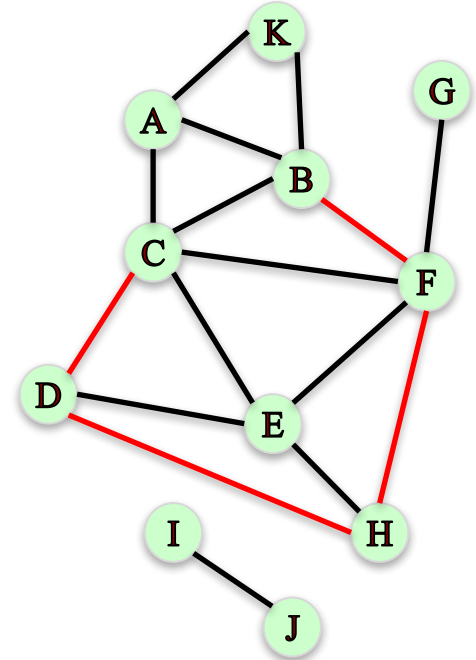


# Triadic Closure

**Triadic closure:** The tendency for people who share connections in a social network to become connected.

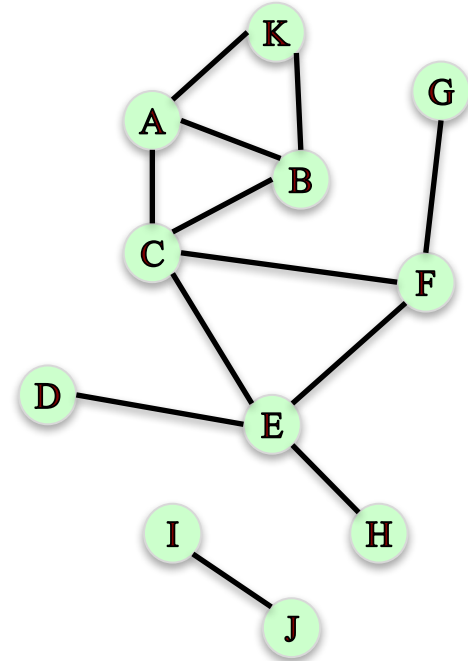
How can we measure the prevalence of triadic closure in a network?



# Local Clustering Coefficient

## Local clustering coefficient of a node:

Fraction of pairs of the node's friends that are friends with each other.



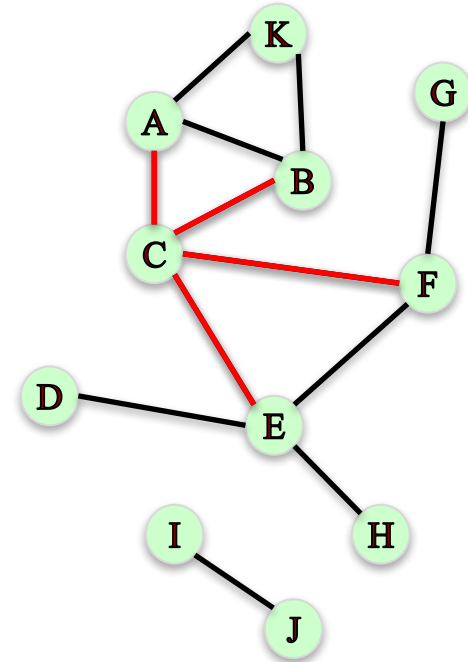
# Local Clustering Coefficient

Compute the local clustering coefficient of node C:

$$\frac{\text{\# of pairs of } C' \text{'s friends who are friends}}{\text{\# of pairs of } C' \text{'s friends}}$$

# of  $C'$ 's friends =  $d_C = 4$  (the “degree” of C)

# of pairs of  $C'$ 's friends =



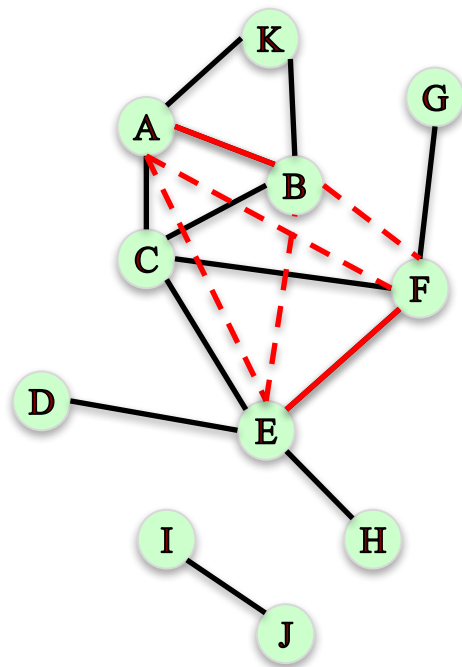
# Local Clustering Coefficient

Compute the local clustering coefficient of node C:

$$\frac{\text{\# of pairs of } C' \text{'s friends who are friends}}{\text{\# of pairs of } C' \text{'s friends}}$$

# of  $C'$ 's friends =  $d_c = 4$  (the “degree” of C)

$$\text{\# of pairs of } C' \text{'s friends} = \frac{d_c(d_c - 1)}{2}$$



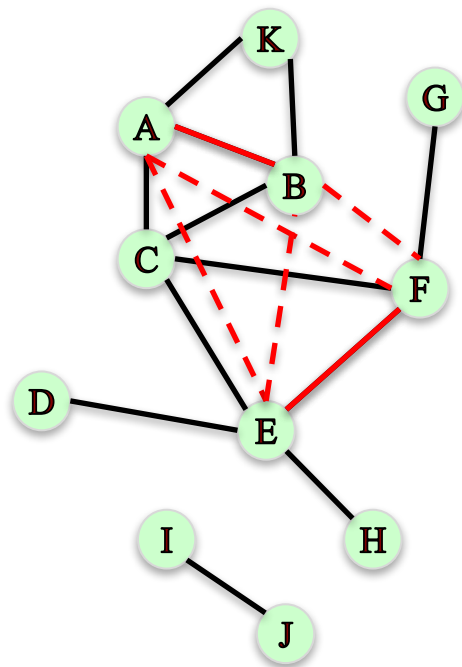
# Local Clustering Coefficient

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$$\text{\# of pairs of } C' \text{'s friends} = \frac{d_c(d_c - 1)}{2} = \frac{12}{2} = 6$$



# Local Clustering Coefficient

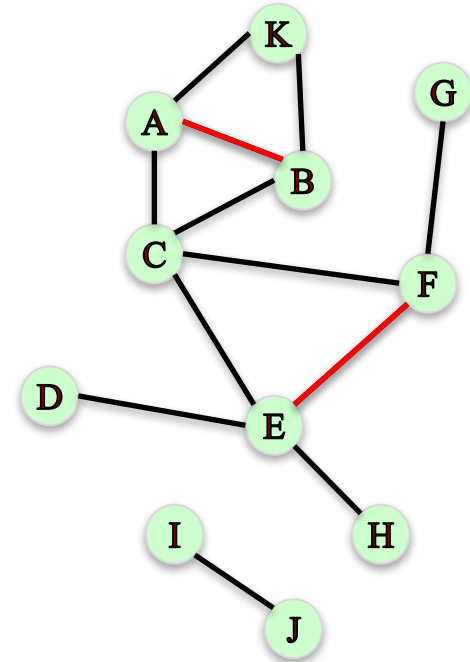
Compute the local clustering coefficient of node C:

$$\frac{\text{\# of pairs of } C' \text{'s friends who are friends}}{\text{\# of pairs of } C' \text{'s friends}}$$

# of  $C'$ 's friends =  $d_c = 4$  (the “degree” of C)

$$\text{\# of pairs of } C' \text{'s friends} = \frac{d_c(d_c - 1)}{2} = \frac{12}{2} = 6$$

# of pairs of  $C'$ 's friends who are friends =



# Local Clustering Coefficient

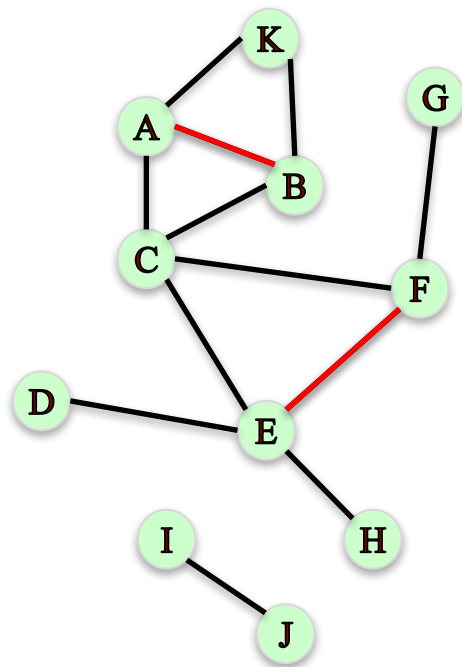
Compute the local clustering coefficient of node C:

$$\frac{\text{\# of pairs of } C' \text{'s friends who are friends}}{\text{\# of pairs of } C' \text{'s friends}}$$

# of  $C'$ 's friends =  $d_c = 4$  (the “degree” of C)

$$\text{\# of pairs of } C' \text{'s friends} = \frac{d_c(d_c - 1)}{2} = \frac{12}{2} = 6$$

# of pairs of  $C'$ 's friends who are friends = 2



# Local Clustering Coefficient

Compute the local clustering coefficient of node C:

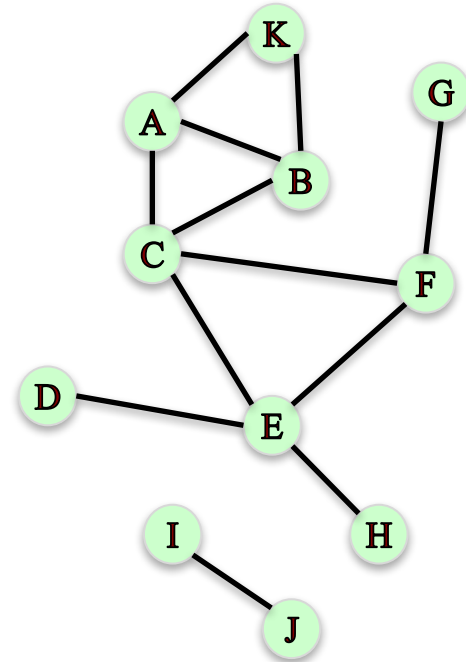
$$\frac{\text{\# of pairs of C's friends who are friends}}{\text{\# of pairs of C's friends}}$$

# of C's friends =  $d_c = 4$  (the “degree” of C)

$$\text{\# of pairs of C's friends} = \frac{d_c(d_c - 1)}{2} = \frac{12}{2} = 6$$

# of pairs of C's friends who are friends = 2

$$\text{Local clustering coefficient of C} = \frac{2}{6} = \frac{1}{3}$$





# Local Clustering Coefficient

Compute the local clustering coefficient of node F:

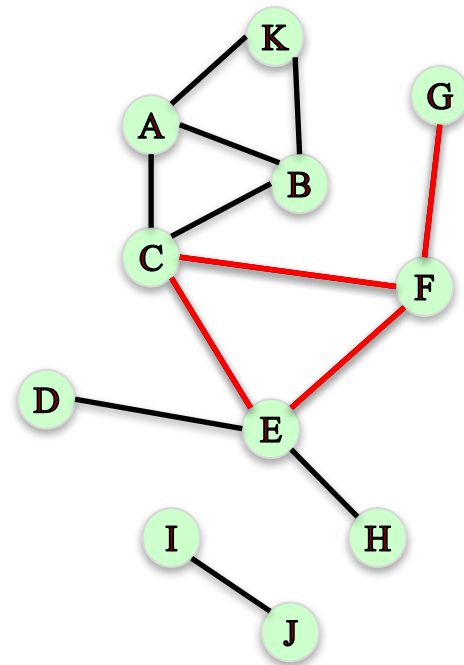
$$\frac{\text{\# of pairs of } F' \text{'s friends who are friends}}{\text{\# of pairs of } F' \text{'s friends}}$$

$$d_F = 3$$

$$\# \text{ of pairs of } F' \text{'s friends} = \frac{d_F(d_F - 1)}{2} = \frac{6}{2} = 3$$

# of pairs of F's friends who are friends = 1

Local clustering coefficient of F =  $\frac{1}{3}$



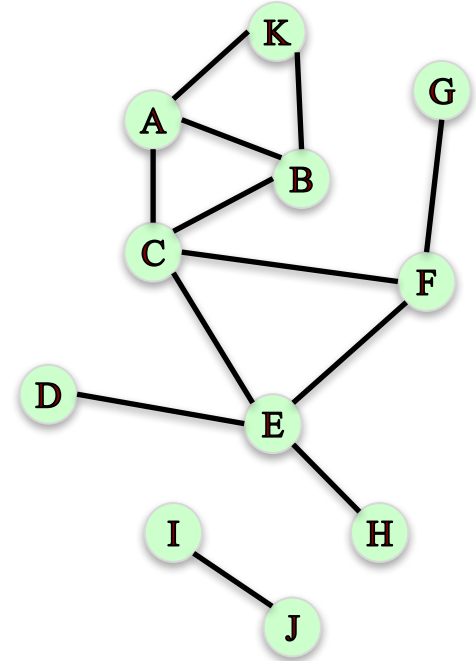
# Local Clustering Coefficient

Compute the local clustering coefficient of node J:

$$\frac{\text{\# of pairs of J's friends who are friends}}{\text{\# of pairs of J's friends}}$$

\# of pairs of J's friends = 0 (Can not divide by 0)

We will assume that the local clustering coefficient of a node of degree less than 2 to be 0.



# Local Clustering Coefficient

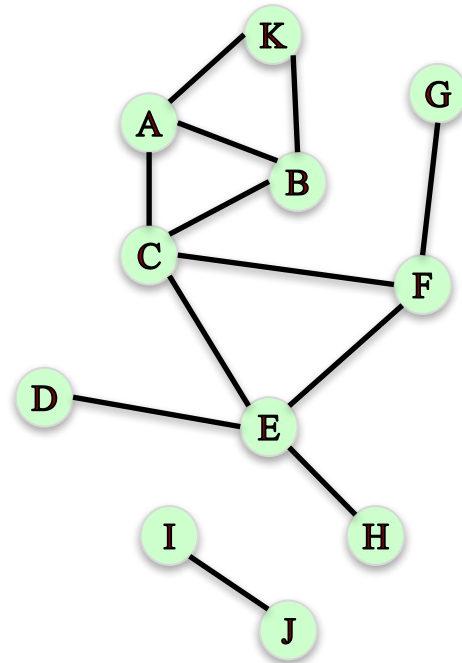
## Local clustering coefficient in NetworkX:

```
G = nx.Graph()
G.add_edges_from([('A', 'K'), ('A', 'B'), ('A', 'C'), ('B', 'C'), ('B', 'K'),
('C', 'E'), ('C', 'F'), ('D', 'E'), ('E', 'F'), ('E', 'H'), ('F', 'G'), ('I', 'J')])
```

```
In: nx.clustering(G, 'F')
Out: 0.3333333333333333
```

```
In: nx.clustering(G, 'A')
Out: 0.6666666666666666
```

```
In: nx.clustering(G, 'J')
Out: 0.0
```

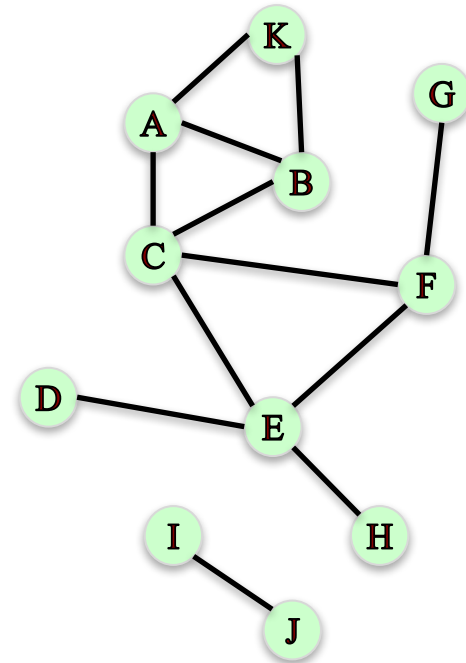


# Global Clustering Coefficient

Measuring clustering on the whole network:

**Approach 1:** Average local clustering coefficient over all nodes in the graph.

```
In: nx.average_clustering(G)  
Out: 0.28787878787878785
```

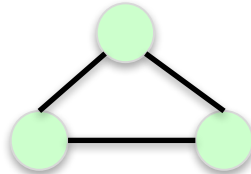


# Global Clustering Coefficient

## Measuring clustering on the whole network (Approach 2):

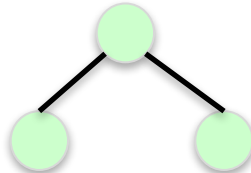
Percentage of “open triads” that are triangles in a network.

Triangles:



$$\text{Transitivity} = \frac{3 * \text{Number of closed triads}}{\text{Number of open triads}}$$

Open triads:

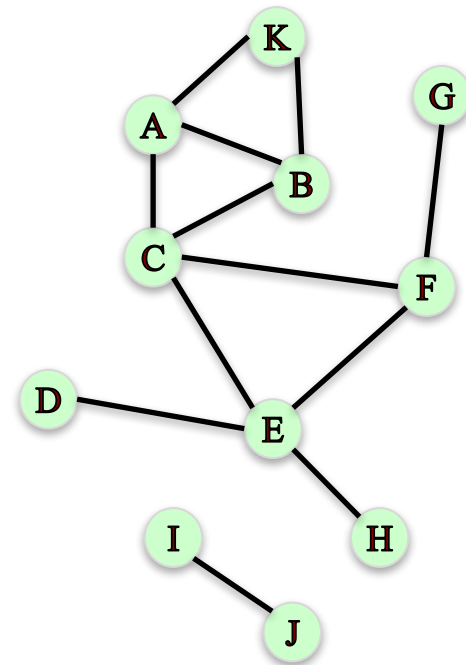


# Global Clustering Coefficient

Measuring clustering on the whole network:

**Transitivity:** Ratio of number of triangles and number of “open triads” in a network.

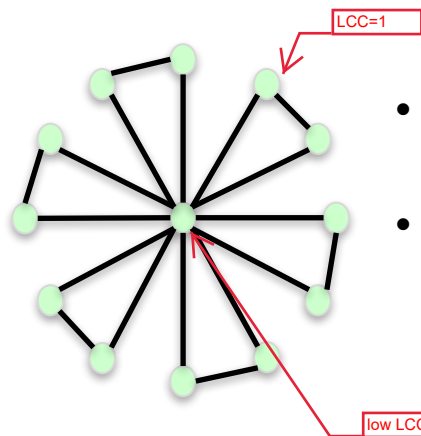
```
In: nx.transitivity(G)  
Out: 0.409090909091
```



# Transitivity vs. Average Clustering Coefficient

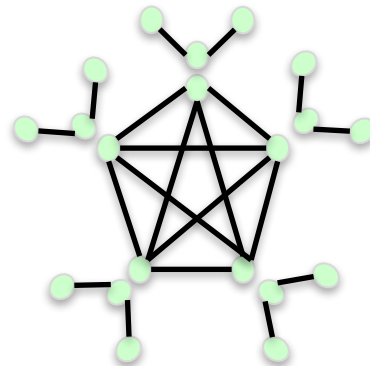
Both measure the tendency for edges to form triangles.

Transitivity weights nodes with large degree higher.



- Most nodes have high LCC
- The high degree node has low LCC

Ave. clustering coeff. = 0.93  
Transitivity = 0.23



- Most nodes have low LCC
- High degree node have high LCC

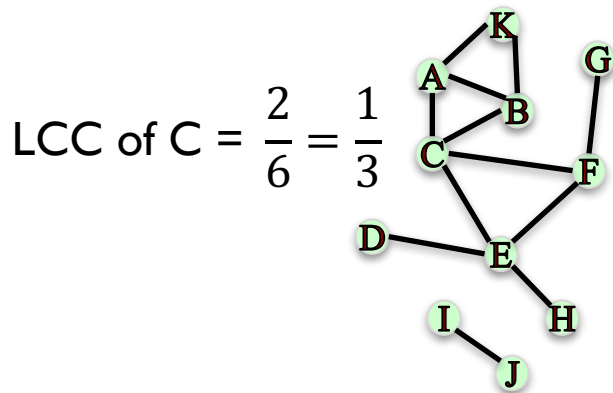
Ave. clustering coeff. = 0.25  
Transitivity = 0.86

# Summary

**Clustering coefficient** measures the degree to which nodes in a network tend to “cluster” or form triangles.

## Local Clustering Coefficient

Fraction of pairs of the node's friends that are friends with each other.



## Global Clustering Coefficient

### Average Local Clustering Coefficient

`nx.average_clustering(G)`

### Transitivity

Ratio of number of triangles and number of “open triads”.

Puts larger weight on high degree nodes.

`nx.transitivity(G)`