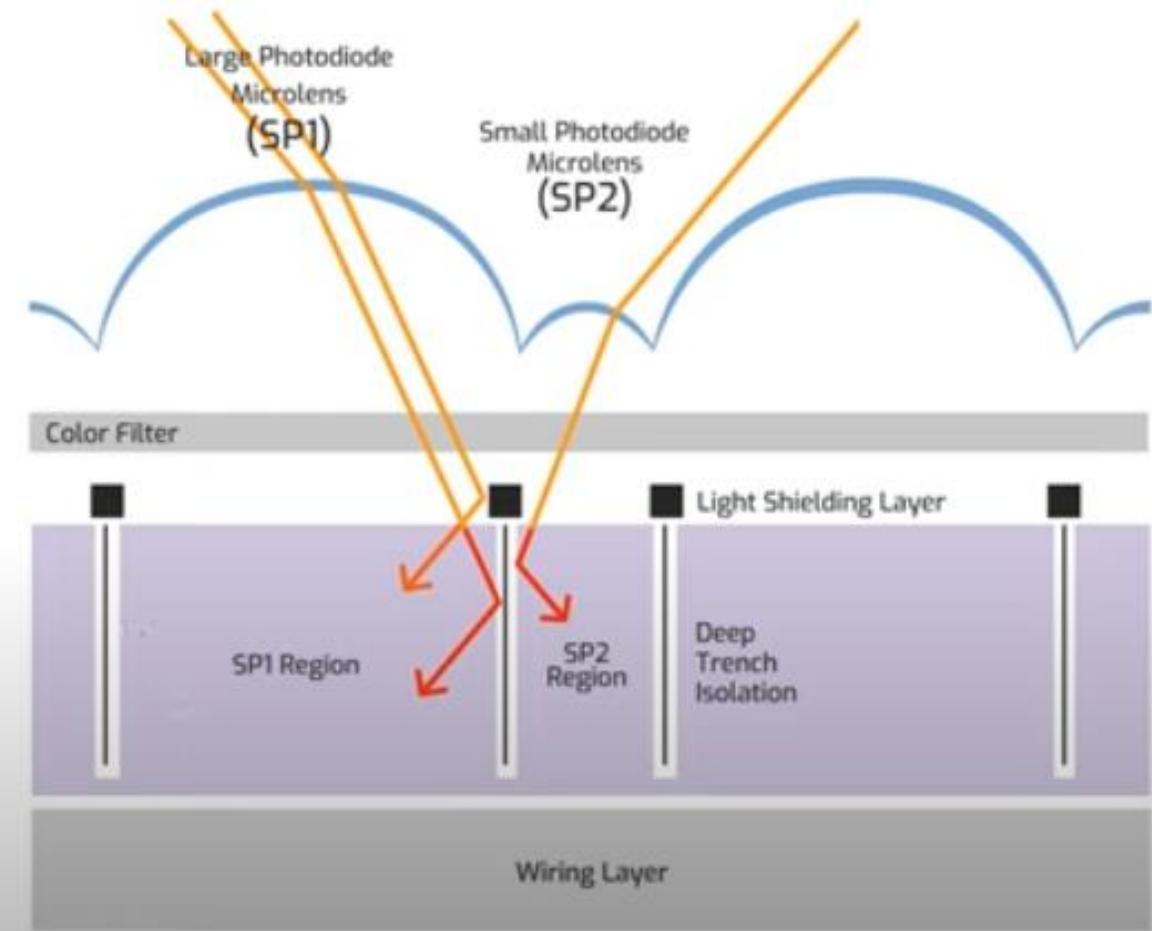
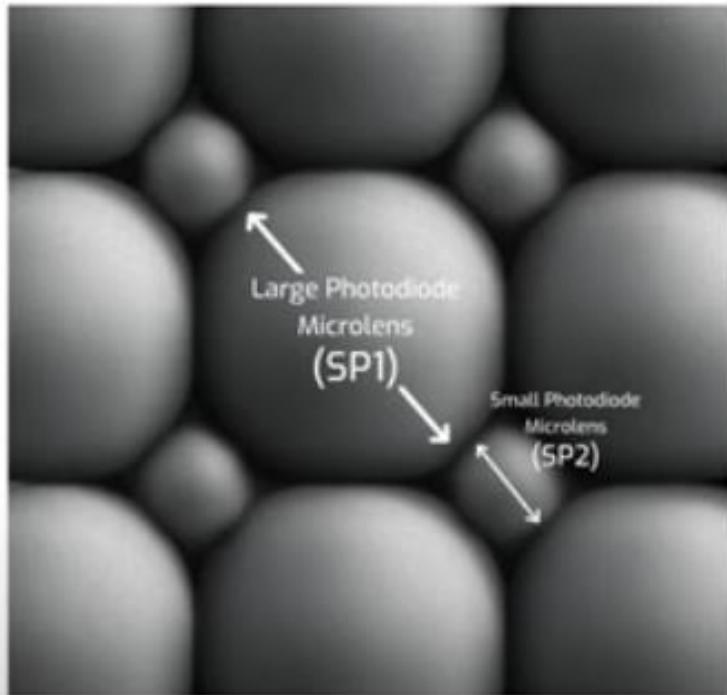


Imaging Sensors for Vision

Matthew O'Toole
Email: motoole2@andrew.cmu.edu

Sony IMX490 Sensor





Sensing polarization

Polarization Photography : Reflections



Reduce Reflections

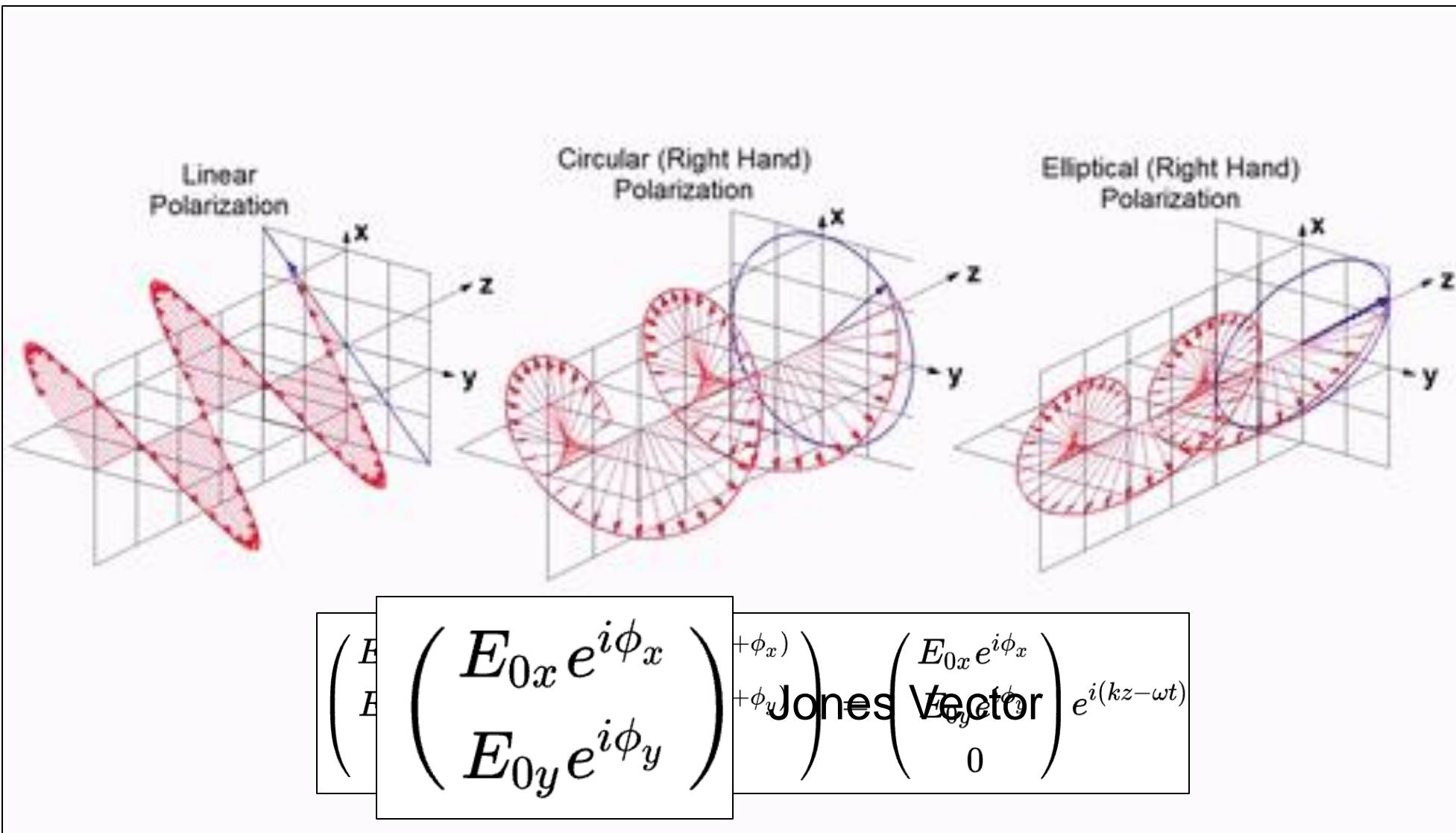
Classification of Polarization

Linear : Two orthogonal plane waves with same phase but possibly different amplitudes.

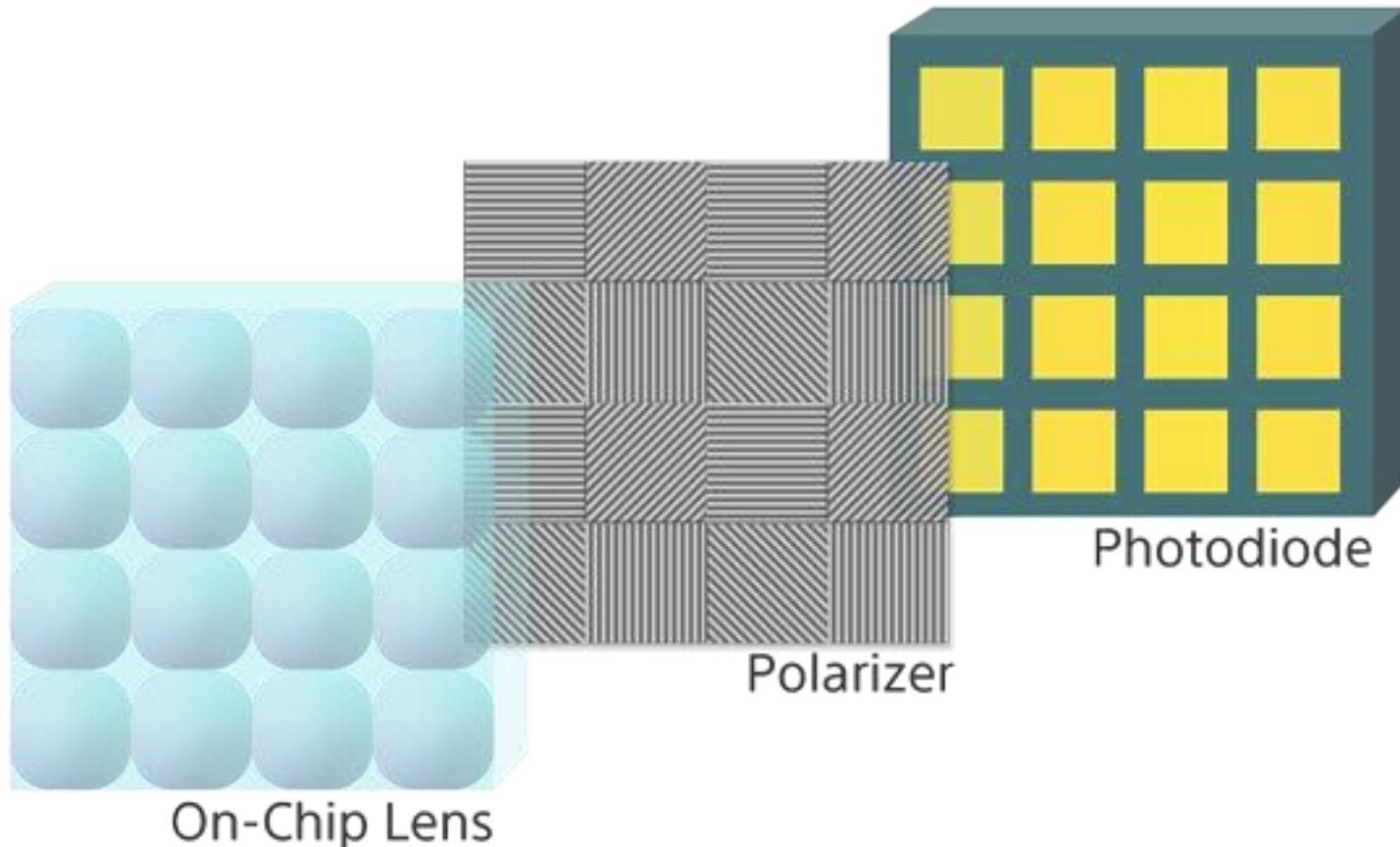
Circular: Two orthogonal plane waves with 90 deg phase shift but same amplitudes.

Elliptical: Possibly any degree phase shift with different amplitudes.

Classification of Polarization



Polarization Image Sensor



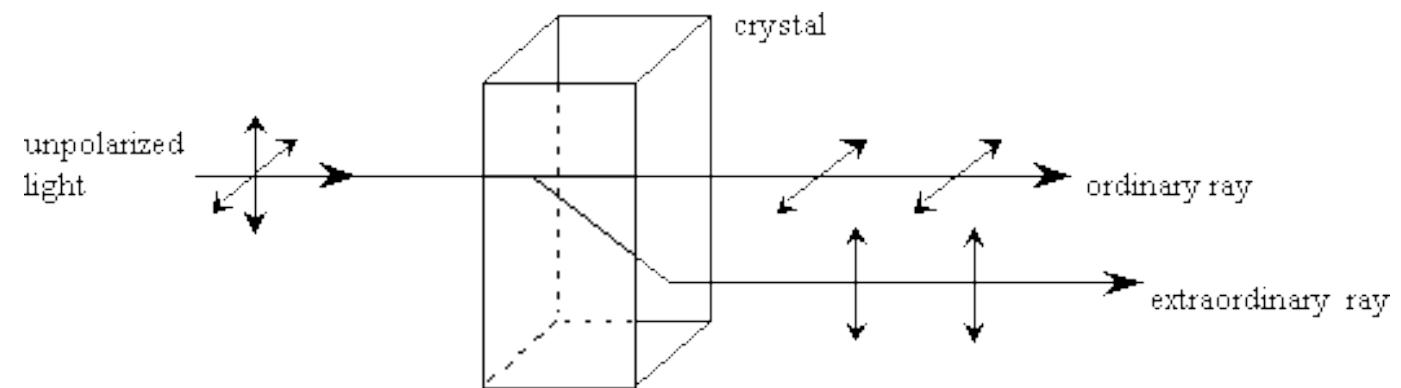
Without polarizer



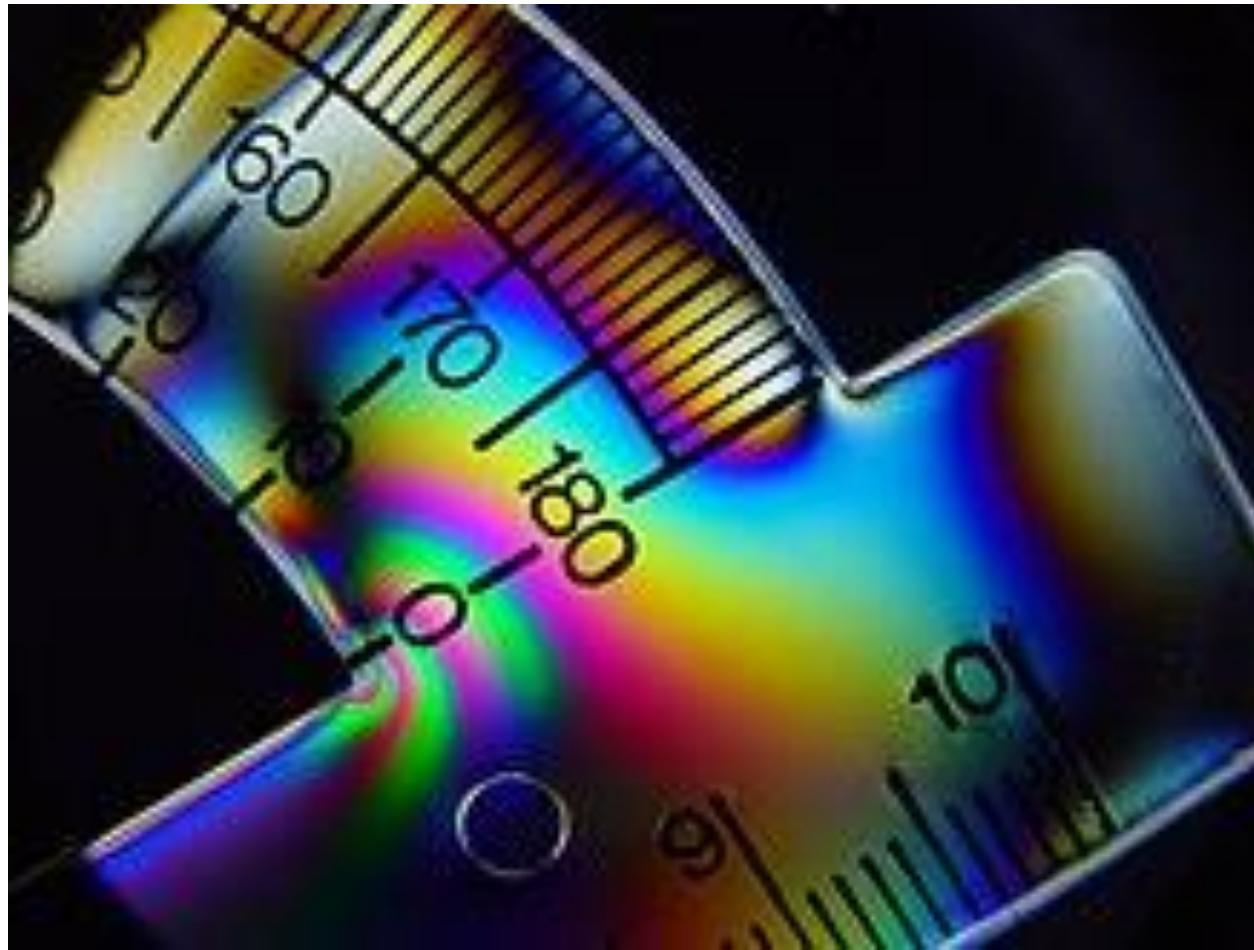
With polarizer



Birefringence



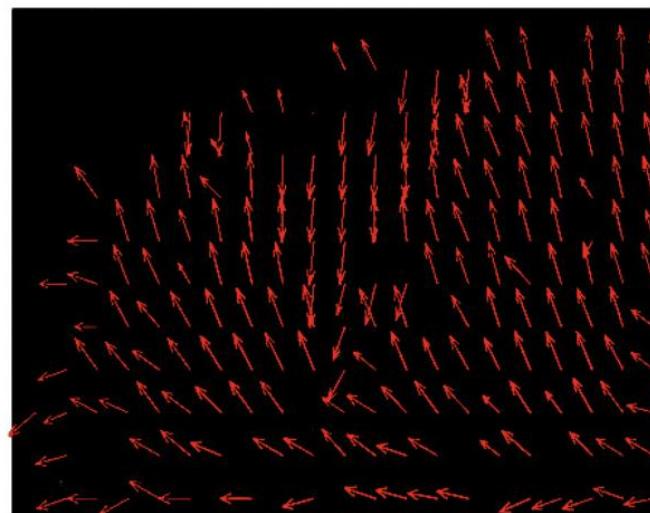
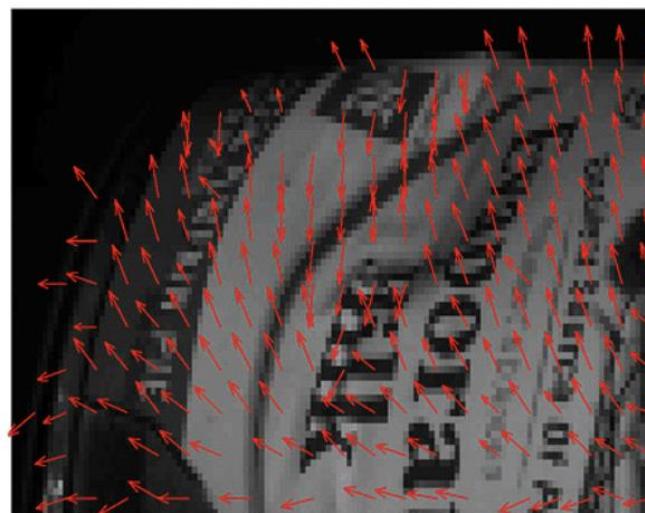
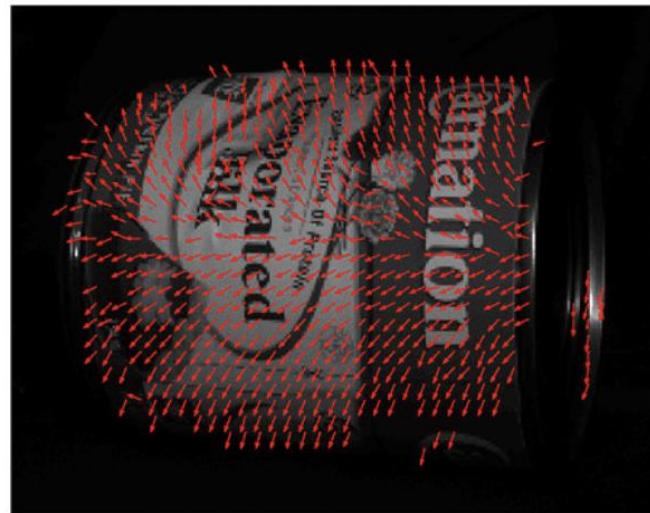
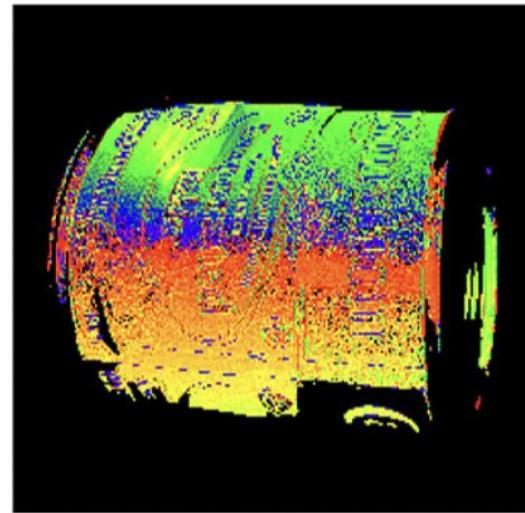
Measuring stress distributions



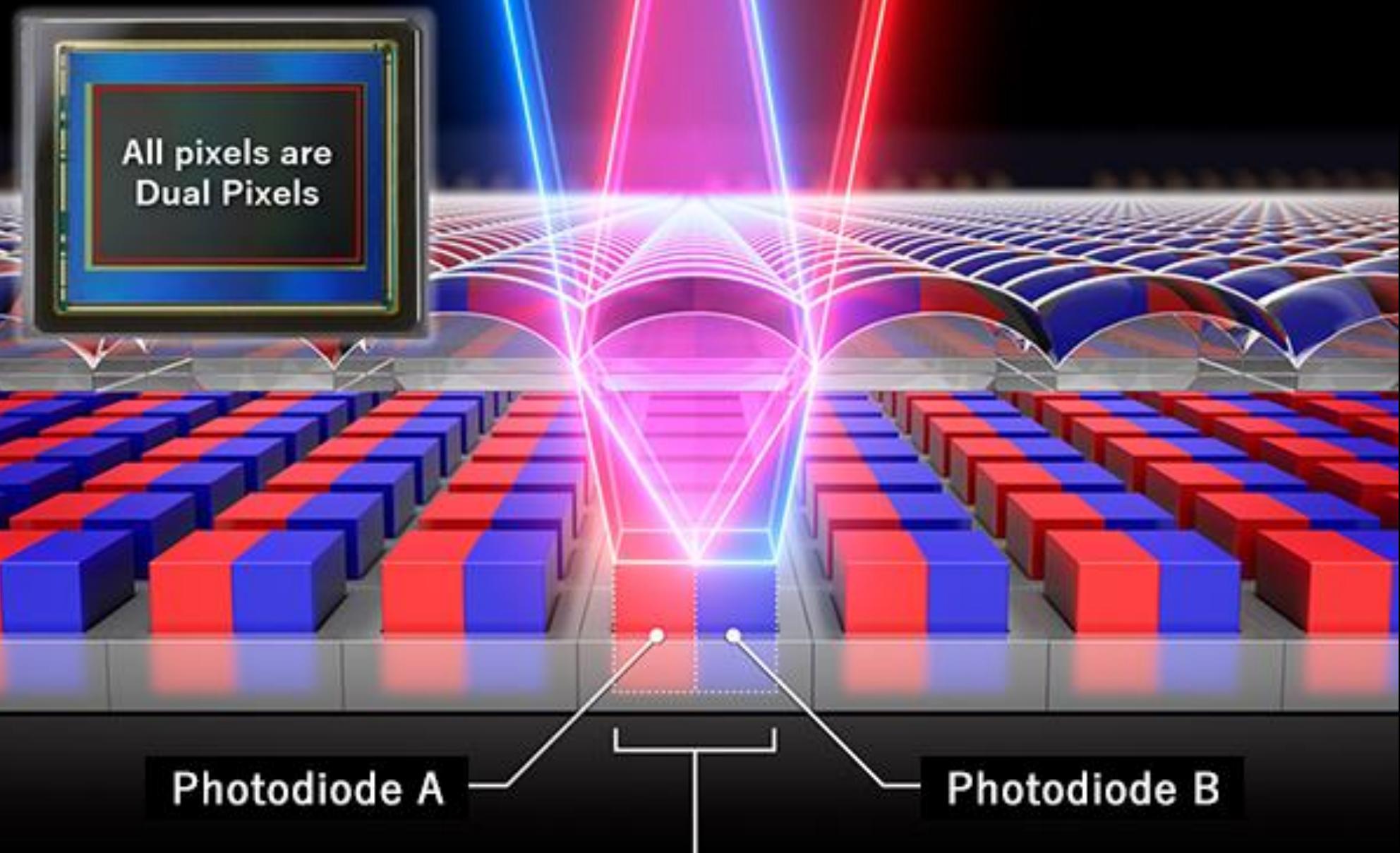
3D Movies



Shape from polarization



Dual pixel sensors



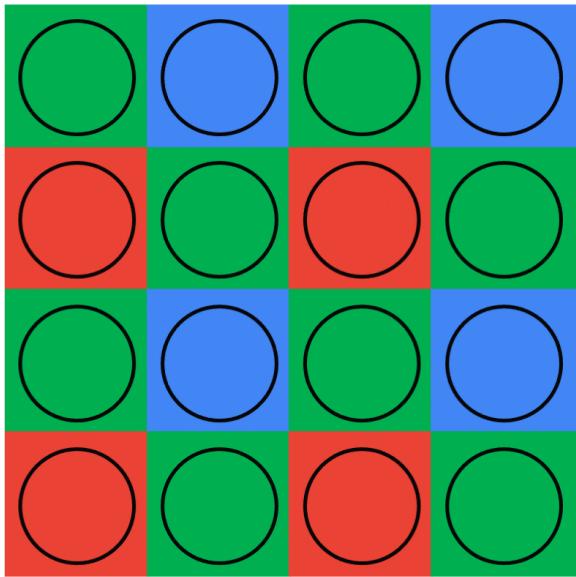
All pixels are
Dual Pixels

Photodiode A

Photodiode B

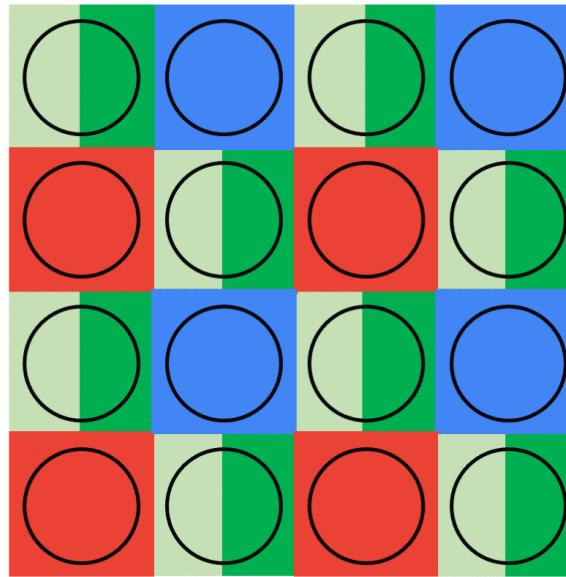
Pixels which enable both
phase-difference AF and imaging

Dual Pixel (DP) Sensors

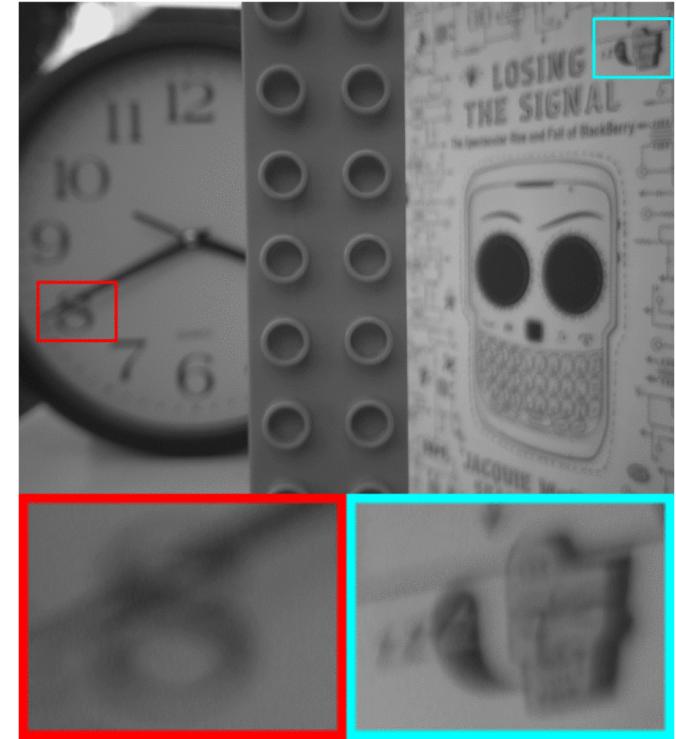


Regular sensor

Left photodiode ← → Right photodiode



DP sensor



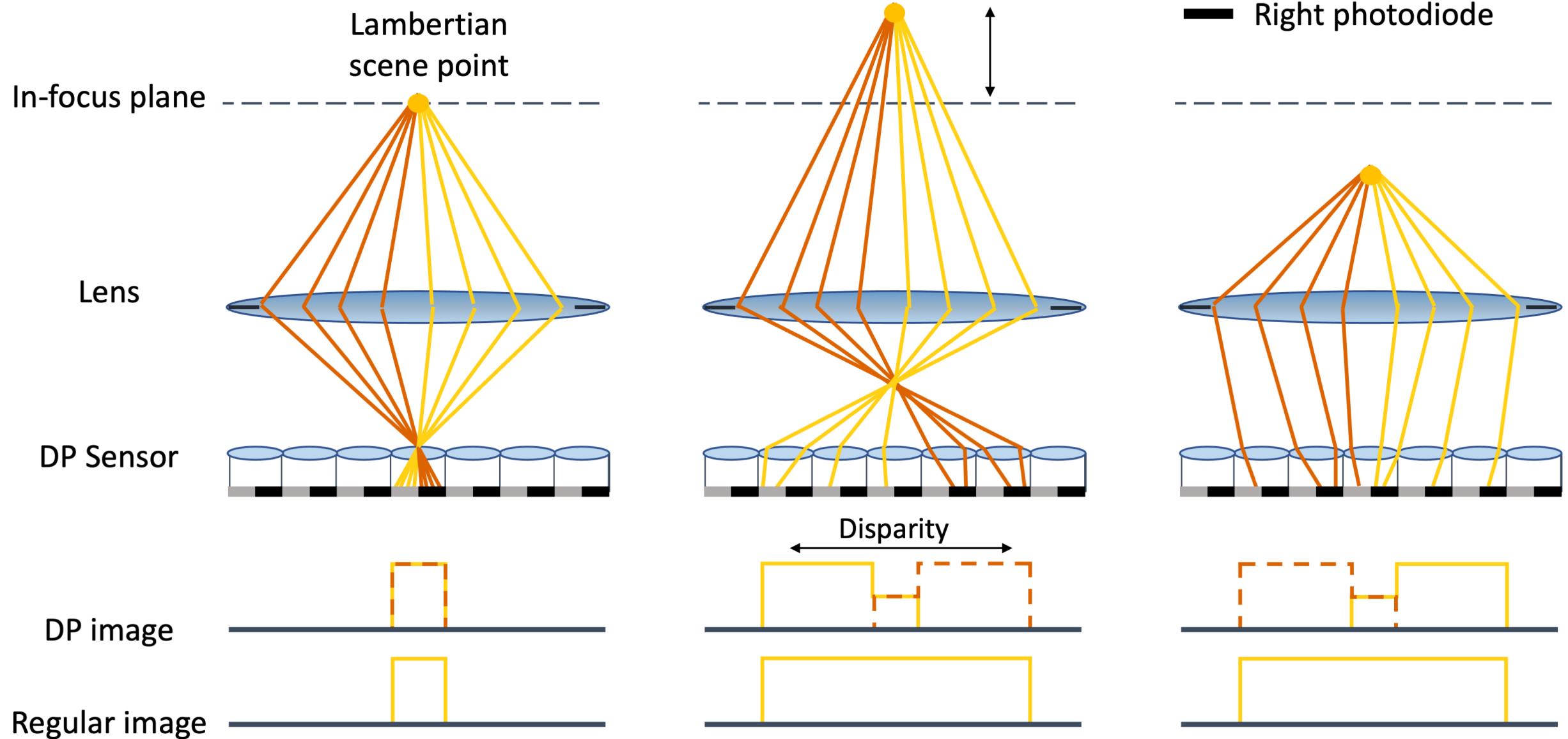
DP image



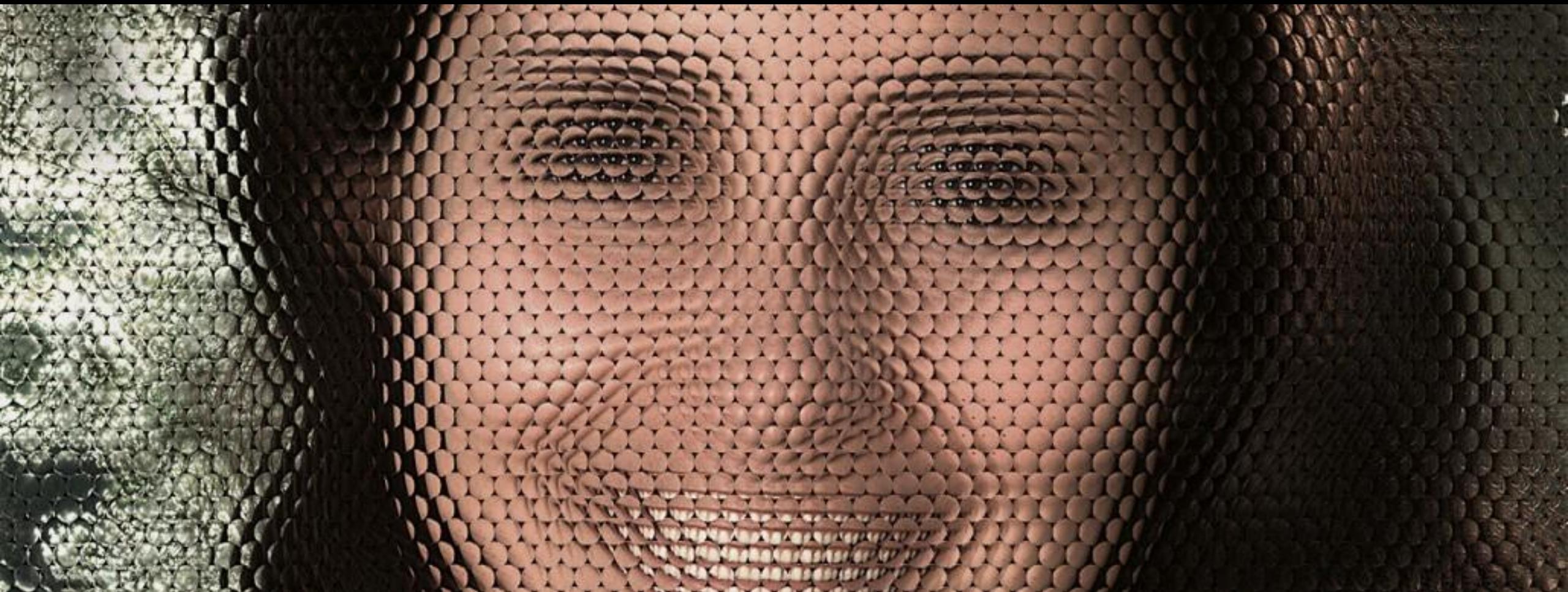
Canon EOS R5

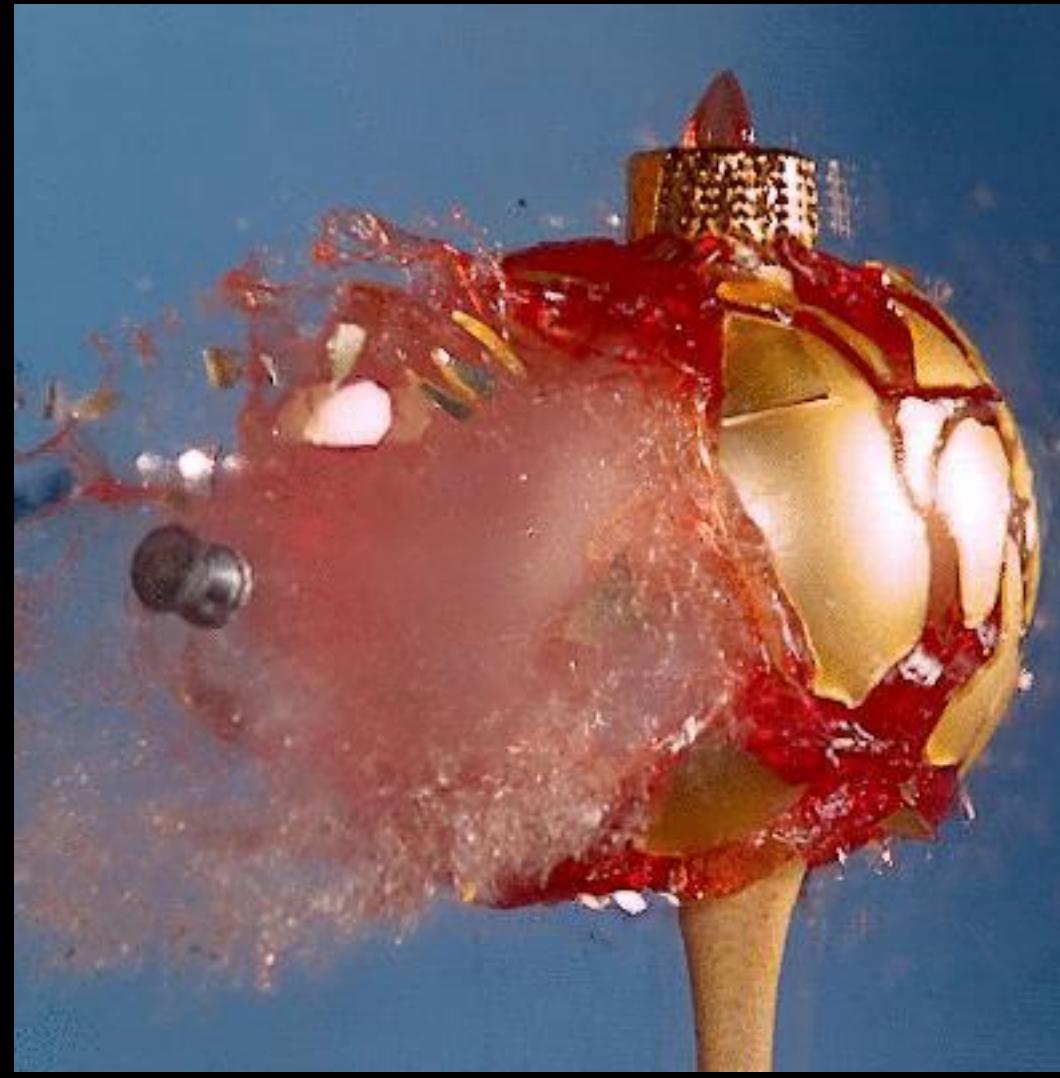
Google Pixel 4

DP Image Formation



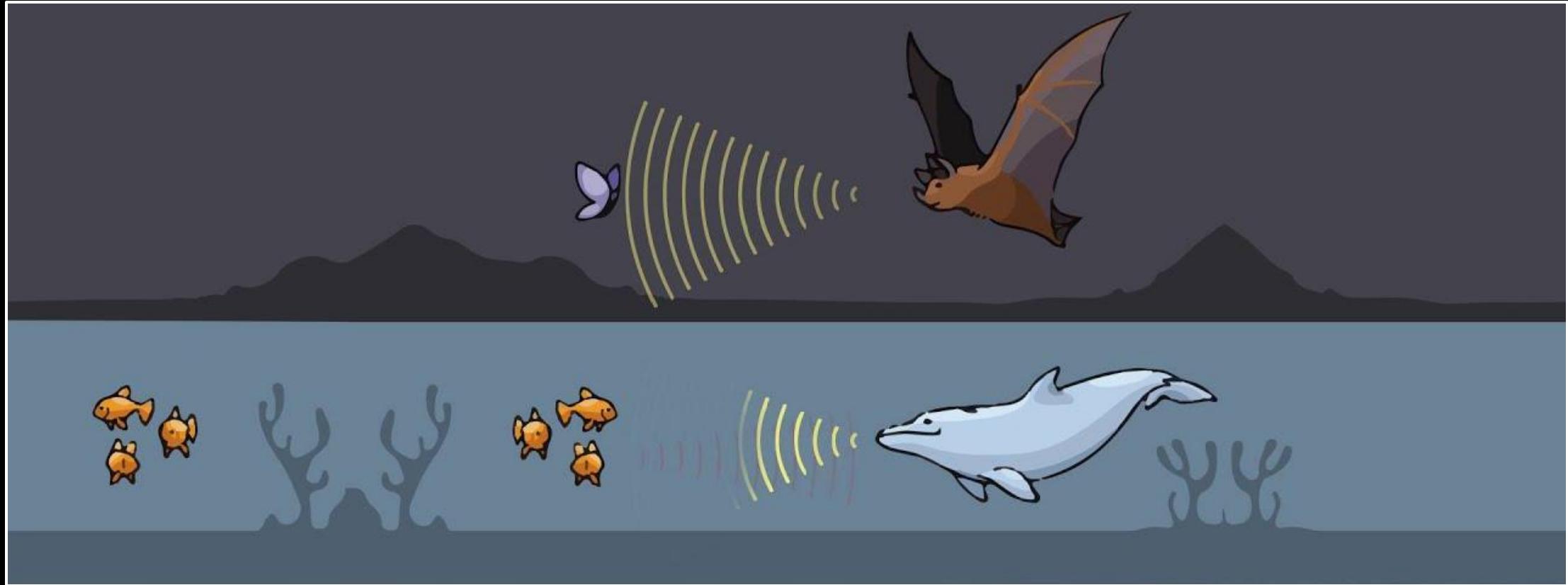
Light field imaging





Time-of-flight sensing

echolocation



speed of sound in air: 343 meters / sec
in water: 1480 meters / sec

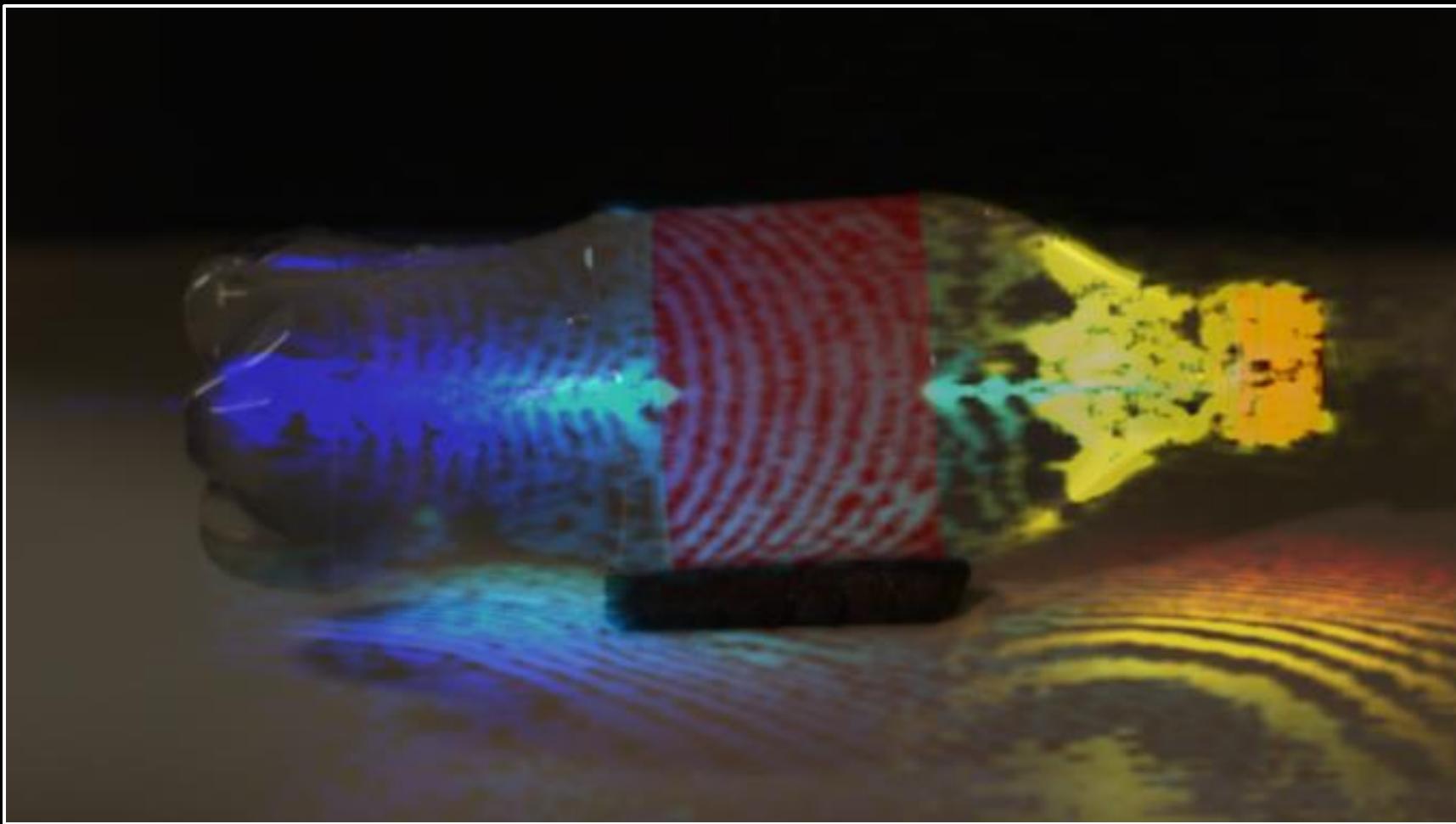
Light takes 1.255 seconds to travel from the earth to the moon



speed of light in a vacuum: **299,792,458** meters / sec

(Light travels approximation **1 MILLION** times faster than sound!)

transient imaging



speed of light in a vacuum: **299,792,458** meters / sec

(Light travels approximation **1 MILLION** times faster than sound!)

transient imaging (a.k.a. femtophotography)



“Femto-photography: capturing and visualizing the propagation of light”, [Velten et al., 2012]

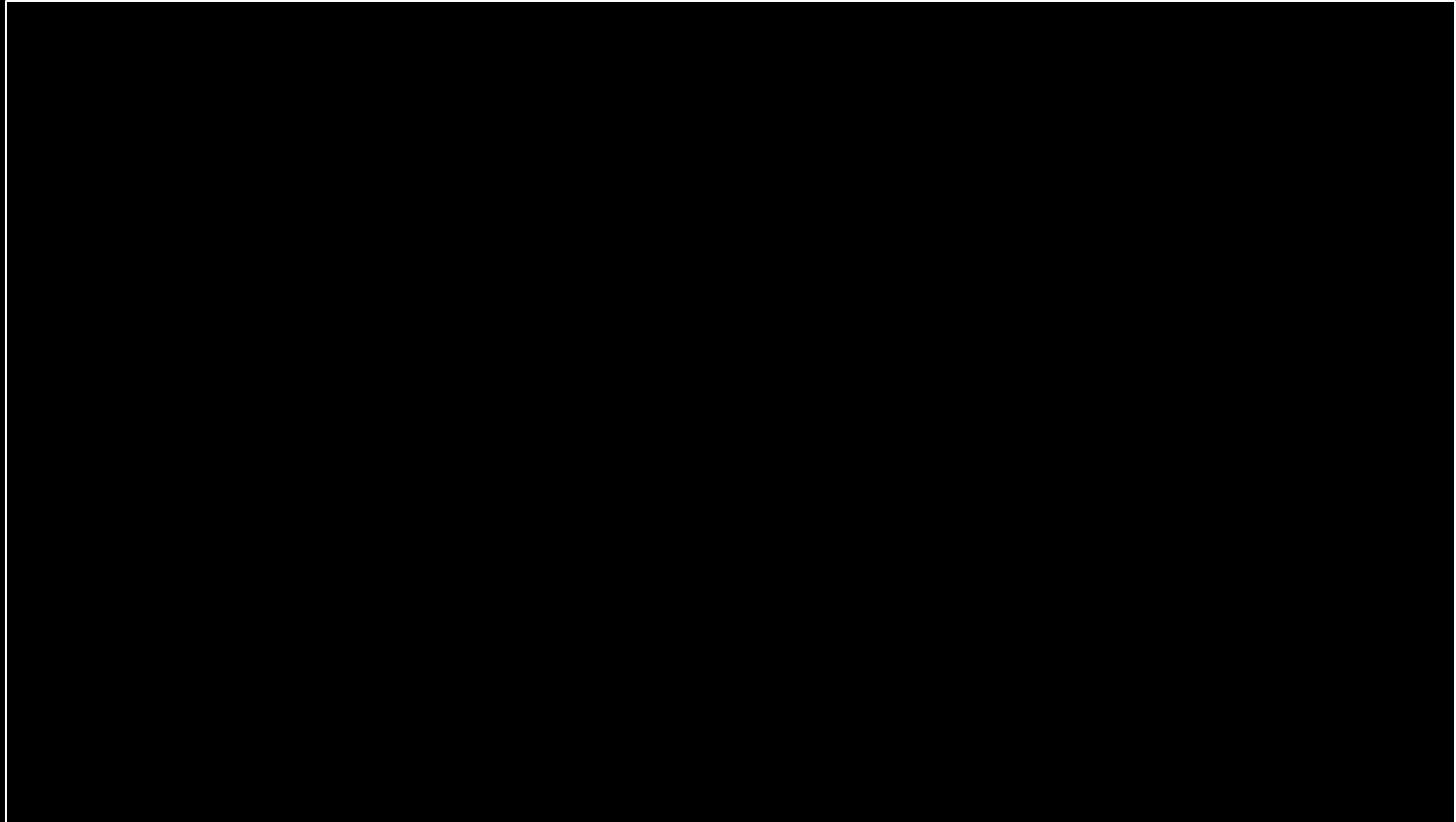
direct and indirect time-of-flight sensors for transient imaging



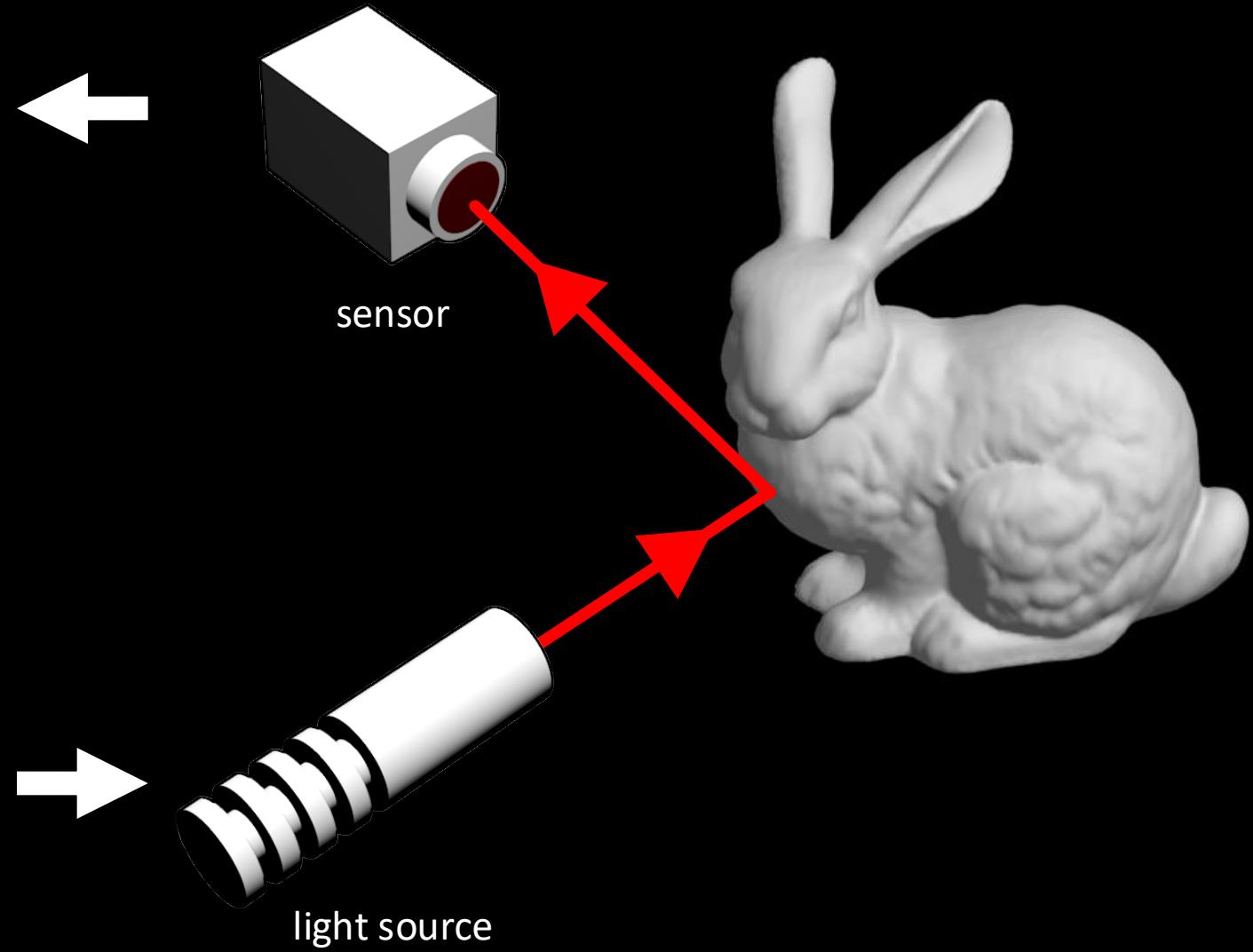
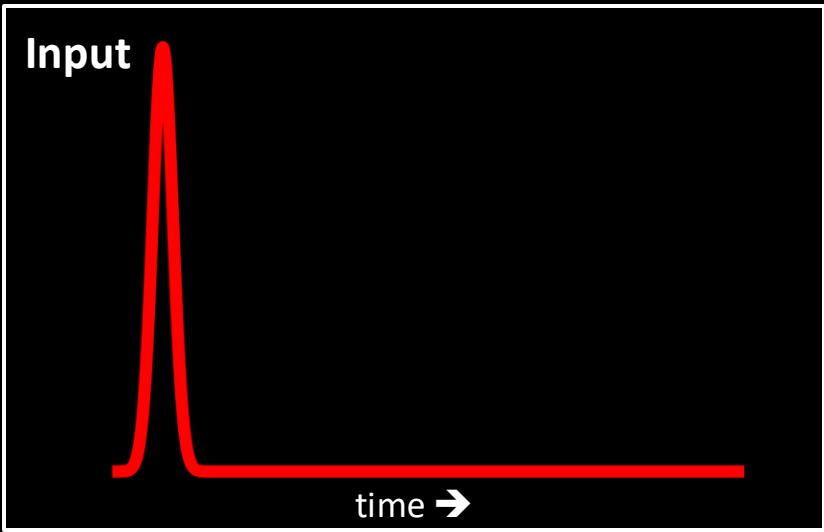
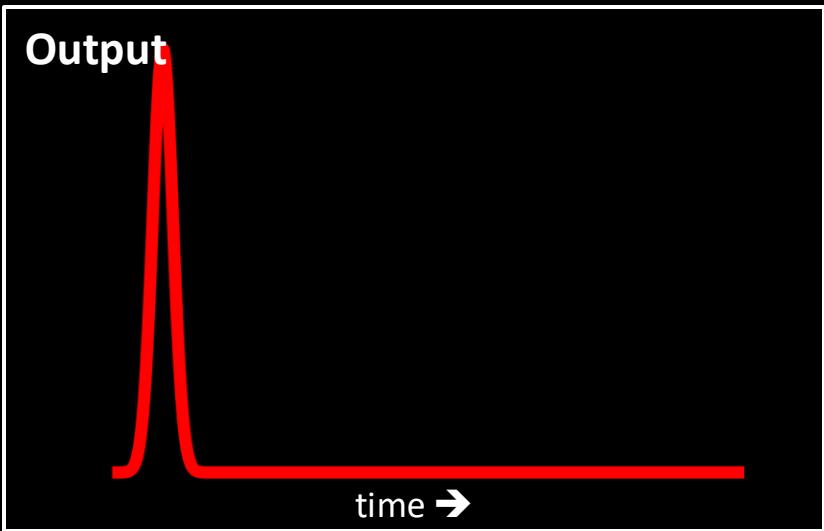
direct and indirect time-of-flight sensors for transient imaging



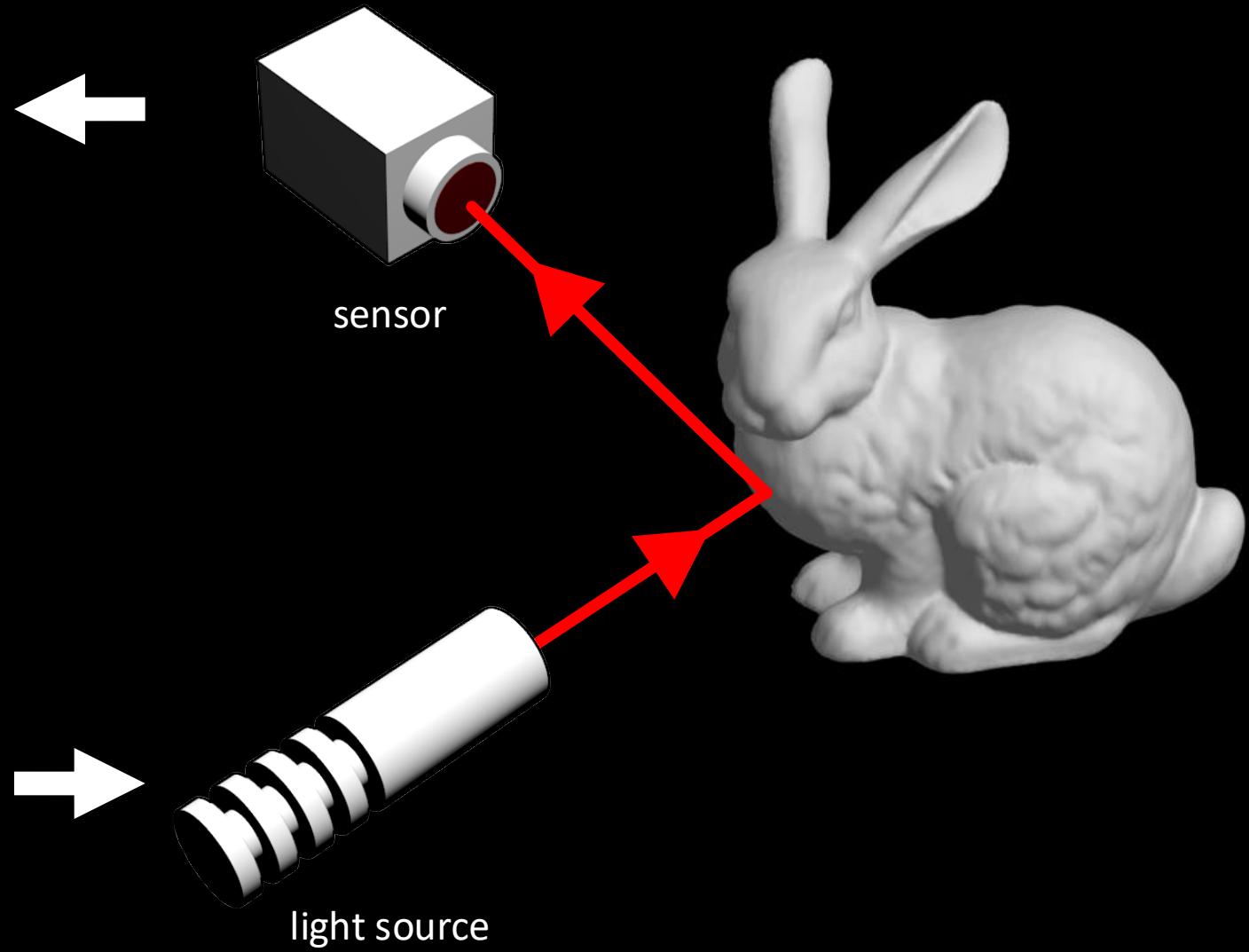
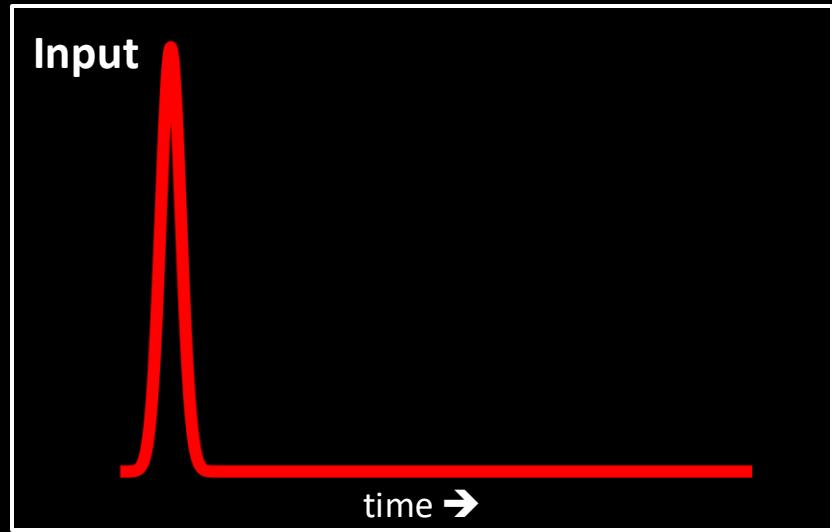
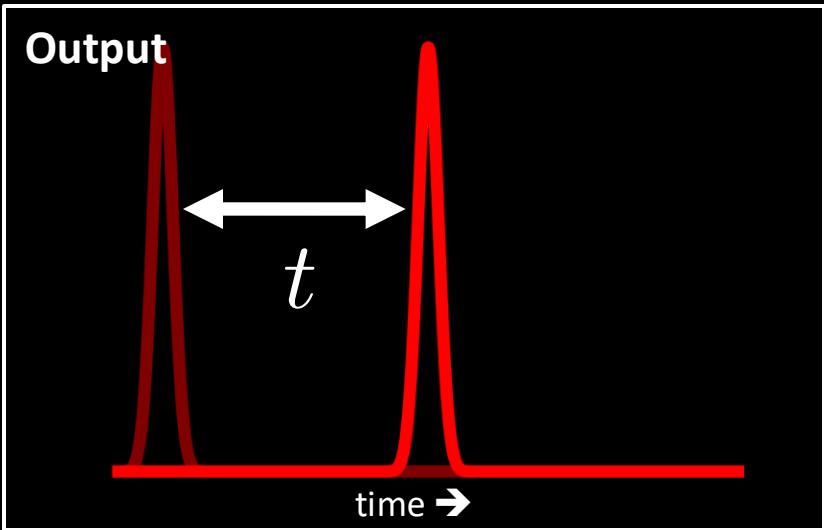
direct and indirect time-of-flight sensors for transient imaging



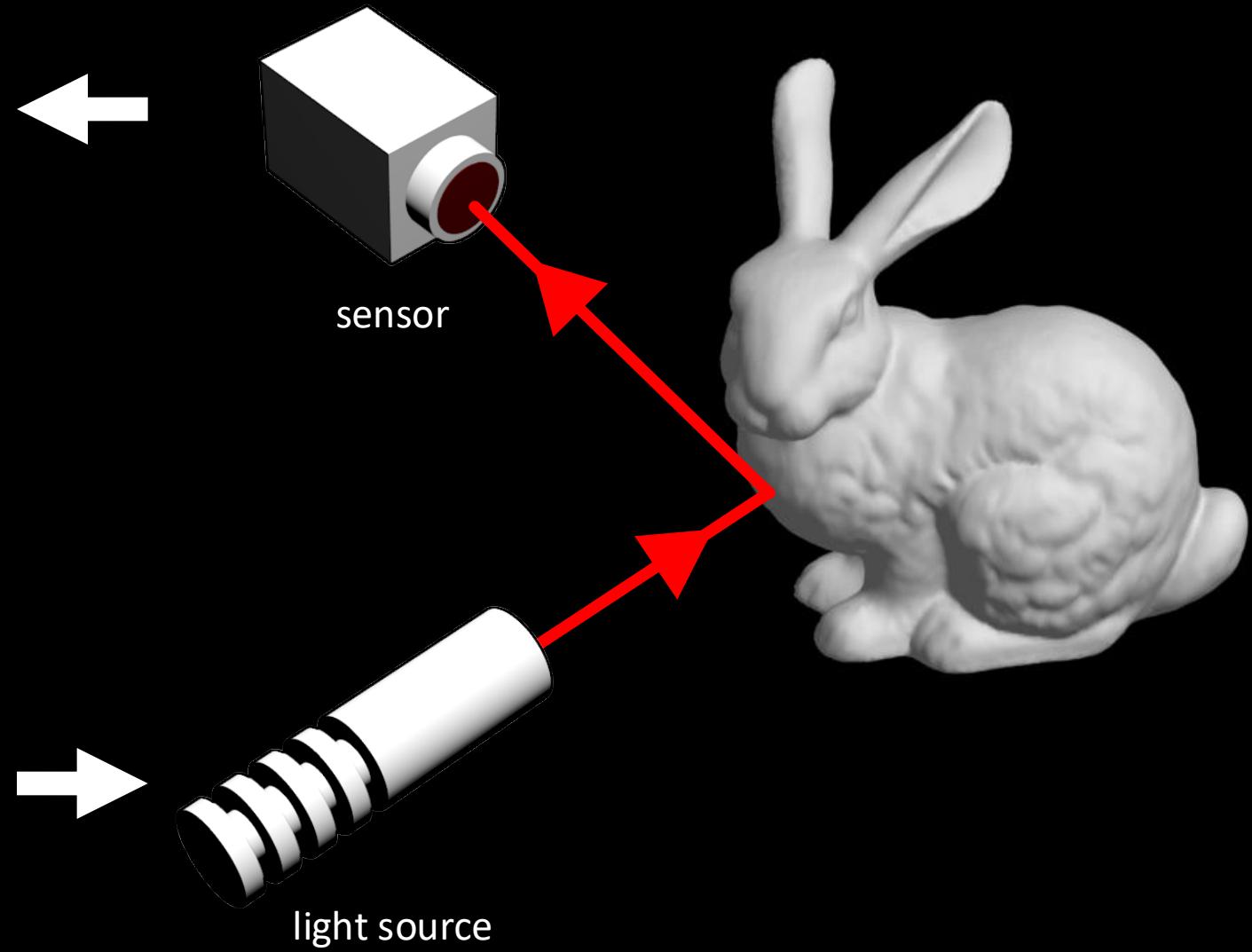
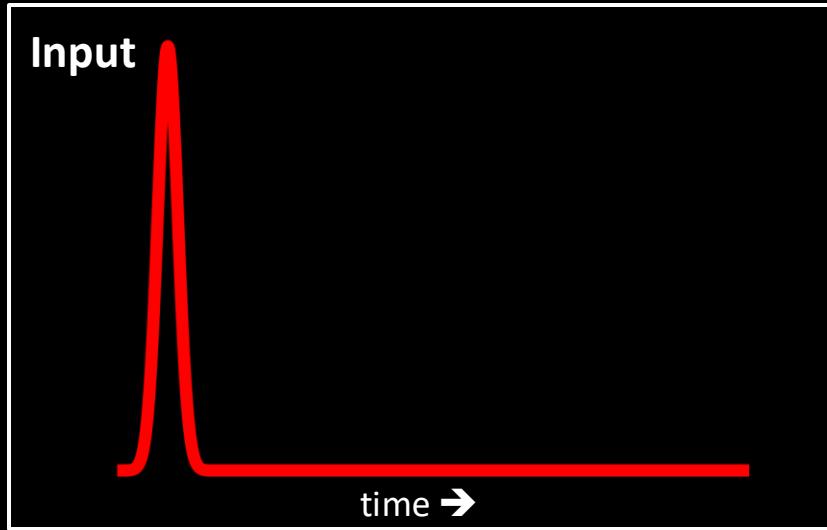
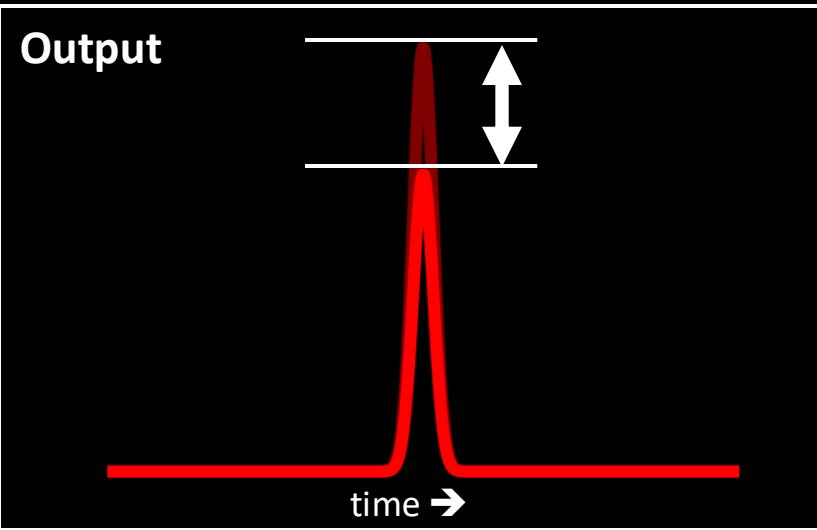
direct time-of-flight principle



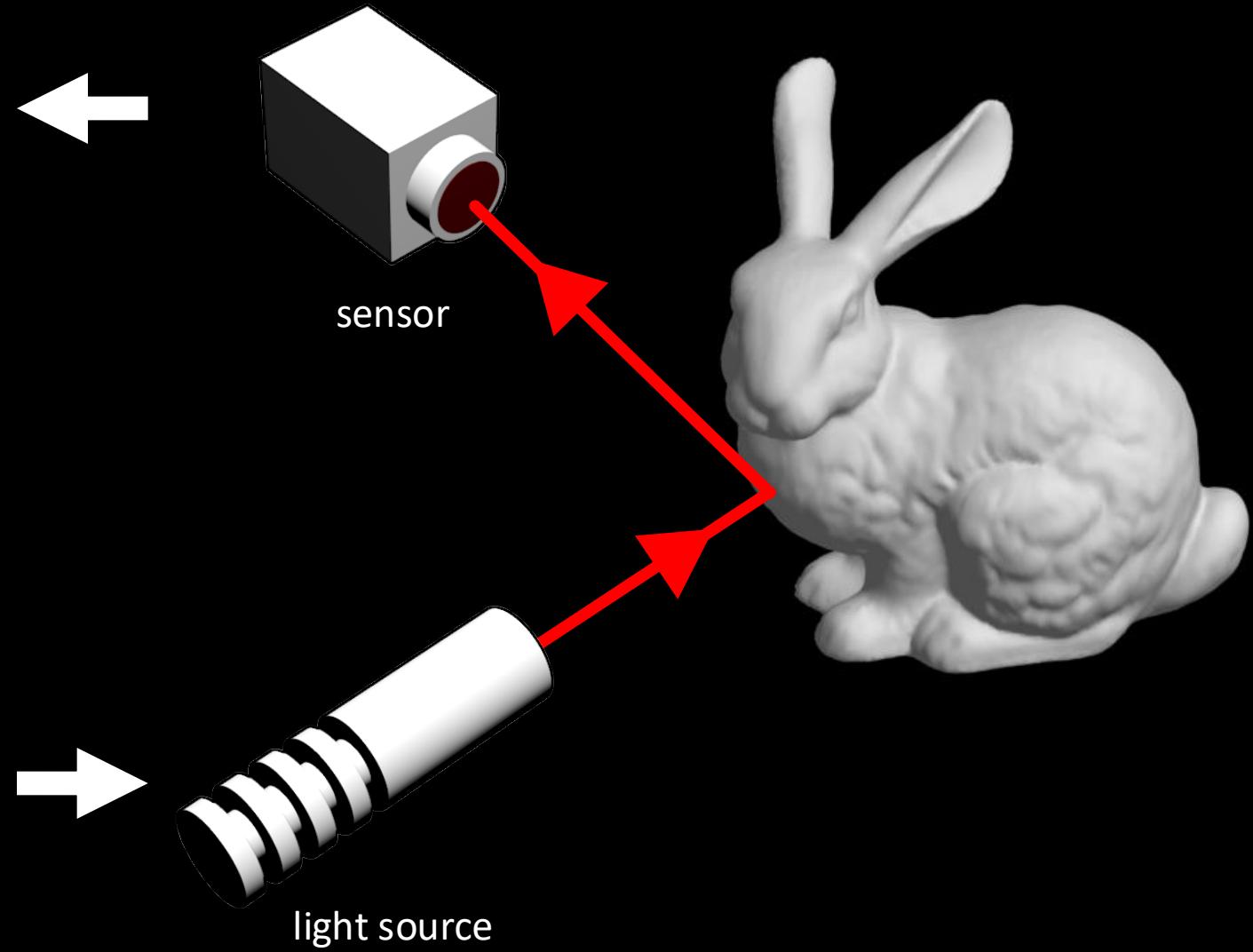
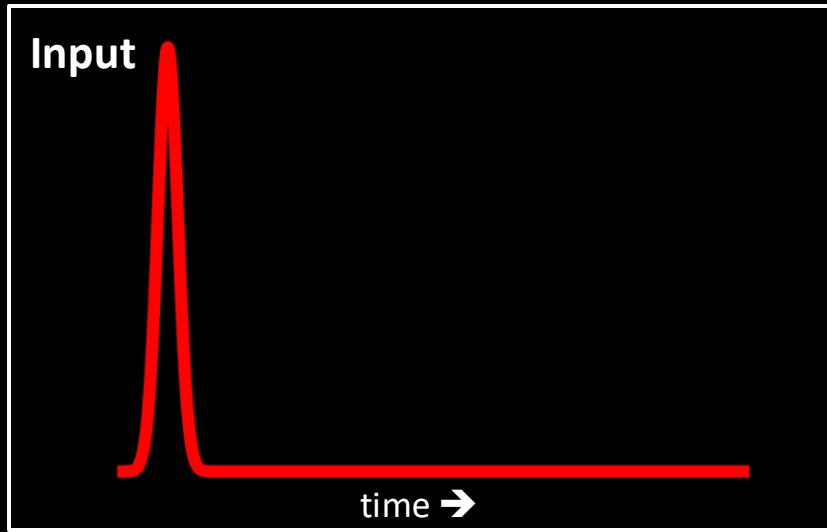
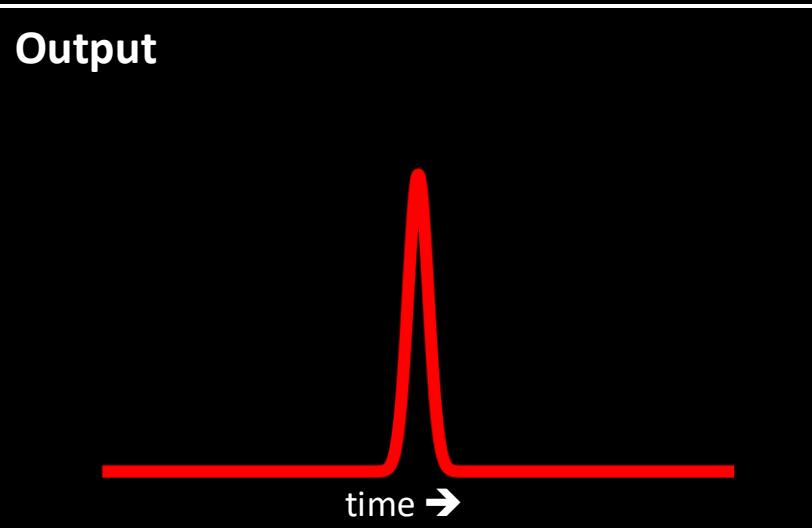
direct time-of-flight principle



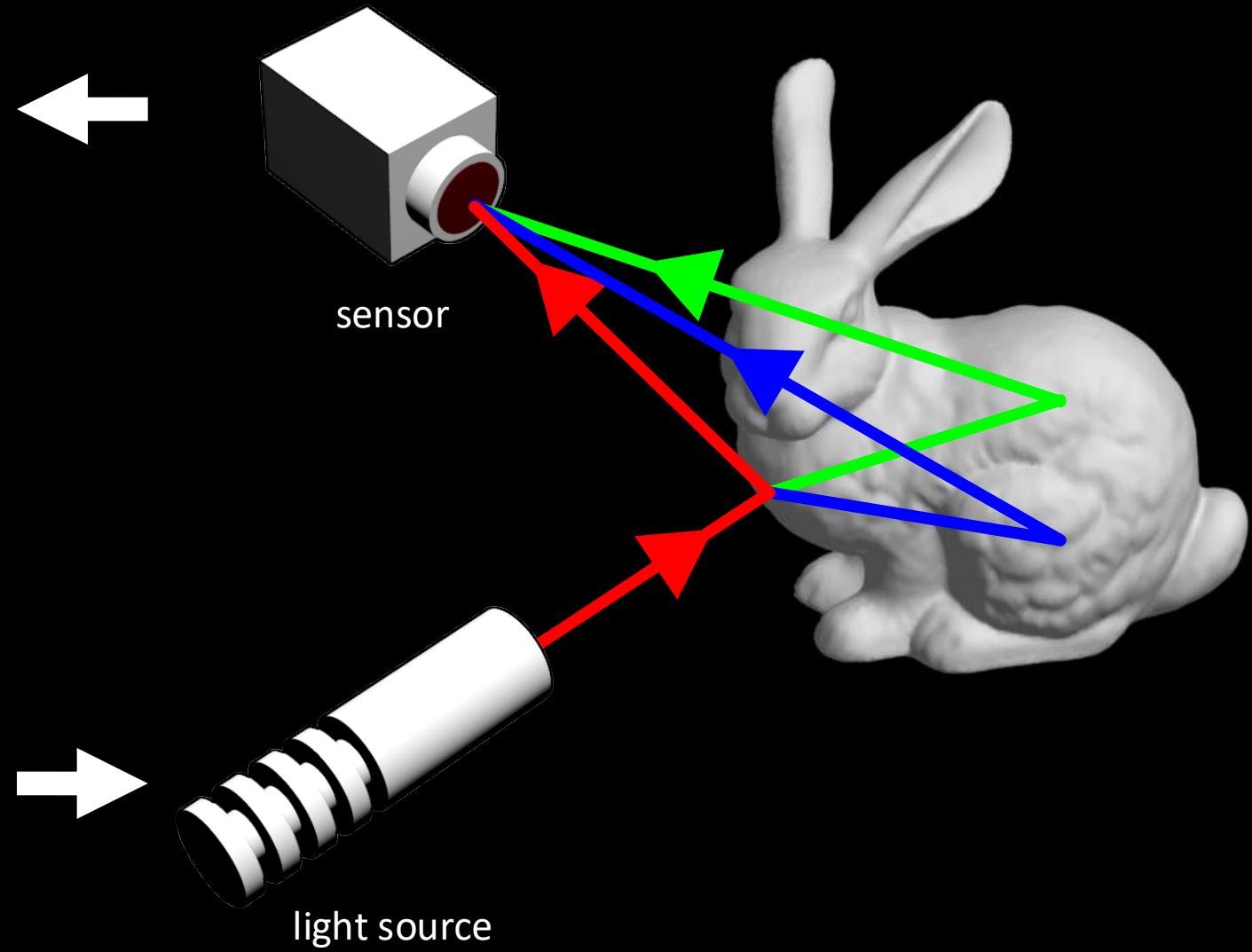
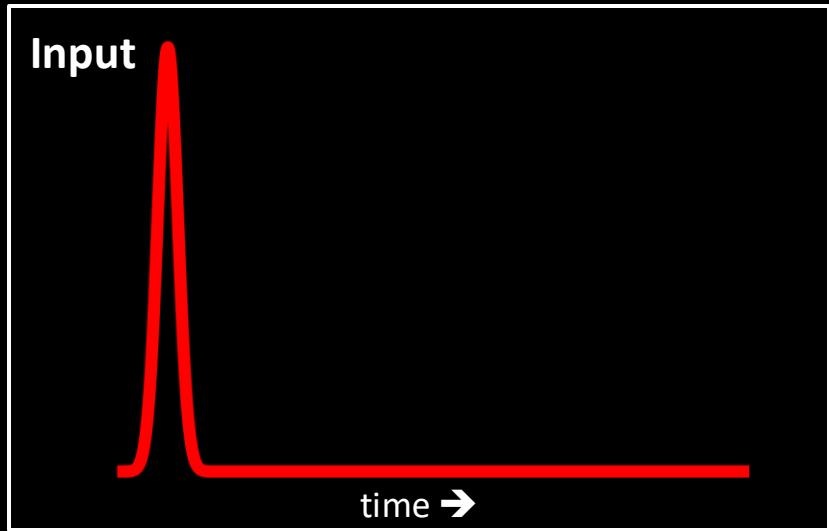
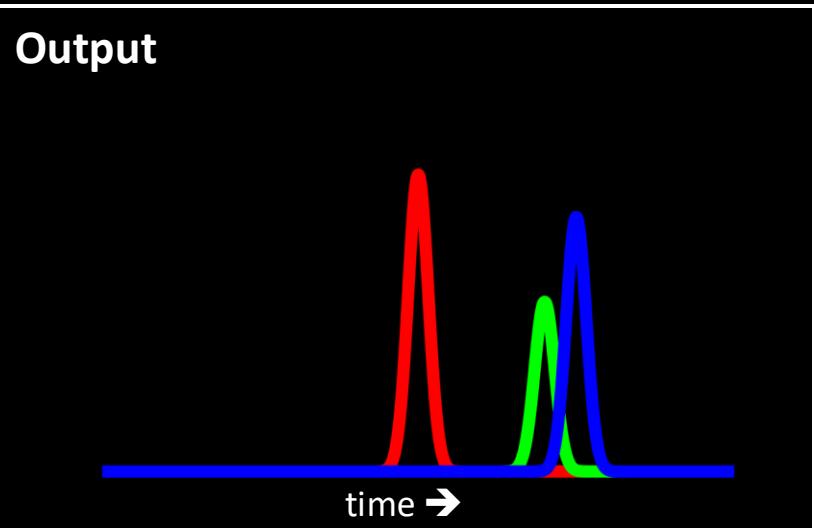
direct time-of-flight principle



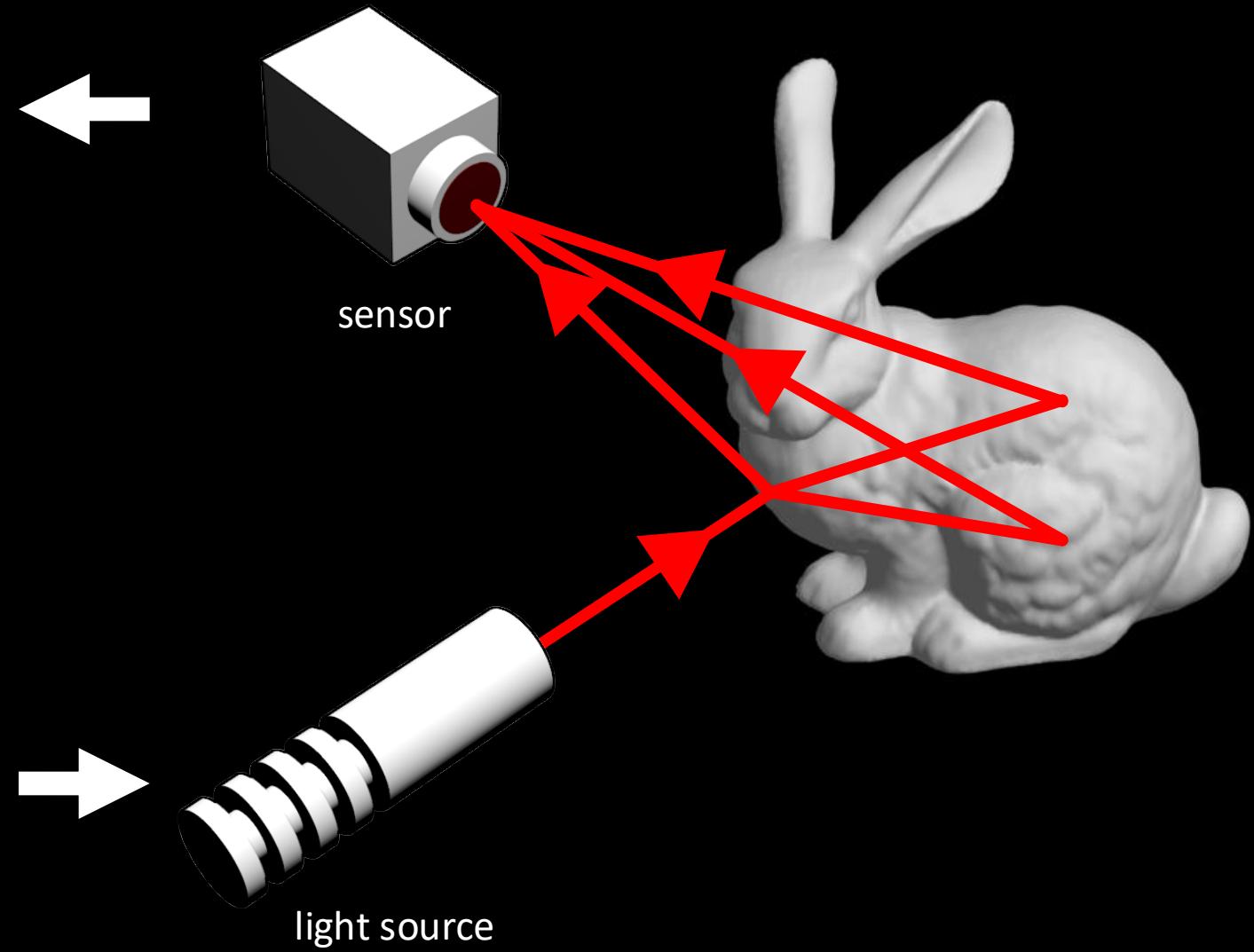
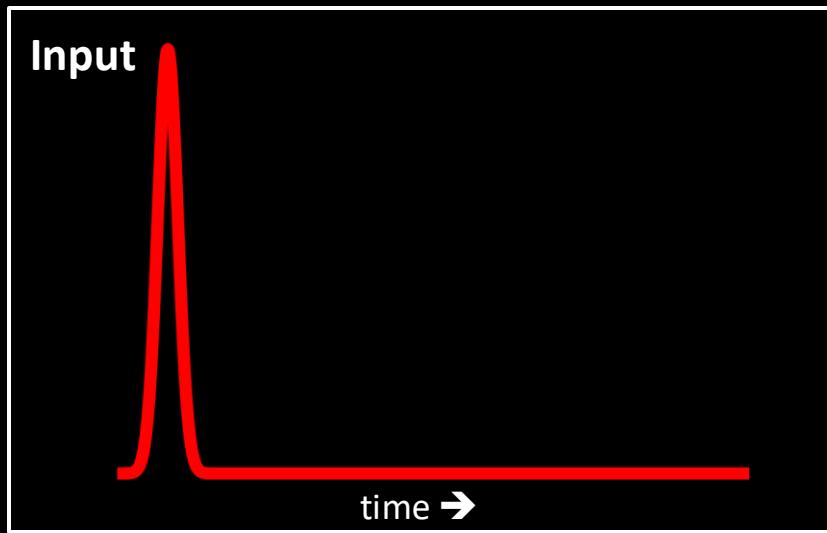
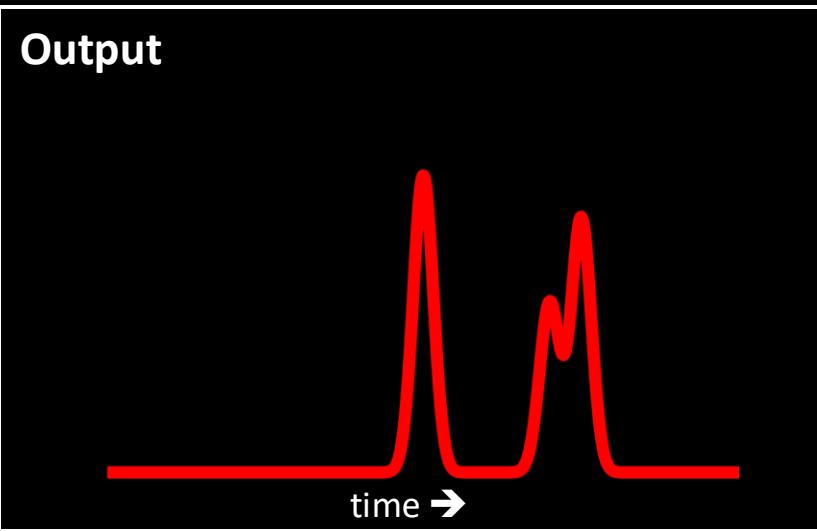
direct time-of-flight principle



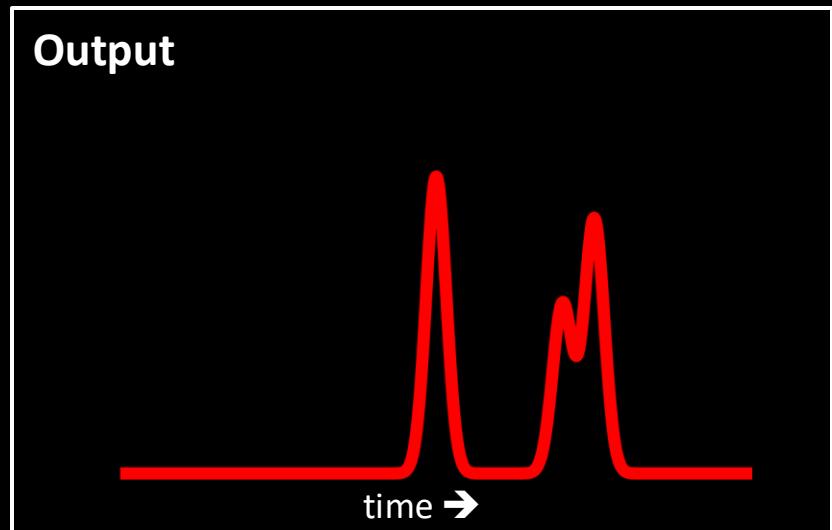
direct time-of-flight principle



direct time-of-flight principle



direct time-of-flight principle

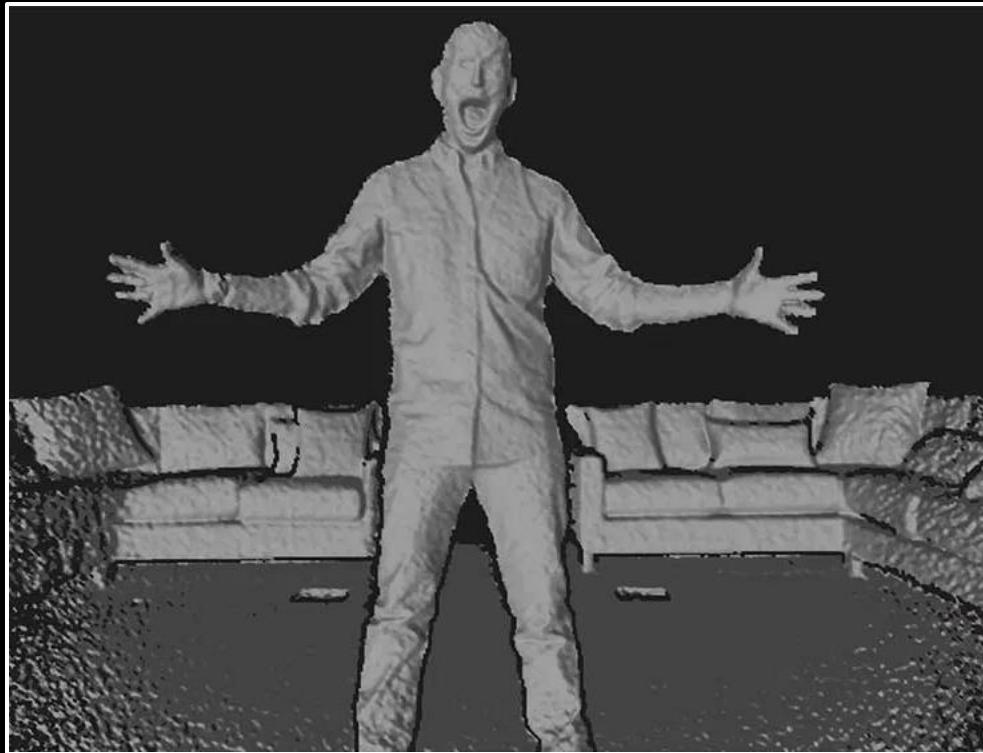


transient measurement

direct and indirect time-of-flight sensors for transient imaging

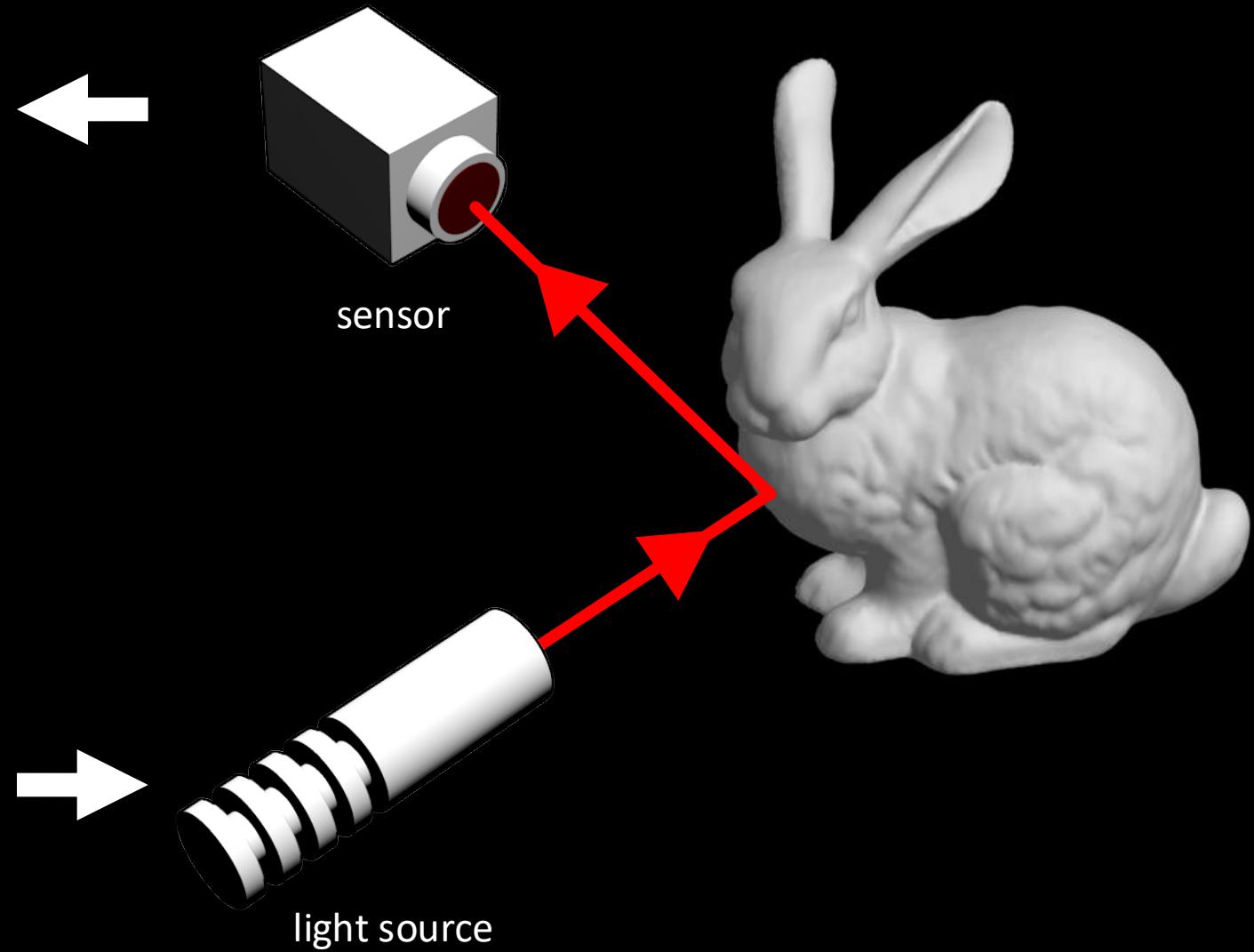
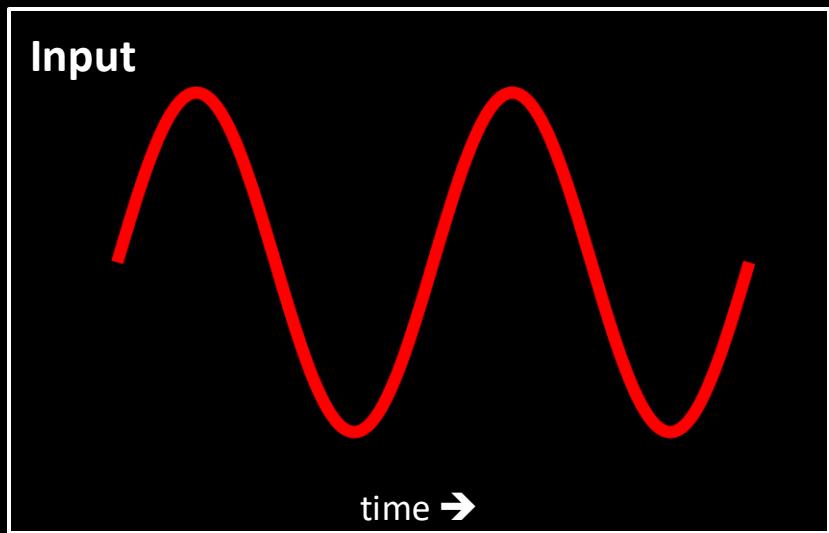
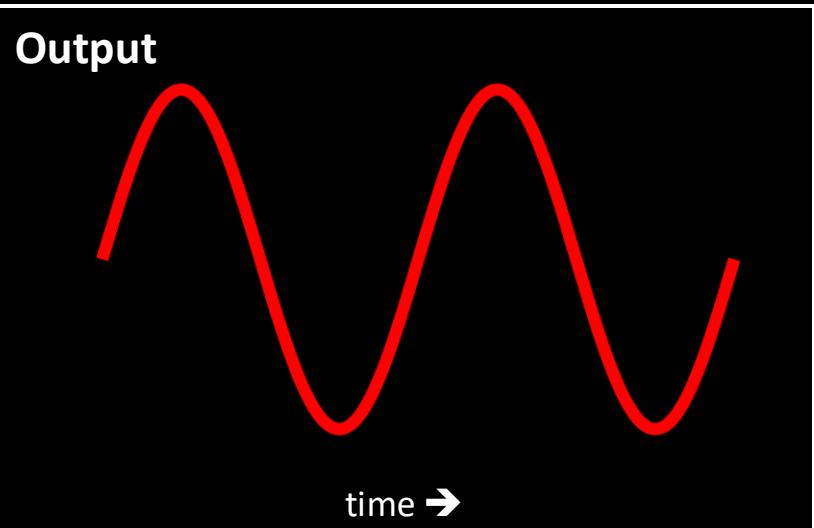


direct and indirect time-of-flight sensors for transient imaging

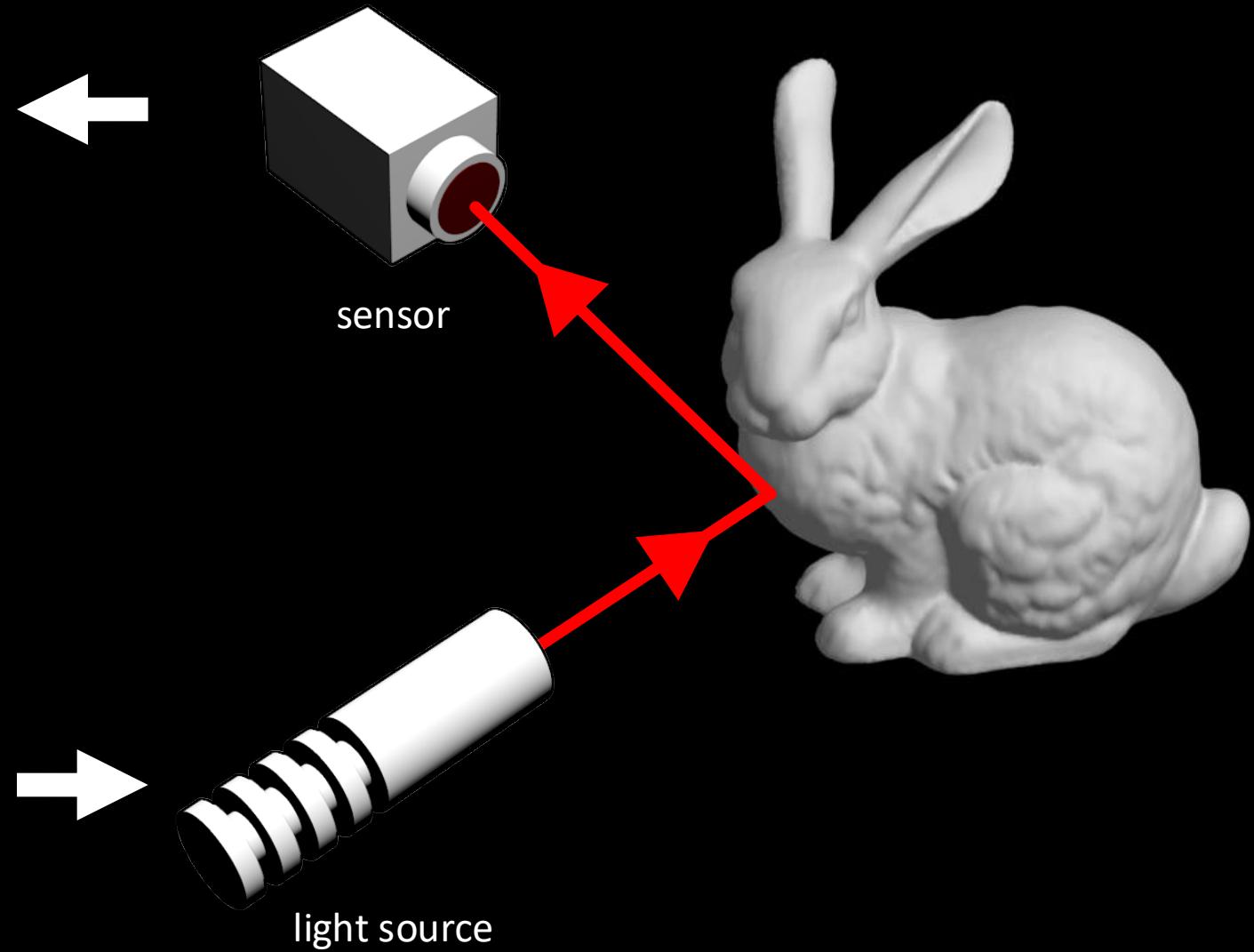
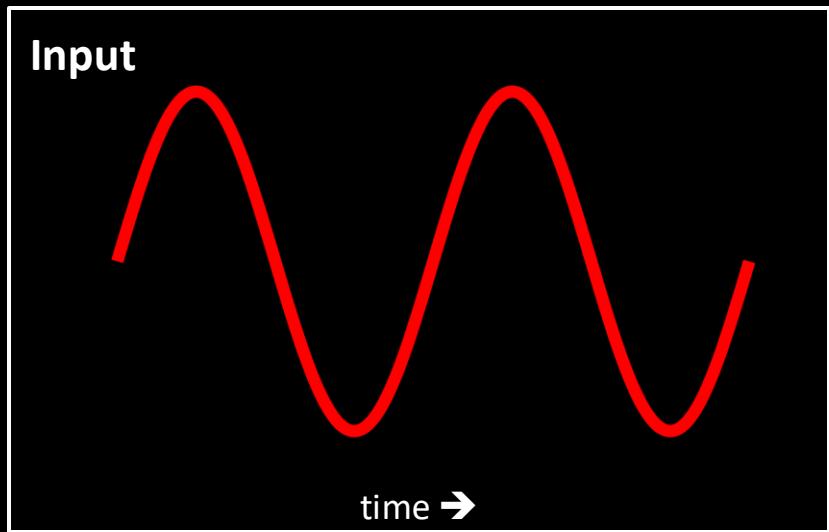
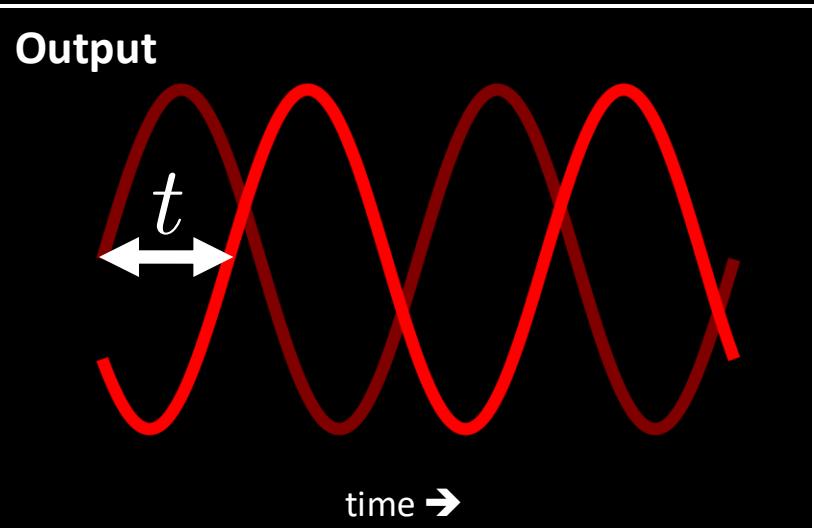


Microsoft Kinect v2

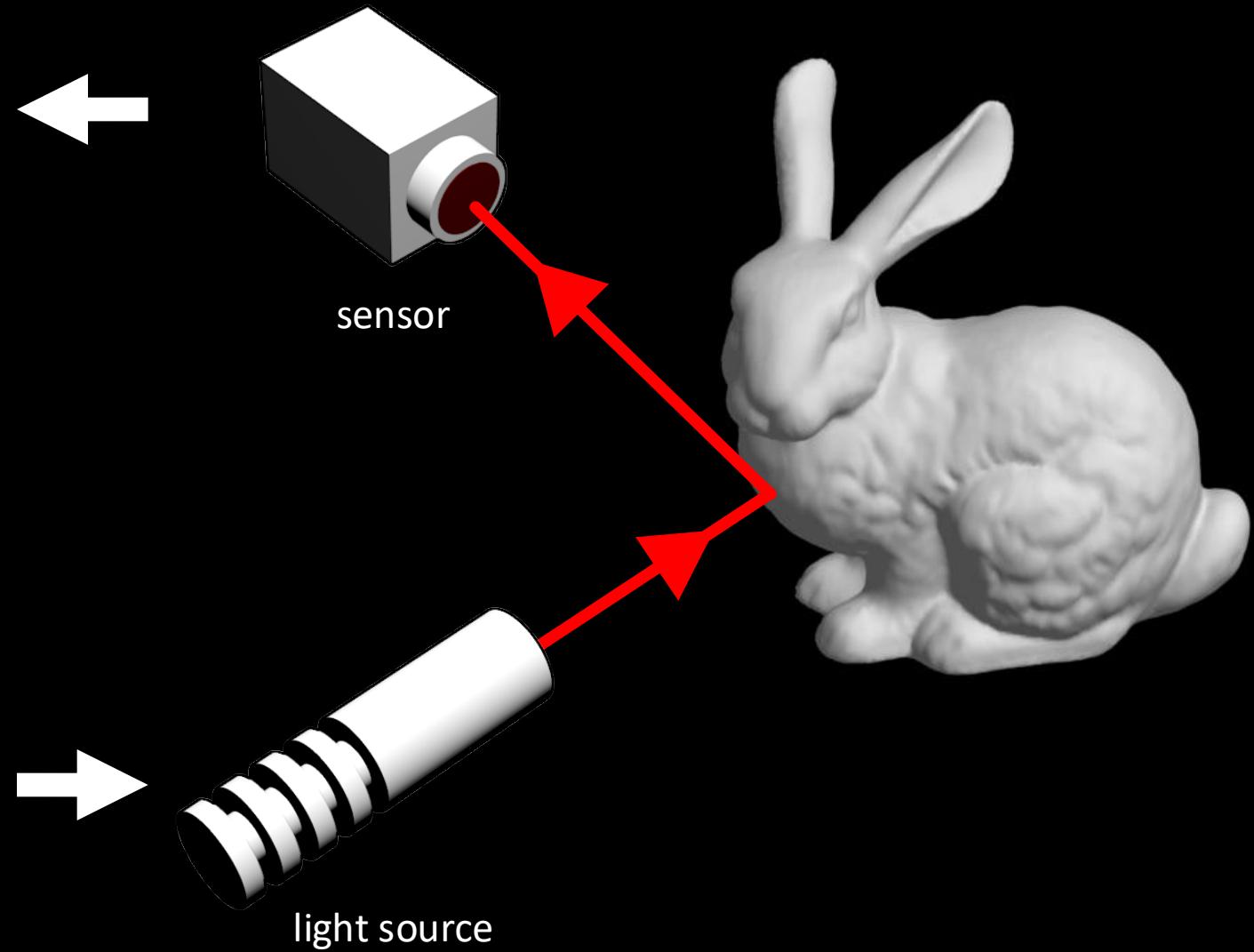
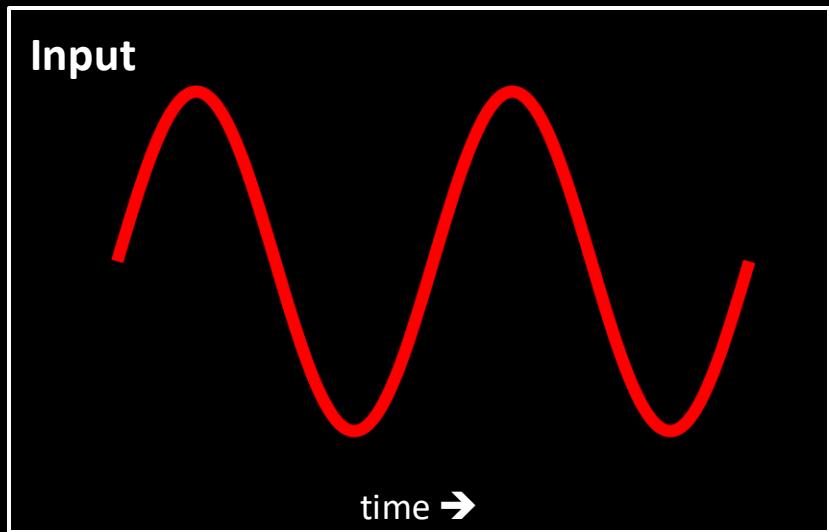
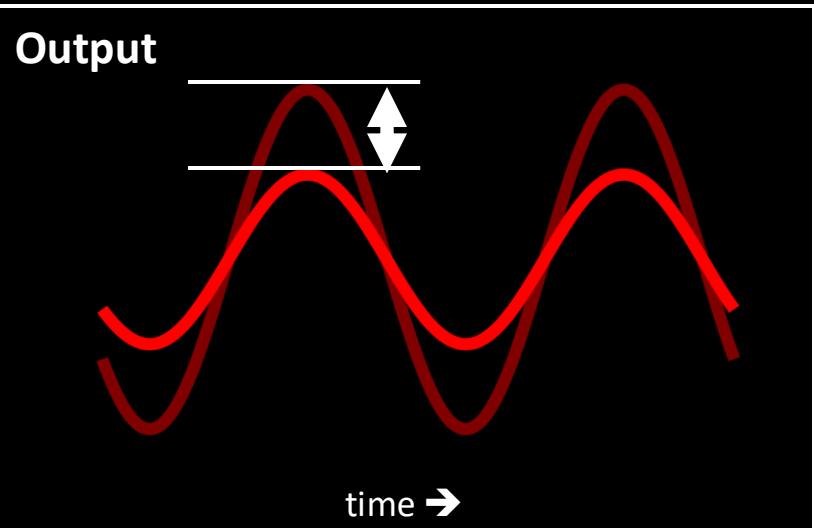
indirect time-of-flight principle



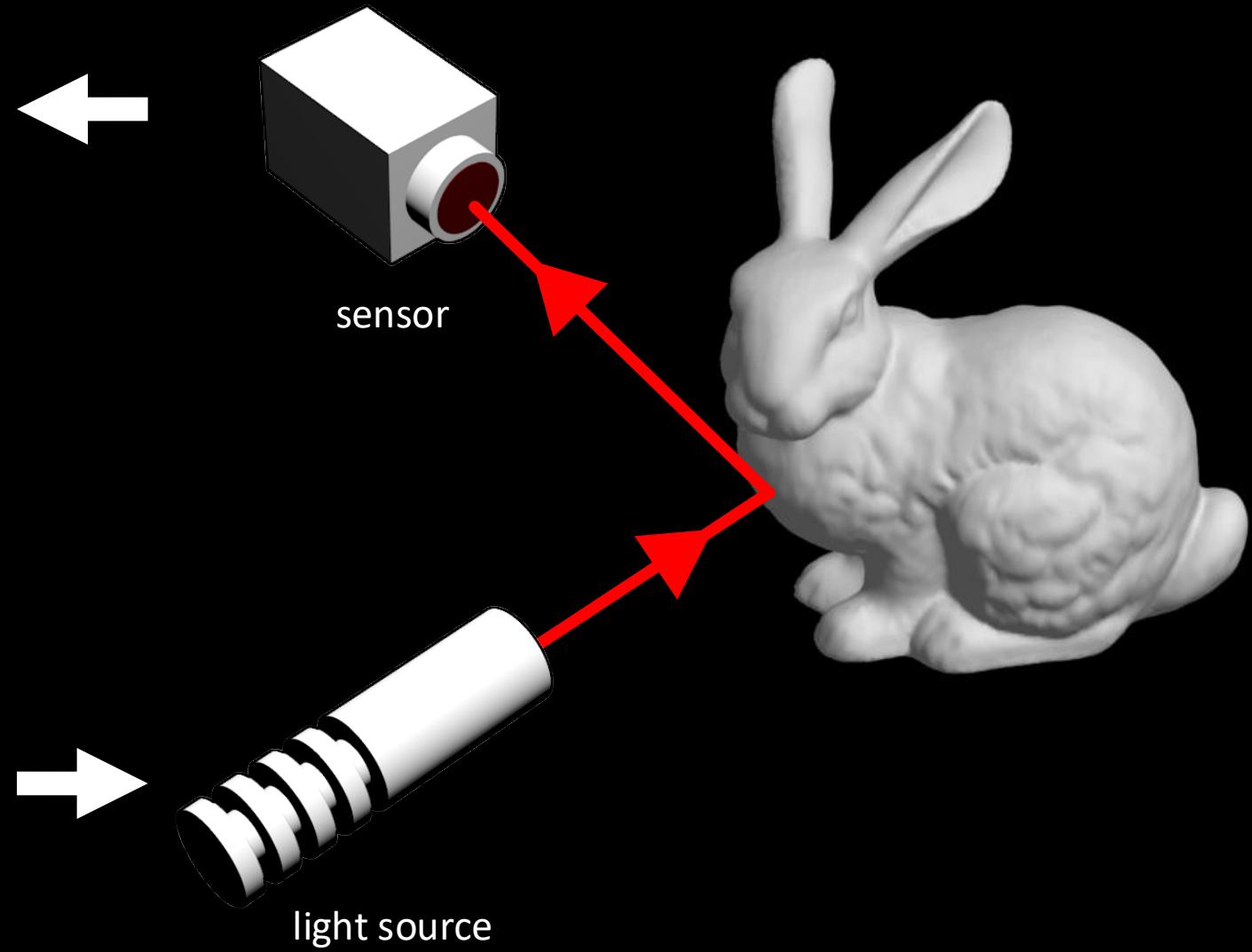
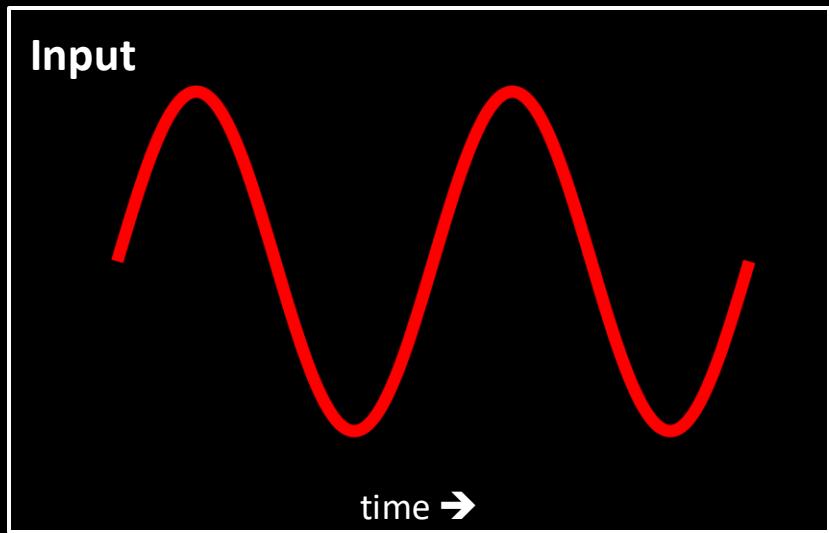
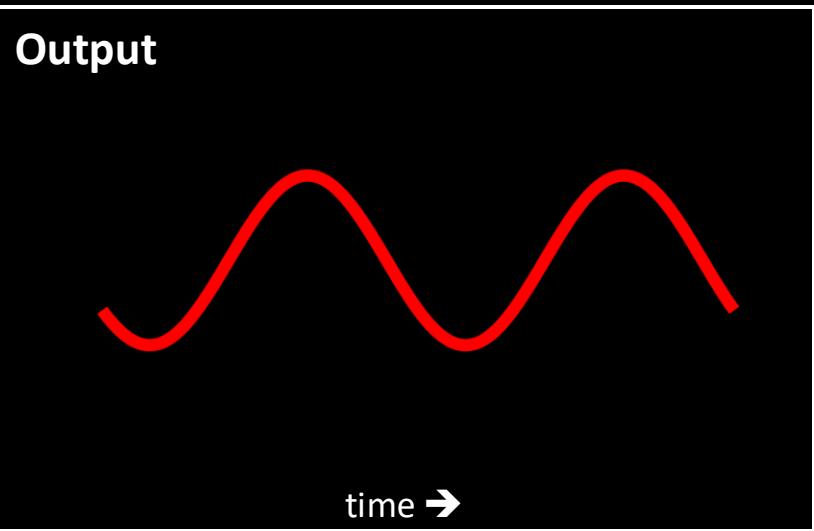
indirect time-of-flight principle



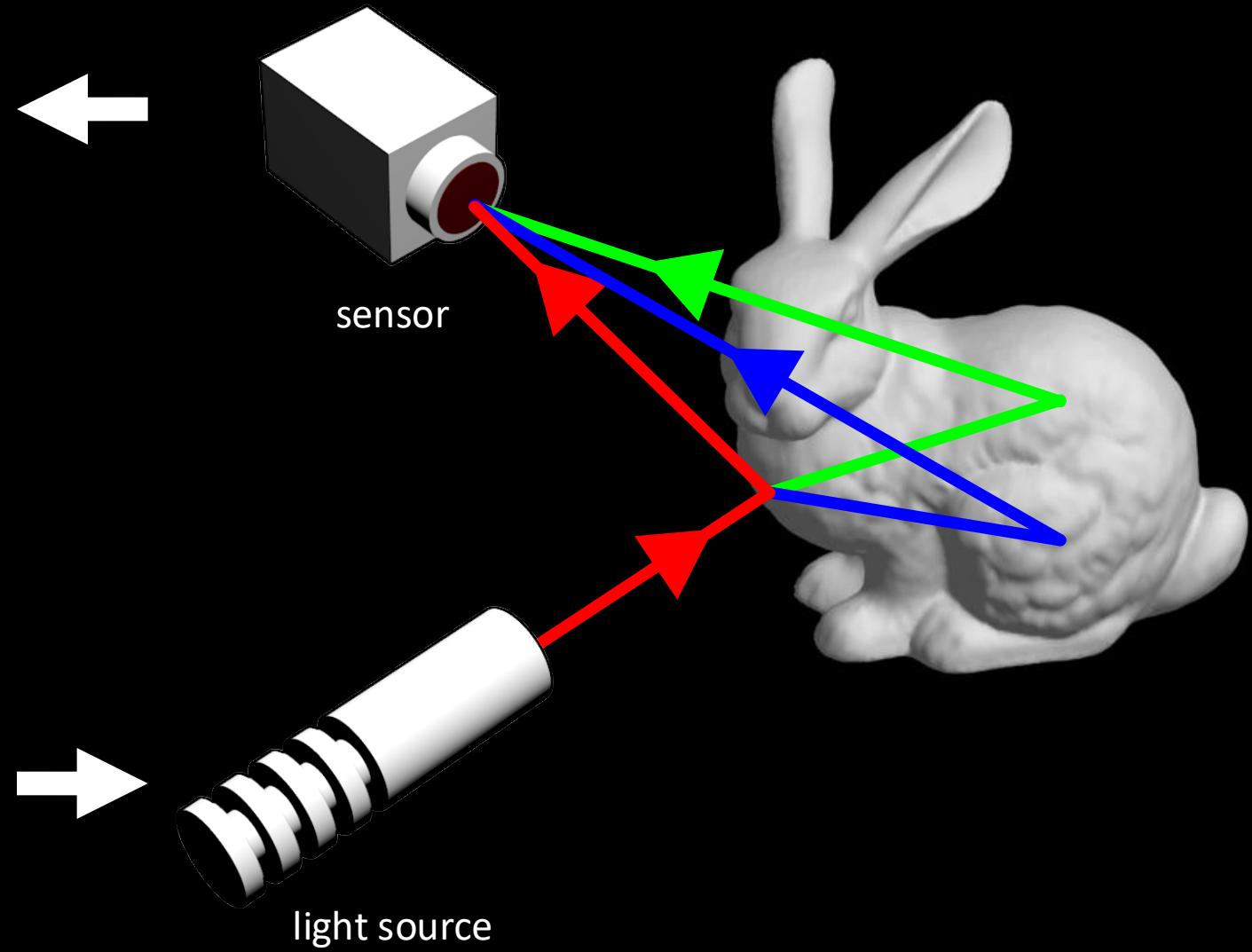
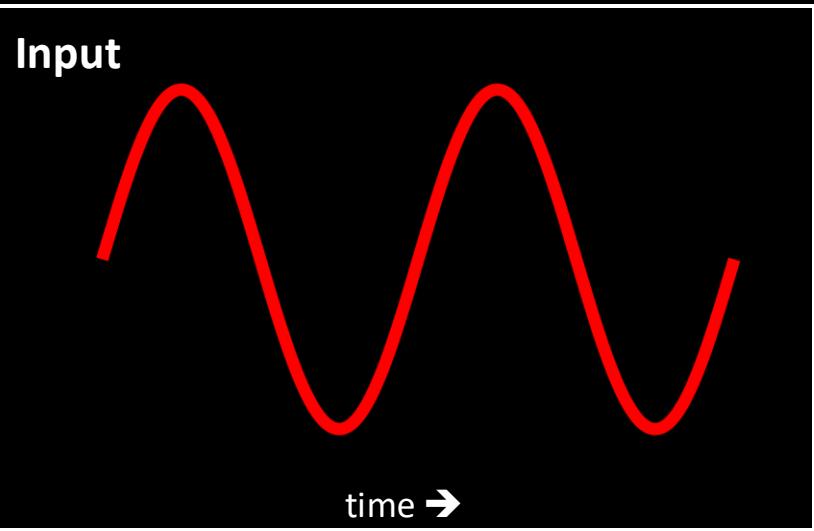
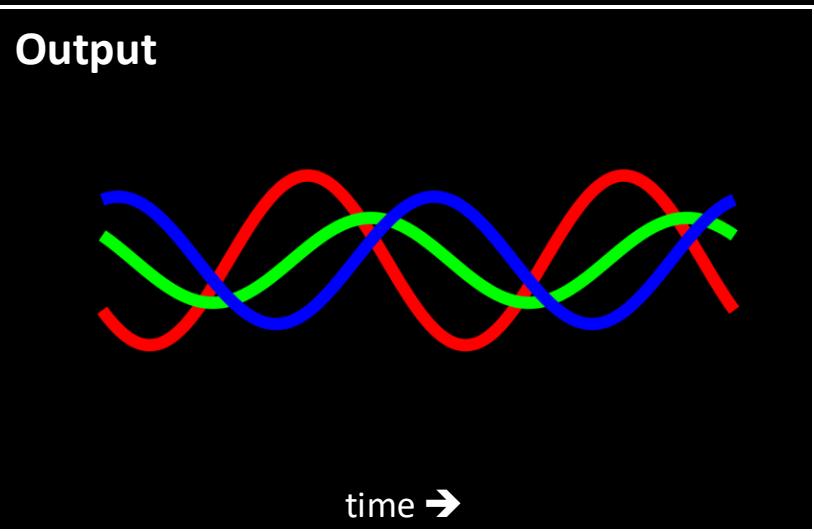
indirect time-of-flight principle



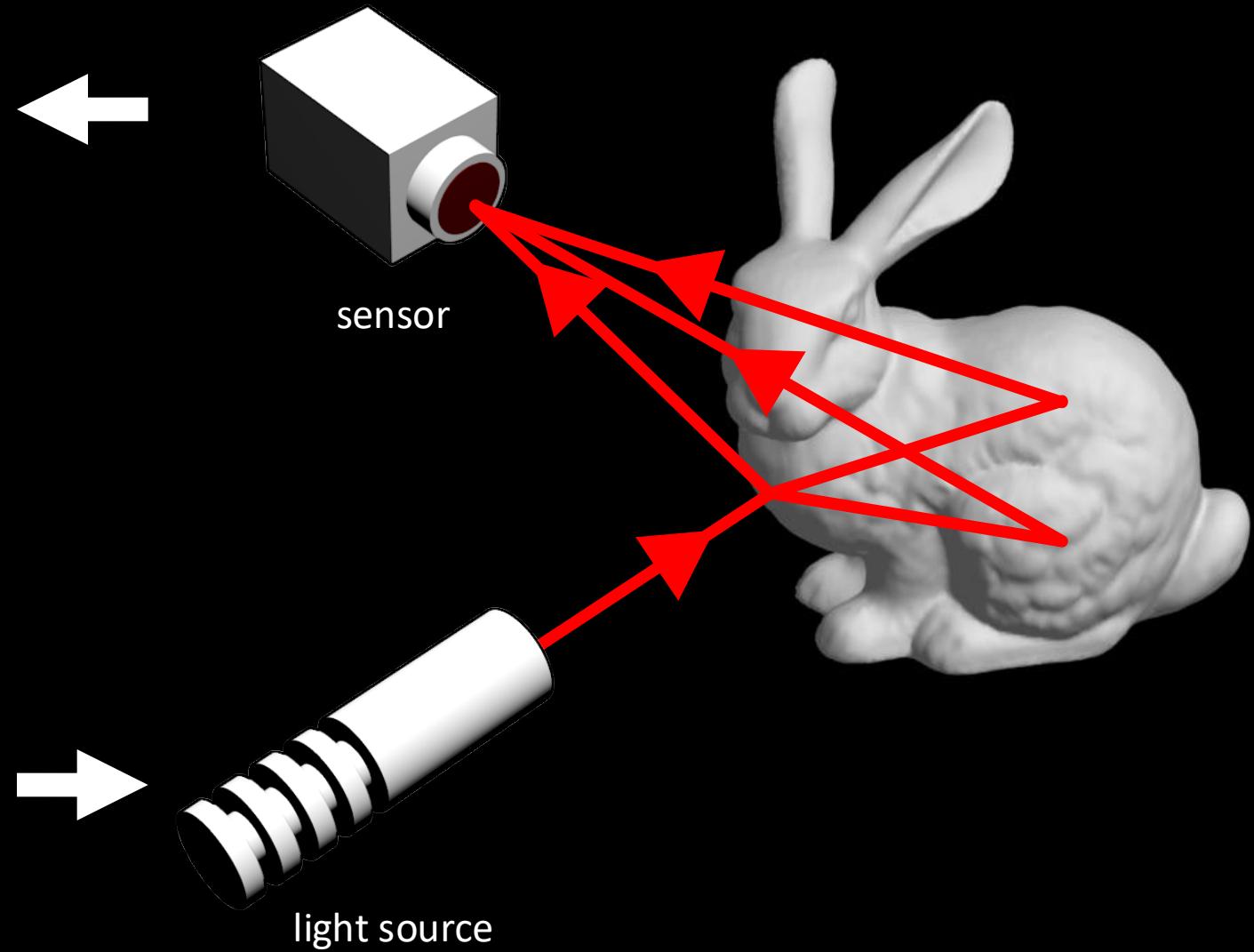
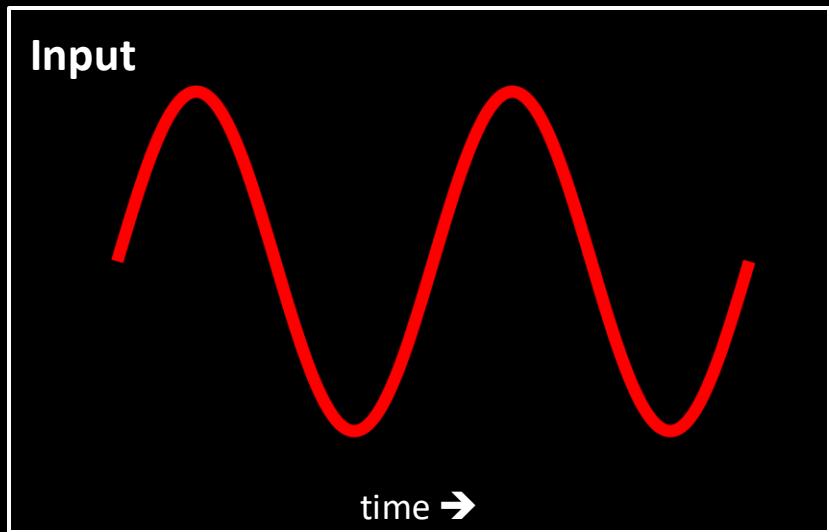
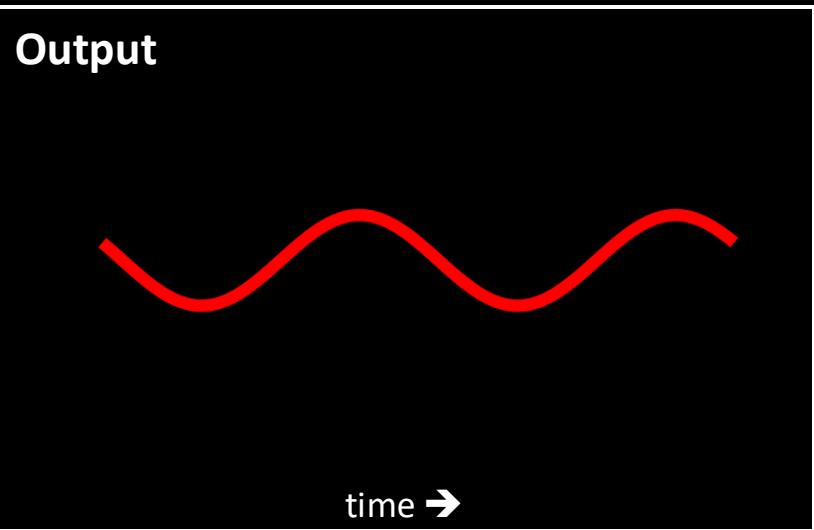
indirect time-of-flight principle



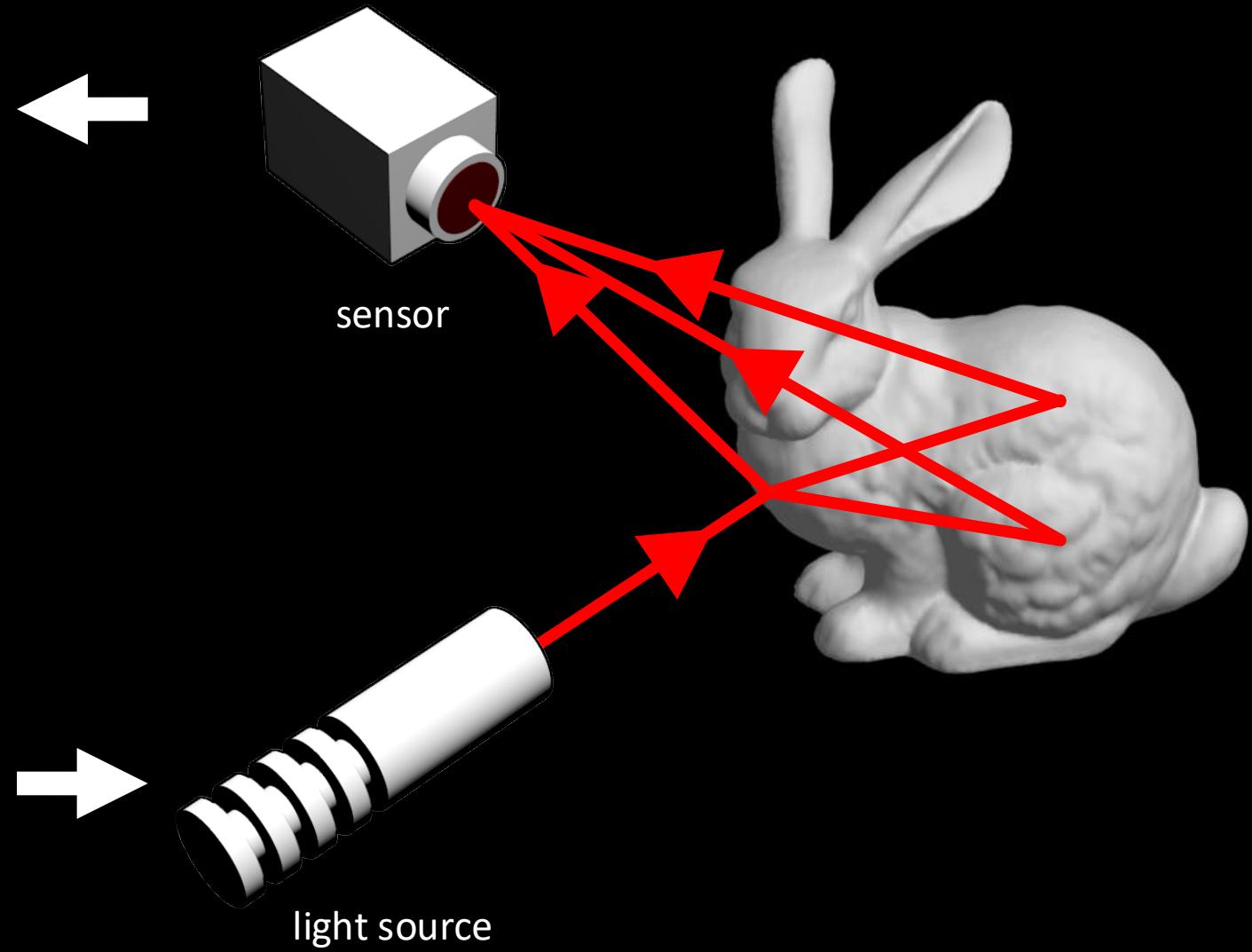
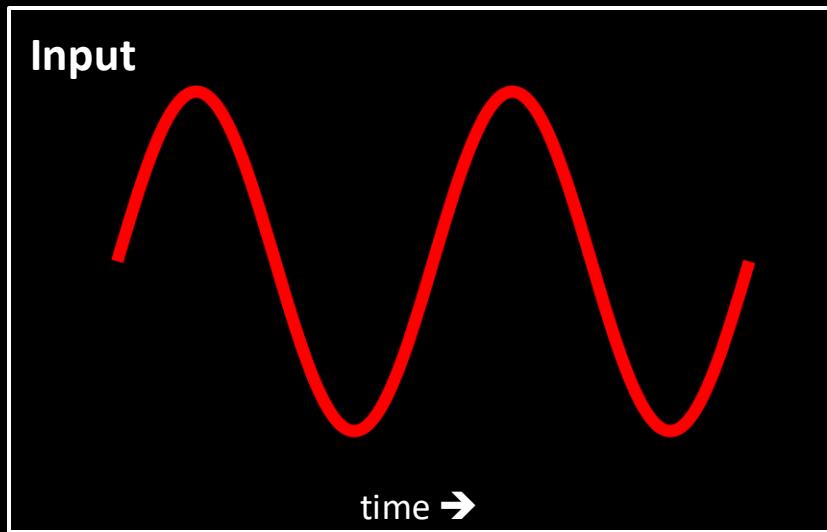
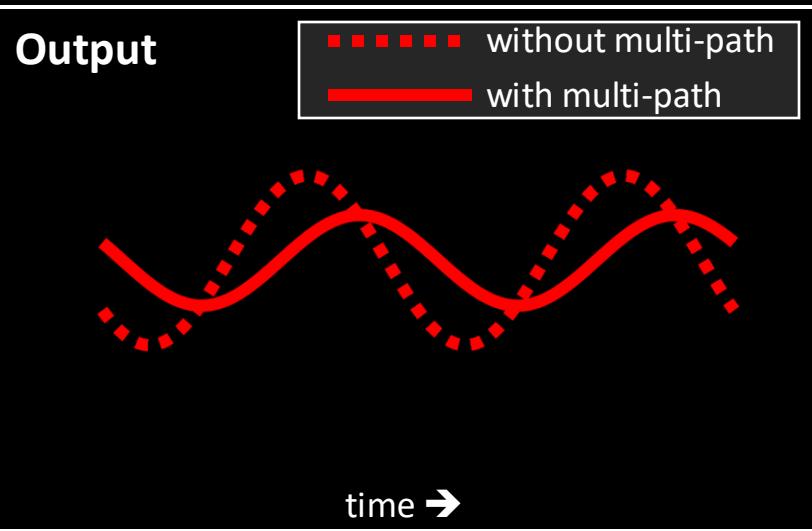
indirect time-of-flight principle



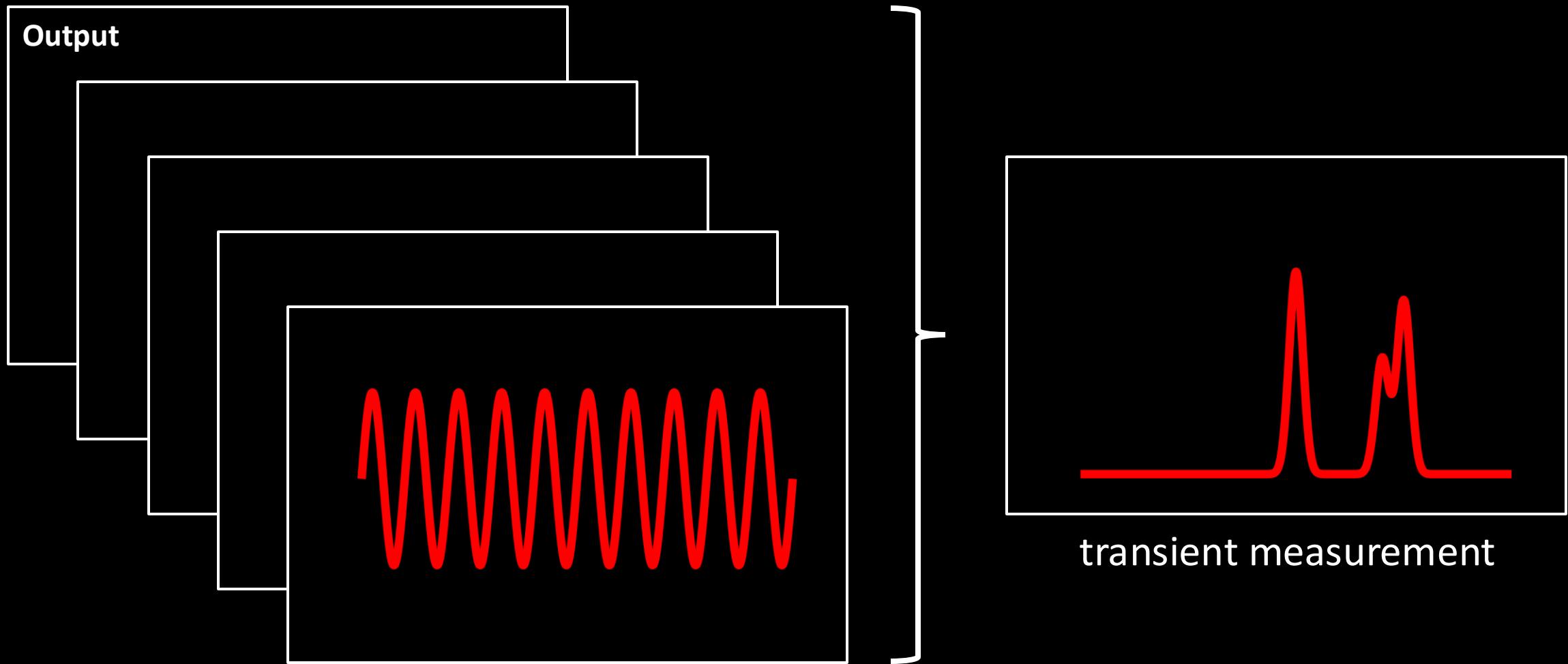
indirect time-of-flight principle



indirect time-of-flight principle



indirect time-of-flight principle



transient sensing technologies

optical coherence tomography	streak camera	single-photon avalanche diodes	time-of-flight cameras	avalanche photodiode	
1 femtosecond (10^{-15} secs)	1 picosecond (10^{-12} secs)	100 picosecond (10^{-10} secs)	1 nanosecond (10^{-9} secs)	10 nanoseconds (10^{-8} secs)	temporal resolution
quadrillion fps	trillion fps	10 billion fps	billion fps	100 million fps	frame rate
1 micron (10^{-6} meters)	1 millimeter (10^{-3} meters)	10 centimeters (10^{-1} meters)	1 meter (10^0 meters)	10 meters (10^1 meters)	distance travelled

transient sensing technologies

optical coherence tomography	streak camera (direct)	single-photon avalanche diodes (direct)	time-of-flight cameras	avalanche photodiode (direct)	temporal resolution
1 femtosecond (10^{-15} secs)	1 picosecond (10^{-12} secs)	100 picosecond (10^{-10} secs)	1 nanosecond (10^{-9} secs)	10 nanoseconds (10^{-8} secs)	
quadrillion fps	trillion fps	10 billion fps	billion fps	100 million fps	frame rate
1 micron (10^{-6} meters)	1 millimeter (10^{-3} meters)	10 centimeters (10^{-1} meters)	1 meter (10^0 meters)	10 meters (10^1 meters)	distance travelled

transient sensing technologies

optical coherence
tomography

1 femtosecond
(10^{-15} secs)

quadrillion fps

1 micron
(10^{-6} meters)

streak camera

(direct)

1 picosecond
(10^{-12} secs)

trillion fps

1 millimeter
(10^{-3} meters)

10 centimeters
(10^{-1} meters)

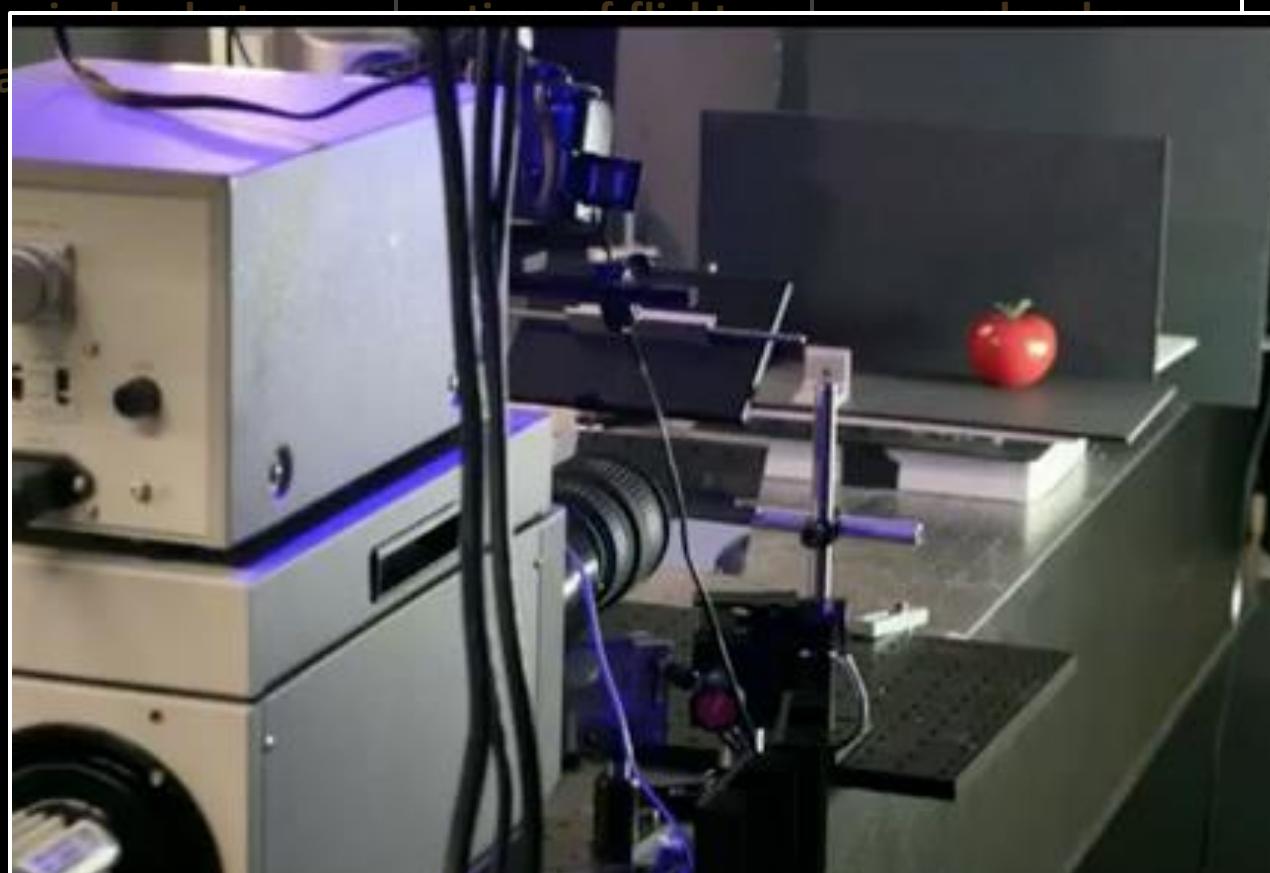
1 meter
(10^0 meters)

10 meters
(10^1 meters)

**temporal
resolution**

frame rate

**distance
travelled**



transient sensing technologies

optical coherence tomography	streak camera	single-photon avalanche diodes (direct)	time-of-flight cameras	avalanche photodiode (direct)	temporal resolution
					frame rate
					distance travelled



Micro Photon Devices

transient sensing technologies

optical coherence
tomography

1 femtosecond
(10^{-15} secs)

quadrillion fps

1 micron
(10^{-6} meters)

streak camera

(direct)

1 picosecond
(10^{-12} secs)

trillion fps

1 millimeter
(10^{-3} meters)

single-photon
avalanche diodes

time-of-flight
cameras

avalanche
photodiode

(direct)

10 nanoseconds
(10^{-8} secs)

temporal
resolution

100 million fps

frame rate

10 meters
(10^1 meters)

distance
travelled



transient sensing technologies

optical coherence tomography (indirect)	streak camera (direct)	single-photon avalanche diodes (direct)	time-of-flight cameras (indirect)	avalanche photodiode (direct)	temporal resolution
1 femtosecond (10^{-15} secs)	1 picosecond (10^{-12} secs)	100 picosecond (10^{-10} secs)	1 nanosecond (10^{-9} secs)	10 nanoseconds (10^{-8} secs)	frame rate
quadrillion fps	trillion fps	10 billion fps	billion fps	100 million fps	distance travelled
1 micron (10^{-6} meters)	1 millimeter (10^{-3} meters)	10 centimeters (10^{-1} meters)	1 meter (10^0 meters)	10 meters (10^1 meters)	

transient sensing technologies

**optical coherence
tomography**
(indirect)

1 femtosecond
(10^{-15} secs)

quadrillion fps

1 micron
(10^{-6} meters)

single-photon

time-of-flight

avalanche
photodiode

(direct)

10 nanoseconds
(10^{-8} secs)

**temporal
resolution**

100 million fps

frame rate

Gkioulekas et al. [2015]

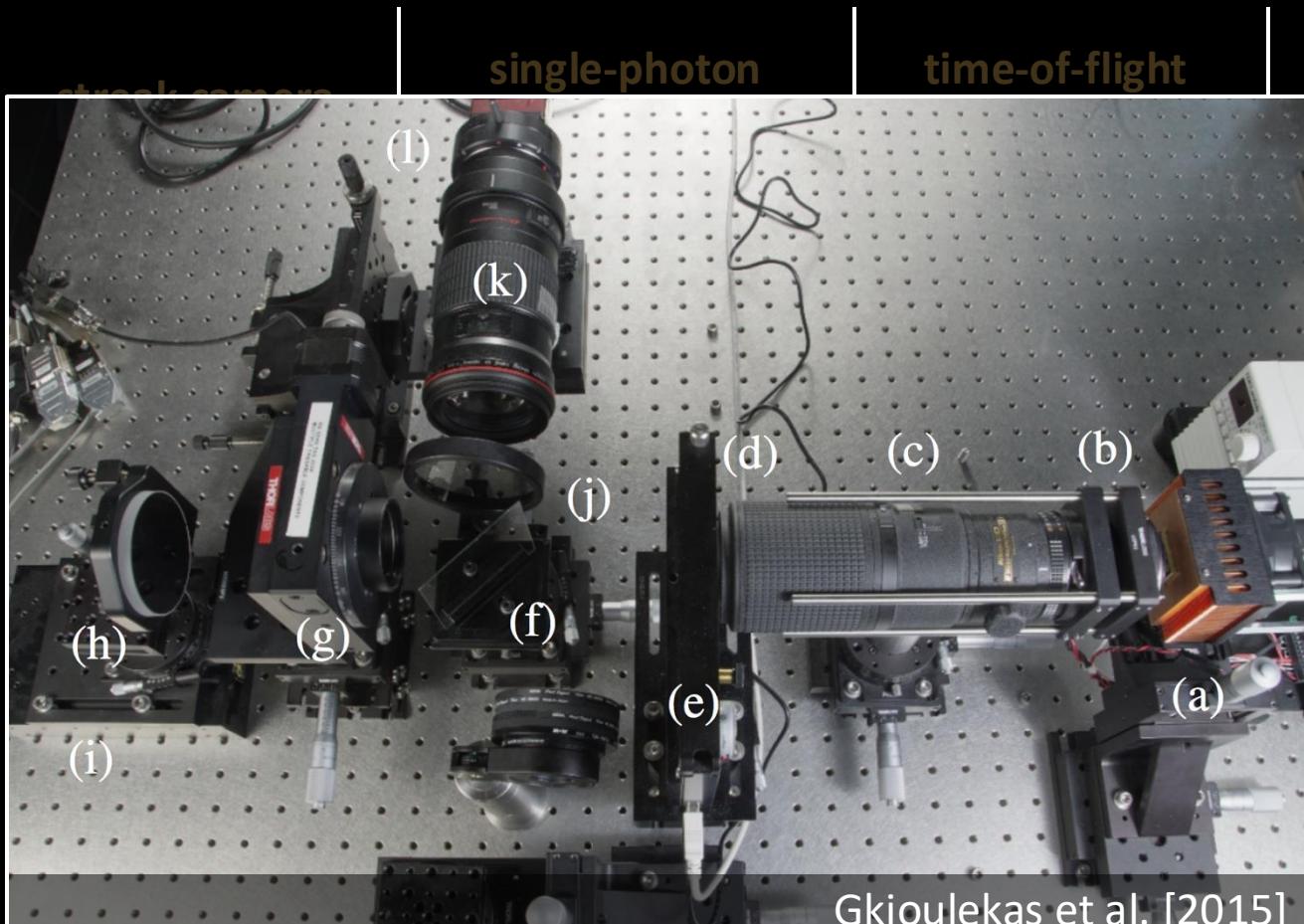
1 millimeter
(10^{-3} meters)

10 centimeters
(10^{-1} meters)

1 meter
(10^0 meters)

10 meters
(10^1 meters)

**distance
travelled**



transient sensing technologies

optical coherence
tomography
(indirect)

streak camera
(direct)

single-photon
avalanche diodes
(direct)

time-of-flight
cameras
(indirect)

avalanche
photodiode
(direct)

temporal
resolution

frame rate

distance
travelled



Heide et al. [2013]

1 micron
(10^{-6} meters)

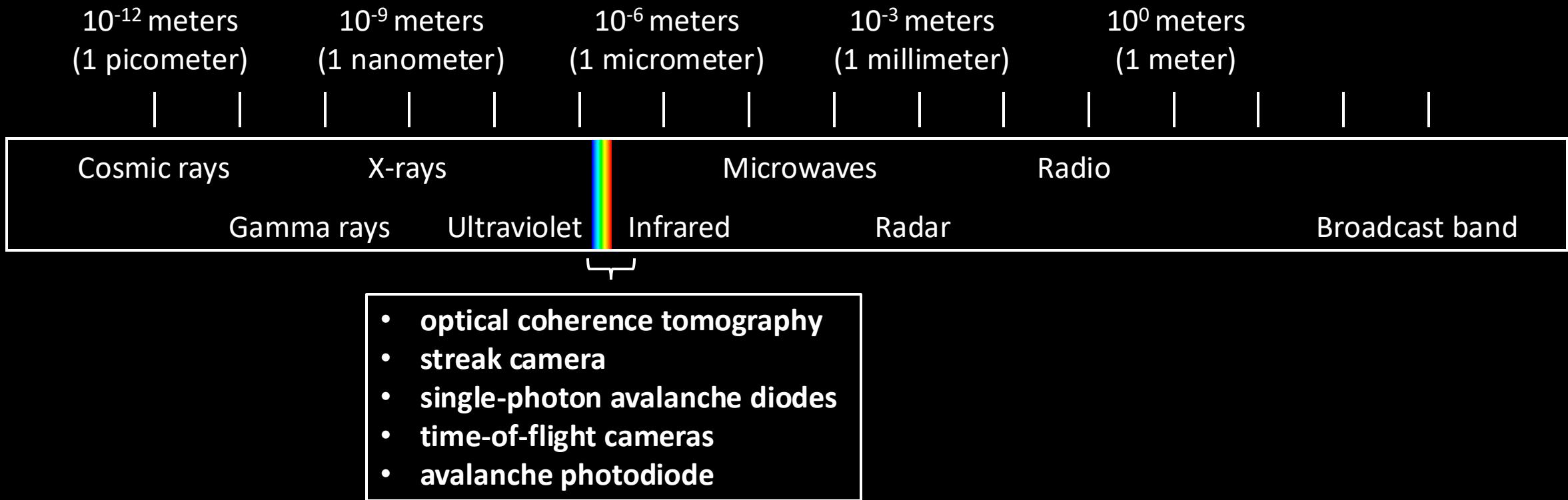
1 millimeter
(10^{-3} meters)

10 centimeters
(10^{-1} meters)

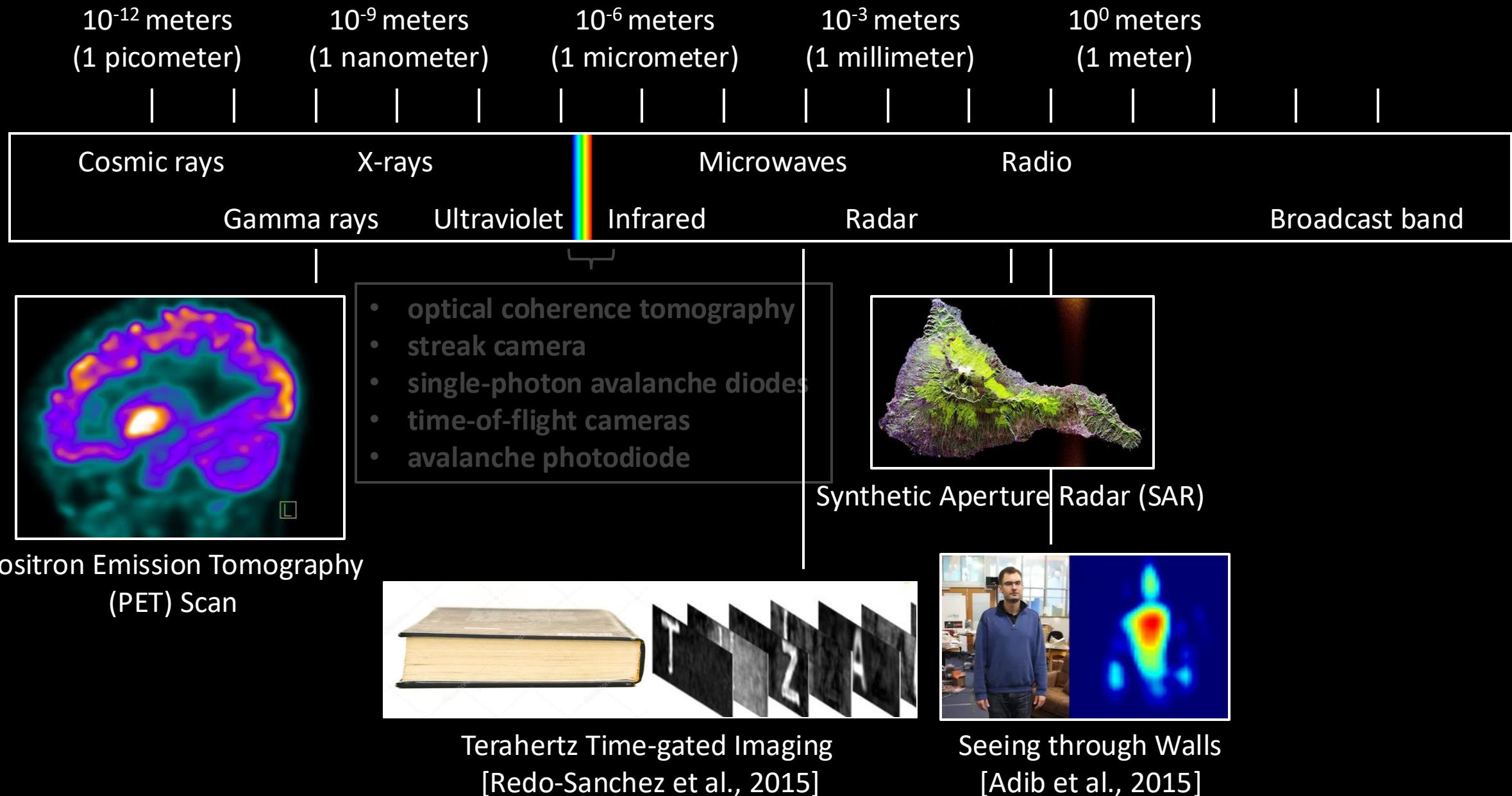
1 meter
(10^0 meters)

10 meters
(10^1 meters)

spectrum of transient sensing technologies



spectrum of transient sensing technologies



spectrum of transient sensing technologies

10^{-12} meters
(1 picometer)

10^{-9} meters
(1 nanometer)

10^{-6} meters
(1 micrometer)

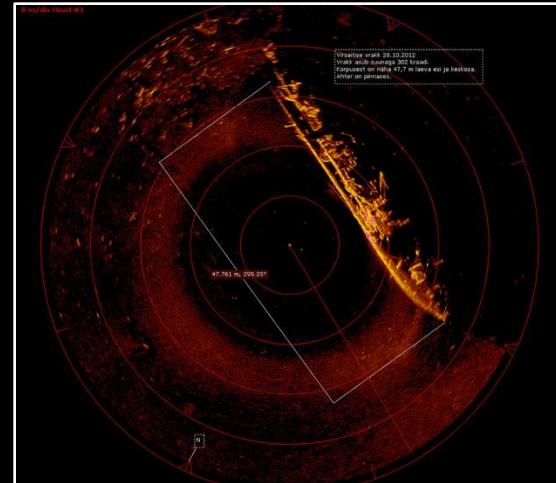
10^{-3} meters
(1 millimeter)

10^0 meters
(1 meter)

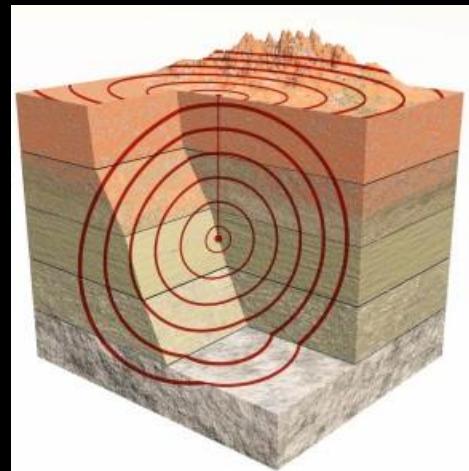
mechanical waves (e.g., acoustic, seismic)



Ultrasound Imaging



SONAR
(Sound Navigation and Ranging)



Seismic Imaging

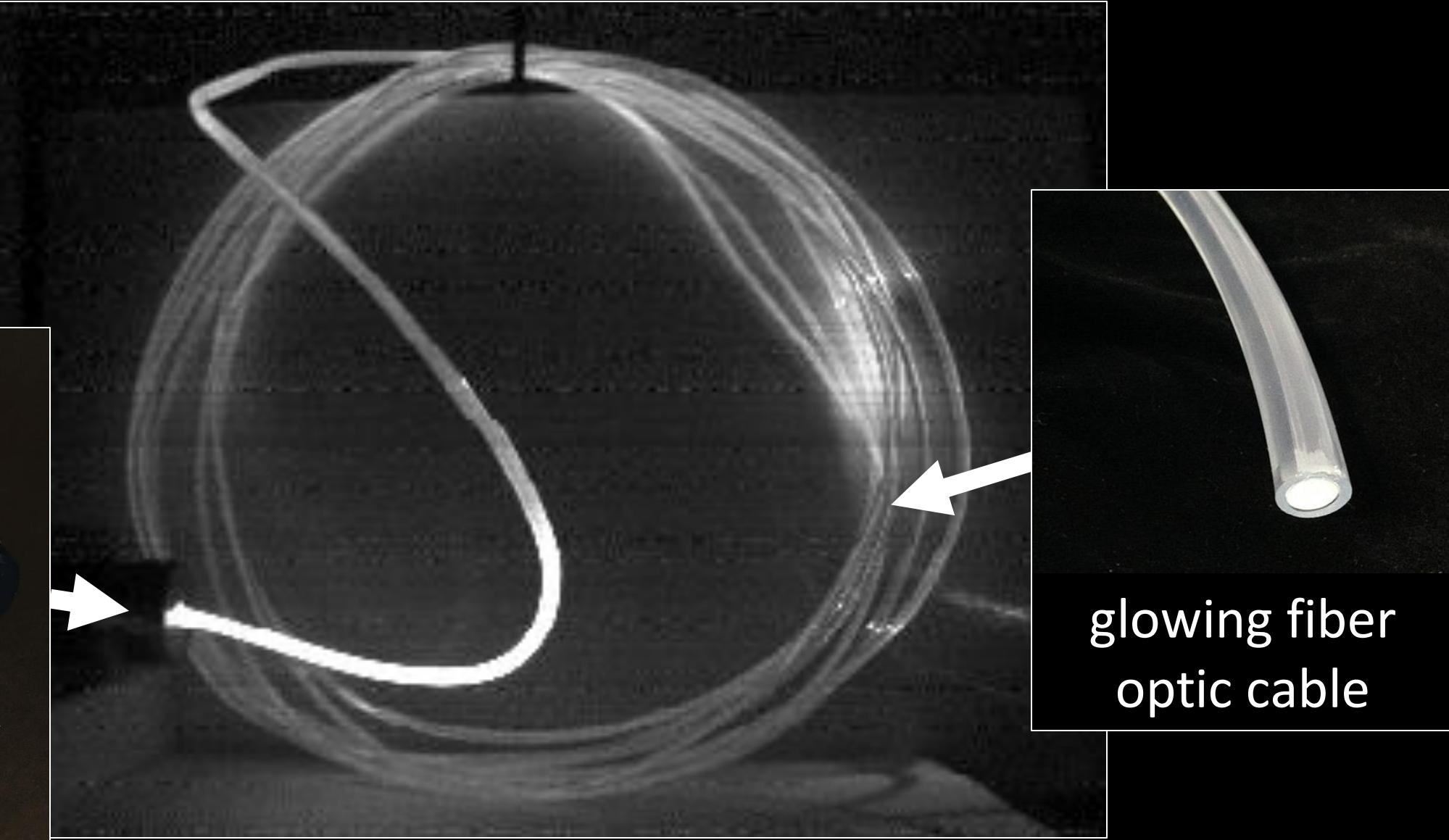
Single-Photon Avalanche Diodes (SPADs)

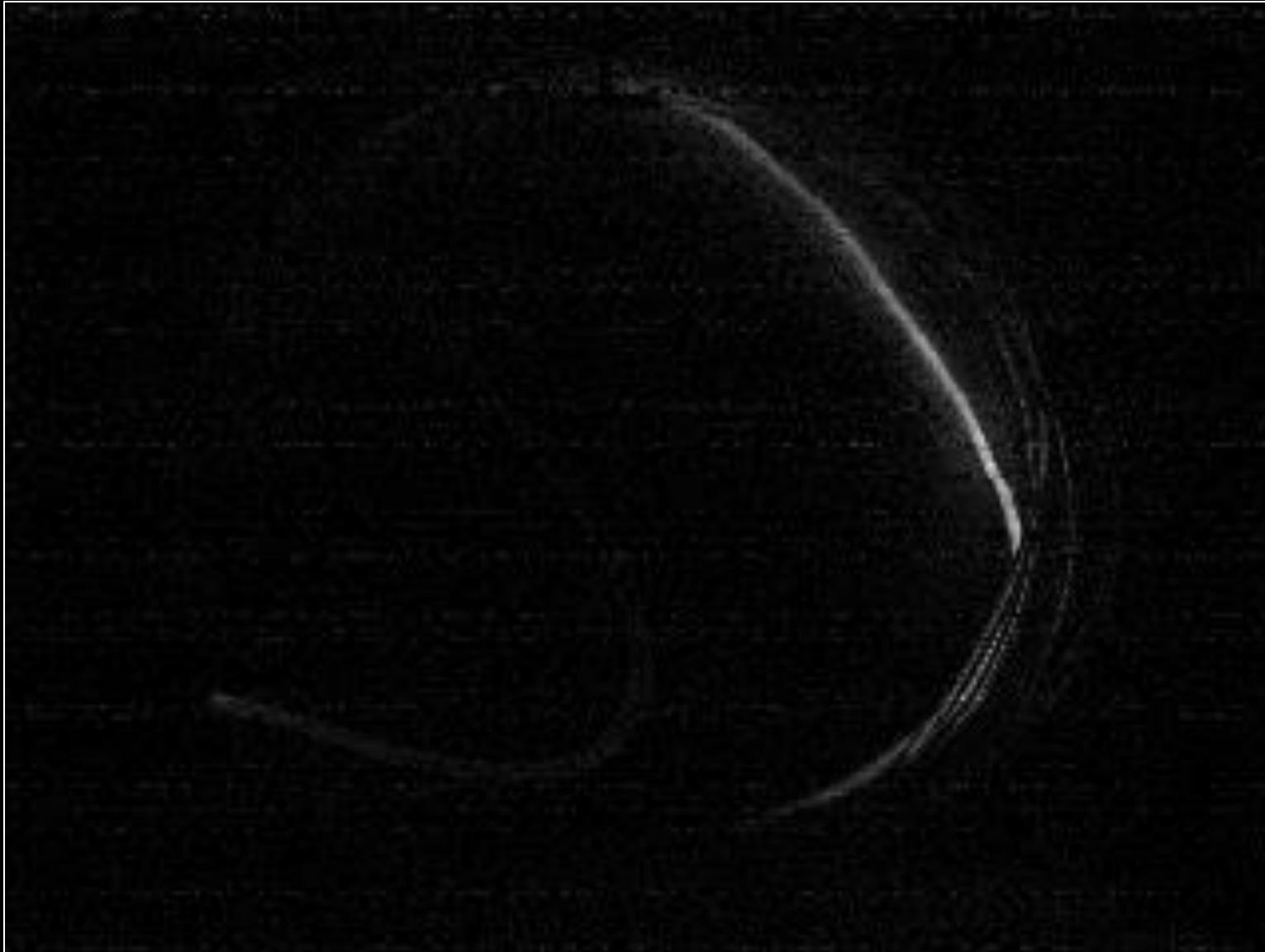
picosecond
laser



regular image

glowing fiber
optic cable



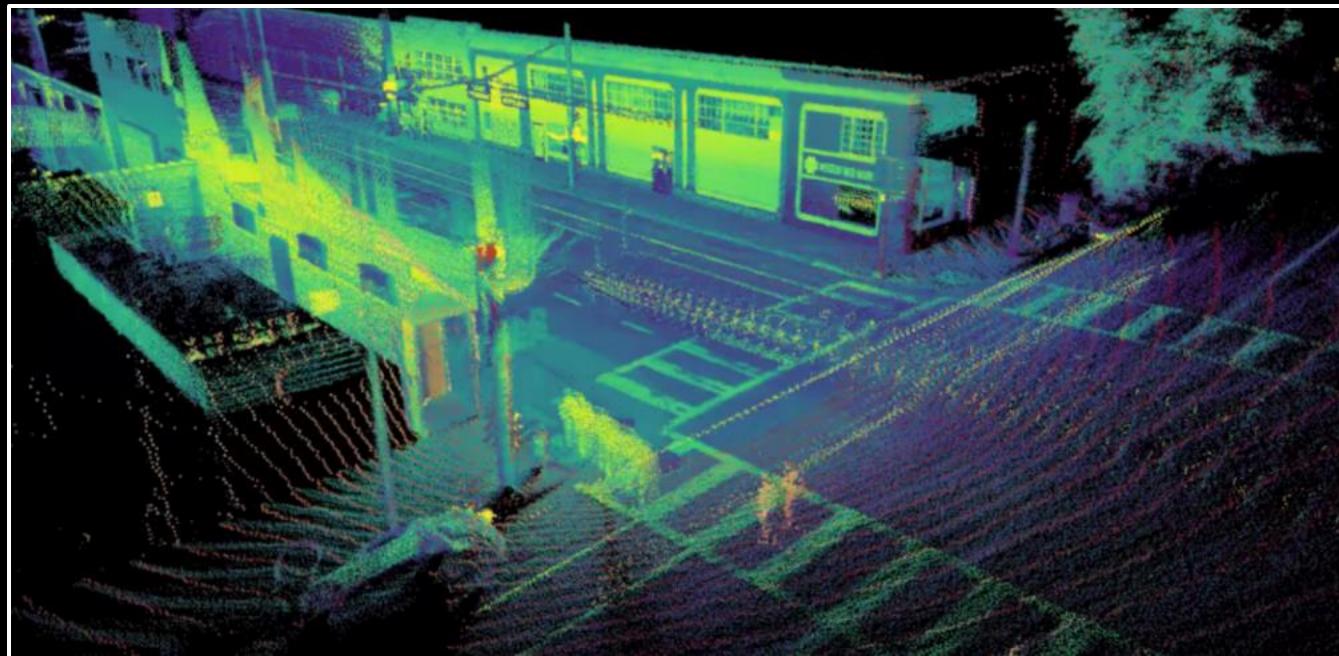


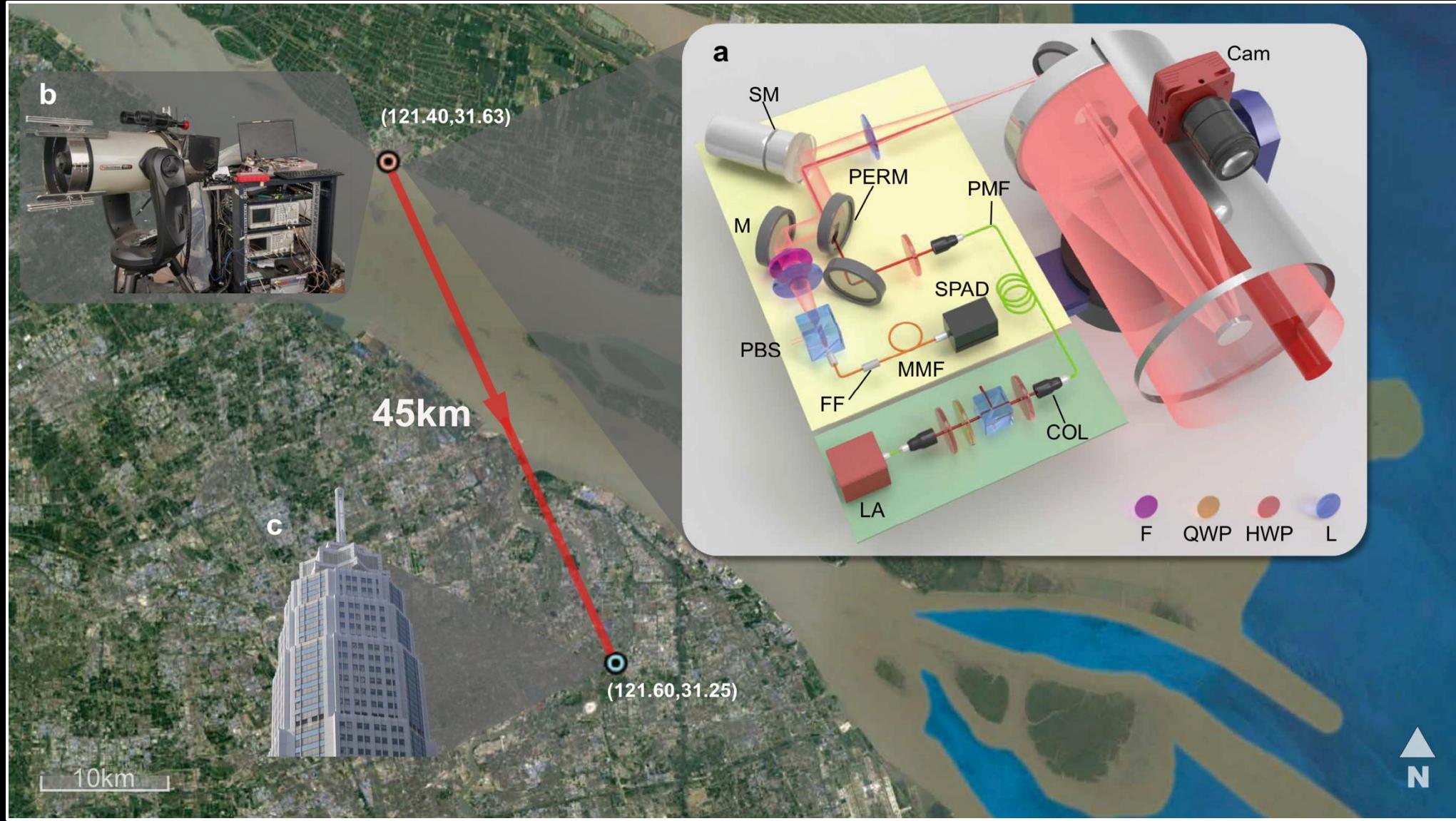
transient image

single-photon LIDARs



Ouster OS1-64



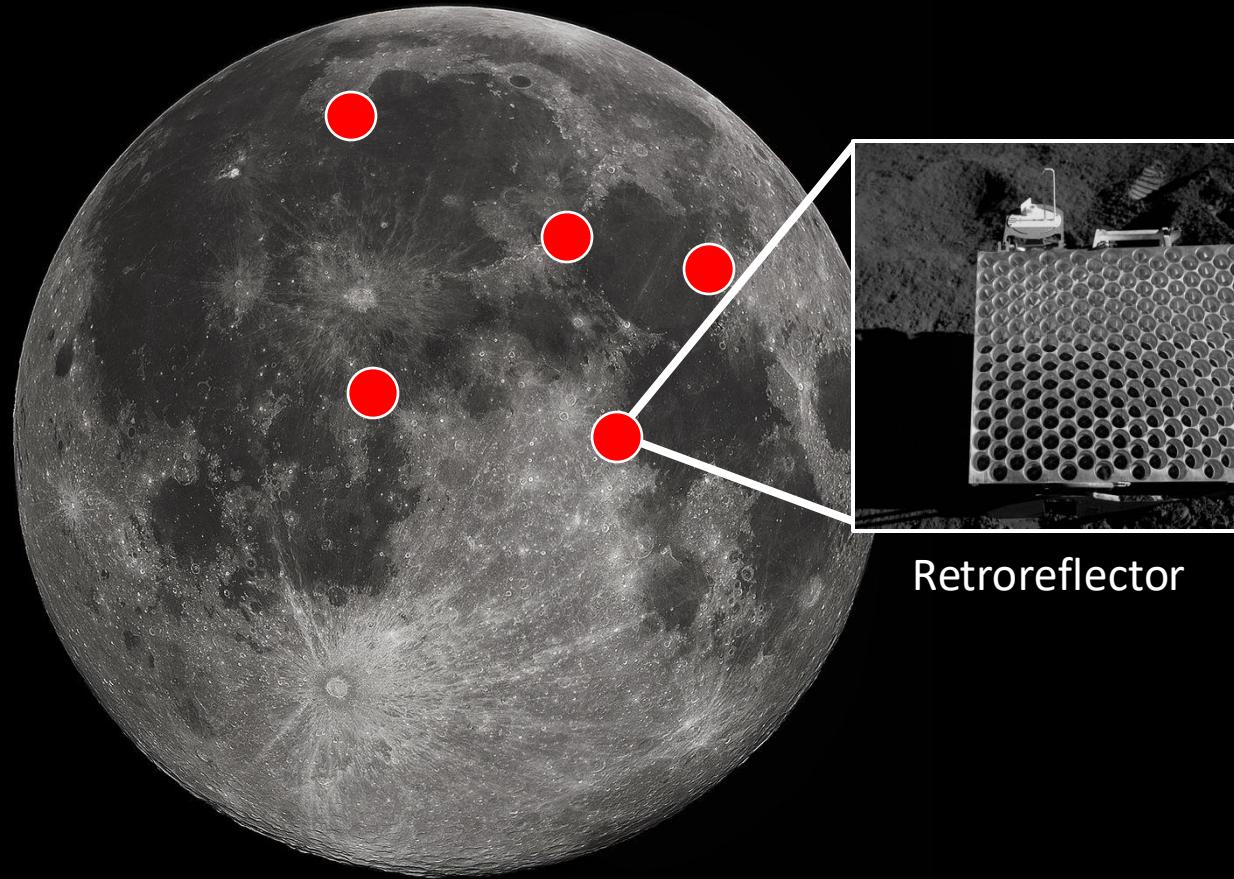


"Single-Photon Computational 3D Imaging at 45 km" [Li et al., 2019]

lunar & satellite laser ranging



International Laser Ranging Service (ILRS)

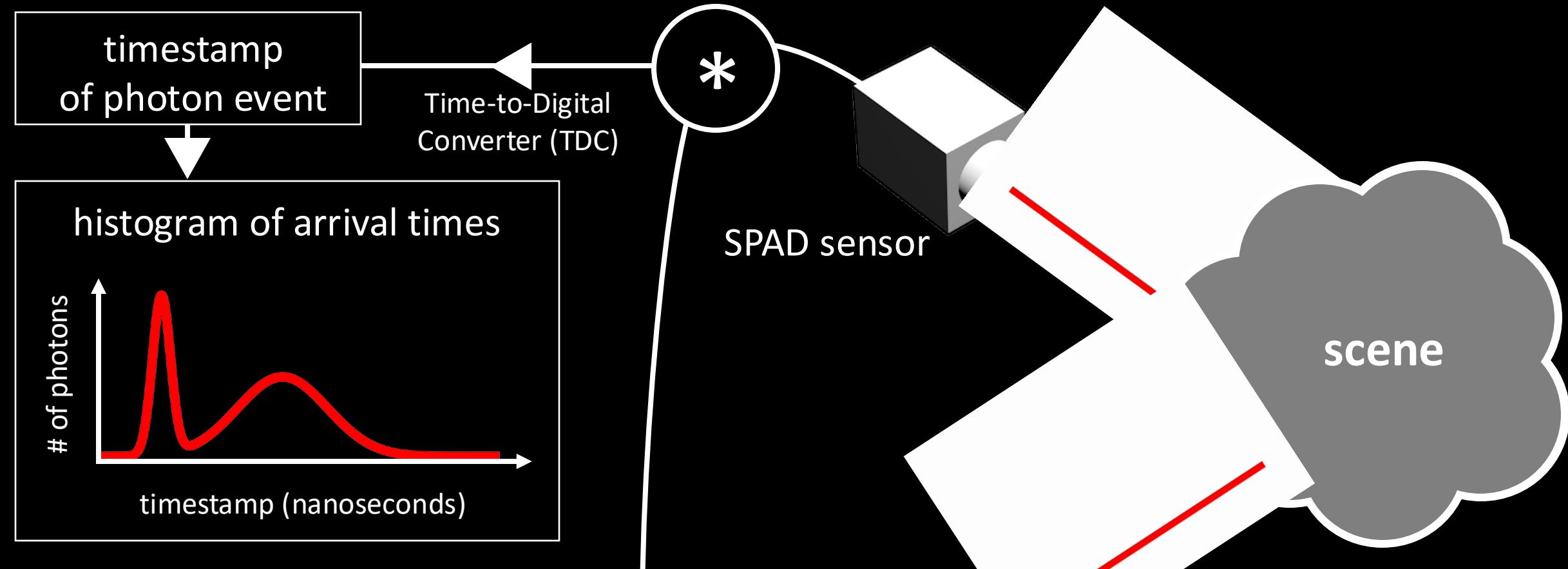


Lunar Laser Ranging (LLR)

● - Location of Lunar Retroreflector

Retroreflector

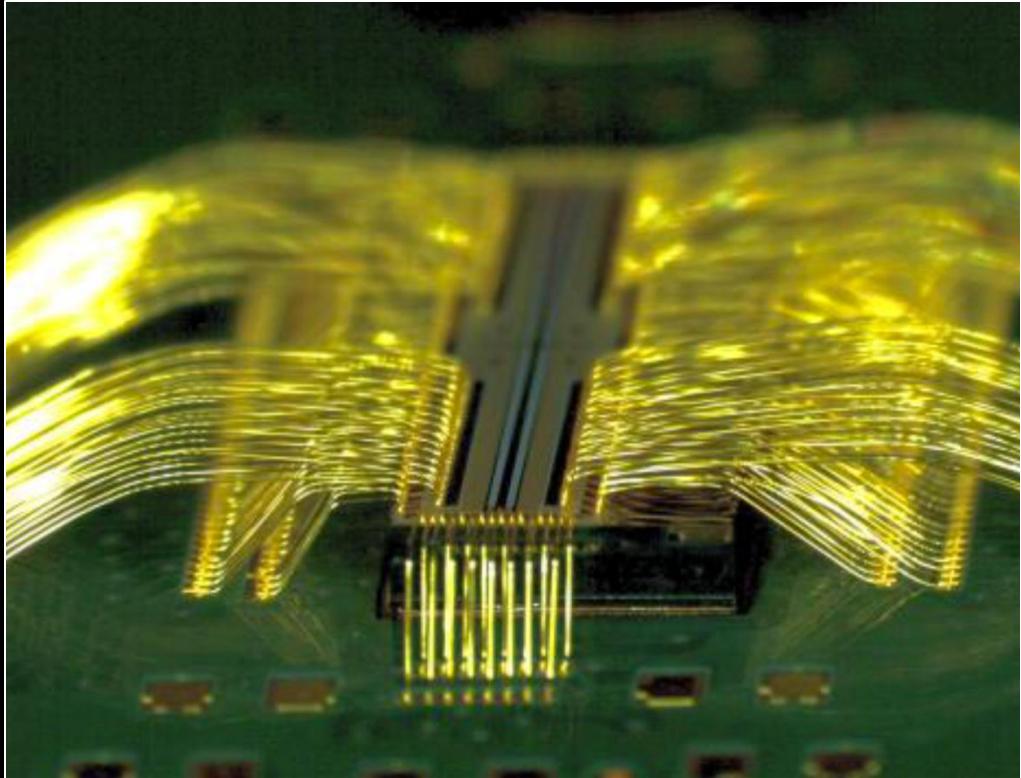
single-photon avalanche diode (SPAD)



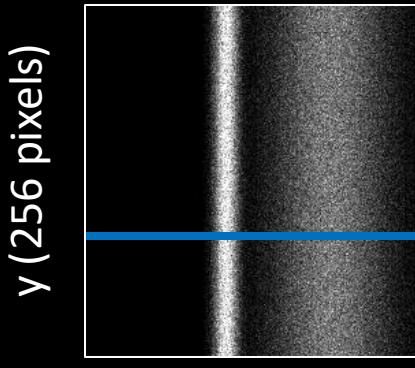
SPAD properties:

- Each photon timestamped with 60 ps precision
- Measure up to 10 million photons a second
- No electronic read noise

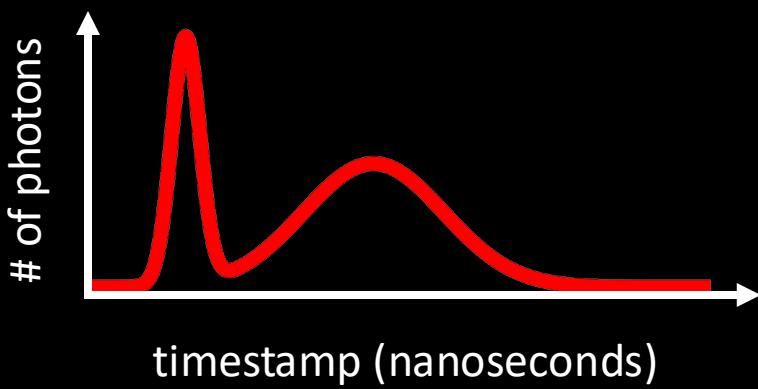
linear array of SPADs



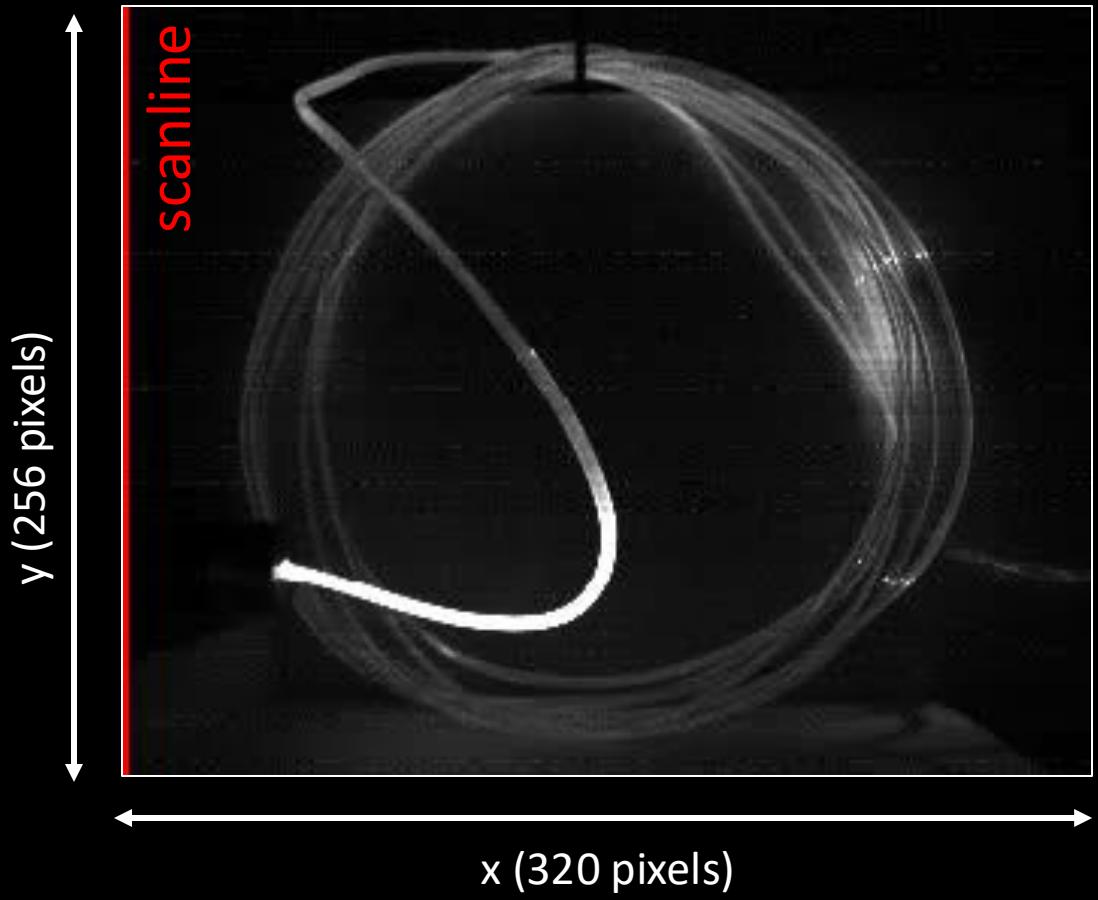
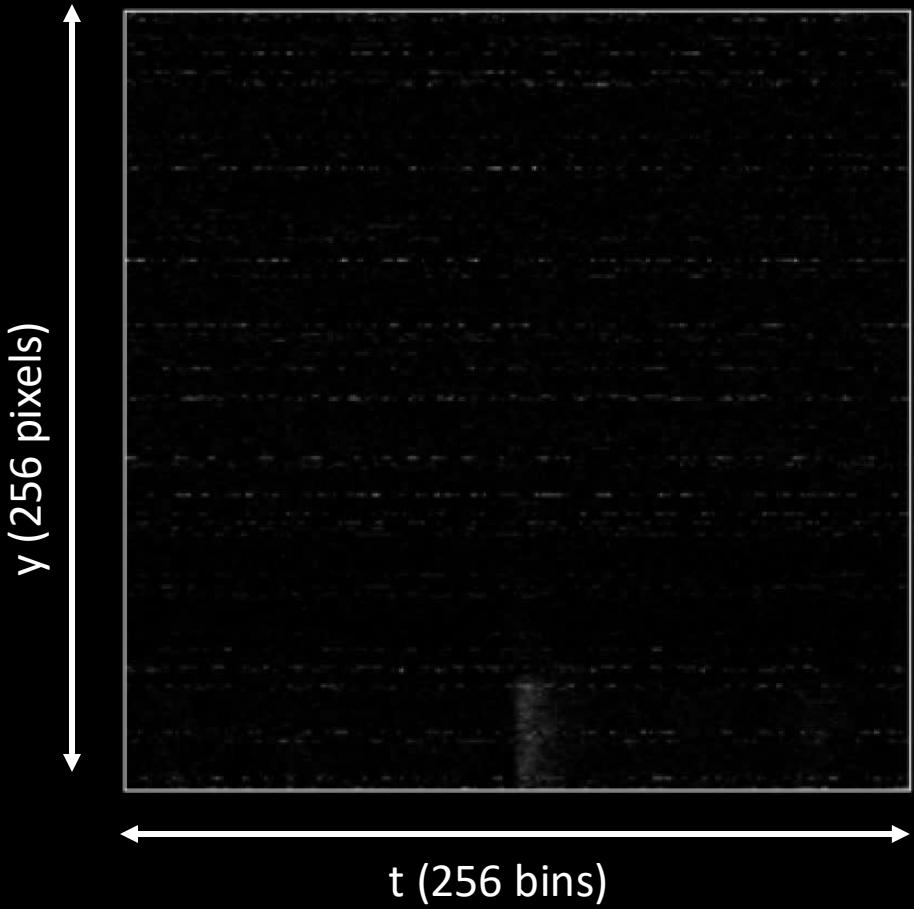
spatiotemporal image



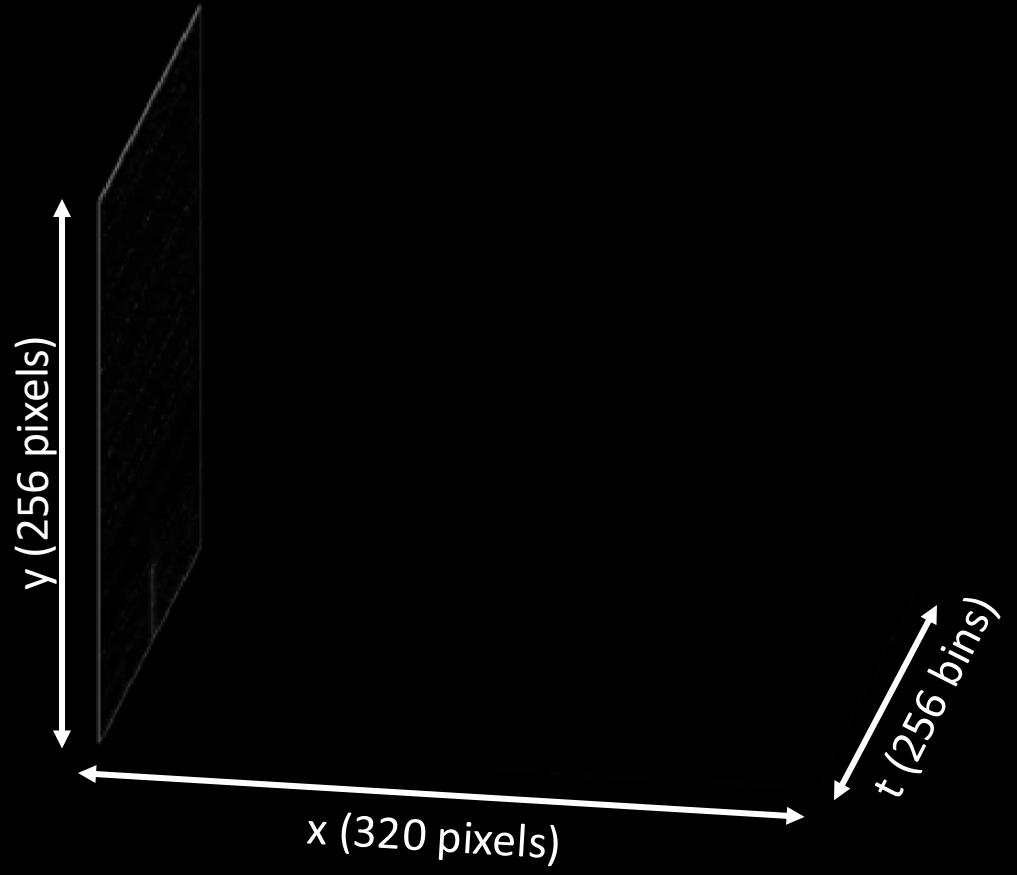
histogram of arrival times



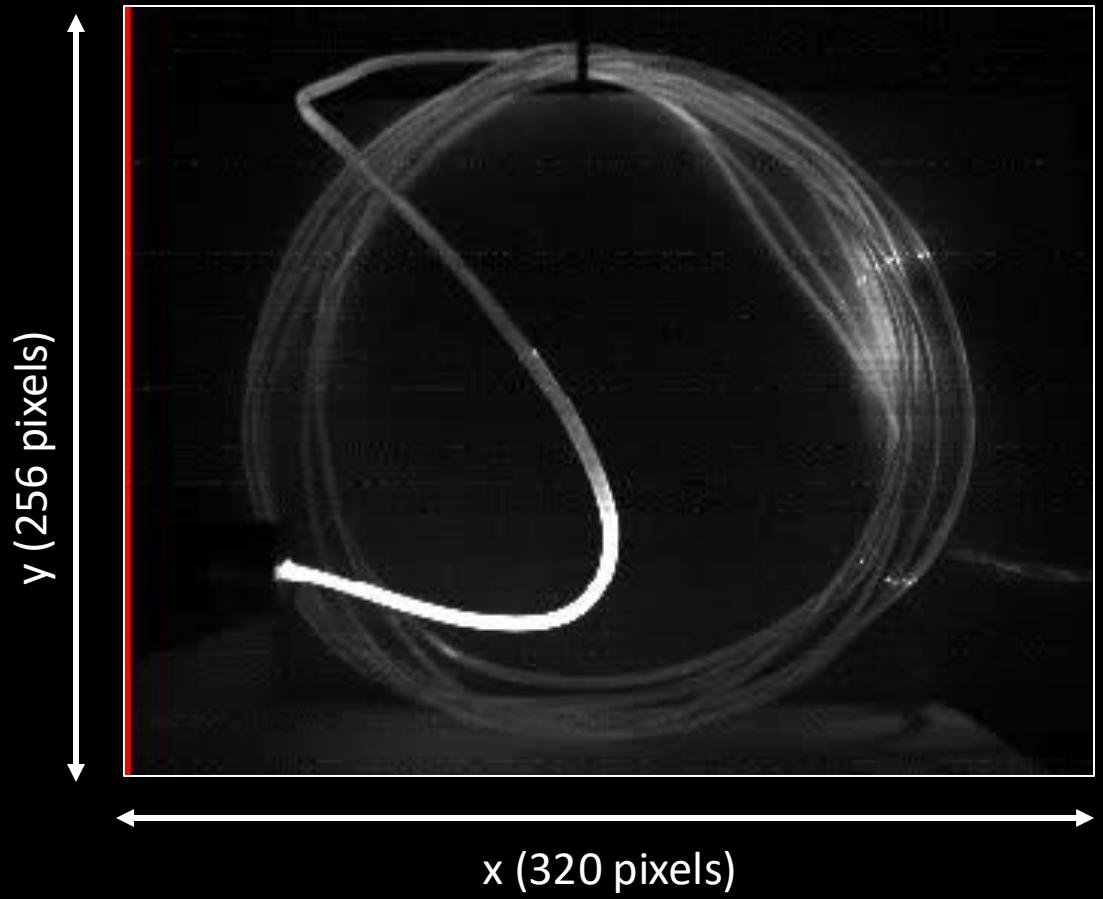
scanning procedure



scanning procedure

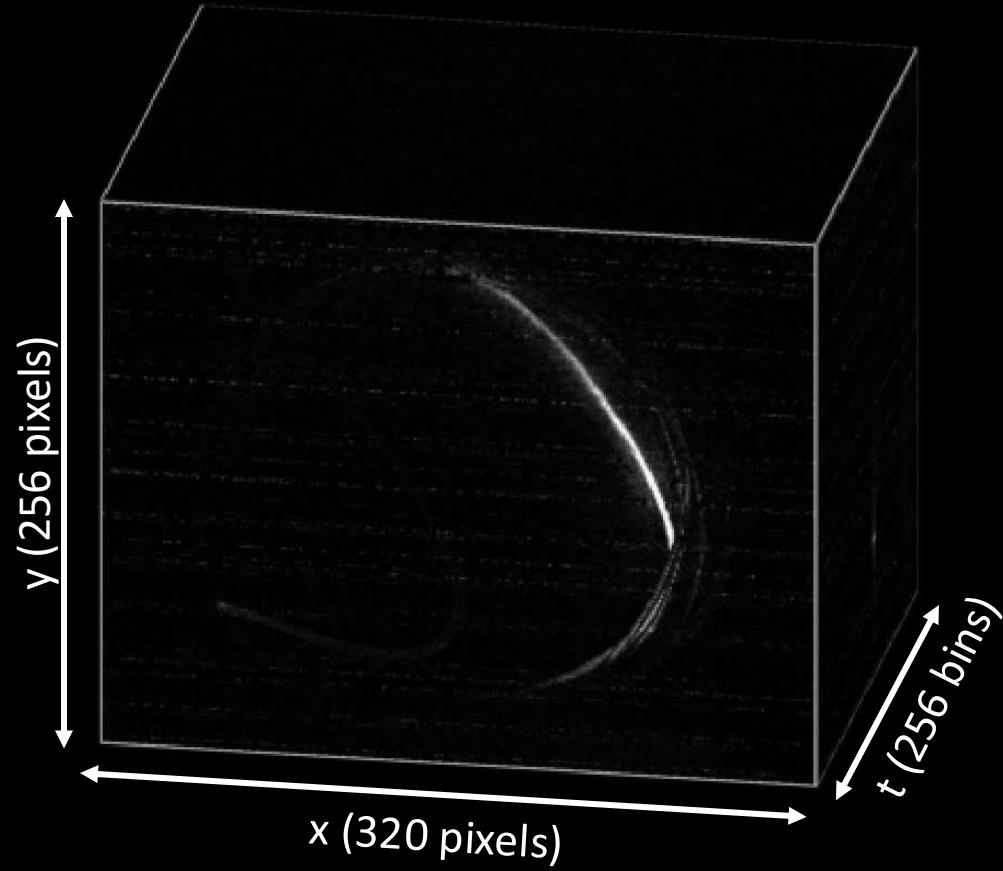


transient image

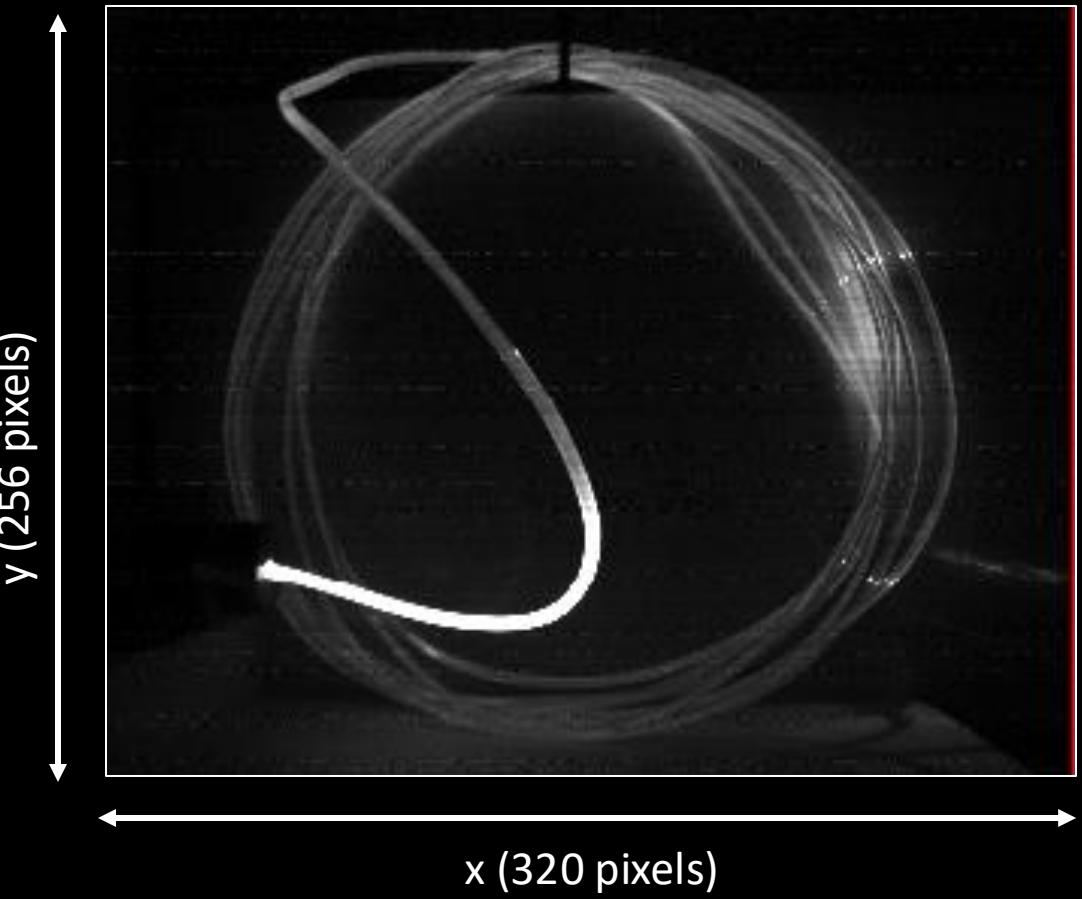


regular image

scanning procedure



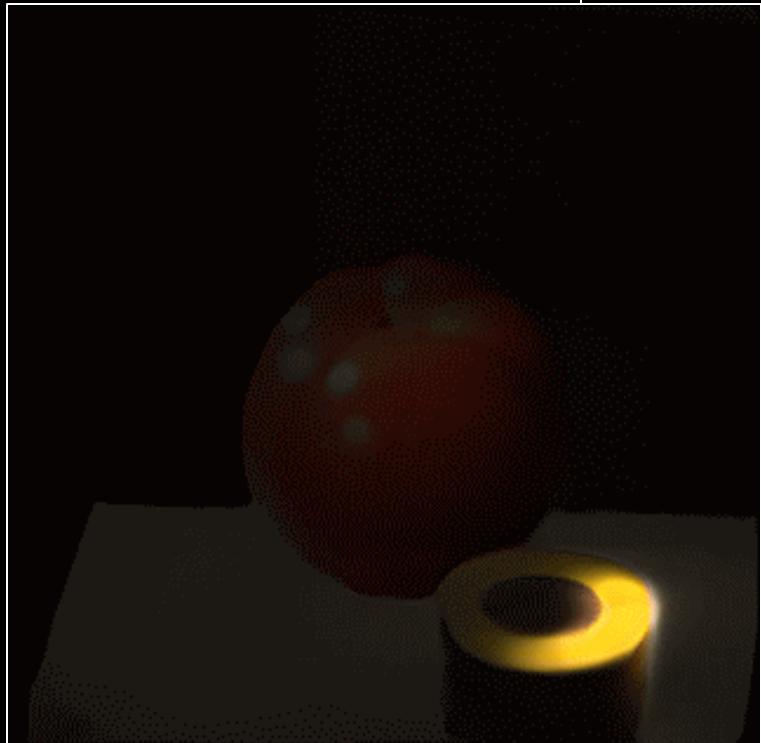
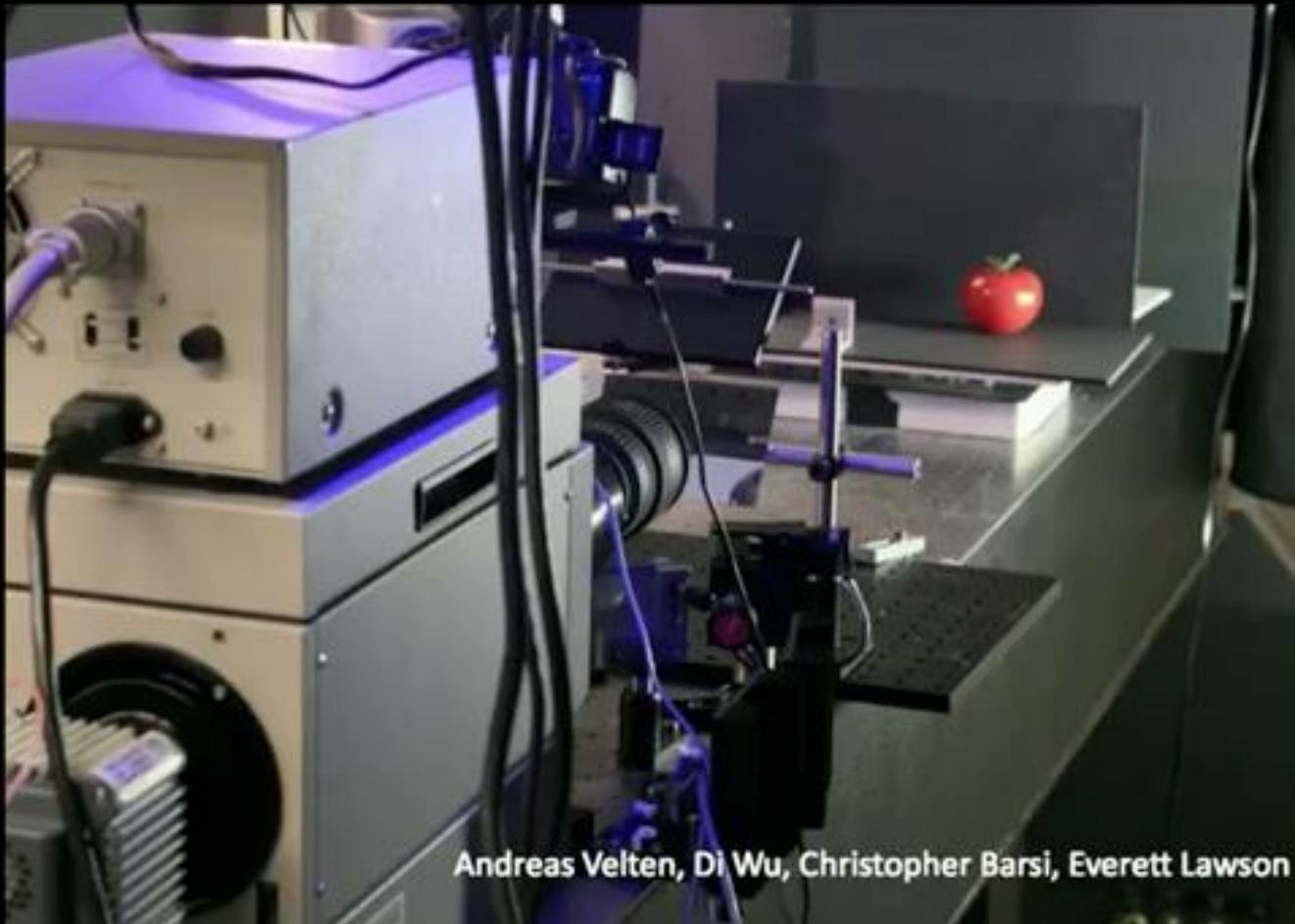
transient image



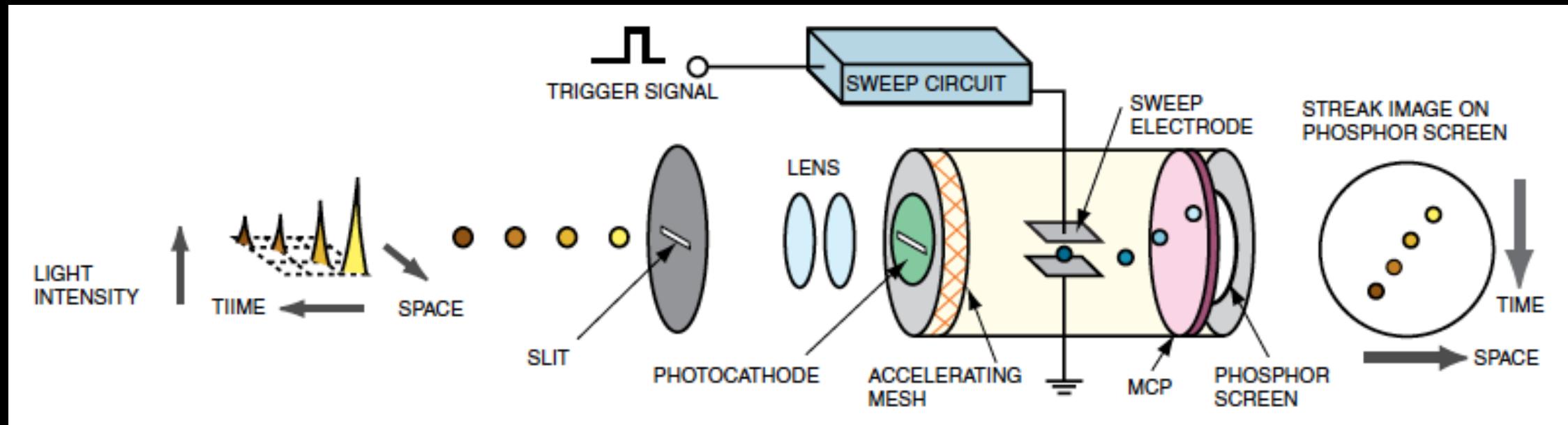
regular image

Streak Cameras

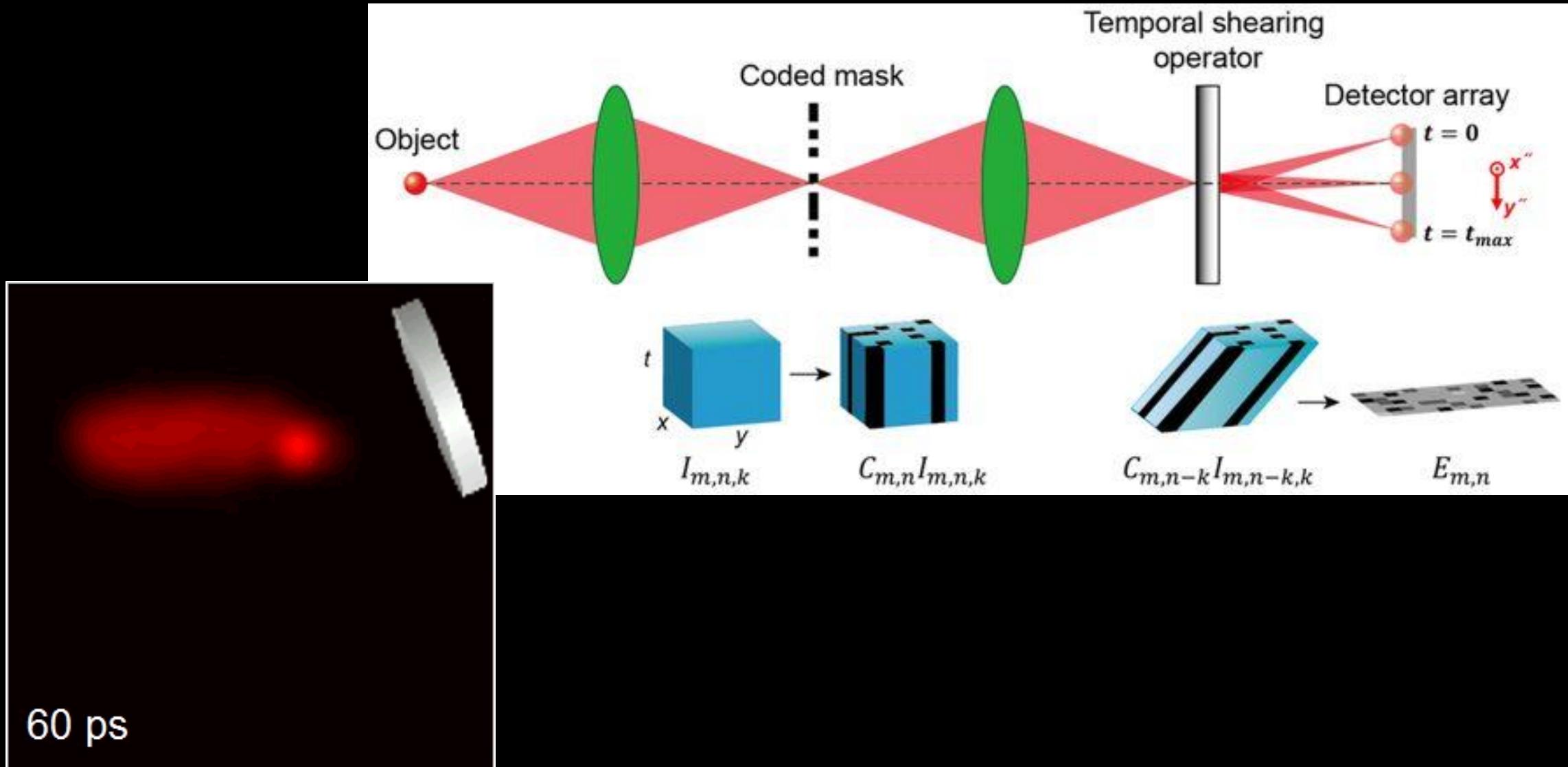
streak cameras



streak cameras

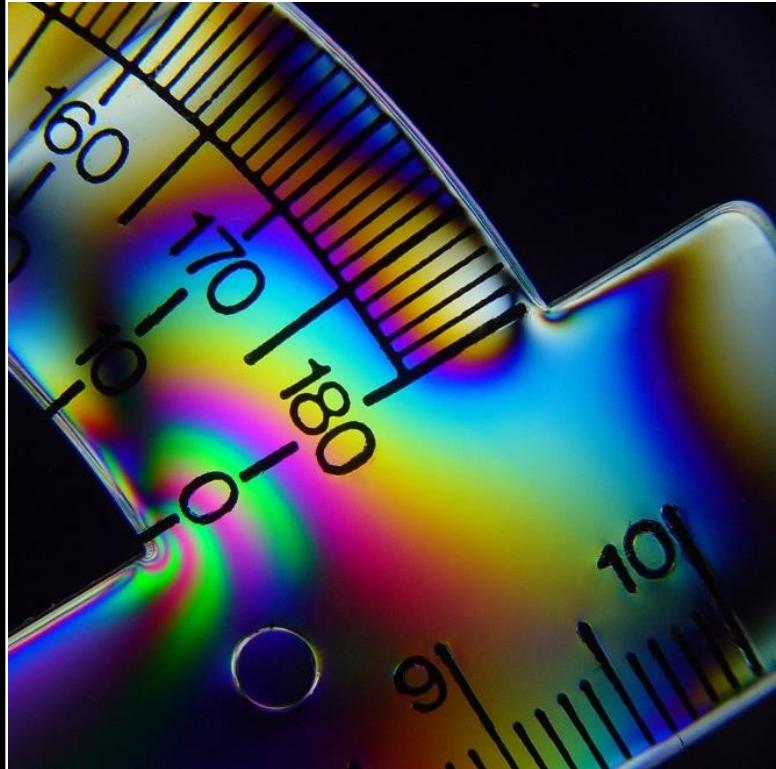


streak cameras – compressed ultrafast photography



Interferometric Cameras

Material properties



birefringence

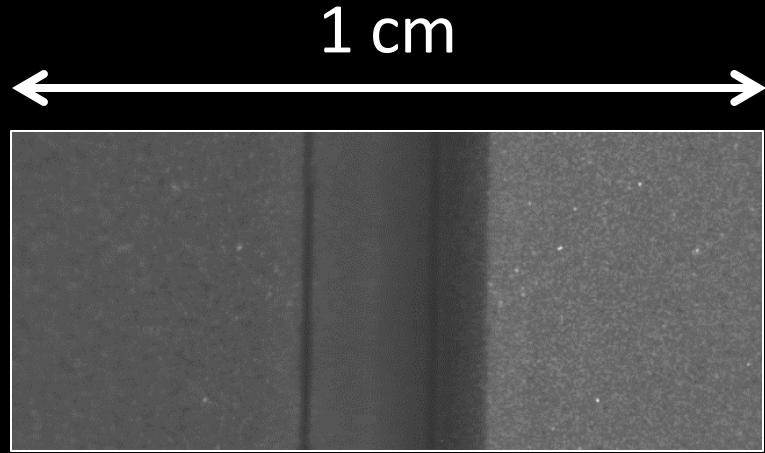


dispersion

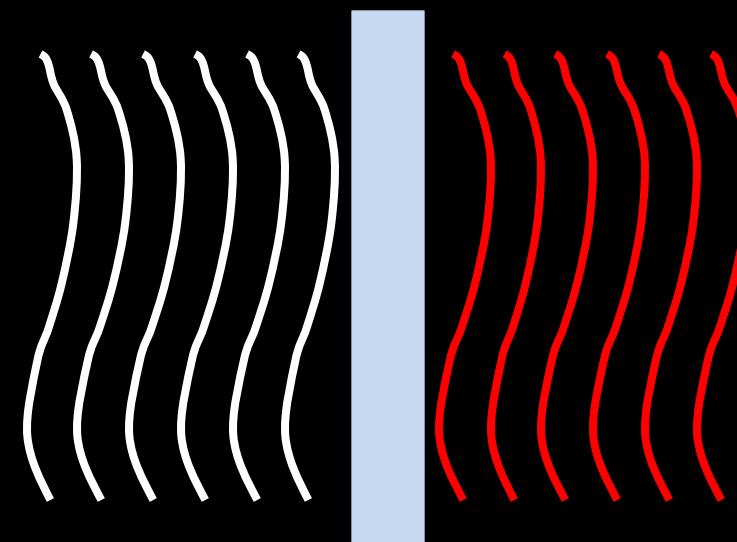
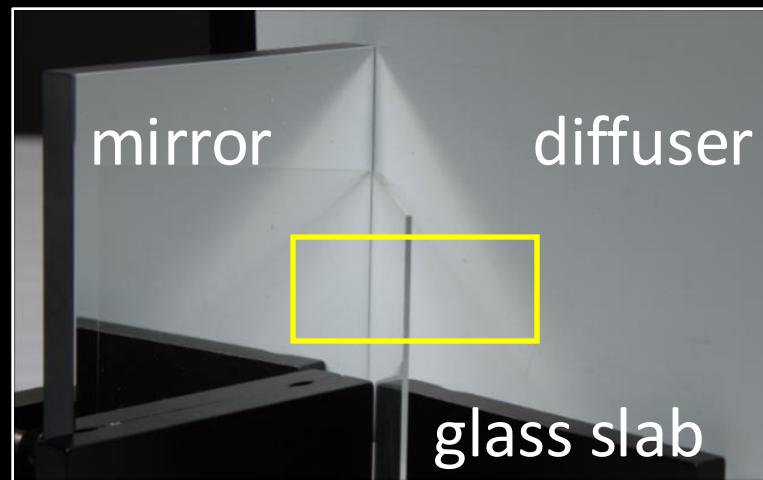
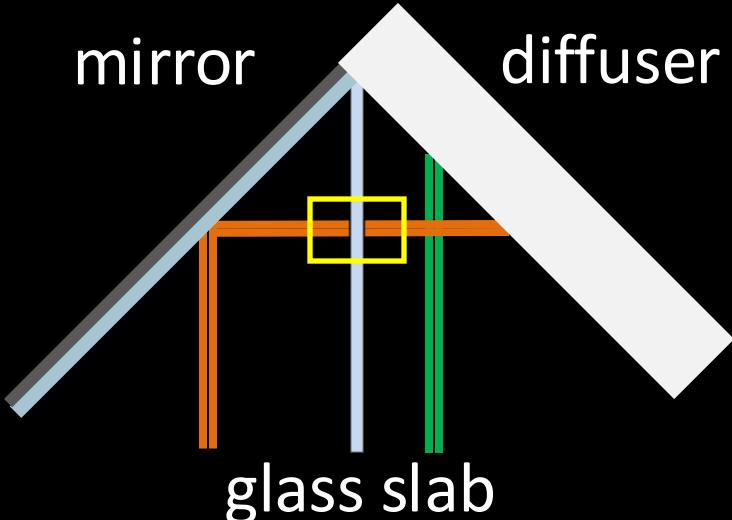


scattering

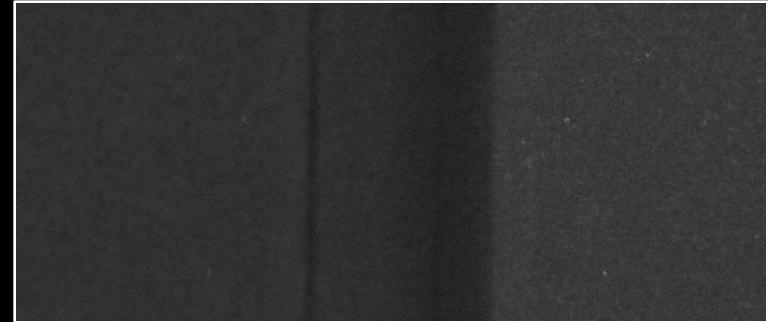
Dispersion



cropped frame



refractive index η (wavelength)

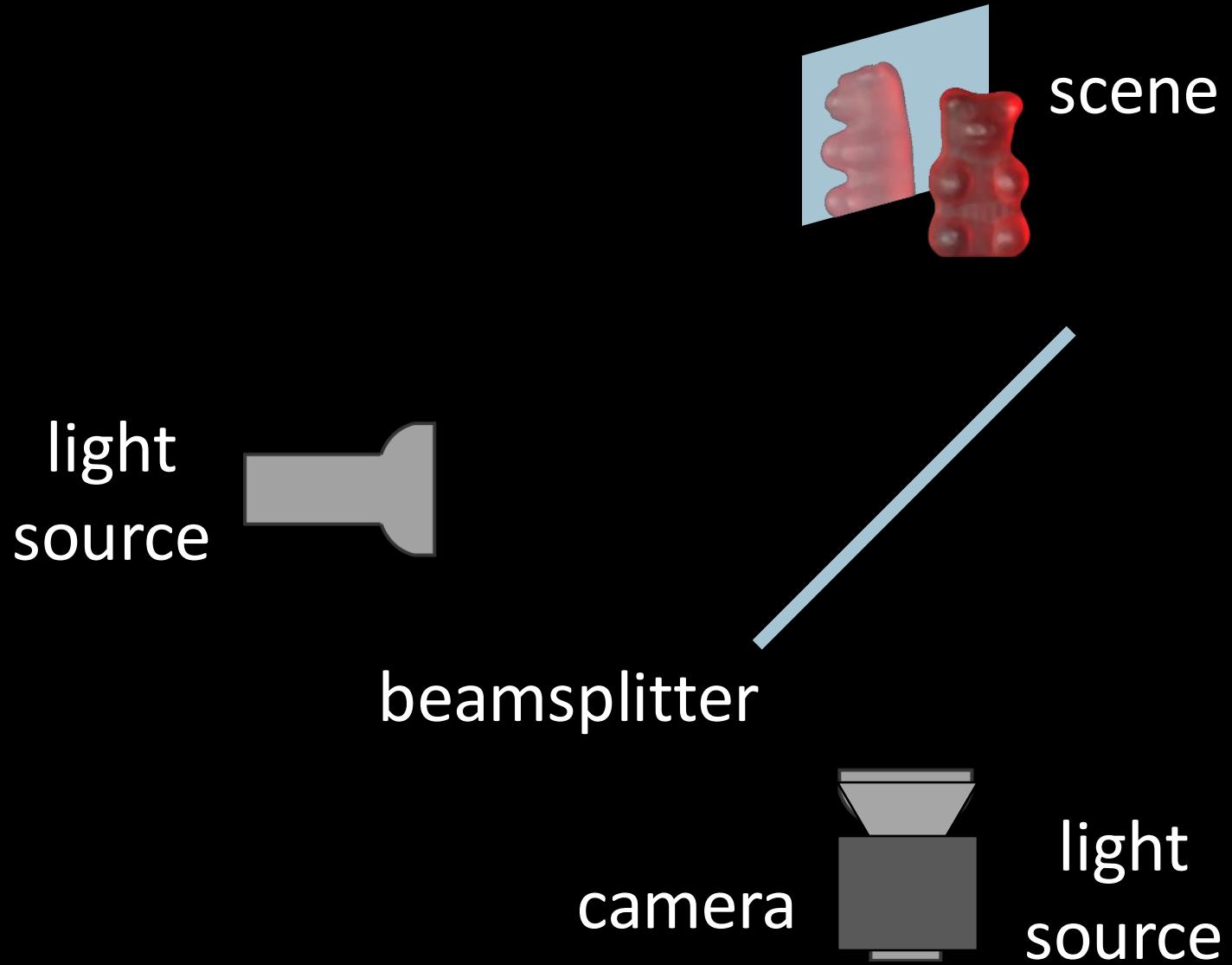


$\Delta t \sim \text{ns}$

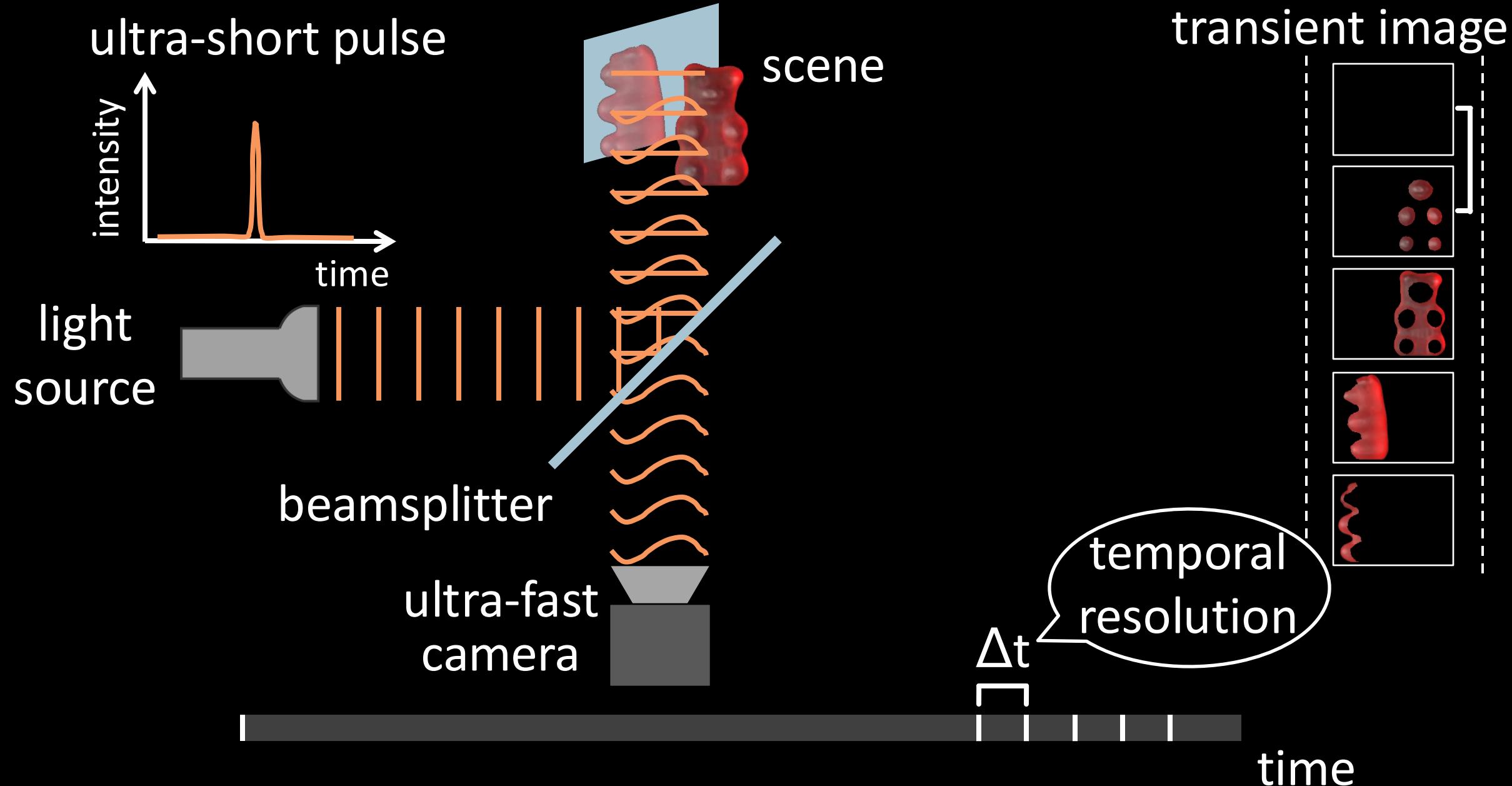


$\Delta t \sim 10^{-3} \text{ ns}$

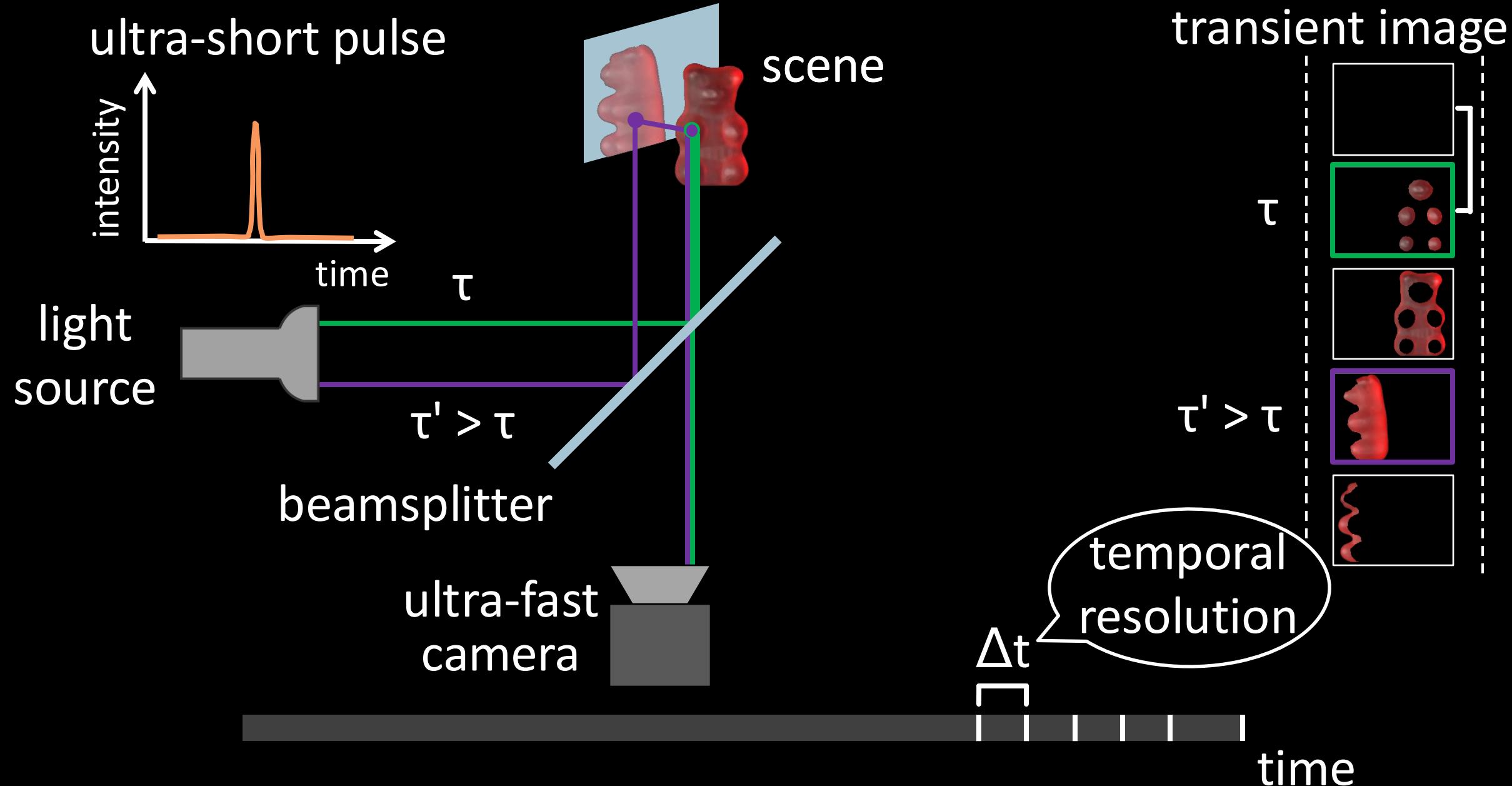
Transient imaging example



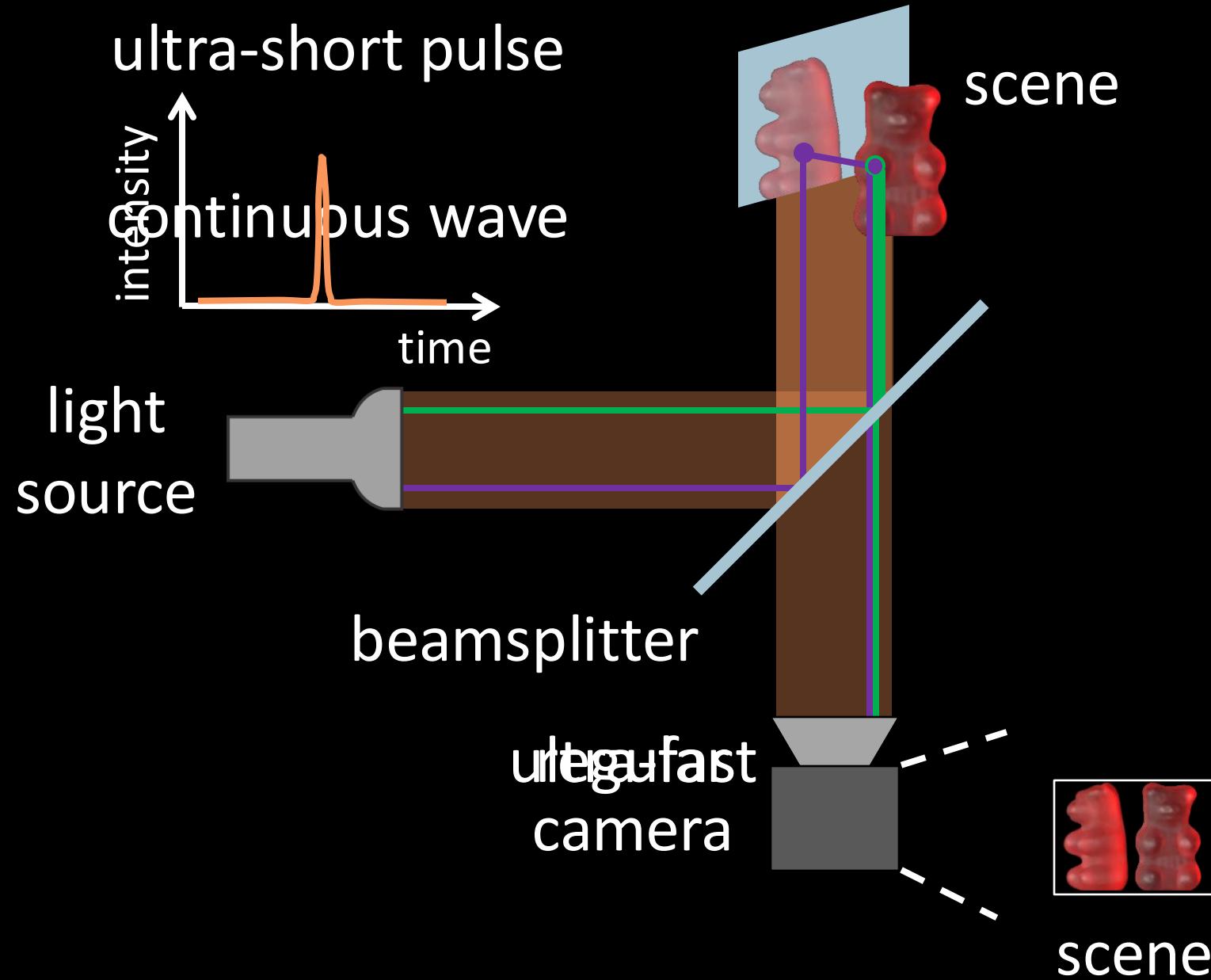
Transient imaging: light-in-flight



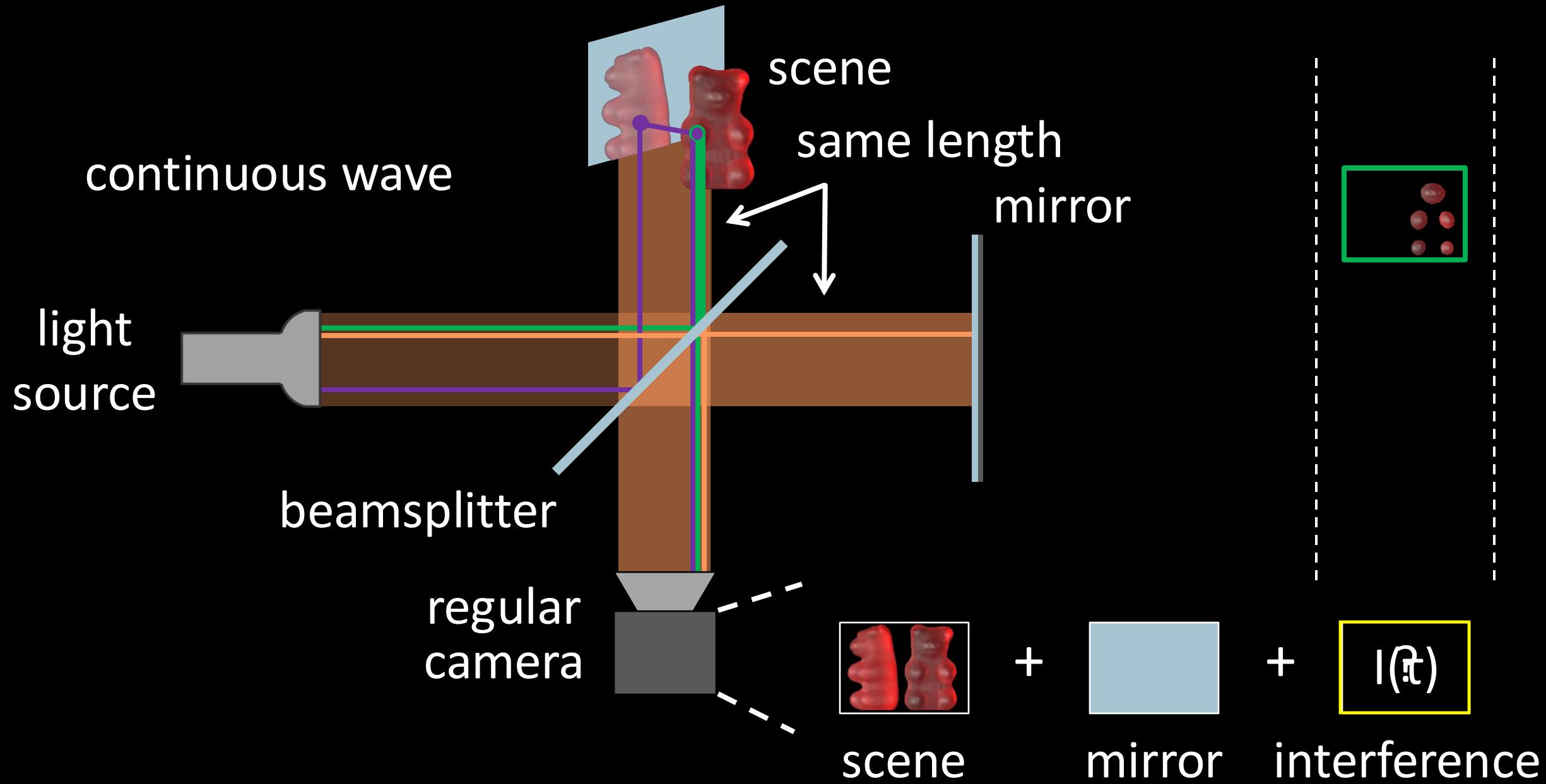
Transient imaging: light-in-flight



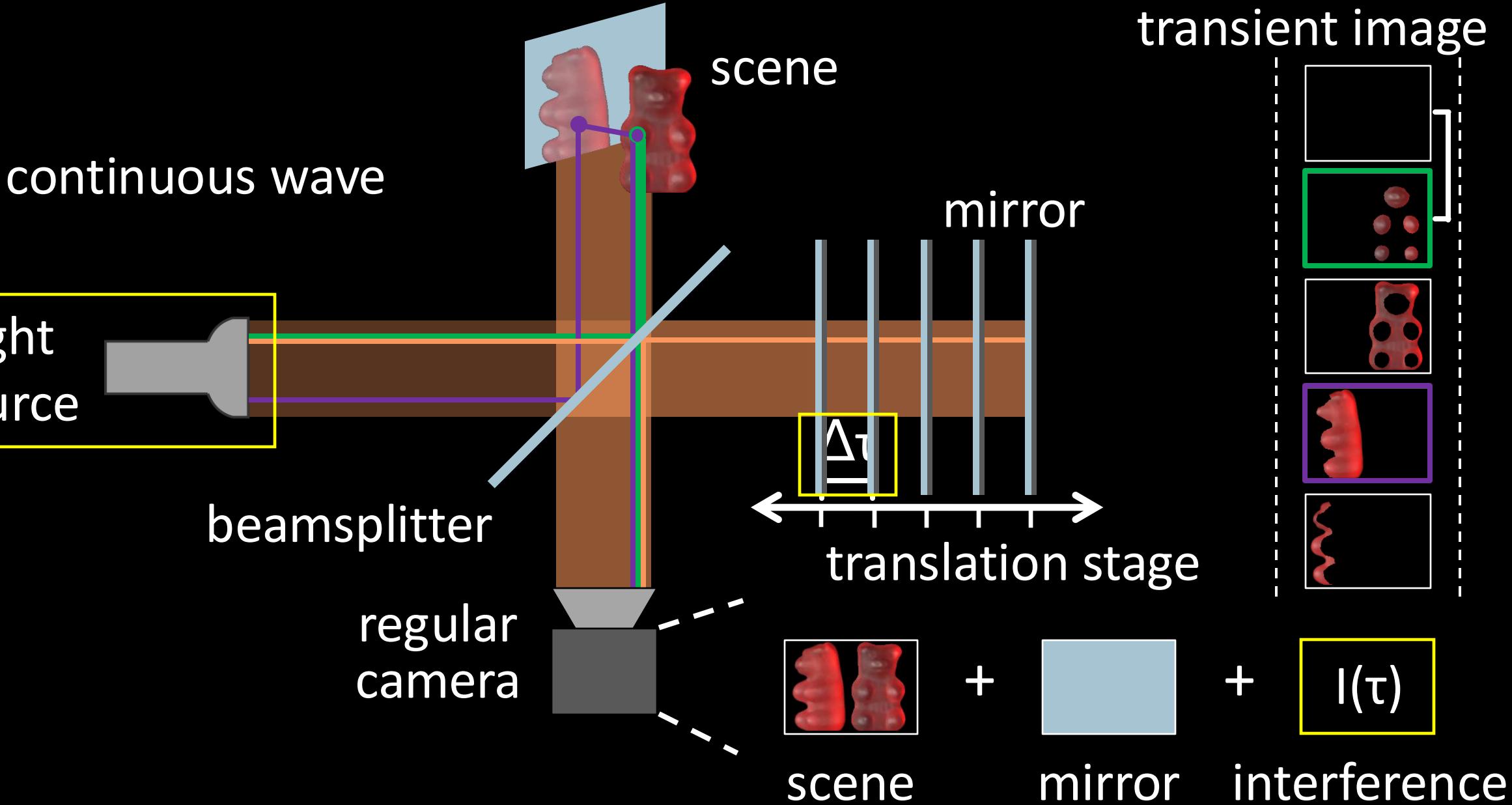
Michelson interferometer



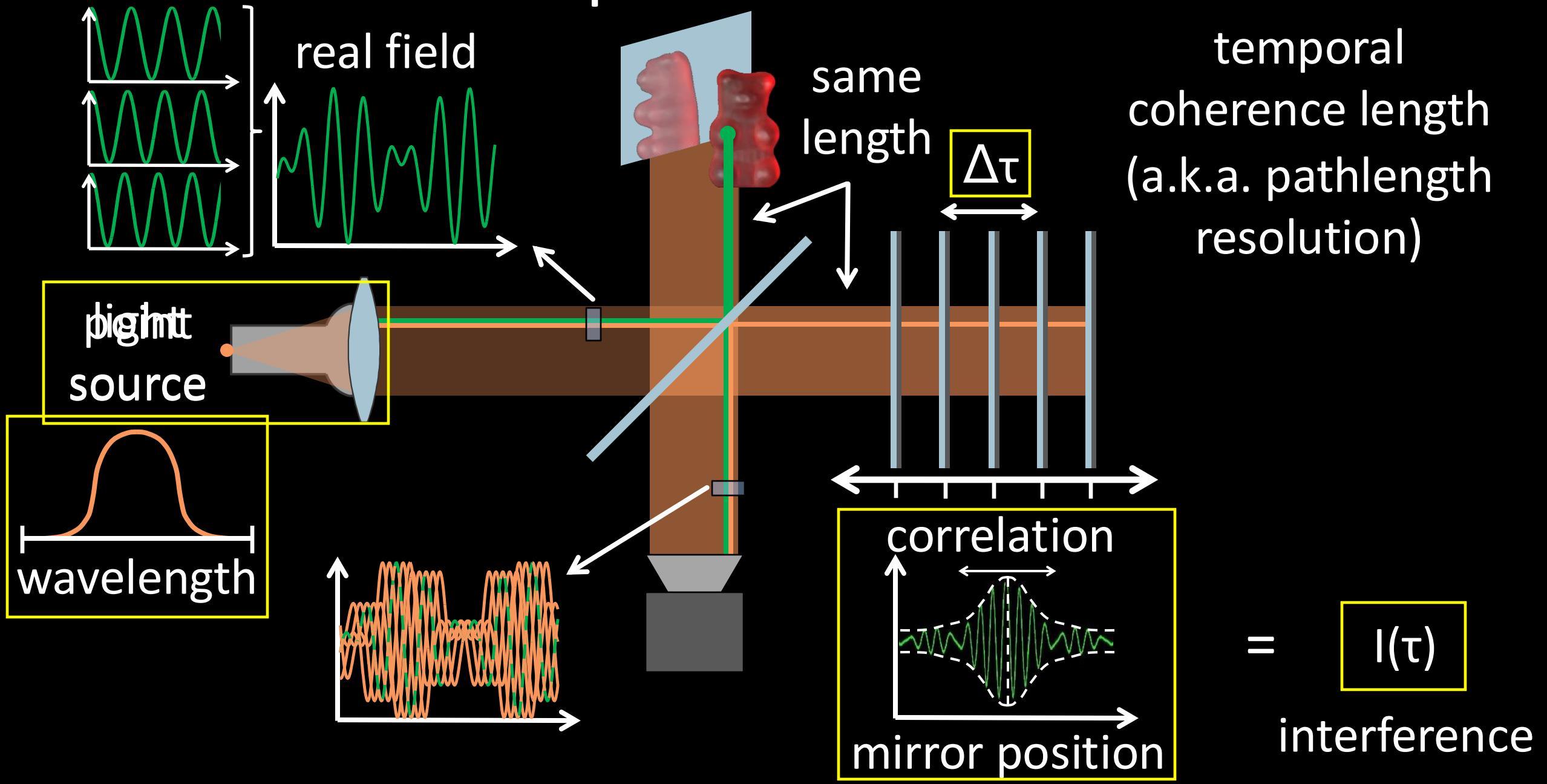
Michelson interferometer



Optical coherence tomography



Temporal coherence

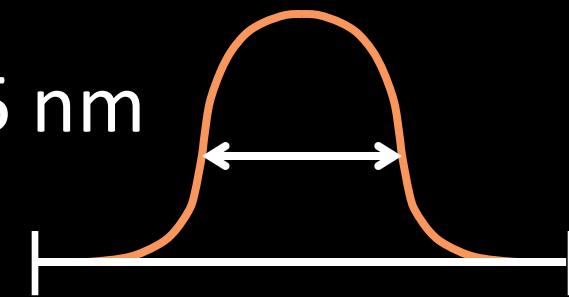


Temporal coherence length

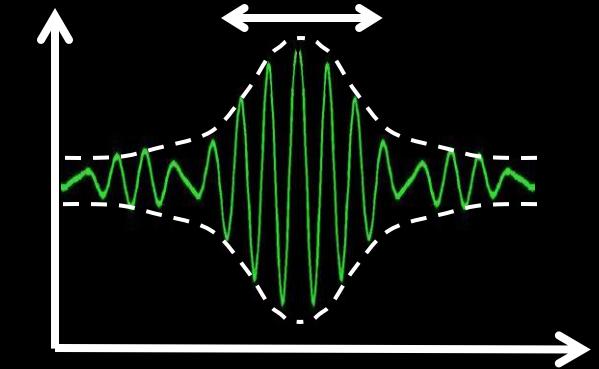
bandwidth

broadband

25 nm

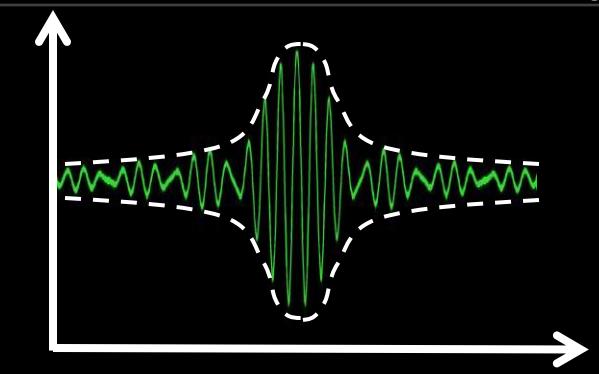
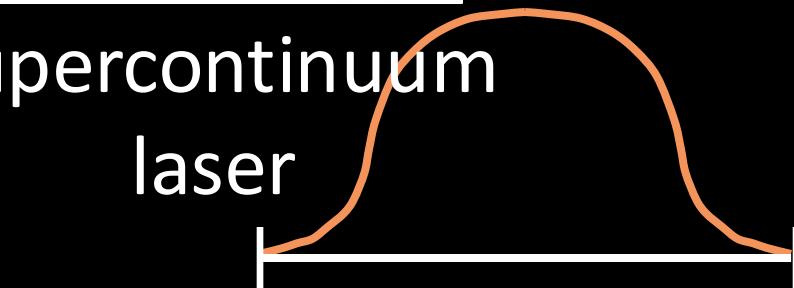


correlation



pathlength resolution $\Delta\tau \sim 10 \mu\text{m}$

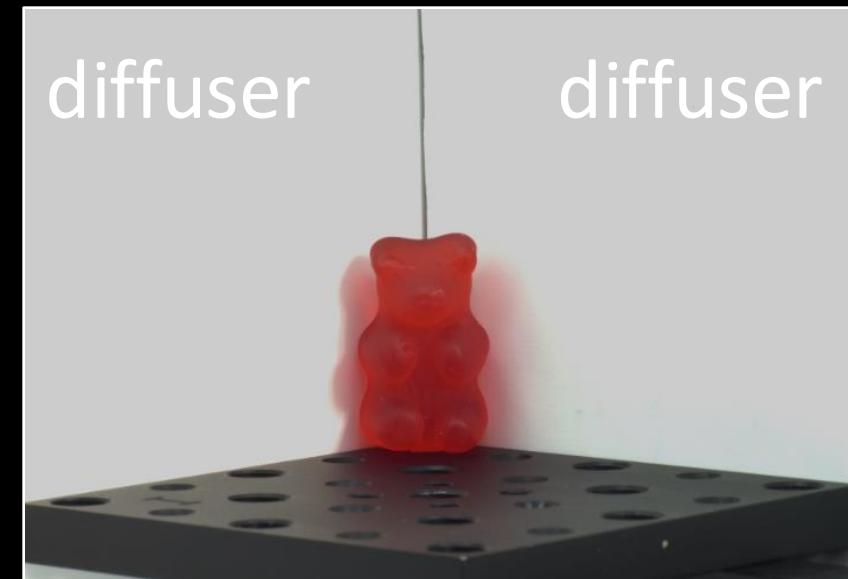
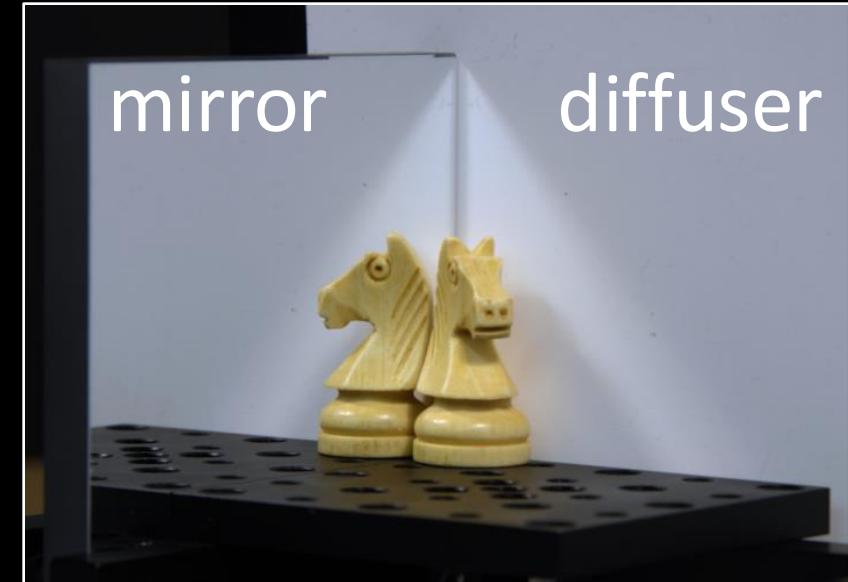
superluminescent
broadband
diode



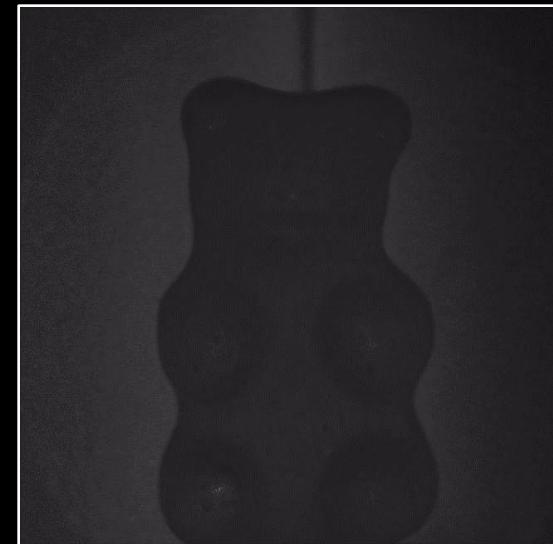
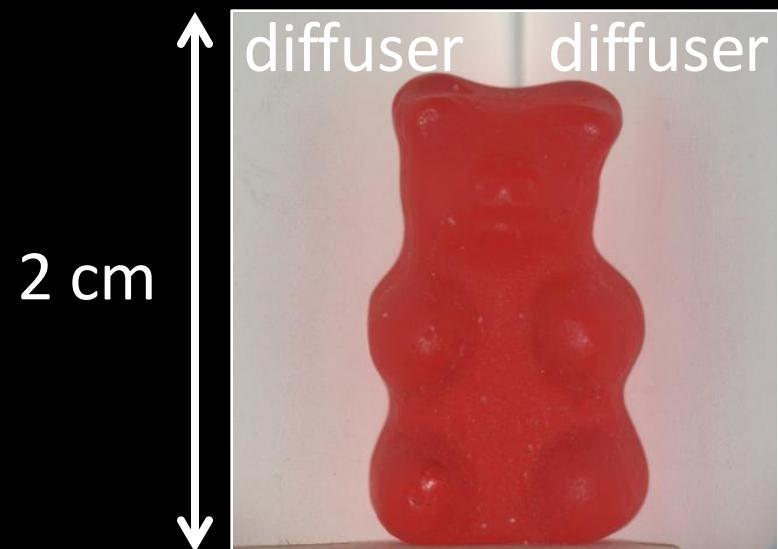
Some transient images



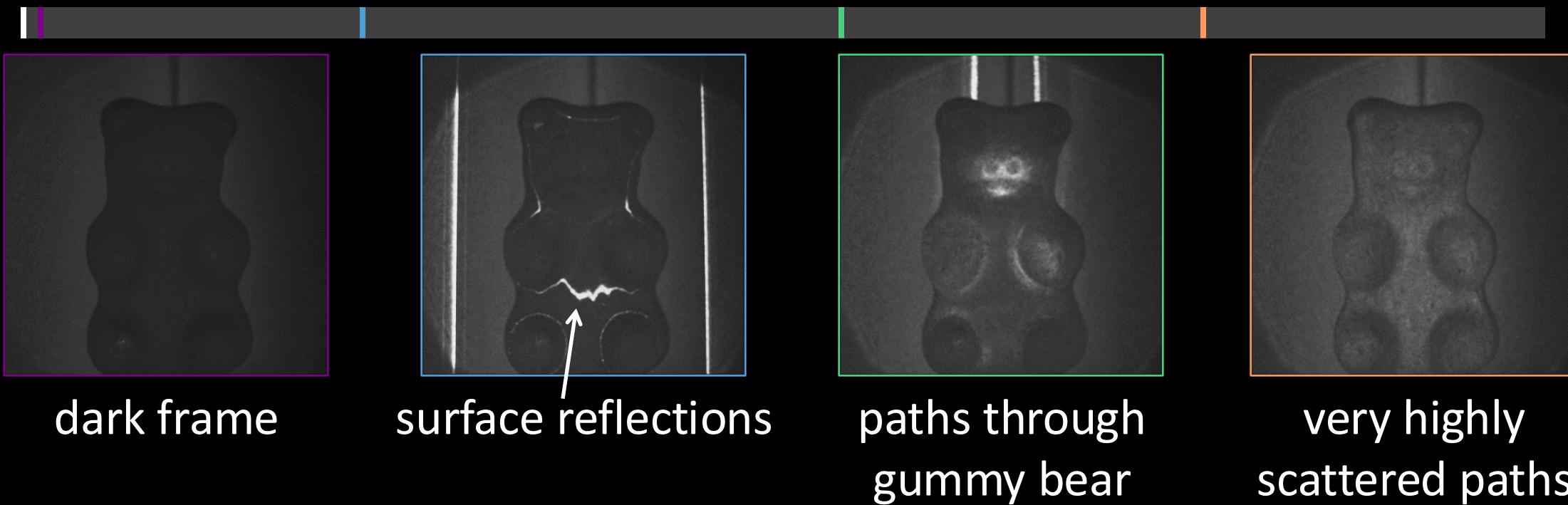
centimeter-sized objects



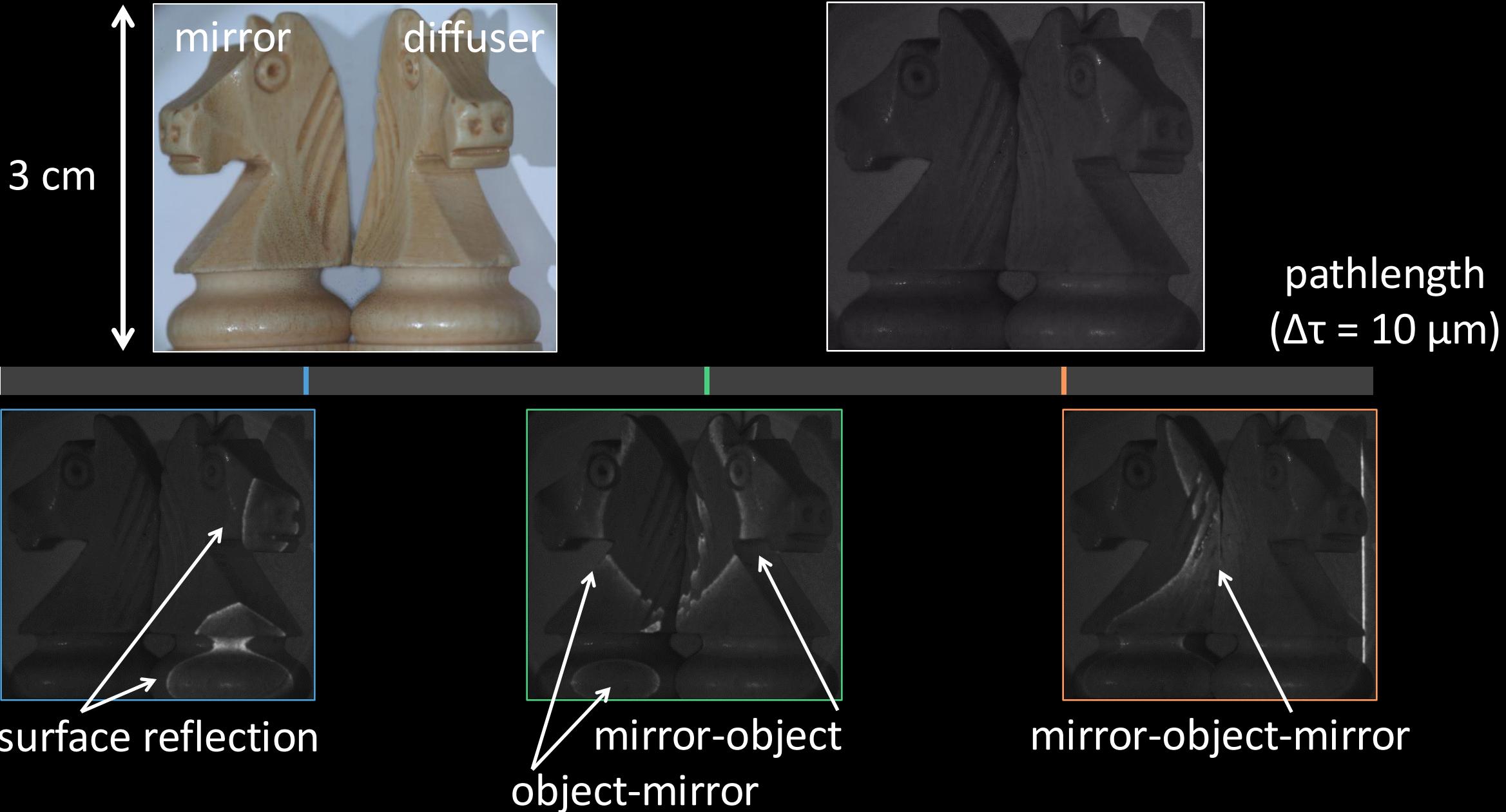
Gummy bear and diffuse corner



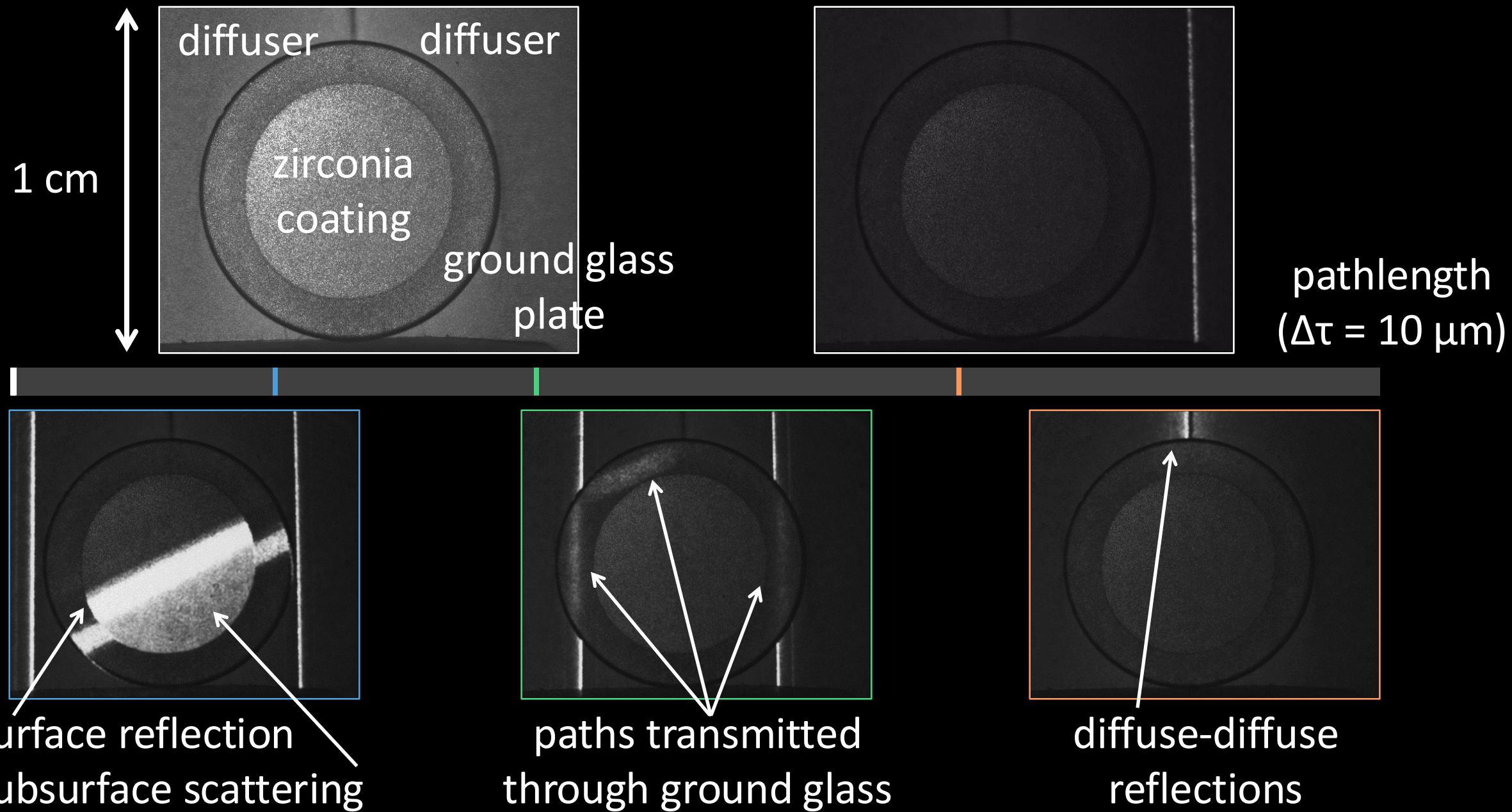
pathlength
($\Delta\tau = 10 \mu\text{m}$)



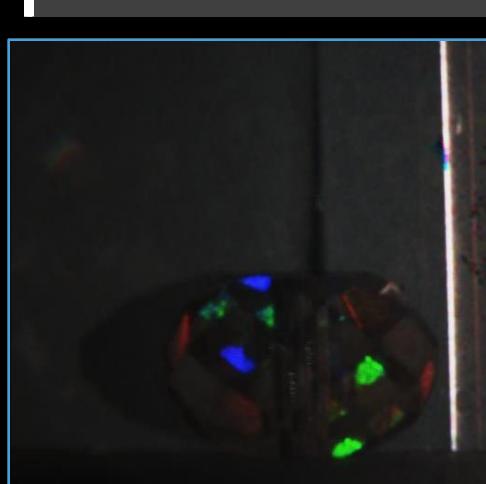
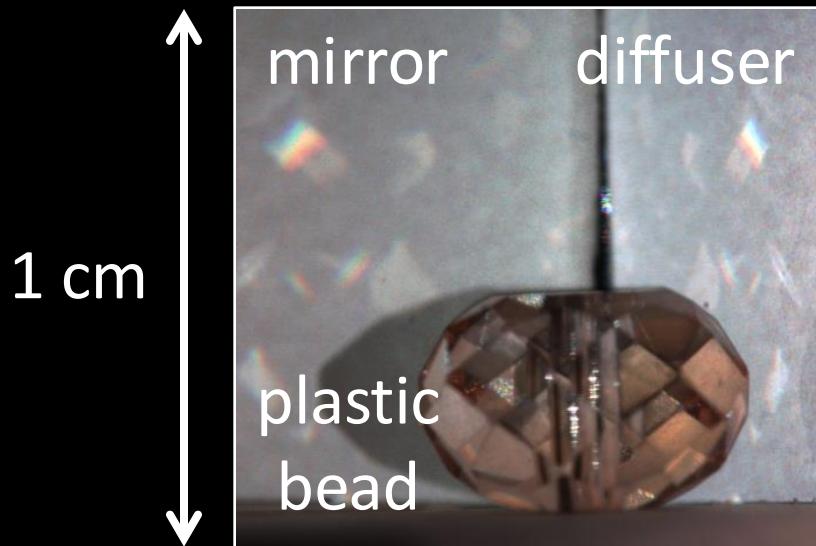
Chess knight and mirror



Subsurface scattering



Dispersion



facets changing color

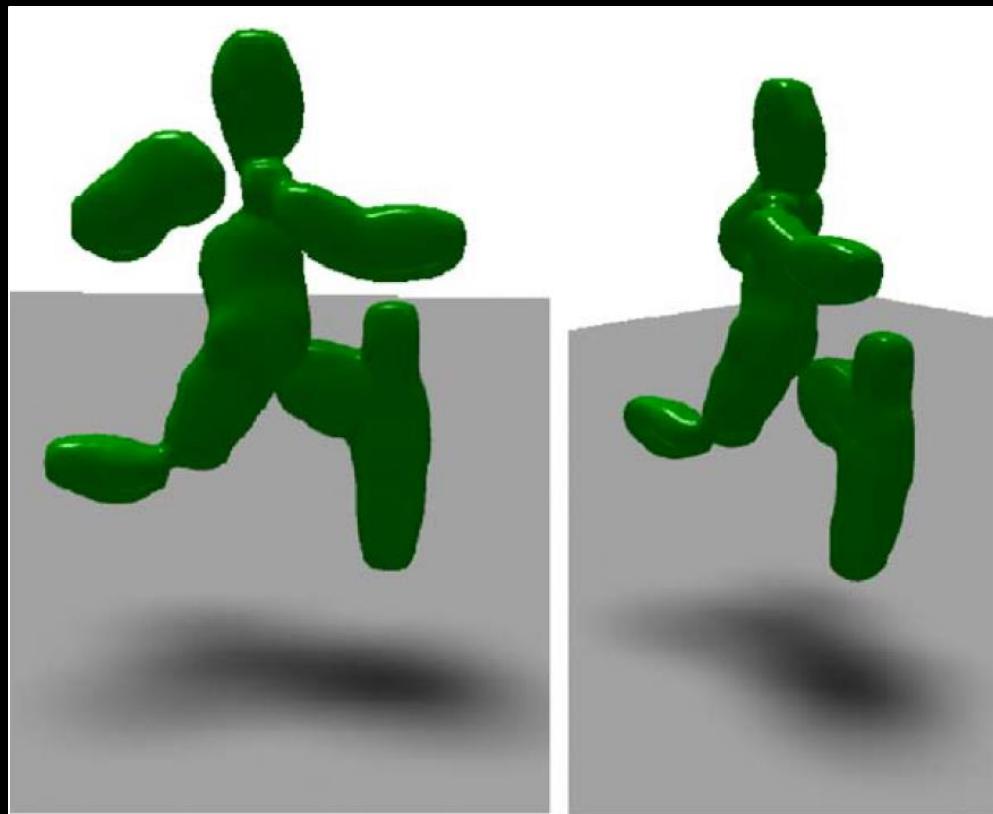
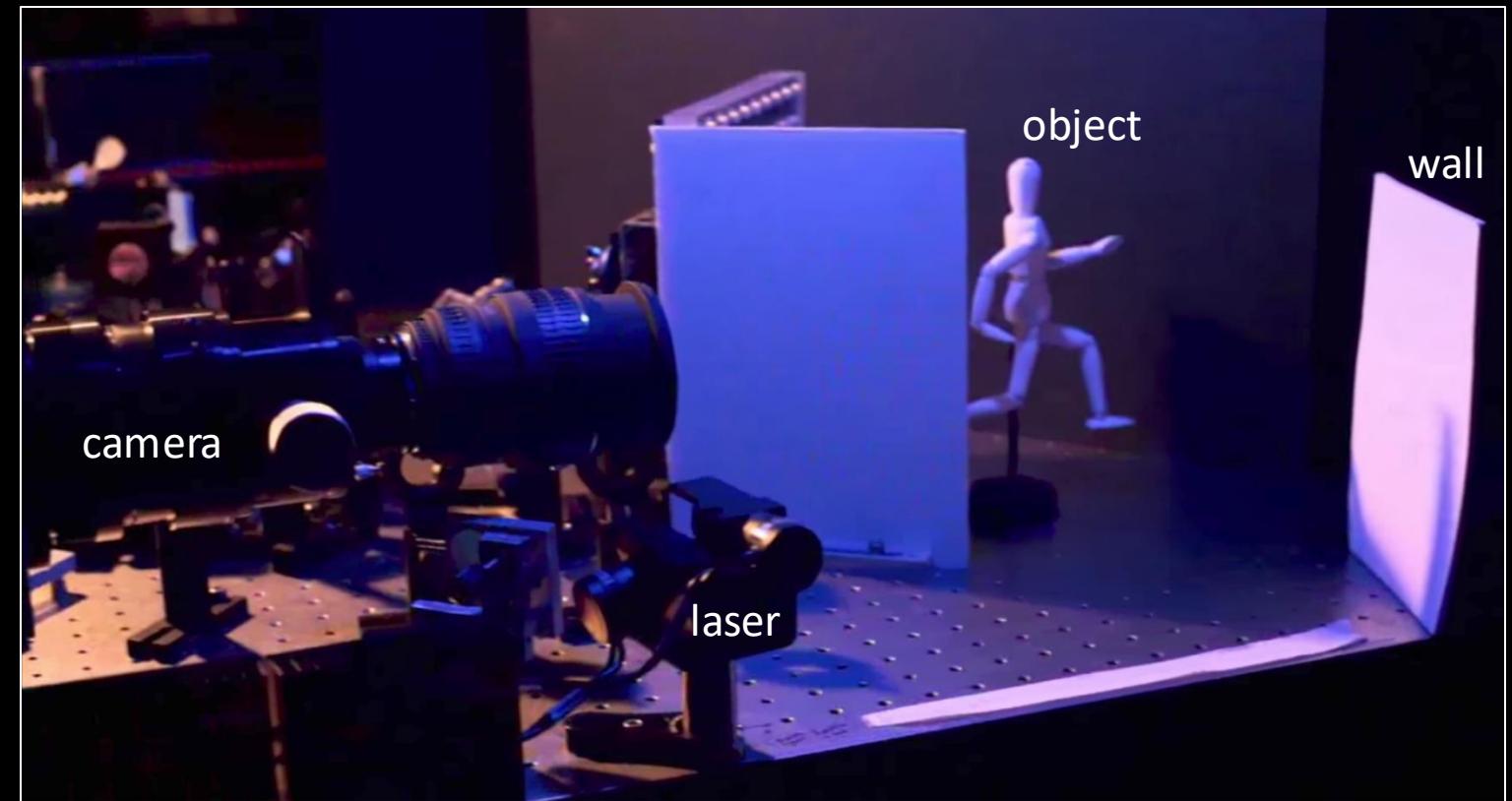


surface reflections
surface-wall reflections



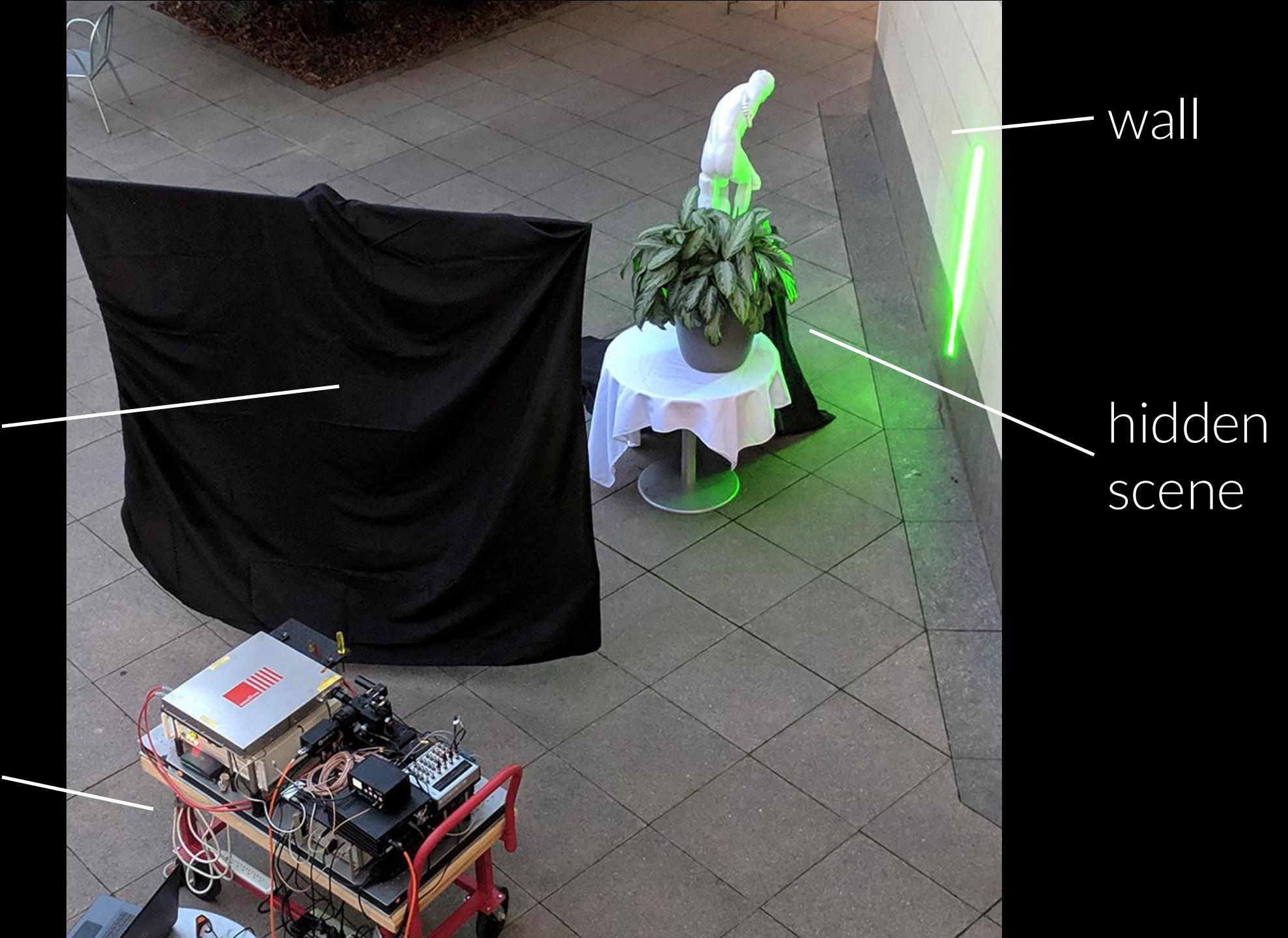
rainbow

Non-line-of-sight Imaging



Velten et al., Nature Communications 2012

NLOS
imaging
system



scanning mirrors

laser

detector



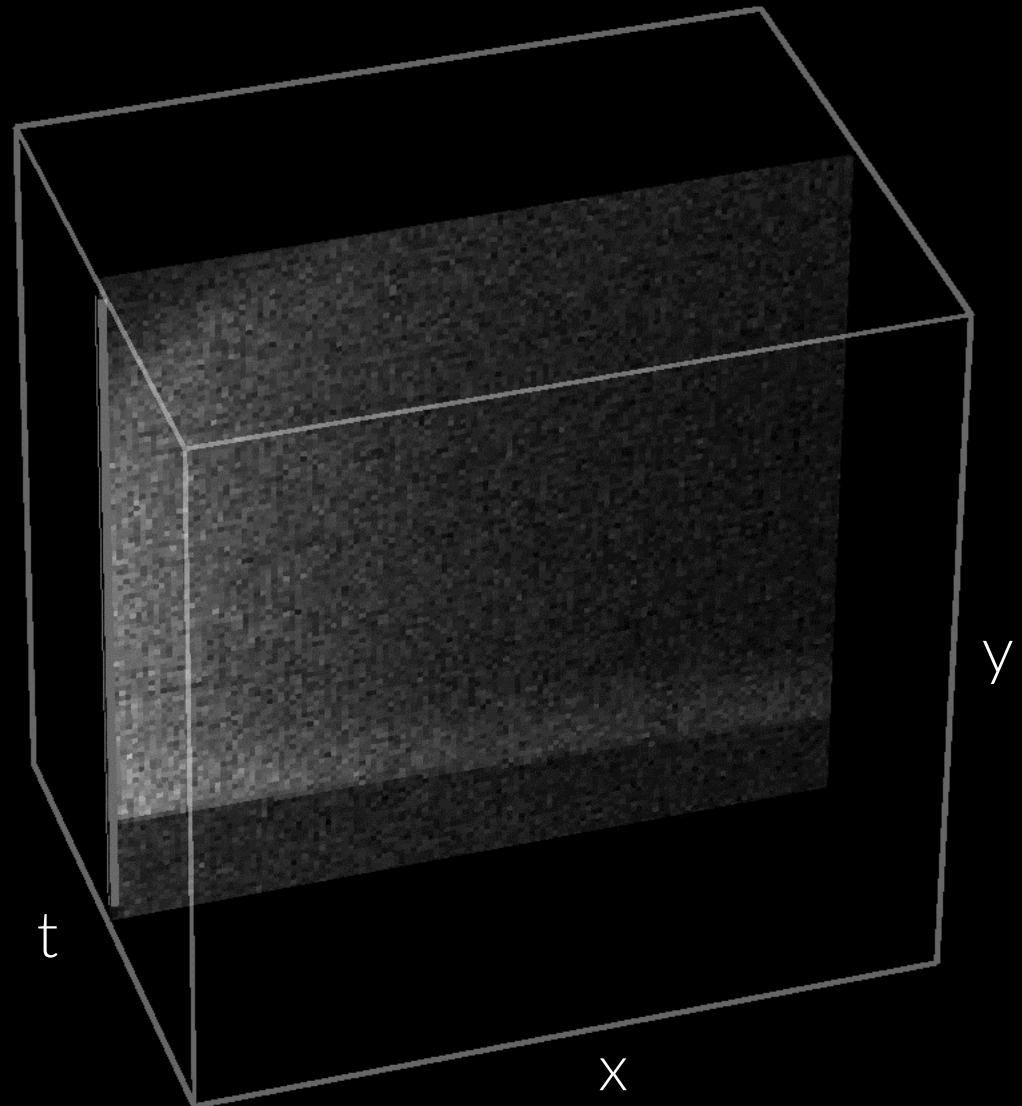
resolution: 128 x 128
area: 2 m x 2 m



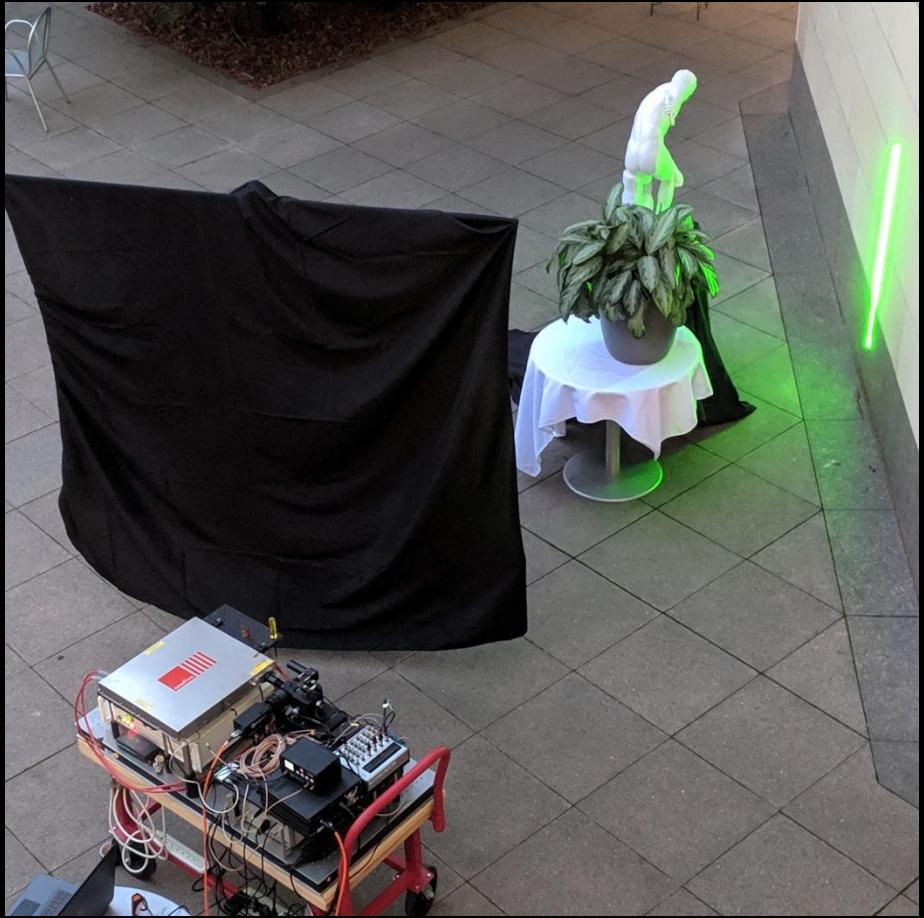
scene photo



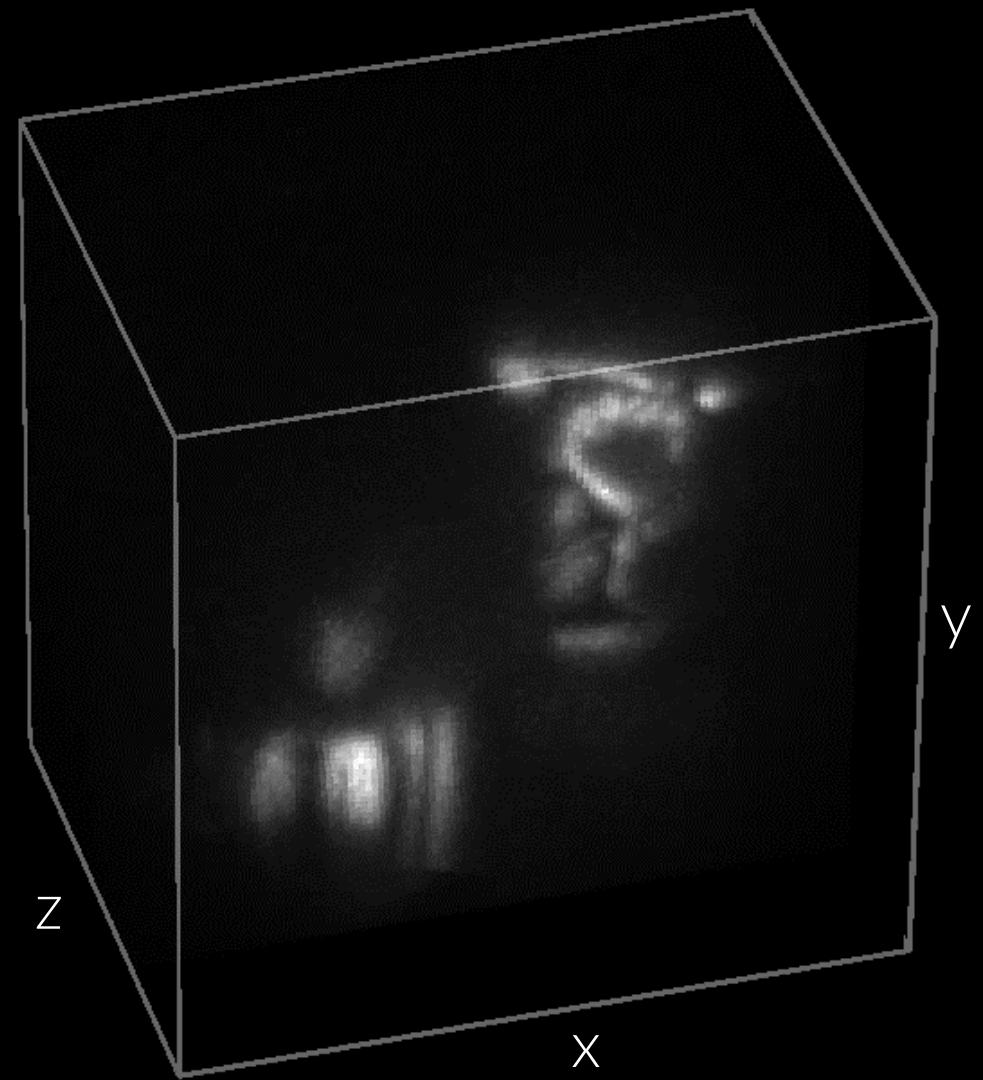
measurements



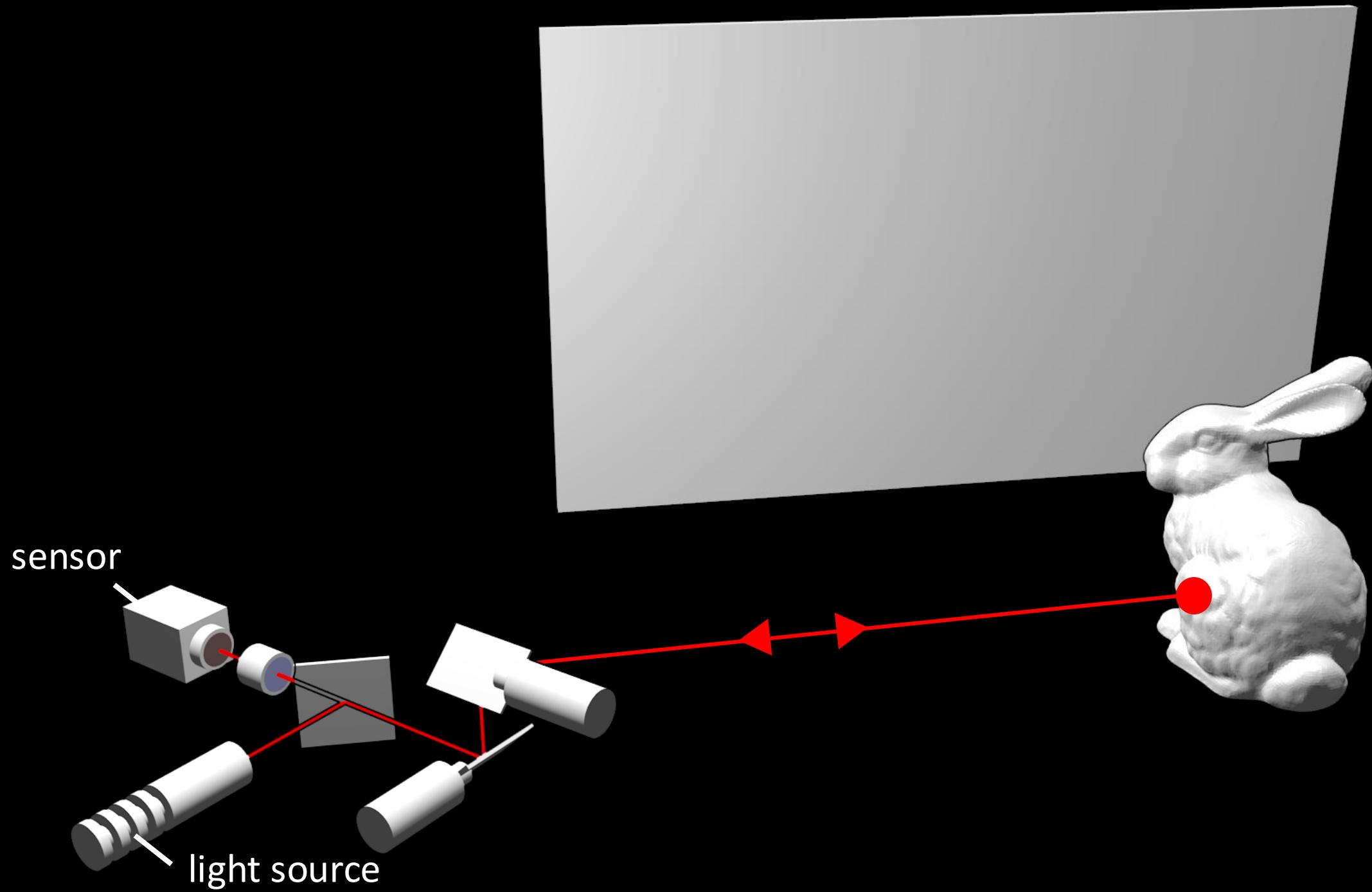
scene photo

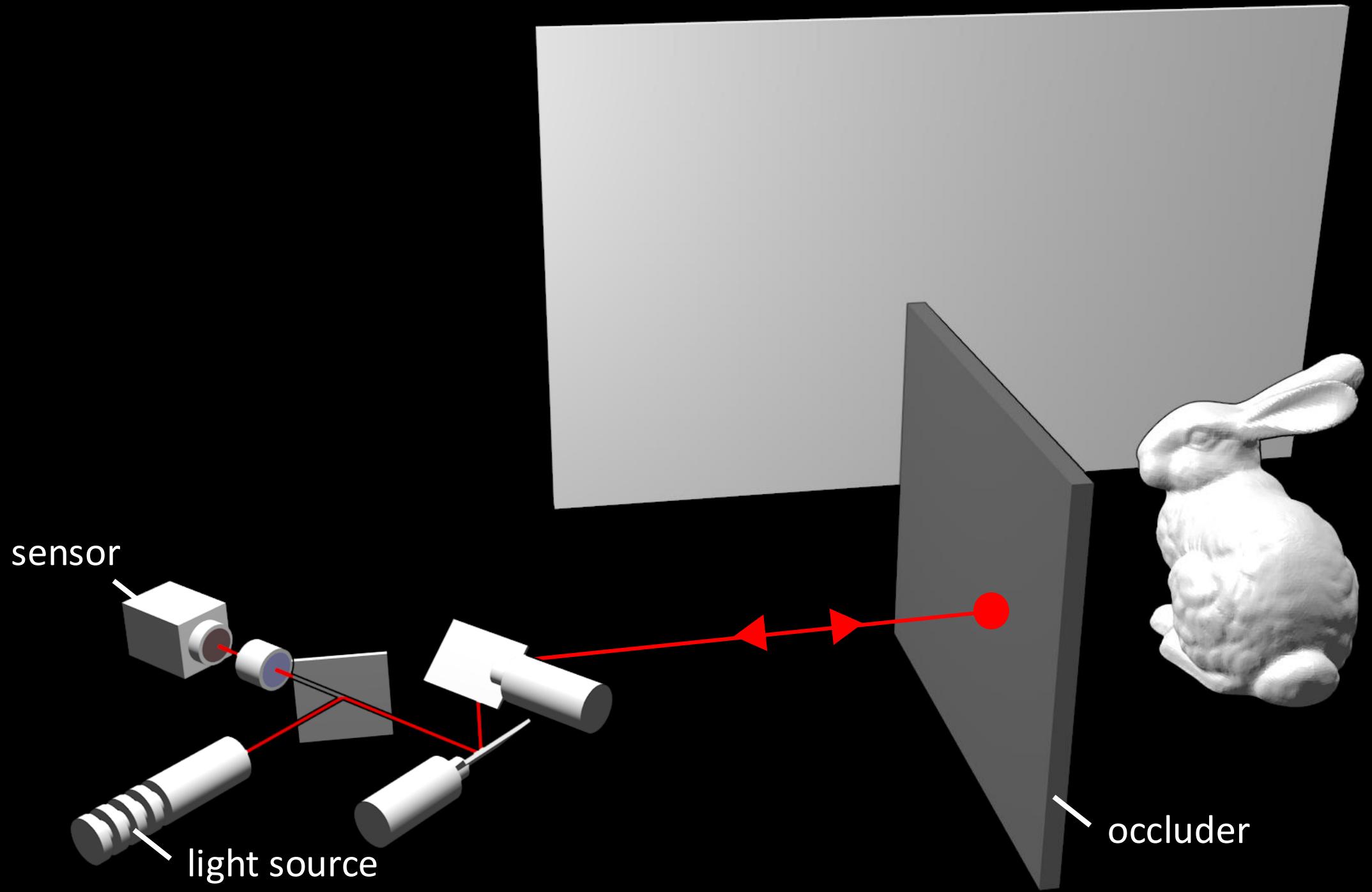


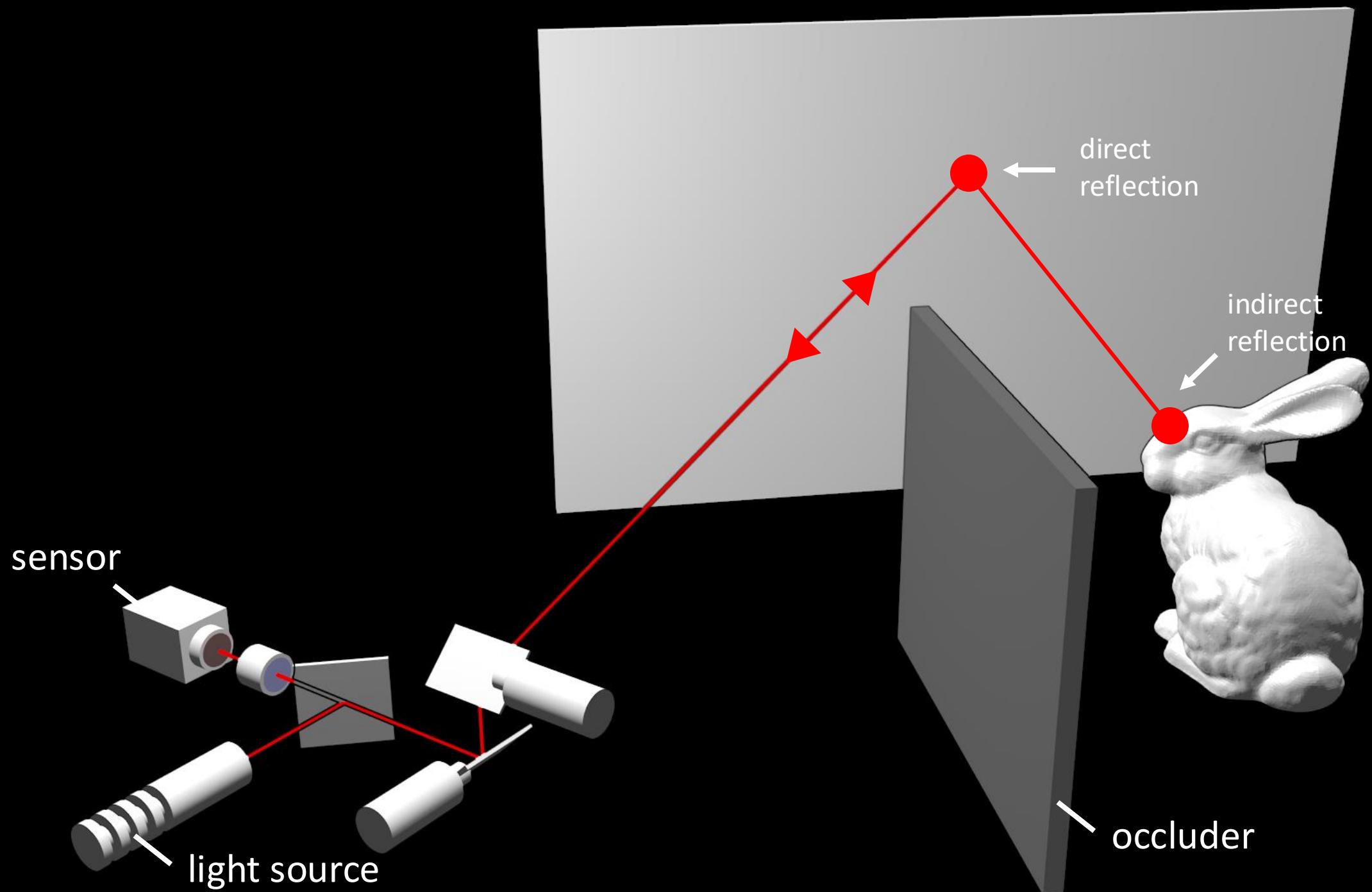
reconstruction



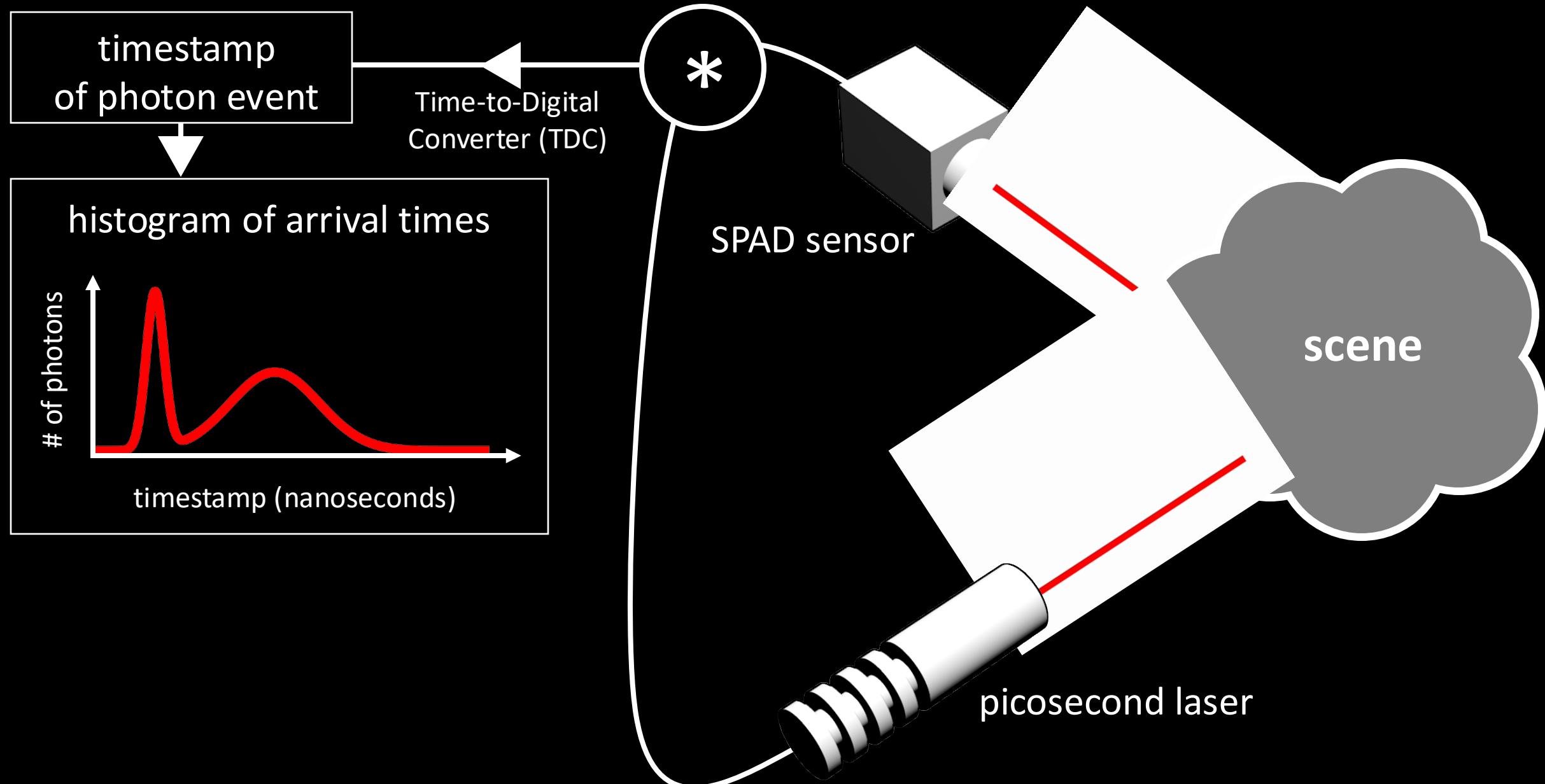
Dimensions: 2 m x 2 m x 1.5 m

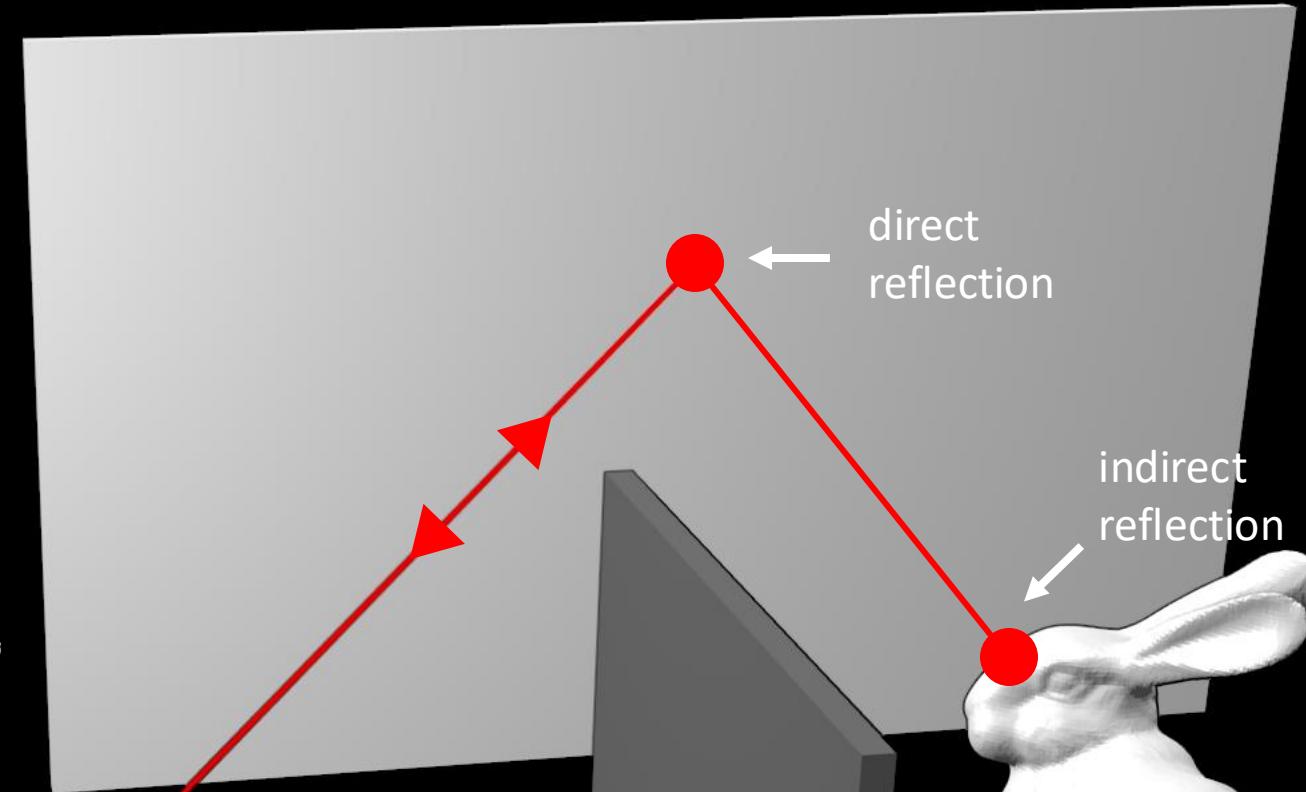
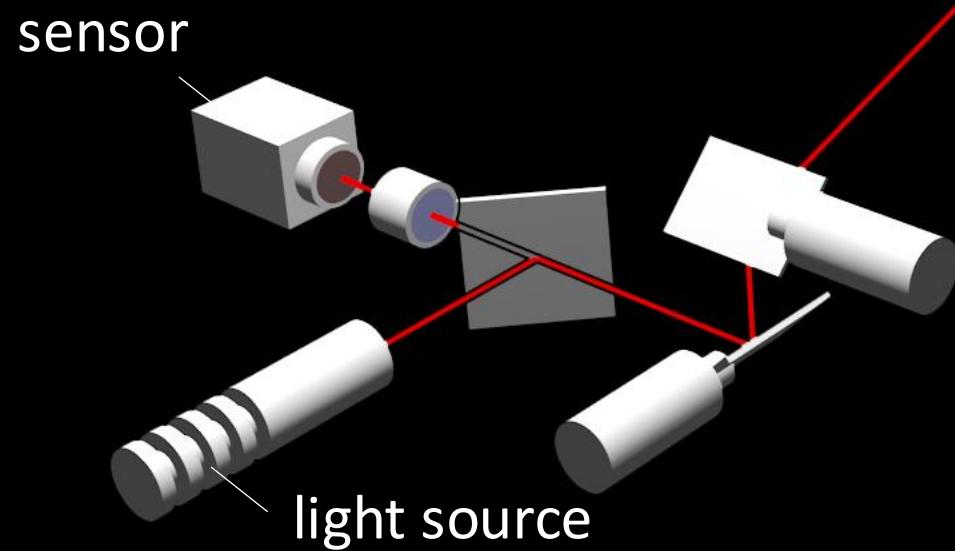
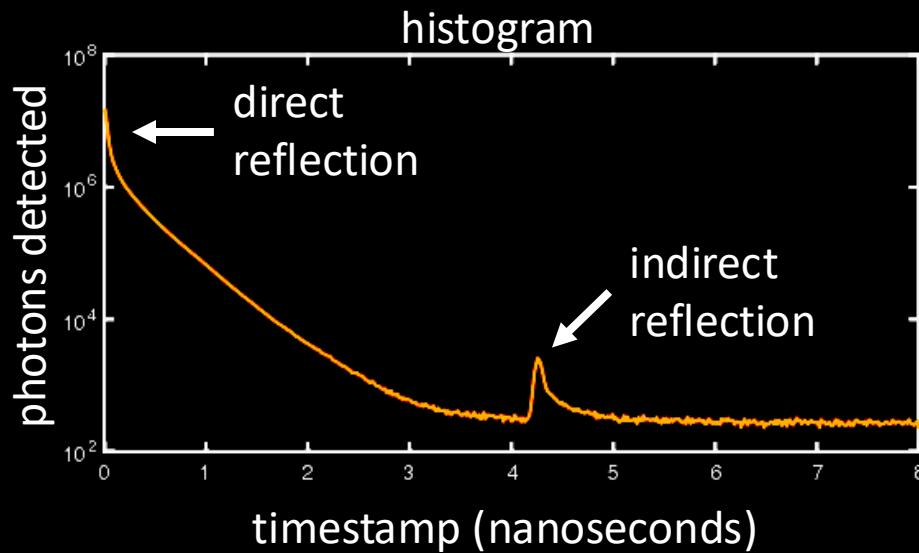


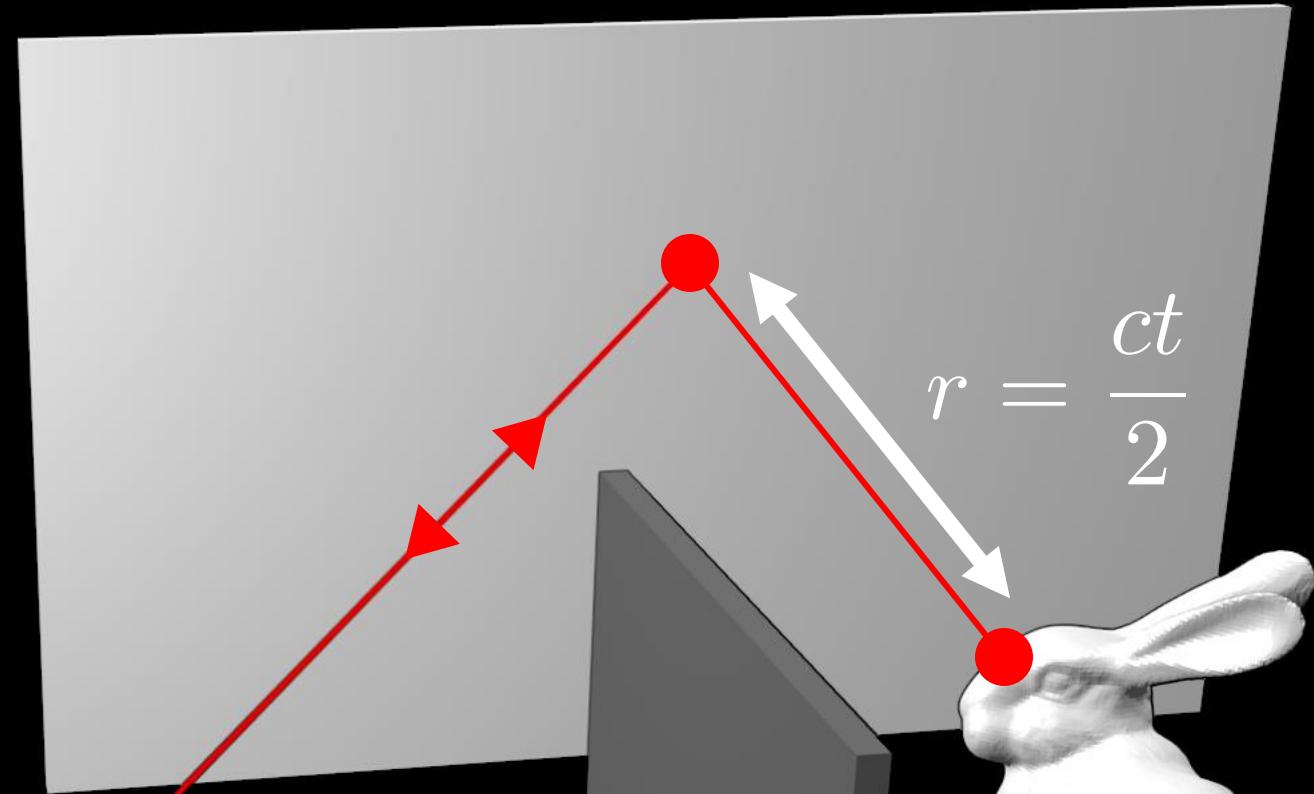
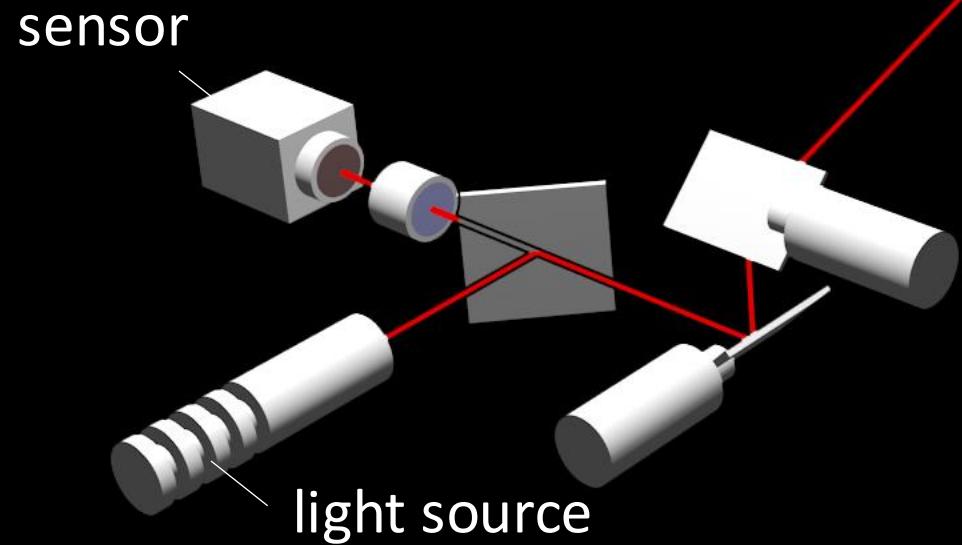
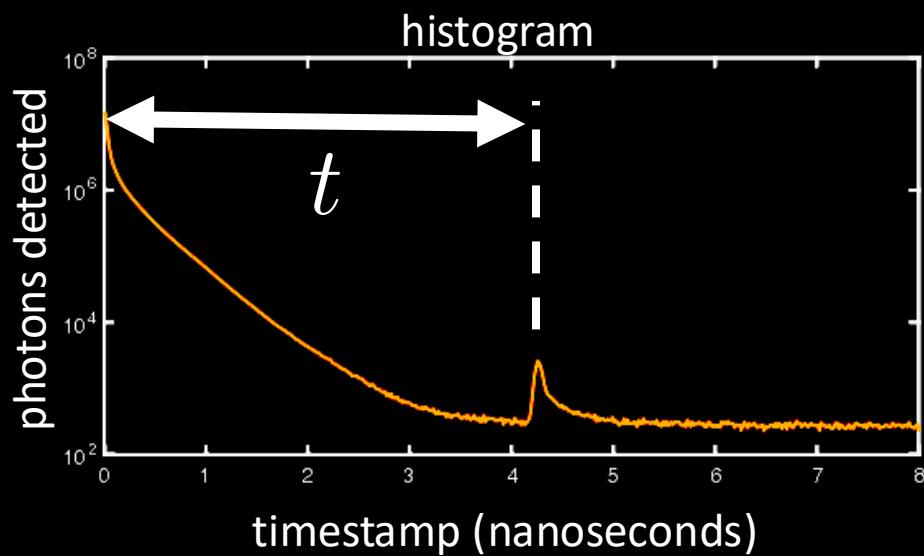




single photon avalanche diodes (SPADS)

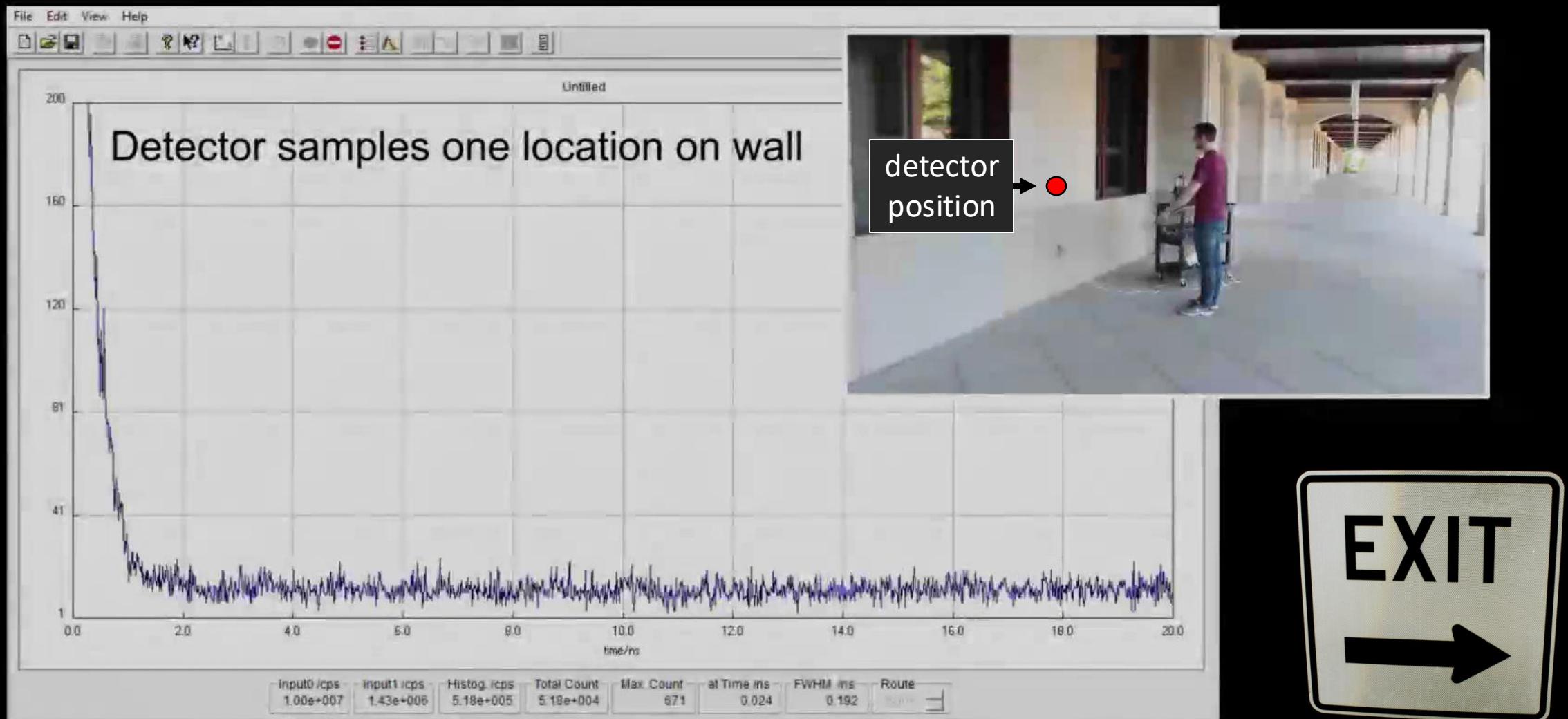




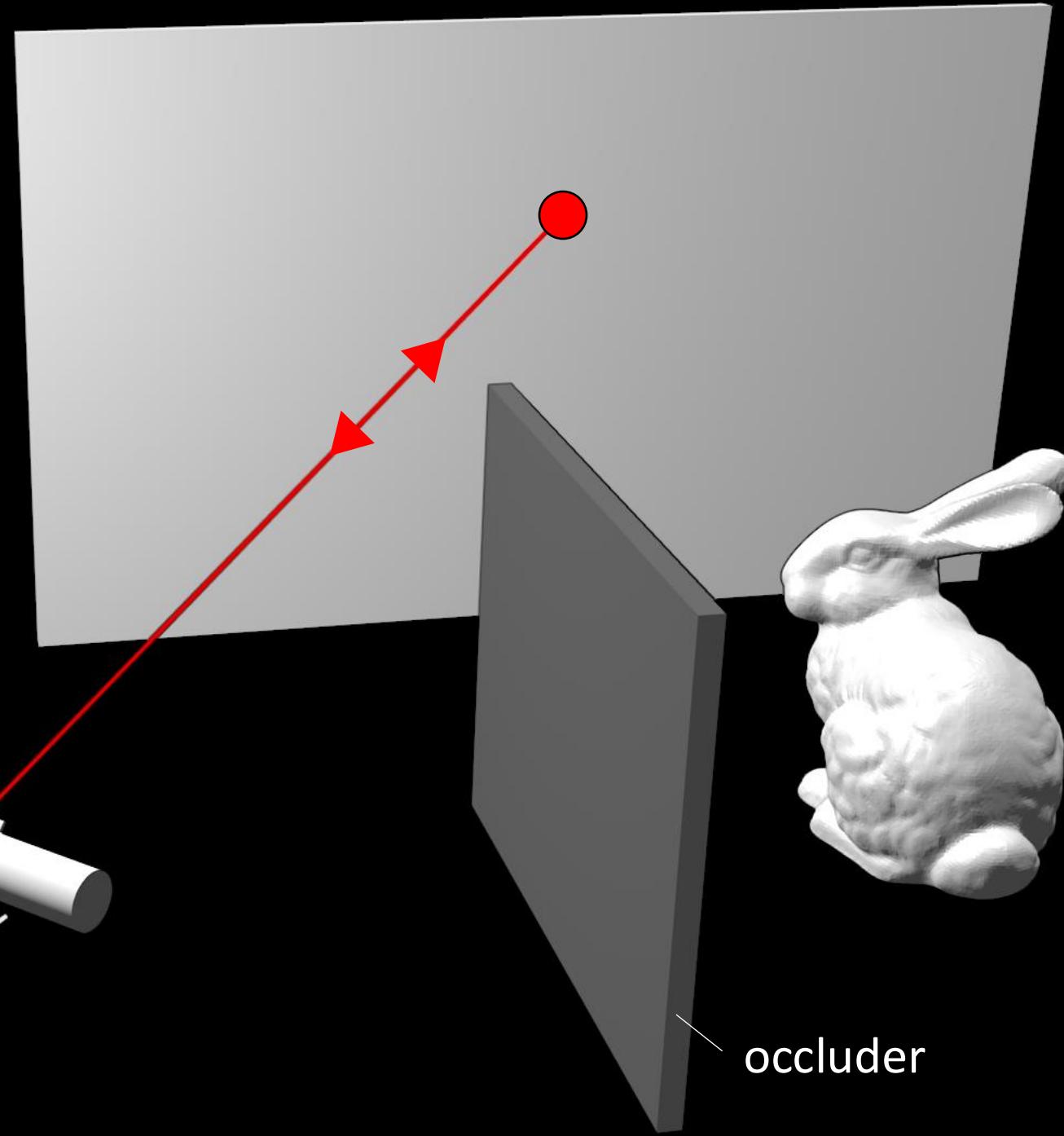
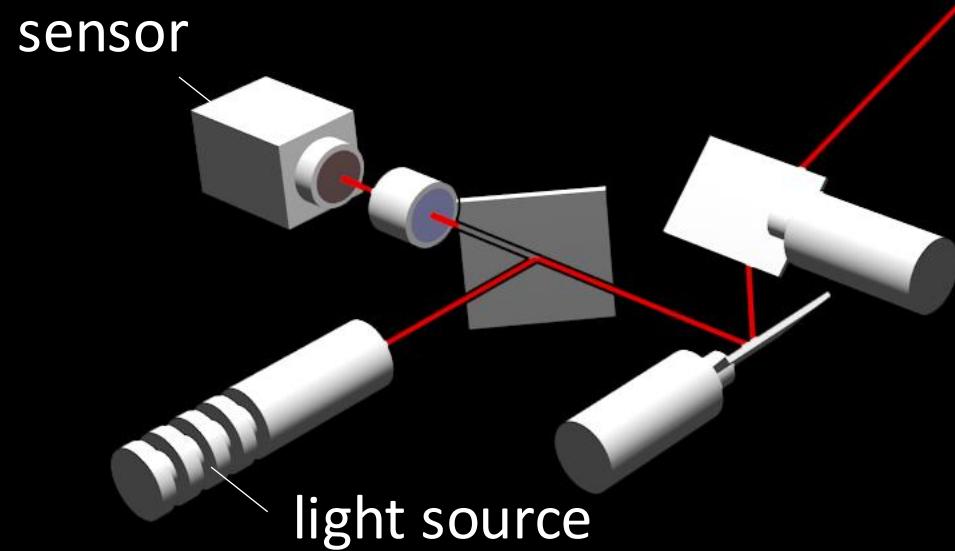
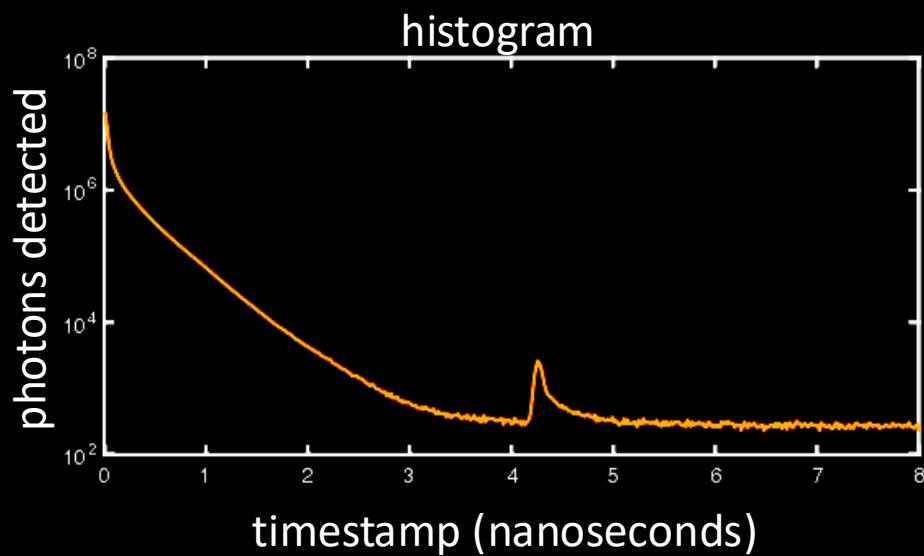


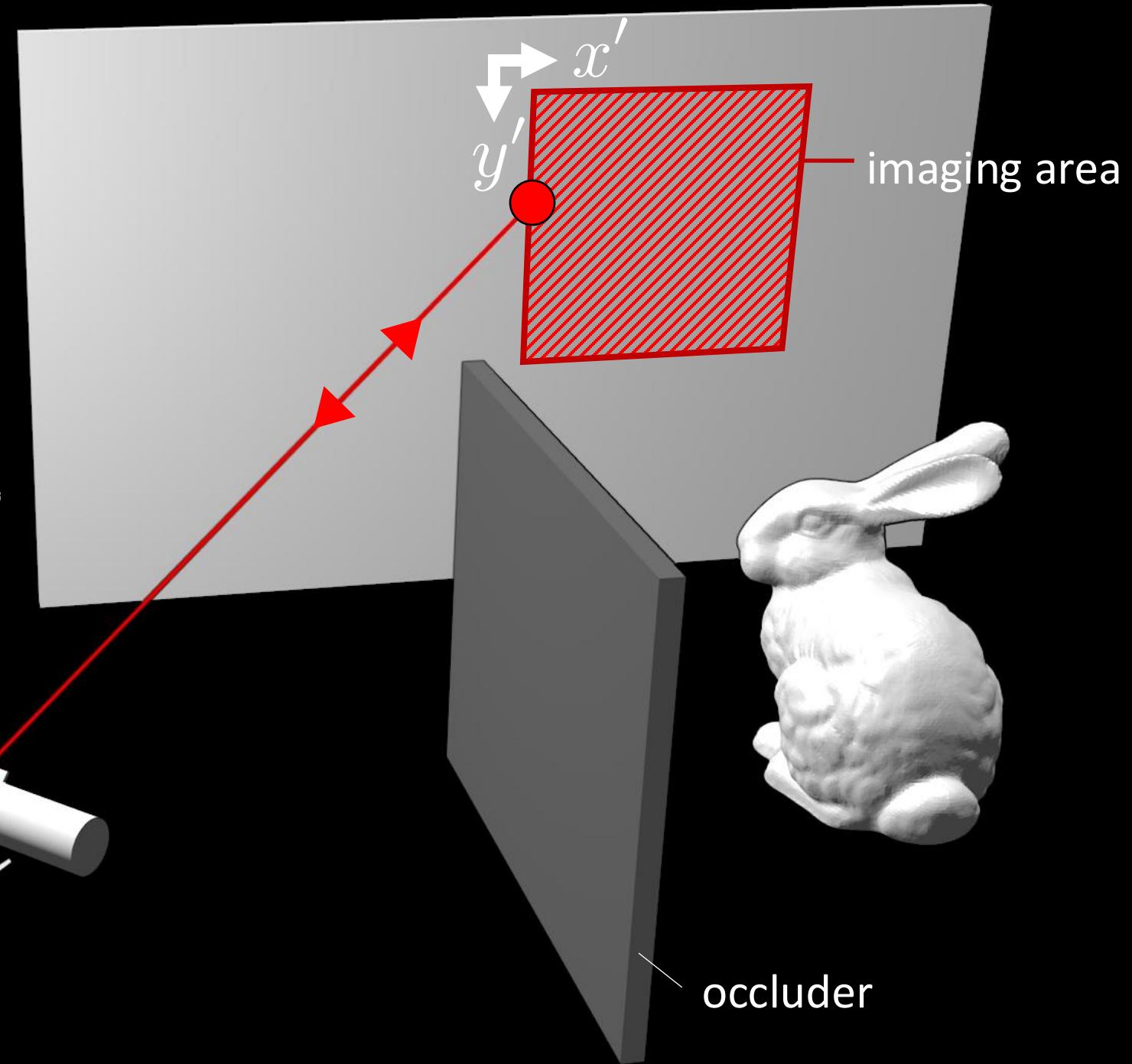
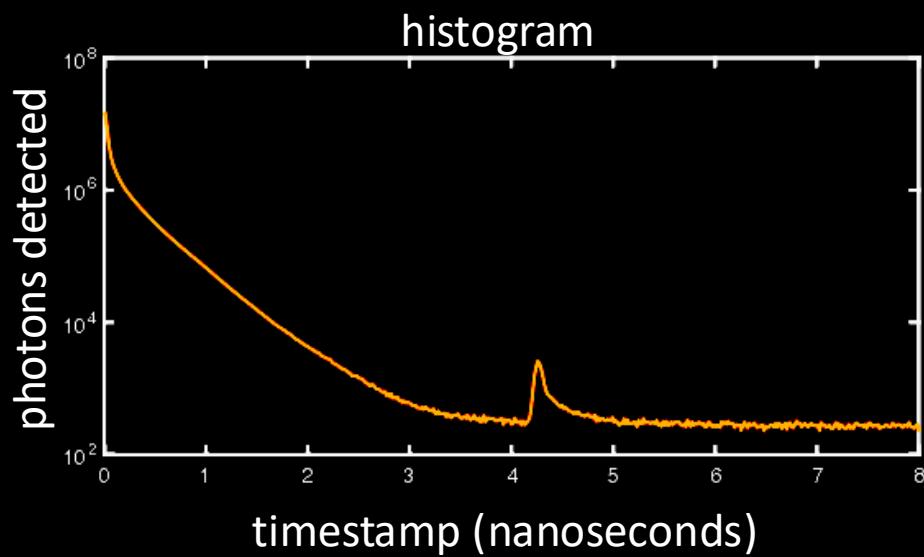
occluder

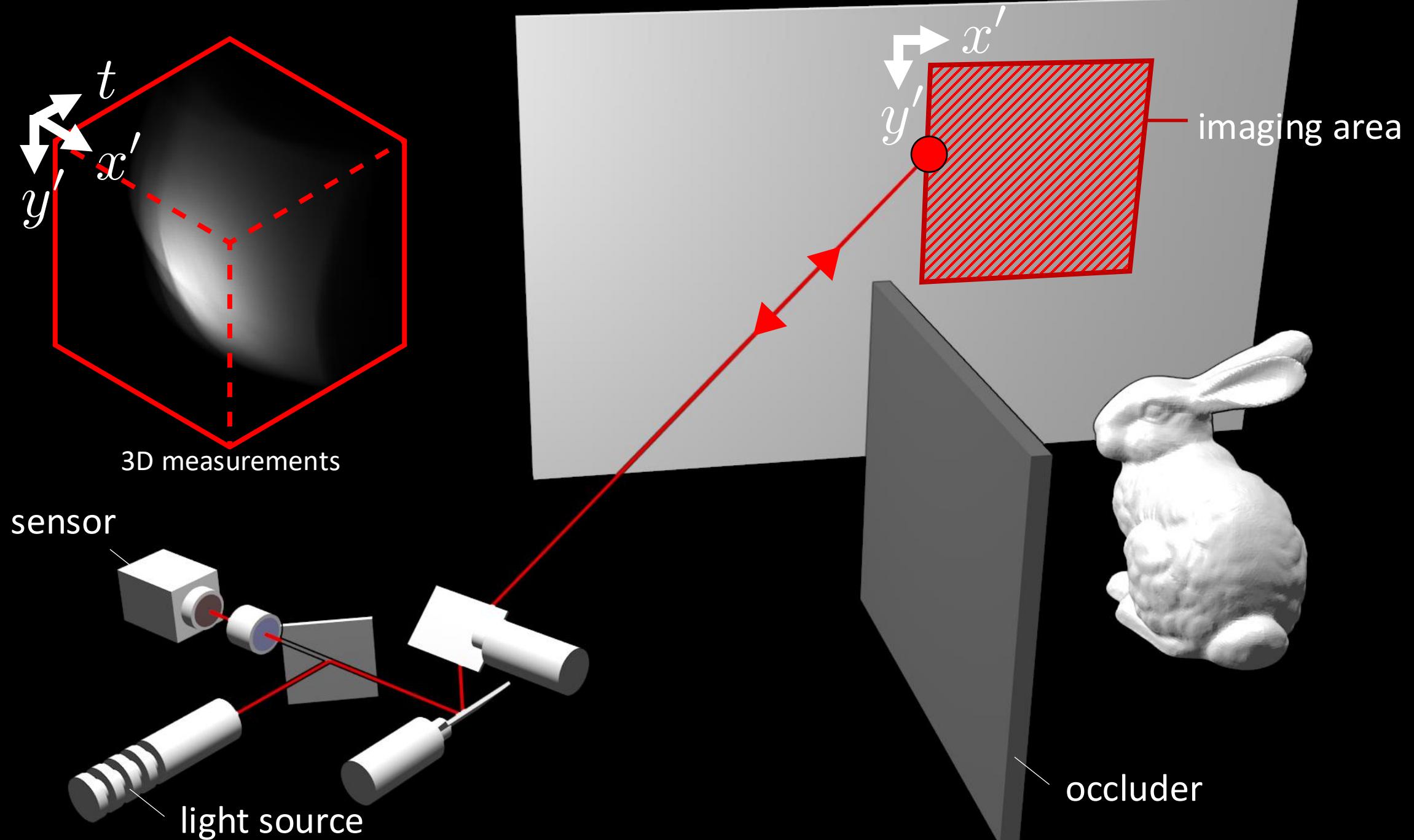
RAW histogram (10 FPS)

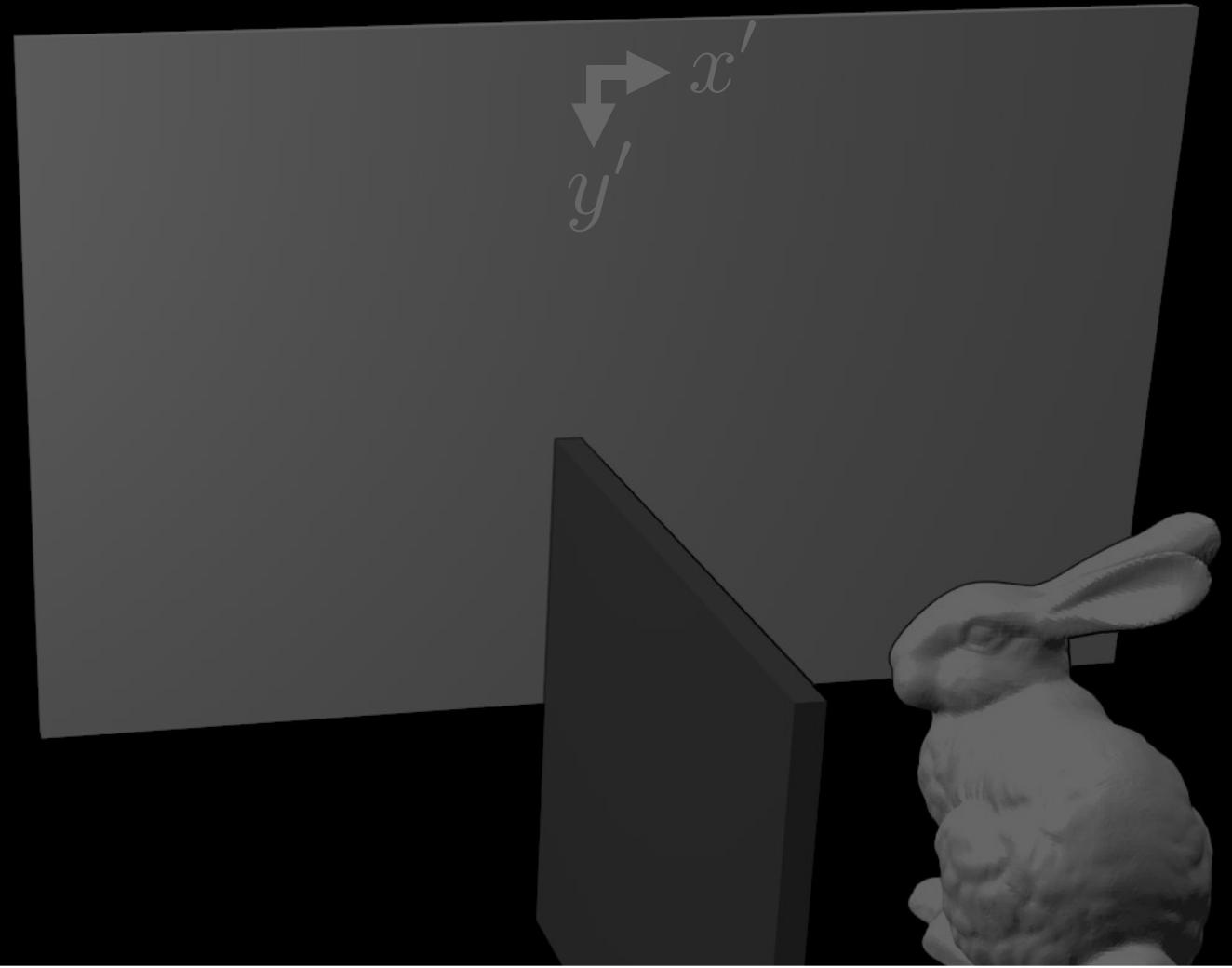
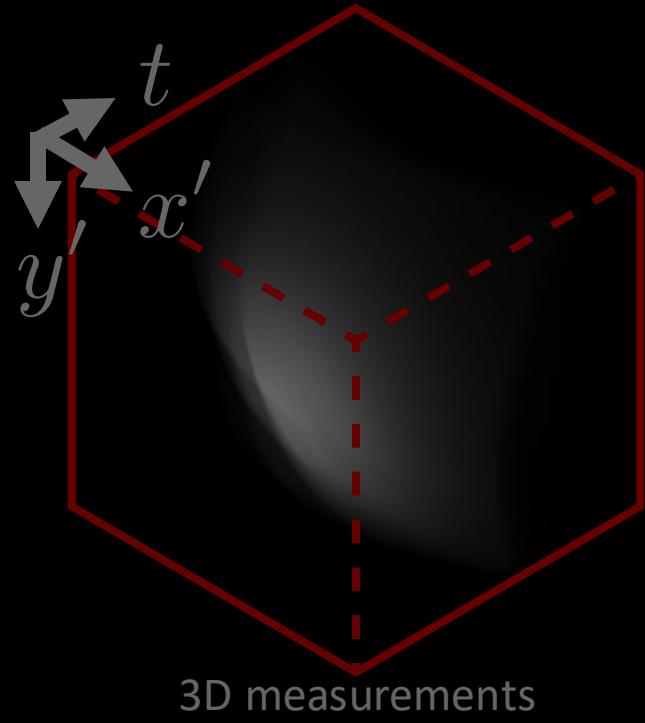


object



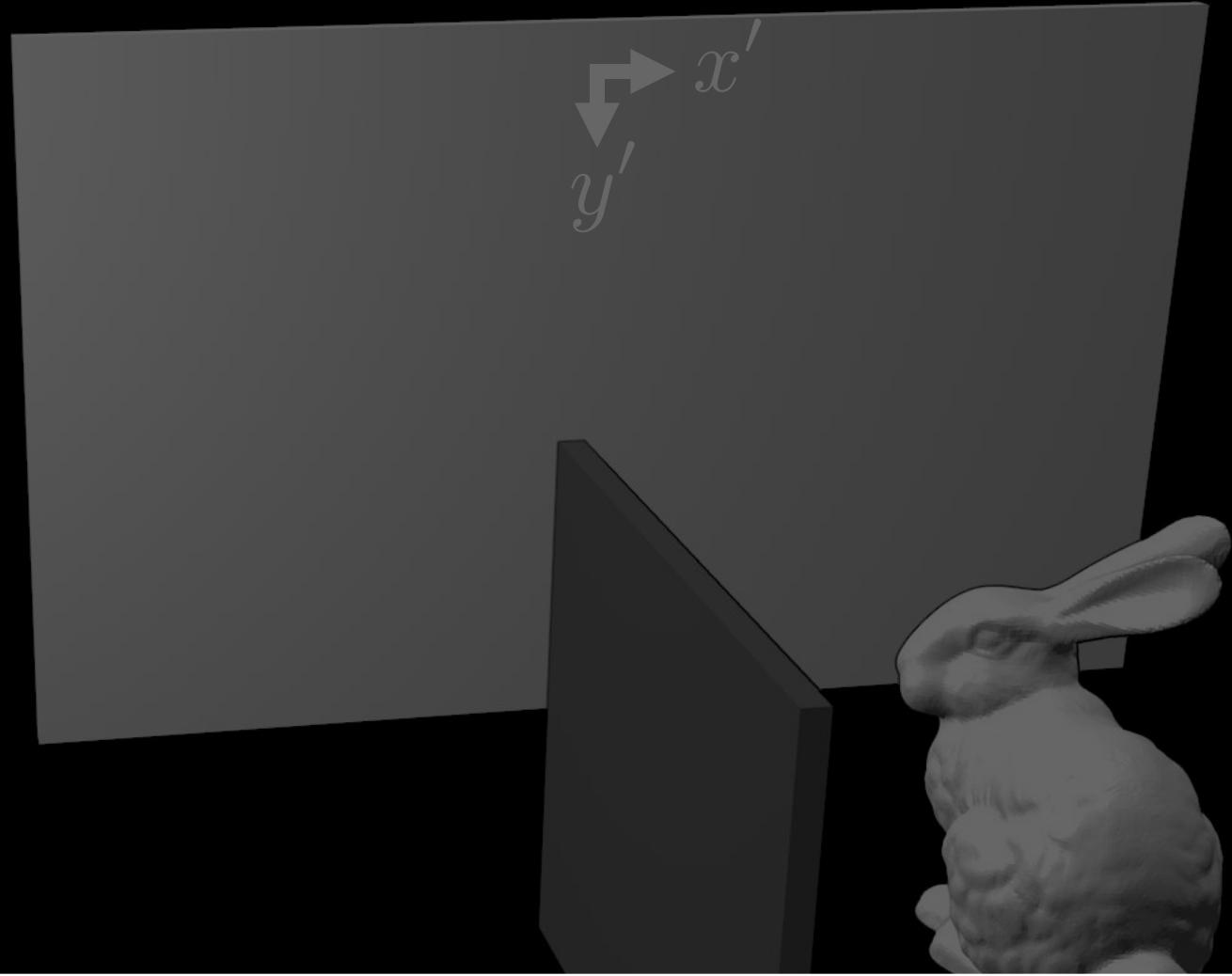
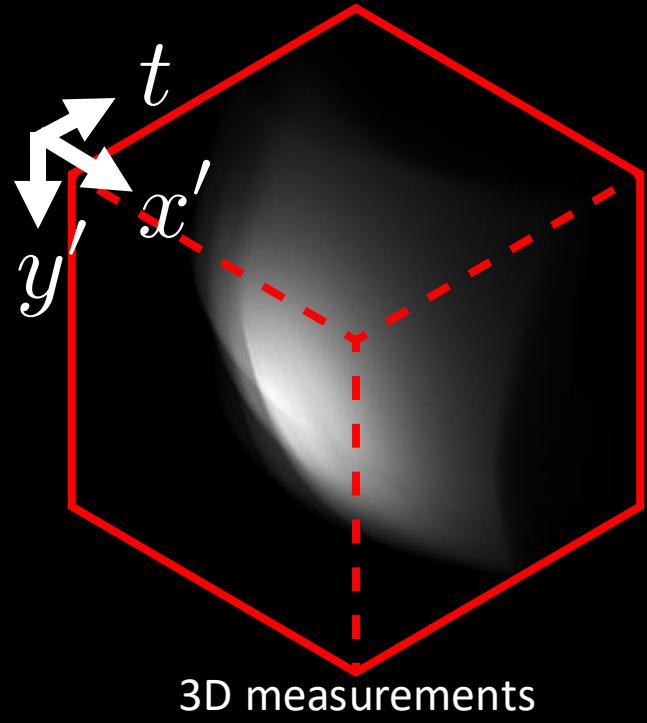






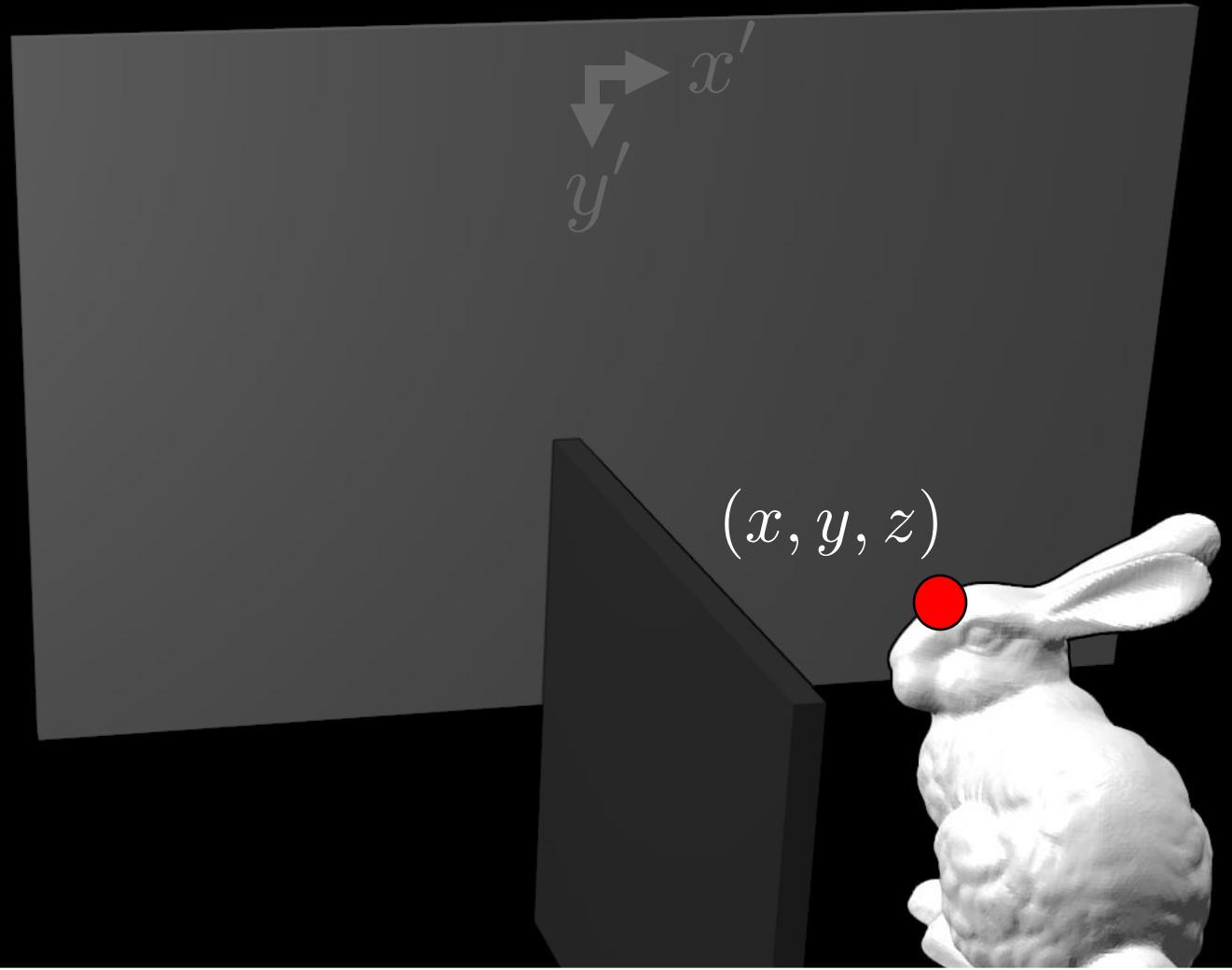
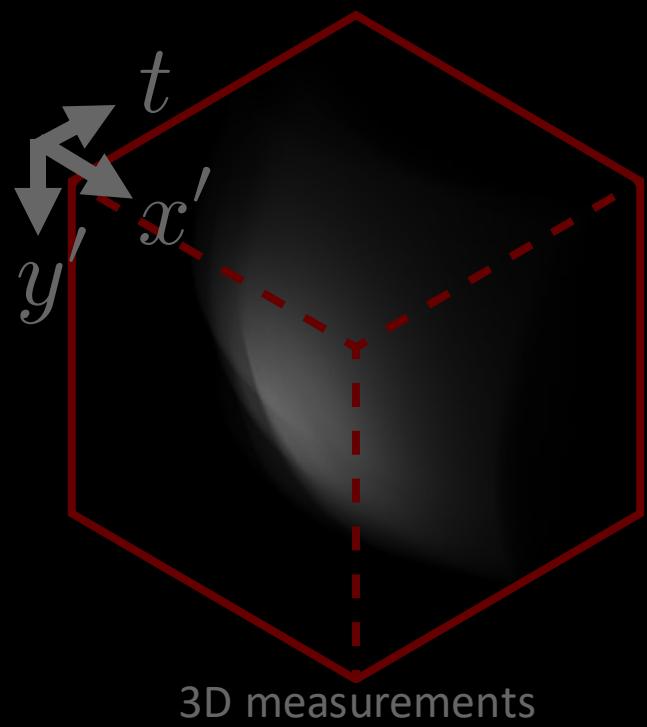
$$\tau(x', y', t) = \iiint_{\Omega} \frac{1}{r_l^2 r^2} \delta(r_l + r - tc) \cdot \rho(x, y, z) \, dx \, dy \, dz$$

[] 3D measurements [] radiometric term [] geometric term [] hidden 3D volume



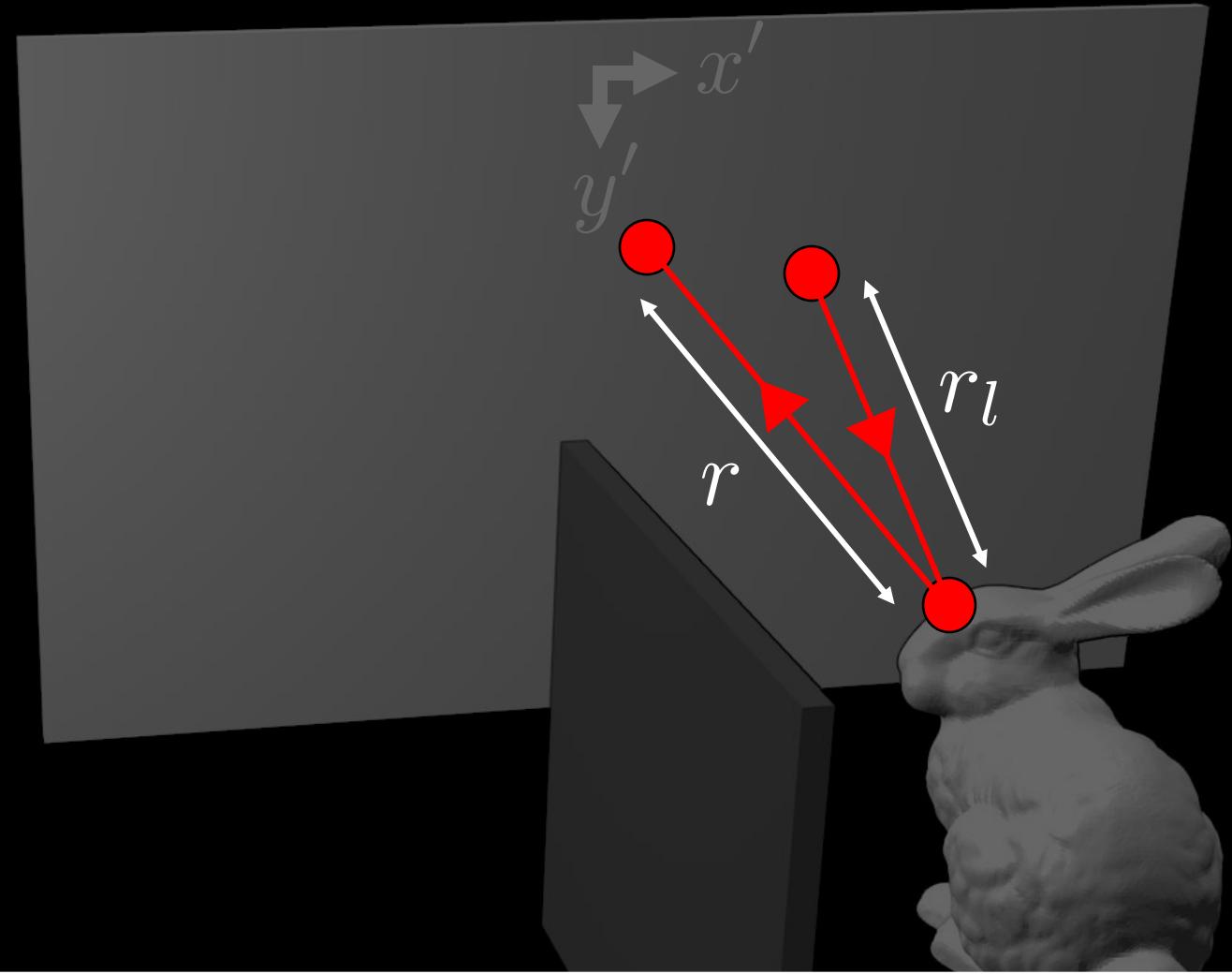
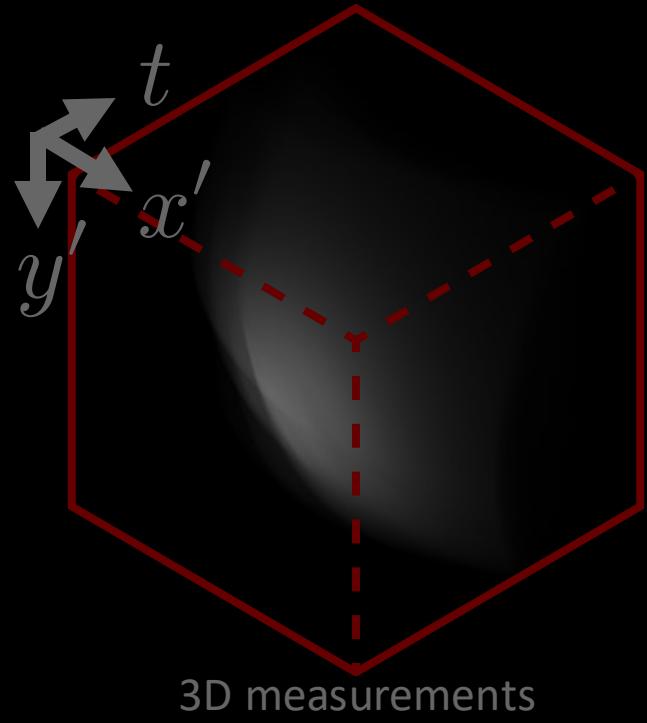
$$\tau(x', y', t) = \iiint_{\Omega} \frac{1}{r_l^2 r^2} \delta(r_l + r - tc) \cdot \rho(x, y, z) \, dx \, dy \, dz$$

[] 3D measurements [] radiometric term [] geometric term [] hidden 3D volume



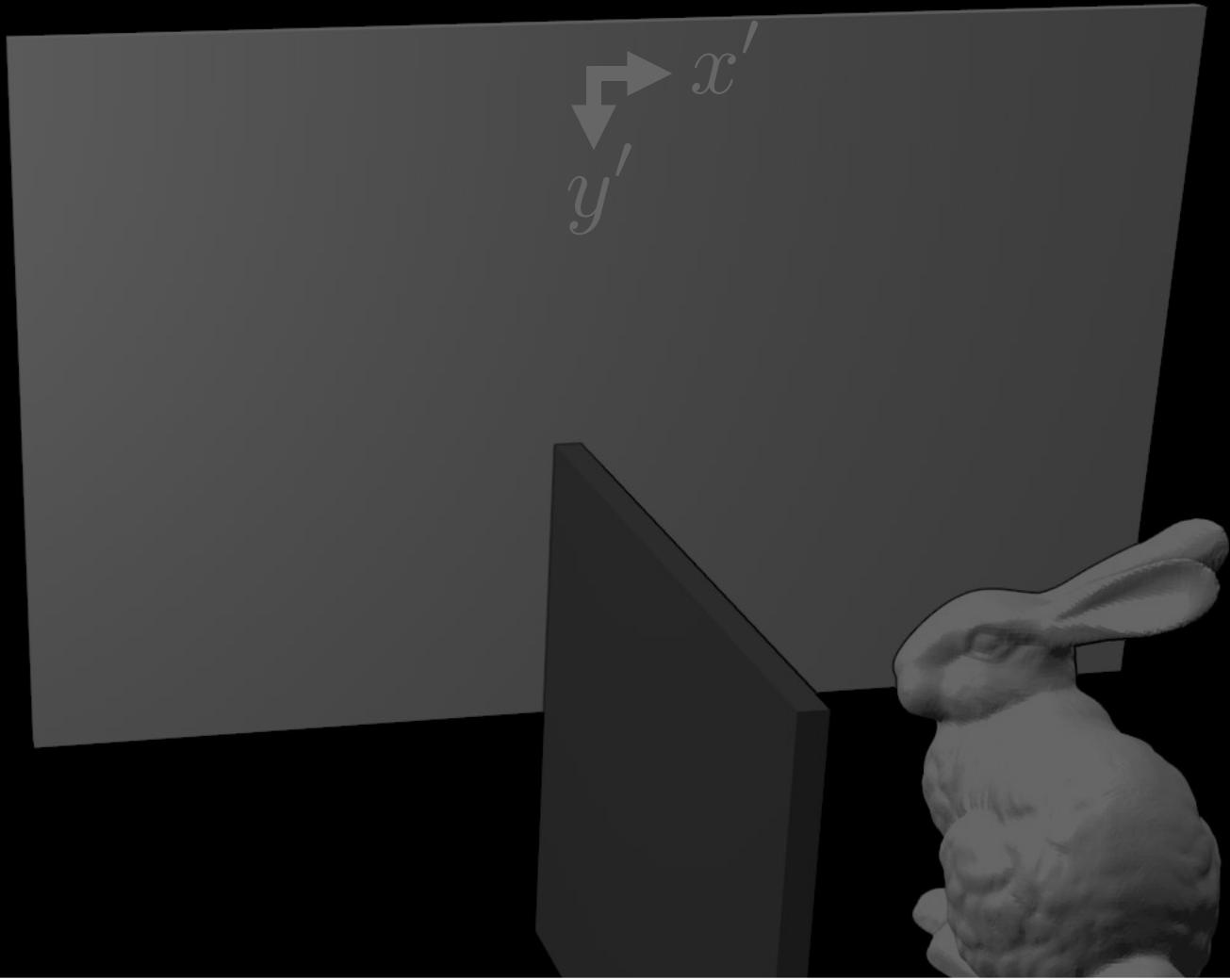
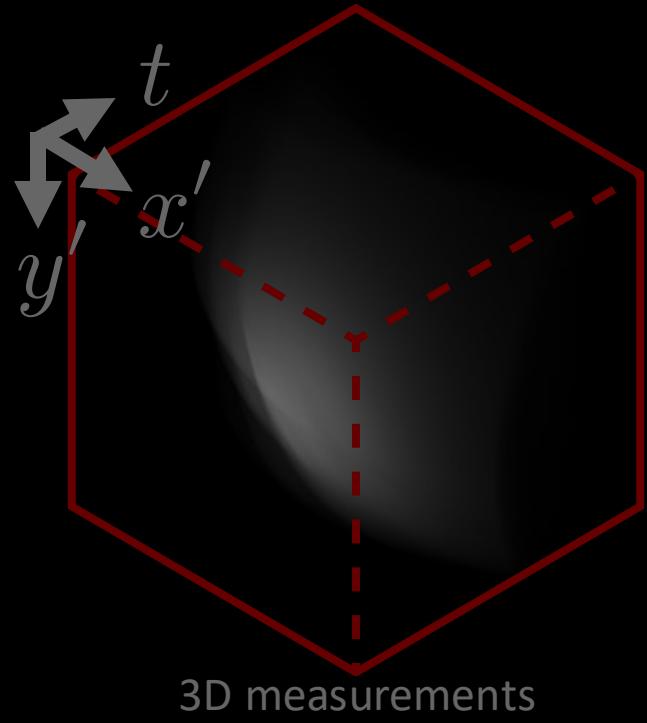
$$\tau(x', y', t) = \iiint_{\Omega} \frac{1}{r_l^2 r^2} \delta(r_l + r - tc) \cdot \rho(x, y, z) \, dx \, dy \, dz$$

3D measurements
radiometric term
geometric term
hidden 3D volume

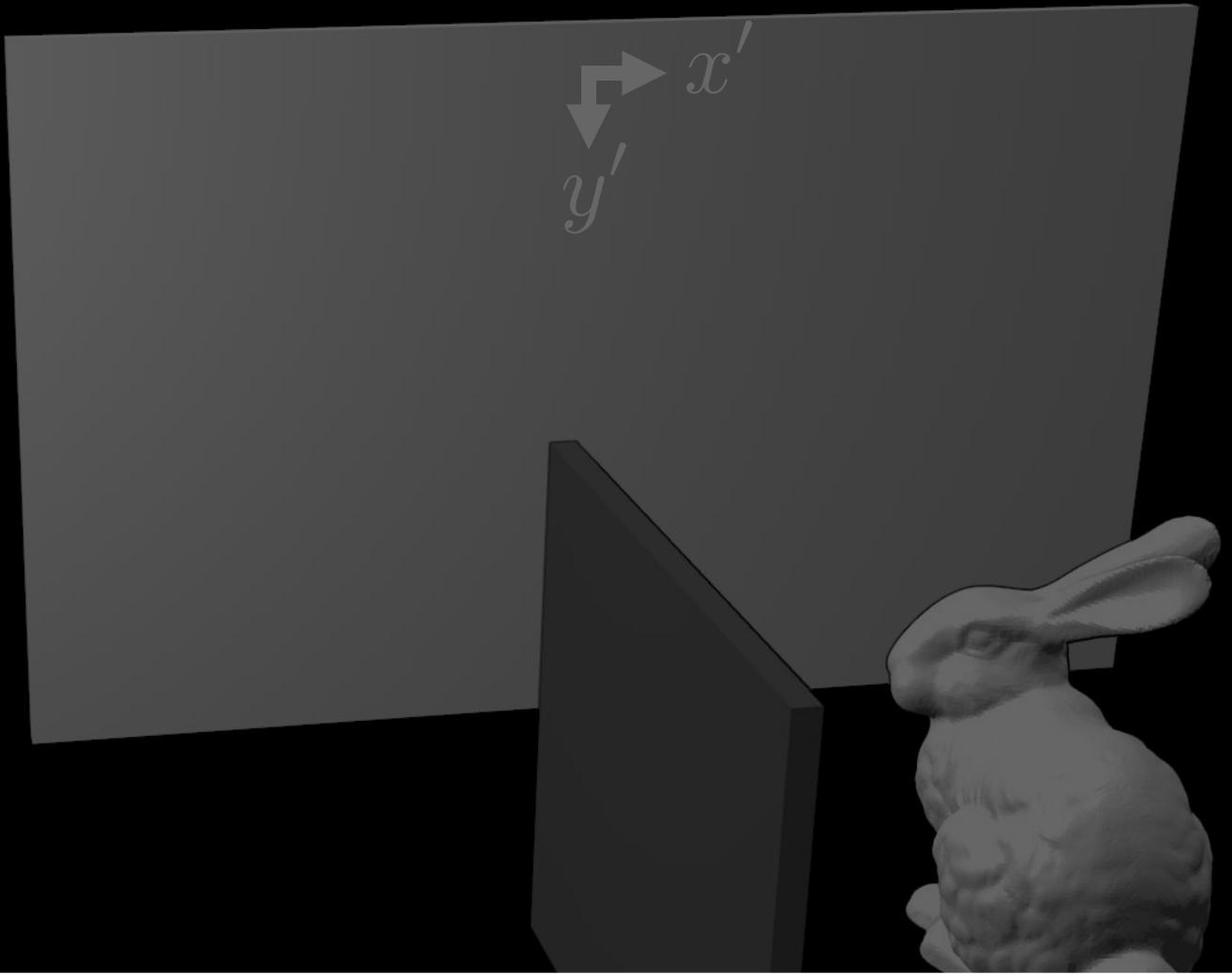
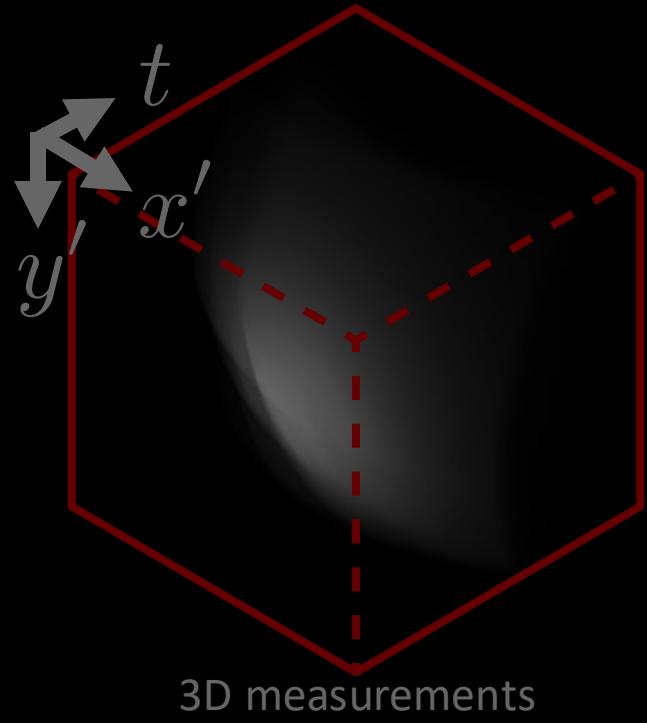


$$\tau(x', y', t) = \iiint_{\Omega} \frac{1}{r_l^2 r^2} \delta(r_l + r - tc) \cdot \rho(x, y, z) \, dx \, dy \, dz$$

3D measurements radiometric term geometric term hidden 3D volume



$$\tau(x', y', t) = \iiint_{\Omega} \frac{1}{r_l^2 r^2} \delta(r_l + r - tc) \cdot \rho(x, y, z) \, dx \, dy \, dz$$



$$\tau(x', y', t) = \underbrace{\iiint_{\Omega} \frac{1}{r_l^2 r^2} \delta(r_l + r - tc)}_{\mathcal{T}} \cdot \underbrace{\rho(x, y, z)}_{\mathcal{A}} dx dy dz$$

\times ρ

NLOS image formation mode:

$$\tau = \mathbf{A} \rho$$

↑
measurements ↑ transport matrix ↘ unknown volume
 $n^3 \times 1$ $n^3 \times n^3$ $n^3 \times 1$

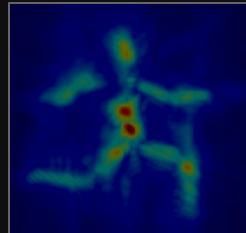
PROBLEM: \mathbf{A} extremely large in practice
(e.g., for $n = 100$, \mathbf{A} has 1 trillion elements)

Backpropagation [Velten 12, Buttafava 15]

Flops: $O(n^5)$

Memory: $O(n^3)$

Runtime: Approx. 10 min.



Iterative Inversion [Gupta 12, Heide 13]

Flops: $O(n^5)$ per iter.

Memory: $O(n^5)$

Runtime: > 1 hour

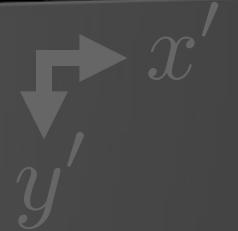


Our approach

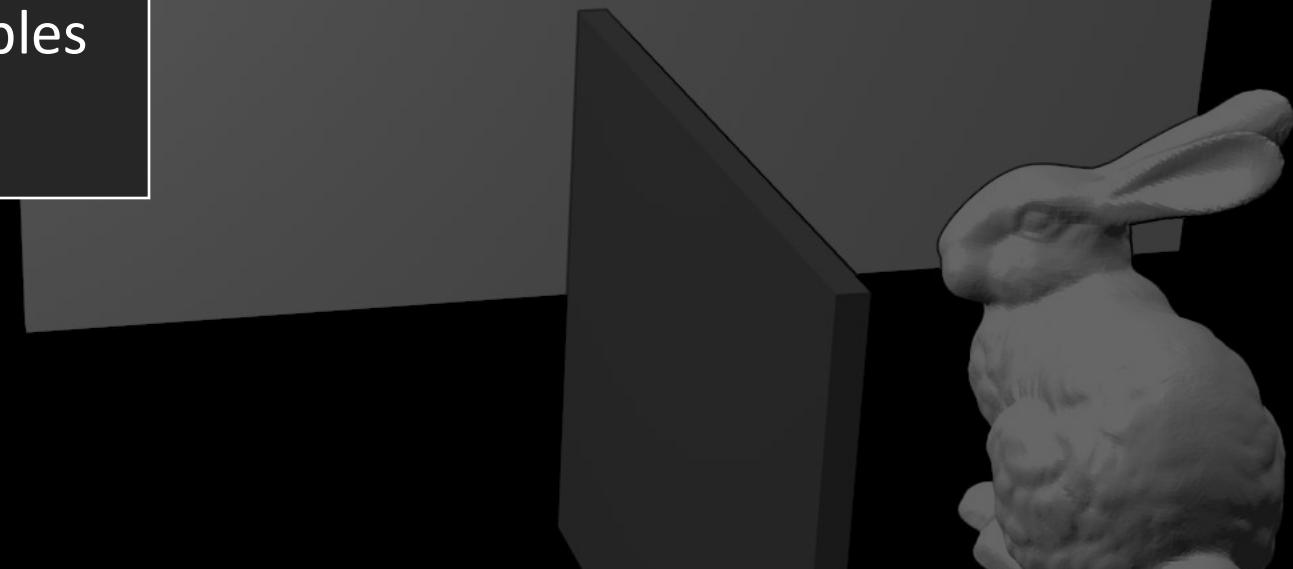
express image formation model as a 3D convolution, by:

1. confocalizing measurements
2. performing a change of variables
(set $z = \sqrt{u}$, $t = 2\sqrt{v}/c$)

3D measurements



$$\tau(x', y', t) = \iiint_{\Omega} \frac{1}{r_l^2 r^2} \delta(r_l + r - tc) \cdot \rho(x, y, z) \, dx \, dy \, dz$$

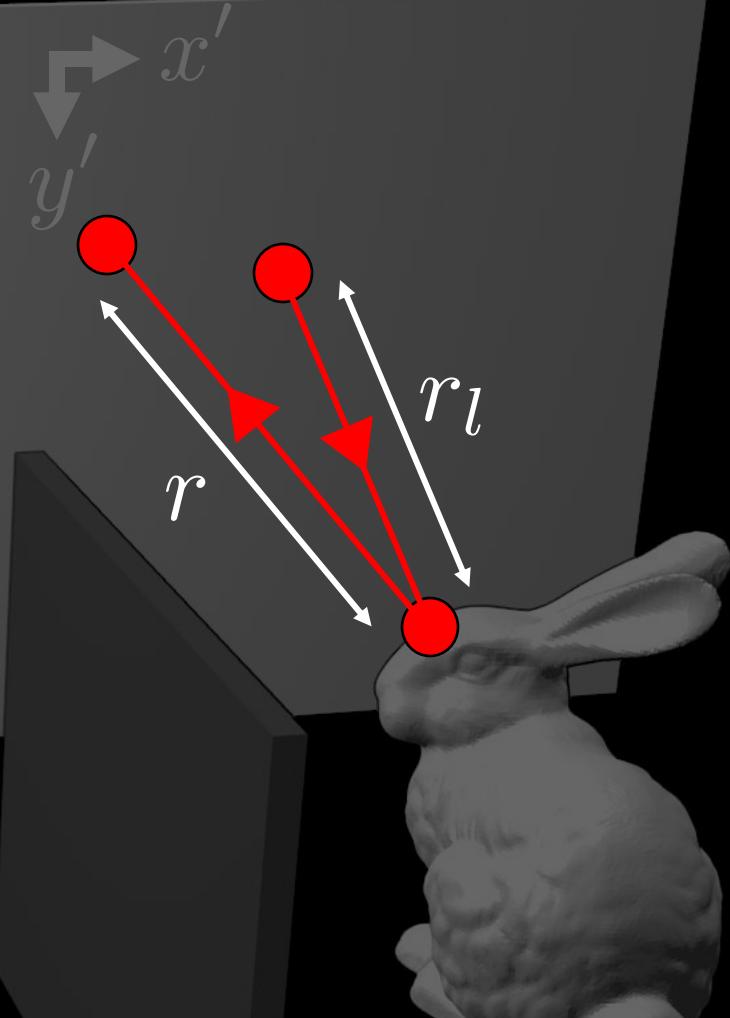


Our approach

express image formation model as a
3D convolution, by:

1. confocalizing measurements
2. performing a change of variables
(set $z = \sqrt{u}$, $t = 2\sqrt{v}/c$)

3D measurements



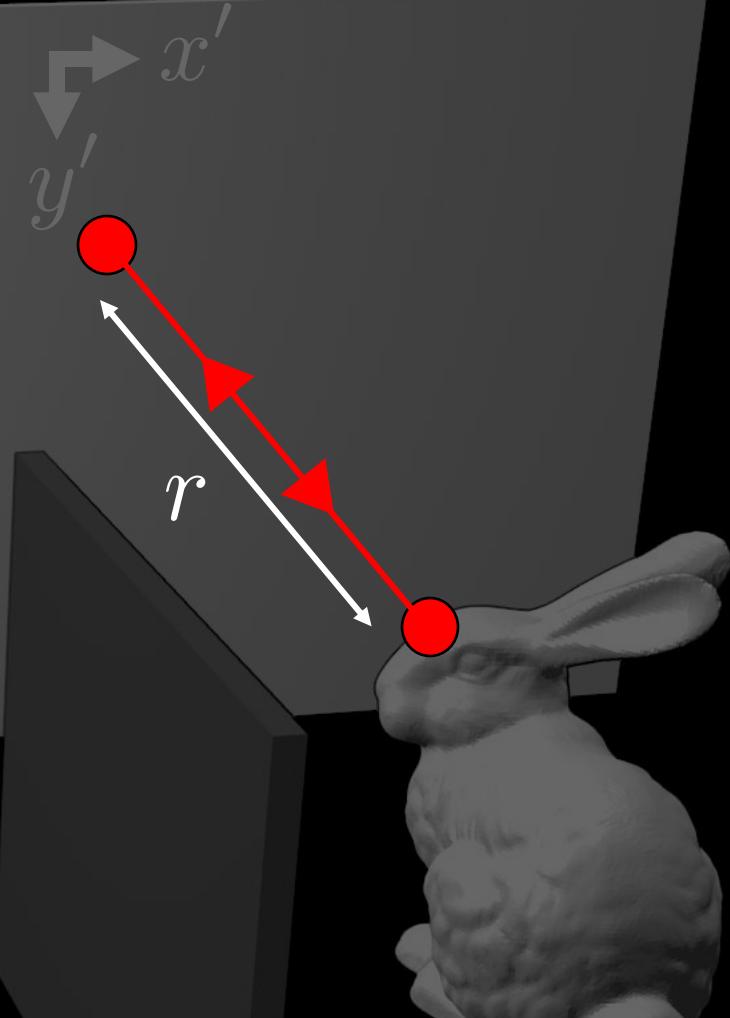
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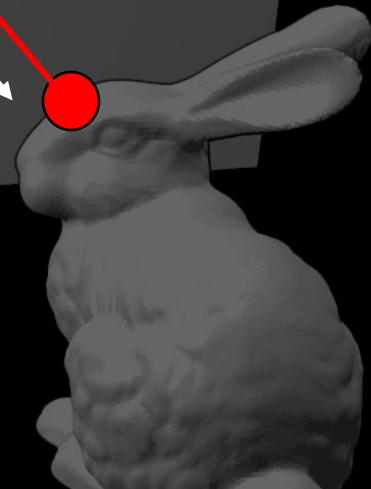
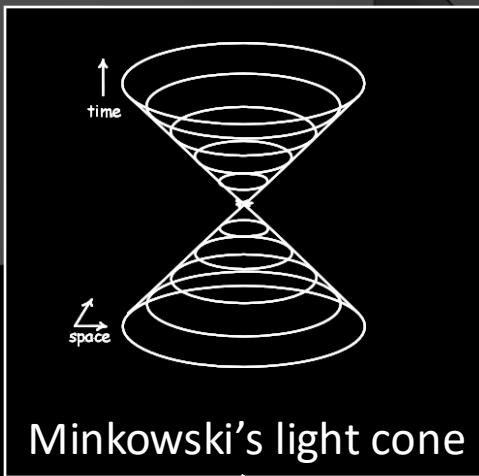
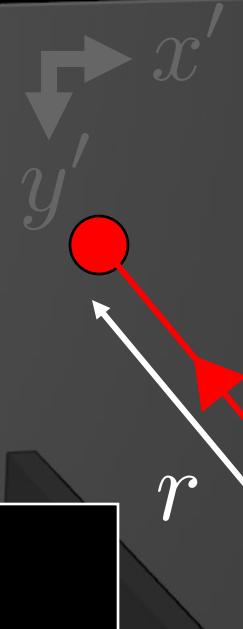
$$\tau(x', y', t) = \iiint_{\Omega} \frac{1}{r^4} \delta(2r - tc) \cdot \rho(x, y, z) \, dx \, dy \, dz$$

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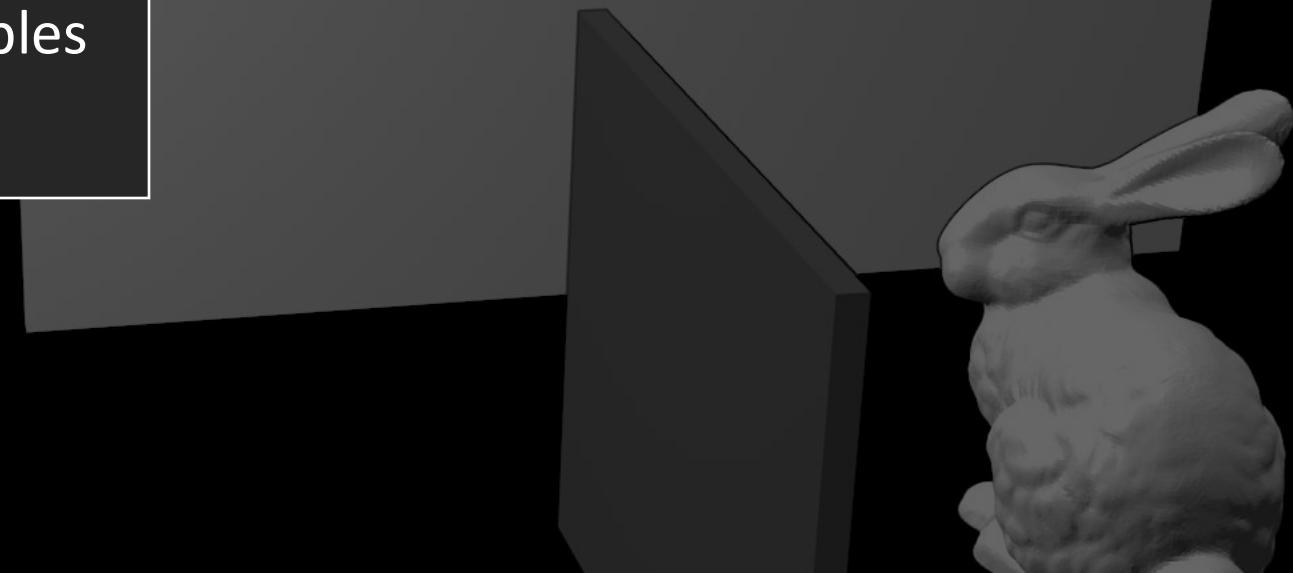
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$$v^{3/2} \tau(x', y', \frac{2}{c}\sqrt{v}) = \iiint_{\Omega} \frac{1}{2\sqrt{u}} \delta((x' - x)^2 + (y' - y)^2 + u - v) \cdot \rho(x, y, \sqrt{u}) dx dy du$$

Our approach

express image formation model as a
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τ = \mathbf{a} * ρ

NLOS image formation mode:

$$\mathcal{T} = \mathbf{A}\rho$$

↑
measurements
 $n^3 \times 1$

↑
transport matrix
 $n^3 \times n^3$

↑
unknown volume
 $n^3 \times 1$

Confocal NLOS image formation mode:

$$\mathcal{T} = \mathbf{a} * \rho$$

↑
measurements
 $n \times n \times n$

↑
blur kernel
 $n \times n \times n$

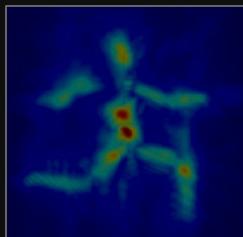
↑
unknown volume
 $n \times n \times n$

Backpropagation [Velten 12, Buttafava 15]

Flops: $O(n^5)$

Memory: $O(n^3)$

Runtime: Approx. 10 min.



Iterative Inversion [Gupta 12, Heide 13]

Flops: $O(n^5)$ per iter.

Memory: $O(n^5)$

Runtime: > 1 hour



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$$\tau = \mathbf{A} \rho$$

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↑
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↑
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 $n \times n \times n$

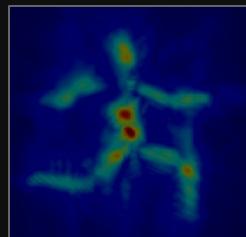
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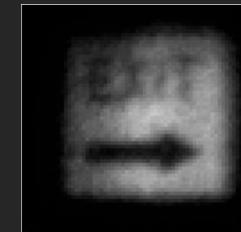


3D Deconvolution (with Light Cone Transform) [O'Toole et al. 2018]

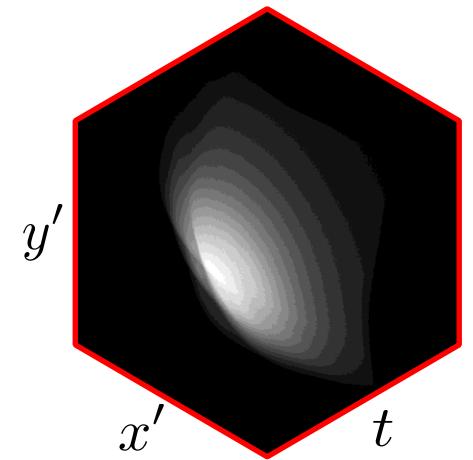
Flops: $O(n^3 \log(n))$

Memory: $O(n^3)$

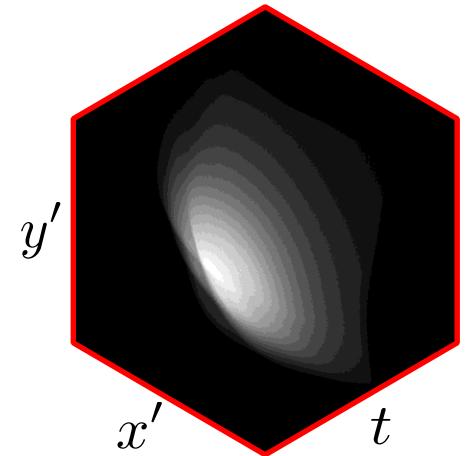
Runtime: 1/30 second



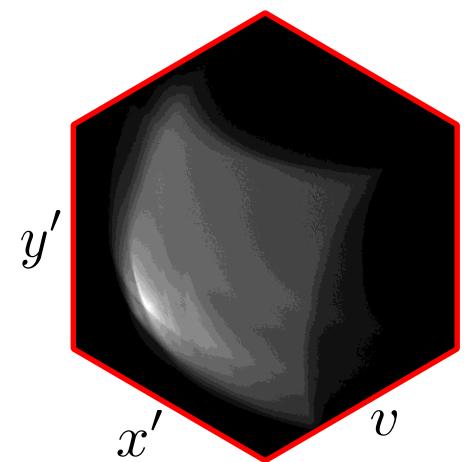
measurements



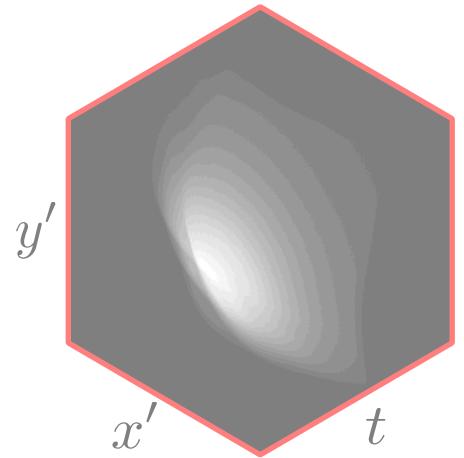
measurements



Step 1: resample
and attenuate
along t -axis



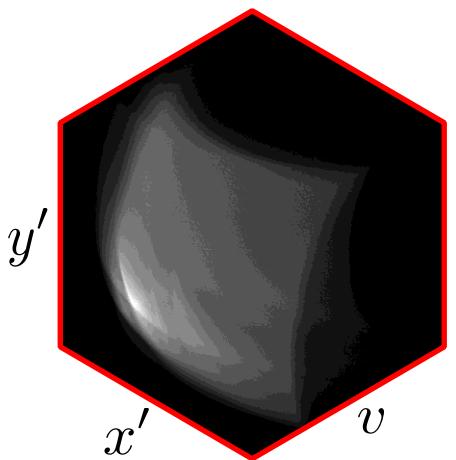
measurements



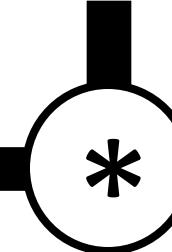
convolution kernel



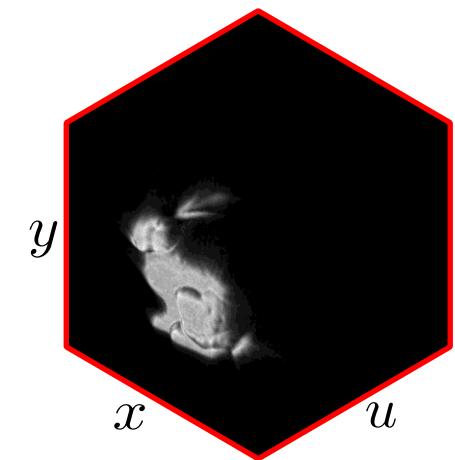
Step 1: resample
and attenuate
along t -axis



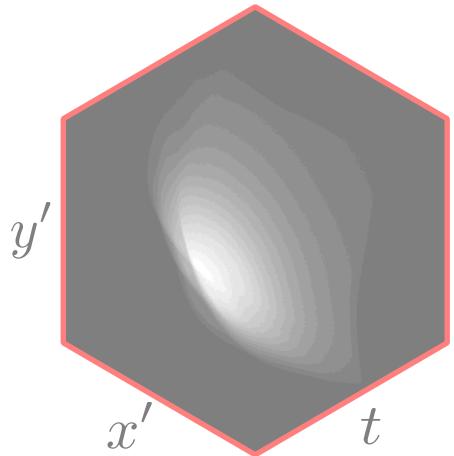
inverse filter



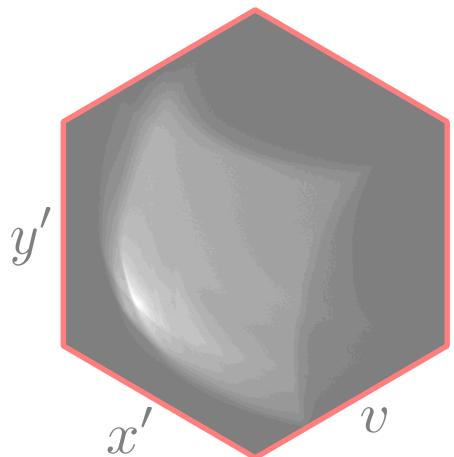
Step 2: 3D
convolution



measurements



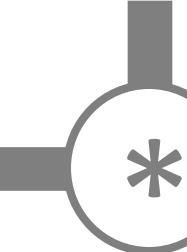
Step 1: resample
and attenuate
along t -axis



convolution kernel

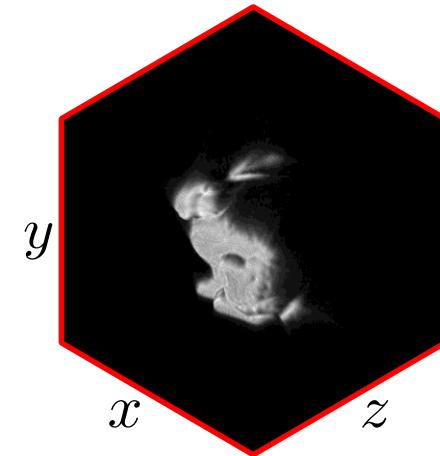


inverse filter

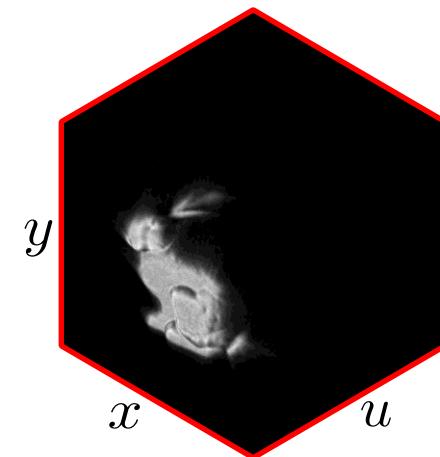


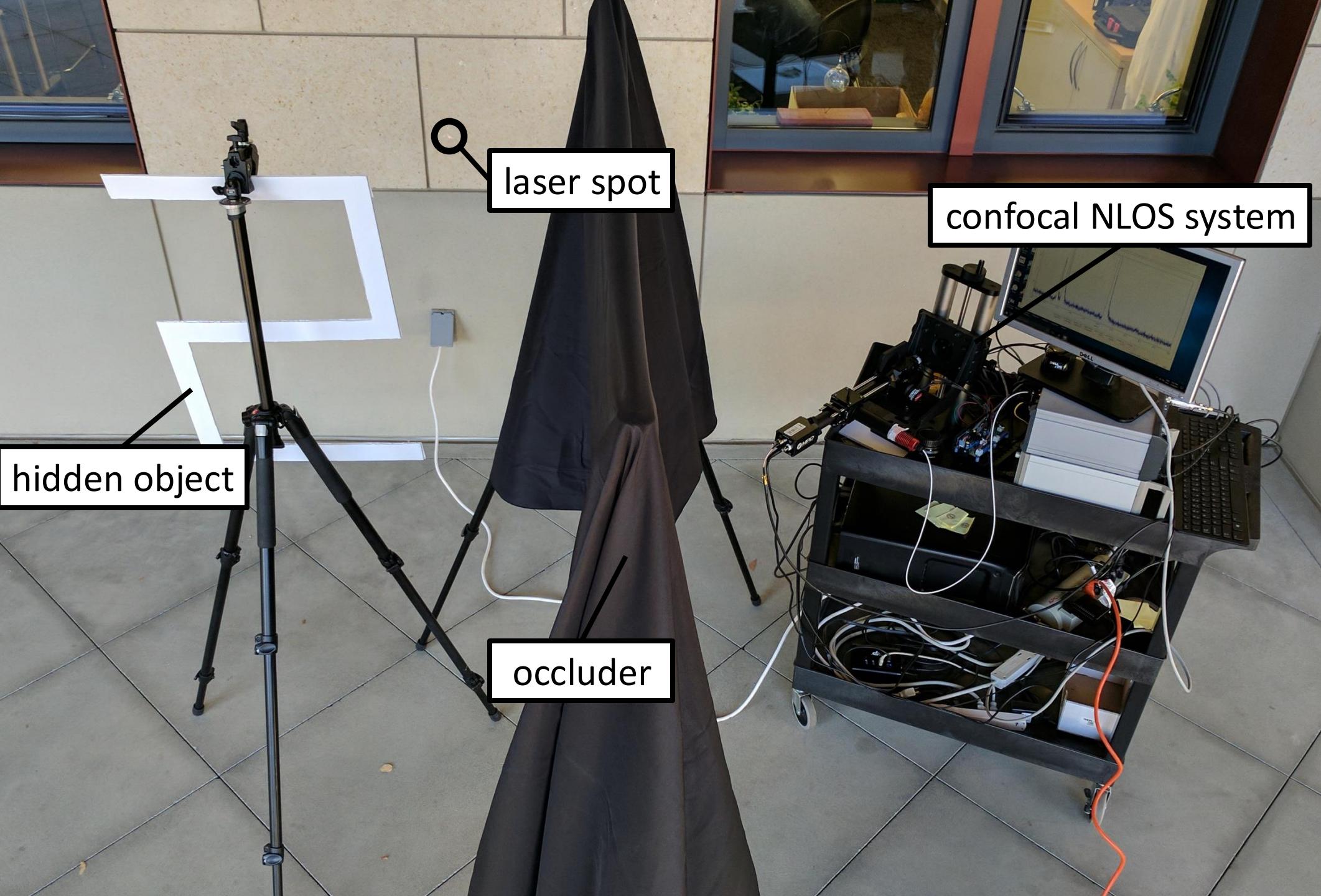
Step 2: 3D
convolution

recovered volume



Step 3: resample
and attenuate
along z -axis

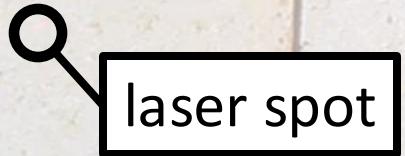




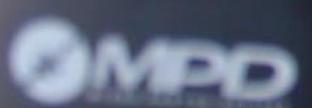
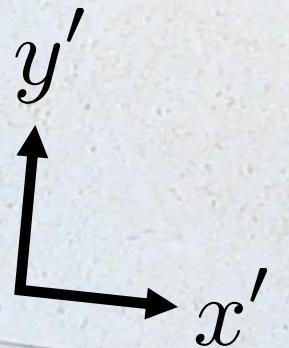


1.25 meters



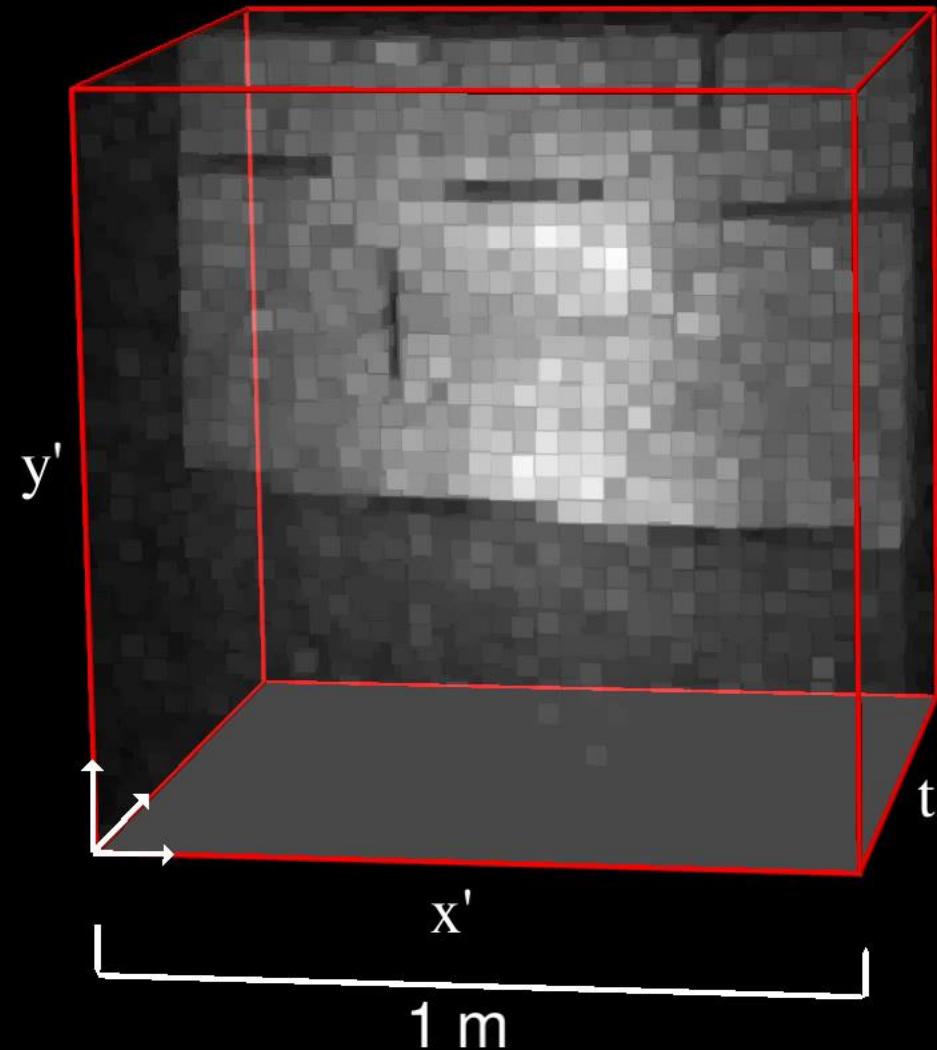


laser spot



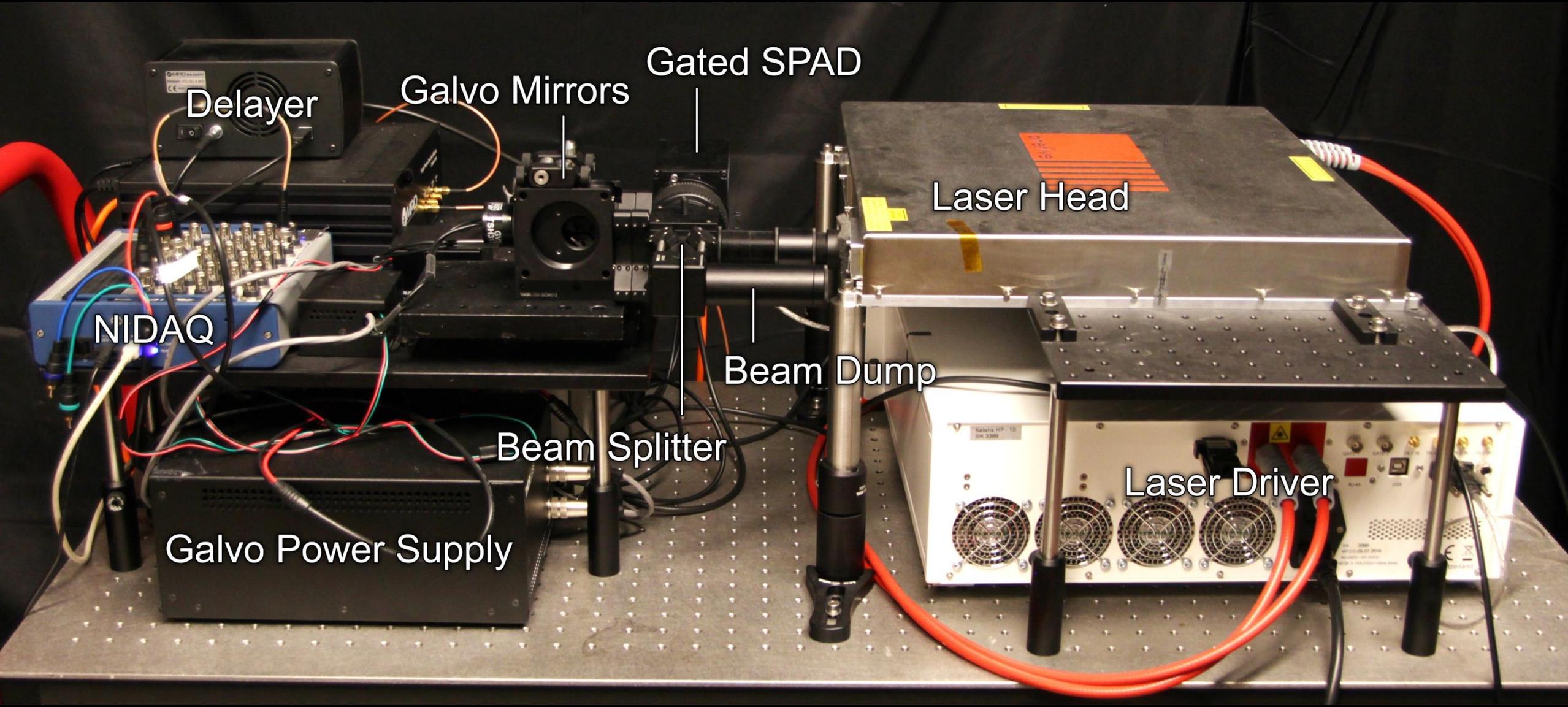
MPD

measurements

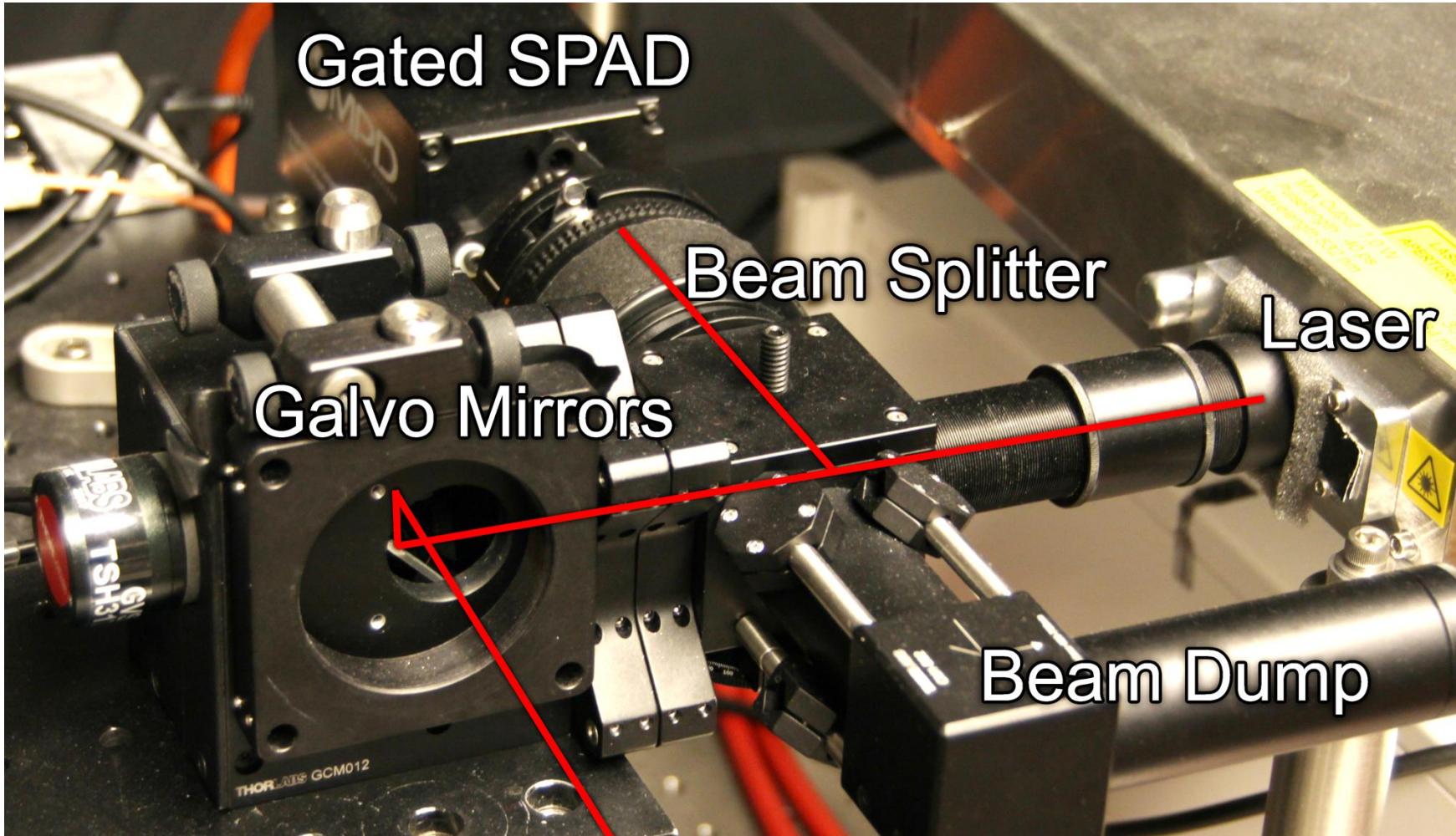


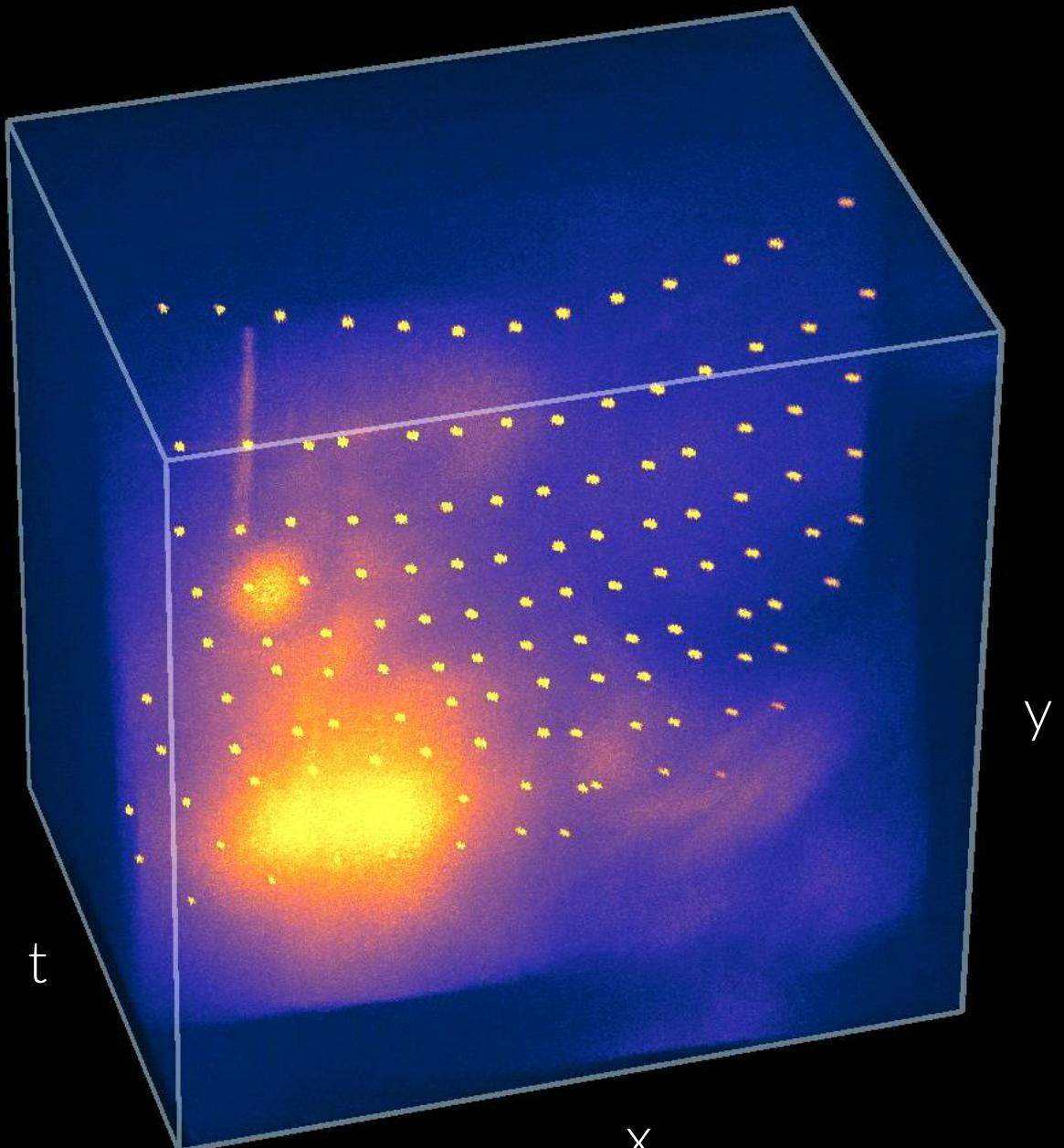
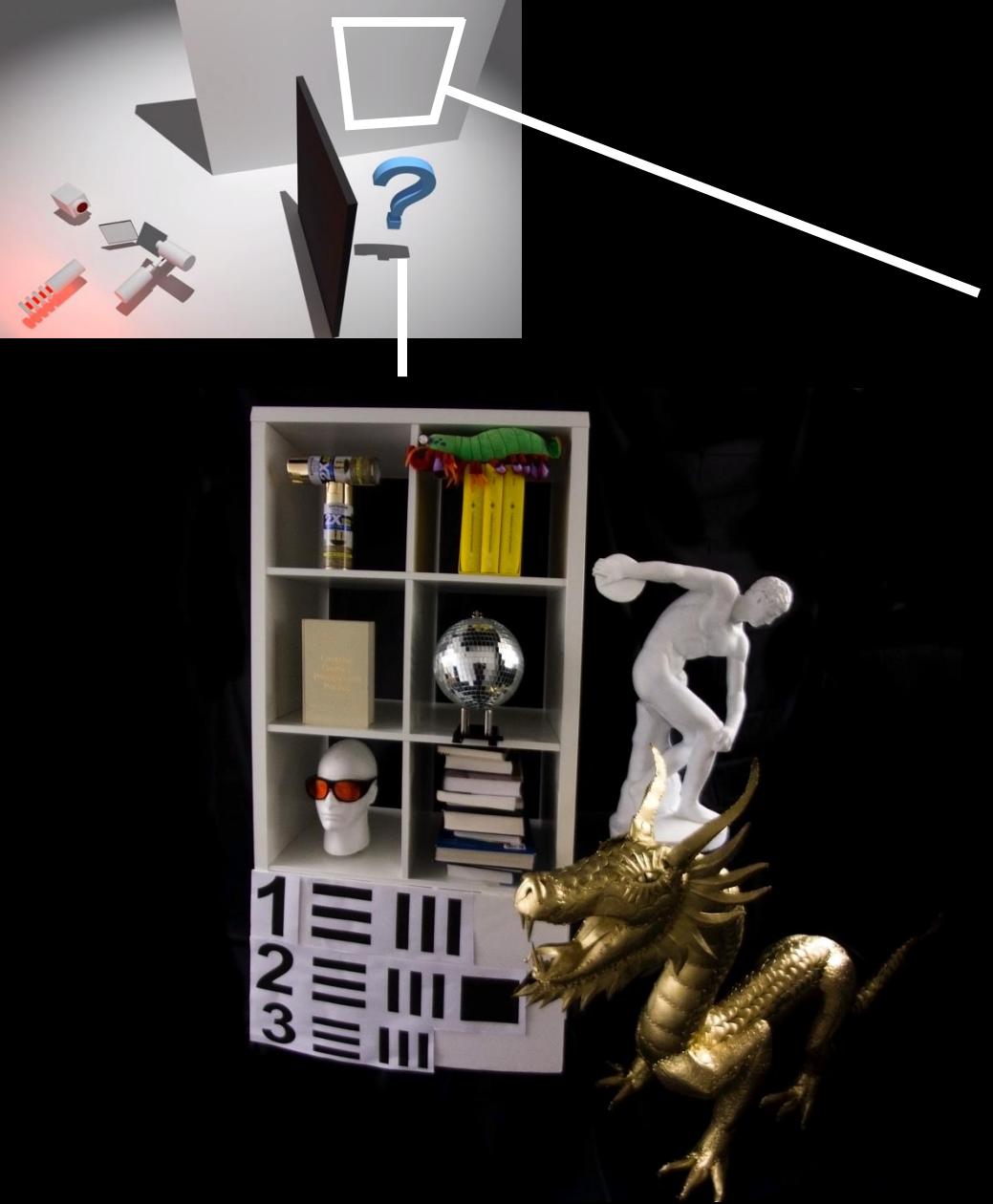
Maximum Intensity Projection

hardware prototype

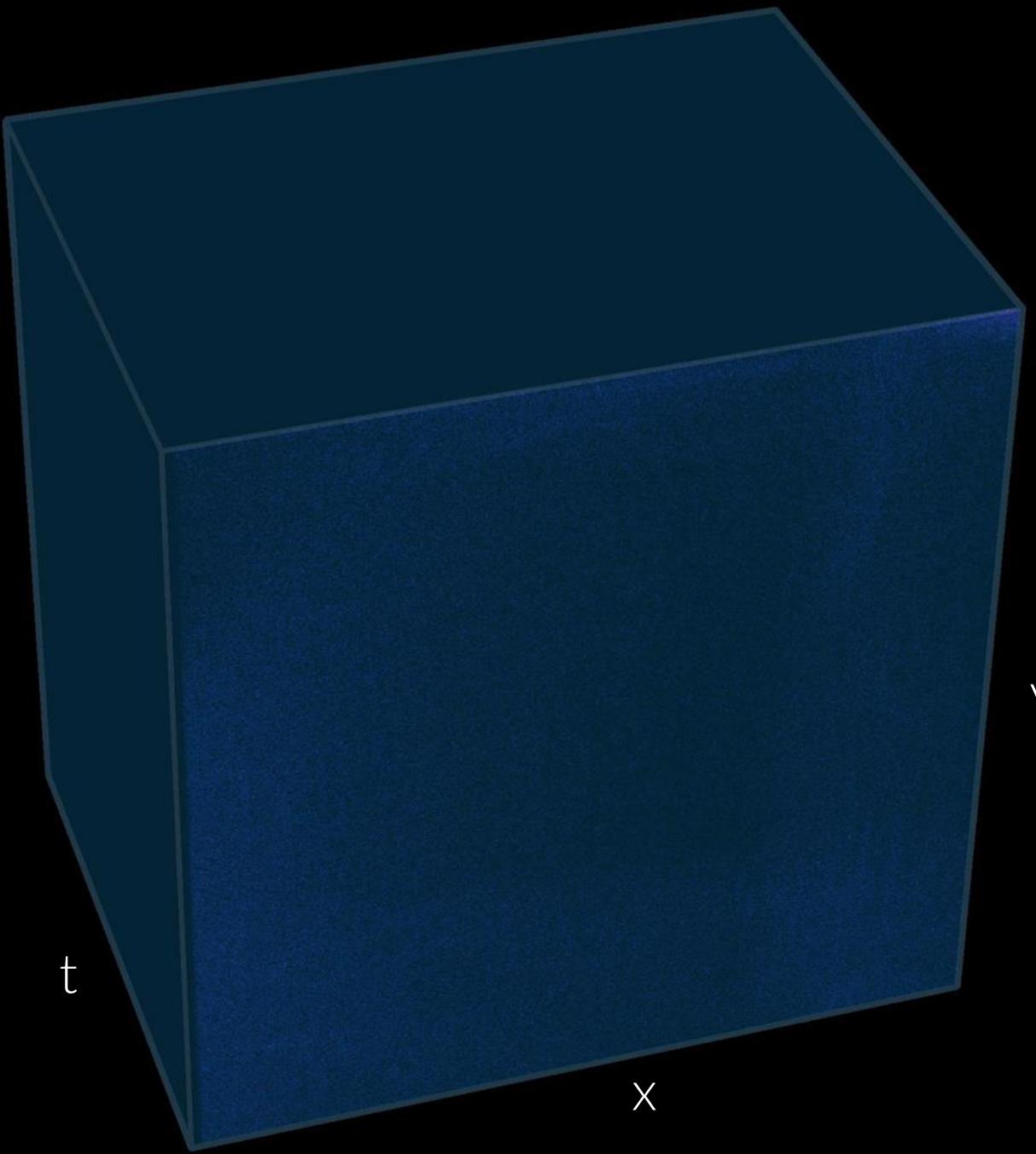


hardware prototype





Captured Measurements

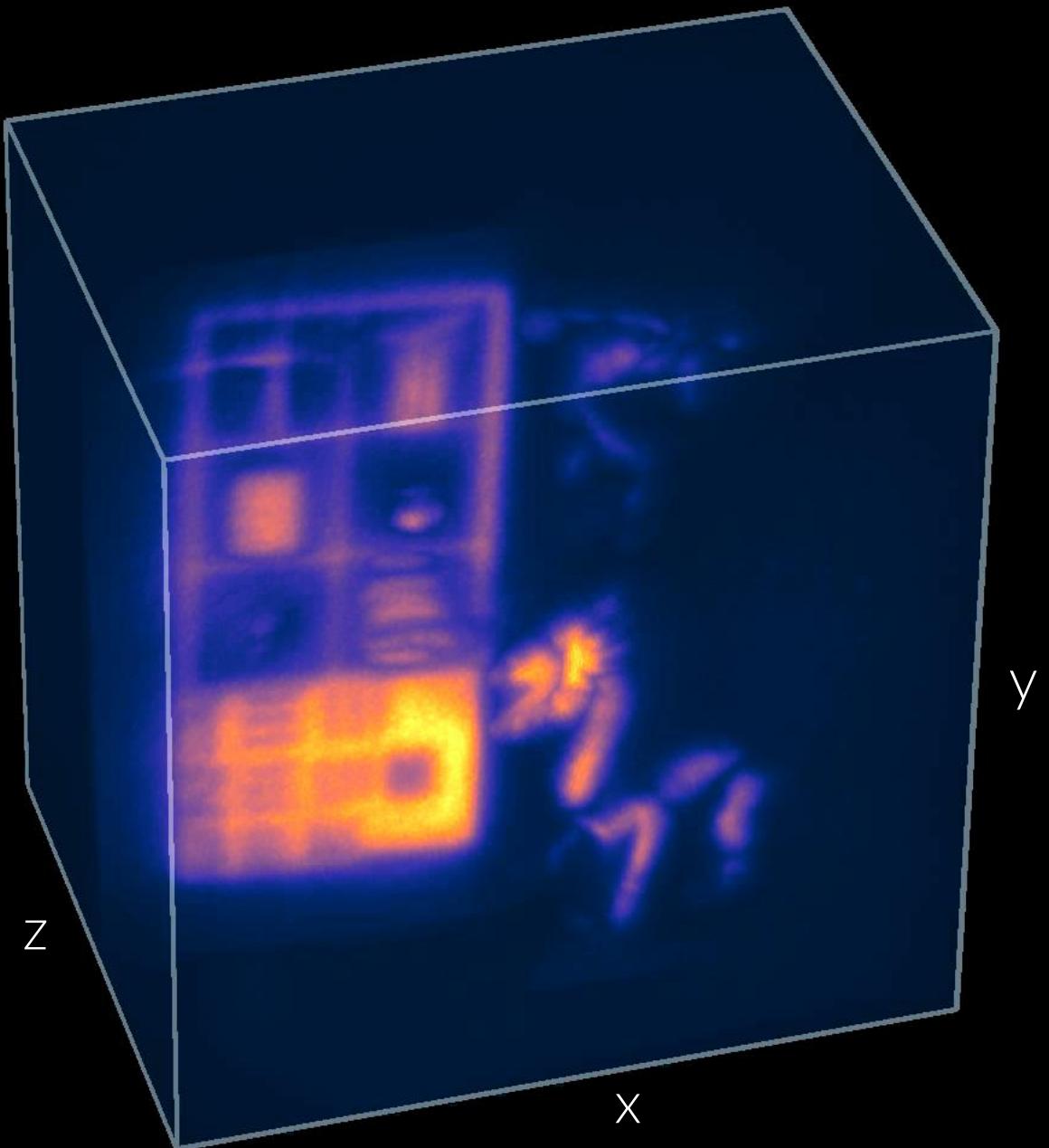




Dimensions: 2 x 2 m

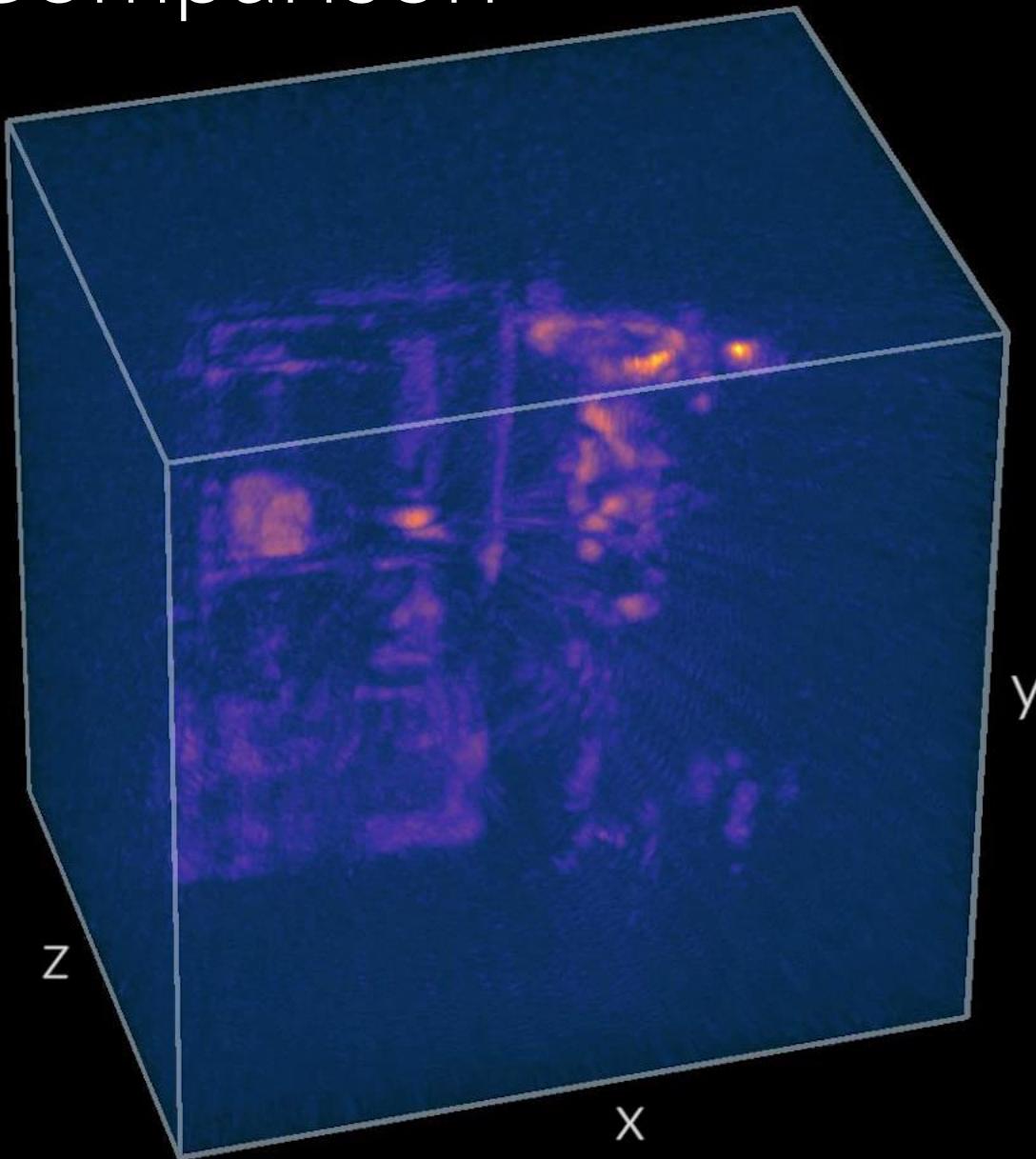
Exposure: 180 min

Time Resolution: 32 ps



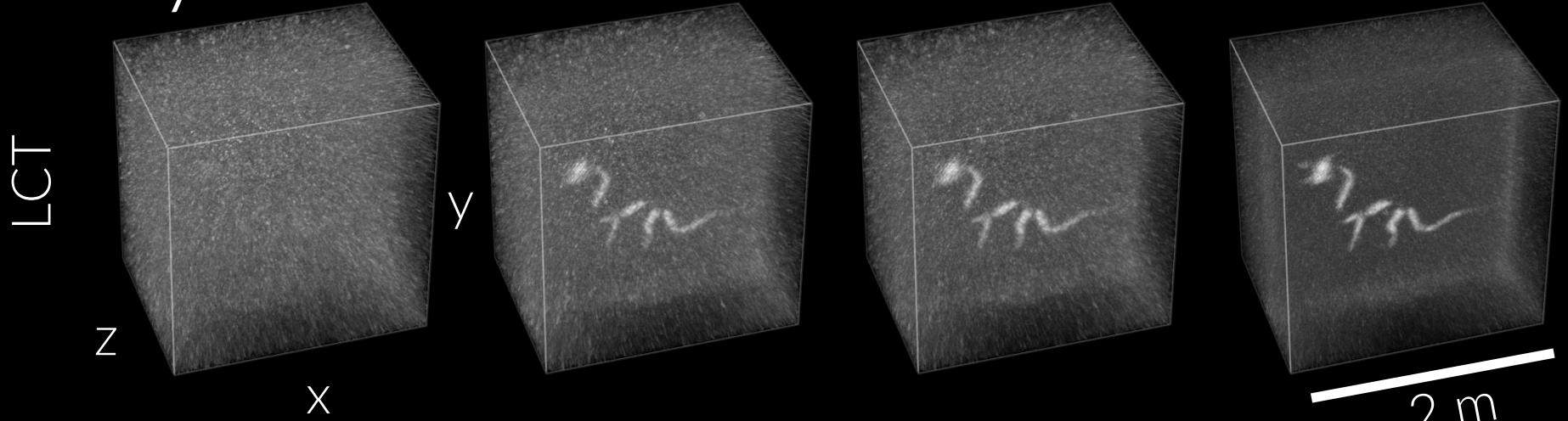
Reconstruction Comparison

dimensions: 2 m x 2 m x 1.5 m

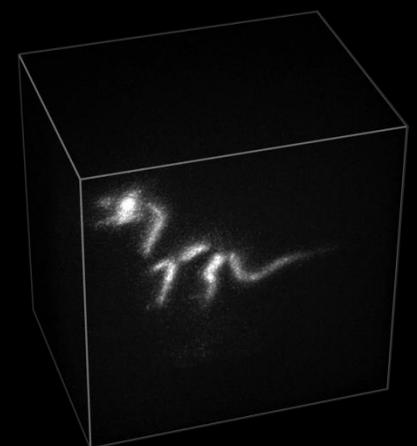
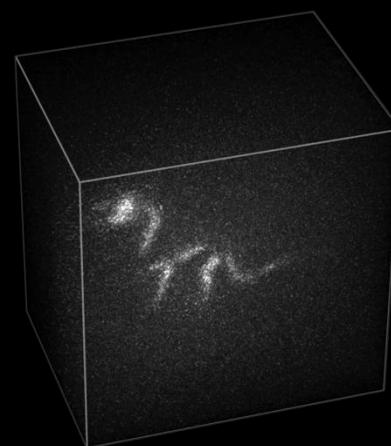
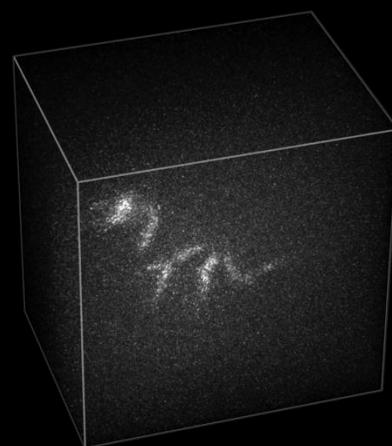
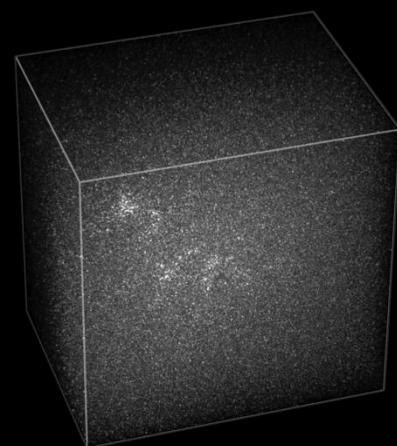


Filtered
Backprojection

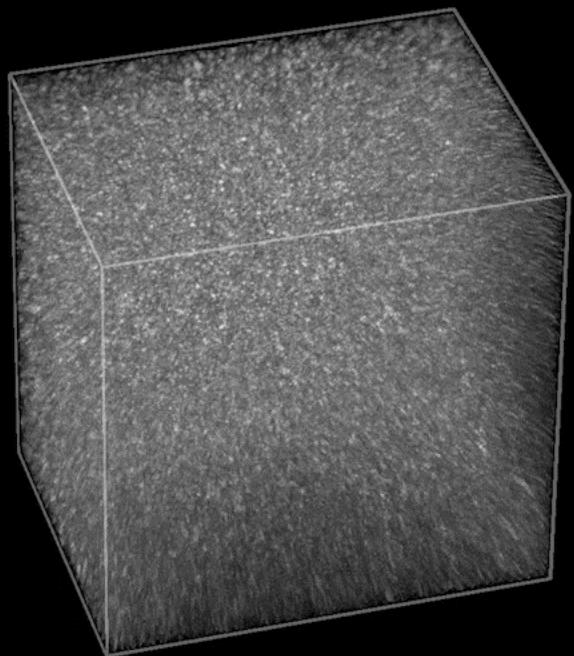
noise sensitivity



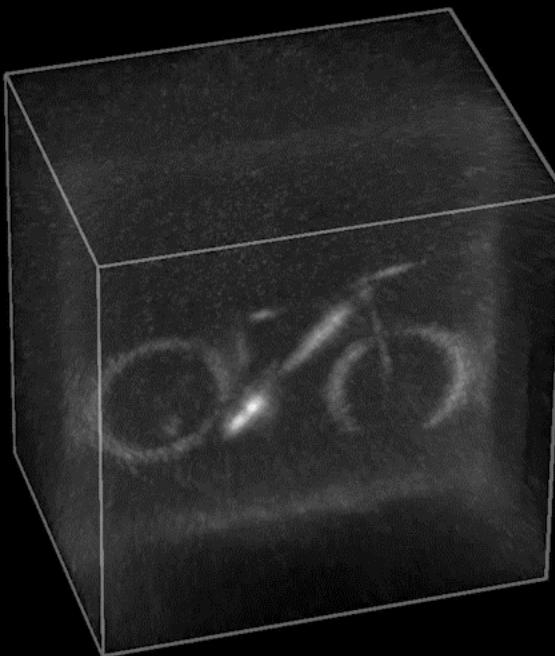
$f-k$
Migration



noise comparison



Filtered Backprojection

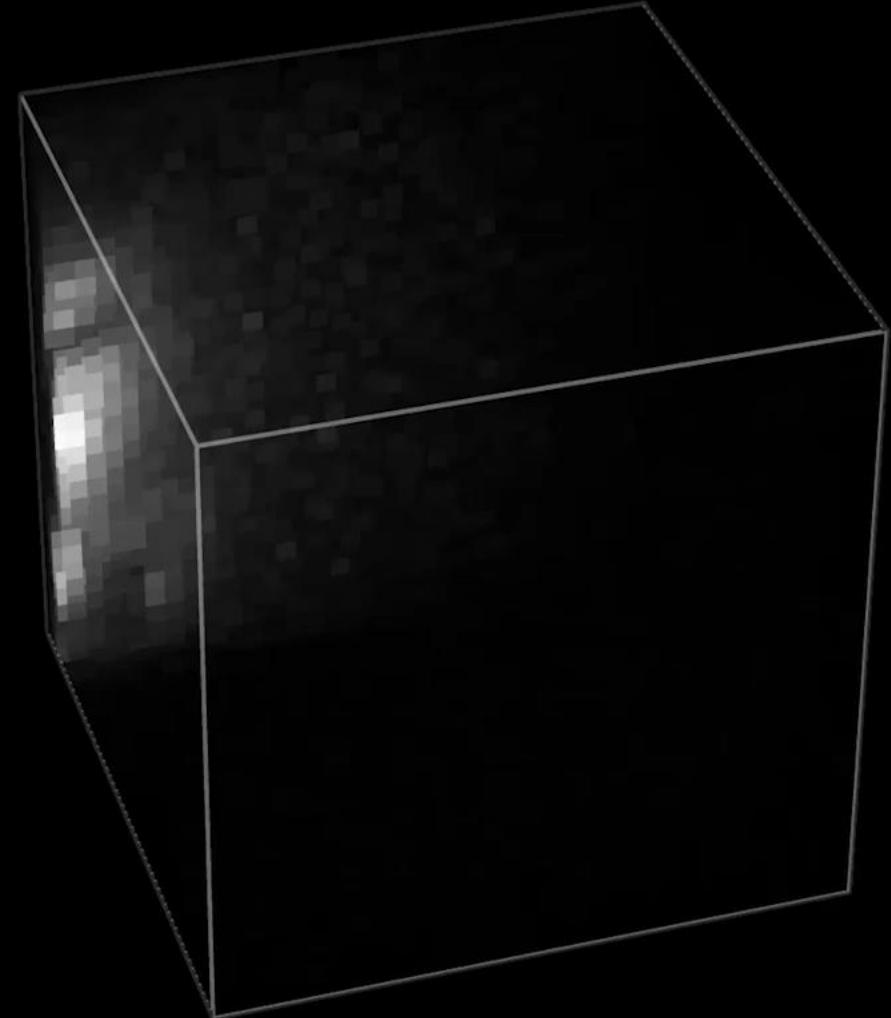


LCT



$f\text{-}k$ Migration
10 min. exposure

real-time scanning

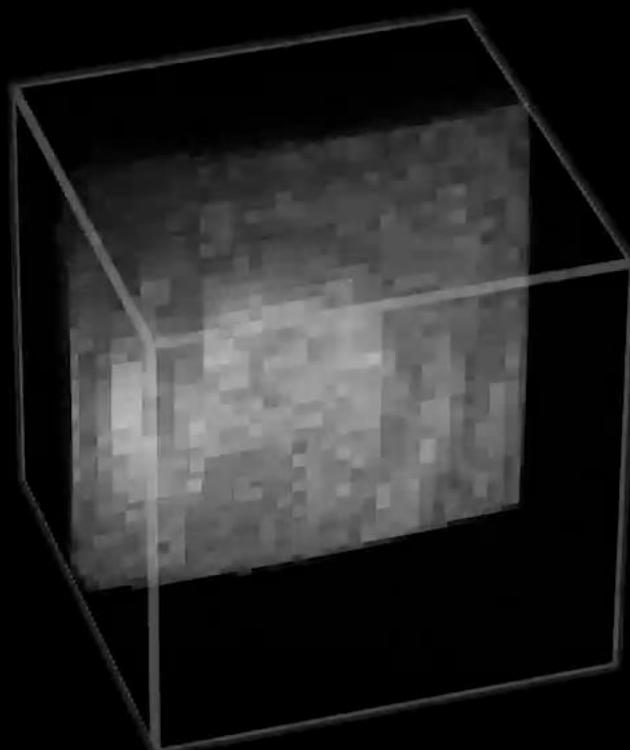


Framerate: 4 Hz

Resolution: 32 x 32

Dimensions: 2 m x 2 m x 2 m

Transient Image (Input)



3D Human Pose (Output)



(Reference Only)
Person Hidden by Wall

