



# **Decision Trees**

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# Predicting potential loan defaults

# What makes a loan risky?



### Credit history explained

Did I pay previous loans on time?

Example: excellent, good, or fair

Credit History

\*\*\*\*

Income

\*\*\*\*

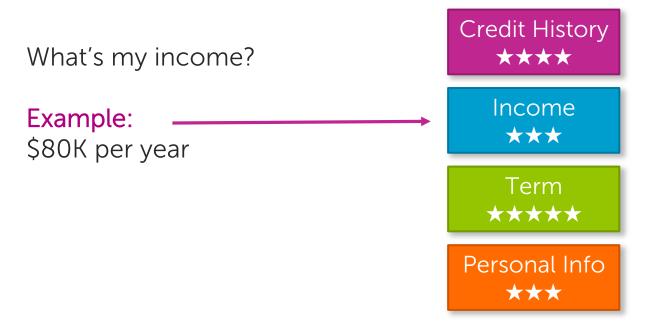
Term

\*\*\*\*

Personal Info

\*\*\*\*

#### Income



#### Loan terms

How soon do I need to pay the loan?

Example: 3 years,

5 years,...









#### Personal information

Age, reason for the loan, marital status,...

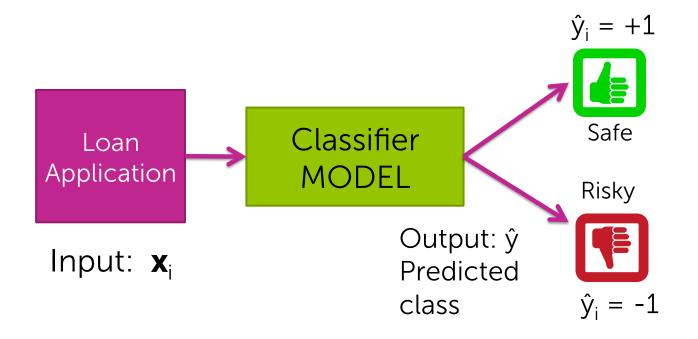
**Example:** Home loan for a married couple



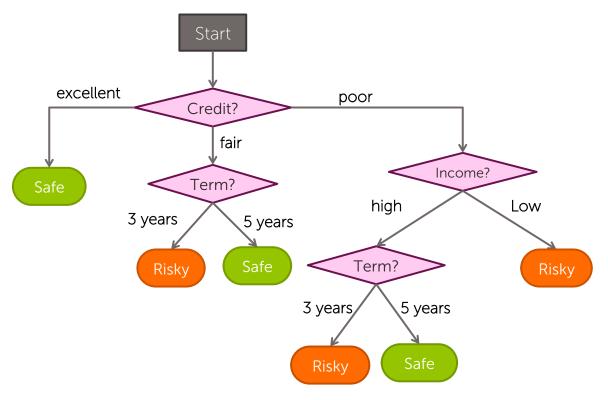
# Intelligent application



#### Classifier review

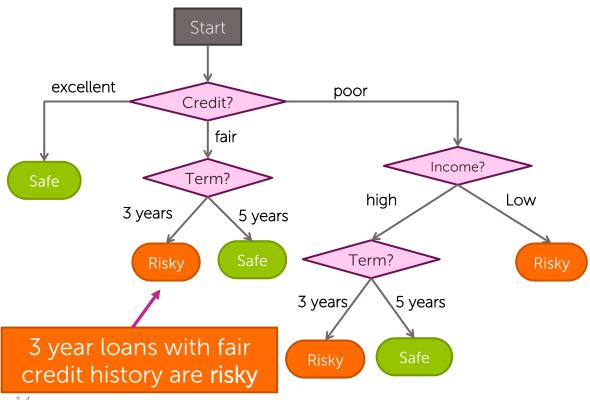


#### This module ... decision trees

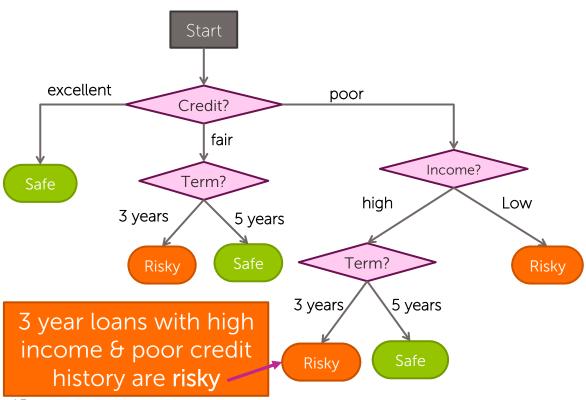


# Decision trees: Intuition

#### What does a decision tree represent?



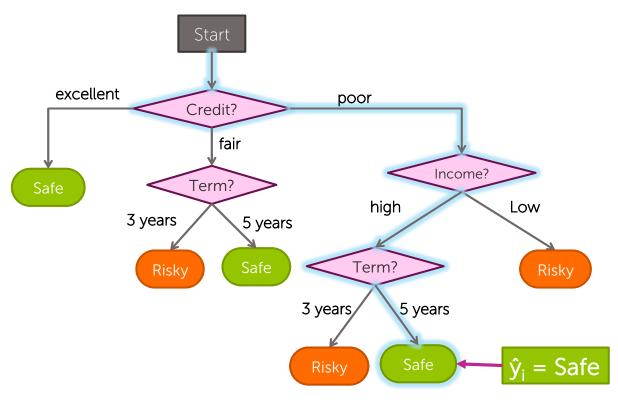
#### What does a decision tree represent?



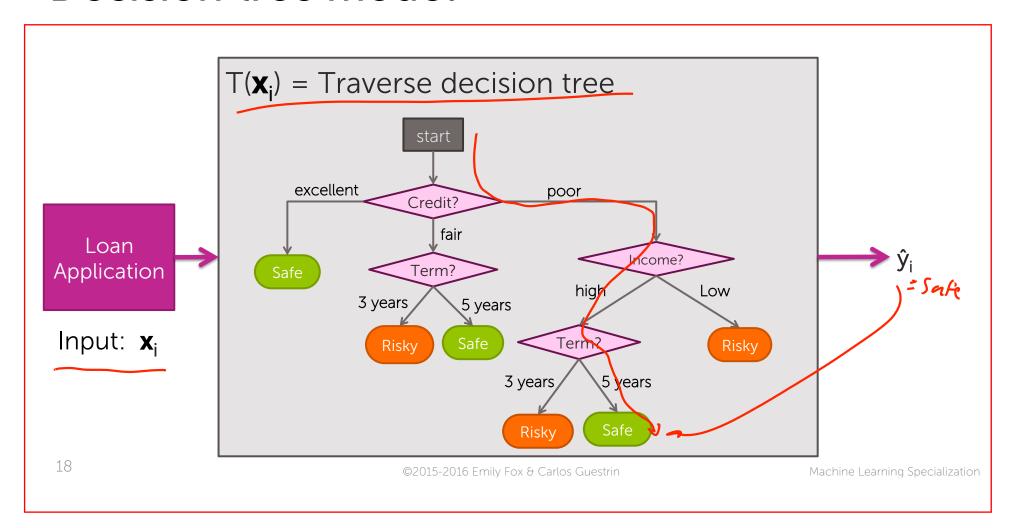
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# Scoring a loan application

 $\mathbf{x}_{i}$  = (Credit = poor, Income = high, Term = 5 years)

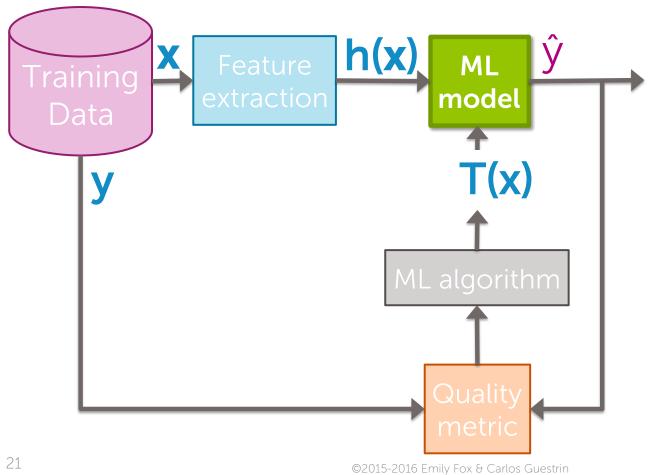


#### Decision tree model



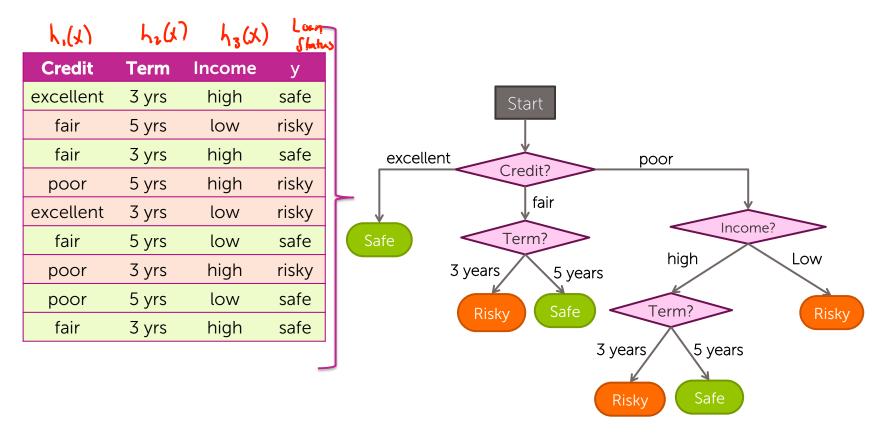
# Decision tree learning task

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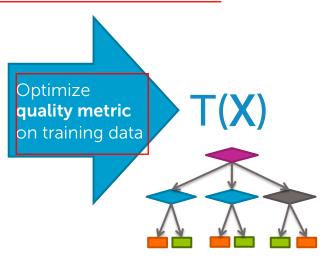
#### Learn decision tree from data?



# Decision tree learning problem

Training data: N observations  $(\mathbf{x}_i, y_i)$ 

Credit	Term	Income	у
excellent	3 yrs	high	safe
fair	5 yrs	low	risky
fair	3 yrs	high	safe
poor	5 yrs	high	risky
excellent	3 yrs	low	risky
fair	5 yrs	low	safe
poor	3 yrs	high	risky
poor	5 yrs	low	safe
fair	3 yrs	high	safe



#### Quality metric: Classification error

Error measures fraction of mistakes

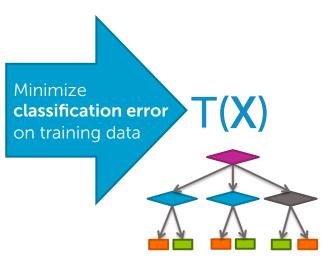
Error = # incorrect predictions # examples

- Best possible value : 0.0

- Worst possible value: 1.0

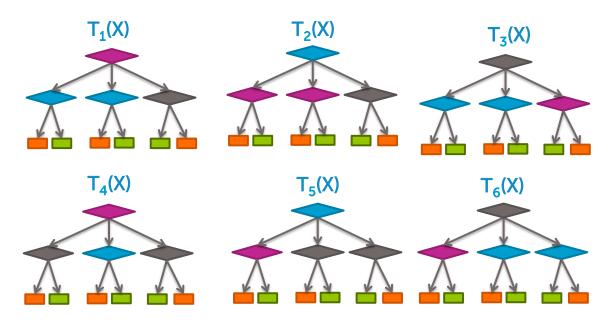
#### Find the tree with lowest classification error

Credit	Term	Income	у
excellent	3 yrs	high	safe
fair	5 yrs	low	risky
fair	3 yrs	high	safe
poor	5 yrs	high	risky
excellent	3 yrs	low	risky
fair	5 yrs	low	safe
poor	3 yrs	high	risky
poor	5 yrs	low	safe
fair	3 yrs	high	safe



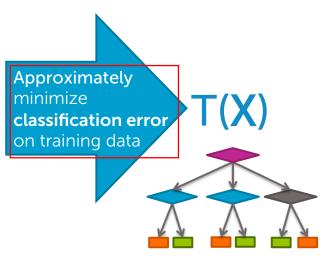
#### How do we find the best tree?

Exponentially large number of possible trees makes decision tree learning hard! (NP-hard problem)



# Simple (greedy) algorithm finds "good" tree

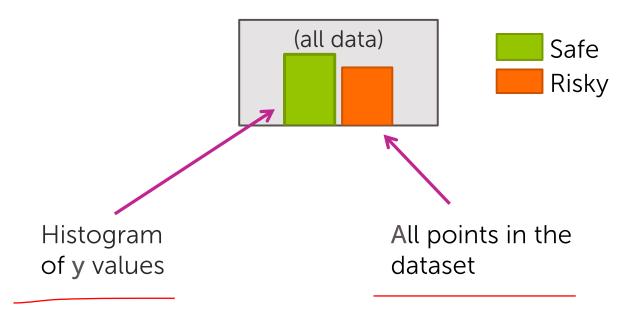
Credit	Term	Income	у
excellent	3 yrs	high	safe
fair	5 yrs	low	risky
fair	3 yrs	high	safe
poor	5 yrs	high	risky
excellent	3 yrs	low	risky
fair	5 yrs	low	safe
poor	3 yrs	high	risky
poor	5 yrs	low	safe
fair	3 yrs	high	safe



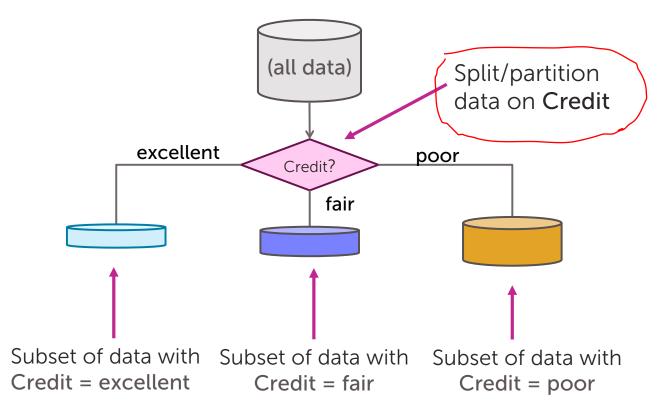
# Greedy decision tree learning: *Algorithm outline*

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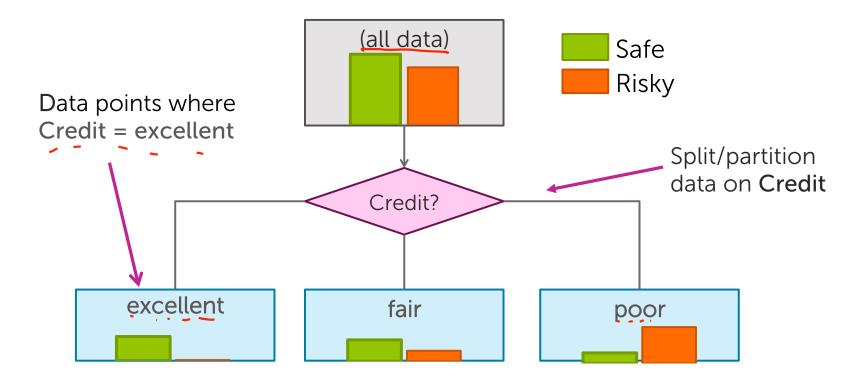
# Step 1: Start with an empty tree



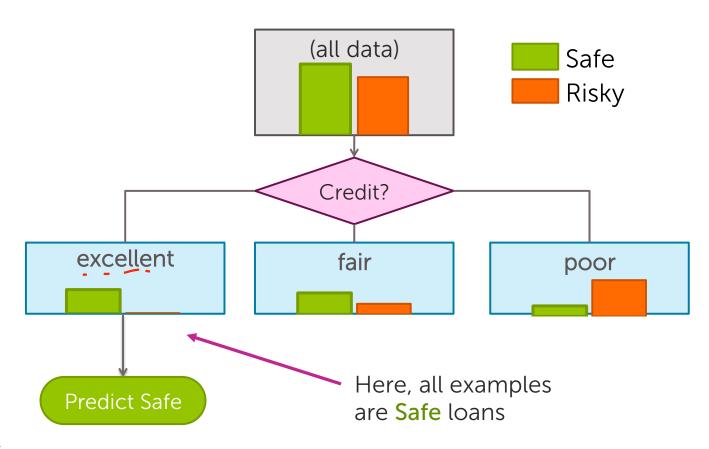
# Step 2: Split on a feature



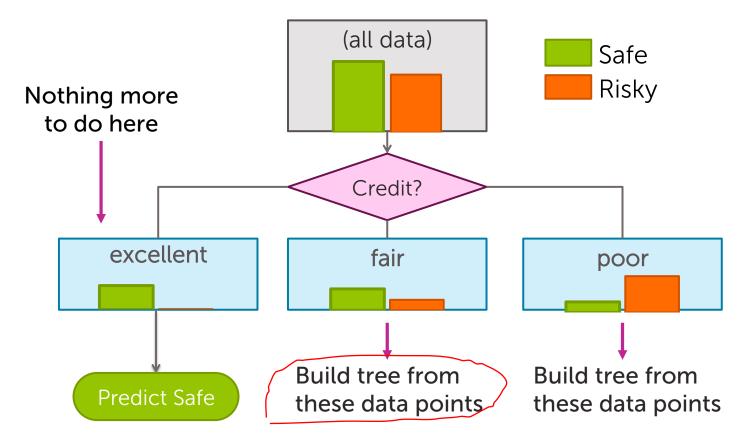
# Feature split explained



# Step 3: Making predictions



# Step 4: Recursion



### Greedy decision tree learning

- Step 1: Start with an empty tree
- Step 2: Select a feature to split data
- For each split of the tree:
  - Step 3: If nothing more to, make predictions
  - Step 4: Otherwise, go to Step 2 & continue (recurse) on this split

Problem 1: Feature split selection

Problem 2: Stopping condition

Recursion

Feature split learning

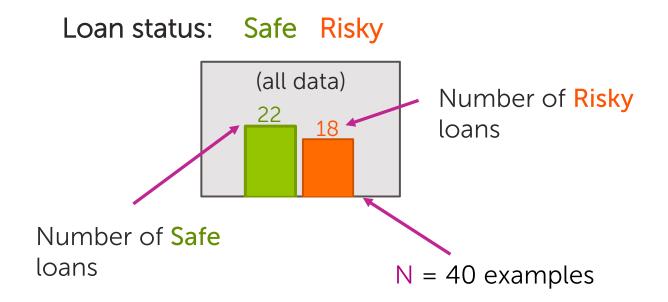
Decision stump learning

#### Start with the data

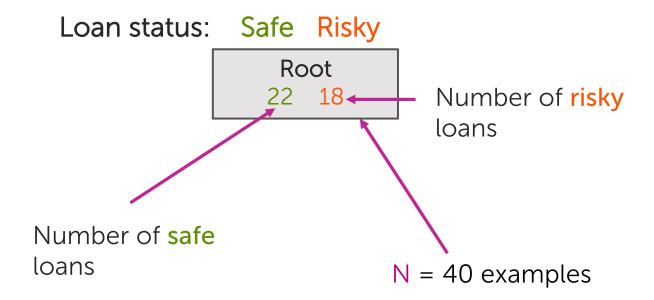
#### Assume N = 40, 3 features

Credit	Term	Income	У
excellent	3 yrs	high	safe
fair	5 yrs	low	risky
fair	3 yrs	high	safe
poor	5 yrs	high	risky
excellent	3 yrs	low	risky
fair	5 yrs	low	safe
poor	3 yrs	high	risky
poor	5 yrs	low	safe
fair	3 yrs	high	safe

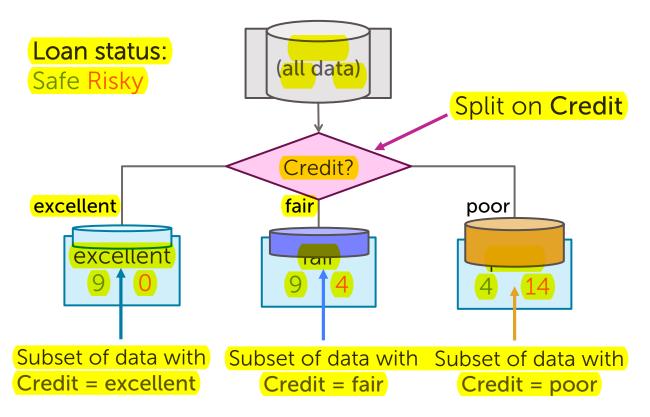
#### Start with all the data



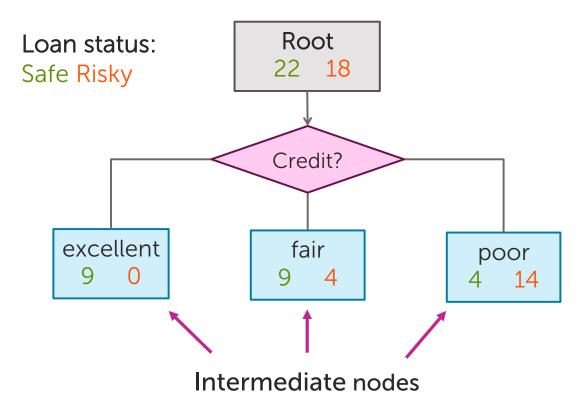
# Compact visual notation: Root node



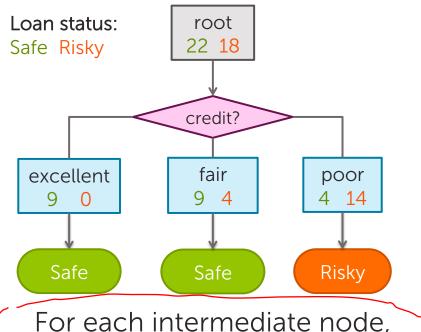
## Decision stump: Single level tree



# Visual Notation: Intermediate nodes



# Making predictions with a decision stump



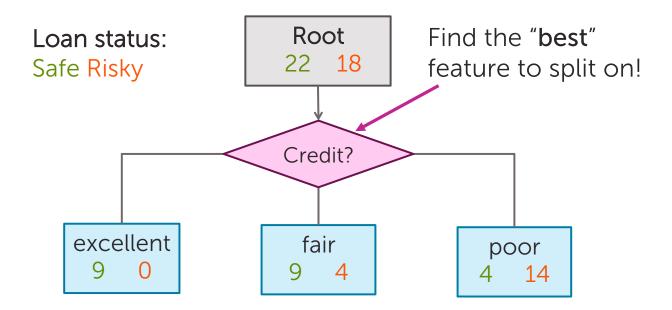
For each intermediate node, set  $\hat{y} = majority value$ 

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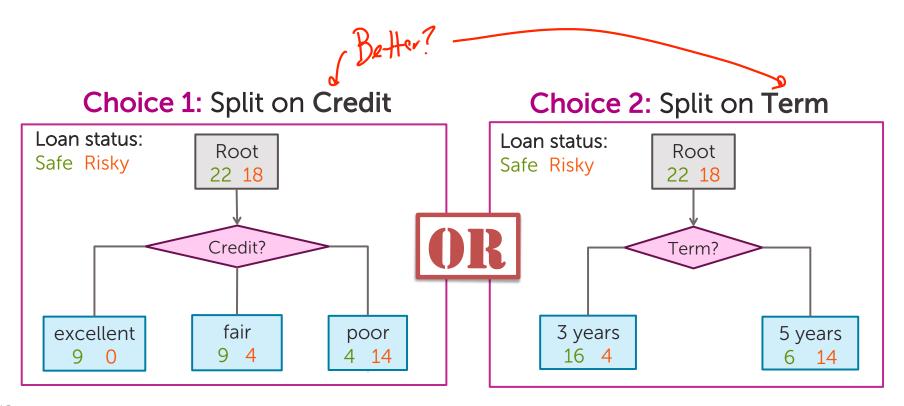
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### Selecting best feature to split on

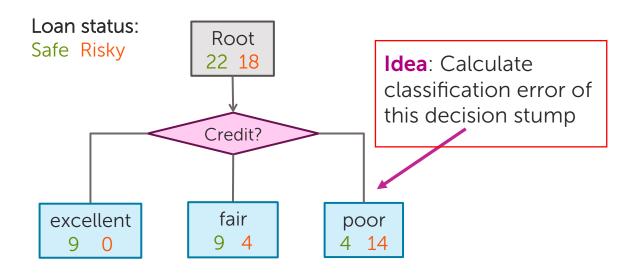
## How do we learn a decision stump?



#### How do we select the best feature?



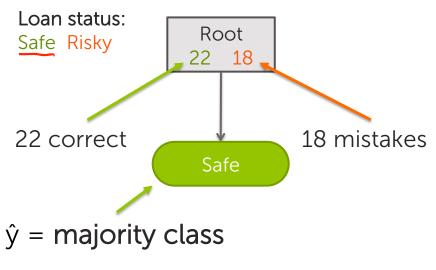
# How do we measure effectiveness of a split?



Error = # mistakes # data points

## Calculating classification error

- Step 1:  $\hat{y}$  = class of majority of data in node
- Step 2: Calculate classification error of predicting ŷ for this data

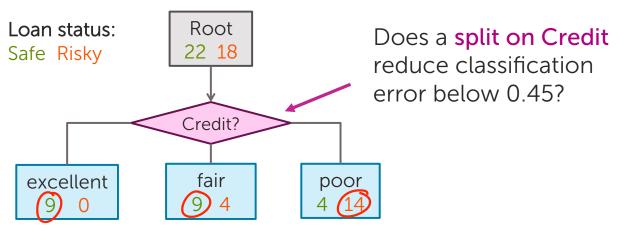


Error =	18
=	

Tree	Classification error	
(root)	0.45	

## Choice 1: Split on credit history?

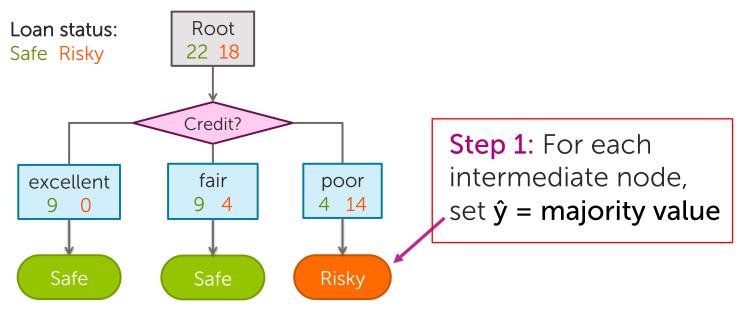
Choice 1: Split on Credit



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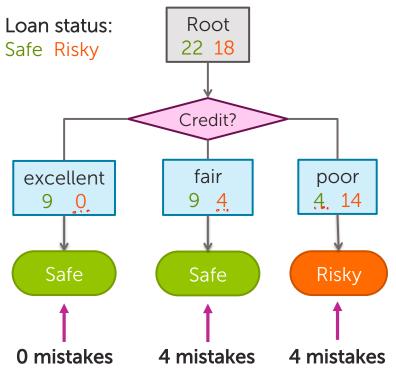
## How good is the split on Credit?

Choice 1: Split on Credit



## Split on Credit: Classification error

Choice 1: Split on Credit



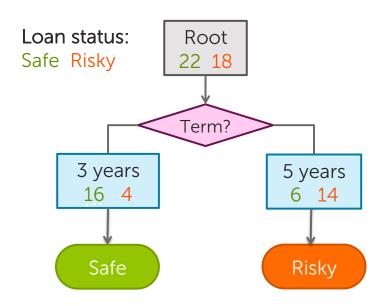
$$Error = \underbrace{4+4}_{40}$$

$$= 0.20$$

Tree	Classification error	
(root)	0.45	
Split on <b>credit</b>	0.2	

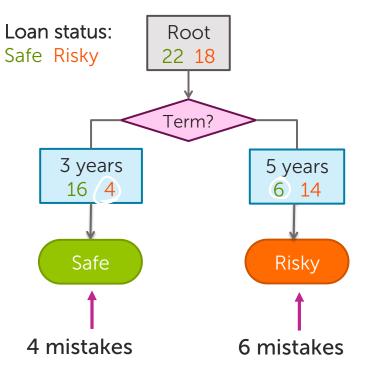
## Choice 2: Split on Term?

#### Choice 2: Split on Term



## Evaluating the split on Term

#### Choice 2: Split on Term



$$Error = \frac{4+6}{40}$$
$$= 0.25$$

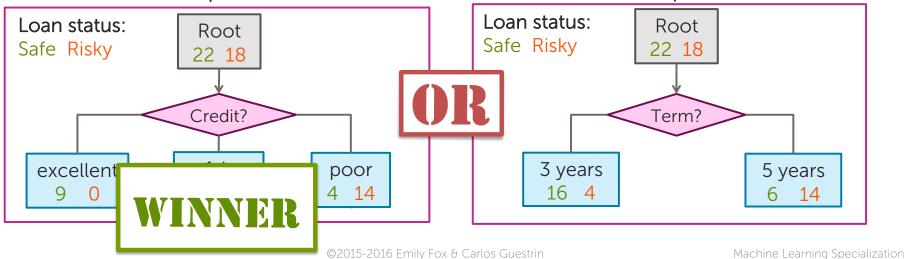
Tree	Classification error	
(root)	0.45	
Split on <b>credit</b>	0.2	
Split on term	0.25	

#### Choice 1 vs Choice 2

Tree	Classification error	
(root)	0.45	
split on <b>credit</b>	0.2	-First
split on <b>loan term</b>	0.25	35

Choice 1: Split on Credit

Choice 2: Split on Term



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### Feature split selection algorithm

- Given a subset of data M (a node in a tree)
- For each feature  $h_i(x)$ :  $\checkmark$  credit, two, income
  - 1. Split data of M according to feature  $h_i(x)$
  - 2. Compute classification error split
- Chose feature <u>h\*(x)</u> with lowest classification error \( \)

## Greedy decision tree learning

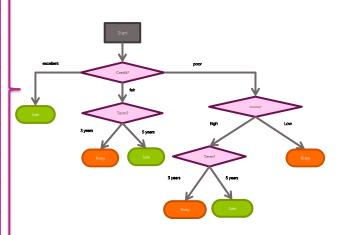
- Step 1: Start with an empty tree
- Step 2: Select a feature to split data
- For each split of the tree:
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  - Step 4: Otherwise, go to Step 2 & continue (recurse) on this split

Pick feature split leading to lowest classification error

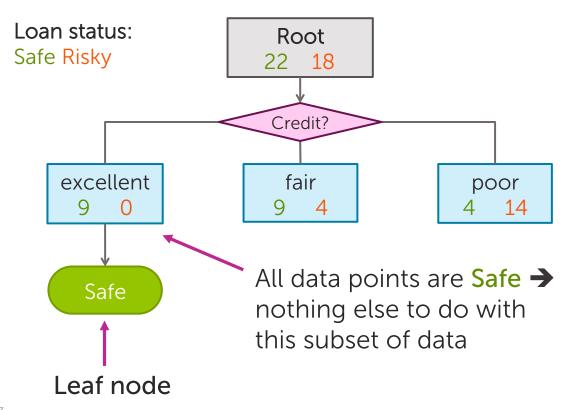
# Decision Tree Learning: Recursion & Stopping conditions

### Learn decision tree from data?

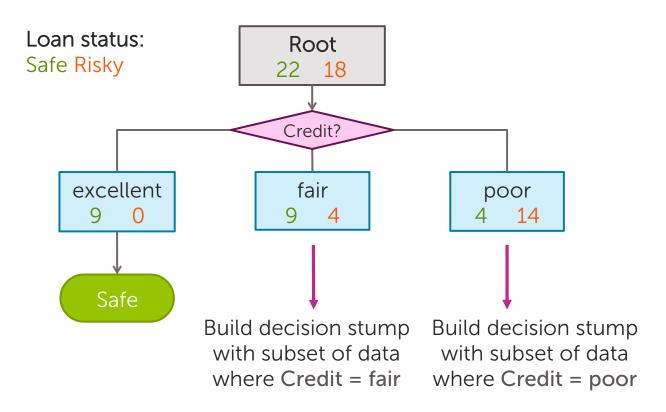
Credit	Term	Income	у
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poor	3 yrs	high	risky
poor	5 yrs	low	safe
fair	3 yrs	high	safe



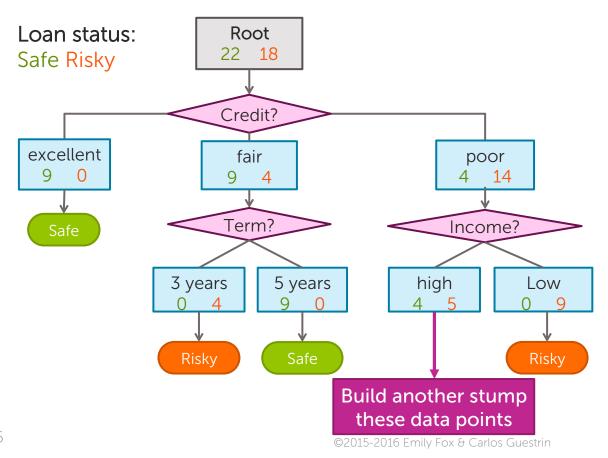
#### We've learned a decision stump, what next?



## Tree learning = Recursive stump learning

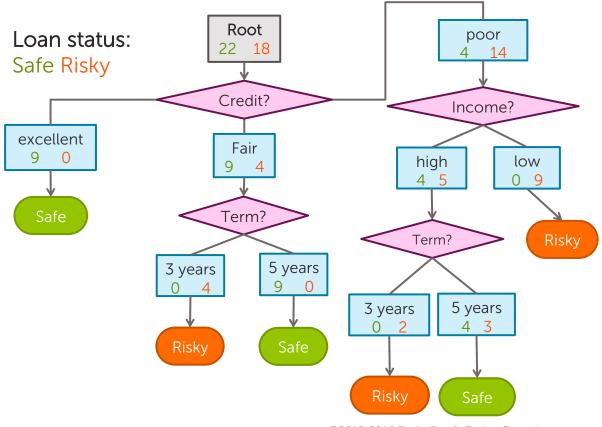


#### Second level



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### Final decision tree



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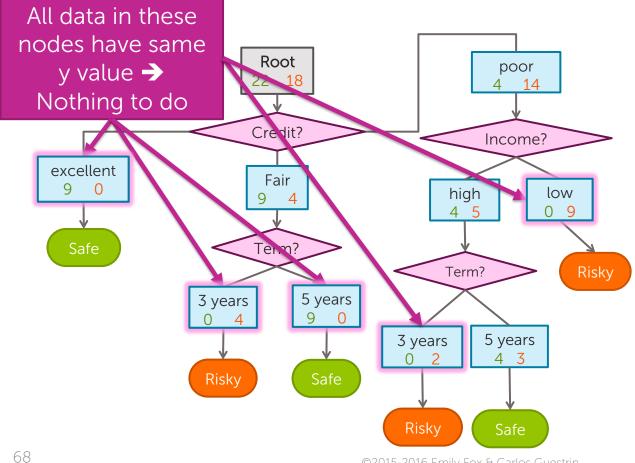
## Simple greedy decision tree learning

Pick best feature to split on Learn decision stump with this split For each leaf of decision stump, recurse When do we stop??? 67

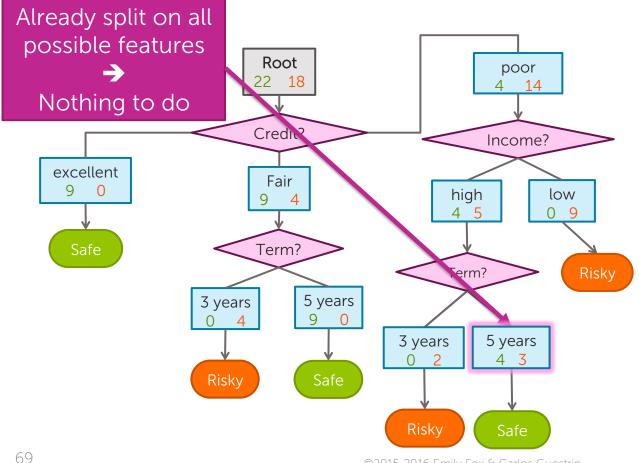
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## Stopping condition 1: All data agrees on y



### Stopping condition 2: Already split on all features



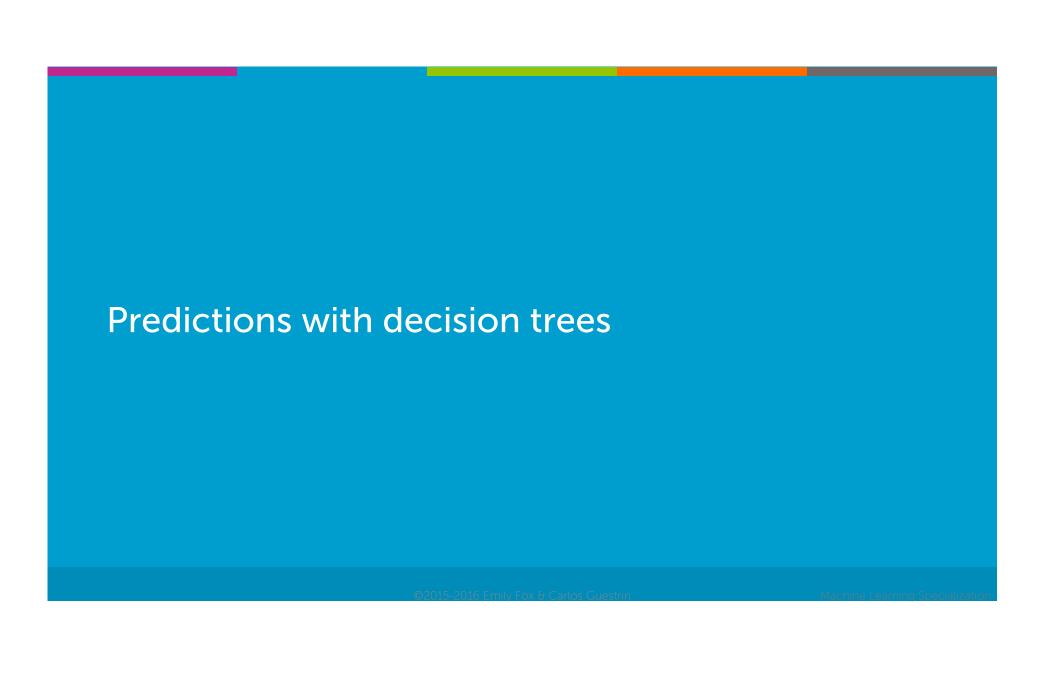
## Greedy decision tree learning

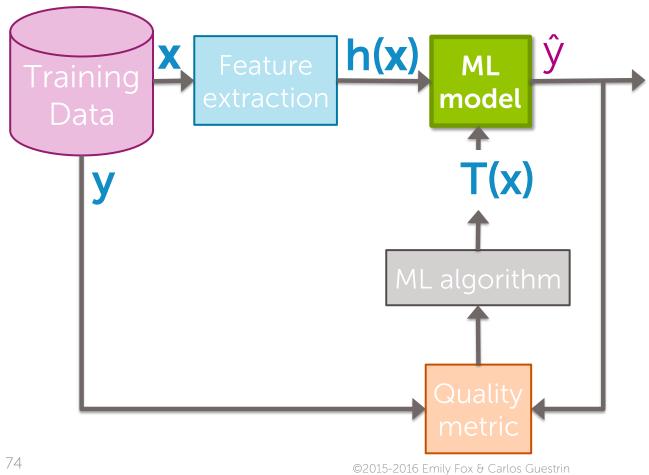
- Step 1: Start with an empty tree
- Step 2: Select a feature to split data
- For each split of the tree:
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  - Step 4: Otherwise, go to Step 2 & continue (recurse) on this split

Pick feature split leading to lowest classification error

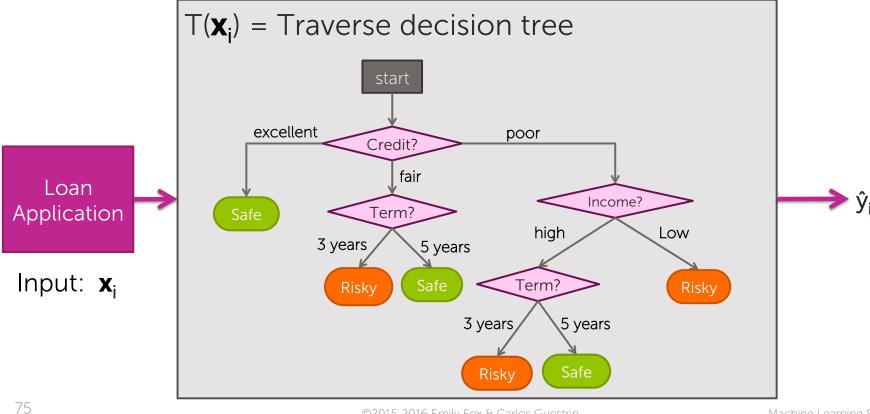
Stopping conditions 1 & 2

Recursion



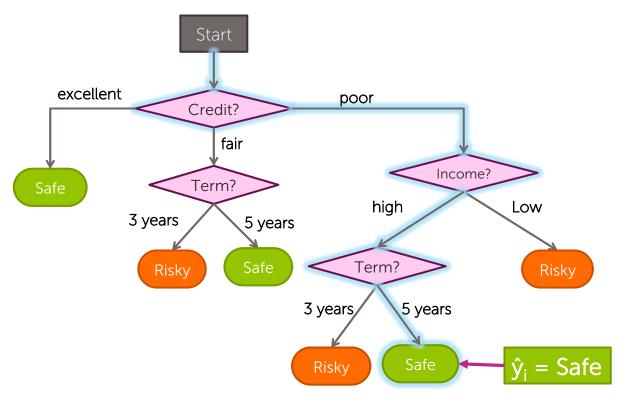


#### Decision tree model



# Traversing a decision tree

 $\mathbf{x}_{i}$  = (Credit = poor, Income = high, Term = 5 years)



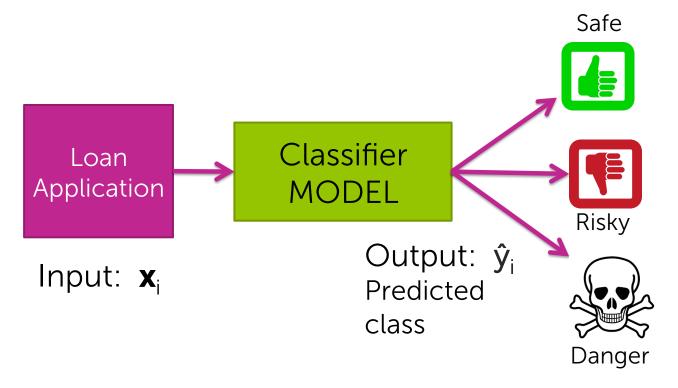
## Decision tree prediction algorithm

#### predict(tree\_node, input)

- If current tree\_node is a leaf:
  - return majority class of data points in leaf
- else:
  - next\_note = child node of tree\_node whose feature value agrees with input
  - return predict(next\_note, input)

# Multiclass classification & predicting probabilities

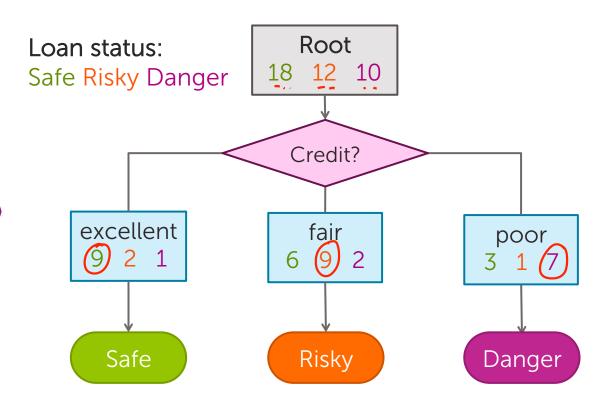
## Multiclass prediction



## Multiclass decision stump

N = 40, 1 feature, 3 classes

Credit	у	
excellent	safe	
fair	risky	
fair	safe	
poor	danger	
excellent	risky	
fair	safe	
poor	danger	
poor	safe	
fair	safe	

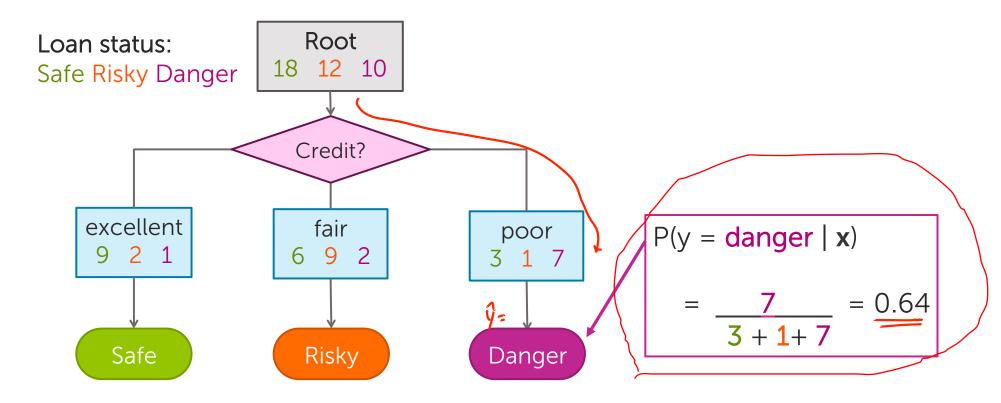


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# Predicting probabilities with decision trees

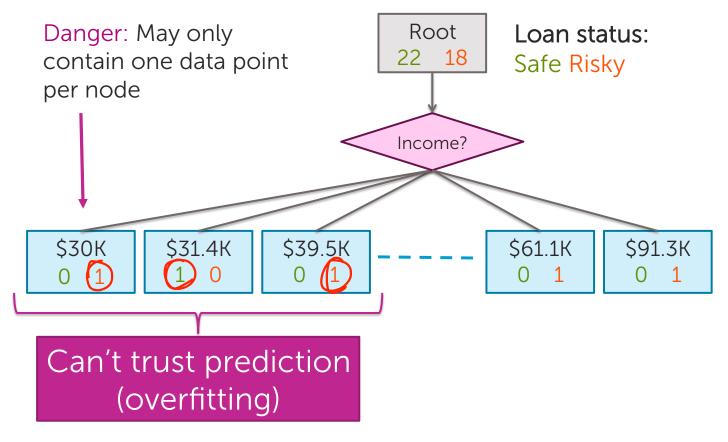


# Decision tree learning: *Real valued features*

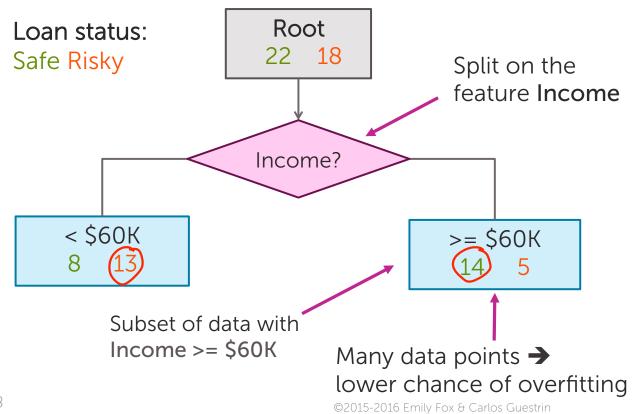
## How do we use real values inputs?

Income	Credit	Term	у
\$105 K	excellent	3 yrs	Safe
\$112 K	good	5 yrs	Risky
\$73 K	fair	3 yrs	Safe
\$69 K	excellent	5 yrs	Safe
\$217 K	excellent	3 yrs	Risky
\$120 K	good	5 yrs	Safe
\$64 K	fair	3 yrs	Risky
\$340 K	excellent	5 yrs	Safe
\$60 K	good	3 yrs	Risky

## Split on each numeric value?

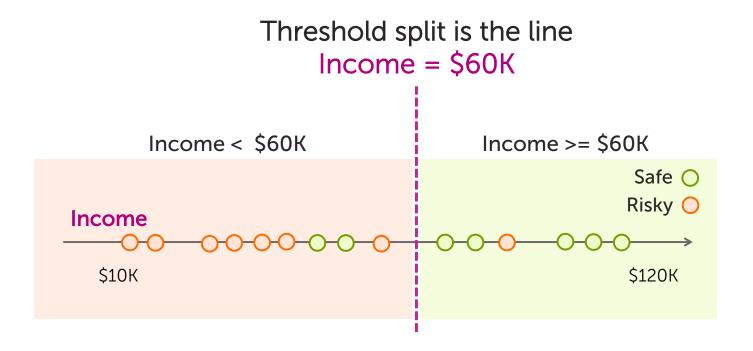


#### Alternative: Threshold split

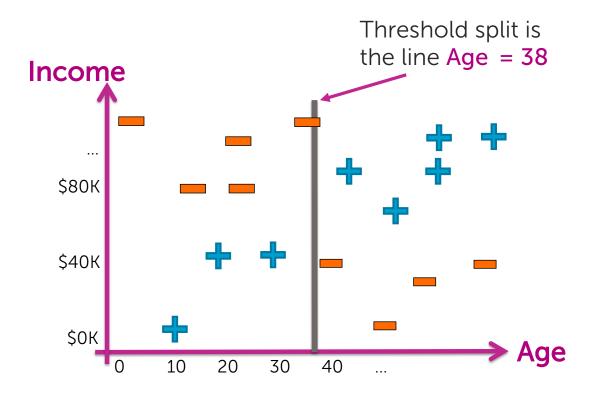


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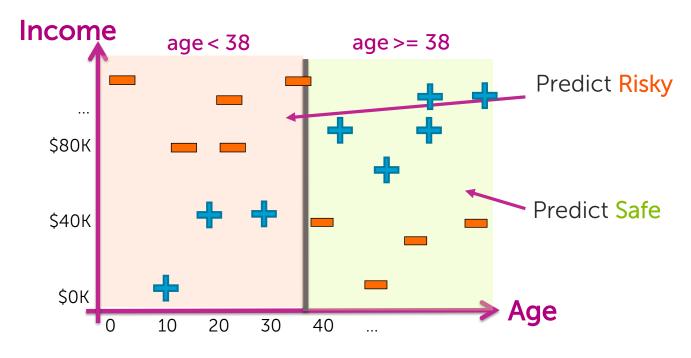
#### Threshold splits in 1-D



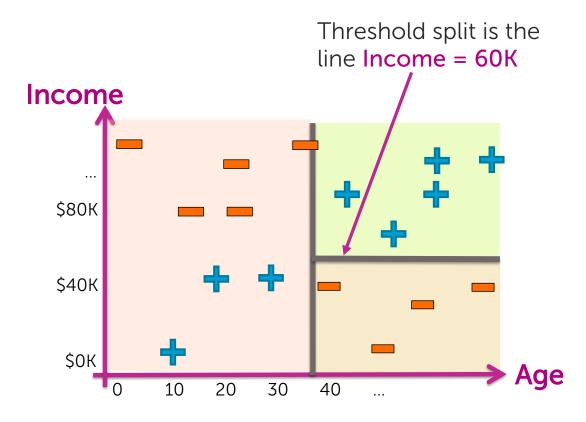
## Visualizing the threshold split



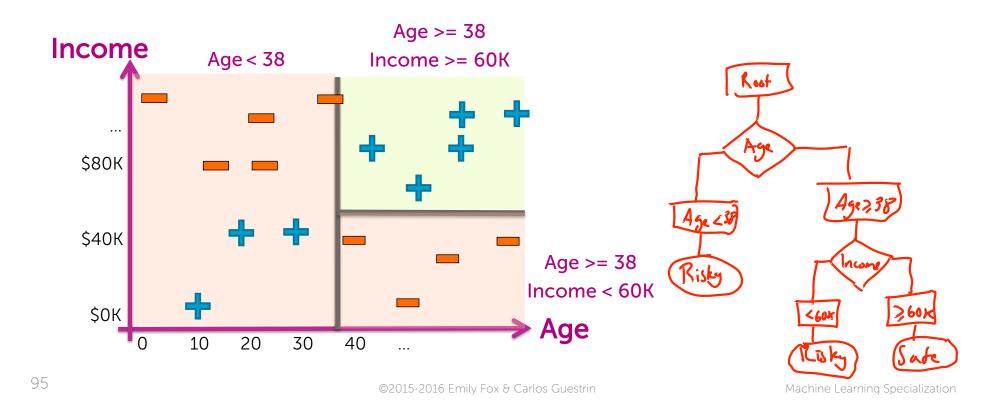
# Split on Age >= 38



#### Depth 2: Split on Income >= \$60K



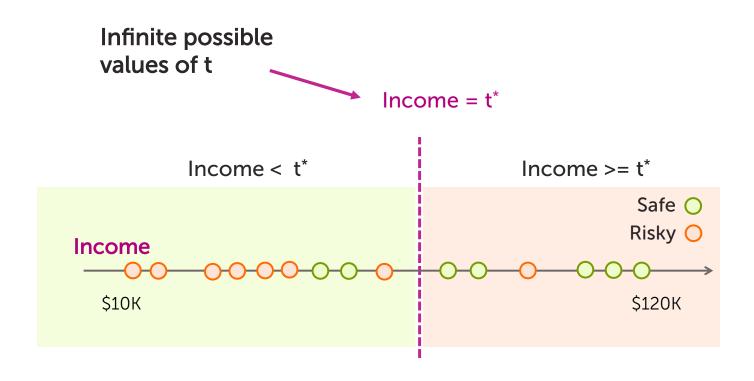
# Each split partitions the 2-D space



#### Finding the best threshold split



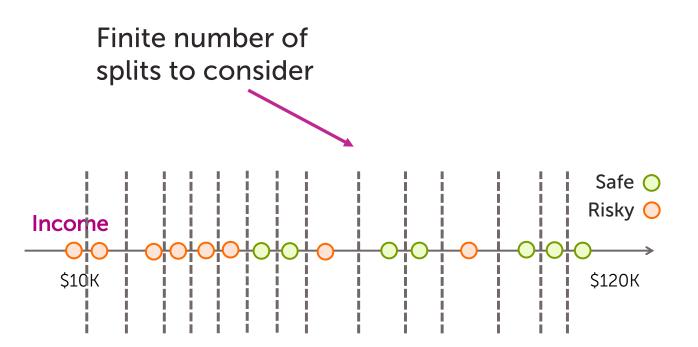
## Finding the best threshold split



#### Consider a threshold between points

Same classification error for any threshold split between  $v_A$  and  $v_B$ Safe O
Risky O
\$10K

#### Only need to consider mid-points



#### Threshold split selection algorithm

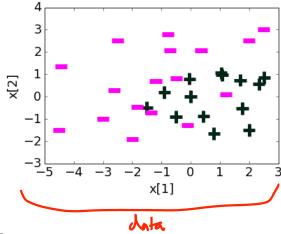
/ Income

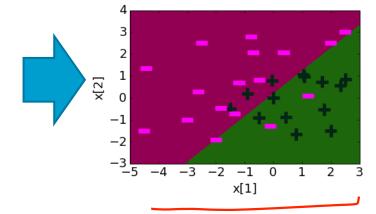
- Step 1: Sort the values of a feature  $h_j(\mathbf{x})$ : Let  $\{\mathbf{v_1}, \mathbf{v_2}, \mathbf{v_3}, ... \mathbf{v_N}\}$  denote sorted values
- Step 2:
  - For i = 1 ... N-1
    - Consider split  $t_i = (v_i + v_{i+1}) / 2$
    - Compute classification error for treshold split  $h_j(\mathbf{x}) >= \mathbf{t}_i$
  - Chose the t with the lowest classification error



# Logistic regression

Feature	Value	Weight Learned
h <sub>0</sub> ( <b>x</b> )	1	0.22
h <sub>1</sub> ( <b>x</b> )	<b>x</b> [1]	1.12
h <sub>2</sub> ( <b>x</b> )	<b>x</b> [2]	-1.07



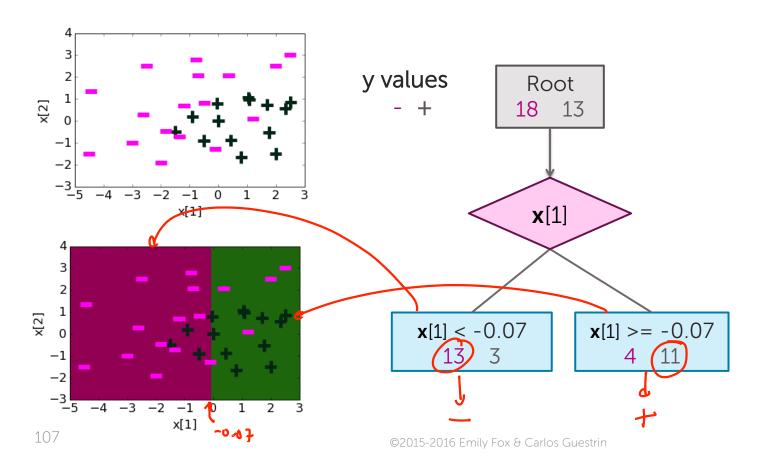


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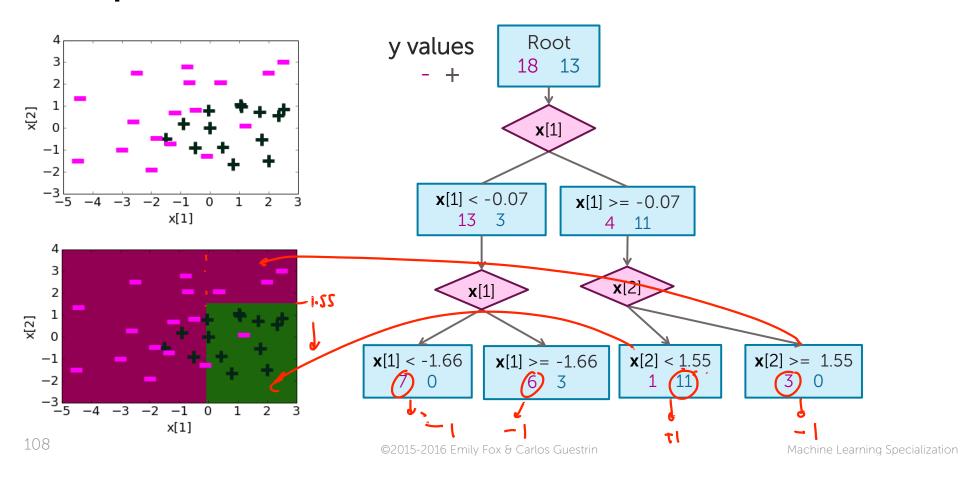
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# Depth 1: Split on x[1]

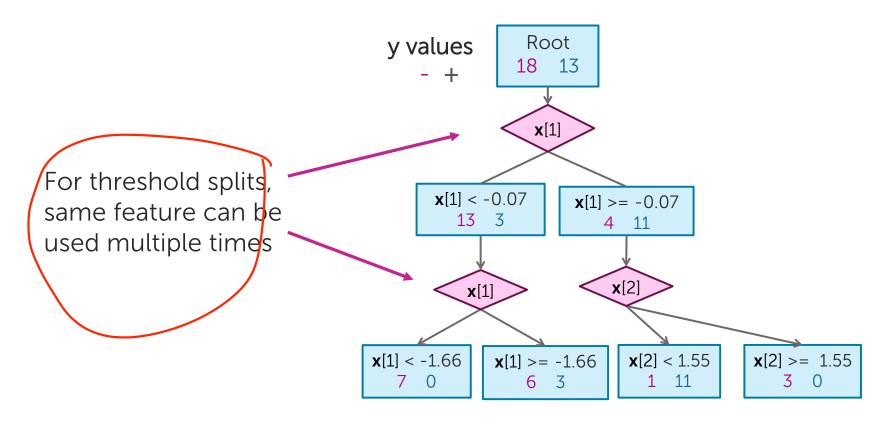


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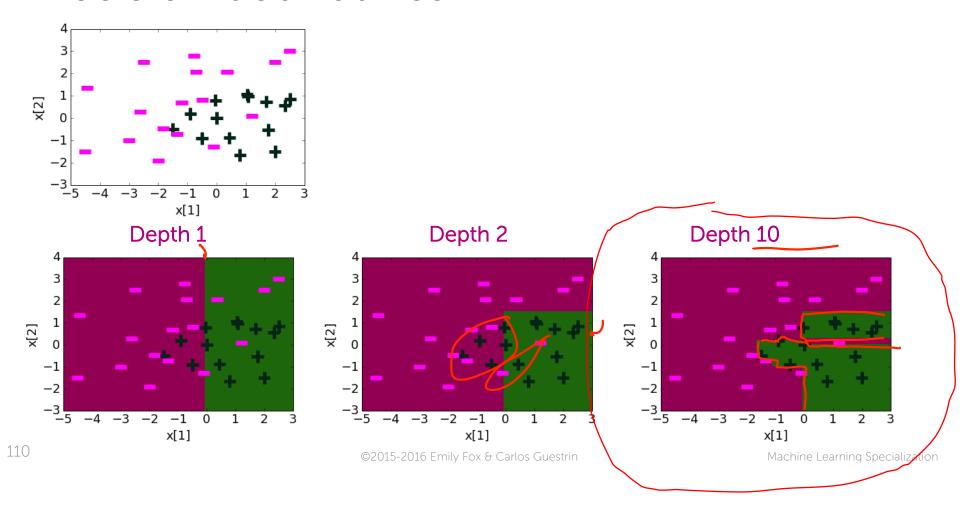
# Depth 2



# Threshold split caveat

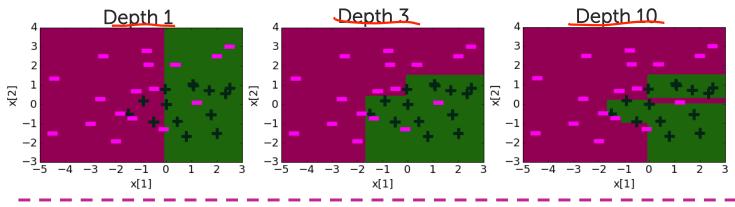


#### **Decision boundaries**

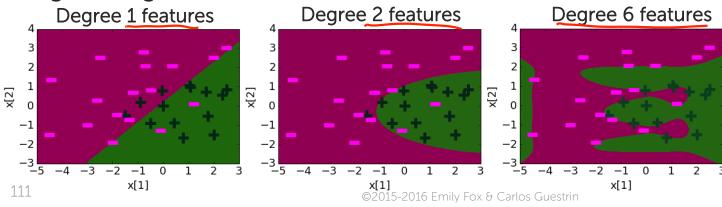


## Comparing decision boundaries

#### **Decision Tree**



#### **Logistic Regression**



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# Summary of decision trees

#### What you can do now

- Define a decision tree classifier
- Interpret the output of a decision trees
- Learn a decision tree classifier using greedy algorithm
- Traverse a decision tree to make predictions
  - Majority class predictions
  - Probability predictions
  - Multiclass classification

## Thank you to Dr. Krishna Sridhar



Dr. Krishna Sridhar Staff Data Scientist, Dato, Inc.