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Name: David Wang

Signature: David Wang

Note: 14 questions on both sides, maximum 100 points.

1. [5 points] Let f be an image and g be a Gaussian filter. When we compute x image gradient, why do we want to apply Gaussian filter first, i.e., $\frac{\partial}{\partial x}(f * g)$?

Applying a Gaussian filter first allows us to reduce noise and remove unwanted details and textures, smoothing the image out.

2. [5 points] Let f be an image and g be a Gaussian filter. When we compute x gradient, why can we first compute $\frac{\partial}{\partial x}g$ and then convolve an image f with $\frac{\partial}{\partial x}g$? What are the advantages?

An advantage of computing and then convolving is that we would save a step compared to convolving an image with g and then taking the derivative of the image. We are allowed to do this because convolution is associative.

3. [5 points] Let f be an image and g be a Gaussian filter. When we find the zero crossing on the x image gradient, why can we convolve an image f with $\frac{\partial^2}{\partial x^2}g$ directly? What are the advantages?

4. [5 points] Canny edge detector. Which of the following statement is true? Explain your answers for full credits.
- a. Non-maximum suppression is used to select a pixel that is close to the true edge
 - b. The edges found by a Canny edge detector are determined by the Gaussian kernel scale
 - c. In hysteresis process, we start with low thresholds and then high thresholds
 - d. a, b and c are correct
 - e. a and b are correct

The answer is **e**: a and b are correct. c is false since with the hysteresis process we start with high then low thresholds, thus d is false as well since it assumes c is true. a and b are both true, therefore the answer is e.

5. [10 points] For Harris point detector, the second moment matrix at a pixel p is computed by $M = \begin{bmatrix} I_x^2 & I_x I_y \\ I_y I_x & I_y^2 \end{bmatrix}$ where I_x, I_y are x and y image gradients. Let the first and second eigenvalues of M be $\lambda_1, \lambda_2, \lambda_1 \geq \lambda_2$. Explain why the eigenvalues can tell us the whether we find an edge, corner, or flat region at pixel p ?

If the eigenvalues are $\lambda_2 \gg \lambda_1$ or $\lambda_1 \gg \lambda_2$ then there will be an edge at pixel p .

If the eigenvalues of λ_1 or λ_2 are large and not close to zero, then it is a corner at pixel p .

If the eigenvalues are close to zero, then there will be a flat region at pixel p .

6. [10 points] For Harris point detector, the corner response $R = \det(M) - 0.04 \operatorname{tr}(M)$ where \det and tr are the determinant and trace of a matrix. For a point where $M = \begin{bmatrix} I_x^2 & I_x I_y \\ I_y I_x & I_y^2 \end{bmatrix} = \begin{bmatrix} 0.8 & 0.2 \\ 0.2 & 0.9 \end{bmatrix}$ where I_x, I_y are x and y image gradients, is this point on an edge? a corner? or a flat region?

$$R = \det(M) - 0.04 \operatorname{tr}(M)$$

$$\det(M) = \lambda_1 \lambda_2 = (0.8)(0.9) = 0.72$$

$$\operatorname{tr}(M) = \lambda_1 + \lambda_2 = (0.8) + (0.9) = 1.7$$

$$R = 0.72 - 0.04(1.7) = 0.652$$

The point is not on an edge, since R is not less than 0. R is close to 0, so it is a **flat region**.

7. [5 points] Hough transform. Given one points $(x, y) = (2, 6)$ in the image plane, write down the corresponding line in the Hough parameter space (describe a line in terms of m and b , your

answer should be $m = \underline{\hspace{1cm}}$).

Haugh Space: $m = (-1/x)b + (y/x)$

Plugging in the point $(2, 6)$ should give $m = (-1/2)b + 3$

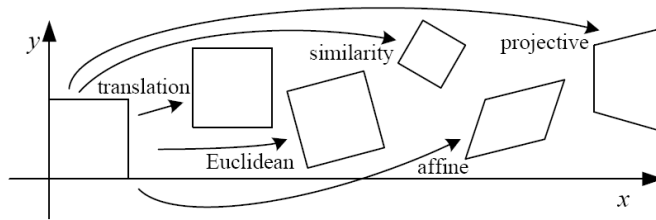
8. [5 points] Which of the following statements regarding line fitting is true?
- a. Line fitting with least squares minimization gives a closed form solution.
 - b. Line fitting with least squares minimization is not sensitive to outliers.
 - c. Hough transform can be efficiently applied to model fitting with a large number of parameters.
 - d. Model fitting with RANSAC does not the same answer every time.
 - e. a and d are correct

The answer is e : a and d

9. [5 points] Which of the following statements is true when we use RANSAC to fit data points with an objective function?
- a. Applicable to an objective function with more parameters than the Hough transform
 - b. Optimization parameters are easier to choose than Hough transform
 - c. Computational time grows quickly with fraction of outliers
 - d. Not good for getting multiple fits
 - e. a, b, and d are correct

The answer is e: a, b and d are correct.

10. [5 points] Which of the following statements regarding 2D transformation are correct?

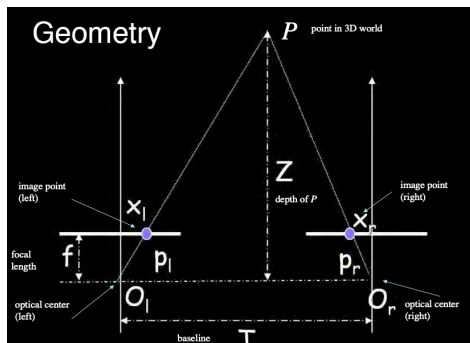


- a. Euclidean transformation has 3 parameters
- b. Similarity transformation has 4 parameters
- c. Affine transformation has 6 parameters
- d. a, b, and c are true
- e. a and c are true

The answer is **d**: since a, b, and c are all true.

11. [10 points] Given a pair of stereo images. Show every step on how to compute depth $Z =$

$$f \frac{T}{x_r - x_l}$$



Disparity is represented by $x_r - x_l$

Assuming that the axes are parallel, we can assume that the triangles formed by (p_l, P, p_r) , and (O_l, P, O_r) are similar triangles.

Since they are similar triangles we can set them equal to each other

$$\frac{T + (x_l - x_r)}{Z - f} = \frac{T}{Z}$$

solving for Z gives us

$$Z = f \frac{T}{x_r - x_l}$$

12. [10 points] Which of the following statements are true? Explain your answers.

- a. Given a pair of images from a calibrated stereo camera, for each pixel in one image, we can use the essential matrix to compute the corresponding epipolar line in the other image
- b. Give a pair of images from an uncalibrated stereo camera, for each pixel in one image, we can use the essential matrix to compute the corresponding epipolar line in the other image.
- c. Epipolar lines are always horizontal lines on an image
- d. When we use larger window for search correspondence, we can capture more details
- e. a and c are correct

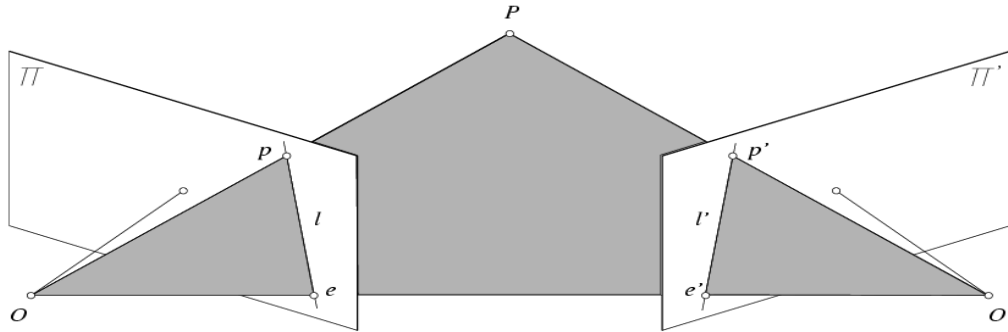
The answer is a. b is false because it should be a calibrated stereo camera, using an essential matrix. c is false because epipolar lines are horizontal after rectifying, therefore they are not always horizontal. A smaller window is required for capturing more details therefore d is false as well. Thus, e is false since c is not correct.

13. [10 points] Given a pair of left and right images for a calibrated stereo camera, which of the following statements for the calibrated stereo camera are true? Explain your answers.

- a. Given one point in one image, the corresponding point in the second image of a stereo pair is on a line passing through its epipole.
- b. We can use the essential matrix to map a point in the left image to a line in the right image.
- c. Depth is inversely proportional to disparity
- d. a and c are correct
- e. a, b and c are correct

The answer is e. Essential matrices allow you to map a point from one image to a line in another image, so b is true. d is false since b is true. c is true because the equation for depth has disparity in the denominator thus it is inversely proportional.

14. [10 points] Epipolar geometry. Given a point P in the world coordinate with two mapped points p and p' on two image planes with two optical centers O and O' . Derive the following equations.



$$\vec{Op} \cdot [\vec{OO'} \times \vec{O'p'}] = 0$$

Explain every step (what does the cross product of two vectors do and what does the inner product of two vectors do?) to earn full credit.

The cross product, N , of vectors OO' and $O'p'$ gives a surface perpendicular to the plane $OO'p'$, and the inner product of vector Op and the cross product N gives 0 since they are perpendicular to each other.