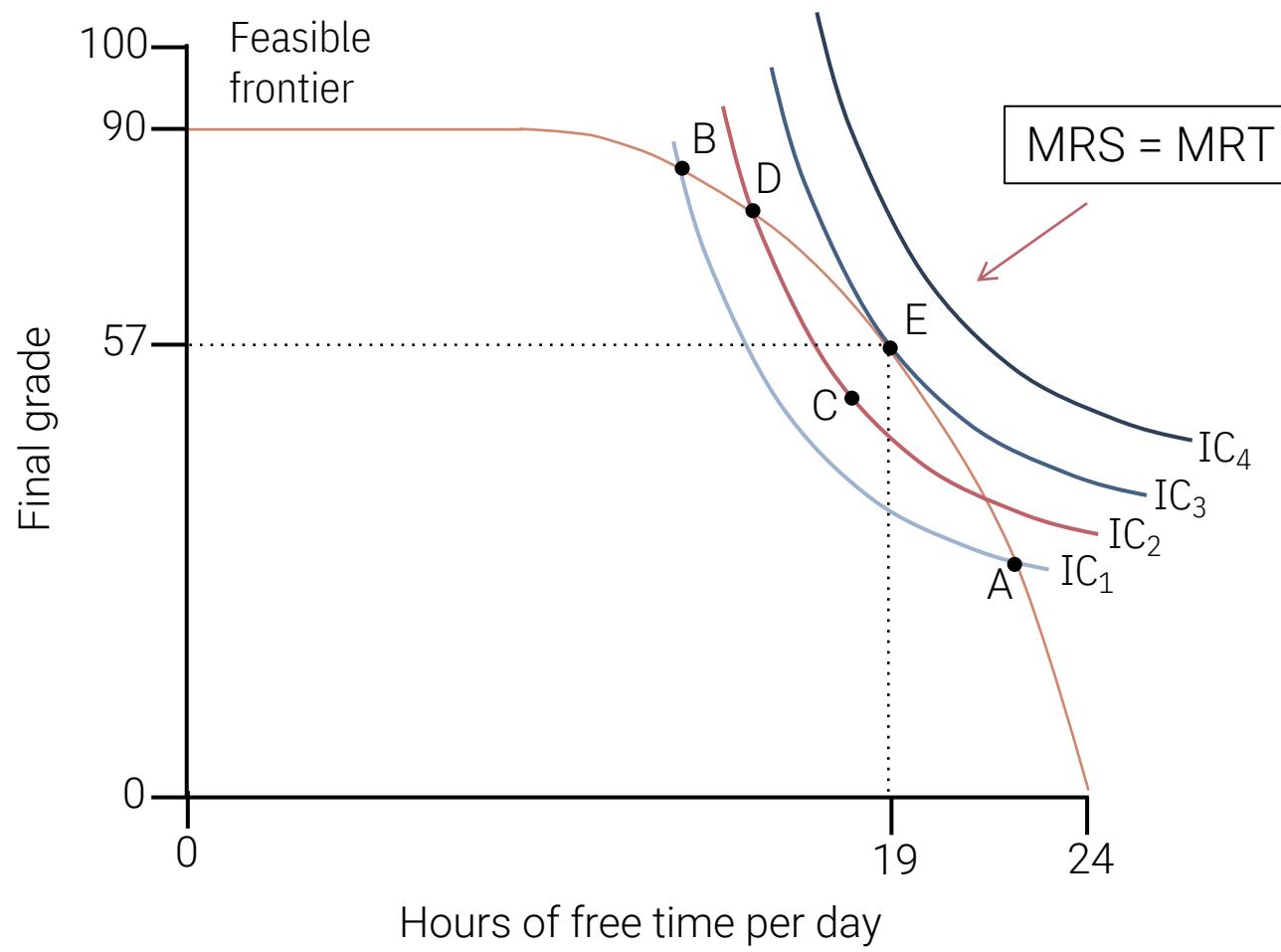
# Marginal rate of transformation (MRT)

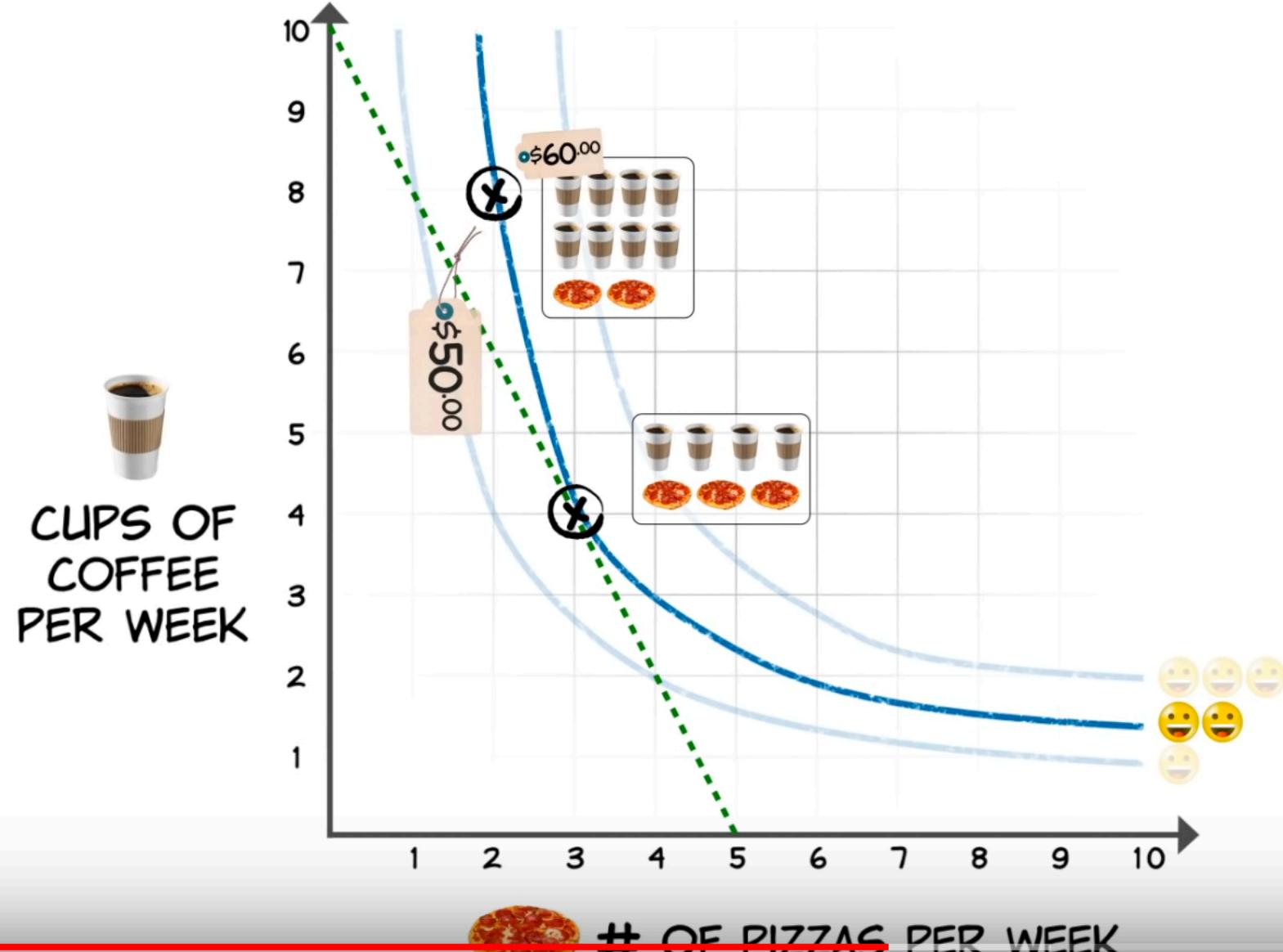
**Actual** tradeoff between inputs  
constrained by feasible frontier

Slope of feasible frontier

**What's the best combination of  
hours studied / free time?**

**Where the ideal meets reality!**





A set of small, light-gray navigation icons typically found in video player software like VLC. From left to right, they include: a left arrow, a right arrow, a double left arrow, a double right arrow, a volume icon, and a full-screen icon.

<https://www.youtube.com/watch?v=MXIgp-P-FeY>



# Utility maximization

0. Plot indifference curve

1. Figure out feasible set or MRT  
(budget line)

2. Use calculus and prices to  
figure out ideal MRS  
( $\Delta y / \Delta x = \text{price } x / \text{price } y = MUX / MUy$ )

3. MRT = MRS and solve for x and y

Waffles (x)

\$1

Calzones (y)

\$2

Utility

$u = xy$

Budget

\$20