Concepts in Machine Learning
Winter Institute in Data Science

Ryan T. Moore

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Building Models

Modeling Helper Functions

Example: `mtcars`

Example: Social Pressure Experiment (`recipes`)

Regularization Methods: LASSO, ridge regression, elastic nets

Building Models

How do we build models?

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What are our goals?

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1. Generative modeling
2. Predictive modeling

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1. Generative modeling
2. Predictive modeling

Breiman (2001b)

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  (novel theory, prior theory, prior findings)
- Raw data
  ("data look nonlinear, so $\ldots + \beta x^2 + \ldots$")
- Specification searching
  (repeat modeling with same data)
- Training and testing
  (repeat modeling, different data)

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  (No omitted variable bias)

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Helpful?

- Affect outcome
- Confounders
- Pre-treatment only
- Avoid post-treatment
- “In-horizon”
- Test something “out-of-horizon”

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Helpful?

- Affect outcome
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- Pre-treatment only
- Avoid post-treatment
- "In-horizon"
- Test something "out-of-horizon"

(Sometimes it will depend on goals.)

What to include, when thousands of predictors?

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"Machine learning"

What to include, when thousands of predictors?

“Machine learning”

(but “machine learning” can mean different things.)

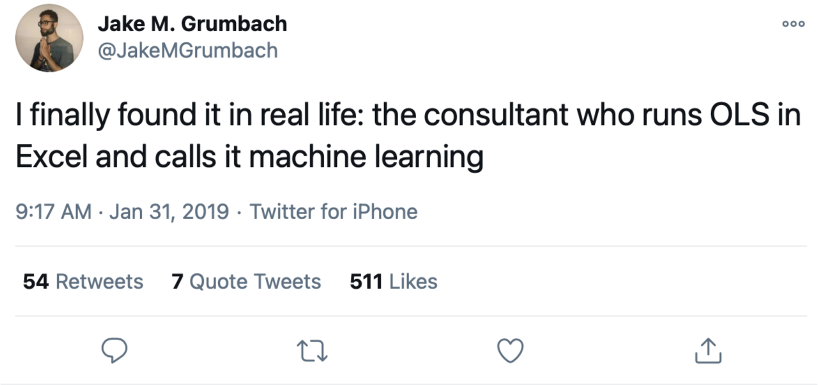


Figure 1: Don't do this.

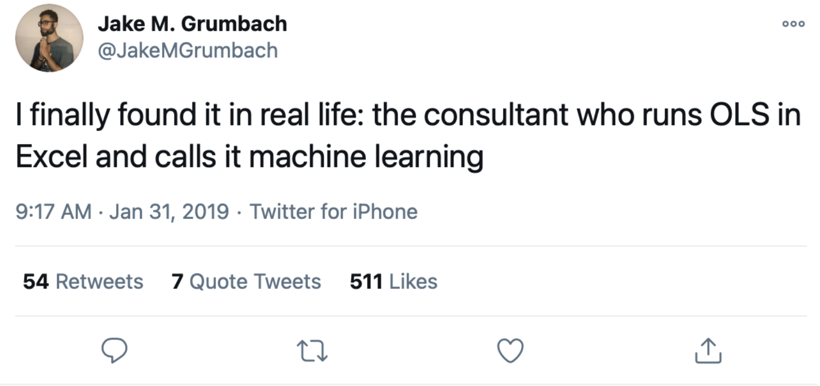


Figure 1: Don't do this.

If you can't describe the procedure's "learning", it may not be "machine learning".

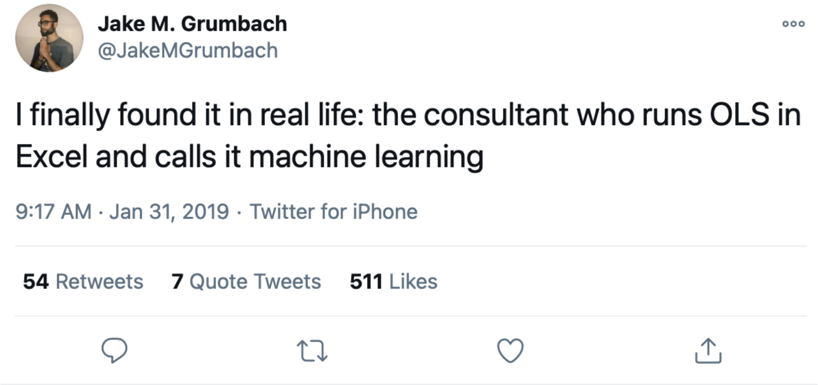


Figure 1: Don't do this.

If you can't describe the procedure's "learning", it may not be "machine learning".

There should probably be some testing/training, regularization, ...

Modeling Helper Functions

modelr Helper Functions

```r
data(sim1)

lm_out <- lm(y ~ x, data = sim1)

tidy(lm_out)
```

```
## # A tibble: 2 x 5
##   term        estimate std.error statistic  p.value
##   <chr>          <dbl>     <dbl>     <dbl>    <dbl>
## 1 (Intercept)     4.22     0.869      4.86 4.09e- 5
## 2 x               2.05     0.140     14.7  1.17e-14
```

modelr Helper Functions

```
glance(lm_out) |> select(1:5)
```

```
## # A tibble: 1 x 5
##   r.squared adj.r.squared sigma statistic  p.value
##       <dbl>         <dbl> <dbl>     <dbl>    <dbl>
## 1     0.885         0.880  2.20      215. 1.17e-14
```

```
glance(lm_out) |> select(6:12)
```

```
## # A tibble: 1 x 7
##      df logLik   AIC   BIC deviance df.residual  nobs
##   <dbl>  <dbl> <dbl> <dbl>    <dbl>       <int> <int>
## 1     1  -65.2  136.  141.     136.          28    30
```

`modelr` Helper Functions

Special `mutate()` functions:

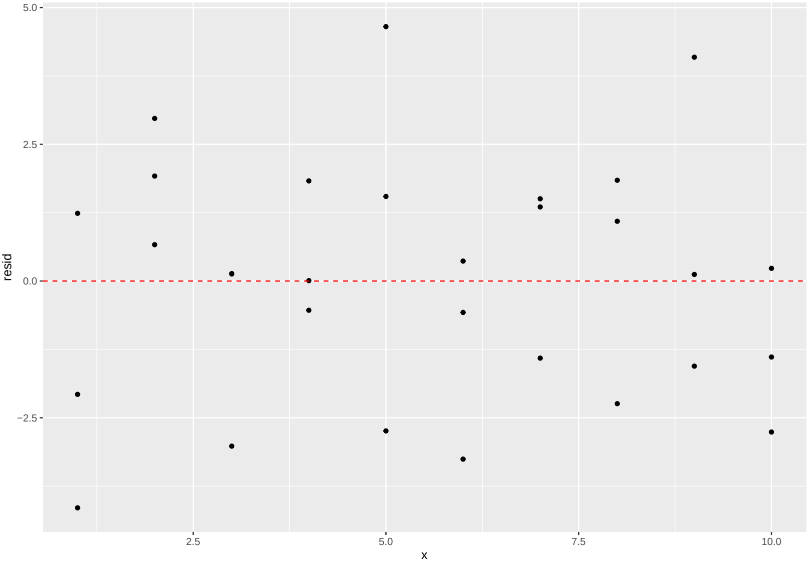
modelr Helper Functions

Special `mutate()` functions:

```
(sim1 <- sim1 |> add_residuals(lm_out))
```

```
## # A tibble: 30 x 3
##         x     y    resid
##     <int> <dbl>    <dbl>
##  1      1  4.20 -2.07
##  2      1  7.51  1.24
##  3      1  2.13 -4.15
##  4      2  8.99  0.665
##  5      2 10.2   1.92
##  6      2 11.3   2.97
##  7      3  7.36 -3.02
##  8      3 10.5   0.130
##  9      3 10.5   0.136
## 10      4 12.4   0.00763
## # i 20 more rows
```

```
ggplot(sim1, aes(x, resid)) + geom_point() +
  geom_hline(yintercept = 0, linetype = 2, color = "re
```



modelr Helper Functions

Special mutate() functions:

```
(sim1 <- sim1 |> add_predictions(lm_out))
```

```
## # A tibble: 30 x 4
##        x     y    resid  pred
##    <int> <dbl>    <dbl> <dbl>
##  1     1  4.20 -2.07     6.27
##  2     1  7.51  1.24     6.27
##  3     1  2.13 -4.15     6.27
##  4     2  8.99  0.665    8.32
##  5     2 10.2   1.92     8.32
##  6     2 11.3   2.97     8.32
##  7     3  7.36 -3.02    10.4
##  8     3 10.5   0.130   10.4
##  9     3 10.5   0.136   10.4
## 10     4 12.4   0.00763 12.4
## # i 20 more rows
```

modelr Helper Functions

```r
lm_out2 <- lm(y ~ x - 1, data = sim1)
```

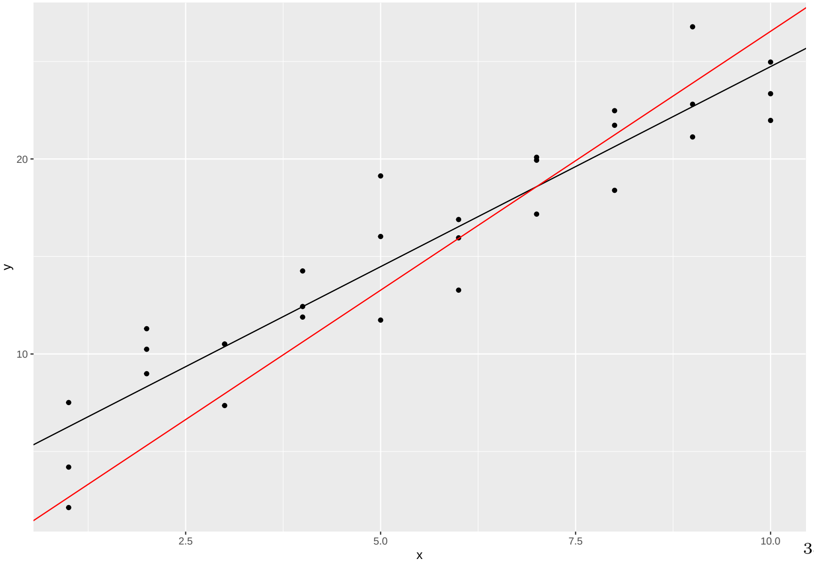
modelr Helper Functions

```r
lm_out2 <- lm(y ~ x - 1, data = sim1)
```

```r
coef(lm_out2)
```

```
##        x
## 2.654508
```

```
ggplot(sim1, aes(x, y)) + geom_point() +
  geom_abline(intercept = coef(lm_out)[1], slope = coef(lm_
  geom_abline(intercept = 0, slope = coef(lm_out2)["x"], co
```



```r
glance(lm_out)
```

```
## # A tibble: 1 x 12
##   r.squared adj.r.squared sigma statistic  p.value    df
##       <dbl>         <dbl> <dbl>     <dbl>    <dbl> <dbl>
## 1     0.885         0.880  2.20      215. 1.17e-14     1
## # i 3 more variables: deviance <dbl>, df.residual <int>,
```

```r
glance(lm_out2)
```

```
## # A tibble: 1 x 12
##   r.squared adj.r.squared sigma statistic  p.value    df
##       <dbl>         <dbl> <dbl>     <dbl>    <dbl> <dbl>
## 1     0.970         0.969  2.94      943. 1.15e-23     1
## # i 3 more variables: deviance <dbl>, df.residual <int>,
```

```r
glance(lm_out)
```

```
## # A tibble: 1 x 12
##   r.squared adj.r.squared sigma statistic  p.value    df
##       <dbl>         <dbl> <dbl>     <dbl>    <dbl> <dbl>
## 1     0.885         0.880  2.20      215. 1.17e-14     1
## # i 3 more variables: deviance <dbl>, df.residual <int>,
```

```r
glance(lm_out2)
```

```
## # A tibble: 1 x 12
##   r.squared adj.r.squared sigma statistic  p.value    df
##       <dbl>         <dbl> <dbl>     <dbl>    <dbl> <dbl>
## 1     0.970         0.969  2.94      943. 1.15e-23     1
## # i 3 more variables: deviance <dbl>, df.residual <int>,
```

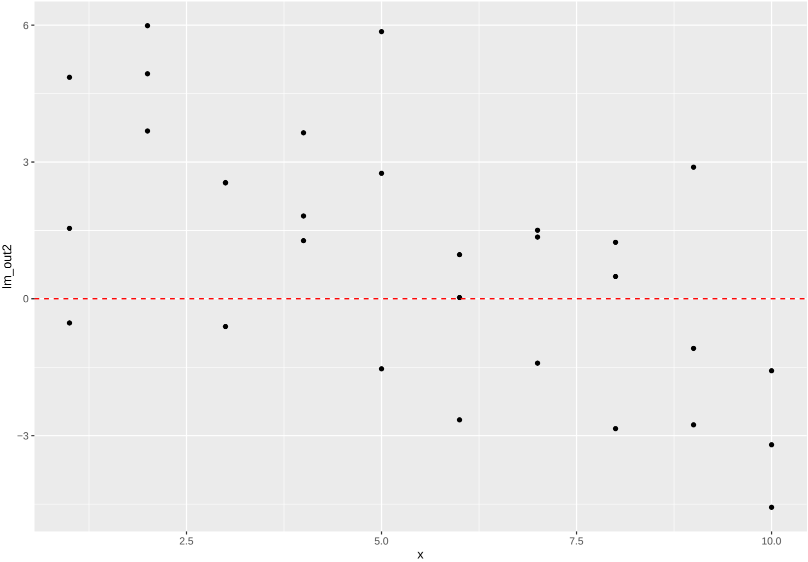
(R^2 and predictive quality are not the same thing ...)

modelr Helper Functions

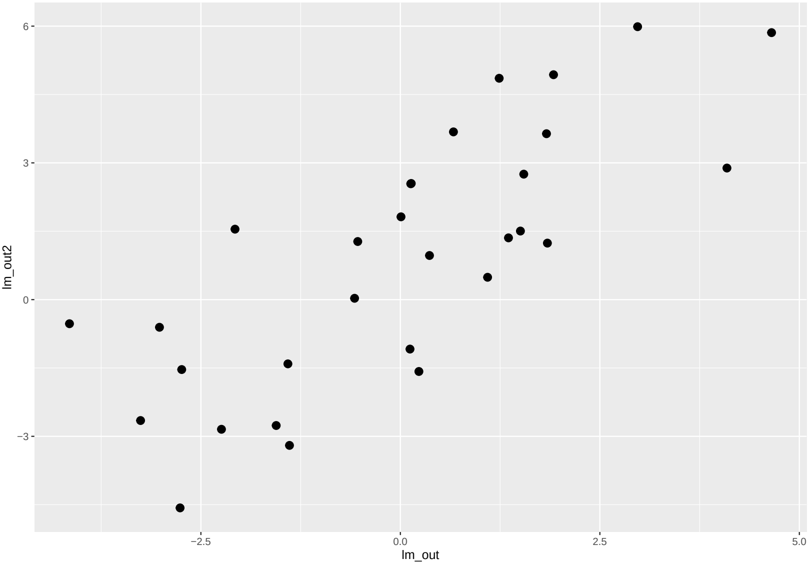
```
( sim1 <- sim1 |> spread_residuals(lm_out, lm_out2) )
```

```
## # A tibble: 30 x 6
##        x     y   resid  pred   lm_out lm_out2
##    <int> <dbl>   <dbl> <dbl>    <dbl>   <dbl>
##  1     1  4.20 -2.07    6.27 -2.07      1.55
##  2     1  7.51  1.24    6.27  1.24      4.86
##  3     1  2.13 -4.15    6.27 -4.15     -0.529
##  4     2  8.99  0.665   8.32  0.665     3.68
##  5     2 10.2   1.92    8.32  1.92      4.93
##  6     2 11.3   2.97    8.32  2.97      5.99
##  7     3  7.36 -3.02   10.4  -3.02     -0.607
##  8     3 10.5   0.130  10.4   0.130     2.54
##  9     3 10.5   0.136  10.4   0.136     2.55
## 10     4 12.4   0.00763 12.4  0.00763   1.82
## # i 20 more rows
```

```r
ggplot(sim1, aes(x, lm_out2)) + geom_point() +
  geom_hline(yintercept = 0, linetype = 2, color = "red")
```



```r
ggplot(sim1, aes(lm_out, lm_out2)) + geom_point(size = 3)
```

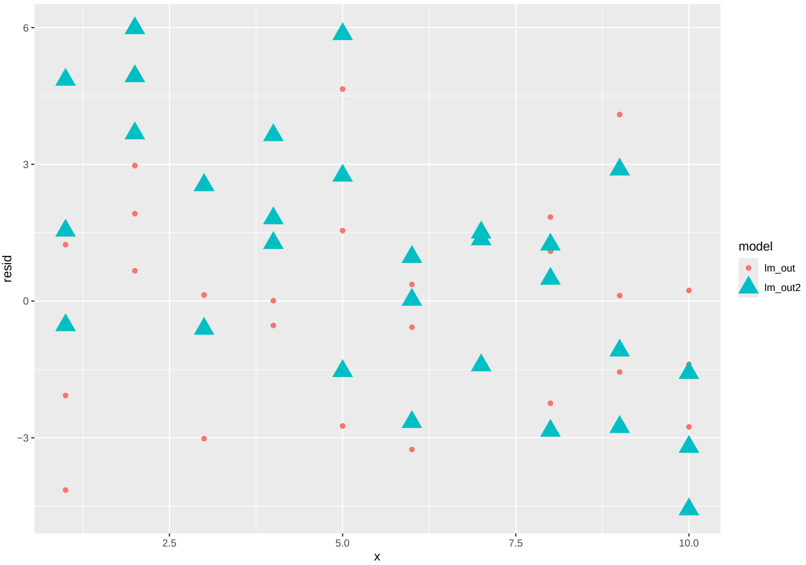


modelr Helper Functions

```
data(sim1)
( sim1 <- sim1 |> gather_residuals(lm_out, lm_out2) )
```

```
## # A tibble: 60 x 4
##    model       x     y    resid
##    <chr>   <int> <dbl>    <dbl>
##  1 lm_out      1  4.20 -2.07
##  2 lm_out      1  7.51  1.24
##  3 lm_out      1  2.13 -4.15
##  4 lm_out      2  8.99  0.665
##  5 lm_out      2 10.2   1.92
##  6 lm_out      2 11.3   2.97
##  7 lm_out      3  7.36 -3.02
##  8 lm_out      3 10.5   0.130
##  9 lm_out      3 10.5   0.136
## 10 lm_out      4 12.4   0.00763
## # i 50 more rows
```

```
ggplot(sim1, aes(x, resid)) +
  geom_point(aes(color = model, size = model, shape = model
```



`modelr` Helper Functions

- `add_residuals()`
- `spread_residuals()`
- `gather_residuals()`
- `add_predictions()`
- `spread_predictions()`
- `gather_predictions()`

Other Helpers for Many Models: `tidy()`

```
ll <- list(lm_out, lm_out2)

ll |> map_df(tidy)
```

```
## # A tibble: 3 x 5
##   term        estimate std.error statistic  p.value
##   <chr>          <dbl>     <dbl>     <dbl>    <dbl>
## 1 (Intercept)     4.22    0.869       4.86 4.09e- 5
## 2 x               2.05    0.140      14.7  1.17e-14
## 3 x               2.65    0.0865     30.7  1.15e-23
```

Many Models: glance()

```r
ll |> map_df(glance) |> select(1:5)
```

```
## # A tibble: 2 x 5
##   r.squared adj.r.squared sigma statistic  p.value
##       <dbl>         <dbl> <dbl>     <dbl>    <dbl>
## 1     0.885         0.880  2.20      215. 1.17e-14
## 2     0.970         0.969  2.94      943. 1.15e-23
```

Many Models: glance()

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ll |> map_df(glance) |> select(1:5)
```

```
## # A tibble: 2 x 5
##   r.squared adj.r.squared sigma statistic  p.value
##       <dbl>         <dbl> <dbl>     <dbl>    <dbl>
## 1     0.885         0.880  2.20      215. 1.17e-14
## 2     0.970         0.969  2.94      943. 1.15e-23
```

```
ll |> map_df(glance) |> select(6:12)
```

```
## # A tibble: 2 x 7
##      df logLik   AIC   BIC deviance df.residual  nobs
##   <dbl>  <dbl> <dbl> <dbl>    <dbl>       <int> <int>
## 1     1  -65.2  136.  141.     136.          28    30
## 2     1  -74.4  153.  156.     250.          29    30
```

Example: `mtcars`

Machine Learning Steps

1. Feature engineering

Machine Learning Steps

1. Feature engineering: collect/create the data

Machine Learning Steps

1. Feature engineering: collect/create the data
2. Data splitting

Machine Learning Steps

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2. Data splitting: split the data

Machine Learning Steps

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2. Data splitting: split the data

- Training. (80%? further split ("cross-validation")?)
- Validation. (for hyperparams; can be small (?))
- Testing. (20%?)

Machine Learning Steps

1. Feature engineering: collect/create the data
2. Data splitting: split the data

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3. Feature selection

Machine Learning Steps

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2. Data splitting: split the data

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3. Feature selection: algorithms decide predictors to include
4. Model estimation

Machine Learning Steps

1. Feature engineering: collect/create the data
2. Data splitting: split the data

- Training. (80%? further split ("cross-validation")?)
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4. Model estimation: find the slopes (e.g.)

Machine Learning Steps

1. Feature engineering: collect/create the data
2. Data splitting: split the data

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3. Feature selection: algorithms decide predictors to include
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5. Validation + testing

Machine Learning Steps

1. Feature engineering: collect/create the data
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- Training. (80%? further split ("cross-validation")?)
- Validation. (for hyperparams; can be small (?))
- Testing. (20%?)

3. Feature selection: algorithms decide predictors to include
4. Model estimation: find the slopes (e.g.)
5. Validation + testing: evaluate preds from trained models using new data

tidymodels Example

```r
library(tidymodels)
data_split <- initial_split(mtcars, prop = 2 / 3)

df_train <- training(data_split)
df_test <- testing(data_split)
```

tidymodels Example

```r
library(tidymodels)
data_split <- initial_split(mtcars, prop = 2 / 3)

df_train <- training(data_split)
df_test <- testing(data_split)
```

```r
dim(df_train)
```

```
## [1] 21 11
```

```r
dim(df_test)
```

```
## [1] 11 11
```

tidymodels Example

```
lm_fit <- linear_reg() |> fit(mpg ~ ., data = df_train)
lm_fit
```

```
## parsnip model object
##
##
## Call:
## stats::lm(formula = mpg ~ ., data = data)
##
## Coefficients:
## (Intercept)          cyl         disp           hp
##    -3.07537     -0.19100      0.02830     -0.02431
##        qsec           vs           am         gear
##     0.53145     -0.51353      1.54036      3.84550
```

tidymodels Example

```
out_preds <- bind_cols(df_test |> select(mpg),
                       predict(lm_fit, new_data = df_test)
                         rename(lm = .pred))
out_preds
```

```
##                      mpg       lm
## Mazda RX4 Wag       21.0 21.66514
## Hornet 4 Drive      21.4 20.20164
## Hornet Sportabout   18.7 18.80151
## Merc 450SE          16.4 13.48582
## Cadillac Fleetwood  10.4 14.11564
## Lincoln Continental 10.4 13.17200
## Toyota Corolla      33.9 28.64901
## Fiat X1-9           27.3 27.68602
## Porsche 914-2       26.0 30.67169
## Ford Pantera L      15.8 25.50938
## Ferrari Dino        19.7 19.95970
```

`tidymodels` Example

Next, predict with *random forest* algorithm.

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Ensemble learning algorithms:

- Boosting: models build on prior models

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`tidymodels` Example

Next, predict with *random forest* algorithm.

Ensemble learning algorithms:

- Boosting: models build on prior models $\rightsquigarrow$ pick feature, predict, upweight mispredicted data, ... Do several times and combine.
- Bagging: (random select units, model) $\rightarrow$ many times. No building.

`tidymodels` Example

Next, predict with *random forest* algorithm.

Ensemble learning algorithms:

- Boosting: models build on prior models $\rightsquigarrow$ pick feature, predict, upweight mispredicted data, ... Do several times and combine.
- Bagging: (random select units, model) $\rightarrow$ many times. No building.

`tidymodels` Example

Next, predict with *random forest* algorithm.

Ensemble learning algorithms:

- Boosting: models build on prior models $\rightsquigarrow$ pick feature, predict, upweight mispredicted data, ... Do several times and combine.
- Bagging: (random select units, model) $\rightarrow$ many times. No building.

Random Forests are bagging algorithms.

Breiman (2001a)

tidymodels Example

```r
rf_fit <- rand_forest(mode = "regression") |>
  fit(mpg ~ ., data = df_train)
rf_fit
```

```
## parsnip model object
##
## Ranger result
##
## Call:
##  ranger::ranger(x = maybe_data_frame(x), y = y, num.thre
##
## Type:                             Regression
## Number of trees:                  500
## Sample size:                      21
## Number of independent variables:  10
## Mtry:                             3
## Target node size:                 5
## Variable importance mode:         none
```

tidymodels Example

parsnip::rand_forest() uses ranger engine

`tidymodels` Example

`parsnip::rand_forest()` uses `ranger` engine

There is also "Spark".

tidymodels Example

```r
out_preds <- bind_cols(out_preds,
                       predict(rf_fit, new_data = df_test) 
                         rename(rf = .pred))
out_preds
```

```
##                      mpg       lm       rf
## Mazda RX4 Wag       21.0 21.66514 20.36497
## Hornet 4 Drive      21.4 20.20164 19.52452
## Hornet Sportabout   18.7 18.80151 16.45822
## Merc 450SE          16.4 13.48582 16.42280
## Cadillac Fleetwood  10.4 14.11564 16.26746
## Lincoln Continental 10.4 13.17200 15.78517
## Toyota Corolla      33.9 28.64901 29.41605
## Fiat X1-9           27.3 27.68602 29.41278
## Porsche 914-2       26.0 30.67169 25.27119
## Ford Pantera L      15.8 25.50938 17.23360
## Ferrari Dino        19.7 19.95970 19.91055
```

tidymodels Example

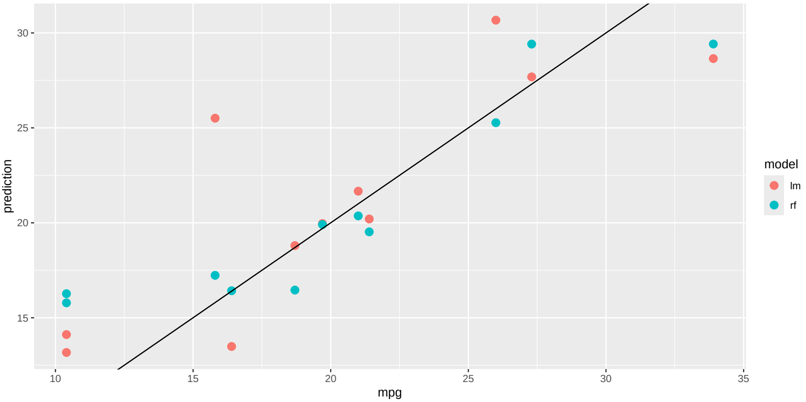
```
out_preds_long <- out_preds |>
  pivot_longer(cols = c(lm, rf),
               names_to = "model",
               values_to = "prediction")

out_preds_long
```

```
## # A tibble: 22 x 3
##      mpg model prediction
##    <dbl> <chr>      <dbl>
##  1  21   lm          21.7
##  2  21   rf          20.4
##  3  21.4 lm          20.2
##  4  21.4 rf          19.5
##  5  18.7 lm          18.8
##  6  18.7 rf          16.5
##  7  16.4 lm          13.5
##  8  16.4 rf          16.4
```

tidymodels Example

```
ggplot(out_preds_long, aes(mpg, prediction)) +
  geom_point(aes(color = model), size = 3) +
  geom_abline(slope = 1, intercept = 0)
```



tidymodels Example

Evaluate:

```
out_preds |> metrics(truth = mpg, estimate = lm) |>
  rename(lm = .estimate) |>
  left_join(out_preds |>
              metrics(truth = mpg, estimate = rf) |>
              rename(rf = .estimate))
```

```
## Joining with `by = join_by(.metric, .estimator)`
```

```
## # A tibble: 3 x 4
##   .metric .estimator    lm    rf
##   <chr>   <chr>      <dbl> <dbl>
## 1 rmse    standard   4.00  3.01
## 2 rsq     standard   0.683 0.842
## 3 mae     standard   2.88  2.27
```

Example: Social Pressure Experiment (`recipes`)

Data Splitting

```
social <- read_csv("https://raw.githubusercontent.com/I

soc_split <- initial_split(social)
soc_train <- training(soc_split)
soc_test <- testing(soc_split)
```

Data Splitting

```
social <- read_csv("https://raw.githubusercontent.com/I

soc_split <- initial_split(social)
soc_train <- training(soc_split)
soc_test <- testing(soc_split)
```

```
dim(soc_train)
```

```
## [1] 229399      6
```

```
dim(soc_test)
```

```
## [1] 76467     6
```

Feature Engineering

```r
social_recip <- recipe(primary2006 ~ ., data = soc_train)

social_recip
```

Feature Engineering

```r
summary(social_recip)
```

```
## # A tibble: 6 x 4
##   variable    type       role      source
##   <chr>       <list>     <chr>     <chr>
## 1 sex         <chr [3]> predictor original
## 2 yearofbirth <chr [2]> predictor original
## 3 primary2004 <chr [2]> predictor original
## 4 messages    <chr [3]> predictor original
## 5 hhsize      <chr [2]> predictor original
## 6 primary2006 <chr [2]> outcome   original
```

Feature Engineering

```
social_recip <- social_recip |>
  step_mutate(age = 2006 - yearofbirth) |>
  step_dummy(all_nominal(), -all_outcomes())
```

```
social_recip
```

```
##
## -- Recipe ----------------------------------------------
##
## -- Inputs
## Number of variables by role
## outcome:   1
## predictor: 5
##
## -- Operations
## * Variable mutation for: 2006 - yearofbirth
## * Dummy variables from: all_nominal() -all_outcomes()
```

Feature Engineering

```r
social_recip <- social_recip |>
  step_zv(all_predictors())
```

```
social_recip
```

```
##
## -- Recipe ------------------------------------------------------------------
##
## -- Inputs
## Number of variables by role
## outcome:   1
## predictor: 5
##
## -- Operations
## * Variable mutation for: 2006 - yearofbirth
## * Dummy variables from: all_nominal() -all_outcomes()
## * Zero variance filter on: all_predictors()
```

Feature Engineering

```r
social_recip <- social_recip |>
  step_center(all_predictors(), -primary2004)
```

```r
social_recip
```

```
##
## -- Recipe ----------------------------------------------------
##
## -- Inputs
## Number of variables by role
## outcome:   1
## predictor: 5
##
## -- Operations
## * Variable mutation for: 2006 - yearofbirth
## * Dummy variables from: all_nominal() -all_outcomes()
## * Zero variance filter on: all_predictors()
## * Centering for: all_predictors() -primary2004
```

Feature Engineering

```r
social_recip <- social_recip |>
  step_interact(terms = ~
                  age:all_predictors() +
                  primary2004:all_predictors()
                  )
```

Feature Engineering

Recipe complete. Time to prep and bake.

Feature Engineering

Recipe complete. Time to prep and bake.

```r
social_recip |>
  prep()
```

```
##

## -- Recipe -----------------------------------------

##

## -- Inputs

## Number of variables by role

## outcome:   1
## predictor: 5

##

## -- Training information
```

```r
soc_train_processed <- social_recip |>
  prep() |>
  bake(new_data = NULL)

soc_train_processed
```

```
## # A tibble: 229,399 x 22
##    yearofbirth primary2004 hhsize primary2006    age sex
##          <dbl>       <dbl>  <dbl>       <dbl>  <dbl>
##  1     -13.2             1 -0.185           0 13.2     -
##  2       0.779           1 -0.185           0 -0.779   -
##  3      -6.22            1 -0.185           0  6.22
##  4      -4.22            0  0.815           0  4.22    -
##  5      -5.22            1 -1.18            1  5.22    -
##  6     -19.2             0  0.815           0 19.2
##  7     -25.2             0 -0.185           1 25.2
##  8     -29.2             0 -0.185           1 29.2     -
##  9     -12.2             0  0.815           0 12.2
## 10      -4.22            0  0.815           0  4.22    -
## # i 229,389 more rows
```

```r
names(soc_train_processed)
```

```
##  [1] "yearofbirth"                         "primary2004
##  [3] "hhsize"                              "primary2006
##  [5] "age"                                 "sex_male"
##  [7] "messages_Control"                    "messages_Ha
##  [9] "messages_Neighbors"                  "age_x_yearo
## [11] "age_x_primary2004"                   "age_x_hhsiz
## [13] "age_x_sex_male"                      "age_x_messa
## [15] "age_x_messages_Hawthorne"            "age_x_messa
## [17] "yearofbirth_x_primary2004"           "primary2004
## [19] "primary2004_x_sex_male"              "primary2004
## [21] "primary2004_x_messages_Hawthorne" "primary2004
```

```r
soc_test_processed <- social_recip |>
  prep() |>
  bake(new_data = soc_test)

soc_test_processed
```

```
## # A tibble: 76,467 x 22
##    yearofbirth primary2004 hhsize primary2006    age sex
##          <dbl>       <dbl>  <dbl>       <dbl>  <dbl>
##  1      -15.2            0 -0.185           0  15.2
##  2       -6.22           0  0.815           1   6.22   -
##  3       10.8            0 -0.185           0 -10.8
##  4      -15.2            1 -1.18            1  15.2
##  5       12.8            1 -1.18            0 -12.8    -
##  6       10.8            1 -0.185           1 -10.8    -
##  7       26.8            0  1.82            0 -26.8    -
##  8        8.78           0 -0.185           0  -8.78
##  9      -24.2            0 -0.185           0  24.2    -
## 10        2.78           0 -0.185           0  -2.78   -
## # i 76,457 more rows
```

Now, with train and test data ready, add *model specification*, *fitting*, *evaluation*, *deployment* to workflow.

Regularization Methods: LASSO, ridge regression, elastic nets

Feature Selection

- Wrappers: pick subset of covars, train on data (estimate model), test on hold-out, score predictions. Keep best-scoring subset.

Feature Selection

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- Filters: correlate covars with outcome. Keep strongest.

Feature Selection

- Wrappers: pick subset of covars, train on data (estimate model), test on hold-out, score predictions. Keep best-scoring subset.
- Filters: correlate covars with outcome. Keep strongest.
- Embeds: select features and estimate model at same time. Penalize using more predictors.

Embedded Regularization Methods

OLS reminder

Minimize SSR:

$$\arg\min_{\beta} \sum_{i=1}^{n} \left(y_i - \hat{y}_i\right)^2$$

$$\arg\min_{\beta} \sum_{i=1}^{n} \left(\mathbf{y} - \mathbf{X}\hat{\beta}\right)^2$$

Embedded Regularization Methods

L1 regularization: the LASSO (Least Absolute Shrinkage and Selection Operator)

$$\arg\min_{\beta}\left[\sum_{i=1}^{n}\left(y_i-\mathbf{X}\hat{\beta}\right)^2+\lambda\sum_{j=1}^{k}|\hat{\beta}_j|\right]$$

Embedded Regularization Methods

L1 regularization: the LASSO (Least Absolute Shrinkage and Selection Operator)

$$\arg\min_{\beta} \left[\sum_{i=1}^{n} \left(y_i - \mathbf{X}\hat{\beta} \right)^2 + \lambda \sum_{j=1}^{k} |\hat{\beta}_j| \right]$$

L2 regularization: Ridge regression

$$\arg\min_{\beta} \left[\sum_{i=1}^{n} \left(y_i - \mathbf{X}\hat{\beta} \right)^2 + \lambda \sum_{j=1}^{k} \hat{\beta}_j^2 \right]$$

Embedded Regularization Methods

Mix L1 and L2: Elastic net

$$\arg\min_{\beta} \left(\frac{\sum_{i=1}^{n} \left(y_i - \mathbf{X}\hat{\beta} \right)^2}{2n} + \lambda \left[\alpha \sum_{j=1}^{k} |\hat{\beta}_j| + \frac{1-\alpha}{2} \sum_{j=1}^{k} \hat{\beta}_j^2 \right] \right)$$

Embedded Regularization Methods

Mix L1 and L2: Elastic net

$$\arg\min_{\beta} \left(\frac{\sum_{i=1}^{n} \left(y_i - \mathbf{X}\hat{\beta} \right)^2}{2n} + \lambda \left[\alpha \sum_{j=1}^{k} |\hat{\beta}_j| + \frac{1-\alpha}{2} \sum_{j=1}^{k} \hat{\beta}_j^2 \right] \right)$$

Regularized trees, ...

R packages for Regularization, etc.

- `glmnet`
- `caret`

See also `tidymodels`, `parsnip`, ...

References

Breiman, Leo. 2001a. "Random Forests." *Machine Learning* 45: 5–32.

———. 2001b. "Statistical Modeling: The Two Cultures." *Statistical Science* 16 (3): 199–215. http://www.jstor.org/stable/2676681.