

Exercises in Bayesian Modeling and Machine Learning

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Set Up

```
library(here)
library(tidyverse)

# Bayes:
library(coda)
library(MCMCpack)

# LASSO, ridge, elastic net:
library(glmnet)

# tidymodels:
library(tidymodels)
```

Scan the available Bayesian models in `MCMCpack` with `help(package = "MCMCpack")`.

Next, prepare the data. We'll do some usually-unnecessary mutations just to facilitate the way `glmnet` expects the data (it doesn't adopt the typical $y \sim x$ formula specification). We could do this through a `recipe()`, as well.

```
# Set random seed, so that samples, train-test sets consistent:
set.seed(233559574)
```

We load, mutate, and sample from the data:

```
social <- read_csv("http://j.mp/2Et71U0")

social <- social |> mutate(age = 2006 - yearofbirth,
  isFemale = (sex == "female"),
  isFemale = as.numeric(isFemale),
  sentNeighbors = (messages == "Neighbors"),
  sentNeighbors = as.numeric(sentNeighbors))

social <- social |> sample_n(50000)
```

Estimate Bayesian logistic regression

For practice, estimate the simple Bayesian logistic regression (with Gaussian priors on the β 's):

```
mc_post <- MCMClogit(primary2006 ~ messages, data = social)
```

Look at the summary of `mc_post`.

Now, estimate a fuller Bayesian logistic regression, modeling `primary2006` as function of `primary2004`, `age`, `age2`, and `messages`. The algorithm is a Metropolis one, similar to the “full conditional probability distribution” Gibbs sampling. Set the MCMC burnin to 500, the number of MCMC draws to 2000, with a thinning value of 2. Store output as `mc_post_full`.

Look at summary of `mc_post_full`.

Examine the “highest posterior density” intervals for the coefficients. These are the 95% of values most common in the posterior. They may differ from the central credible interval.

```
HPDinterval(mc_post_full)
```

Create graphics to diagnose the MCMC. Careful – check where the plot will be stored. What working directory will your plot be produced from?

```
pdf("mcmc_diagnose.pdf")
plot(mc_post_full)
dev.off()
```

Do a posterior probability calculation from the posterior draws. Specifically, what’s the posterior probability the `Neighbors` postcard has a larger coefficient than the `Hawthorne` card?

```
mean(mc_post_full[, "messagesHawthorne"] < mc_post_full[, "messagesNeighbors"])
```

```
## [1] 1
```

Now, what’s the posterior probability that the `Neighbors` coefficient is greater than 0.7?

Estimate Machine Learning Models

Set up the data objects for `glmnet`. `X` will be a raw numeric matrix; `y` will be a raw numeric vector. (We can avoid much of this with the `tidyverse`.)

```
predictors <- c("isFemale", "primary2004", "sentNeighbors", "hhsz", "age")
X <- social[, predictors]
```

Next we’ll do some naive “feature engineering”. This might include polynomial functions of predictors, logarithmic and power transformations, deep interactions, or other transformations of predictors.

```
X <- X |> mutate(age2 = age^2,
                 age3 = age^3,
                 age4 = age^4,
                 age5 = age^5) |>
  as.matrix()

# Extract outcome as raw numeric vector, for glmnet:
y <- social[, "primary2006"] |> unlist() |> as.numeric()
```

Estimate the least squares (LS) model using all these predictors.

```
lm_out <- lm(primary2006 ~ isFemale + primary2004 + sentNeighbors + hhsz +
             age + I(age ^ 2) + I(age ^ 3) + I(age ^ 4) + I(age ^ 5),
             data = social)

coefs_lm <- coef(lm_out)
```

Examine your results. Next, estimate the LASSO:

```
lasso_out <- glmnet(X, y, alpha = 1)
```

Look at the `lasso_out` and `coef(lasso_out)` objects.

How should we choose among these sets of coefficients? We'll use cross-validation to see which predicts best in *out-of-sample* tests. `glmnet` automates creating many training data sets, estimating the LASSO, then seeing how well the trained coefficients do in held-out test data.

```
cv_lasso_out <- cv.glmnet(X, y, alpha = 1)
```

Now, show the coefficients of the “best” fit model, the one that gives the minimum deviance:

```
coef(cv_lasso_out, s = "lambda.min")
```

```
## 10 x 1 sparse Matrix of class "dgCMatrix"
##           lambda.min
## (Intercept) 9.282795e-02
## isFemale    -8.443326e-03
## primary2004 1.483147e-01
## sentNeighbors 7.287352e-02
## hhsz        -3.688179e-03
## age         4.286091e-04
## age2        6.636937e-05
## age3        1.057836e-07
## age4       -3.627766e-14
## age5       -8.639266e-11
```

Consider the coefficients of a more parsimonious model, one that has deviance within 1 SE of the minimum:

```
coef(cv_lasso_out, s = "lambda.1se")
```

```
## 10 x 1 sparse Matrix of class "dgCMatrix"
##           lambda.1se
## (Intercept) 0.099832733
## isFemale    .
## primary2004 0.128768845
## sentNeighbors 0.040204894
## hhsz        .
## age         0.003153443
## age2        .
## age3        .
## age4        .
## age5        .
```

```
coefs_lasso <- coef(cv_lasso_out, s = "lambda.1se")
```

Compare the model coefficients:

```
cbind(coefs_lasso, coefs_lm)
```

```
## 10 x 2 sparse Matrix of class "dgCMatrix"
##           lambda.1se      coefs_lm
## (Intercept) 0.099832733 -2.444646e+00
## isFemale    .          -8.056825e-03
## primary2004 0.128768845  1.463093e-01
## sentNeighbors 0.040204894  7.281984e-02
## hhsize      .          -1.151567e-03
## age         0.003153443  2.767556e-01
## age2        .          -1.111901e-02
## age3        .          2.127652e-04
## age4        .          -1.916426e-06
## age5        .          6.510128e-09
```