## M9-L1 Problem 1

Here, you will implement three loss functions from scratch in numpy: MAE, MSE, and MAPE.

```
import numpy as np
y gt1 = np.array([1,2,3,4,5,6,7,8,9,10])
y pred1 = np.array([1,1.3,3.1,4.6,5.9,5.9,6.4,9.2,8.1,10.5])
y gt2 = np.array([-3.23594765, -3.74125693, -2.3040903, 0.
0.30190142, -1.68434859, 1.10160357, 0.8587438, 1.76546802,
3.13787123, 3.72990216, 5.89871795, 6.06406803, 6.28329118,
7.46406525, 8.21246221, 10.23145281,
                                      9.39080133, 10.76761316,
10.45903557, 9.61872736, 13.68392163, 14.75332509, 14.00530973,
17.87581523, 15.01028079, 17.36899084, 17.99463433, 20.57318325,
21.36834867, 20.91252318, 21.99432414, 21.58696173, 21.35253687,
23.84400704, 25.20685402, 27.13938159, 27.97005662, 27.23893581,
28.18254573, 28.29488138, 28.78200226, 29.35433587, 33.86996731,
32.2681256, 33.19828933, 33.24215413, 36.13102571, 34.59822336,
36.85796679, 37.03382637, 39.17478129, 39.13565951, 39.32441832,
41.33545414, 42.65055409, 43.1473253 , 44.24186584, 44.1636577 ,
45.29382449, 45.84269107, 47.01418421, 47.41917695, 47.36462649,
50.12692109, 50.40629987, 50.03646832, 52.98803478, 52.47654002,
54.29436964, 55.83010066, 56.08857887, 57.9575825 , 56.44194186,
58.93769518, 58.7091293 , 59.3817281 , 60.53226145, 61.65814444,
62.88444817, 62.52171885, 65.44628103, 65.86970284, 64.72638258,
68.60946432, 69.87568716, 70.01716341, 69.51704486, 69.48480293,
72.46859314, 71.86955033, 74.3537582 , 74.19817397, 75.82512388,
76.0634371 , 77.27222973 , 77.43474244 , 80.06869878 , 79.26832623 ,
80.40198936])
y \text{ pred2} = \text{np.array}([-3.17886560e+00, -3.72628642e+00, -2.28154027e+00,
-2.42424242e-06, 2.96261368e-01, -1.70080838e+00,
                                                    1.09113641e+00,
8.60043722e-01, 1.76729042e+00,
                                  3.12498677e+00,
                                                   3.72452933e+00,
5.81293300e+00, 6.01791742e+00,
                                 6.27564586e+00,
                                                   7.43093457e+00,
8.18505900e+00, 1.00785853e+01,
                                  9.41006754e+00,
                                                   1.07339029e+01,
1.05483666e+01, 9.86429504e+00,
                                 1.35944803e+01,
                                                   1.46257911e+01,
1.41092530e+01, 1.74700758e+01,
                                 1.52285866e+01,
                                                   1.73610430e+01,
1.80283176e+01, 2.02578402e+01,
                                  2.10543695e+01,
                                                   2.08801196e+01,
2.19111495e+01, 2.17786086e+01,
                                                   2.39269636e+01,
                                 2.17754891e+01,
2.51674432e+01, 2.68054871e+01,
                                  2.76337491e+01,
                                                   2.73444399e+01,
2.82677426e+01, 2.85915692e+01,
                                 2.91907133e+01,
                                                   2.98552019e+01.
3.32092384e+01, 3.24325813e+01,
                                  3.33437229e+01,
                                                   3.36586115e+01,
3.58501097e+01, 3.51566050e+01,
                                 3.69363787e+01,
                                                   3.73654528e+01,
3.90232127e+01, 3.93355670e+01,
                                 3.97886962e+01.
                                                   4.13471034e+01.
4.24678677e+01, 4.31186248e+01,
                                 4.41080463e+01,
                                                   4.44437982e+01,
4.54581242e+01, 4.61509657e+01,
                                 4.71832256e+01,
                                                   4.78047650e+01,
4.81822755e+01, 5.00379827e+01,
                                 5.06088232e+01,
                                                   5.08521636e+01,
```

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5.27428151e+01, 5.29526597e+01, 5.42661662e+01, 5.54230479e+01, 5.60162341e+01, 5.72972123e+01, 5.71389028e+01, 5.87005639e+01, 5.91111760e+01, 5.98988234e+01, 6.08826528e+01, 6.18502423e+01, 6.28491288e+01, 6.32501917e+01, 6.48567227e+01, 6.55629719e+01, 6.57207391e+01, 6.75883810e+01, 6.85509197e+01, 6.91918142e+01, 6.96421235e+01, 7.02288144e+01, 7.17044458e+01, 7.21593122e+01, 7.34448231e+01, 7.40436375e+01, 7.50845851e+01, 7.57923722e+01, 7.67262442e+01, 7.74266118e+01, 7.86387737e+01, 7.91677250e+01, 8.00787815e+01])
```

## Mean Absolute Error

Complete the definition for MAE(y gt, y pred) below.

MAE = 
$$\frac{1}{n} \sum_{i=1}^{n} |y_i - \hat{y}_i| = \frac{1}{n} \sum_{i=1}^{n} |e_i|$$

MAE(y\_gt1, y\_pred1) should return 0.560.

```
def MAE(y_gt, y_pred):
    # YOUR CODE GOES HERE
    return np.mean(np.abs(y_gt - y_pred))

print(f"MAE(y_gt1, y_pred1) = {MAE(y_gt1, y_pred1):.3f}")
print(f"MAE(y_gt2, y_pred2) = {MAE(y_gt2, y_pred2):.3f}")

MAE(y_gt1, y_pred1) = 0.560
MAE(y_gt2, y_pred2) = 0.290
```

## Mean Squared Error

Complete the definition for MSE(y\_gt, y\_pred) below.

MSE = 
$$\frac{1}{n} \sum_{i=1}^{n} (y_i - \hat{y}_i)^2 = \frac{1}{n} \sum_{i=1}^{n} (e_i)^2 = \frac{1}{n} e^T e^T$$

MSE(y gt1, y pred1) should return 0.454.

```
def MSE(y_gt, y_pred):
    # YOUR CODE GOES HERE
    return np.mean((y_gt - y_pred)**2)

print(f"MSE(y_gt1, y_pred1) = {MSE(y_gt1, y_pred1):.3f}")
print(f"MSE(y_gt2, y_pred2) = {MSE(y_gt2, y_pred2):.3f}")

MSE(y_gt1, y_pred1) = 0.454
MSE(y_gt2, y_pred2) = 0.174
```

## Mean Absolute Percentage Error

Complete the definition for MAPE(y\_gt, y\_pred, epsilon) below.

$$MAE = \frac{1}{n} \sum_{i=1}^{n} \frac{|y_i - \hat{y}_i|}{|y_i| + \varepsilon} = \frac{1}{n} \sum_{i=1}^{n} \frac{|e_i|}{|y_i| + \varepsilon}$$

MAPE(y gt1, y pred1, 1e-6) should return 0.112.

```
def MAPE(y_gt, y_pred, epsilon=1e-6):
    # YOUR CODE GOES HERE
    return np.mean(np.abs((y_gt - y_pred) / (y_gt + epsilon)))

print(f"MAPE(y_gt1, y_pred1) = {MAPE(y_gt1, y_pred1):.3f}")

print(f"MAPE(y_gt2, y_pred2) = {MAPE(y_gt2, y_pred2):.3f}")

MAPE(y_gt1, y_pred1) = 0.112
MAPE(y_gt2, y_pred2) = 0.032
```