### Comments on Fu & Green, Clark & Estes

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- ▶ Practical concern (?): RI with SEM

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#### Connection to "sparse potential outcomes":

Interference (Rosenbaum 2007)

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(Path figures helpful here!)

#### References I

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