Blocking

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Then what?



Covariate balance

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- Estimate closer to truth

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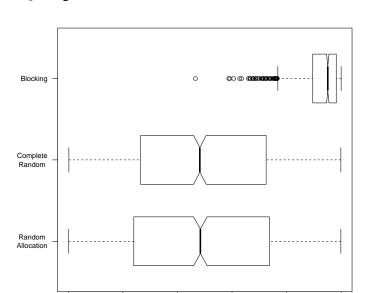
- Covariate balance
- Estimate closer to truth
- ► Increased efficiency
- ➤ Triply-robust estimates: block, randomize, adjust
- ▶ Block-level effects
 - \rightarrow different actors interested in different effects
- ▶ Guidelines for limited/uncertain resources

Why Block: Balance

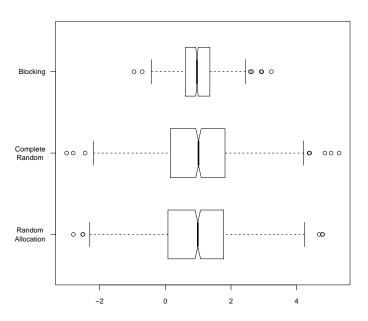
Simulation study: 100 units, $X_1 \sim N(0,1)$, $X_2 \sim \text{Unif}(0,1)$, $X_3 \sim \chi_2^2$; 1000 such experiments. Assg treatmnt in 3 ways.

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Why Block: Efficiency

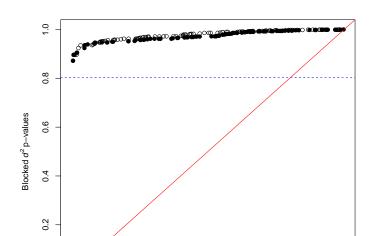


Blocking in Applications: Balance and Efficiency

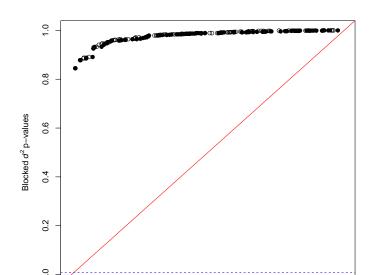
Moore (2012): Perry Preschool Experiment

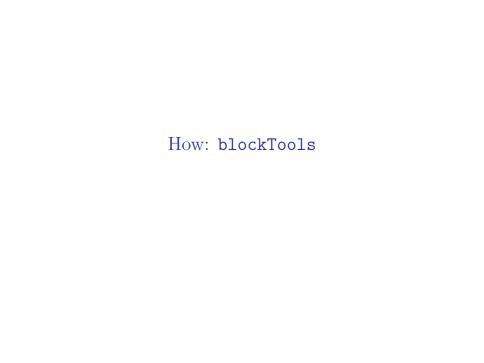
Left: QQ plot of balance (100 blocked vs. unblocked)

Right: Est TE under sharp null (100 blocked vs. unblocked)



Balance in Applications: Balance and Efficiency Considering more variables ...





Start with some sample data:

```
library(blockTools)
data(x100)

x100 |> head()
```

```
id id2 b1 b2 g ig
1 1001 101 156 795 b 729
2 1002 102 813 469 a 627
3 1003 103 950 978 a 959
4 1004 104 991 781 a 661
5 1005 105 613 759 a 819
6 1006 106 654 838 b 643
```

(Moore 2012; Moore and Schnakenberg 2023)

```
bl <- b$blocks$`1`
bl |> head()
```

```
Unit 1 Unit 2 Distance

1 1043 1040 0.01240000

2 1100 1020 0.02259275

3 1065 1027 0.02912651

4 1085 1081 0.03498815

5 1088 1061 0.04789253

6 1064 1014 0.07985116
```

Why all this?

```
bl <- b$blocks$`1`</pre>
```

We are extracting just the blocked pairs themselves.

▶ Why b\$blocks? Since b has 3 components:

names(b)

```
[1] "blocks" "level.two" "call"
```

▶ Why blocks\$1'? Since this is (default-named) first (and only) "group":

```
names(b$blocks)
```

```
[1] "1"
```

What else could we do?

```
b_3groups_3conditions <- block(</pre>
 x100,
 groups = "g",
                                 # (Factor variable in data)
 n.tr = 3,
 id.vars = "id",
 block.vars = c("b1", "b2"),
 distance = "mve"
```

```
b_3groups_3conditions$blocks
```

1010

2 3

1 O E O

```
$a
  Unit 1 Unit 2 Unit 3 Max Distance
1
    1076
           1039 1056 0.2509889
```

1065 1061 1002 0.4335040

1084 1058 1017 0.4373315

1 0 0 1

0 4E04767

Some rows from each "group":

```
rows_a <- b_3groups_3conditions$blocks$a |> slice(1:2) |> mutate
rows_b <- b_3groups_3conditions$blocks$b |> slice(1:2) |> mutate
rows_c <- b_3groups_3conditions$blocks$c |> slice(1:2) |> mutate
bind_rows(rows_a, rows_b, rows_c)
```

```
Unit 1 Unit 2 Unit 3 Max Distance group
   1076
         1039
              1056
                     0.2509889
                                а
2
   1065 1061 1002 0.4335040 a
   1043 1040 1019 0.1664608
3
                                b
4
   1048 1031 1062 0.2288718
                                h
5
   1095 1092 1049 0.3778655
                                С
6
   1045
         1015 1082
                     0.3808569
                                C.
```

Other arguments to block()

- vcov.data
- **proups:** for exact-blocks
- n.tr
- id.vars
- block.vars
- algorithm: optGreedy, optimal, naiveGreedy, randGreedy, sortGreedy
- \blacktriangleright distance: mahalanobis, mcd, mve, euclidean, $k \times k$ matx
- weight
- ▶ level.two: block states by most similar cities
- valid.var, valid.range: Goldilocks
- seed.dist: (for mcd and mve)

Assign

```
a <- assignment(b, seed = 71573706)
a</pre>
```

Assignments:

	Treatment 1	Treatment 2	Distance
1	1040	1043	0.01240000
2	1100	1020	0.02259275
3	1065	1027	0.02912651
4	1081	1085	0.03498815
5	1088	1061	0.04789253
6	1014	1064	0.07985116
7	1032	1070	0.08279625
8	1097	1098	0.08882421
9	1038	1018	0.09316331
10	1031	1048	0.10391953
11	1084	1058	0.10835825

Get Assignments

```
a |> extract conditions(x100, id.var = "id")
 [1] 2 1 2 2 2 2 1 2 2 1 1 1 1 1 1 1 1 2 2 1 2 2 2 1 2 1 1 1
 [38] 1 1 1 2 2 2 2 2 2 2 1 2 1 2 2 2 2 1 1 2 1 2 1 2 2 1 3
 x100 |> mutate(
 condition = extract conditions(a, x100, id.var = "id"))
     id id2 b1 b2 g ig condition
   1001 101 156 795 b 729
   1002 102 813 469 a 627
   1003 103 950 978 a 959
3
4
   1004 104 991 781 a 661
5
   1005 105 613 759 a 819
   1006 106 654 838 b 643
6
   1007 107 640 645 c 12
8
   1008 108 681 404 a 221
```

Assign 3 Conditions, within Groups

```
a3 <- assignment(b_3groups_3conditions, seed = 979677744)
```

Assignments:

```
Group: a
    Treatment 1
                   Treatment 2
                                 Treatment 3
                                                Max Distance
    1056
                   1076
                                 1039
                                                0.2509889
2
    1002
                   1061
                                 1065
                                                0.4335040
3
    1058
                   1084
                                 1017
                                                0.4373315
4
    1046
                   1081
                                 1059
                                                0.4524767
5
    1073
                   1098
                                 1029
                                                0.4599752
6
    1060
                   1067
                                 1004
                                                0.5921446
    1089
                   1024
                                 1032
                                                0.7554402
8
    1052
                   1054
                                 1030
                                                0.8848444
9
    1093
                   1026
                                 1068
                                                0.8975495
10
    1036
                   1008
                                 1091
                                                1.3586913
```



Blocking with randomizr::block_ra()

1006 106 654 838 b 643 1 1007 107 640 645 c 12 1 1008 108 681 404 a 221 0

823 b 321

1009 109 530

6

8 9

```
library(randomizr)
tr <- block_ra(x100$g)
# Better:
x100 \mid > mutate(tr = block ra(x100$g))
      id id2 b1 b2 g ig tr
1
    1001 101 156 795 b 729 1
    1002 102 813 469 a 627 1
3
    1003 103 950 978 a 959 1
    1004 104 991 781 a 661 1
4
5
    1005 105 613 759 a 819 0
```



blockTools: diagnose, get block IDs, check balance

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Diagnose:

Get block IDs

```
createBlockIDs(a, data = x100, id.var = "id")
```

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Diagnose:

Get block IDs

```
createBlockIDs(a, data = x100, id.var = "id")
```

Get balance:

```
assg2xBalance(a, x100, id.var = "id",
bal.vars = c("b1", "b2"))
```

▶ Generally, use Lin or Blocked Diff-in-Means

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$$p_j(1-p_j)n_j$$

where

- $\triangleright p_i = \text{share of block } j \text{ treated}$
- $n_j = \text{size of block } j$
- $(\text{I.e., } p_j(1 p_j) = \text{var}(TE) \text{ in block } j)$

Can I just ignore blocks and pool?

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ightharpoonup If p_j varies, no

Thanks!

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References I

- Moore, Ryan T. 2012. "Multivariate Continuous Blocking to Improve Political Science Experiments." *Political Analysis* 20 (4): 460–79. https://doi.org/10.1093/pan/mps025.
- Moore, Ryan T., and Keith Schnakenberg. 2023. blockTools: Blocking, Assignment, and Diagnosing Interference in Randomized Experiments. http://www.ryantmoore.org/html/software.blockTools.html.