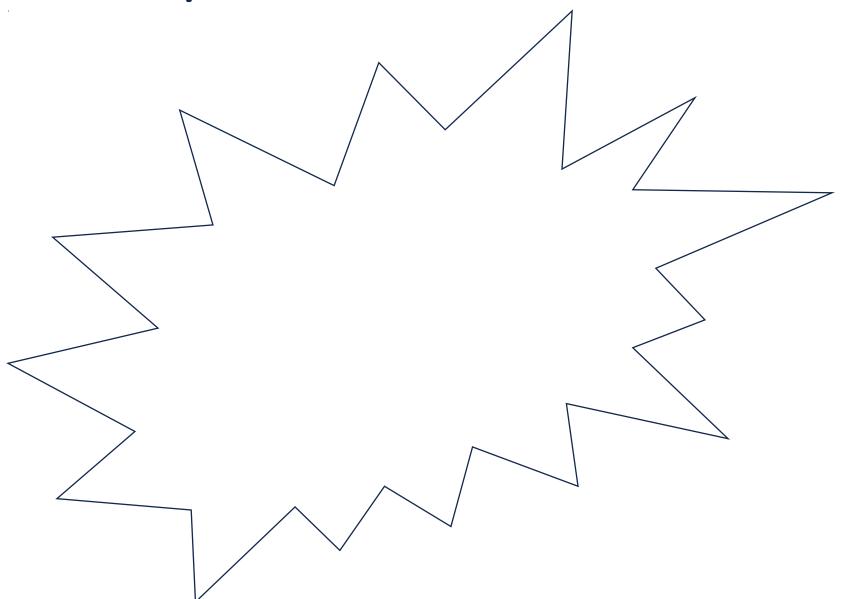
CS 400

Heap - Introduction

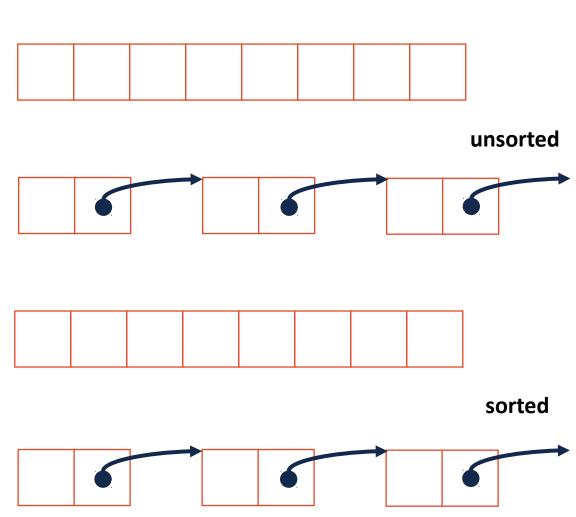
ID: 10-01

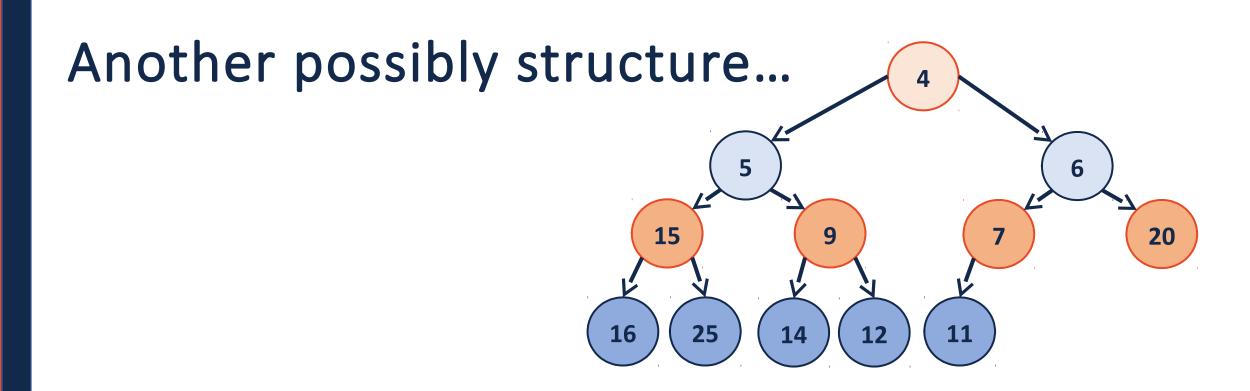
Priority Queue



Priority Queue Implementation

insert	removeMin	
O(1)*	O(n)	
O(1)	O(n)	
O(n)	O(1)	
O(n)	O(1)	

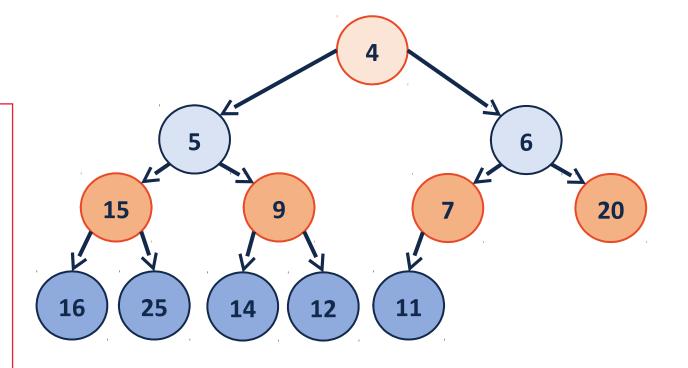




(min)Heap

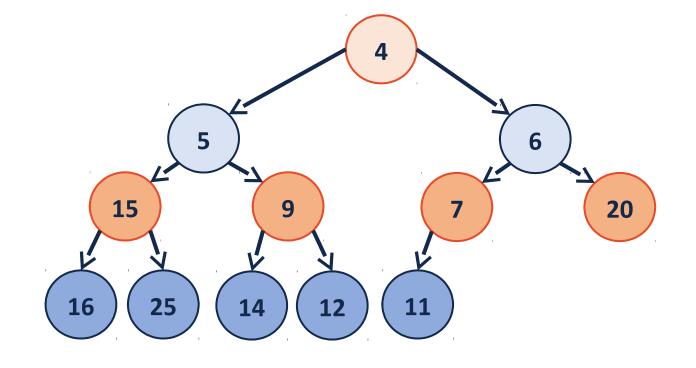
A complete binary tree T is a min-heap if:

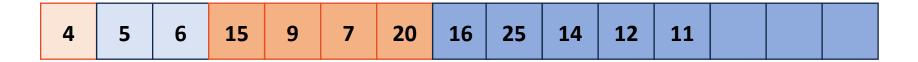
- T = {} or
- T = {r, T_L, T_R}, where r is less than the roots of {T_L, T_R} and {T_L, T_R} are min-heaps.



(min)Heap

```
parent = index / 2
Left Child = index * 2
Right Child = index * 2 + 1
```



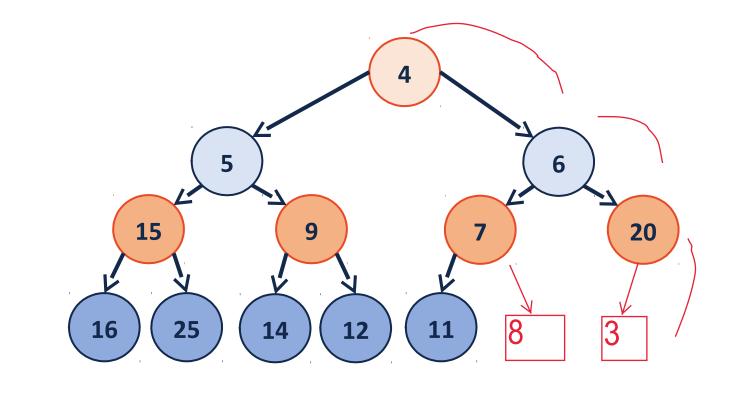


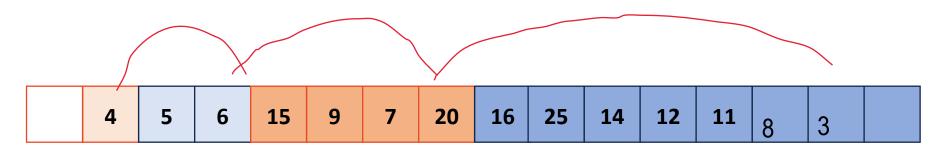
CS 400

Heap – Insert and removeMin

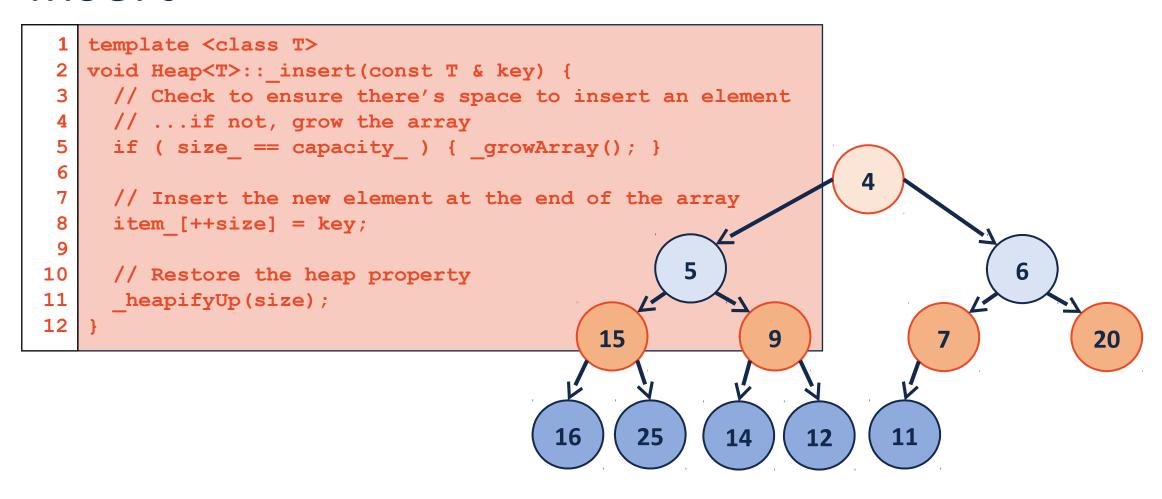
ID: 10-02

insert





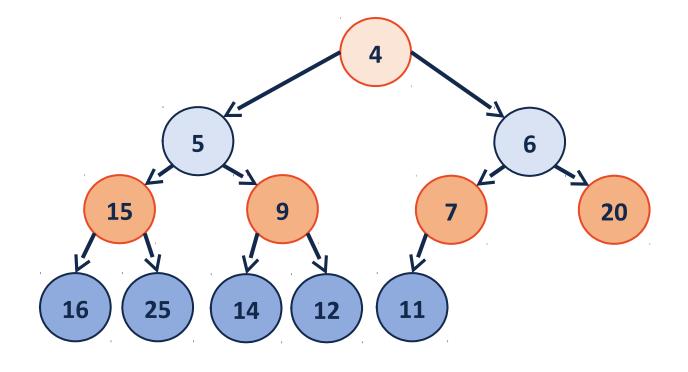
insert





growArray

double size every time





insert-heapifyUp

```
template <class T>
void Heap<T>::_insert(const T & key) {
    // Check to ensure there's space to insert an element
    // ...if not, grow the array
    if ( size_ == capacity_ ) { _growArray(); }

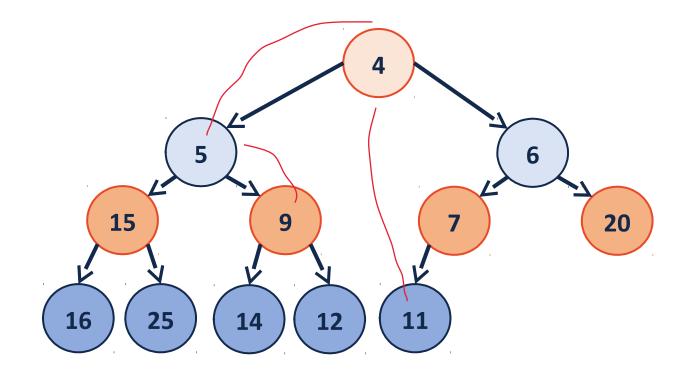
// Insert the new element at the end of the array
    item_[++size] = key;

// Restore the heap property
    _heapifyUp(size);
}
```

```
template <class T>
void Heap<T>::_heapifyUp( ___int index ___) {
   if ( index > ____ ) {
      if ( item_[index] < item_[ parent(index) ] ) {
        std::swap( item_[index], item_[ parent(index) ] );
        __heapifyUp( __parent(index) __);
}

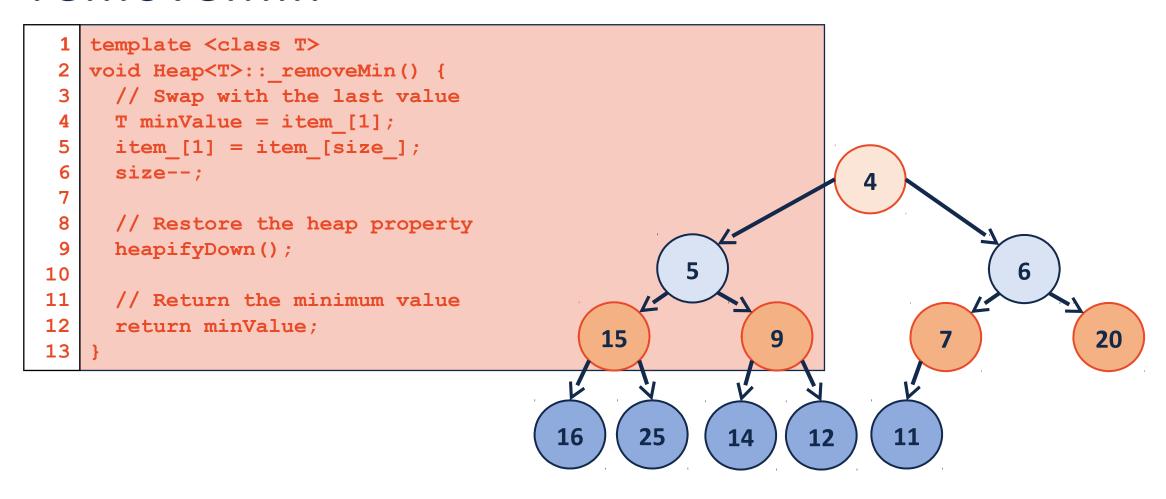
index / 2
</pre>
```

removeMin





removeMin





removeMin-heapifyDown

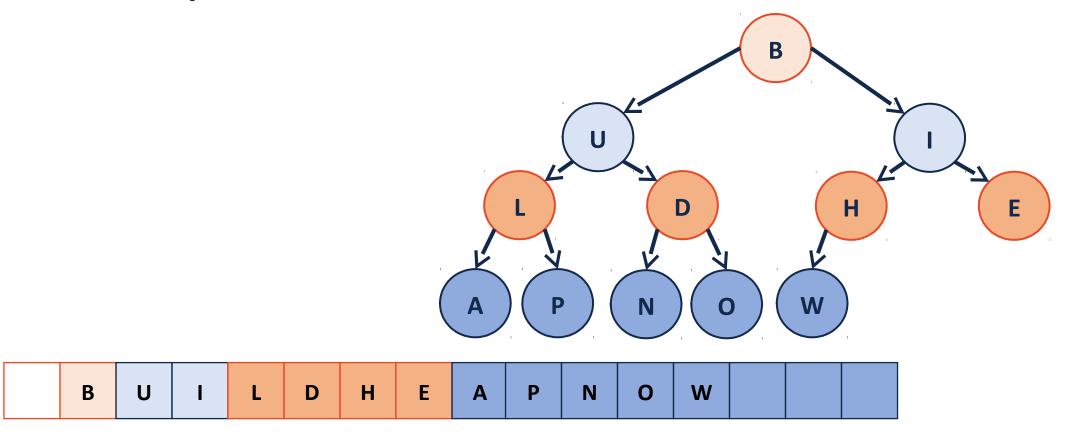
```
template <class T>
   void Heap<T>:: removeMin() {
     // Swap with the last value
     T minValue = item [1];
     item [1] = item [size ];
     size--;
     // Restore the heap property
     heapifyDown();
10
     // Return the minimum value
11
12
     return minValue;
                             template <class T>
13
                             void Heap<T>:: heapifyDown(int index) {
                              if (! isLeaf(index) ) {
                                 T minChildIndex = minChild(index);
                                 if ( item [index] > item [minChildIndex] ) {
                                    std::swap( item [index], item [minChildIndex] );
                                    heapifyDown ( minChild(index) );
```

CS 400

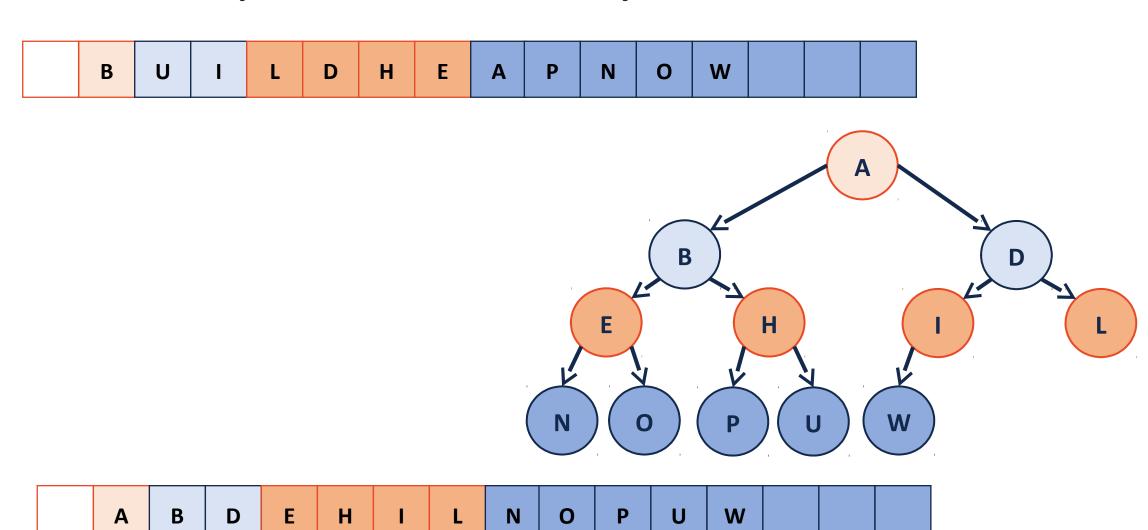
Heap – buildHeap

ID: 10-03

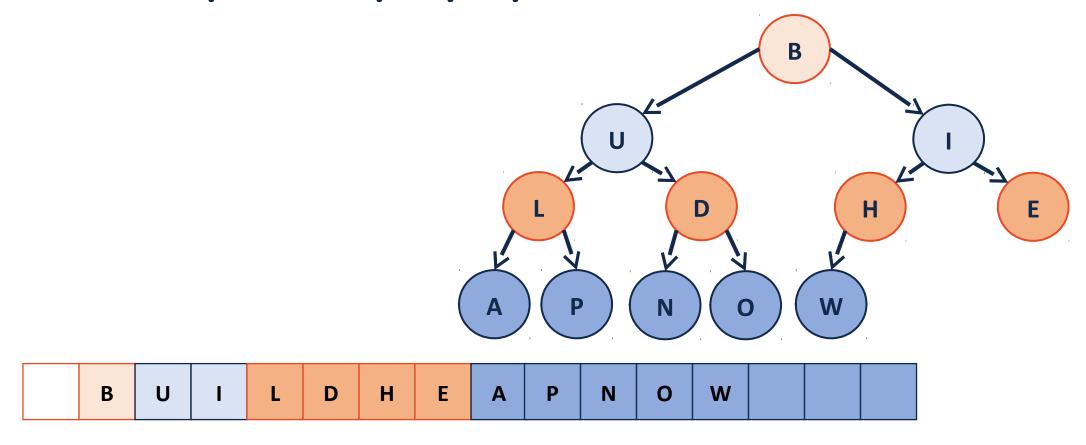
buildHeap



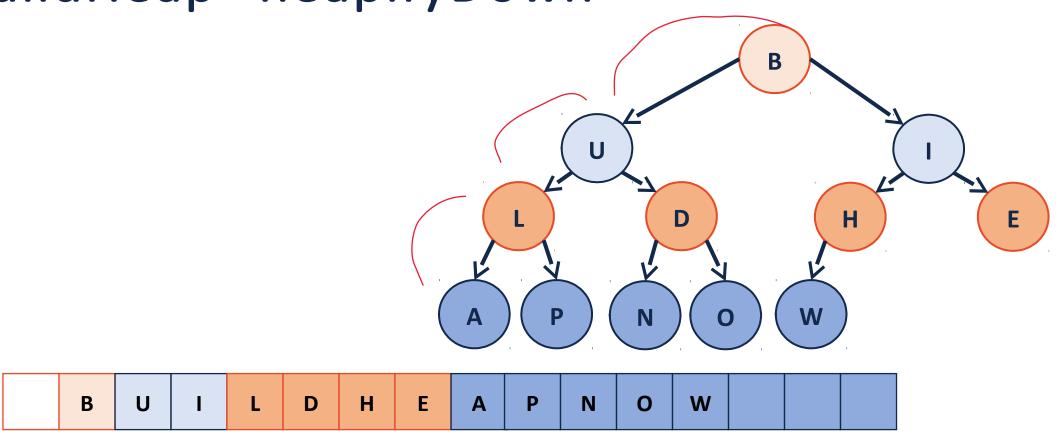
buildHeap - sorted array



buildHeap-heapifyUp



buildHeap-heapifyDown



buildHeap

1. Sort the array – it's a heap!

2.

```
1 template <class T>
2 void Heap<T>::buildHeap() {
3   for (unsigned i = 2; i <= size_; i++) {
4         heapifyUp(i);
5   }
6 }</pre>
```

```
D H E
```

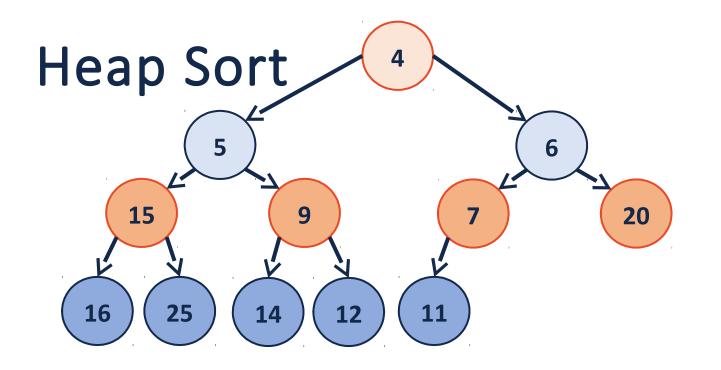
```
1 template <class T>
2 void Heap<T>::buildHeap() {
3    for (unsigned i = parent(size); i > 0; i--) {
4         heapifyDown(i);
5    }
6 }
```

B U I L D H E A P N O W

CS 400

Heap – Runtime Analysis

ID: 10-04



- **1.** Build Healp O(n)
- 2. n * removeMin O(log(n))
- **3.** Swap element to main property



Running Time?

n * log(n) for worst case

Why do we care about another sort?