16-833 JEAN HW4 Dense SLAM with Point-based Fusion

2 Iterative Clarest Point (ICP)

2.2 Cinearitation

Given:
$$\begin{cases}
1 & -r & B \\
8R = r & 1 & -\alpha
\end{cases}$$

$$\begin{cases}
SR = r & 1 & -\alpha \\
-B & \alpha & 1
\end{cases}$$

$$\begin{cases}
Ai & \text{is } 6x1
\end{cases}$$
Find:
$$\begin{cases}
R_{i}(x, B, r, t_{x}, t_{y}, t_{z}) = Ai \\
t_{x} & t_{y} & t_{z}
\end{cases}$$

$$\begin{cases}
Ai & \text{is } 6x1
\end{cases}$$

$$t_{x} & t_{y} & t_{z}
\end{cases}$$

$$\begin{cases}
Ai & \text{is } s \text{ calar}
\end{cases}$$

Solution:

$$\begin{split} R_{i}(\delta R, \delta t) &= N_{q_{i}}^{T}((\delta R)R_{i}^{2} + \delta t - q_{i}) \\ &\rightarrow R_{i}(\delta R, \delta t) = N_{q_{i}}^{T}((\delta R)R_{i}^{2} + \delta t - q_{i}) \\ &\rightarrow R_{i}(\delta R, \delta t) = N_{q_{i}}^{T}((\delta R)R_{i}^{2} + \delta t - q_{i}) \\ &\rightarrow R_{i}^{T}(\delta R, \delta t) = [N_{q_{i}} N_{q_{2}} N_{q_{3}}] \\ &\rightarrow R_{i}^{T}(\delta R, \delta t) = [N_{q_{i}} N_{q_{2}} N_{q_{3}}] \\ &\rightarrow R_{i}^{T}(\delta R, \delta t) = [N_{q_{i}} N_{q_{2}} N_{q_{3}}] \\ &\rightarrow R_{i}^{T}(\delta R, \delta t) = [N_{q_{i}} N_{q_{2}} N_{q_{3}}] \\ &\rightarrow R_{i}^{T}(\delta R, \delta t) = [N_{q_{i}} N_{q_{2}} N_{q_{3}}] \\ &\rightarrow R_{i}^{T}(\delta R, \delta t) = [N_{q_{i}} N_{q_{2}} N_{q_{3}}] \\ &\rightarrow R_{i}^{T}(\delta R, \delta t) = [N_{q_{i}} N_{q_{2}} N_{q_{3}}] \\ &\rightarrow R_{i}^{T}(\delta R, \delta t) = [N_{q_{i}} N_{q_{2}} N_{q_{3}}] \\ &\rightarrow R_{i}^{T}(\delta R, \delta t) = [N_{q_{i}} N_{q_{2}} N_{q_{3}}] \\ &\rightarrow R_{i}^{T}(\delta R, \delta t) = [N_{q_{i}} N_{q_{2}} N_{q_{3}}] \\ &\rightarrow R_{i}^{T}(\delta R, \delta t) = [N_{q_{i}} N_{q_{2}} N_{q_{3}}] \\ &\rightarrow R_{i}^{T}(\delta R, \delta t) = [N_{q_{i}} N_{q_{2}} N_{q_{3}}] \\ &\rightarrow R_{i}^{T}(\delta R, \delta t) = [N_{q_{i}} N_{q_{2}} N_{q_{3}}] \\ &\rightarrow R_{i}^{T}(\delta R, \delta t) = [N_{q_{i}} N_{q_{2}} N_{q_{3}}] \\ &\rightarrow R_{i}^{T}(\delta R, \delta t) = [N_{q_{i}} N_{q_{2}} N_{q_{3}}] \\ &\rightarrow R_{i}^{T}(\delta R, \delta t) = [N_{q_{i}} N_{q_{2}} N_{q_{3}}] \\ &\rightarrow R_{i}^{T}(\delta R, \delta t) = [N_{q_{i}} N_{q_{2}} N_{q_{3}}] \\ &\rightarrow R_{i}^{T}(\delta R, \delta t) = [N_{q_{i}} N_{q_{2}} N_{q_{3}}] \\ &\rightarrow R_{i}^{T}(\delta R, \delta t) = [N_{q_{i}} N_{q_{2}} N_{q_{3}}] \\ &\rightarrow R_{i}^{T}(\delta R, \delta t) = [N_{q_{i}} N_{q_{2}} N_{q_{3}}] \\ &\rightarrow R_{i}^{T}(\delta R, \delta t) = [N_{q_{i}} N_{q_{2}} N_{q_{3}}] \\ &\rightarrow R_{i}^{T}(\delta R, \delta t) = [N_{q_{i}} N_{q_{3}} N_{q_{3}}] \\ &\rightarrow R_{i}^{T}(\delta R, \delta t) = [N_{q_{i}} N_{q_{3}} N_{q_{3}}] \\ &\rightarrow R_{i}^{T}(\delta R, \delta t) = [N_{q_{i}} N_{q_{3}} N_{q_{3}}] \\ &\rightarrow R_{i}^{T}(\delta R, \delta t) = [N_{q_{i}} N_{q_{3}} N_{q_{3}}] \\ &\rightarrow R_{i}^{T}(\delta R, \delta t) = [N_{q_{i}} N_{q_{3}} N_{q_{3}}] \\ &\rightarrow R_{i}^{T}(\delta R, \delta t) = [N_{q_{i}} N_{q_{3}} N_{q_{3}}] \\ &\rightarrow R_{i}^{T}(\delta R, \delta t) = [N_{q_{i}} N_{q_{3}} N_{q_{3}}] \\ &\rightarrow R_{i}^{T}(\delta R, \delta t) = [N_{q_{i}} N_{q_{3}} N_{q_{3}}] \\ &\rightarrow R_{i}^{T}(\delta R, \delta t) = [N_{q_{i}} N_{q_{3}} N_{q_{3}}] \\ &\rightarrow R_{i}^{T}(\delta R, \delta t) = [N_{q_{i}} N_{q_{3}} N_{q_{3}}] \\ &\rightarrow R_{i}^{T}($$

2.3 Optimization

Given:

$$\sum_{i=1}^{\infty} |\hat{x}^{i}(x, \beta, \tau, t_{x}, t_{y}, t_{z}) = \sum_{i=1}^{\infty} ||A_{i}||^{2} + b_{i}||^{2}$$

Find: Write down the linear system that provides a closed form solution. Solution:

3 Point-based Fusion

3.2 Merge

Given: PER3, W, QER3, W=1

Find: the weight average of the positions in terms of p,q, R_c^w , t_c^w , w the weight average of normals in terms of np, nq, R_c^w , w

Equation: $W = \frac{\sum_{i=1}^{n} W_i \chi_i}{\sum_{i=1}^{n} W_i}$

Solutions: Wi= (W+1)

Wpasitions = W(p)+1[RW(q)+ti] #

Wnomals = W(np) + 1[Rcu(nq)] #

3.4 Results

Given: Width = 680, height = 480, # of total points = 1,363,469

Find: the compression ratio

Equation: CR = # of total points (H/2·W/2·zoo)

Solution:

CR = 1,363,469 2 0.08355 or 8.355% #