

# TraceDiff: Debugging Unexpected Code Behavior Using Trace Divergences

Ryo Suzuki, Gustavo Soares, Andrew Head, Elena Glassman,  
Ruan Reis, Melina Mongiovi, Loris D'Antoni, Björn Hartmann



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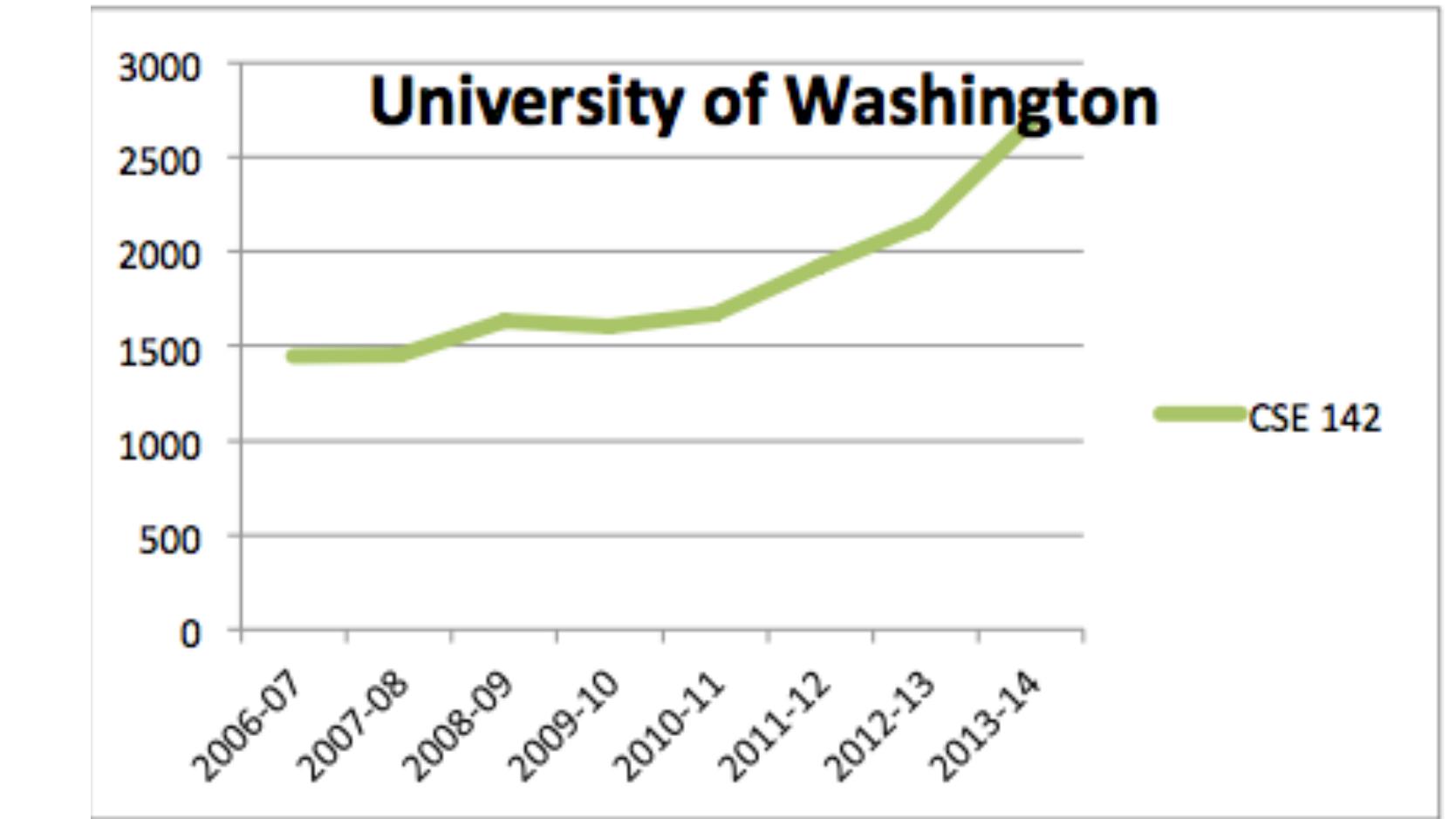
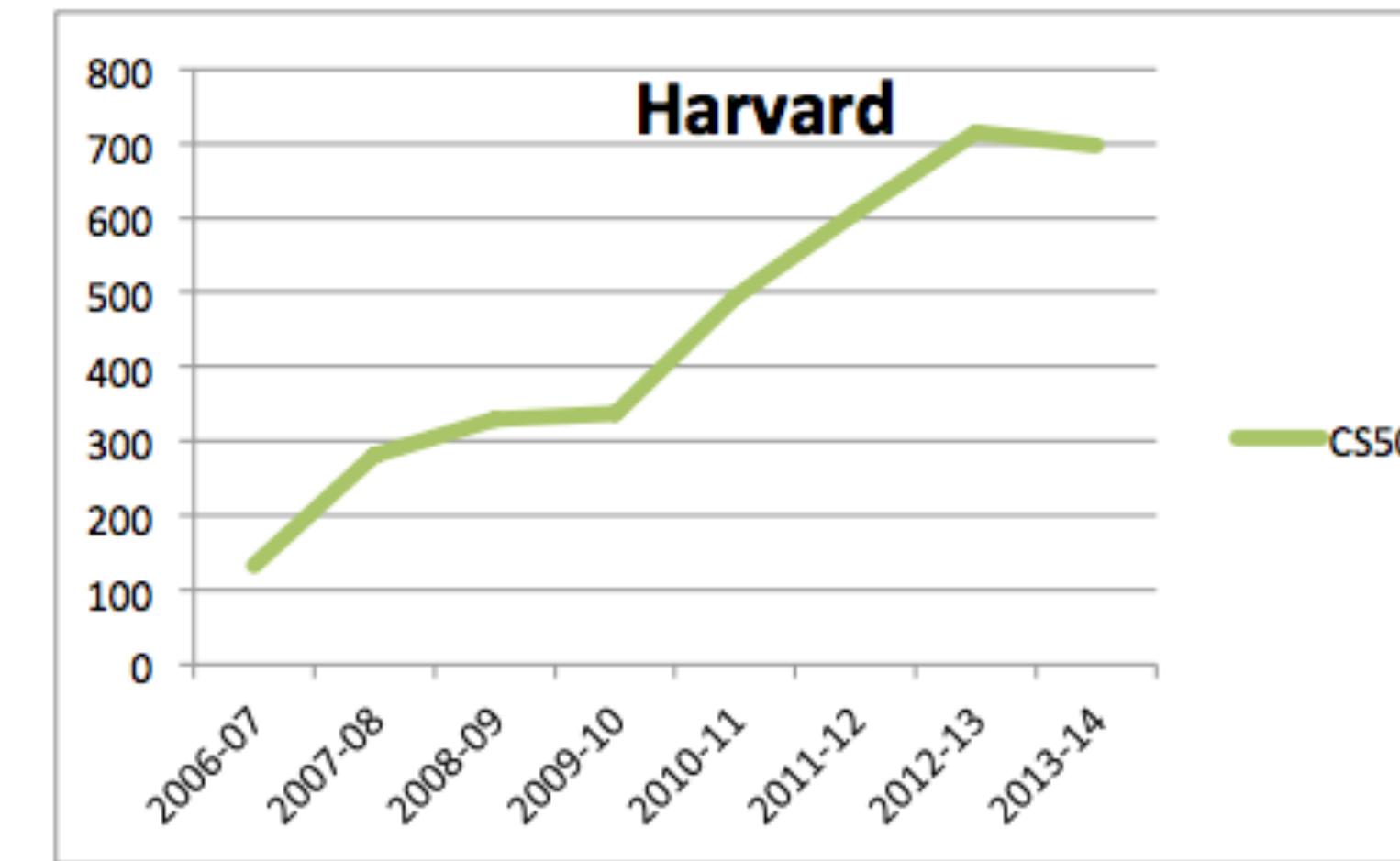
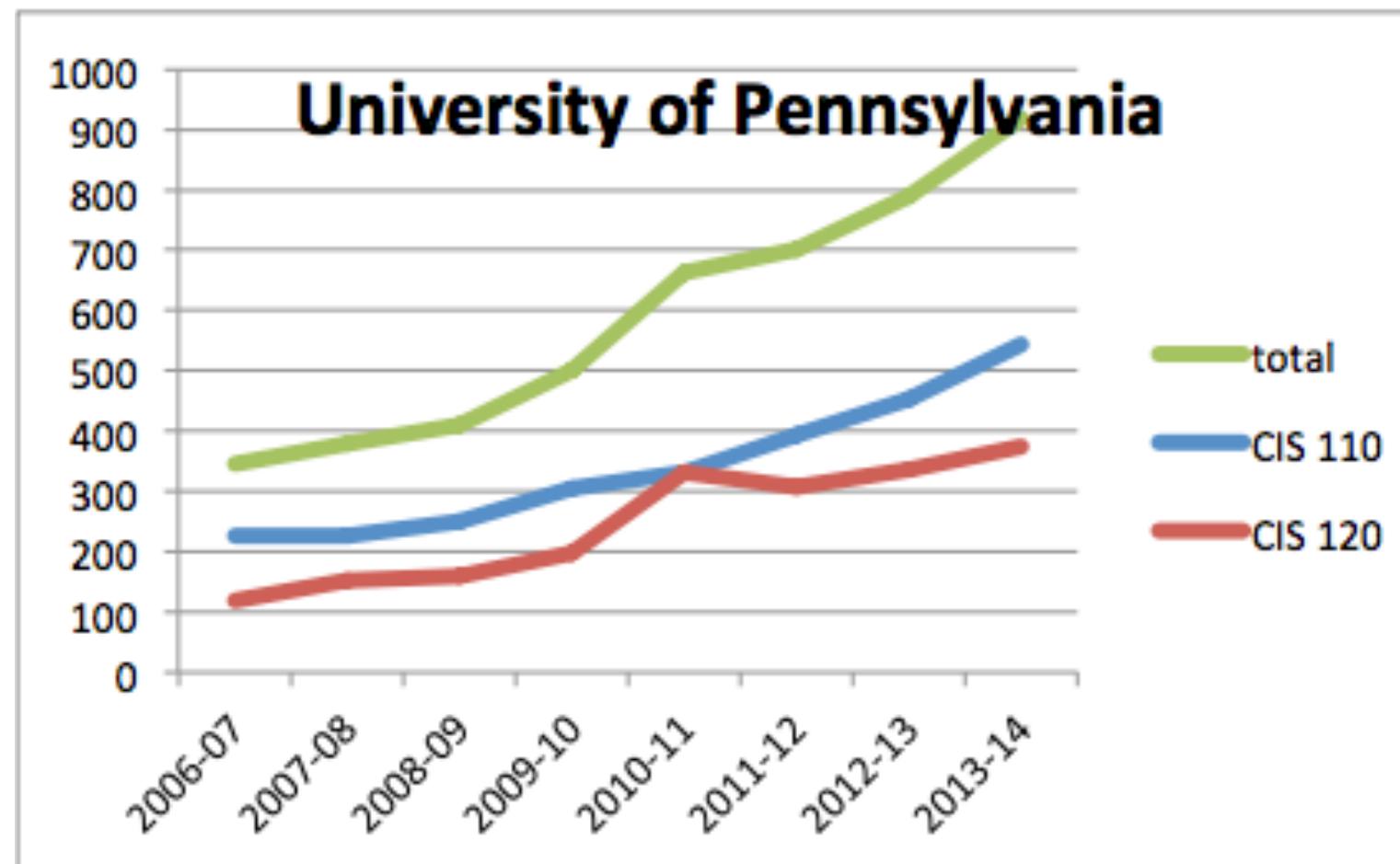
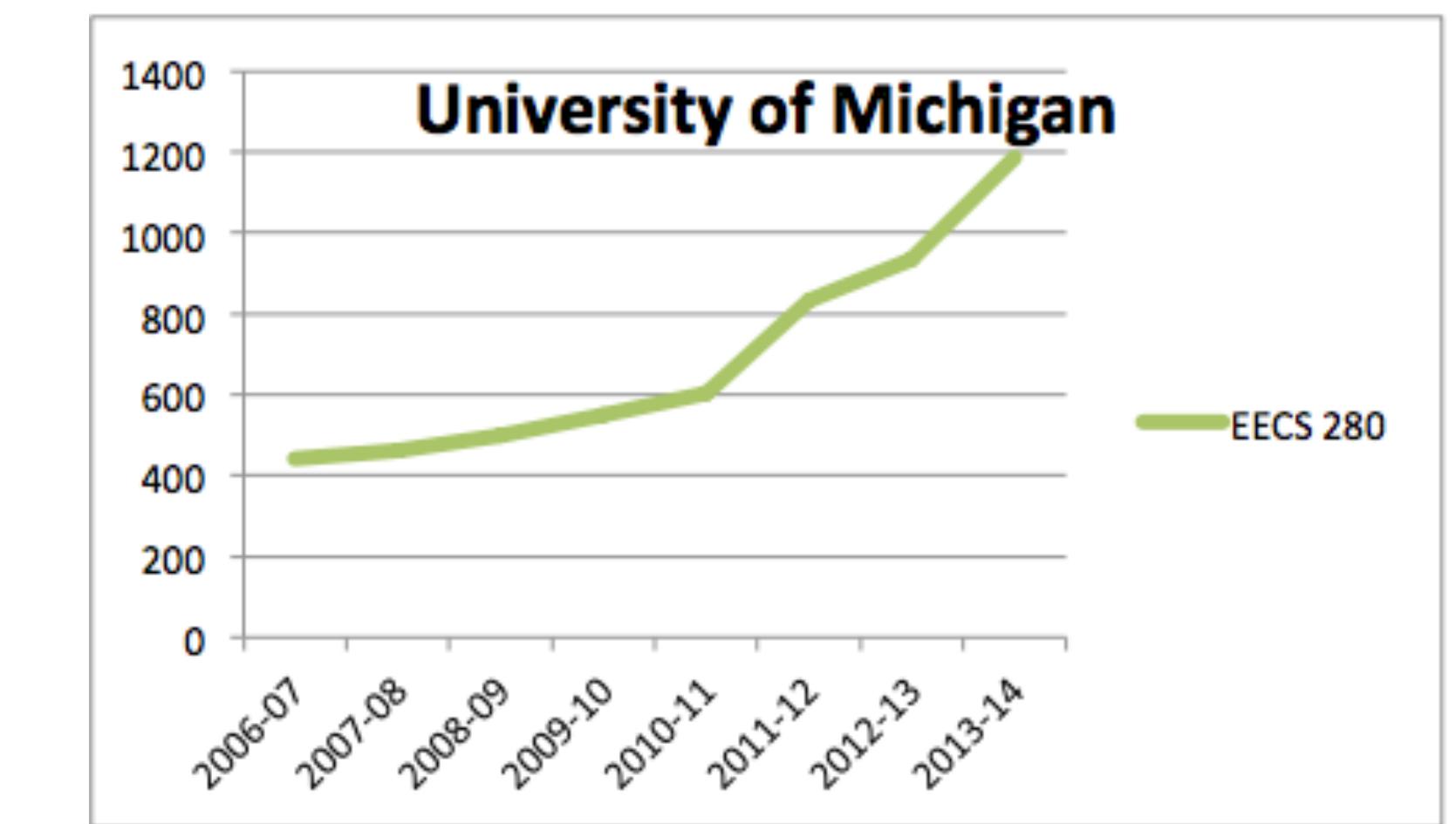
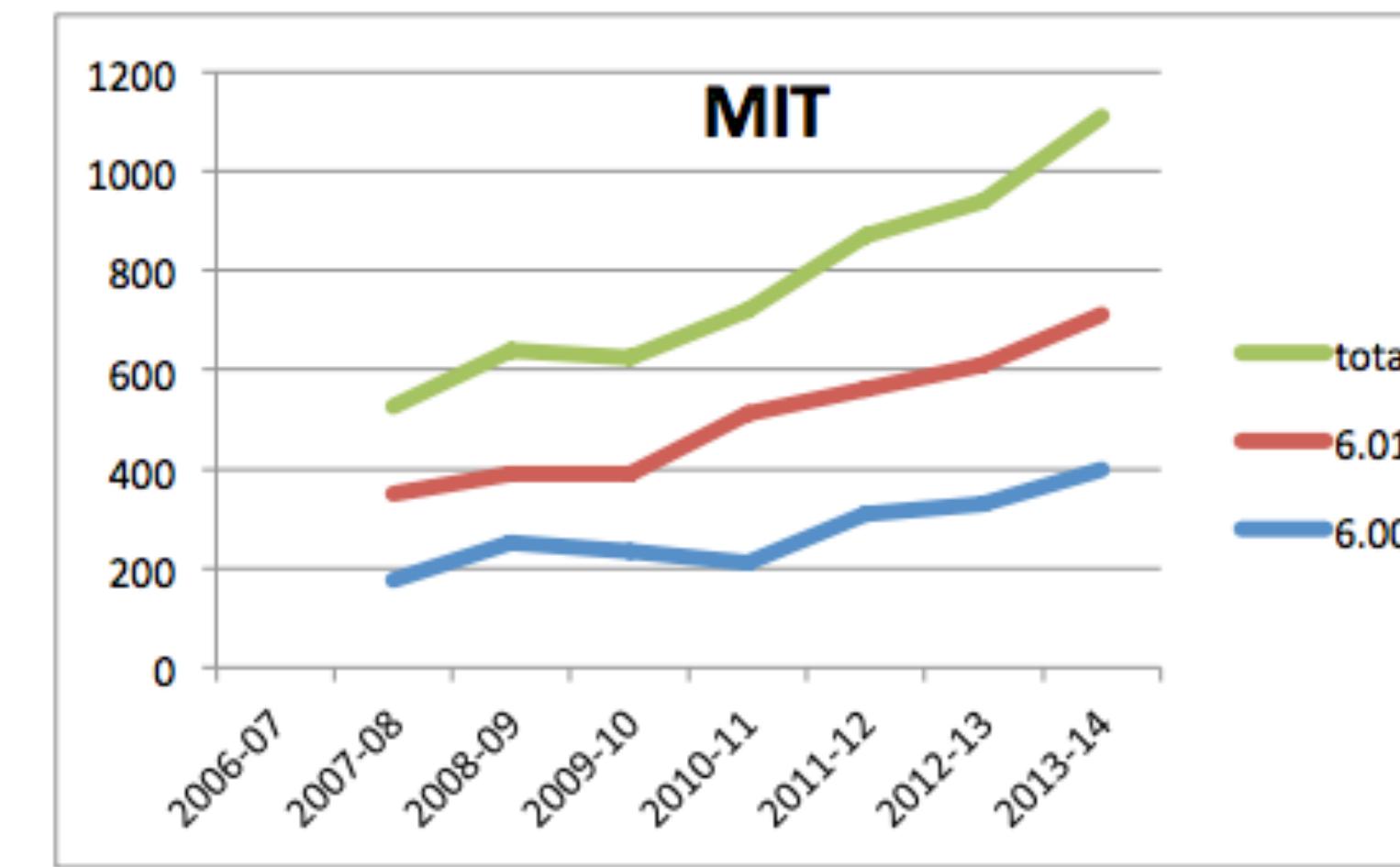
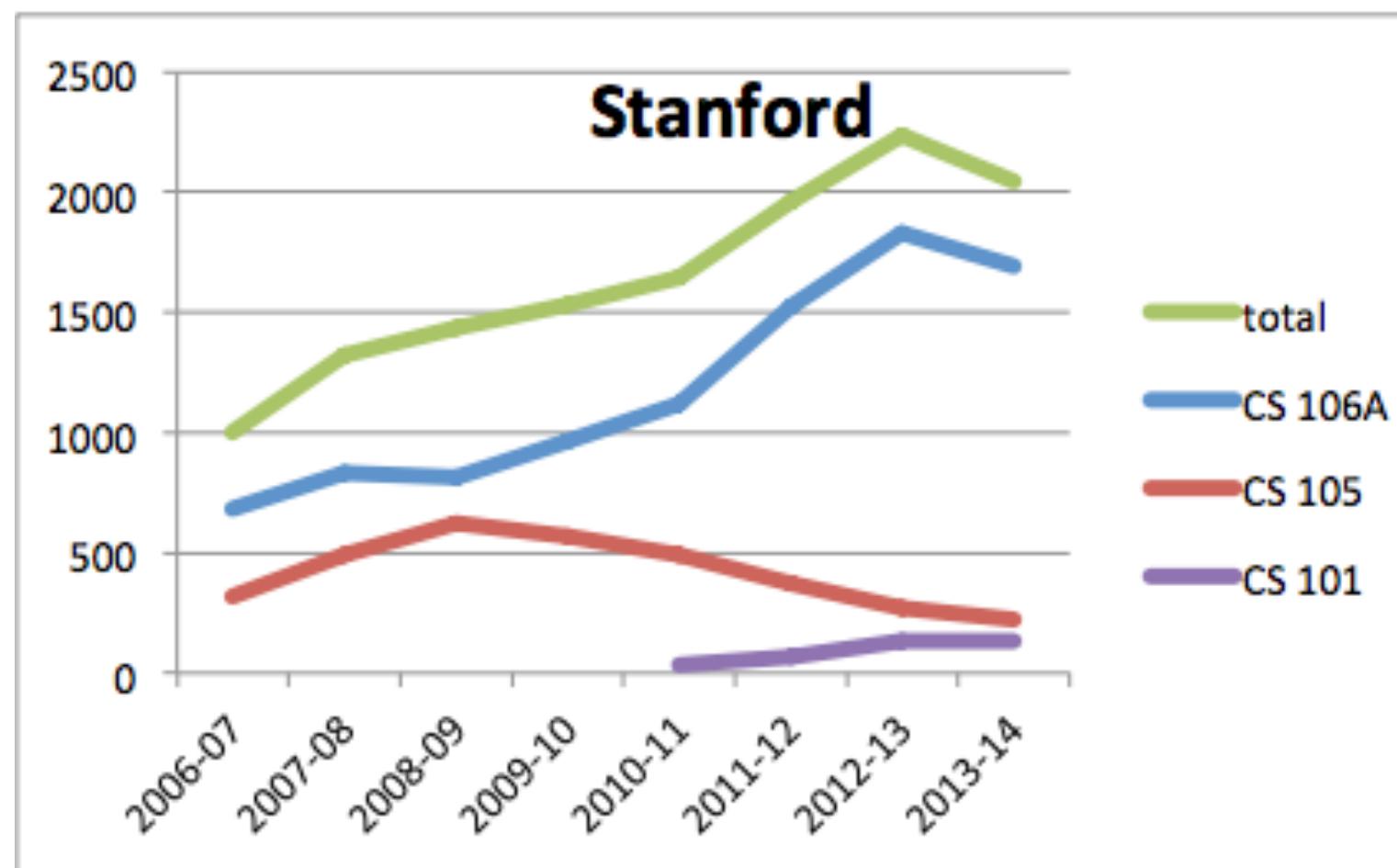


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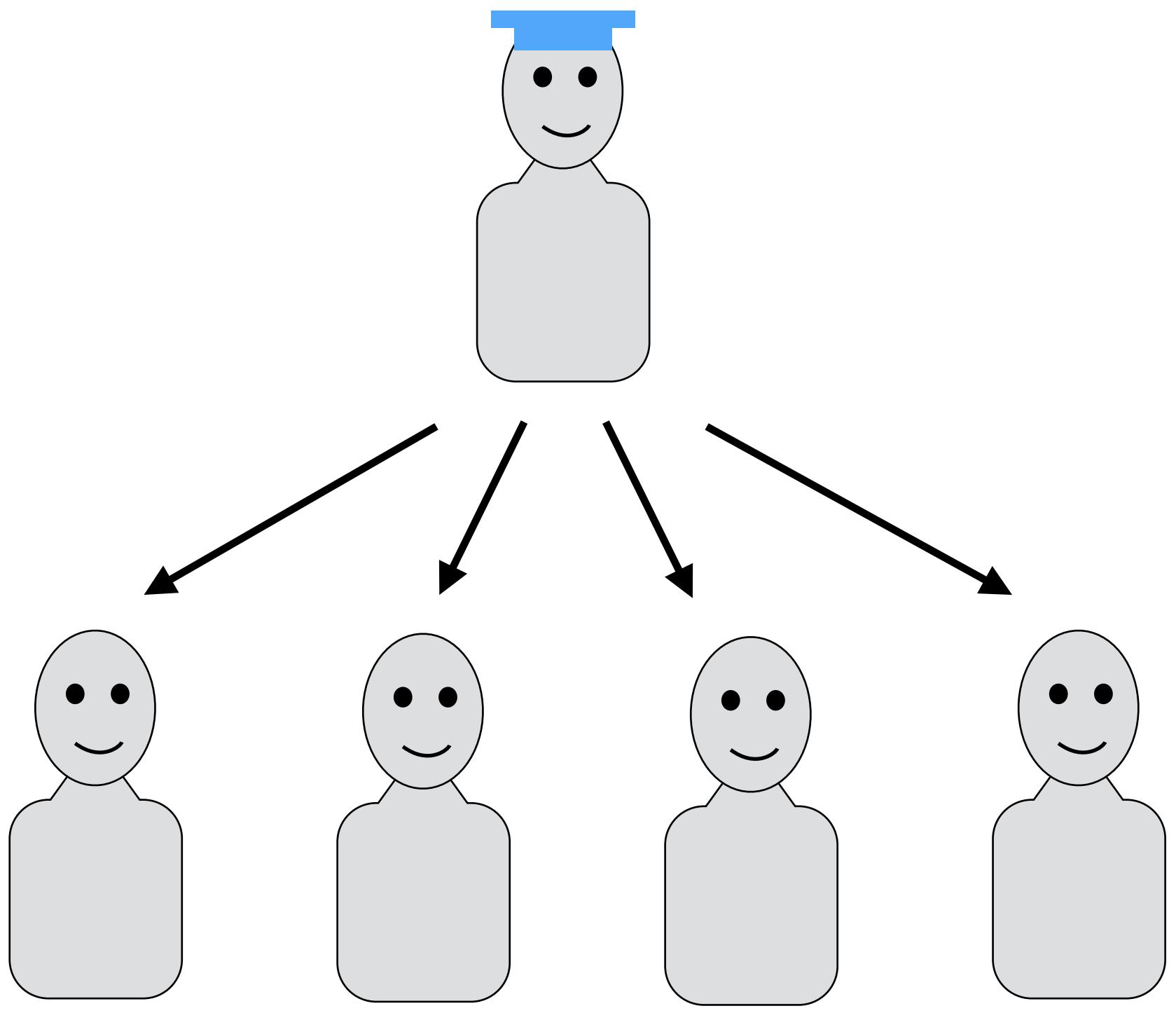


WISCONSIN  
UNIVERSITY OF WISCONSIN-MADISON

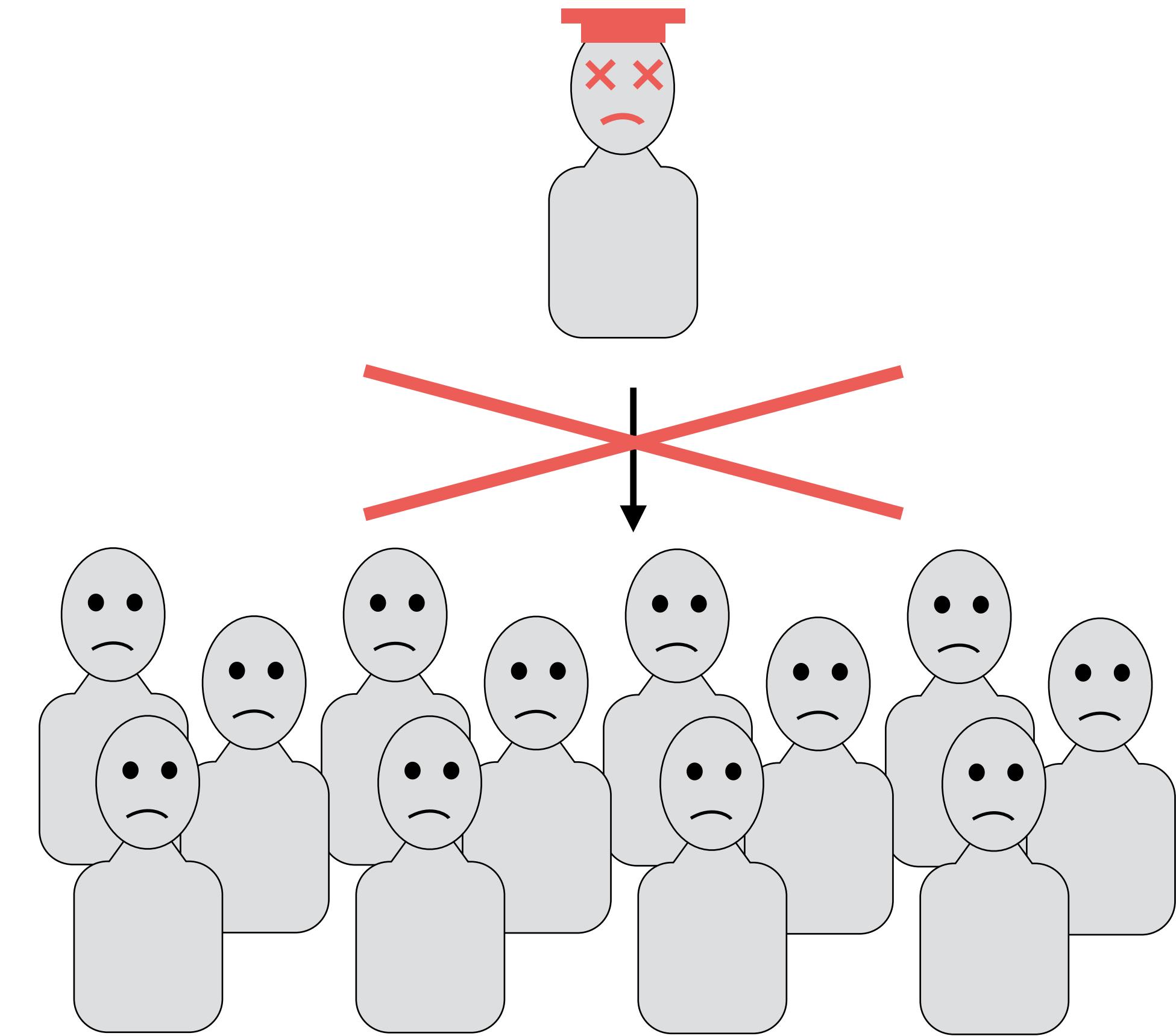
# Increasing Demand for Introductory CS Courses



# Teachers' Personalized Attention **Does Not Scale**

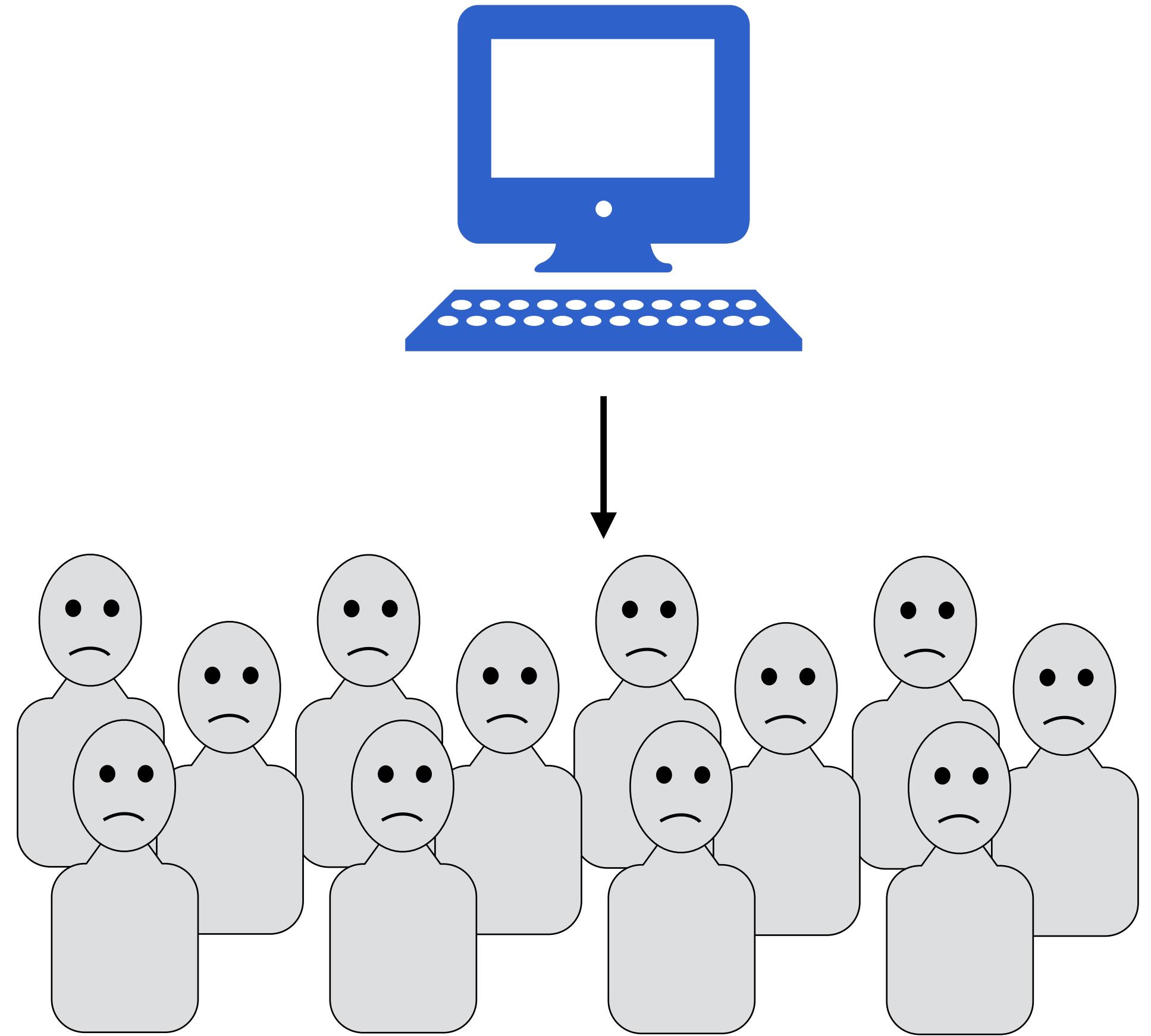


**Traditional** Classroom



**Massive** Classroom  
(1,000-2,000 students)

# Automatic Programming Feedback



**Massive** Classroom  
(1,000-2,000 students)

## Code

```
def accumulate(combiner, base, n, term):  
    if n == 1:  
        if n == 0:  
            return base  
    else:  
        return combiner(term(n),  
                         accumulate(..., n-1, ...))
```

---

```
>>> accumulate(add, 0, 5, identity)
```

```
15 # 0 + 1 + 2 + 3 + 4 + 5
```

```
>>> accumulate(mul, 2, 3, square)
```

```
72 # 2 * 1^2 * 2^2 * 3^2
```

## Code

```
def accumulate(combiner, base, n, term):  
    if n == 1:  
        if n == 0:  
            return base  
    else:  
        return combiner(term(n),  
                         accumulate(..., n-1, ...))
```

---

## Test Case Feedback

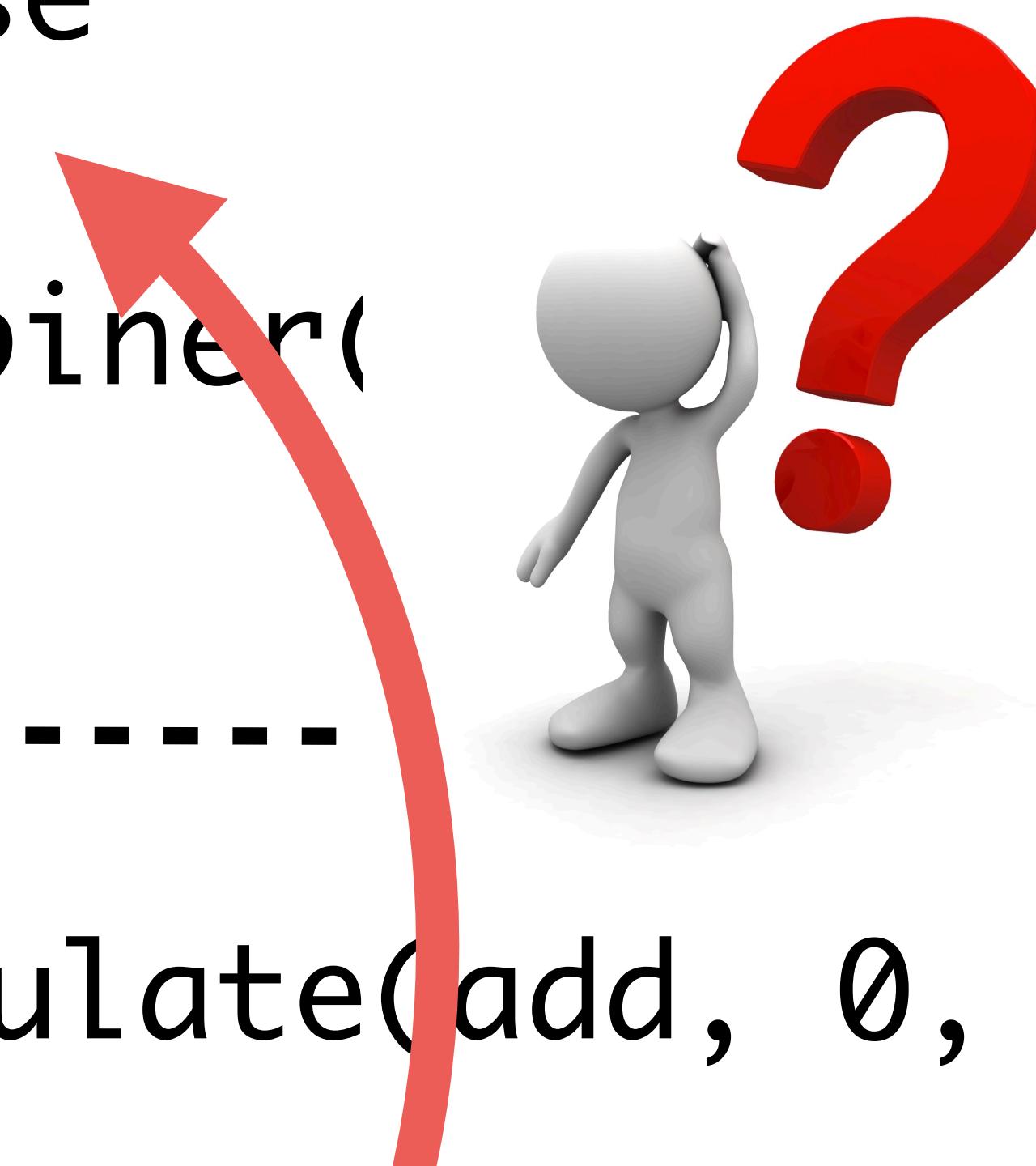
```
>>> accumulate(add, 0, 5, identity)  
x 14  
o 15
```

## Code

```
def accumulate(combiner, base, n, term):  
    if n == 1:  
        if n == 0:  
            return base  
    else:  
        return combiner(  
            e(..., n-1, ...))
```

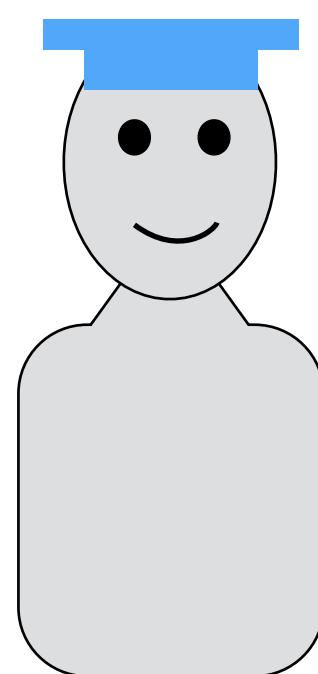
## Test Case Feedback

```
>>> accumulate(add, 0, 5, identity)  
x 14  
o 15
```



## Code

```
def accumulate(combiner, base, n, term):  
    if n == 1:  
        if n == 0:  
            return base  
    else:  
        return combiner(term(n),  
                         accumulate(..., n-1, ...))
```



accumulate(add, 0, 5, identity)

x 14 # 0 + 0 + 2 + 3 + 4 + 5

o 15 # 0 + 1 + 2 + 3 + 4 + 5

Python 2.7

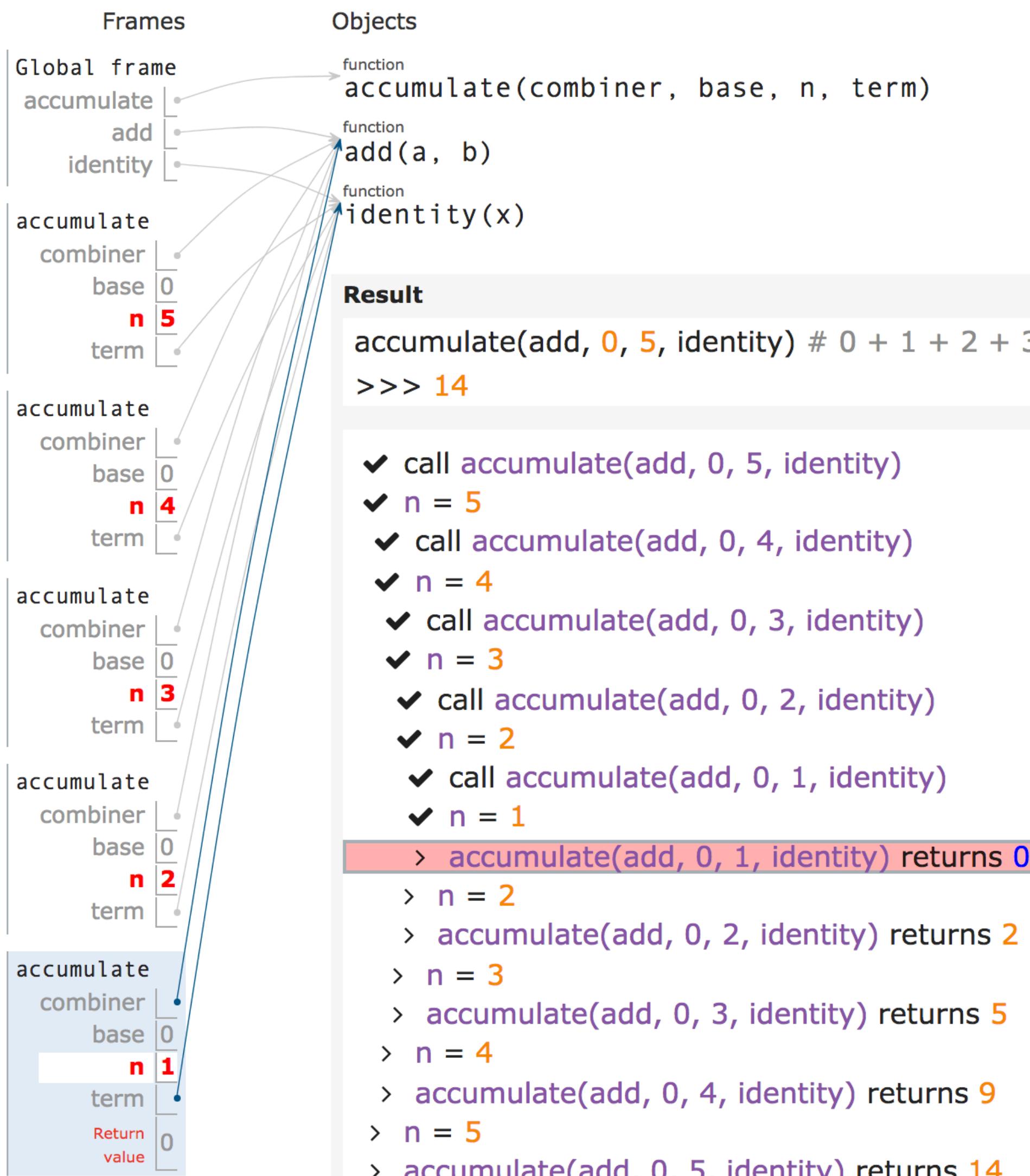
```

1 def accumulate(combiner, bas
→2 if n==1:
3     return base
4 else:
5     return combiner(term(n),
6
7 def add(a, b):
8     return a + b
9
10 def identity(x):
11     return x
12
13 accumulate(add, 0, 5, identi

```

line that has just executed  
next line to execute

< Back Step 32 of 48 Forward >



# TraceDiff

Python 2.7

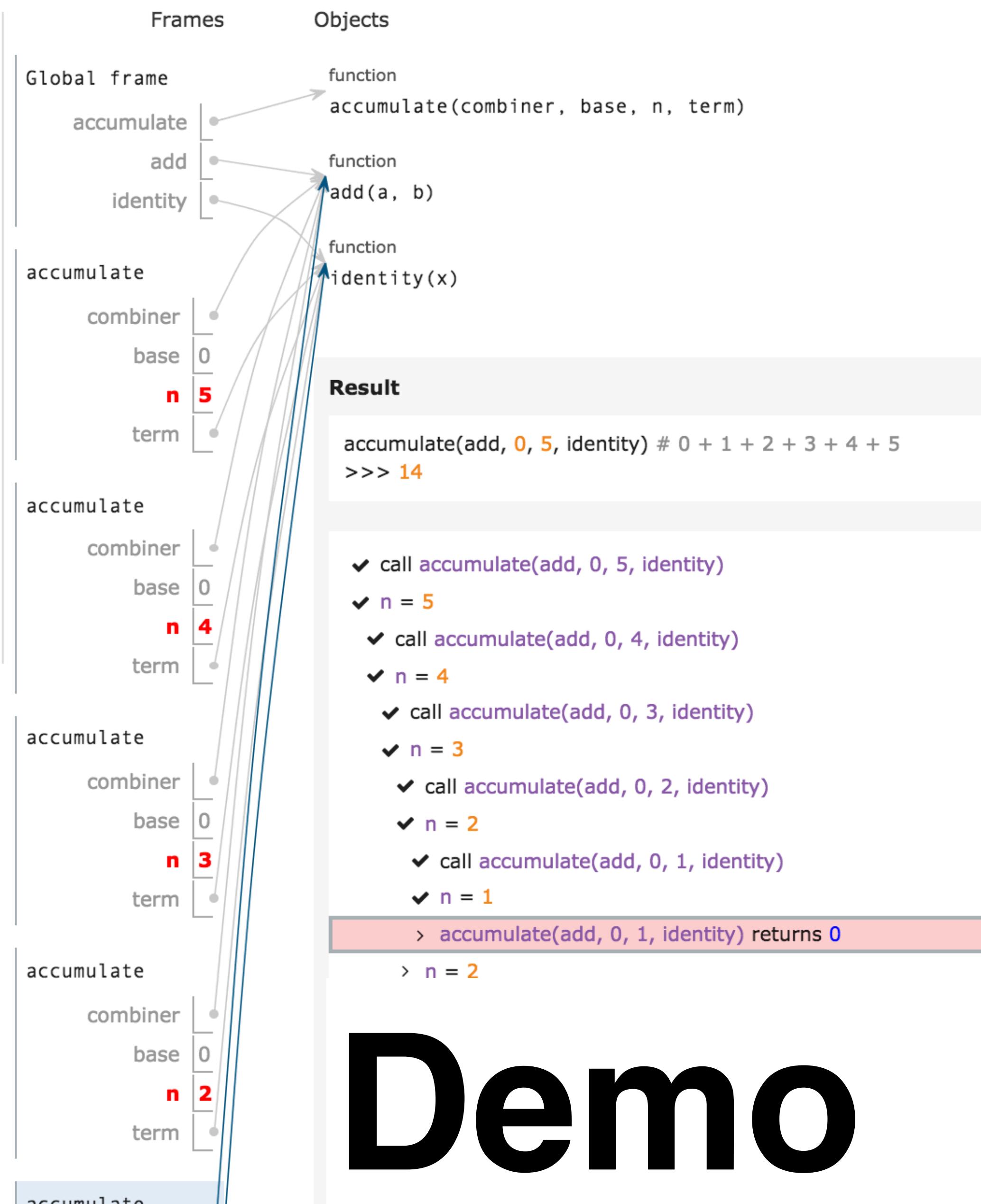
```
1 def accumulate(combiner, base, n, term):  
2     if n==1:  
3         return base  
4     else:  
5         return combiner(term(n), accumulate(  
6  
7 def add(a, b):  
8     return a + b  
9  
10 def identity(x):  
11    return x  
12  
13 accumulate(add, 0, 5, identity)
```

line that has just executed

next line to execute

< Back Step 32 of 48

Forward >



Expected

```
accumulate(add, 0, 5, identity) # 0 + 1 + 2 + 3 + 4 + 5  
>>> 15
```

- ✓ call accumulate(add, 0, 5, identity)
- ✓ n = 5
- ✓ call accumulate(add, 0, 4, identity)
- ✓ n = 4
- ✓ call accumulate(add, 0, 3, identity)
- ✓ n = 3
- ✓ call accumulate(add, 0, 2, identity)
- ✓ n = 2
- ✓ call accumulate(add, 0, 1, identity)
- ✓ n = 1

> call accumulate(add, 0, 0, identity)  
> n = 0  
> accumulate(add, 0, 0, identity) returns 0  
> n = 1  
> accumulate(add, 0, 1, identity) returns 1  
> n = 2  
> accumulate(add, 0, 2, identity) returns 3  
> n = 3

<https://ryosuzuki.github.io/trace-diff/?type=accumulate&id=10>

rns 6

### Result

```
accumulate(add, 0, 5, identity) # 0 + 1 + 2 + 3 +  
>>> 14
```

- ✓ call accumulate(add, 0, 5, identity)
- ✓ n = 5
- ✓ call accumulate(add, 0, 4, identity)
- ✓ n = 4
- ✓ call accumulate(add, 0, 3, identity)
- ✓ n = 3
- ✓ call accumulate(add, 0, 2, identity)
- ✓ n = 2
- ✓ call accumulate(add, 0, 1, identity)
- ✓ n = 1

> accumulate(add, 0, 1, identity) returns 0

- > n = 2
- > accumulate(add, 0, 2, identity) returns 2
- > n = 3
- > accumulate(add, 0, 3, identity) returns 5
- > n = 4
- > accumulate(add, 0, 4, identity) returns 9
- > n = 5
- > accumulate(add, 0, 5, identity) returns 14

### Expected

```
accumulate(add, 0, 5, identity) # 0 + 1 + 2 + 3 +  
>>> 15
```

- ✓ call accumulate(add, 0, 5, identity)
- ✓ n = 5
- ✓ call accumulate(add, 0, 4, identity)
- ✓ n = 4
- ✓ call accumulate(add, 0, 3, identity)
- ✓ n = 3
- ✓ call accumulate(add, 0, 2, identity)
- ✓ n = 2
- ✓ call accumulate(add, 0, 1, identity)
- ✓ n = 1

> call accumulate(add, 0, 0, identity)

- > n = 0
- > accumulate(add, 0, 0, identity) returns 0
- > n = 1
- > accumulate(add, 0, 1, identity) returns 1
- > n = 2
- > accumulate(add, 0, 2, identity) returns 3
- > n = 3
- > accumulate(add, 0, 3, identity) returns 6

# 1. Highlight Differences

Python 2.7

```
1 def accumulate(combiner, bas
→2   if n==1:
3     return base
4   else:
5     return combiner(term(n),
6
7 def add(a, b):
8   return a + b
9
10 def identity(x):
11   return x
12
13 accumulate(add, 0, 5, identi
```

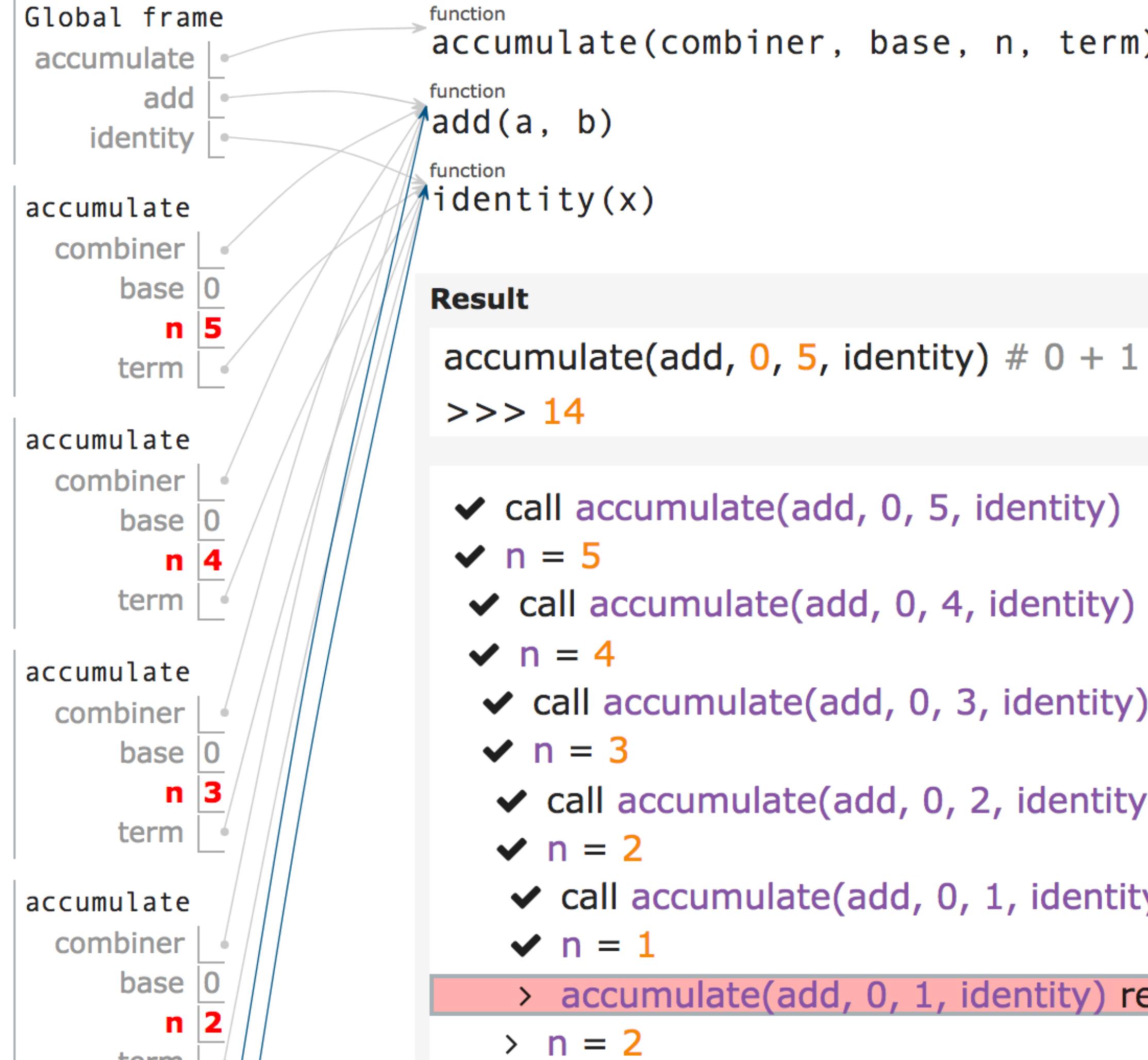
▶ line that has just executed

▶ next line to execute

< Back Step 32 of 48 Forward >

Frames

Objects



### Result

```
accumulate(add, 0, 5, identity) # 0 + 1 + 2 + 3 +
>>> 14
```

- ✓ call `accumulate(add, 0, 5, identity)`
  - ✓ `n = 5`
  - ✓ call `accumulate(add, 0, 4, identity)`
  - ✓ `n = 4`
  - ✓ call `accumulate(add, 0, 3, identity)`
  - ✓ `n = 3`
  - ✓ call `accumulate(add, 0, 2, identity)`
  - ✓ `n = 2`
  - ✓ call `accumulate(add, 0, 1, identity)`
  - ✓ `n = 1`
- > `accumulate(add, 0, 1, identity)` returns 0  
> `n = 2`

### Expected

```
accumulate(ac
>>> 15
```

- ✓ call `accum`
  - ✓ `n = 5`
  - ✓ call `accu`
  - ✓ `n = 4`
  - ✓ call `accu`
  - ✓ `n = 3`
  - ✓ call `accu`
  - ✓ `n = 2`
  - ✓ call `acc`
  - ✓ `n = 1`
- > call `ac`  
> `n = 0`

## 2. Interactively Explore

Return

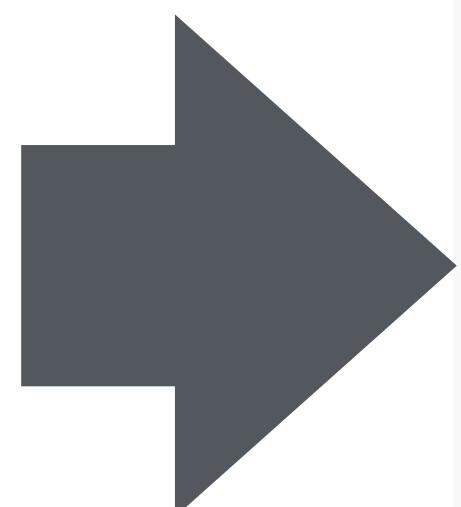
> `n = 5`

> `n = 3`

### Result

```
accumulate(add, 0, 5, identity) # 0 + 1 + 2 + :  
>>> 10
```

- ✓ call `accumulate(add, 0, 5, identity)`
- ✓ `total = 0`
- > `total = 2`
- > `total = 4`
- > `total = 6`
- > `total = 8`
- > `total = 10`
- > `accumulate(add, 0, 5, identity)` returns `10`



### Result

```
accumulate(add, 0, 5, identity) # 0 + 1 + 2 + :  
>>> 10
```

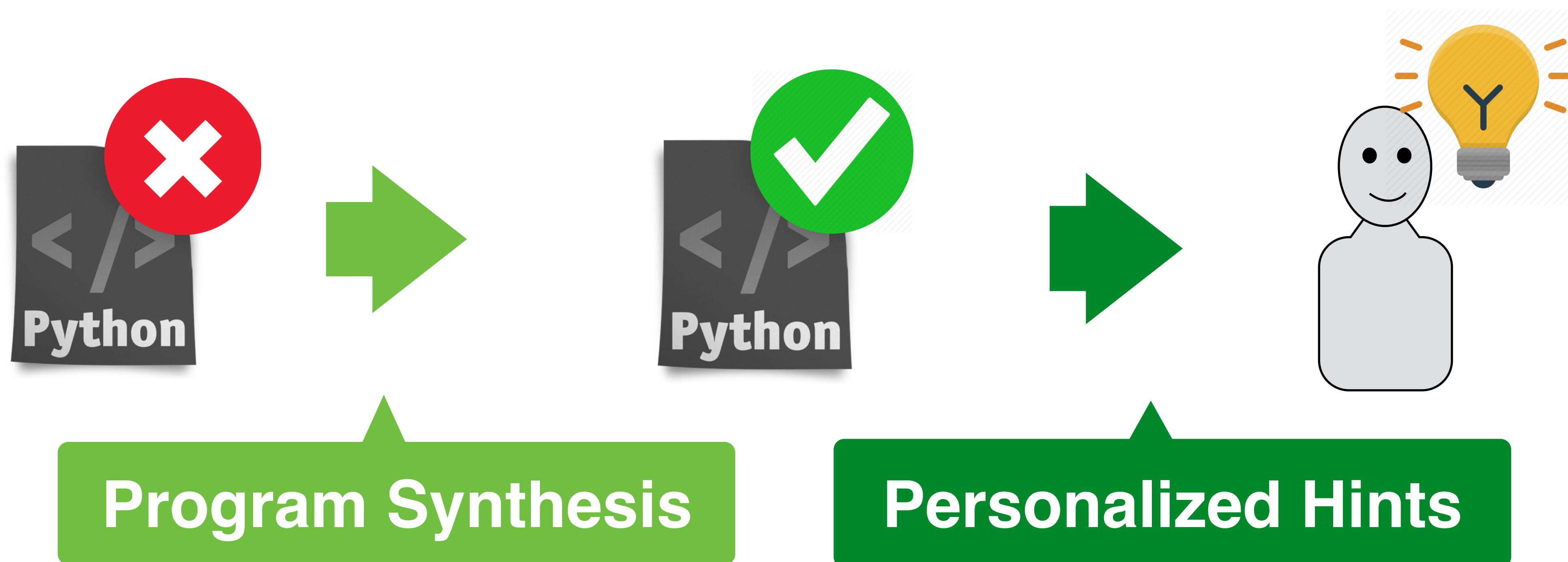
- ✓ call `accumulate(add, 0, 5, identity)`
- ✓ `total = base`
- > `total = add(1, 1)`
- > `total = add(2, 2)`
- > `total = add(3, 3)`
- > `total = add(4, 4)`
- > `total = add(5, 5)`
- > `accumulate(add, 0, 5, identity)` returns `total`

# 3. Abstract Values Into Expressions

# Motivation

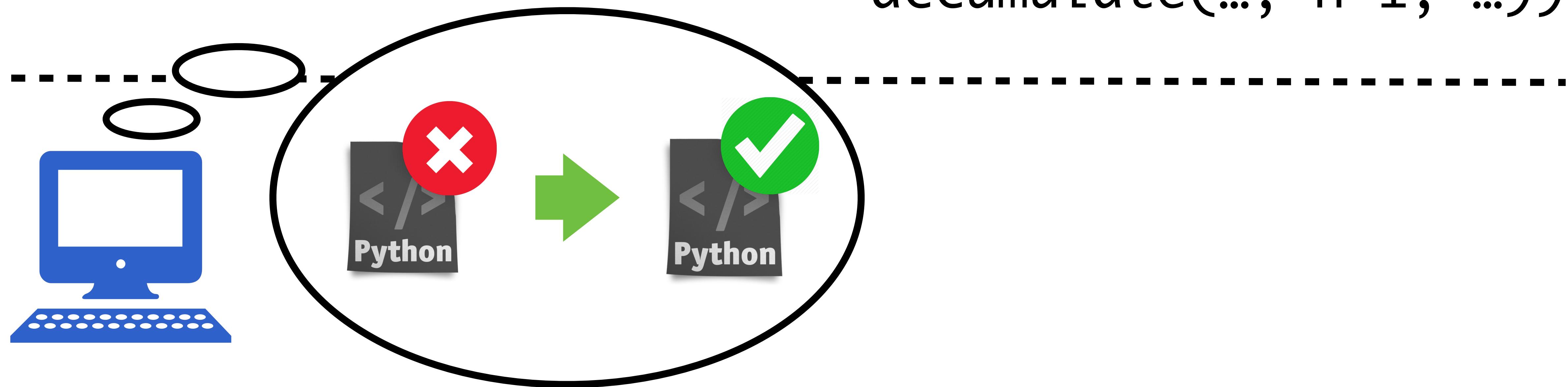
# Program Synthesis Feedback

(e.g. Singh [PLDI'13], D'Antoni [TOCHI'15], Rolim [ICSE'17])



# Code

```
def accumulate(combiner, base, n, term):  
    if n == 1:  
        if n == 0:  
            return base  
    else:  
        return combiner(term(n),  
                        accumulate(..., n-1, ...))
```



## Code

```
def accumulate(combiner, base, n, term):  
    if n == 1:  
        if n == 0:  
            return base  
    else:  
        return combiner(term(n),  
                         accumulate(..., n-1, ...))
```



Line 2 needs to be changed

## Code

```
def accumulate(combiner, base, n, term):  
    if n == 1:  
        if n == 0:  
            return base  
    else:  
        return combiner(term(n),  
                         accumulate(..., n-1, ...))
```



Line 2 needs to be changed

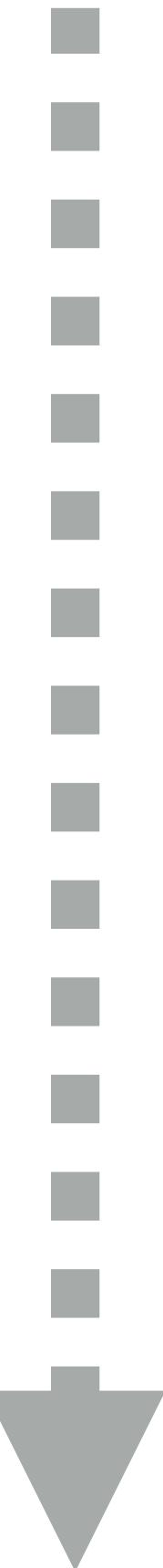
In line 2, change  $n = 1$  to  $n = 0$

# Program Synthesis Feedback

Line 2 needs to be changed

In line 2, check “n”

In line 2, change  $n = 1$  to  $n = 0$



# Program Synthesis Feedback

Pointing

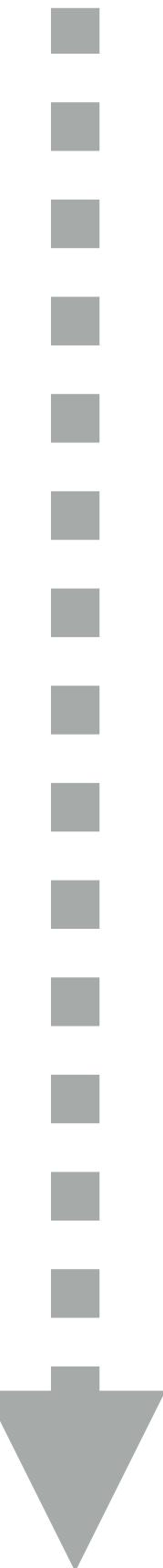
Line 2 needs to be changed  
In line 2, check “n”

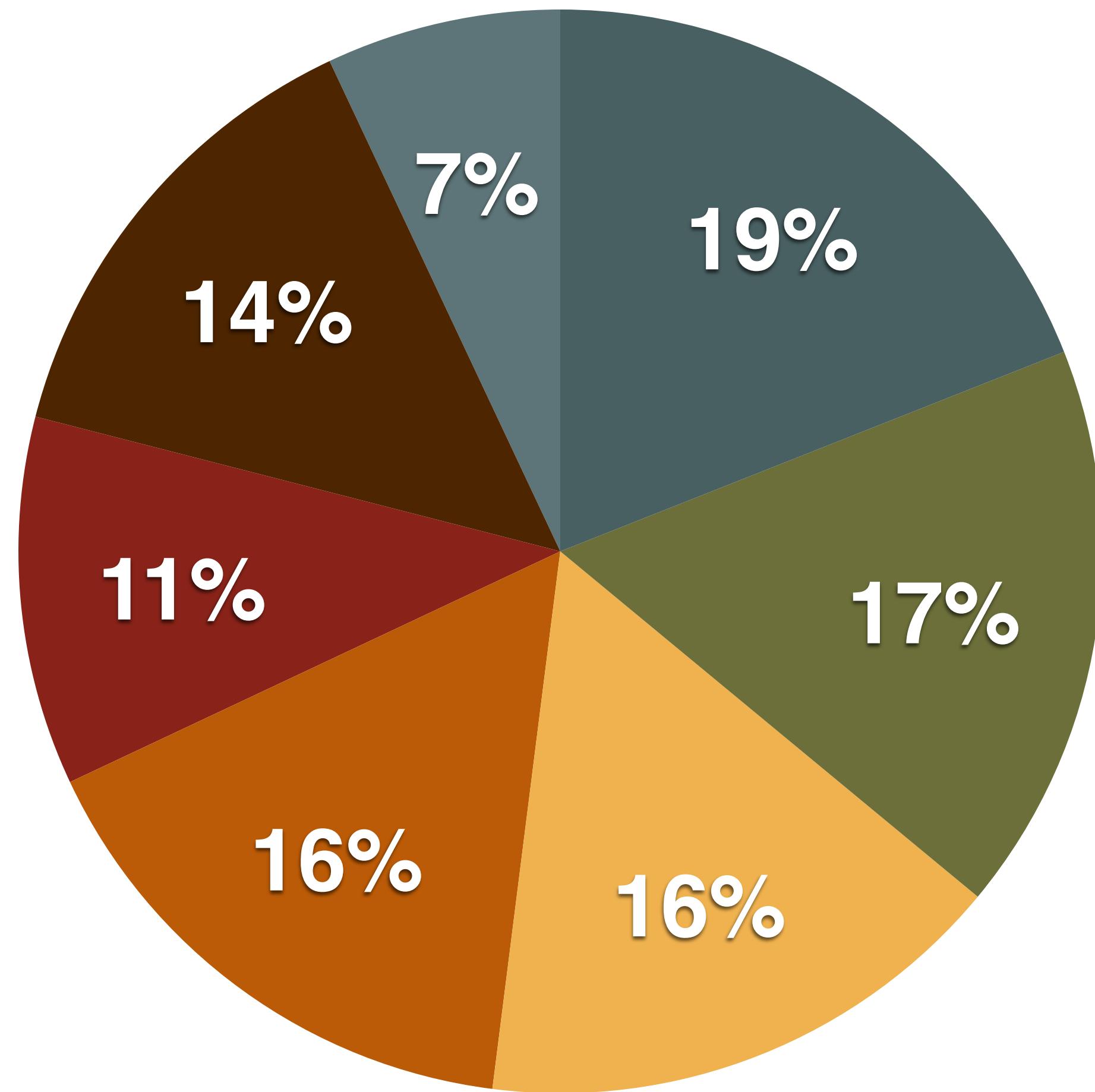
High-level  
Hints



Bottom-out

In line 2, change  $n = 1$  to  $n = 0$

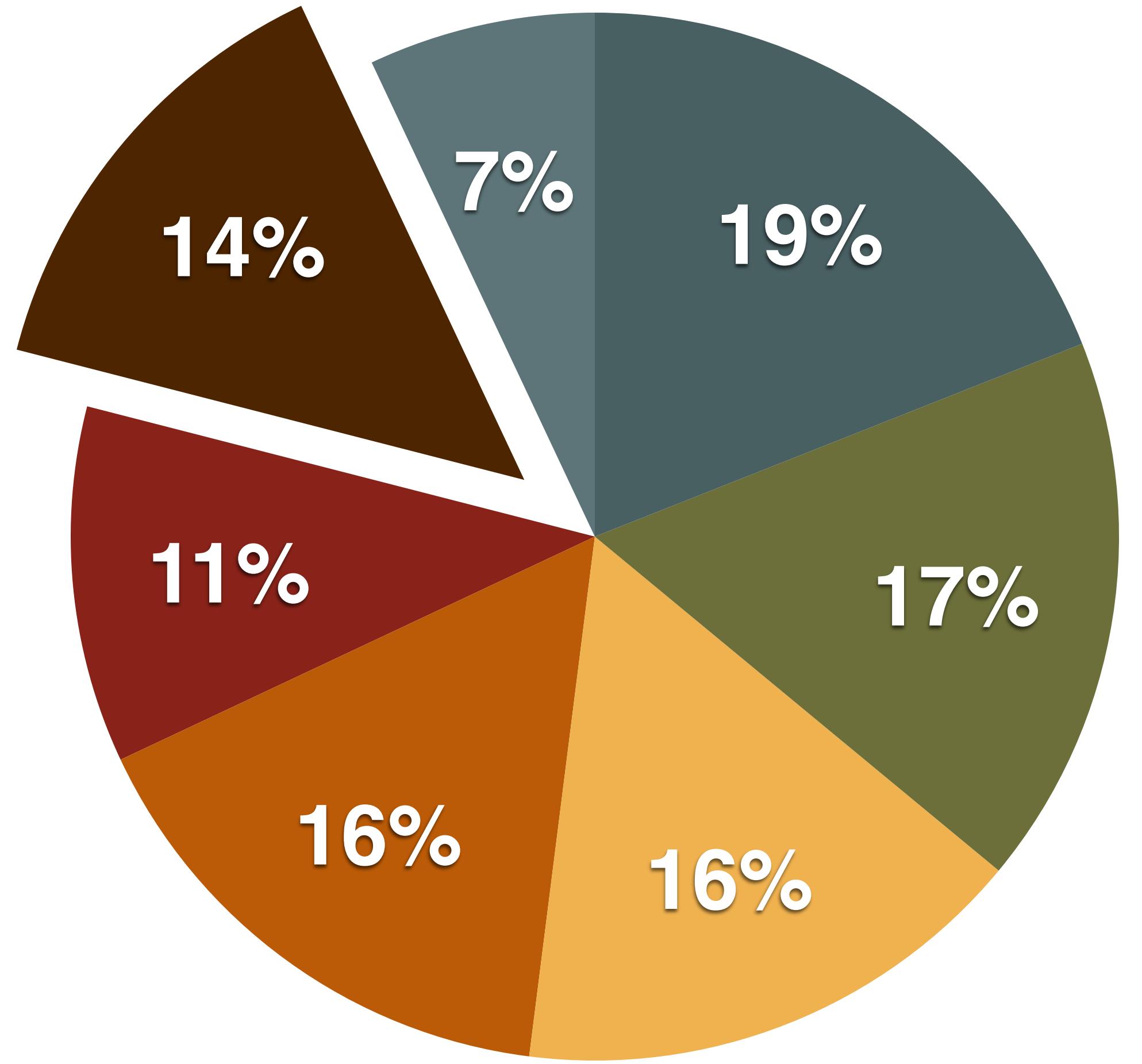




- Diagnose the cause of error: 19%
- Suggest to run code in PythonTutor: 17%
- Explain incorrect behavior: 16%
- Remind relevant resources: 16%
- Provide example usage: 11%
- Point out location: 14%
- Suggest concrete fix: 7%

132 posts on piazza

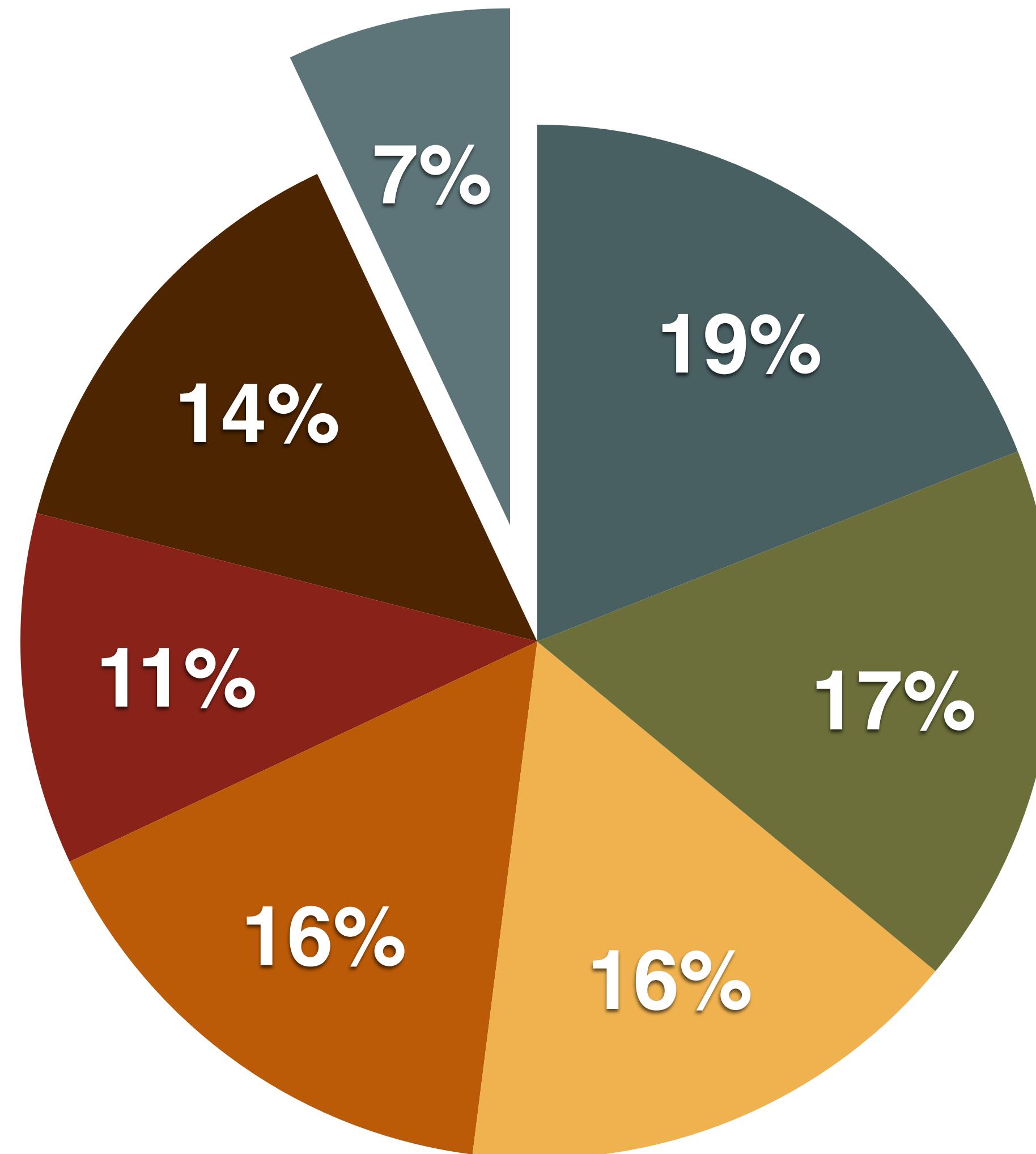




- Diagnose the cause of error: 19%
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- Suggest concrete fix: 7%

132 posts on piazza

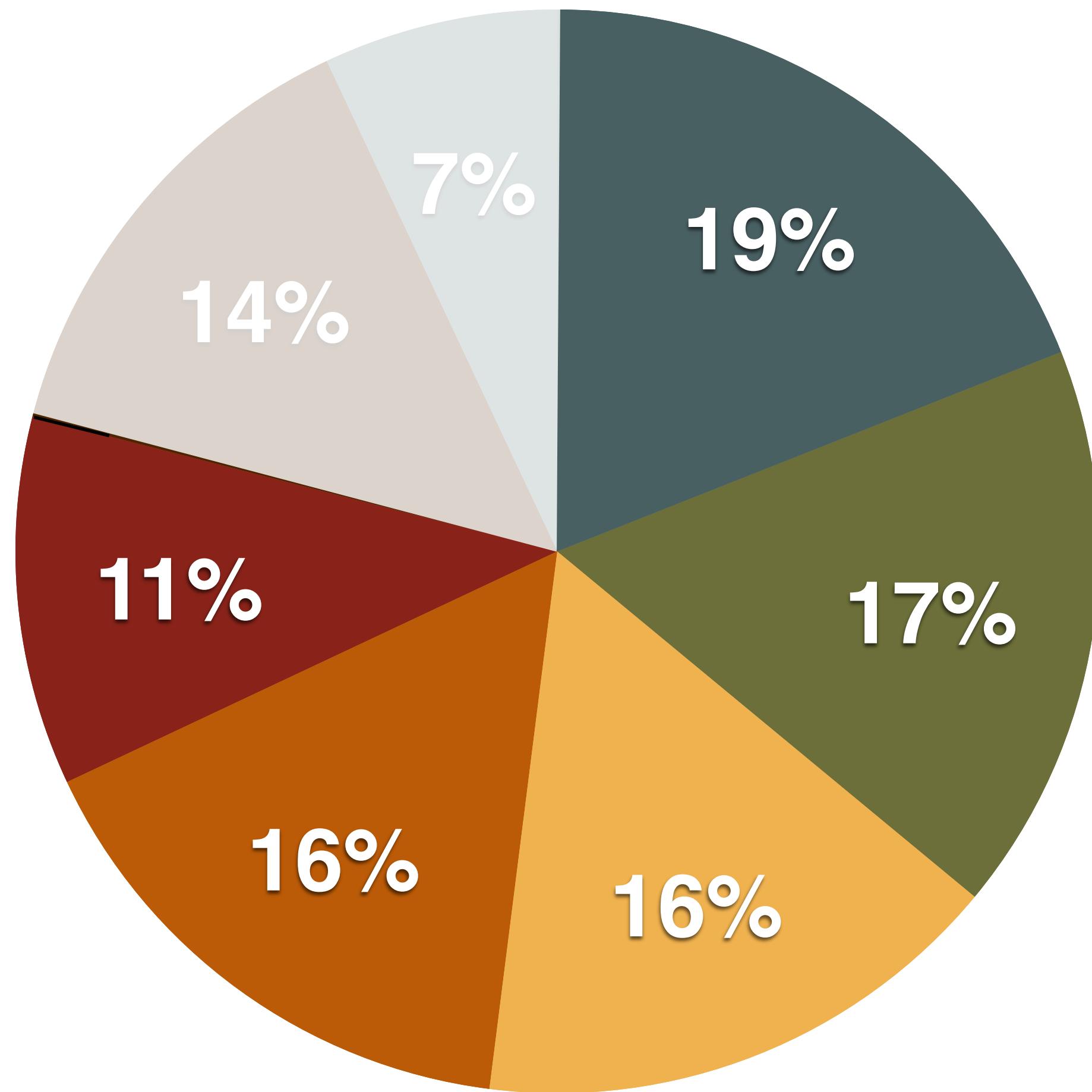




132 posts on piazza

- Diagnose the cause of error: 19%
- Suggest to run code in PythonTutor: 17%
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- **Suggest concrete fix: 7%**





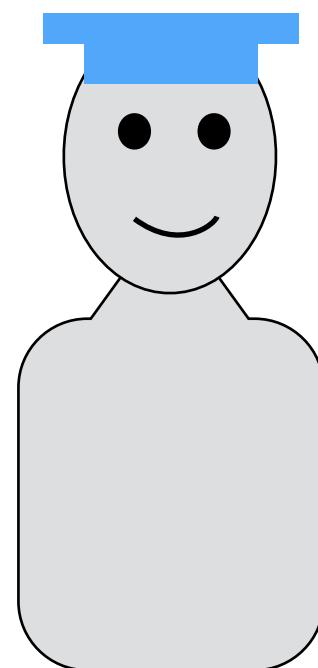
- **Diagnose the cause of error: 19%**
- **Suggest to run in PythonTutor: 17%**
- **Explain incorrect behavior: 16%**
- **Remind relevant resources: 16%**
- **Provide example usage: 11%**
- Point out location: 14%
- Suggest concrete fix: 7%

132 posts on piazza



## Code

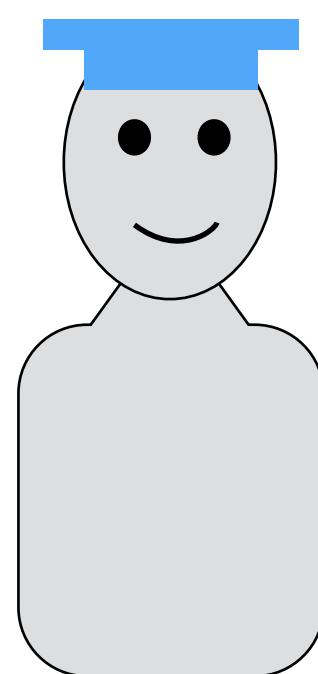
```
def accumulate(combiner, base, n, term):  
    if n == 1:  
        if n == 0:  
            return base  
    else:  
        return combiner(term(n),  
                         accumulate(..., n-1, ...))
```



Check the **base condition**  
in the recursive function

## Code

```
def accumulate(combiner, base, n, term):  
    if n == 1:  
        if n == 0:  
            return base  
    else:  
        return combiner(term(n),  
                         accumulate(..., n-1, ...))
```



accumulate(add, 0, 5, identity)

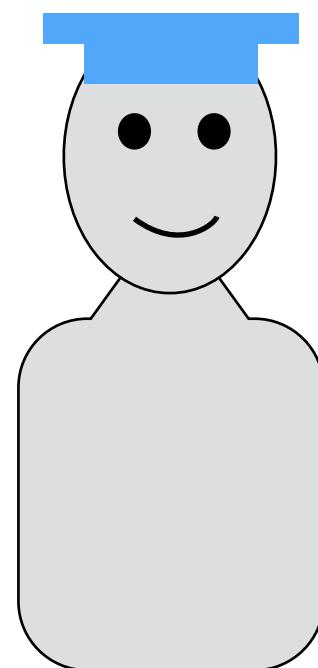
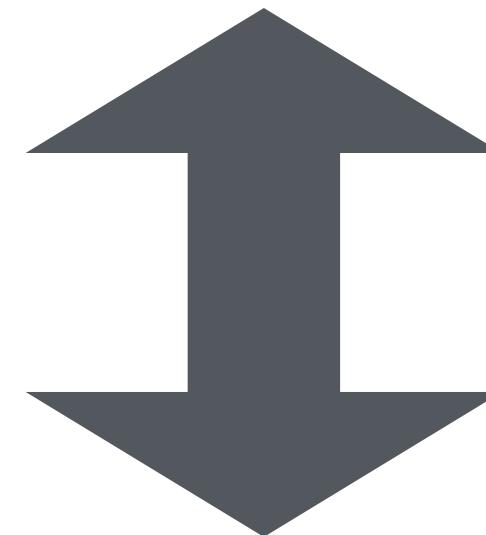
x 14 # 0 + 0 + 2 + 3 + 4 + 5

o 15 # 0 + 1 + 2 + 3 + 4 + 5



Line 2 needs to be changed

In line 2, change n = 1 to n = 0



```
accumulate(add, 0, 5, identity)
```

```
x 14 # 0 + + 2 + 3 + 4 + 5
```

```
o 15 # 0 + 1 + 2 + 3 + 4 + 5
```

**Code**

```
def accumulate(combiner, base, n, term):  
    if n == 1:  
        if n == 0:  
            return base  
    else:  
        return combiner(term(n),  
                         accumulate(..., n-1, ...))
```

**Our Goal**



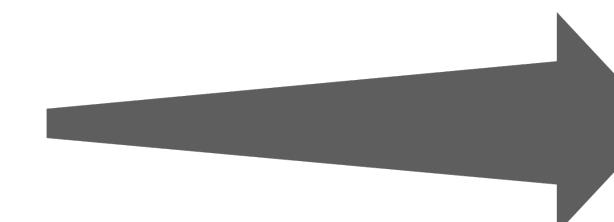
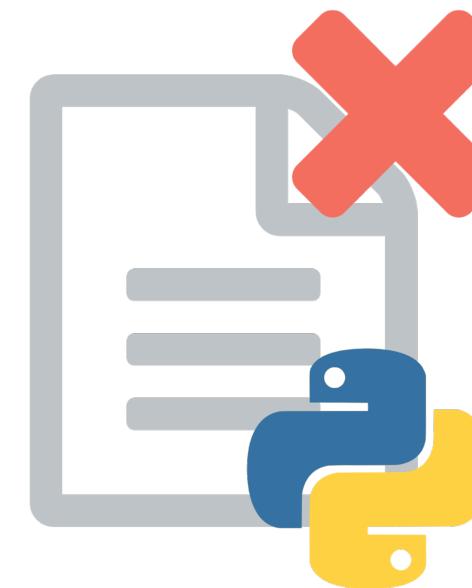
accumulate(add, 0, 5, identity)

x 14 # 0 + + 2 + 3 + 4 + 5

o 15 # 0 + 1 + 2 + 3 + 4 + 5

# Implementation

# Incorrect submission

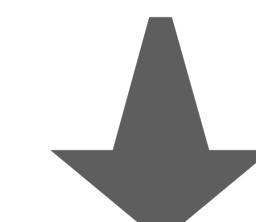


## Result

```
accumulate(add, 0, 5, identity) # 0 +  
>>> 10  
  
✓ call accumulate(add, 0, 5, identity)  
✓ total = 0  
> total = 2
```

## ① Synthesis

# Closest correct program



## ② Execute & Record Trace

## ③

# Filter & Highlight Trace Difference

## Expected

```
accumulate(add, 0, 5, identity) # 0 +  
>>> 15  
  
✓ call accumulate(add, 0, 5, identity)  
✓ total = 0  
> total = 1
```

# Incorrect submission

① Synthesis

Closest correct program



② Execute & Record Trace



## Result

```
accumulate(add, 0, 5, identity) # 0 +  
>>> 10  
  
✓ call accumulate(add, 0, 5, identity)  
✓ total = 0  
> total = 2
```

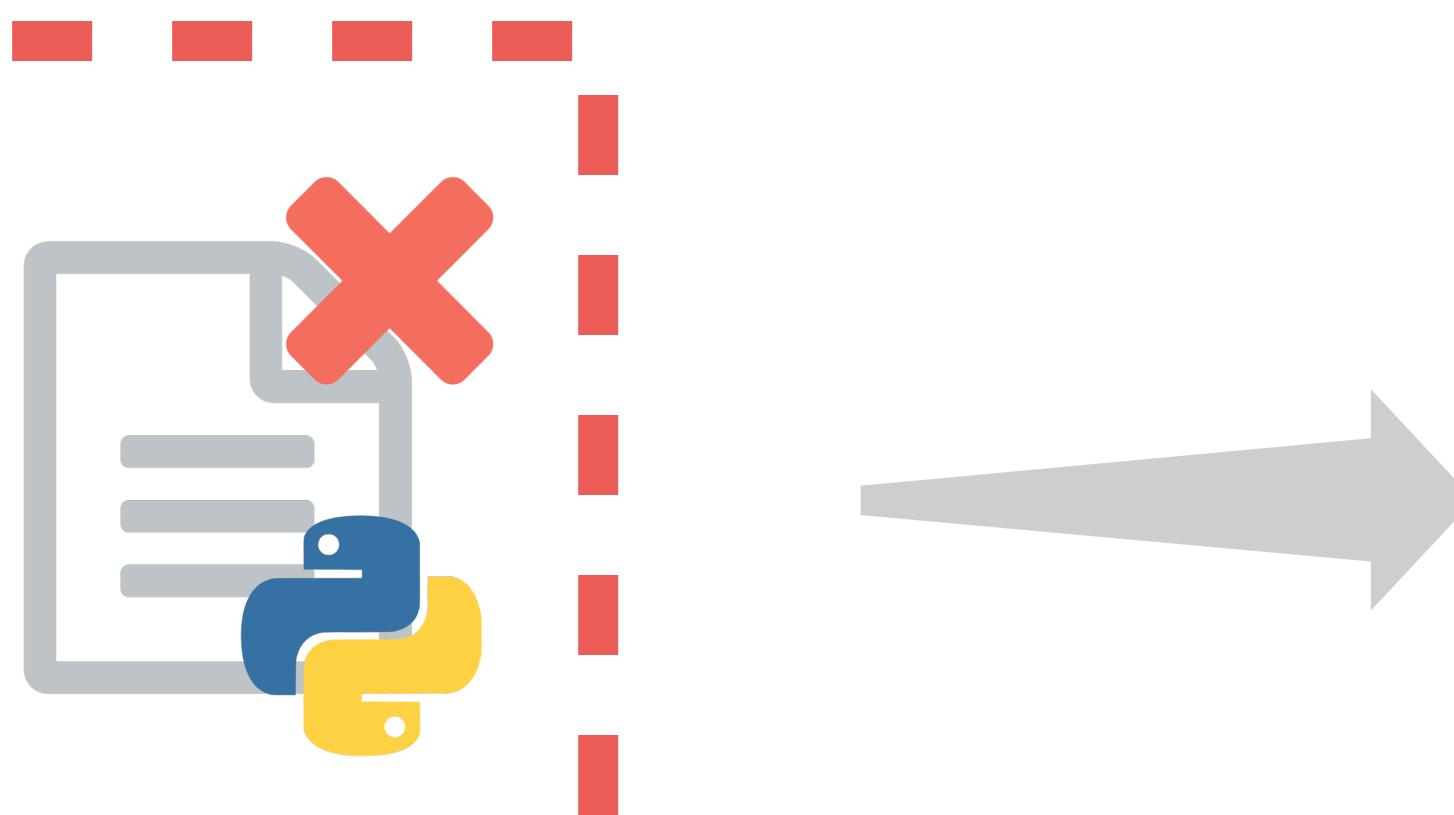
③

Filter & Highlight Trace Difference

## Expected

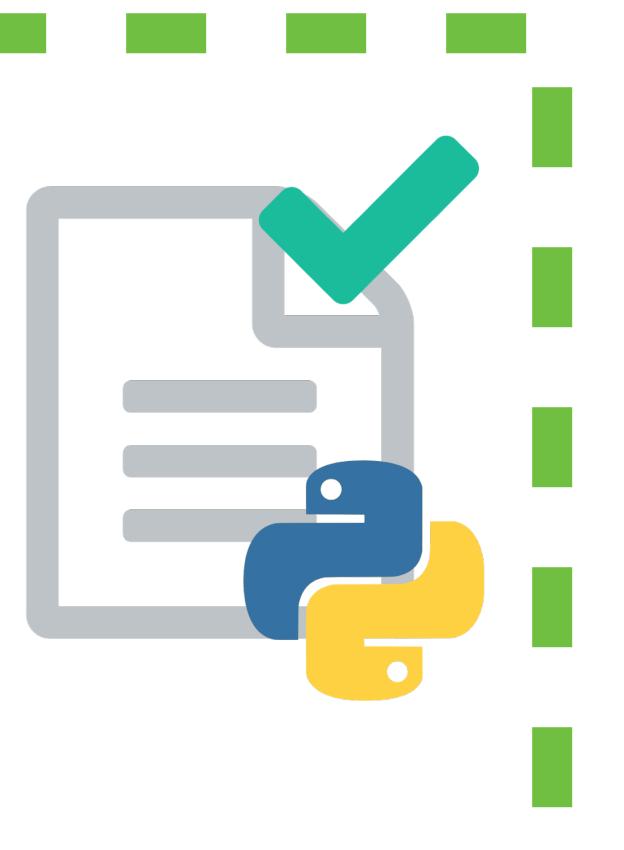
```
accumulate(add, 0, 5, identity) # 0 + :  
>>> 15  
  
✓ call accumulate(add, 0, 5, identity)  
✓ total = 0  
> total = 1
```

# Incorrect submission



## ① Synthesis

Closest correct program



## ② Execute & Record Trace

### Result

```
accumulate(add, 0, 5, identity) # 0 +  
>>> 10  
  
✓ call accumulate(add, 0, 5, identity)  
✓ total = 0  
> total = 2
```

## ③

## Filter & Highlight Trace Difference

### Expected

```
accumulate(add, 0, 5, identity) # 0 + :  
>>> 15  
  
✓ call accumulate(add, 0, 5, identity)  
✓ total = 0  
> total = 1
```

# Learning Code Transformation (e.g., Refazer [ICSE'17])

Example from  
student submissions  
(e.g. Student 1)

```
def product(n, term):
    total, k = 1, 1
    while k<=n:
        - total = total*k
        + total = total*term(k)
        k = k+1
    return total
```

# Learning Code Transformation (e.g., Refazer [ICSE'17])

Example from  
student submissions  
(e.g. Student 1)

Learn code transformation  
from examples

```
def product(n, term):
    total, k = 1, 1
    while k<=n:
        - total = total*k
        + total = total*term(k)
        k = k+1
    return total
```

Insert

$\langle \text{exp} \rangle * \langle \text{name} \rangle \rightarrow \langle \text{exp} \rangle * \boxed{\text{term}(\langle \text{name} \rangle)}$

# Learning Code Transformation (e.g., Refazer [ICSE'17])

Example from  
student submissions  
(e.g. Student 1)

Learn code transformation  
from examples

Apply code transformation  
(e.g., Student 2)

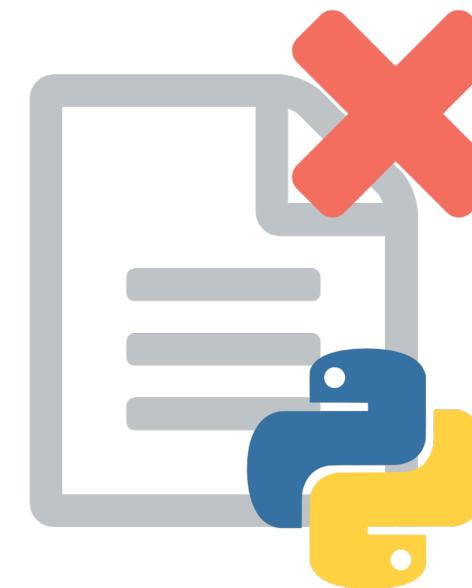
```
def product(n, term):
    total, k = 1, 1
    while k<=n:
        - total = total*k
        + total = total*term(k)
        k = k+1
    return total
```

Insert

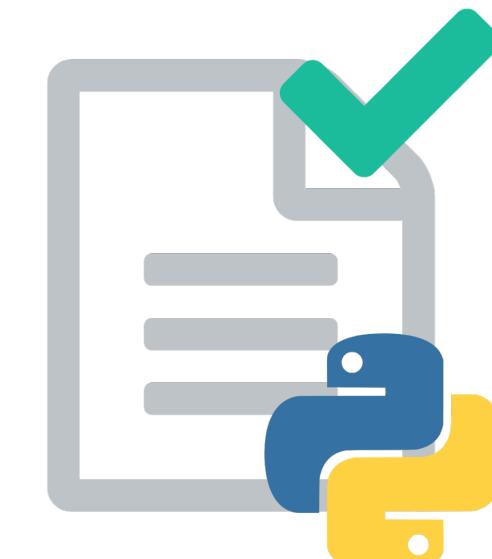
<exp> \* <name> → <exp> \* term(<name>)

```
def product(n, term):
    if (n==1):
        return 1
    - return product(n-1, term)*n
    + return product(n-1, term)*term(n)
```

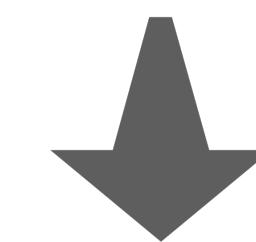
# Incorrect submission



# Closest correct program



## ① Synthesis



## ② Execute & Record Trace



### Result

```
accumulate(add, 0, 5, identity) # 0 +  
>>> 10  
  
✓ call accumulate(add, 0, 5, identity)  
✓ total = 0  
> total = 2
```

## ③

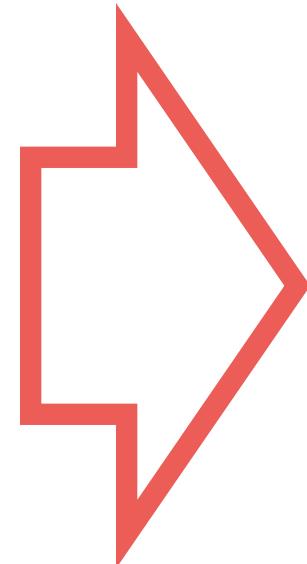
## Filter & Highlight Trace Difference

### Expected

```
accumulate(add, 0, 5, identity) # 0 + :  
>>> 15  
  
✓ call accumulate(add, 0, 5, identity)  
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```

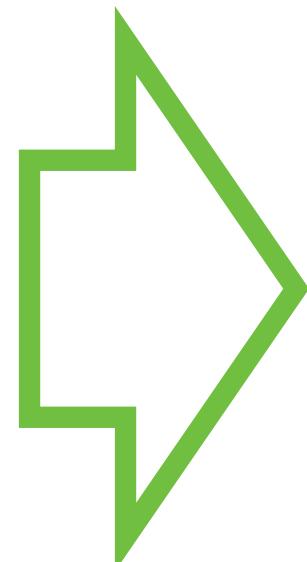
→ def accumulate(n):  
    total = 0  
    i = 1  
    while i <= n:  
        k = square(i)  
        total = total + k  
        i = i + 1

n: 3



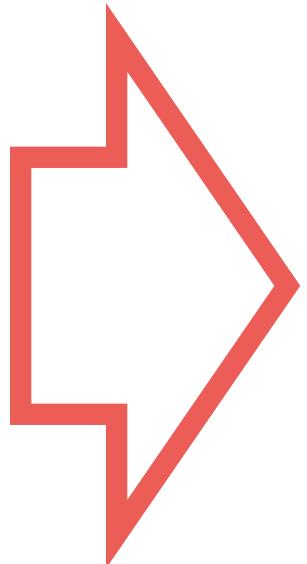
→ def accumulate(n):  
    total = 10  
    i = 1  
    while i <= n:  
        k = square(i)  
        total = total + i  
        i = i + 1

n: 3



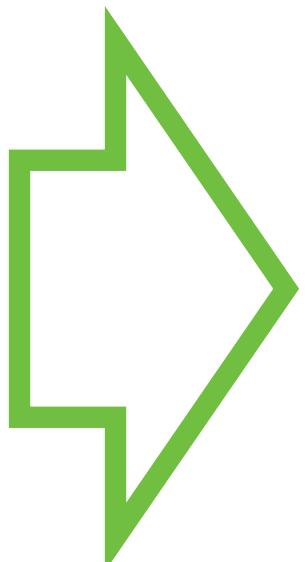
```
def accumulate(n):  
    total = 0  
    i = 1  
    while i <= n:  
        k = square(i)  
        total = total + k  
        i = i + 1
```

n: 3  
total: 0



```
-----  
def accumulate(n):  
    total = 10  
    i = 1  
    while i <= n:  
        k = square(i)  
        total = total + i  
        i = i + 1
```

n: 3  
total: 3



```
def accumulate(n):  
    total = 0  
    → i = 1  
    while i <= n:  
        k = square(i)  
        total = total + k  
        i = i + 1
```

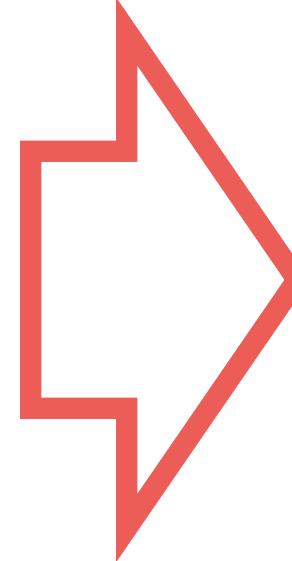
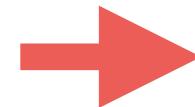
n: 3  
total: 0  
i: 1

---

```
def accumulate(n):  
    total = 10  
    → i = 1  
    while i <= n:  
        k = square(i)  
        total = total + i  
        i = i + 1
```

n: 3  
total: 10  
i: 1

```
def accumulate(n):  
    total = 0  
    i = 1  
    while i <= n:  
        k = square(i)  
        total = total + k  
        i = i + 1
```



```
n: 3  
total: 0  
i: 1  
k: 1
```

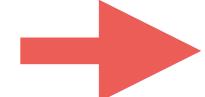
---

```
def accumulate(n):  
    total = 10  
    i = 1  
    while i <= n:  
        k = square(i)  
        total = total + i  
        i = i + 1
```



```
n: 3  
total: 10  
i: 1  
k: 1
```

```
def accumulate(n):  
    total = 0  
    i = 1  
    while i <= n:  
        k = square(i)  
        total = total + k  
        i = i + 1
```



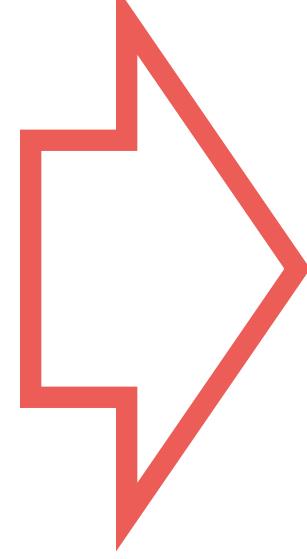
n: 3  
total: 0, 1  
i: 1  
k: 1

```
def accumulate(n):  
    total = 10  
    i = 1  
    while i <= n:  
        k = square(i)  
        total = total + i  
        i = i + 1
```



n: 3  
total: 10, 11  
i: 1  
k: 1

```
def accumulate(n):  
    total = 0  
    i = 1  
    while i <= n:  
        k = square(i)  
        total = total + k  
        i = i + 1
```



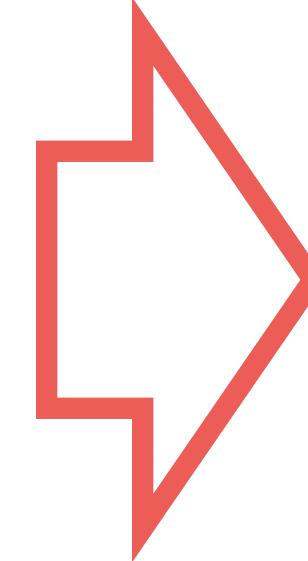
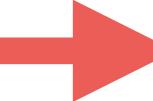
n: 3  
total: 0, 1  
i: 1, 2  
k: 1

```
def accumulate(n):  
    total = 10  
    i = 1  
    while i <= n:  
        k = square(i)  
        total = total + i  
        i = i + 1
```



n: 3  
total: 10, 11  
i: 1, 2  
k: 1

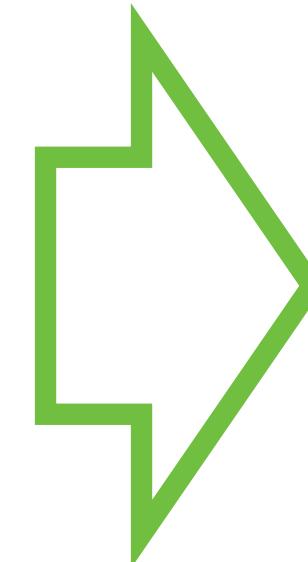
```
def accumulate(n):  
    total = 0  
    i = 1  
    while i <= n:  
        k = square(i)  
        total = total + k  
        i = i + 1
```



```
n: 3  
total: 0, 1  
i: 1, 2  
k: 1, 4
```

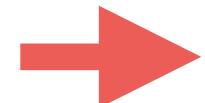
---

```
def accumulate(n):  
    total = 10  
    i = 1  
    while i <= n:  
        k = square(i)  
        total = total + i  
        i = i + 1
```



```
n: 3  
total: 10, 11  
i: 1, 2  
k: 1, 4
```

```
def accumulate(n):  
    total = 0  
    i = 1  
    while i <= n:  
        k = square(i)  
        total = total + k  
        i = i + 1
```



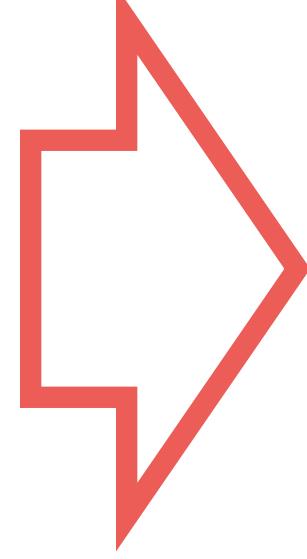
n: 3  
total: 0, 1, 5  
i: 1, 2  
k: 1, 4

```
def accumulate(n):  
    total = 10  
    i = 1  
    while i <= n:  
        k = square(i)  
        total = total + i  
        i = i + 1
```



n: 3  
total: 10, 11, 15  
i: 1, 2  
k: 1, 4

```
def accumulate(n):  
    total = 0  
    i = 1  
    while i <= n:  
        k = square(i)  
        total = total + k  
        i = i + 1
```



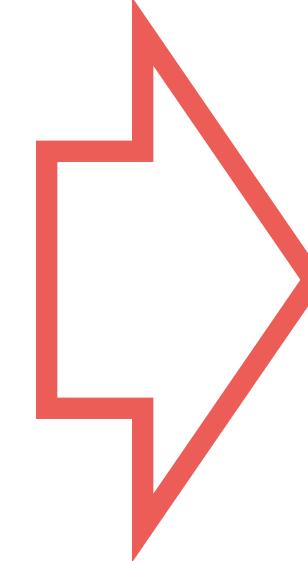
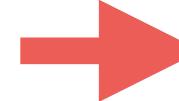
n: 3  
total: 0, 1, 5  
i: 1, 2, 3  
k: 1, 4

```
def accumulate(n):  
    total = 10  
    i = 1  
    while i <= n:  
        k = square(i)  
        total = total + i  
        i = i + 1
```



n: 3  
total: 10, 11, 15  
i: 1, 2, 3  
k: 1, 4

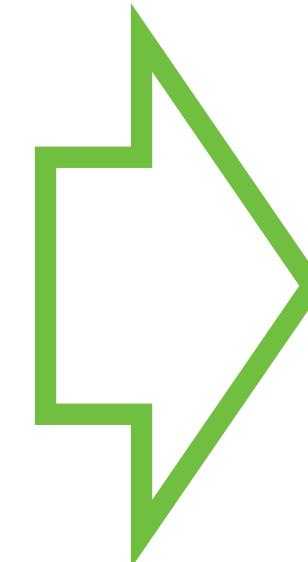
```
def accumulate(n):  
    total = 0  
    i = 1  
    while i <= n:  
        k = square(i)  
        total = total + k  
        i = i + 1
```



n: 3  
total: 0, 1, 5  
i: 1, 2, 3  
k: 1, 4, 9

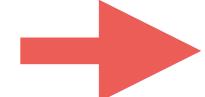
---

```
def accumulate(n):  
    total = 10  
    i = 1  
    while i <= n:  
        k = square(i)  
        total = total + i  
        i = i + 1
```



n: 3  
total: 10, 11, 15  
i: 1, 2, 3  
k: 1, 4, 9

```
def accumulate(n):  
    total = 0  
    i = 1  
    while i <= n:  
        k = square(i)  
        total = total + k  
        i = i + 1
```



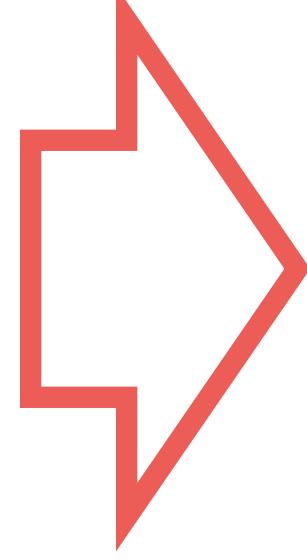
n: 3  
total: 0, 1, 5, 14  
i: 1, 2, 3  
k: 1, 4, 9

```
def accumulate(n):  
    total = 10  
    i = 1  
    while i <= n:  
        k = square(i)  
        total = total + i  
        i = i + 1
```



n: 3  
total: 10, 11, 15, 24  
i: 1, 2, 3  
k: 1, 4, 9

```
def accumulate(n):  
    total = 0  
    i = 1  
    while i <= n:  
        k = square(i)  
        total = total + k  
        i = i + 1
```



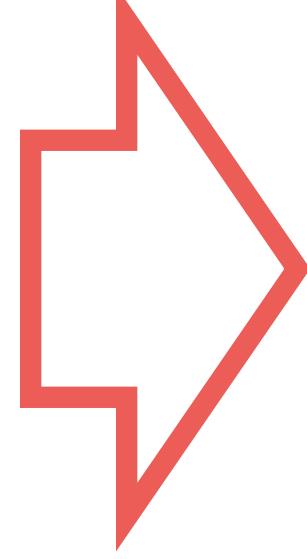
n: 3  
total: 0, 1, 5, 14  
i: 1, 2, 3, 4  
k: 1, 4, 9

```
def accumulate(n):  
    total = 10  
    i = 1  
    while i <= n:  
        k = square(i)  
        total = total + i  
        i = i + 1
```



n: 3  
total: 10, 11, 15, 24  
i: 1, 2, 3, 4  
k: 1, 4, 9

```
def accumulate(n):  
    total = 0  
    i = 1  
    while i <= n:  
        k = square(i)  
        total = total + k  
        i = i + 1
```



n: 3  
total: 0, 1, 5, 14  
i: 1, 2, 3, 4  
k: 1, 4, 9

```
def accumulate(n):  
    total = 10  
    i = 1  
    while i <= n:  
        k = square(i)  
        total = total + i  
        i = i + 1
```



n: 3  
total: 10, 11, 15, 24  
i: 1, 2, 3, 4  
k: 1, 4, 9

## Result

```
accumulate(add, 11, 5, identity) # 11 + 1 + 2 + 3 + 4 + 5  
>>> 81
```

```
> call accumulate(add, 11, 5, identity)  
> term = identity  
> combiner = add  
> base = 11  
> n = 5  
> k = 5  
> call accumulate(add, 11, 4, identity)  
> n = 4  
> k = 4  
> call accumulate(add, 11, 3, identity)  
> n = 3  
> k = 3  
> call accumulate(add, 11, 2, identity)
```

**However,**

showing all of traces  
**can overwhelm**  
students with  
too much information

and make it **difficult to**  
**grasp an overview** of  
the behavior

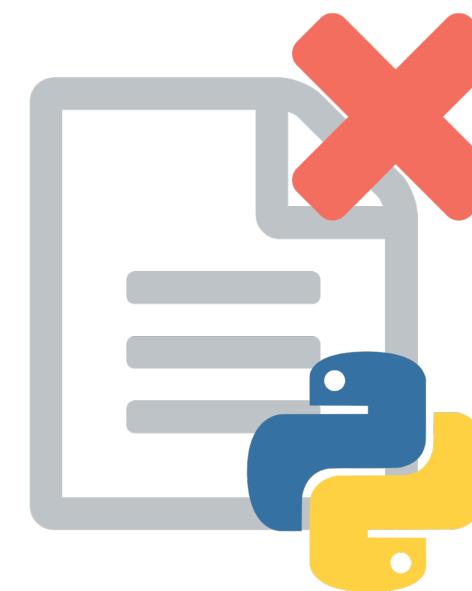
### Result

```
accumulate(add, 11, 5, identity) # 11 + 1 + 2 + 3 + 4 + 5
>>> 81
```

```
> call accumulate(add, 11, 5, identity)
> term = identity
> combiner = add
> base = 11
> n = 5
> k = 5
> call accumulate(add, 11, 4, identity)
> n = 4
> k = 4
> call accumulate(add, 11, 3, identity)
> n = 3
> k = 3
> call accumulate(add, 11, 2, identity)
```

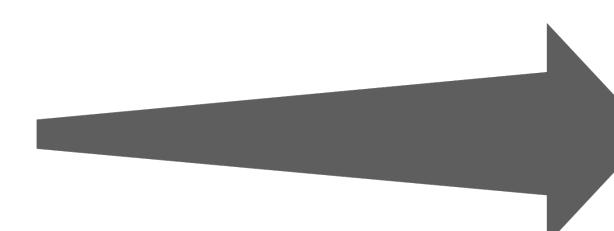
: + 24 lines

# Incorrect submission



② Execute & Record Trace

# Closest correct program



Result

```
accumulate(add, 0, 5, identity) # 0 +  
>>> 10
```

✓ call accumulate(add, 0, 5, identity)  
✓ total = 0  
> total = 2

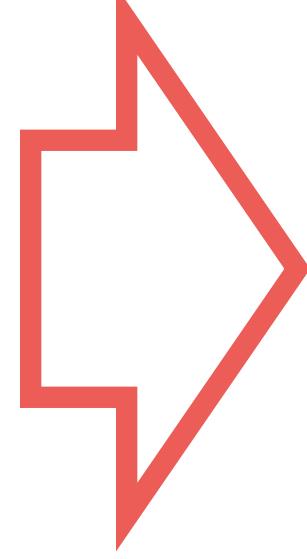
③ Filter & Highlight Trace Difference

Expected

```
accumulate(add, 0, 5, identity) # 0 +  
>>> 15
```

✓ call accumulate(add, 0, 5, identity)  
✓ total = 0  
> total = 1

```
def accumulate(n):  
    total = 0  
    i = 1  
    while i <= n:  
        k = square(i)  
        total = total + k  
        i = i + 1
```



n: 3  
total: 0, 1, 5, 14  
i: 1, 2, 3, 4  
k: 1, 4, 9

```
def accumulate(n):  
    total = 10  
    i = 1  
    while i <= n:  
        k = square(i)  
        total = total + i  
        i = i + 1
```



n: 3  
total: 10, 11, 15, 24  
i: 1, 2, 3, 4  
k: 1, 4, 9

```
def accumulate(n):  
    total = 0  
    i = 1  
    while i <= n:  
        k = square(i)  
        total = total + k  
        i = i + 1
```

---

n: 3

total: 0, 1, 5, 14

i: 1, 2, 3, 4

k: 1, 4, 9

```
def accumulate(n):  
    total = 10  
    i = 1  
    while i <= n:  
        k = square(i)  
        total = total + i  
        i = i + 1
```

n: 3

total: 10, 11, 15, 24

i: 1, 2, 3, 4

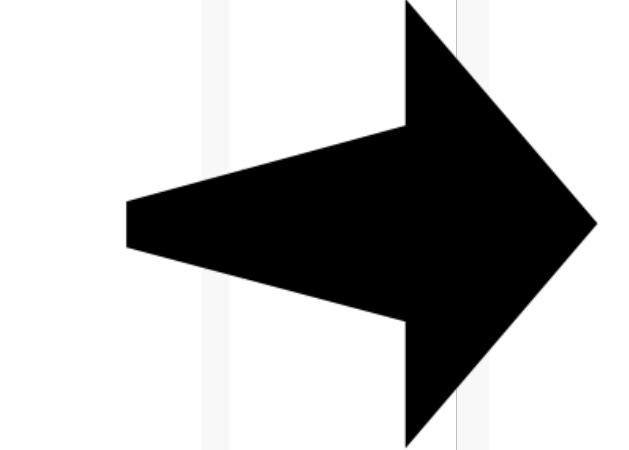
k: 1, 4, 9

# Without filtering

## Result

```
accumulate(add, 11, 5, identity) # 11 + 1 + 2 + 3 + 4 +  
>>> 81
```

- ✓ call accumulate(add, 11, 5, identity)
- ✓ term = identity
- ✓ combiner = add
- ✓ base = 11
- ✓ n = 5
- ✓ k = 5
- ✓ call accumulate(add, 11, 4, identity)
- ✓ n = 4
- ✓ k = 4
- ✓ call accumulate(add, 11, 3, identity)
- ✓ n = 3
- ✓ k = 3
- ✓ call accumulate(add, 11, 2, identity)
- .
- ⋮ + 24 lines



A

# With filtering

## Result

```
accumulate(add, 11, 5, identity) # 11 + 1 + 2 + 3  
>>> 81
```

- ✓ call accumulate(add, 11, 5, identity)
- ✓ call accumulate(add, 11, 4, identity)
- ✓ call accumulate(add, 11, 3, identity)
- ✓ call accumulate(add, 11, 2, identity)
- ✓ call accumulate(add, 11, 1, identity)
- ✓ call accumulate(add, 11, 0, identity)
- ✓ accumulate(add, 11, 0, identity) returns 11
- › accumulate(add, 11, 1, identity) returns 23
- › accumulate(add, 11, 2, identity) returns 36
- › accumulate(add, 11, 3, identity) returns 50
- › accumulate(add, 11, 4, identity) returns 65
- › accumulate(add, 11, 5, identity) returns 81

B

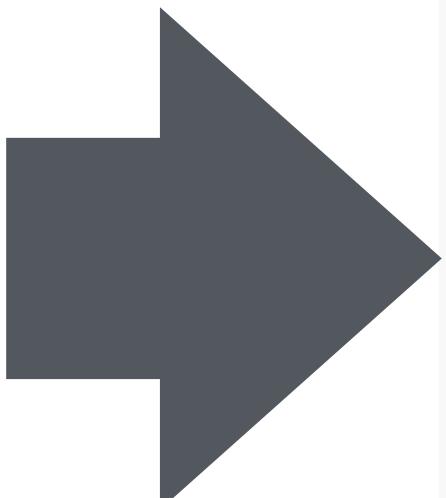
# **Value Abstraction**

# Abstract Values into Expressions

## Result

```
accumulate(add, 0, 5, identity) # 0 + 1 + 2 + :  
>>> 10
```

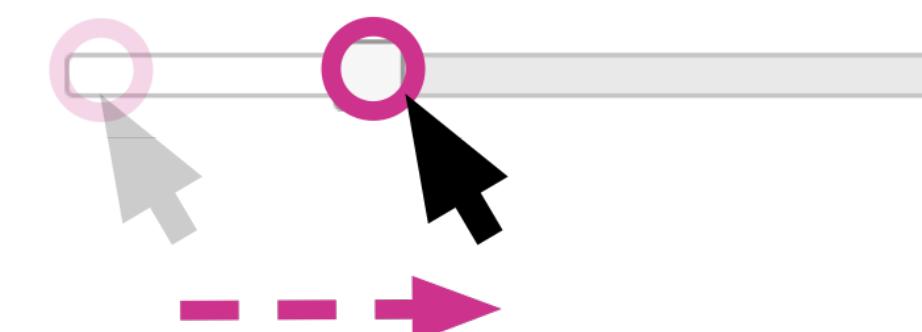
- ✓ call `accumulate(add, 0, 5, identity)`
- ✓ `total = 0`
- › `total = 2`
- › `total = 4`
- › `total = 6`
- › `total = 8`
- › `total = 10`
- › `accumulate(add, 0, 5, identity)` returns `10`



## Result

```
accumulate(add, 0, 5, identity) # 0 + 1 + 2 + :  
>>> 10
```

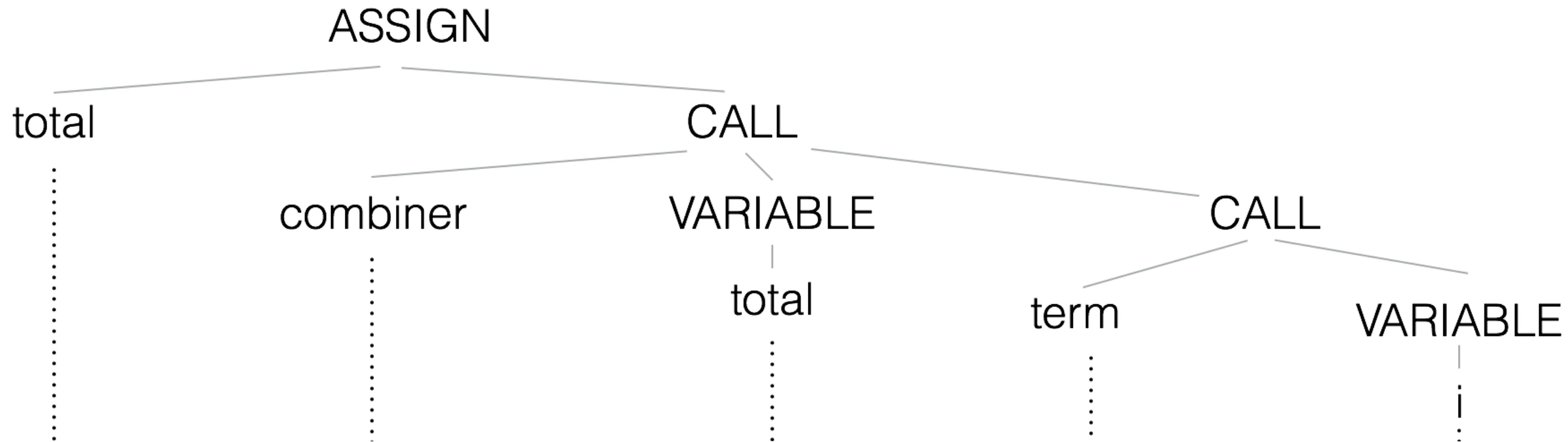
- ✓ call `accumulate(add, 0, 5, identity)`
- ✓ `total = base`
- › `total = add(1, 1)`
- › `total = add(2, 2)`
- › `total = add(3, 3)`
- › `total = add(4, 4)`
- › `total = add(5, 5)`
- › `accumulate(add, 0, 5, identity)` returns `total`



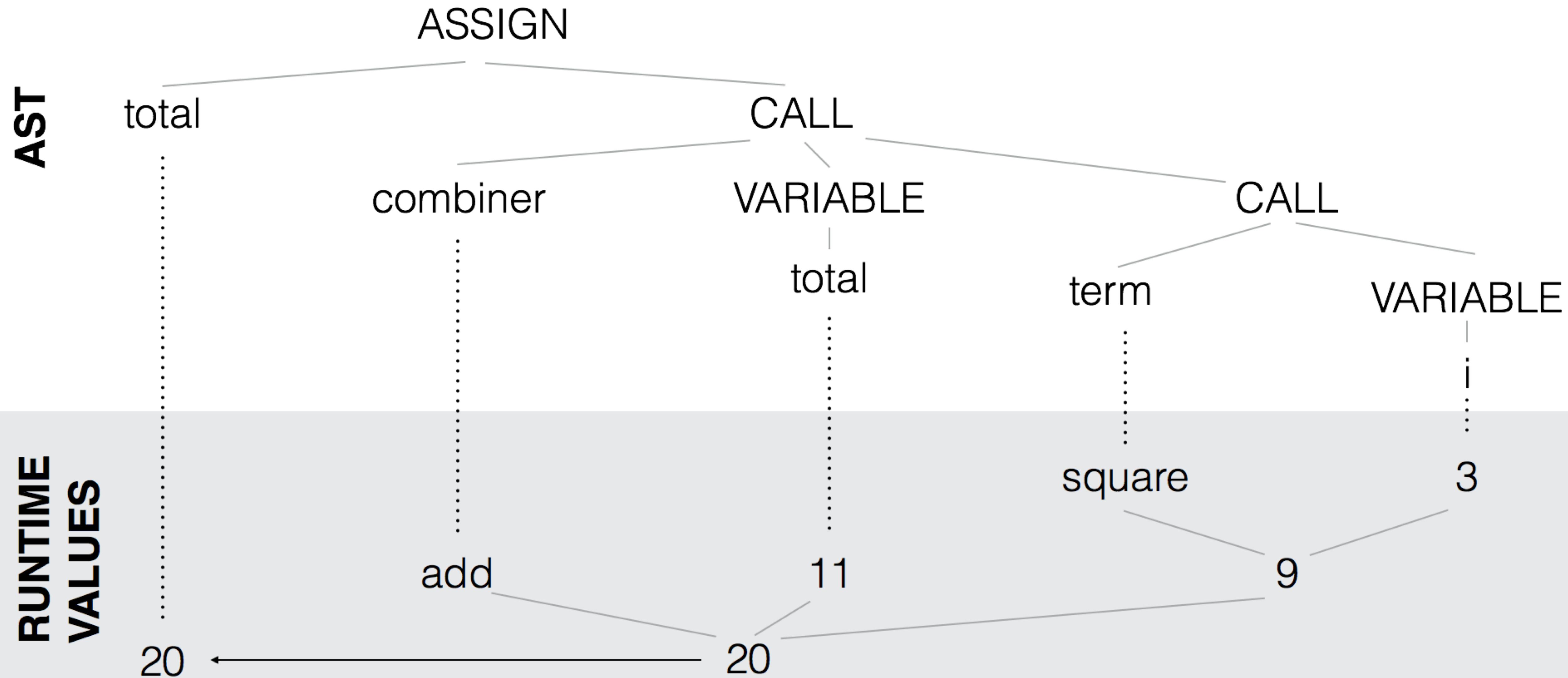
```
total = combiner(i, term(i))
```

```
total = combiner(i, term(i))
```

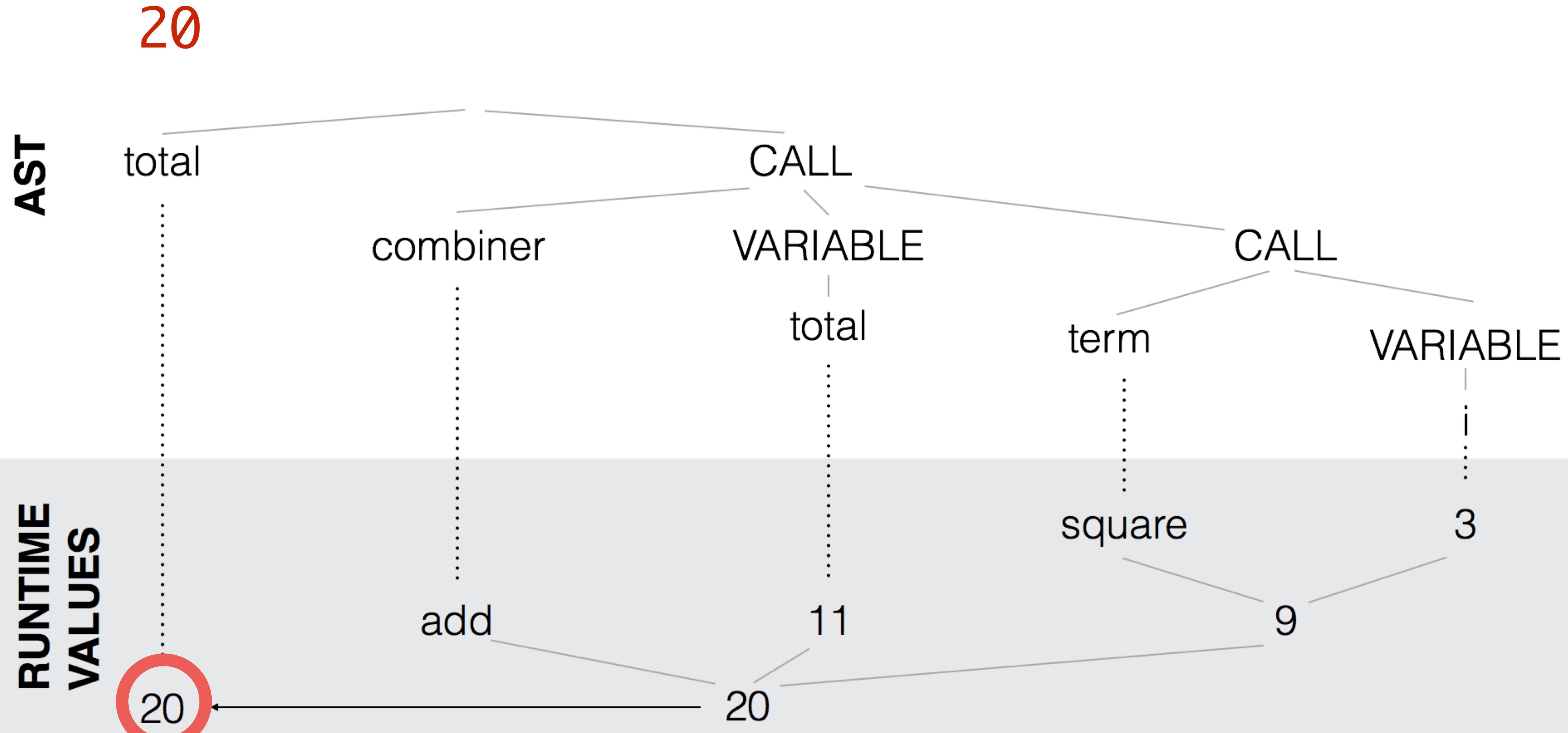
AST



```
total = combiner(i, term(i))
```



```
total = combiner(i, term(i))
```



```
total = combiner(i, term(i))
```

20 → add(11, 9)

AST

total

combiner

CALL

VARIABLE

total

CALL

term

VARIABLE

add

11

9

RUNTIME  
VALUES

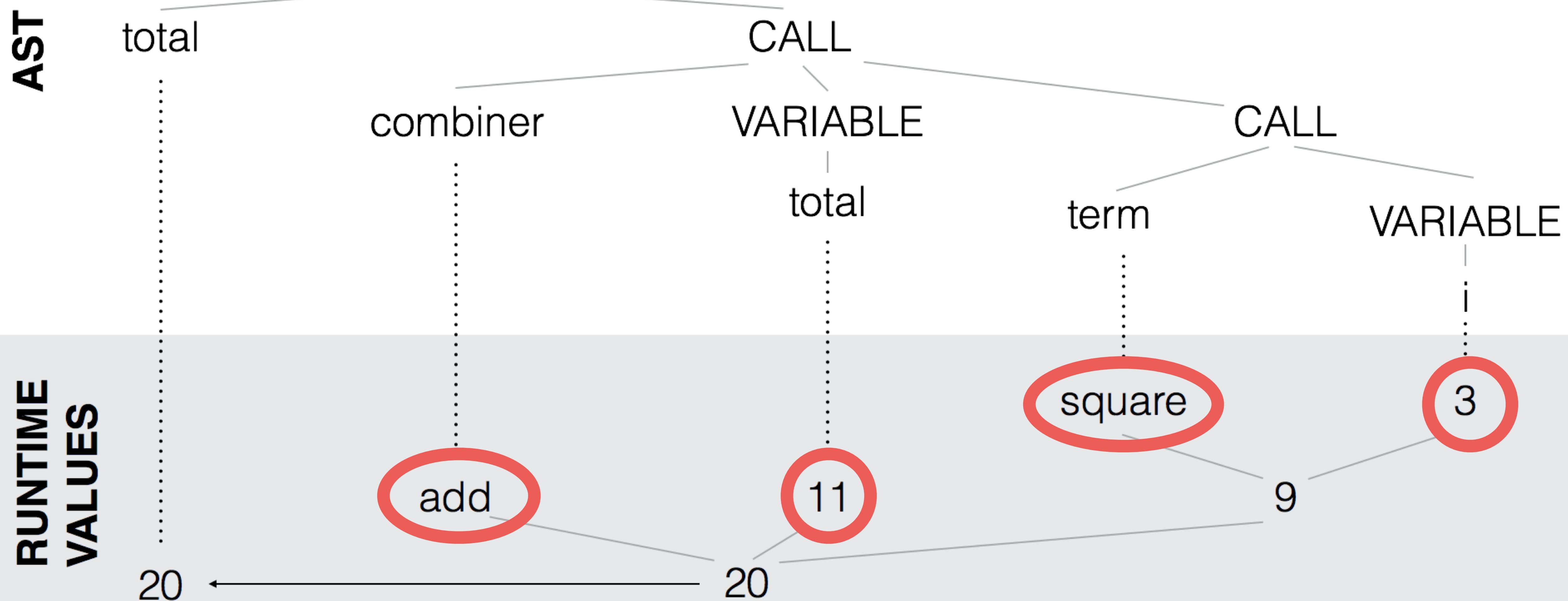
20

20

3

total = combiner(i, term(i))

20 → add(11, 9) → add(11, square(3)) → ...

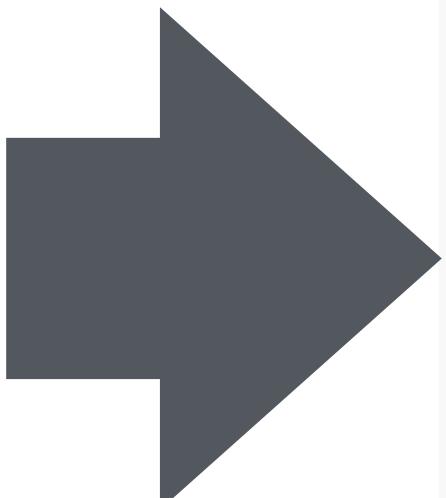


# Abstract Values into Expressions

## Result

```
accumulate(add, 0, 5, identity) # 0 + 1 + 2 + :  
>>> 10
```

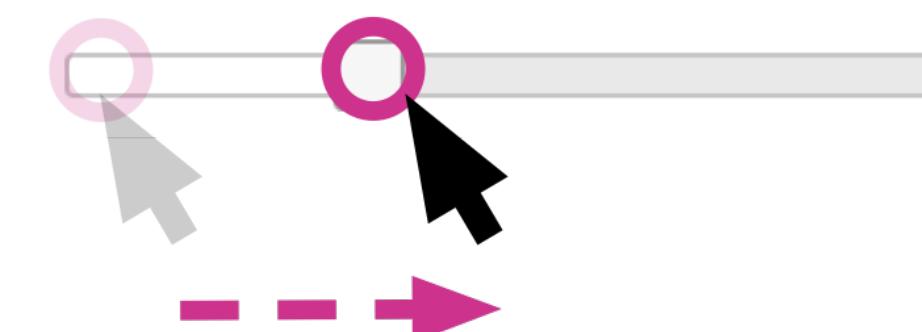
- ✓ call `accumulate(add, 0, 5, identity)`
- ✓ `total = 0`
- › `total = 2`
- › `total = 4`
- › `total = 6`
- › `total = 8`
- › `total = 10`
- › `accumulate(add, 0, 5, identity)` returns `10`



## Result

```
accumulate(add, 0, 5, identity) # 0 + 1 + 2 + :  
>>> 10
```

- ✓ call `accumulate(add, 0, 5, identity)`
- ✓ `total = base`
- › `total = add(1, 1)`
- › `total = add(2, 2)`
- › `total = add(3, 3)`
- › `total = add(4, 4)`
- › `total = add(5, 5)`
- › `accumulate(add, 0, 5, identity)` returns `total`



# Evaluation

# TraceDiff ↔ PythonTutor

**17** participants

**4** problems (2: TraceDiff, 2: PythonTutor)

**2** tasks for each problem:

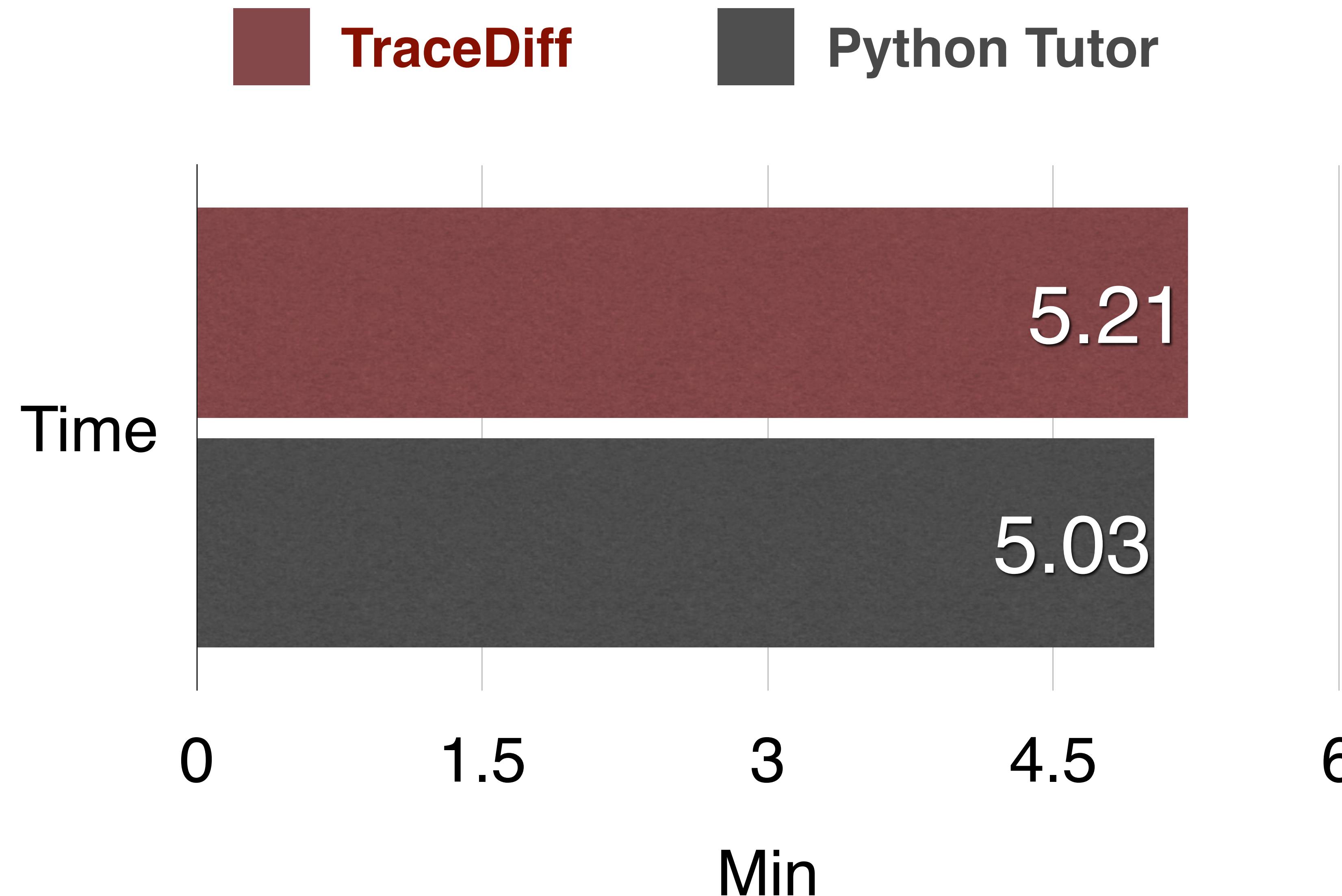
- **Identify** the bug
- **Fix** the bug

**RQ1:** Can TraceDiff help students fix bugs **faster** than Python Tutor?

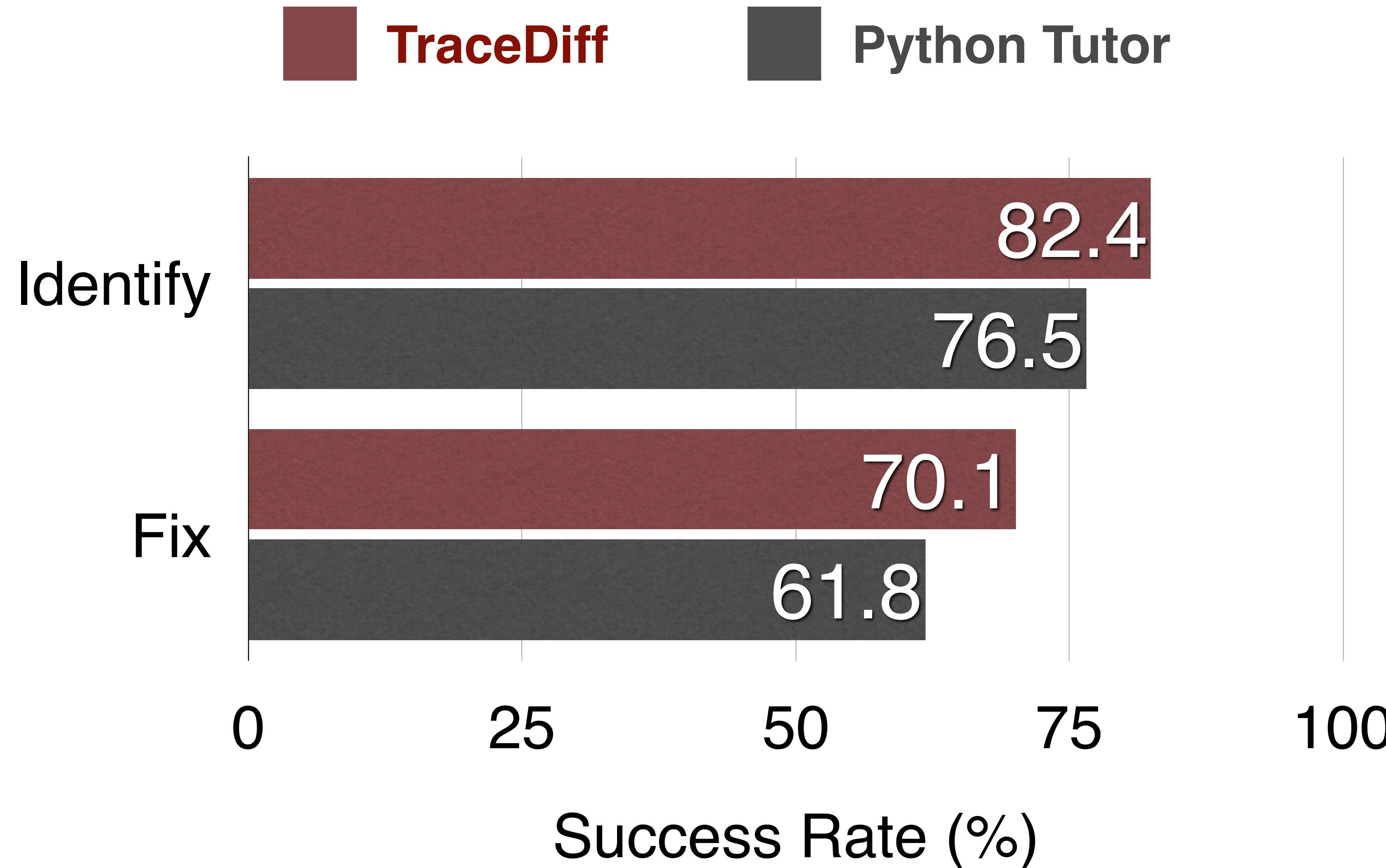
**RQ2:** Can TraceDiff help students identify and fix **more bugs** than Python Tutor?

**RQ3:** Do students perceive TraceDiff to be **more useful** for debugging tasks?

# RQ1: Can students fix bugs **faster**?



# RQ2: Can students identify and fix **more bugs**?



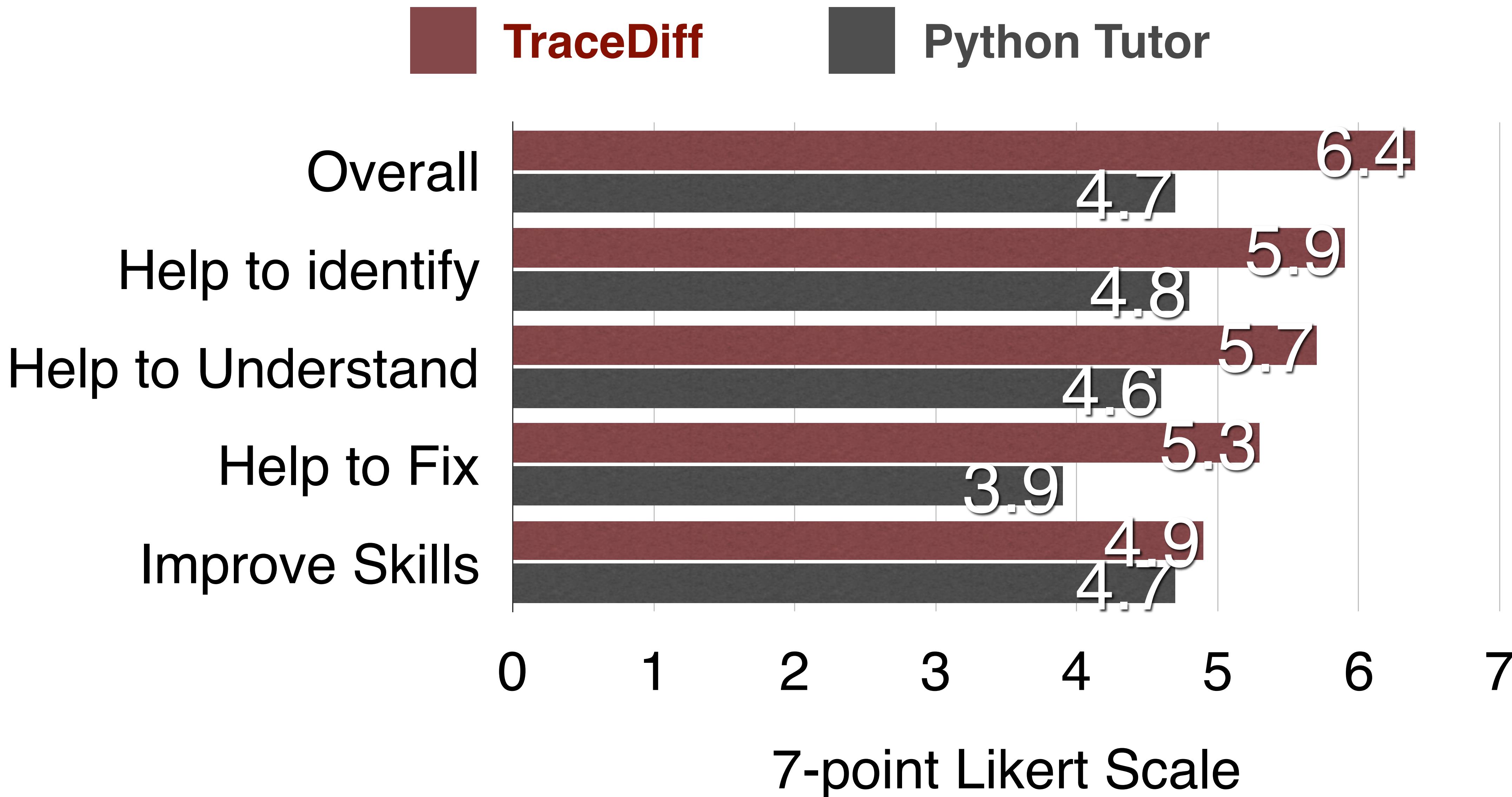
# Discussion

Task Selection: **Simple ↔ Complex**

## Discussion

Task Setting: **Single**  $\leftrightarrow$  **Multiple** Attempts

# RQ3: Do students think the tool is **more useful**?



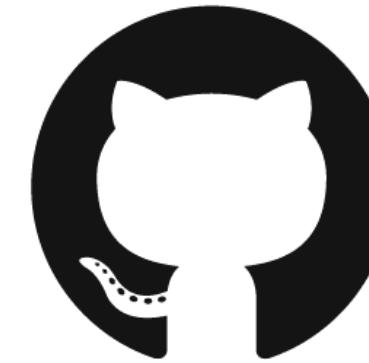
# **Future Work**

## Future Work

**Deploy** to actual programming courses  
and  
**Evaluate** in more realistic situation

# Contributions:

1. **A characterization of key design guidelines** for effective programming feedback that can be generated by state-of-the-art synthesis techniques, informed by a formative study.
2. **The implementation of hints in an interactive debugging interface**, appropriate for deployment and evaluation in a massive programming classroom.
3. **Quantitative and qualitative results of a controlled experiment with 17 students** where we compare TraceDiff with Python Tutor interface.



# GitHub ryosuzuki/trace-diff

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TraceDiff: Debugging Unexpected Code Behavior Using Trace Divergences [VL/HCC 2017]

<https://ryosuzuki.github.io/trace-diff/>

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219 commits

2 branches

2 releases

1 contributor

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ryosuzuki Update README.md

Latest commit 11f24e0 on Aug 14

data

Rebuild

2 months ago

resources

Add resources

2 months ago

**Thank you**















How can we turn  
the synthesized information into  
**more pedagogically useful**  
**higher-level** feedback?



```
accumulate(add, 0, 5, identity)
```

```
x 14 # 0 + + 2 + 3 + 4 + 5
```

```
o 15 # 0 + 1 + 2 + 3 + 4 + 5
```

# Test Case Feedback is Scalable

## Student Code

```
1 def product(n, term):  
2     total, k = 0, 1  
3     while k <= n:  
4         total, k = total * term(k), k + 1  
5     return total  
6
```

## Test Results

Test	Input	Result	Expected	Output
1	(3, lambda x: x),	→ 0	6	
2	(5, lambda x: x),	→ 0	120	
3	(3, lambda x: x * x),	→ 0	36	
4	(5, lambda x: x * x),	→ 0	14400	

# Test Case Feedback does not Provide Scaffolds

## Student Code

```
1 def product(n, term):  
2     total, k = 0, 1  
3     while k <= n:  
4         total, k = total * term(k),  
5     return total  
6
```

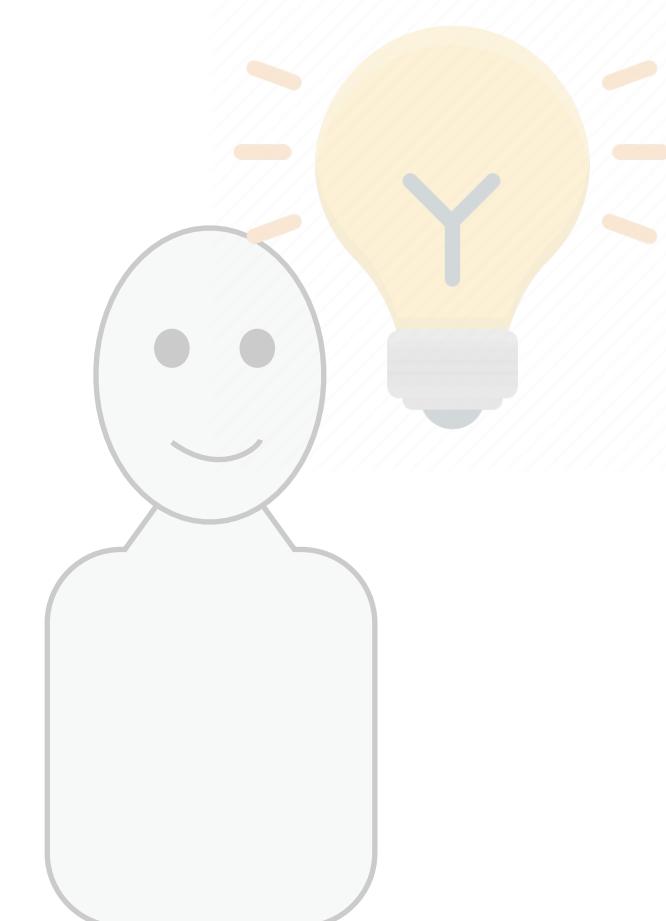
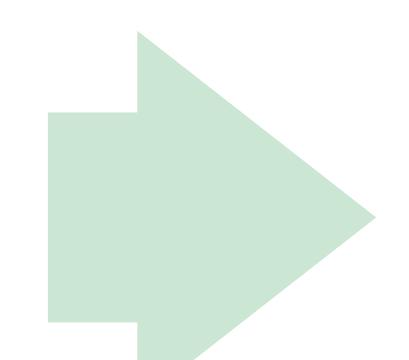
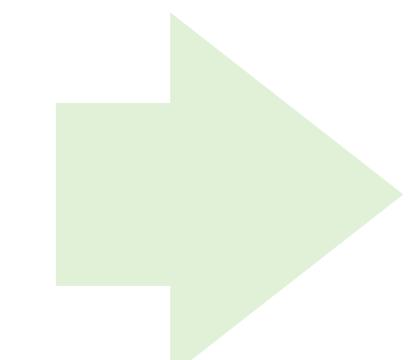
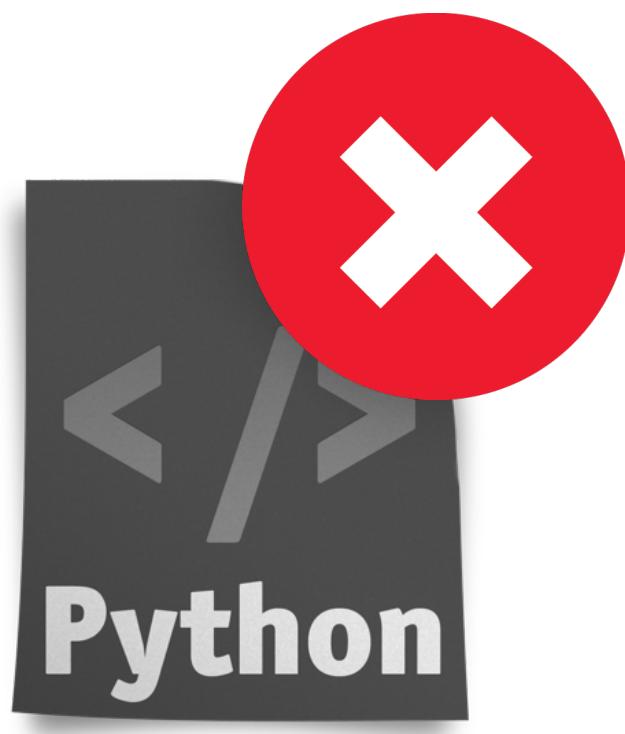
## Test Results

Test	Input	R <sub>i</sub>	Output
1	(3, lambda x: x),	→ 0	6
2	(5, lambda x: x),	→ 0	120
3	(3, lambda x: x * x),	→ 0	36
4	(5, lambda x: x * x),	→ 0	14400



# Program Synthesis Feedback

```
1 def product(n, term):  
2     total, k = 0, 1  
3     while k <= n:  
4         total, k = total * term(k), k + 1  
5     return total  
6
```

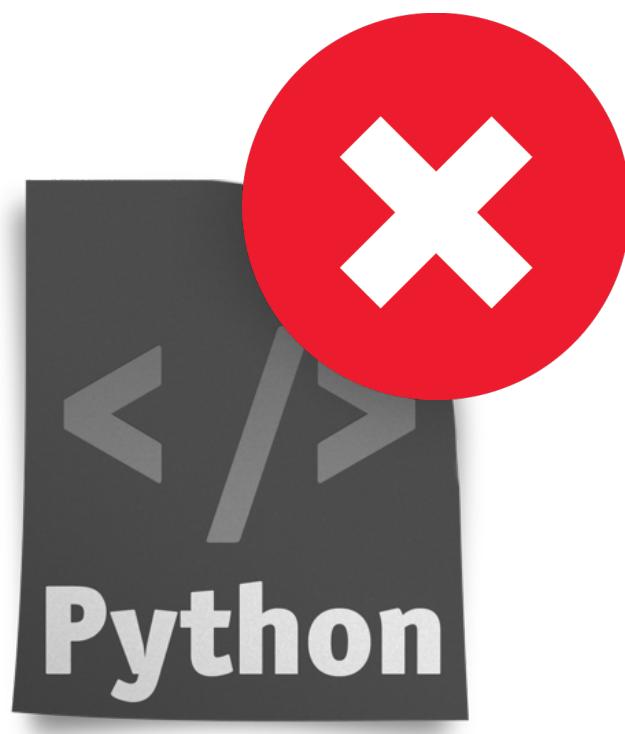


Program Synthesis

Personalized Hints

# Program Synthesis Feedback

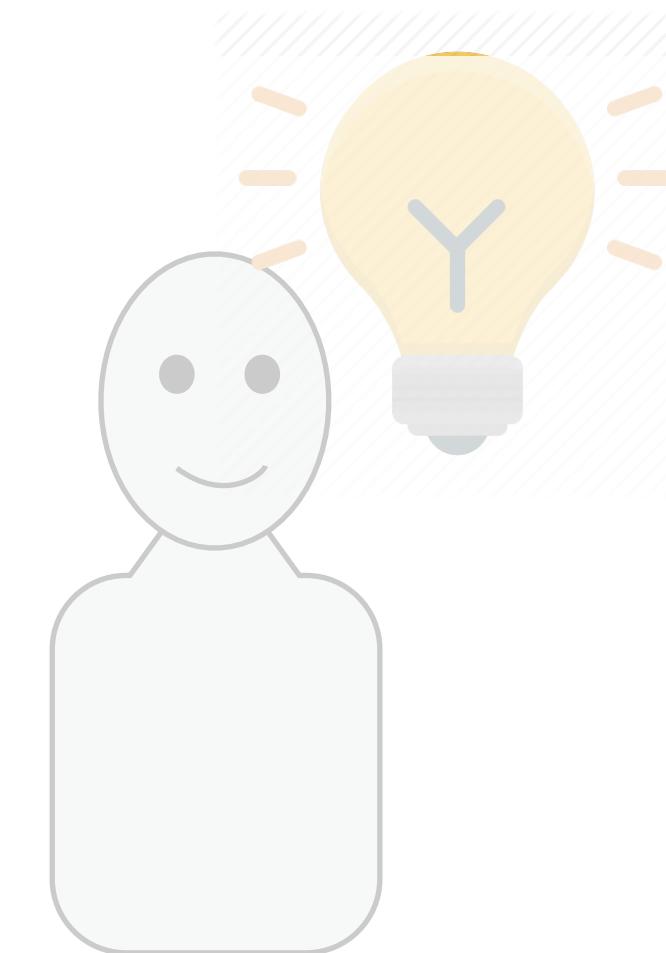
```
1 def product(n, term):  
2     total, k = 0, 1  
3     while k <= n:  
4         total, k = total * term(k), k + 1  
5     return total  
6
```



Program Synthesis



Personalized Hints



# Program Synthesis Feedback

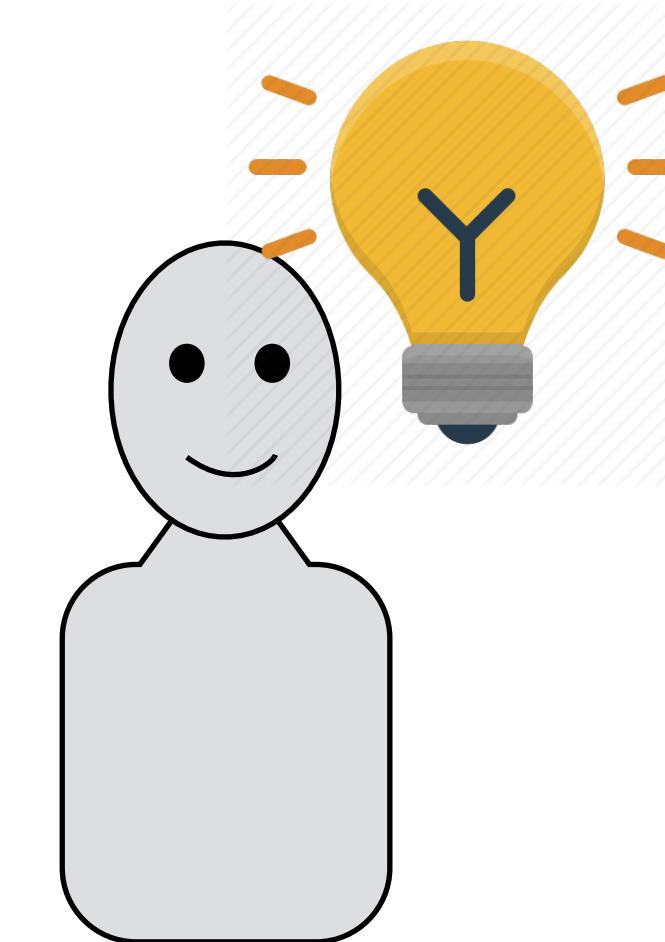
```
1 def product(n, term):  
2     total, k = 0, 1  
3     while k <= n:  
4         total, k = Line 2 needs to be changed  
5     return total  
6
```



Program Synthesis



Personalized Hints

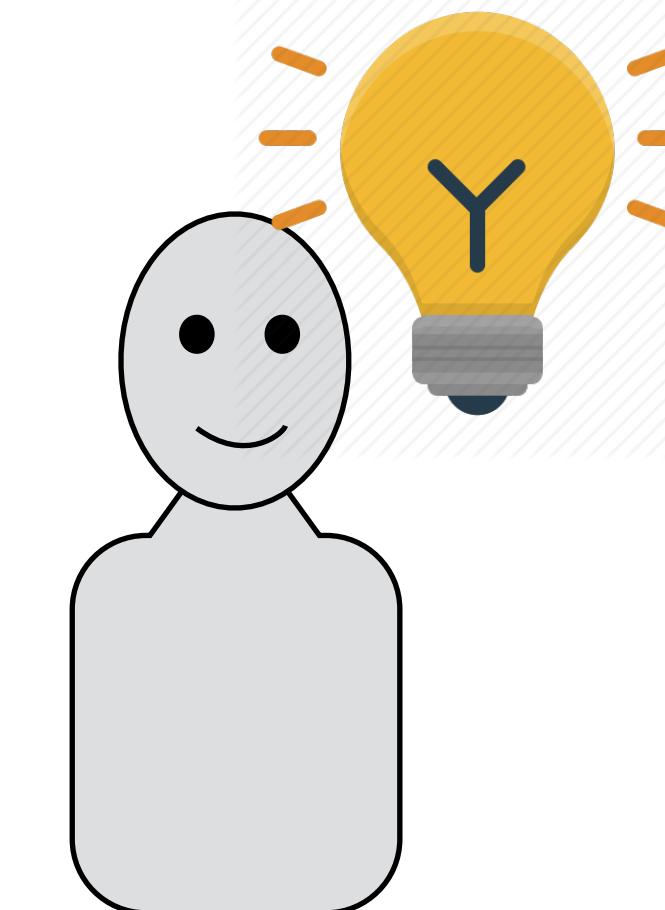
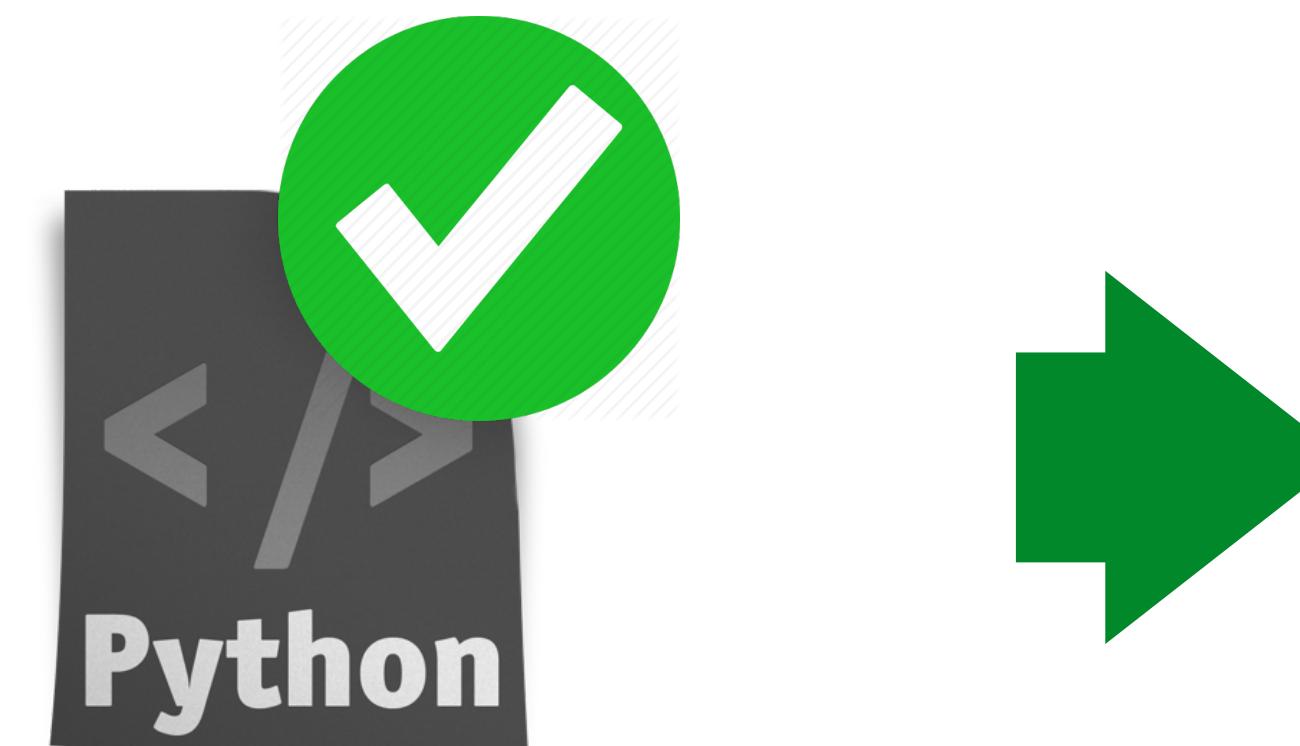
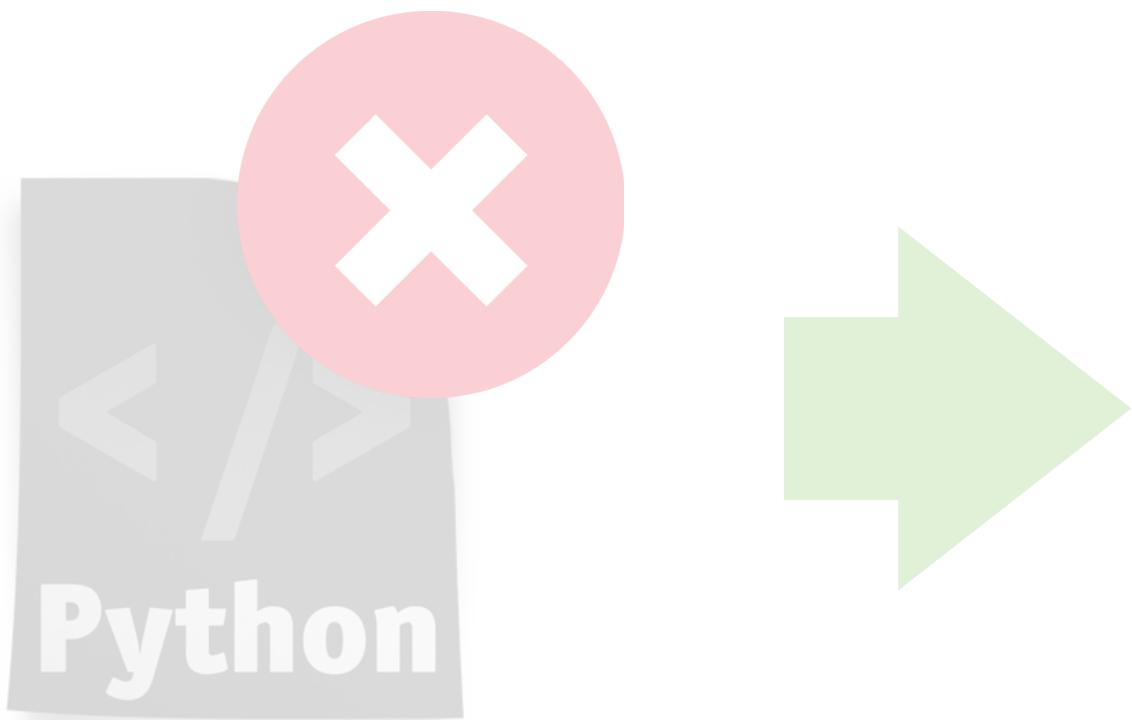


# Program Synthesis Feedback

```
1 def product(n, term):  
2     total, k = 0, 1  
3     while k <= n:  
4         total, k = Line 2 needs to be changed  
5         return total  
6
```

Line 2 needs to be changed

In line 2, change total = 0 to total = 1



Program Synthesis

Personalized Hints

# Program Synthesis Feedback

Pointing

Line 2 needs to be changed

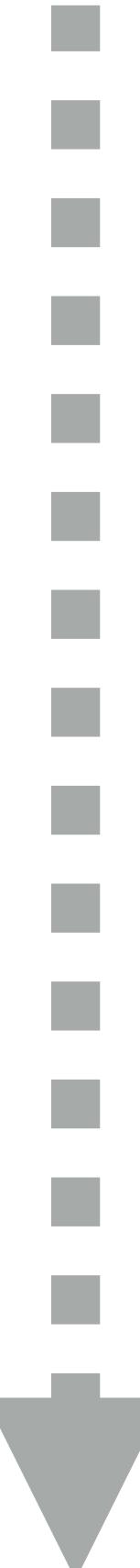
In line 2, check total

High-level  
Hints

?

Bottom-out

In line 2, change total = 0 to total = 1



# Program Synthesis Feedback

Pointing

Line 2 needs to be changed

In line 2, check total

High-level  
Hints

How can we turn  
the synthesized information into  
**more pedagogically useful,  
higher-level feedback?**

Bottom-out

In line 2, change total = 0 to total = 1

```
def accumulate(combiner, base, n, term):  
    total = base  
    i = 1  
    while i<=n:  
        total = combiner(i, term(i))  
        total = combiner(total, term(i))  
        i = i+1  
    return total
```

---

**Test**

```
accumulate(add, 0, 5, identity)  
x 10 # 5 + 5  
o 15 # 0 + 1 + 2 + 3 + 4 + 5
```

# **Record and Filter Code Traces**

1. Function Call
2. Variable Assignment
3. Return Statement

TraceDiff Ryo

Secure | https://ryosuzuki.github.io/trace-diff/?type=accumulate&id=10

Python 2.7      Frames      Objects

```
1 def accumulate(combiner, base, n, term):  
2     if n==1:  
3         return base  
4     else:  
5         return combiner(term(n), accumulate(  
6  
7 def add(a, b):  
8     return a + b  
9  
10 def identity(x):  
11    return x  
12  
13 accumulate(add, 0, 5, identity)
```

Line that has just executed      Next line to execute

Result

```
accumulate(add, 0, 5, identity) # 0 + 1 + 2 + 3 + 4 + 5  
>>> 14
```

✓ call accumulate(add, 0, 5, identity)  
✓ n = 5  
✓ call accumulate(add, 0, 4, identity)  
✓ n = 4  
✓ call accumulate(add, 0, 3, identity)  
✓ n = 3  
✓ call accumulate(add, 0, 2, identity)  
✓ n = 2  
✓ call accumulate(add, 0, 1, identity)  
✓ n = 1  
> accumulate(add, 0, 1, identity) returns 0  
> n = 2  
> accumulate(add, 0, 2, identity) returns 2  
> n = 3  
> accumulate(add, 0, 3, identity) returns 5  
> n = 4  
> accumulate(add, 0, 4, identity) returns 9  
> n = 5  
> accumulate(add, 0, 5, identity) returns 14

Expected

```
accumulate(add, 0, 5, identity) # 0 + 1 + 2 + 3 + 4 + 5  
>>> 15
```

✓ call accumulate(add, 0, 5, identity)  
✓ n = 5  
✓ call accumulate(add, 0, 4, identity)  
✓ n = 4  
✓ call accumulate(add, 0, 3, identity)  
✓ n = 3  
✓ call accumulate(add, 0, 2, identity)  
✓ n = 2  
✓ call accumulate(add, 0, 1, identity)  
✓ n = 1  
> call accumulate(add, 0, 0, identity)  
> n = 0  
> accumulate(add, 0, 0, identity) returns 0  
> n = 1  
> accumulate(add, 0, 1, identity) returns 1  
> n = 2  
> accumulate(add, 0, 2, identity) returns 3  
> n = 3  
> accumulate(add, 0, 3, identity) returns 6  
> n = 4  
> accumulate(add, 0, 4, identity) returns 10  
> n = 5  
> accumulate(add, 0, 5, identity) returns 15

< Back Step 1 of 48 Forward >

TraceDiff Ryo

Secure | <https://ryosuzuki.github.io/trace-diff/?type=accumulate&id=272>

Python 2.7    Frames    Objects

```
1 def accumulate(combiner, base, n, term):
2     if n==0:
3         return base
4     else:
5         k = term(n)
6         return combiner(base, combiner(accumu
7
8 def add(a, b):
9     return a + b
10
11 def identity(x):
12     return x
13
14 accumulate(add, 11, 5, identity)
```

line that has just executed  
next line to execute

< Back Step 1 of 78 Forward >

**Result**

```
accumulate(add, 11, 5, identity) # 11 + 1 + 2 + 3 + 4 + 5
>>> 81
```

- ✓ call accumulate(add, 11, 5, identity)
- ✓ call accumulate(add, 11, 4, identity)
- ✓ call accumulate(add, 11, 3, identity)
- ✓ call accumulate(add, 11, 2, identity)
- ✓ call accumulate(add, 11, 1, identity)
- ✓ call accumulate(add, 11, 0, identity)
- ✓ accumulate(add, 11, 0, identity) returns 11
- > accumulate(add, 11, 1, identity) returns 23
- > accumulate(add, 11, 2, identity) returns 36
- > accumulate(add, 11, 3, identity) returns 50
- > accumulate(add, 11, 4, identity) returns 65
- > accumulate(add, 11, 5, identity) returns 81

**Expected**

```
accumulate(add, 11, 5, identity) # 11 + 1 + 2 + 3 + 4 + 5
>>> 26
```

- ✓ call accumulate(add, 11, 5, identity)
- ✓ call accumulate(add, 11, 4, identity)
- ✓ call accumulate(add, 11, 3, identity)
- ✓ call accumulate(add, 11, 2, identity)
- ✓ call accumulate(add, 11, 1, identity)
- ✓ call accumulate(add, 11, 0, identity)
- ✓ accumulate(add, 11, 0, identity) returns 11
- > accumulate(add, 11, 1, identity) returns 12
- > accumulate(add, 11, 2, identity) returns 14
- > accumulate(add, 11, 3, identity) returns 17
- > accumulate(add, 11, 4, identity) returns 21
- > accumulate(add, 11, 5, identity) returns 26

**Result**

```
accumulate(add, 11, 5, identity) # 11 + 1 + 2 + 3  
>>> 81
```

- ✓ call `accumulate(add, 11, 5, identity)`
- ✓ call `accumulate(add, 11, 4, identity)`
- ✓ call `accumulate(add, 11, 3, identity)`
- ✓ call `accumulate(add, 11, 2, identity)`
- ✓ call `accumulate(add, 11, 1, identity)`
- ✓ call `accumulate(add, 11, 0, identity)`
- ✓ `accumulate(add, 11, 0, identity)` returns 11
  - > `accumulate(add, 11, 1, identity)` returns 23
  - > `accumulate(add, 11, 2, identity)` returns 36
  - > `accumulate(add, 11, 3, identity)` returns 50
  - > `accumulate(add, 11, 4, identity)` returns 65
  - > `accumulate(add, 11, 5, identity)` returns 81

**A****Expected**

```
accumulate(add, 11, 5, identity) # 11 + 1 + 2 + 3  
>>> 26
```

- ✓ call `accumulate(add, 11, 5, identity)`
- ✓ call `accumulate(add, 11, 4, identity)`
- ✓ call `accumulate(add, 11, 3, identity)`
- ✓ call `accumulate(add, 11, 2, identity)`
- ✓ call `accumulate(add, 11, 1, identity)`
- ✓ call `accumulate(add, 11, 0, identity)`
- ✓ `accumulate(add, 11, 0, identity)` returns 11
  - > `accumulate(add, 11, 1, identity)` returns 12
  - > `accumulate(add, 11, 2, identity)` returns 14
  - > `accumulate(add, 11, 3, identity)` returns 17
  - > `accumulate(add, 11, 4, identity)` returns 21
  - > `accumulate(add, 11, 5, identity)` returns 26

**B**

## Python 2.7

```

1 def accumulate(combiner, base, n, term):
2     total = base
3     i = 1
4     while i<=n:
5         total = combiner(i, term(i))
6     i = i+1
7     return total
8
9 def add(a, b):
10    return a + b
11
12 def identity(x):
13     return x
14
15 accumulate(add, 0, 5, identity)

```

→ line that has just executed

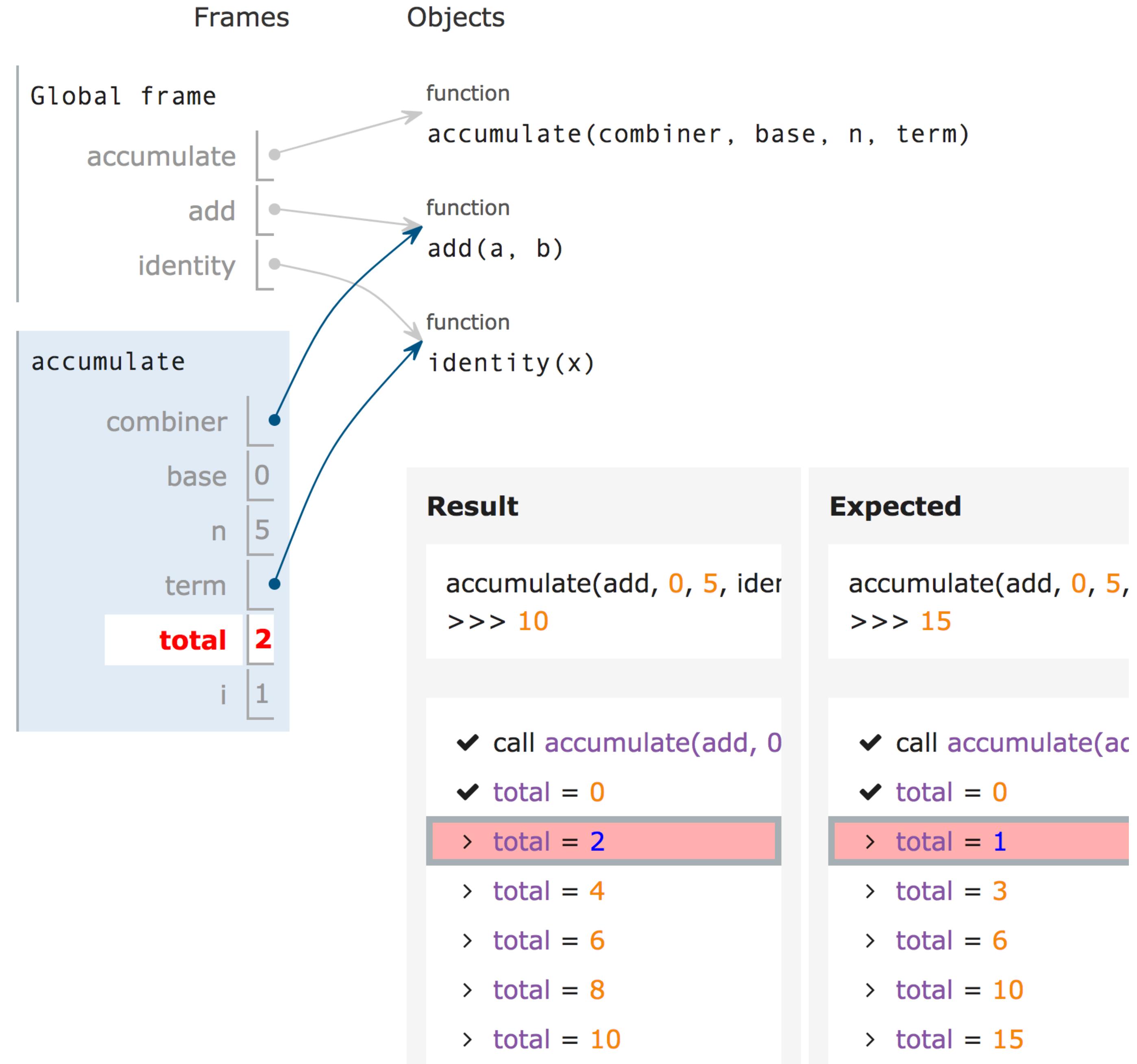
→ next line to execute



< Back

Step 16 of 55

Forward >



**Code**

```
def accumulate(combiner, base, n, term):  
    total = base  
    i = 1  
    while i<=n:  
        total = combiner(i, term(i))  
        total = combiner(total, term(i))  
        i = i+1  
    return total
```

---

**Test**

```
accumulate(add, 0, 5, identity)  
x 10  
o 15
```

D1: Encourage students to explore code execution with a visual debugger

D2: Describe how actual behavior differs from expected behavior

D3: Refer to concrete code locations and behavior to provide a starting point for exploration

**Result**

```
accumulate(add, 0, 5, identity) # 0 + 1 + 2 + 3 +  
>>> 14
```

- ✓ call accumulate(add, 0, 5, identity)
- ✓ n = 5
- ✓ call accumulate(add, 0, 4, identity)
- ✓ n = 4
- ✓ call accumulate(add, 0, 3, identity)
- ✓ n = 3
- ✓ call accumulate(add, 0, 2, identity)
- ✓ n = 2
- ✓ call accumulate(add, 0, 1, identity)
- ✓ n = 1
  - > accumulate(add, 0, 1, identity) returns 0
  - > n = 2
  - > accumulate(add, 0, 2, identity) returns 2
  - > n = 3
  - > accumulate(add, 0, 3, identity) returns 5
  - > n = 4
  - > accumulate(add, 0, 4, identity) returns 9
  - > n = 5
  - > accumulate(add, 0, 5, identity) returns 14

**Expected**

```
accumulate(add, 0, 5, identity) # 0 + 1 + 2 + 3 +  
>>> 15
```

- ✓ call accumulate(add, 0, 5, identity)
- ✓ n = 5
- ✓ call accumulate(add, 0, 4, identity)
- ✓ n = 4
- ✓ call accumulate(add, 0, 3, identity)
- ✓ n = 3
- ✓ call accumulate(add, 0, 2, identity)
- ✓ n = 2
- ✓ call accumulate(add, 0, 1, identity)
- ✓ n = 1
  - > call accumulate(add, 0, 0, identity)
  - > n = 0
  - > accumulate(add, 0, 0, identity) returns 0
  - > n = 1
  - > accumulate(add, 0, 1, identity) returns 1
  - > n = 2
  - > accumulate(add, 0, 2, identity) returns 3
  - > n = 3
  - > accumulate(add, 0, 3, identity) returns 6
  - > n = 4
  - > accumulate(add, 0, 4, identity) returns 10
  - > n = 5
  - > accumulate(add, 0, 5, identity) returns 15

Python 2.7

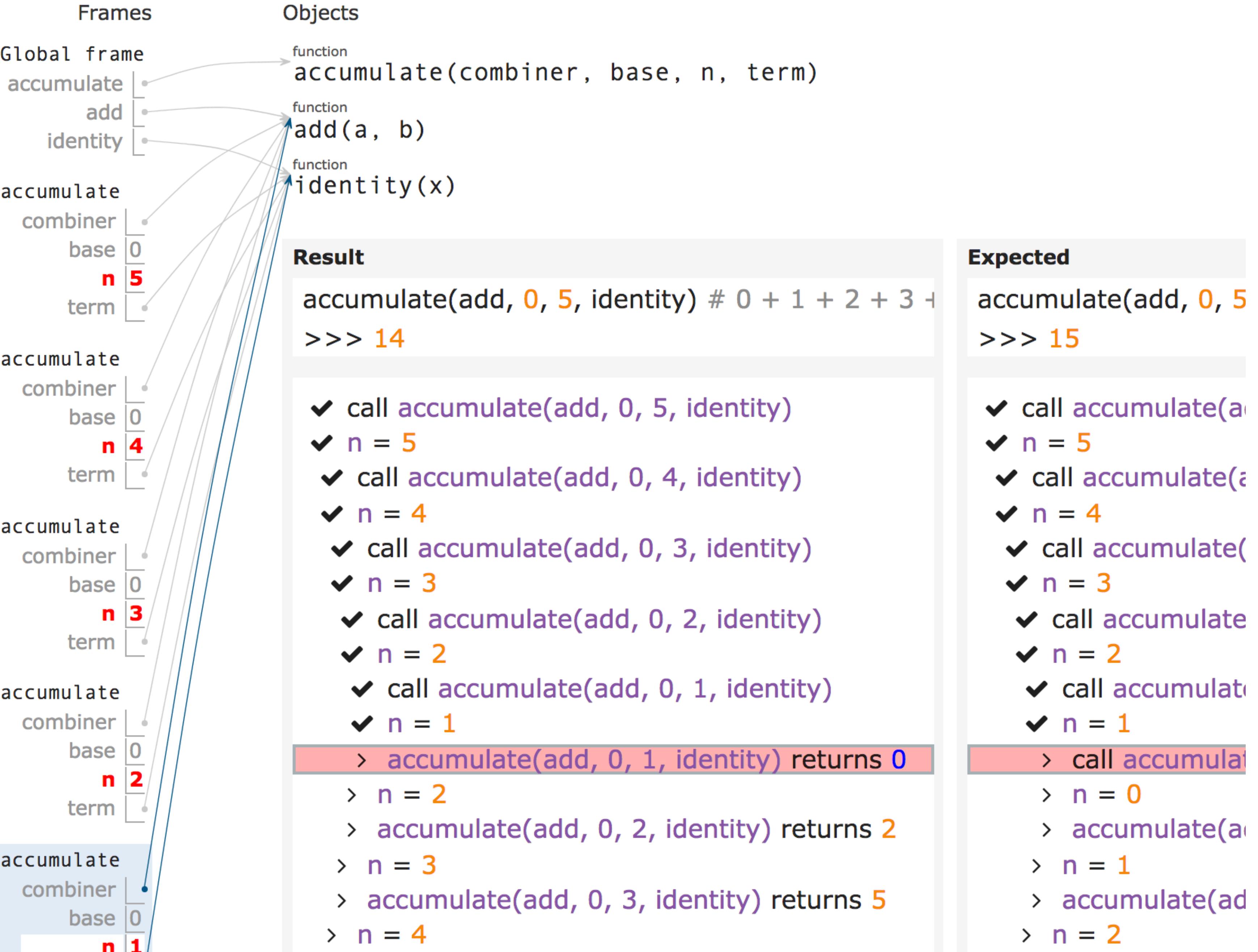
```

1 def accumulate(combiner, bas
2     if n==1:
3         return base
4     else:
5         return combiner(term(n),
6
7 def add(a, b):
8     return a + b
9
10 def identity(x):
11     return x
12
13 accumulate(add, 0, 5, identi

```

line that has just executed  
next line to execute

&lt; Back Step 32 of 48 Forward &gt;



**Result**

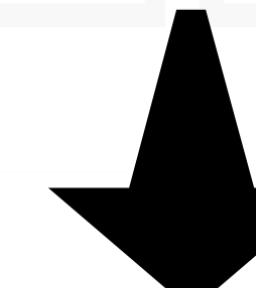
```
accumulate(add, 0, 5, identity) # 0 + 1 + 2 + :  
>>> 10
```

✓ call accumulate(add, 0, 5, identity)  
✓ total = 0  
› total = 2  
› total = 4  
› total = 6  
› total = 8  
› total = 10  
› accumulate(add, 0, 5, identity) returns 10

**Expected**

```
accumulate(add, 0, 5, identity) # 0 + 1 + 2 + :  
>>> 15
```

✓ call accumulate(add, 0, 5, identity)  
✓ total = 0  
› total = 1  
› total = 3  
› total = 6  
› total = 10  
› total = 15  
› accumulate(add, 0, 5, identity) returns 15



**A**

**Result**

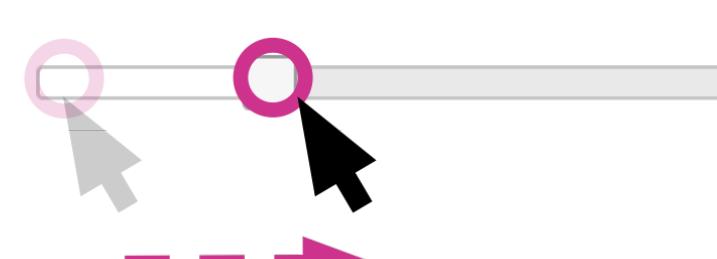
```
accumulate(add, 0, 5, identity) # 0 + 1 + 2 + :  
>>> 10
```

✓ call accumulate(add, 0, 5, identity)  
✓ total = base  
› total = add(1, 1)  
› total = add(2, 2)  
› total = add(3, 3)  
› total = add(4, 4)  
› total = add(5, 5)  
› accumulate(add, 0, 5, identity) returns total

**Expected**

```
accumulate(add, 0, 5, identity) # 0 + 1 + 2 + :  
>>> 15
```

✓ call accumulate(add, 0, 5, identity)  
✓ total = base  
› total = add(0, 1)  
› total = add(1, 2)  
› total = add(3, 3)  
› total = add(6, 4)  
› total = add(10, 5)  
› accumulate(add, 0, 5, identity) returns total



**B**