

$$\bar{\sigma} = 2\bar{\epsilon}_{zz} \left[C_{13}(s_{ij}) (g(s_{ij}) \frac{I_1[V_F]/V_F}{\hat{E}(s_{ij}) I_0[V_F] - 2I_1[V_F]/V_F} - \frac{1}{2}) + \frac{C_{33}(s_{ij})}{2} + f_1(s_{ij}) f_2(c, \tau) \frac{I_0[V_F] - 2I_1[V_F]/V_F}{2(\hat{E}(s_{ij}) I_0[V_F] - I_1[V_F]/V_F)} \right]$$

$$1. \bar{\epsilon}_{zz} = 1 - e^{-s t_0} / s^2, \quad \epsilon_0 = \dot{\epsilon} t_0$$

$$2. \begin{bmatrix} s_{rr} & s_{r\theta} & s_{rz} \\ s_{r\theta} & s_{rr} & s_{rz} \\ s_{rz} & s_{rz} & s_{zz} \end{bmatrix} \quad s_{rr} = \frac{1}{E_{rr}}, \quad s_{r\theta} = -\frac{\nu_{r\theta}}{E_{rr}}, \quad s_{rz} = -\frac{\nu_{rz}}{E_{rr}},$$

$$s_{zz} = \frac{1}{E_{zz}}$$

$$3. C_{13}(s_{ij}) = \frac{s_{rz}}{\alpha(s_{ij})}, \quad C_{33} = -\frac{s_{rr} + s_{r\theta}}{\alpha(s_{ij})}, \quad \alpha(s_{ij}) = 2s_{rz}^2 - s_{zz}s_{r\theta} - s_{rr}s_{zz}$$

$$4. g(s_{ij}) = \frac{(2s_{rz} + s_{zz})(s_{rr} - s_{r\theta})}{\alpha(s_{ij})}$$

$$5. f_1(s_{ij}) = -\frac{(2s_{rz} + s_{zz})}{2} \frac{2(s_{rr}s_{zz} - s_{rz}^2)}{\alpha(s_{ij})}$$

$$6. f_2(c, \tau) = 1 + c \ln \frac{1 + s\tau_2}{1 + s\tau_1}$$

$$7. \hat{E} = -\frac{2(s_{rr}s_{zz} - s_{rz}^2)}{\alpha(s_{ij})}$$

$$8. f = \frac{\sigma_0^2 s}{E k f_2(c, \tau)}$$

$\bar{\sigma}$ - Laplace transform of the average axial stress

$\bar{\varepsilon}_{zz}$ - Laplace transform of the axial strain

$E_{rr}, \nu_R, t_g = r_0^2 / E_K, C, \tilde{\varepsilon}_1, \tilde{\varepsilon}_2$ - unknown material parameters to be determined by the experiment fitting

$\mathcal{L}^{-1}(\bar{\sigma})$ - inverted $\bar{\sigma}$ in time domain

I_0 and I_1 - 1st and 2nd-order modified Bessel functions