

We therefore predict that the CO<sub>2</sub> level will exceed 400 ppm by the year 2019. This prediction is somewhat risky because it involves a time quite remote from our observations.

## POLYNOMIALS

A function  $P$  is called a **polynomial** if

$$P(x) = a_n x^n + a_{n-1} x^{n-1} + \cdots + a_2 x^2 + a_1 x + a_0$$

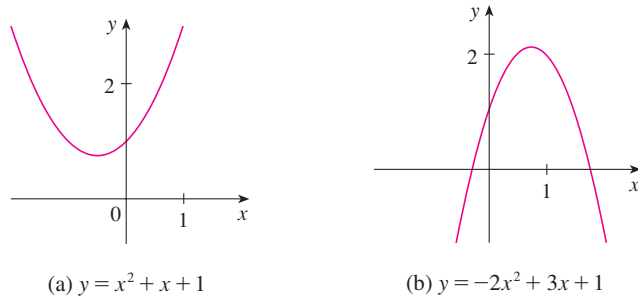
where  $n$  is a nonnegative integer and the numbers  $a_0, a_1, a_2, \dots, a_n$  are constants called the **coefficients** of the polynomial. The domain of any polynomial is  $\mathbb{R} = (-\infty, \infty)$ . If the leading coefficient  $a_n \neq 0$ , then the **degree** of the polynomial is  $n$ . For example, the function

$$P(x) = 2x^6 - x^4 + \frac{2}{5}x^3 + \sqrt{2}$$

is a polynomial of degree 6.

A polynomial of degree 1 is of the form  $P(x) = mx + b$  and so it is a linear function. A polynomial of degree 2 is of the form  $P(x) = ax^2 + bx + c$  and is called a **quadratic function**. Its graph is always a parabola obtained by shifting the parabola  $y = ax^2$ , as we will see in the next section. The parabola opens upward if  $a > 0$  and downward if  $a < 0$ . (See Figure 7.)

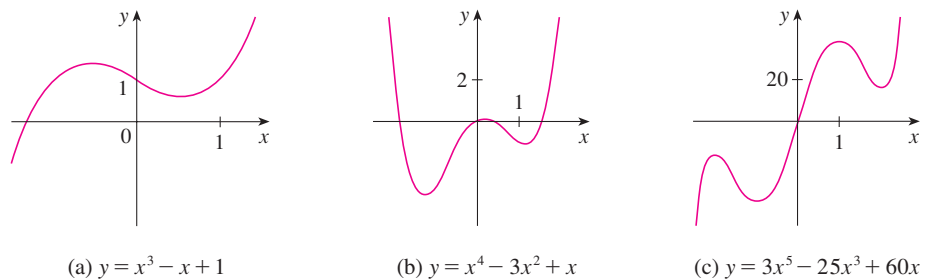
**FIGURE 7**  
The graphs of quadratic functions are parabolas.



A polynomial of degree 3 is of the form

$$P(x) = ax^3 + bx^2 + cx + d \quad (a \neq 0)$$

and is called a **cubic function**. Figure 8 shows the graph of a cubic function in part (a) and graphs of polynomials of degrees 4 and 5 in parts (b) and (c). We will see later why the graphs have these shapes.



**FIGURE 8**