

m1-hw1

January 27, 2024

1 Problem 1 (30 points)

1.1 Problem Description

In this problem you will implement gradient descent on the following function: $f(x) = x^2 + 3x + 6\sin(x)$. You will define your own gradient function `fgrad(x)`, and then using the provided learning rate $\eta = 0.15$ and initial guess $x_0 = 8$, you will print the value of x and $f(x)$ for the first 10 iterations.

Fill out the notebook as instructed, making the requested plots and printing necessary values.

Summary of deliverables: Functions: - `fgrad(x)`

Results: - Printed values of x and $f(x)$ for the first 10 iterations of gradient descent

Discussion: - Do your printed values appear to be converging towards the minimum of the function?

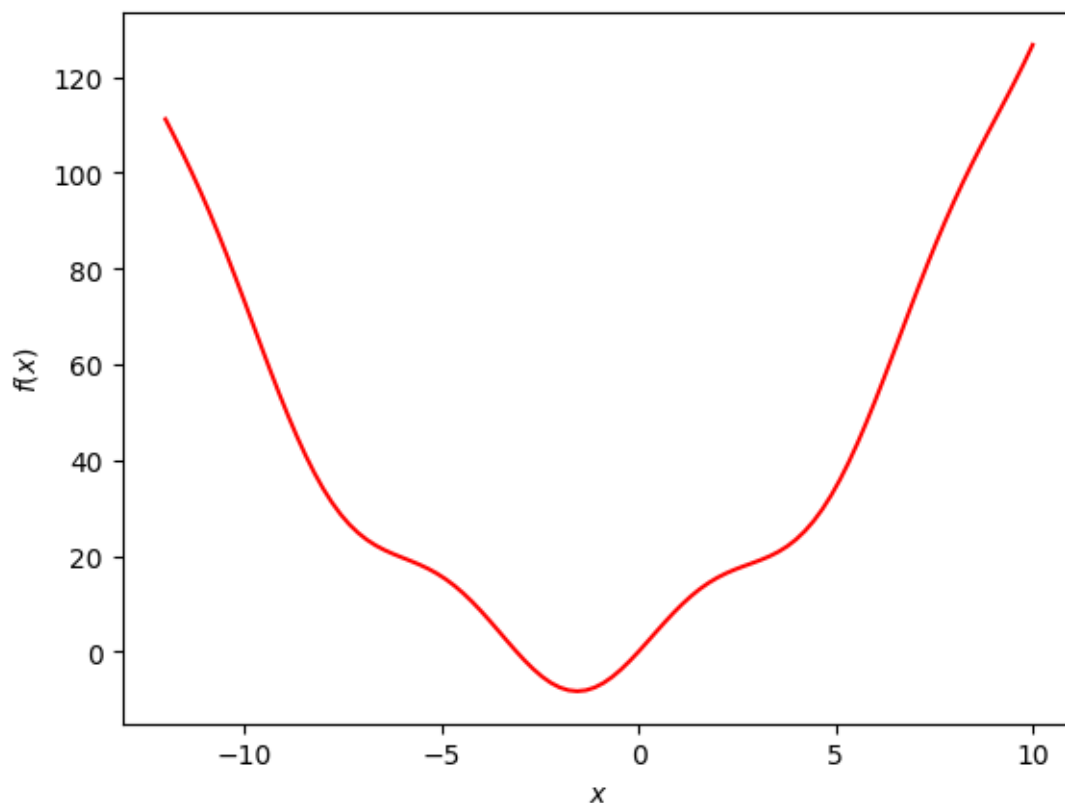
Imports and provided functions:

```
[36]: import numpy as np
import matplotlib.pyplot as plt

def f(x):
    return x**2 + 3*x + 6*np.sin(x)

def plotfx():
    # Sample function
    xs = np.linspace(-12,10,100)
    ys = f(xs)
    # Plot function
    plt.plot(xs,ys,'r-')
    plt.xlabel('$x$')
    plt.ylabel('$f(x)$')
    plt.show()

# Visualize the function
plotfx()
```



1.1.1 First define the function `fgrad(x)`

```
[37]: # Your fgrad(x) function goes here
def fgrad(x):
    return 2*x + 3 + 6*np.cos(x)
```

1.1.2 Fill in the following code with the gradient descent update rule

For reference, your 10th iteration should have $x = -1.554$ and $f(x) = -8.246$

```
[38]: iter = 10
eta = 0.15
x = 8

for i in range(iter):
    # YOUR GRADIENT DESCENT CODE GOES HERE
    x = x - eta*fgrad(x)
    print('Iteration %d, x = %.3f, f(x) = %.3f' %(i+1, x, f(x)))
```

Iteration 1, x = 5.281, f(x) = 38.675

Iteration 2, x = 2.762, f(x) = 18.138

Iteration 3, $x = 2.319$, $f(x) = 16.734$
Iteration 4, $x = 1.786$, $f(x) = 14.410$
Iteration 5, $x = 0.993$, $f(x) = 8.988$
Iteration 6, $x = -0.247$, $f(x) = -2.147$
Iteration 7, $x = -1.496$, $f(x) = -8.233$
Iteration 8, $x = -1.565$, $f(x) = -8.246$
Iteration 9, $x = -1.551$, $f(x) = -8.246$
Iteration 10, $x = -1.554$, $f(x) = -8.246$

1.1.3 Briefly discuss whether your printed values of x and $f(x)$ appear to have converged to the minimum of the function.

Feel free to refer to the provided plot of $f(x)$ above

Your response goes here

From the iteration values, we can see that the value of x is converging to -1.554 and the value of $f(x)$ is converging to -8.246. The plot of $f(x)$ also shows that the minimum value of $f(x)$ is negative and around -8.246. With the above observations, the printed values of x and $f(x)$ appear to have converged to the minimum of the function.