

# LAB 5a

Rules:

$R_0: S_1(a, b, c, d, e) :- S_0(a, b, c, d, e)$

$R_1: S_1(a, b, c, d, e) :- S_2(b, c, d, e, a)$

$R_2: S_2(a, b, c, d, e) :- S_1(b, c, d, e, a)$

$R_3: S_1(a, b, c, d, e) :- S_1(b, a, c, d, e)$

$R_4: S_3(a, f, b, g, c, h, d, i) :- S_1(a, b, c, d, e), S_2(f, g, h, i, j)$

$R_5: S_4(a, b, c, d, e) :- S_3(a, b, z, y, c, d, e, i), S_5(m, n, x, y, z)$

$R_6: S_5(a, a, c, d, e) :- S_4(a, b, c, d, e), S_5(a, w, x, y, z)$

$R_7: S_5(a, b, c, d, e) :- S_5(e, a, b, c, d)$

Dependency graph

Output

$R_0:$

$R_1, R_2$

$R_2: R_0, R_1, R_3$

$R_3: R_0, R_1$

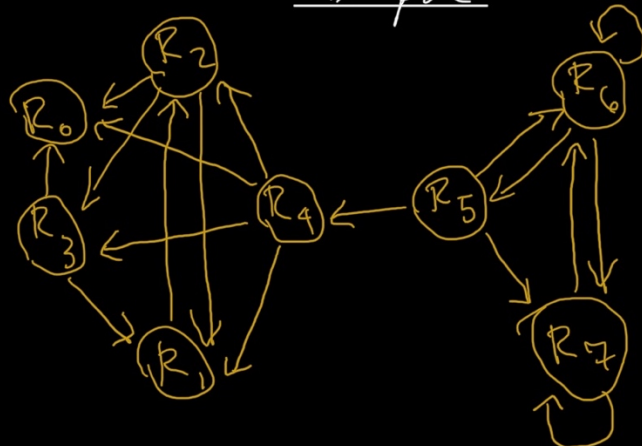
$R_4: R_0, R_1, R_2, R_3$

$R_5: R_4, R_6, R_7$

$R_6: R_5, R_6, R_7$

$R_7: R_6, R_7$

Graph



# Reverse Dependency graph

## Output

$R_0: R_2, R_3, R_4$

$R_1: R_3, R_4$

$R_2: R_1, R_4$

$R_3: R_2, R_4$

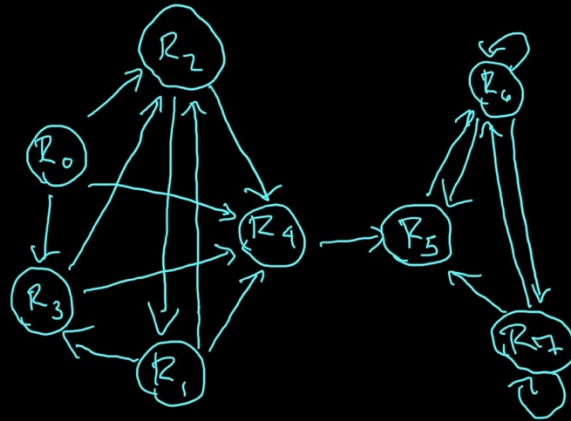
$R_4: R_5$

$R_5: R_6$

$R_6: R_5, R_6, R_7$

$R_7: R_5, R_6, R_7$

## Graph



## DFS on Reverse Dependency Graph

### Postorder List

$[R_0, R_2, R_1, R_3]$

$[R_0, R_2, R_1, R_3, R_4, R_5, R_6]$

$[R_0, R_2, R_1, R_3, R_4, R_5, R_6, R_7]$

### Visited Adj. List

$R_0: R_2, R_3, R_4$

$R_1: R_3, R_4$

$R_2: R_1, R_4$

$R_3: R_2, R_4$

$R_4: R_5$

$R_5: R_6$

$R_6: R_5, R_6, R_7$

$R_7: R_5, R_6, R_7$

### Stack

~~$R_0$~~

~~$R_2$~~

~~$R_1$~~

~~$R_3$~~

~~$R_4$~~

~~$R_5$~~

~~$R_6$~~

~~$R_7$~~

### DFS Forest



# DFS on Reverse of Post Order to get SCCs

Postorder list	Visited Adj List	Stack	DFS forest
$[R_0, R_2, R_1, R_3, R_4, R_5, R_6, R_7]$	✓ $R_0$ :	<del><math>R_7</math></del>	$(R_7)$
$[R_0, R_2, R_1, R_3, R_4, R_5, R_6, R_7]$	✓ $R_1$ : $R_2$	<del><math>R_6</math></del>	$(R_7) \rightarrow (R_6)$
$[R_0, R_2, R_1, R_3, R_4, R_5, R_6, R_7]$	✓ $R_2$ : $R_0, R_1, R_3$	<del><math>R_5</math></del>	$(R_7) \rightarrow (R_6) \rightarrow (R_5)$
$[R_0, R_2, R_1, R_3, R_4, R_5, R_6, R_7]$	✓ $R_3$ : $R_0, R_1$	<del><math>R_4</math></del>	$(R_7) \rightarrow (R_6) \rightarrow (R_5) \rightarrow (R_4)$
$[R_0, R_2, R_1, R_3, R_4, R_5, R_6, R_7]$	✓ $R_4$ : $R_0, R_1, R_2, R_3$	<del><math>R_3</math></del>	$(R_7) \rightarrow (R_6) \rightarrow (R_5) \rightarrow (R_4) \rightarrow (R_0)$
$[R_0, R_2, R_1, R_3, R_4, R_5, R_6, R_7]$	✓ $R_5$ : $R_4, R_6, R_7$	<del><math>R_2</math></del>	$(R_7) \rightarrow (R_6) \rightarrow (R_5) \rightarrow (R_4) \rightarrow (R_0) \rightarrow (R_3)$
$[R_0, R_2, R_1, R_3, R_4, R_5, R_6, R_7]$	✓ $R_6$ : $R_5, R_6, R_7$	<del><math>R_1</math></del>	$(R_7) \rightarrow (R_6) \rightarrow (R_5) \rightarrow (R_4) \rightarrow (R_0) \rightarrow (R_3) \rightarrow (R_1)$
$[R_0, R_2, R_1, R_3, R_4, R_5, R_6, R_7]$	✓ $R_7$ : $R_6, R_7$	<del><math>R_0</math></del>	$(R_7) \rightarrow (R_6) \rightarrow (R_5) \rightarrow (R_4) \rightarrow (R_0) \rightarrow (R_3) \rightarrow (R_1) \rightarrow (R_2)$

## SCCs

SCC1:  $R_7, R_6, R_5, R_4, R_0$

SCC2:  $R_3$

SCC3:  $R_1, R_2$

\* The colors of the SCC's correspond to the colors on the image below

