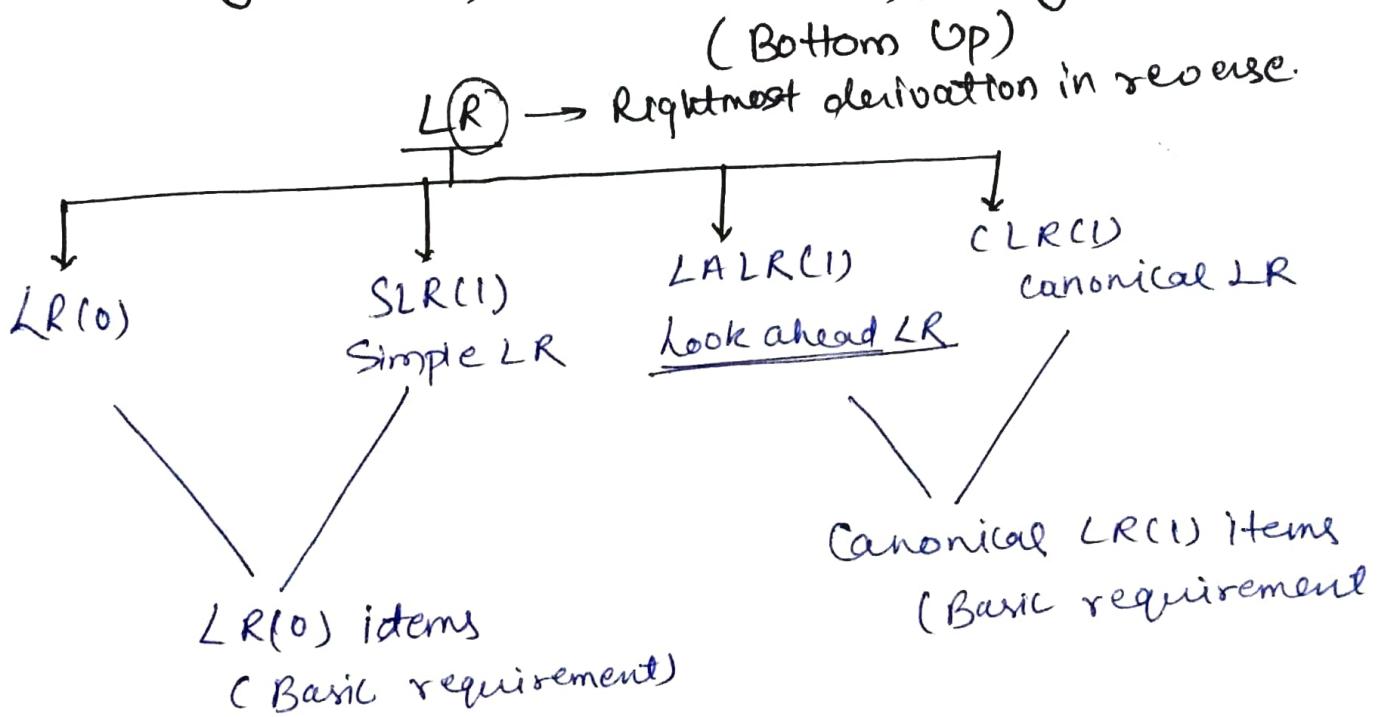


LR Parsing, LR(0), items and LR(0) parsing table



Ex

$$\begin{aligned} S &\rightarrow AA \\ A &\rightarrow aA \mid b \\ &\downarrow S' \rightarrow S \end{aligned}$$

LR(0) Parsing table

- closure
- goto

Augmented Grammar

- ① $S' \rightarrow S$
- ② $S \rightarrow AA$
- ③ $A \rightarrow aA \mid b$

→ Just add one production
to make it augmented

at beginning

Any production with dot ↑ called as $LR(0)$ item.

$$\underline{S \rightarrow \cdot AA}$$

Position of dot can be changed as -

$S \rightarrow \cdot A A \rightarrow$ Not seen anything on RHS [LR(0) item]

$S \rightarrow A \cdot A \rightarrow$ seen A on RHS

$S \rightarrow AA$. → seen everything from RNS. [final item]

Steps

Steps

- ① $S \rightarrow S$: As you see ":" in the beginning of product then include all production derived from variable on RHS of ":" and their respective production

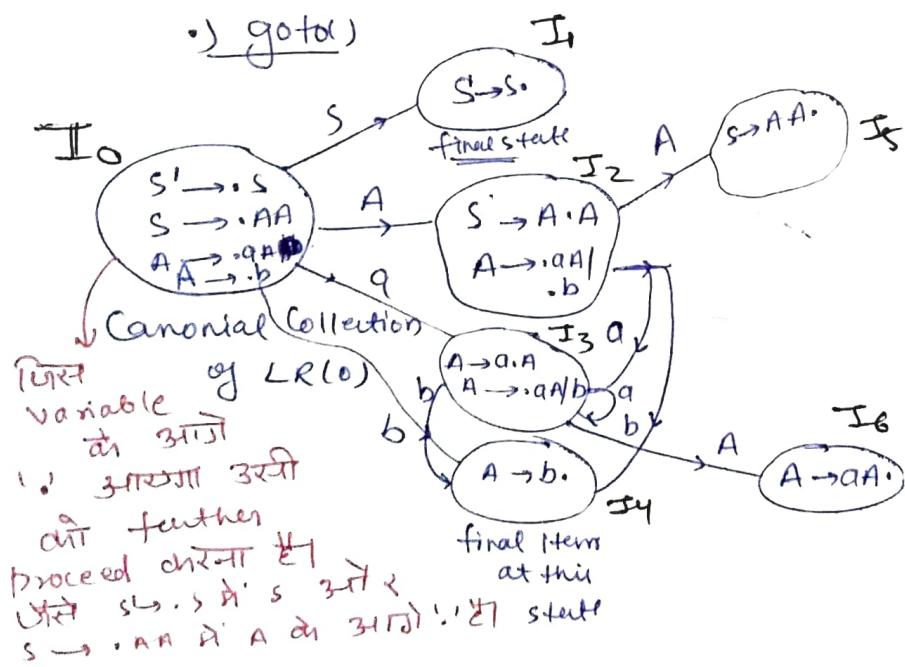
•) Closure of item: $S^* \rightarrow S^*$ is

$$S' \rightarrow S$$

$S \rightarrow \cdot AA$

$A \rightarrow .aA \mid .b$] Respective production

• gotor()



Move 'i' to one
step RHS and
find closure

$I_0 \rightarrow I_6$ (7 states)

→ Same level

पर indexing

level पर आगे बढ़ो

LR(0) Parsing Table

I	(a) Action	(b)	Goto(A)	(S)
0.	s_3	s_4	2	1
		accepting		
1				
2	s_3	s_4	5	
3	s_3	s_4	6	
4	τ_3	τ_3	τ_3	7
5	τ_1	τ_1	τ_1	
6	τ_2	τ_2	τ_2	

We accept
the I_1 because
it derives
from augmented
production specially
added to it.
So, I_1 needs to
accepts

Points to Remember

•) Assume

$$\left. \begin{array}{l} S \rightarrow AA. \rightarrow r_1 \\ A \rightarrow aA. \rightarrow r_2 \\ A \rightarrow b. \rightarrow r_3 \end{array} \right\} \text{reduced move}$$

$S_3 \rightarrow$ Shift on 3: we will do shift operation on looking a terminal from any set of production

$S_3 \rightarrow$ means I₀ on a shifts to I₃

we use numerics in case of showing transitions for variables
as.

Goto(A): 2 means I₀ on 'A' moves to I₂.

This way we use different notations for both terminal and variables.

Since I₄, I₅, I₆ are final reduced states so we consider the productions whose finally reduced form represent by the state.

Ex, $A \rightarrow b$ is r_3 its reduced move is $A \rightarrow b.$ and it is accepted by I₄.

So 4 number entry contain r_3 in all columns.

This way a complete table is designed.

LR(0) Parsing example and SLR(1) table

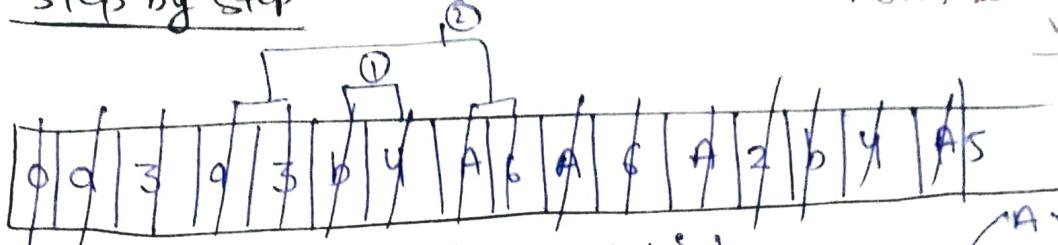
Example : $S' \rightarrow S$
 $S \rightarrow AA$
 $A \rightarrow aA \mid b$

LR(0) Parsing table for given grammar prepared on previous page (backside)

String $w = \underline{aabbb} \$$

Step by step

→ If don't understand by notes watch the video



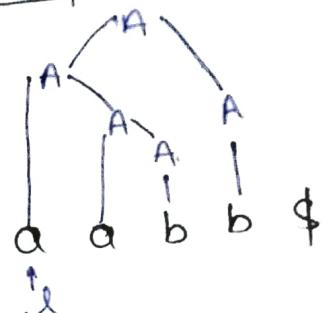
Start from start0 and first symbol 'a'

① $0 \xrightarrow{a} 3$ (increment pointer)

② $3 \xrightarrow{a} 3$ (increment l)

③ $3 \xrightarrow{b} 4$ (increment l)

④ $4 \xrightarrow{b} r_3$ ($A \rightarrow b$)



Reduce $b \rightarrow A$ and then Push A in the stack. We are reducing the previous b (before 4) not current pointing b.

If in reduced production (r) have n elements on RHS then pop ($2n$) elements from stack.

No. of element on RHS means Ex →

$A \rightarrow a \rightarrow 1$ element on RHS (a)

$A \rightarrow aB \rightarrow 2$ element on RHS.

So reduced symbol $b \rightarrow q$ and pop 2 symbols from stack.

⑤ $3 \xrightarrow{A} 6$ (Pointer on b)

⑥ $6 \xrightarrow{b} r_2$ ($A \rightarrow aA$) reduce and pop 4 elements.

⑦ $3 \xrightarrow{A} 6$ (Pointer on b) reduce

⑧ $6 \xrightarrow{b} r_2$ same as above and poped 4 elements

⑨ $0 \xrightarrow{A} 2$

⑩ $2 \xrightarrow{b} s_4$

⑪ $4 \xrightarrow{\$} r_3$ reduce $A \rightarrow b$

⑫ $5 \mid \$ \xrightarrow{} r_1$ $S \rightarrow AA$ (pop 4 symbols and reduce to AA)

SLR(1) → More powerful than LR(0). It also takes LR(0) items to parsing.

It avoids blind reduction. (Remaining part after next Ques) + 11. P9

Ex- $S \rightarrow dA \mid aB$

$A \rightarrow bA \mid C$

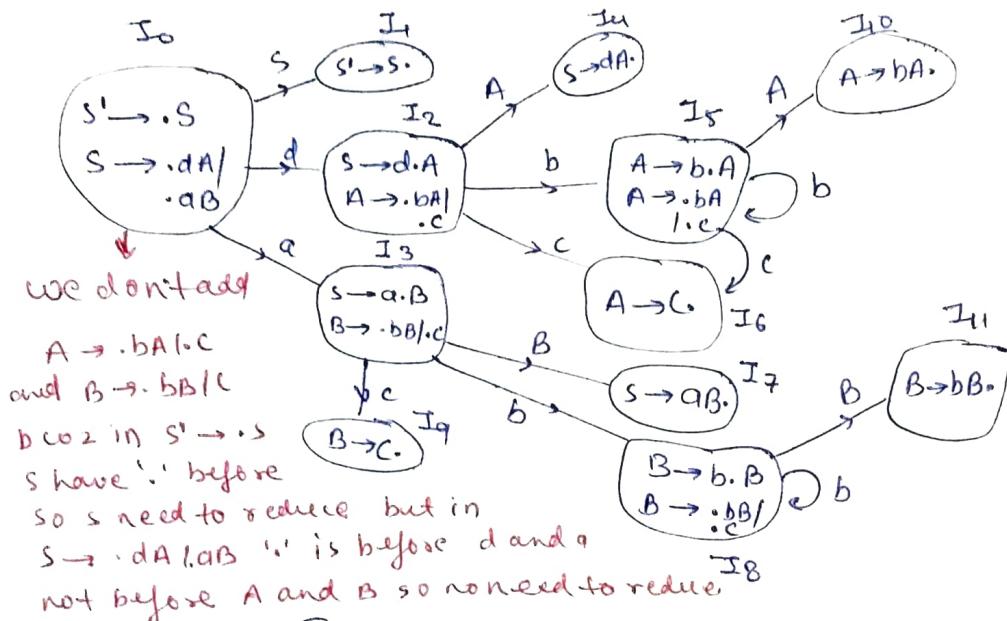
$B \rightarrow bB \mid C$

To find that Grammar is

- i) LL(1) or not
- ii) LR(0) or not
- iii) SLR(1) or not

Do this question after reading this

→ There is no 2 production which comes in same row/column on finding first(variable), so it is definitely LL(1).



Canonical Collection of LR(0) items

If grammar follows LR(0) then it must be SLR(1)
because SLR(1) is reduced form of LR(0).

The grammar is LR(0) because no final state is having any reduce move or shift move (RR | SR conflict).

final state means ' \cdot ' at the end.

Remaining part of previous question

SLR(1) says whenever there is a final state then don't put the reduce moves blindly.

SLR(1)	action			goto A S
	a	b	\$	
4	r_3	r_3	r_3	
5			r_1	
6	r_2	r_2	r_2	

A
a a b b \$
SLC(1) says that -
cont.

on reducing the variable 'b' to 'a' verify that the variable or terminal just after 'b' (here 'B') must be in follow of A otherwise don't reduce.

so $\text{follow}(A) = \{ \$, b, B \}$ → Since it contains 'b' so we can reduce $b \rightarrow A$.

Remember ↓
It can be said as $(A \rightarrow b.) : r_i$ can be placed if the variable next to 'b' (here 'B') is in follow of LHS of ' r_i '.

SLR(1) detects the error earlier than LR(0).

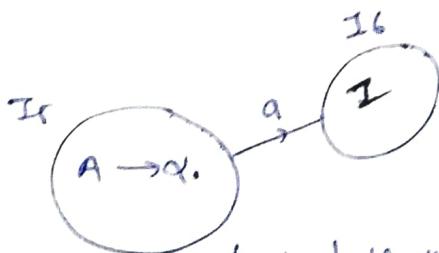
How to handle the error?

✓ Provide pointer to function on blank space . so that function can print the error message

A Grammar can't be in LR(0) due to reasons -

① SR Conflict

Ex:

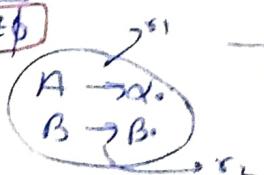


q	b
S_0/r_1	r_1

In IS we need to put both the things the reduce move and the shift moves

② RR conflict

$\text{follow}(A) \cap \text{follow}(B) \neq \emptyset$



s	a	b	c
r_1/r_2	r_1/r_2	r_1/r_2	r_1/r_2

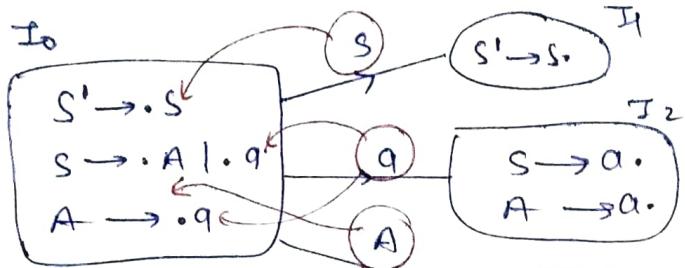
it generate the conflicts btw two reduce moves

If in Canonical LR(0) items graph there is no SR / RR Conflicts then it must be in LR(0).

~~if grammar is LR(0) then it must be SLR(1), but if grammar is not LR(0) it doesn't mean that it will not be SLR(1).~~

Ex \rightarrow S \rightarrow Alg
A \rightarrow a

① Not suitable for LL(1) bcoz $\text{first}(S) = \{a, a^y\}$ and
it is also ambiguous. ~~short notes~~



Two reduce move
in same state
so not a LR(0).

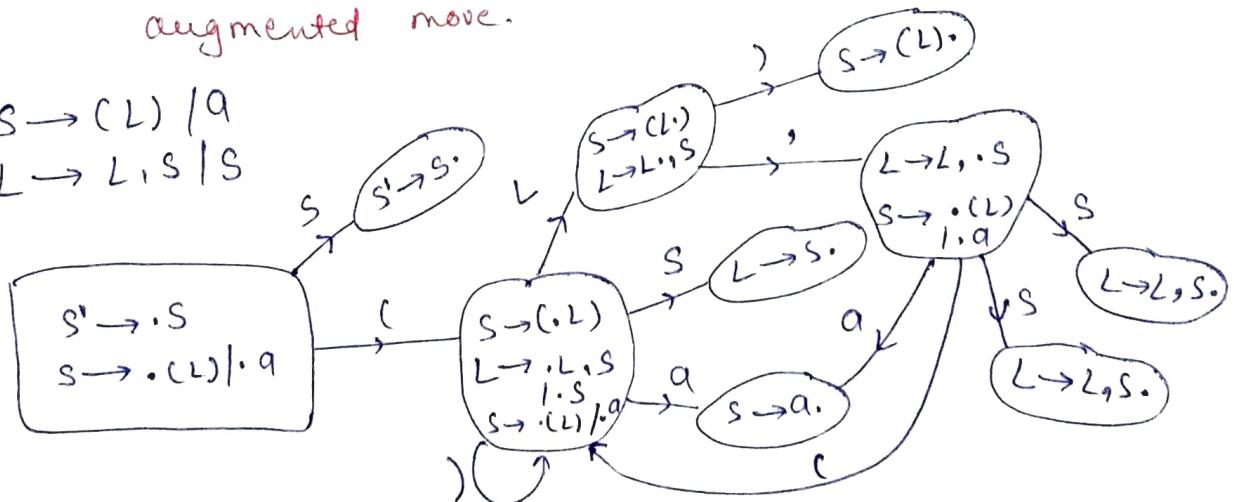
○ पिरं सिम्बोल के अनुकूल
ही उसी के According
परमा है

for SLR(1) find follow(S) = \$ and follow of (A) is \$.
 so two entries needs to placed in same column
 not possible

\rightarrow Note \rightarrow ① Left recursive grammar can't be LL(1).

② for LR(0) & LR(1) check only final states except augmented move.

$$\begin{array}{l} S \rightarrow (L) / a \\ L \rightarrow L, S / S \end{array}$$



→ Grammar is not LR(0).

→ Grammar follows LR'(0) and SLR(1).

$$F \rightarrow F + T/T$$

$$T \rightarrow^o$$

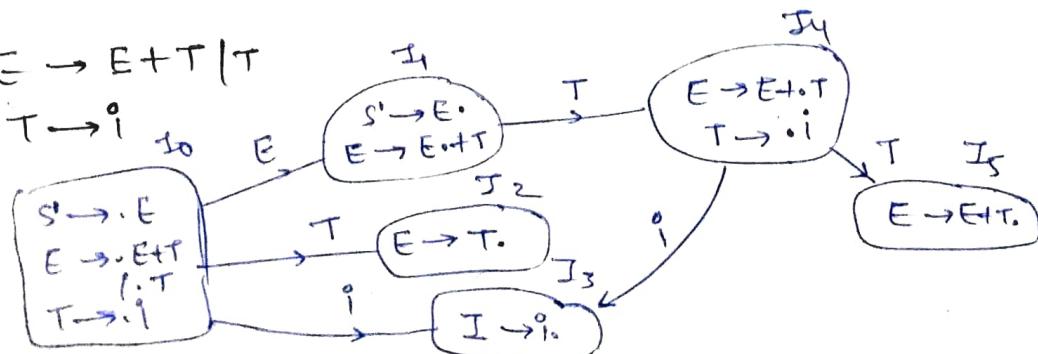
— 1 —

$S \rightarrow E$

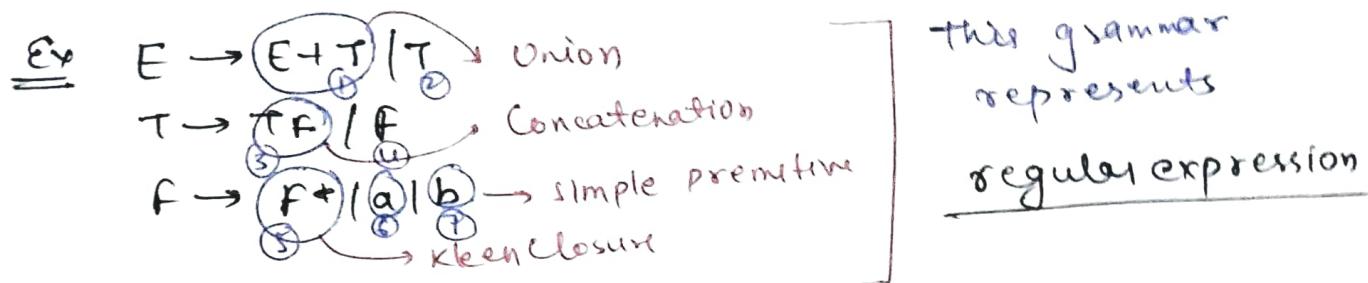
$E \rightarrow E'$

Ergonomics

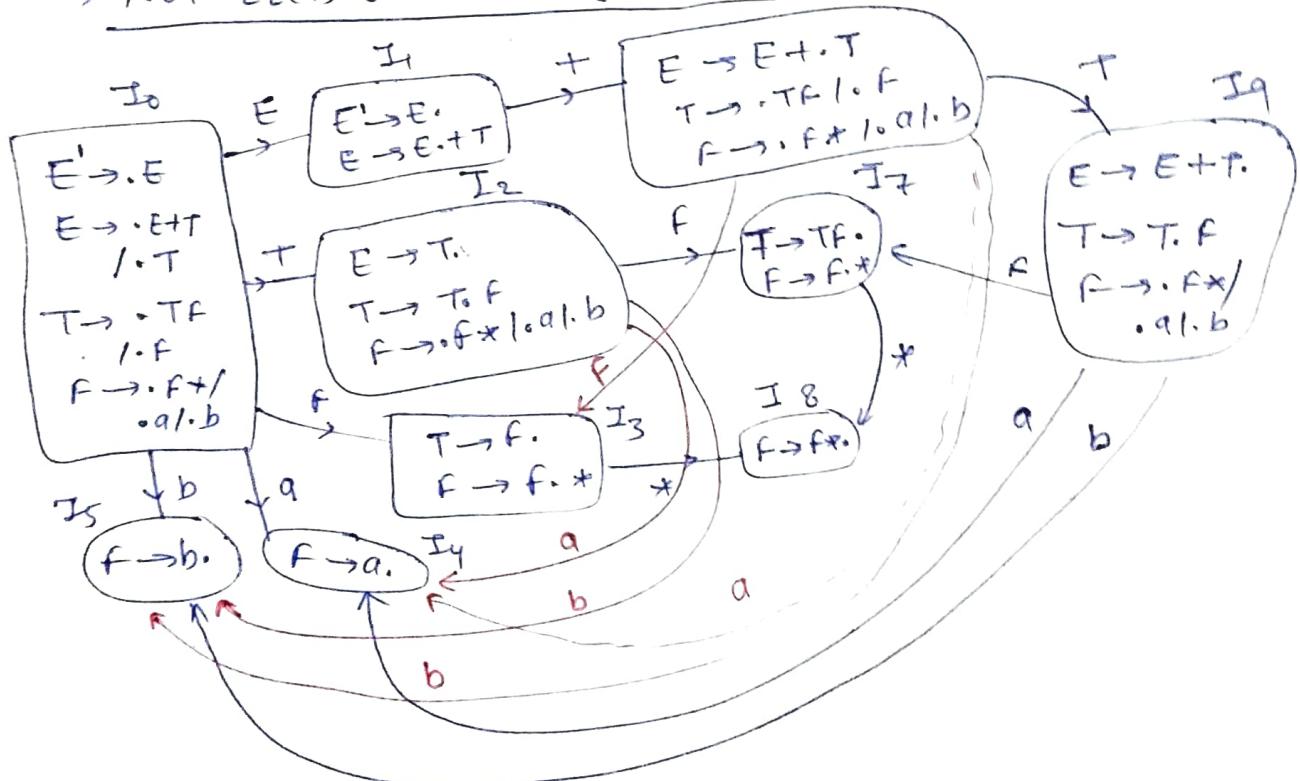
$T \rightarrow \cdot T$



We can assume that T is a final state due to $s \rightarrow E$. and its also have reduce move $E \rightarrow E+T$ and shift move on T . So there is SR conflict. But we don't consider $s \rightarrow E$ as a final state bcoz it is augmented production which is accepting, but not a final state. so there is no SR conflict.



→ Not LL(1) due to left recursion I6



→ Grammar is not LR(0) due to SR conflict on parsing I2.

→ If needed then generate table for only those reductions generated the conflicts, or conflicts generally observed in action part only.

I	a	b	+	*	\$
I2	S4	S5	Σ2	Σ2	
I3	Y4	Y4	Σ4	Σ4	Σ4

↓ Not LR(0) but SLR(1)

$$\text{follow}(E) = \{+, \$\}$$

$$\text{follow}(T) = \{+, \$, a, b\}$$

$$\text{follow}(F) = \{+, \$, ab\}$$

	a	b	+	+	\$	Continue
I7	γ_3	γ_3	γ_3	S8	γ_3	$\rightarrow LR(0) \times \text{due to SR but conflict resolved in } SLR(1)$
I9	S4	S5	γ_1	γ_1		

I_2, I_3, I_7, I_9] Generates SR conflict but it get resolved in $SLR(1)$

So grammar is $SLR(1)$ but not $LR(0)$.

CLR(1) and LALR(1) Parsers

LALR(1) CLR(1)

↓
Canonical collection of $LR(1)$ items

$LR(1) \rightarrow LR(0) \text{ item} + \text{look ahead}$

$S \rightarrow \cdot a A [LR(0)]$

$LRCD$: $S \rightarrow \cdot a A, a/b$ look aheads.

Ex: $S \rightarrow AA$
 $A \rightarrow aA/b$

$S^1 \rightarrow \cdot S \rightarrow LR(0)$
$S^1 \rightarrow \cdot S / \$ [LR(1)]$
$S \rightarrow AA, \$$
$A \rightarrow \cdot a A / \cdot b, \$ / b$

Process → ① write augmented production $LR(0)$ form
 $S^1 \rightarrow \cdot S$
 Since this is augmented, so make it $LR(1)$ by adding look ahead $\$$.

$S^1 \rightarrow \cdot S, \$ [LR(1)]$

② In $S^1 \rightarrow \cdot S$, (•) dot is before S so add all production with S on LHS

$S \rightarrow \cdot AA$

To find out lookahead take the every symbol existing just after the symbol or variable followed by dot.

$S \rightarrow AA$ is due to $\frac{S \rightarrow S_1 \$}{\text{after } S \text{ is only } \$}$ so in ②
 after S is only $\$$. So find $\text{first}(t)$ to get
 look ahead. $\text{first}(\$) = \$$ itself. So LR(1) of
 $S \rightarrow \cdot AA$ is $\boxed{S \rightarrow \cdot AA \# \$}$

Generalise

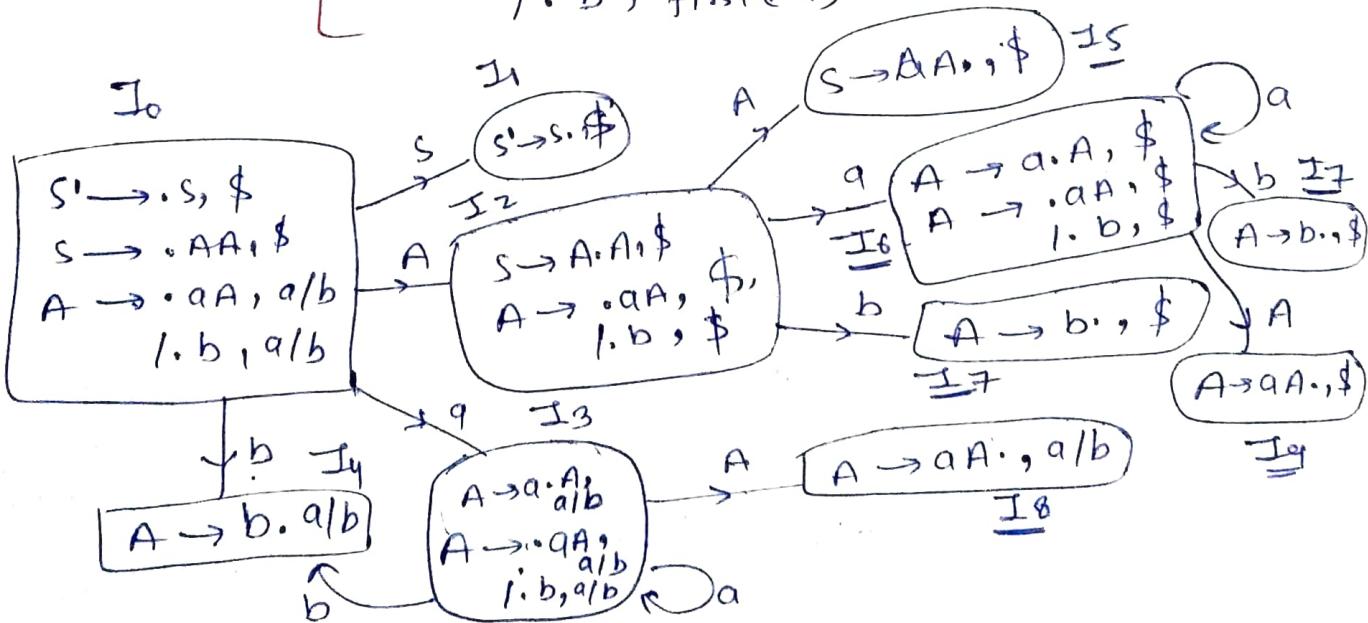
if $A \rightarrow \alpha \cdot B\beta, a/b$
 then $B \rightarrow \cdot (\text{anything})$, look ahead

look ahead = first(βa) / first(βb).
 because after β there is $\beta(a/b)$.

So LR(1) for given grammar

$$\begin{array}{l} S \rightarrow AA \\ A \rightarrow aA \end{array} \quad |^b$$

$$I_0 \leftarrow \begin{cases} S' \rightarrow^* S, \$ \\ S \rightarrow^* AA, \$ \\ A \rightarrow^* aA, \text{first}(A\$) = a/b = aA, a/b \\ \quad \quad \quad 1.b, a/b \\ 1. b, a/b \end{cases}$$



→ On applying transition look ahead might not look ahead changed but on applying closure will get changed.

No. of states in LR(1) canonical collection is more than LR(0) canonical collection for same grammar.

CLR(1) parsing table no. of states is equals to no. of states in LR(1) canonical collection. diagram.

✓ CLR(1) the reduced item will get placed in the look aheads.

[In LR(0) we placing the reduced item in complete row but in CLR(0) we were placing it in follow(LHS) but in CLR(1) placing in only look aheads only. It reduce the no. of conflicts, but due to this blank spaces and error detection capability is going to increased]

①

I_3, I_6 → both have same LR(0) items but different look aheads.

②

I_4, I_7

③ I_8, I_9

CLR(1) Parsing table

	a	b	\$	S	A
0	s_3	s_4		1	2
1			accept		
2	s_6	s_7			5
3	s_3	s_4			8
4	r_3	r_3			
5			r_1		
6	s_6	s_7			9
7			r_3		
8	r_2	r_2			
9			r_2		

Shift move and ~~reduce~~ goto move are same as LR(0) table

but reduce moves are different

$$S \rightarrow A A \rightarrow 0$$

$$A \rightarrow a A : r_2$$

$$A \rightarrow b : r_3$$

Table have very big size so we can reduce the size by merging the space with same LR(0) as

$$[I_3, I_6] \rightarrow I_{36} \quad [I_{34}, I_7] \rightarrow I_{47}, \quad [I_{38}, I_9] \rightarrow I_{89}$$

no. of states in CLR(1) \geq no of states in LR(0) or SLR(1)
No of states LR(0) = SLR(1)

\downarrow
After merging some spaces it becomes LALR(1).

$$\boxed{\text{CLR}(1) \geq \text{LR}(0) = \text{SLR}(1) = \text{LALR}(1)}$$

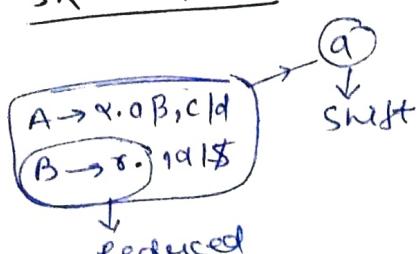
\hookrightarrow No. of states.

then LALR(1) parsing table look like

	a	b	\$	S	A	<u>LR(0) Reduced to LALR(1)</u>	a	b	\$	S	A
0	s_{36}	s_{47}			2		0	s_{36}	s_{47}		2
1							1				
2	s_{36}	s_{47}			5		2	s_{36}	s_{47}		5
36	s_{36}	s_{47}			89		36	s_{36}	s_{47}		89
47	r_3	r_3				union?	47	r_3	r_3	r_3	
5							5				r_1
36	s_{36}	s_{47}			89		89	r_2	r_2	r_2	
47											
89	r_2	r_2									
89											

(Delete duplicates after finding union.)

LRC(1) items SR conflict Depend on look ahead RR conflict



$$A \rightarrow a.19 \\ B \rightarrow b.19$$

Both are reduced and final but due to same look ahead both get placed in same column

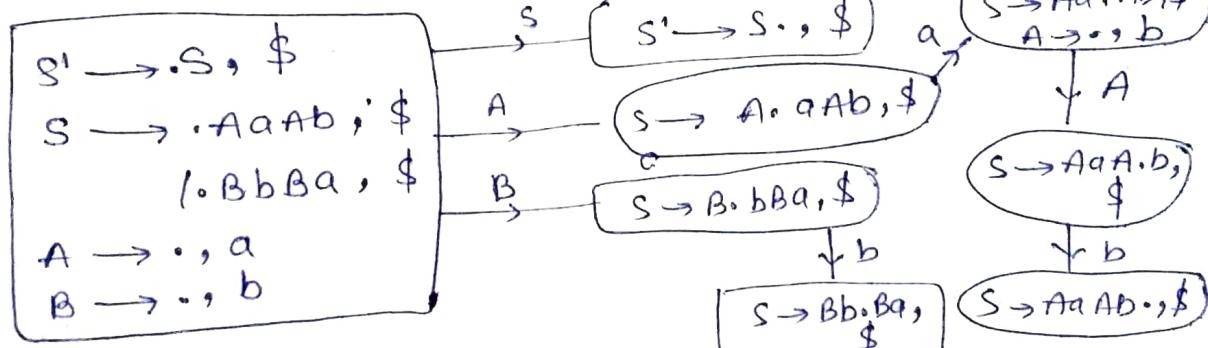
If a grammar is not CLR(1) then it must not be LALR(1).

If a grammar is CLR(1) then it is not necessarily LALR(1).

If there is no SR conflict in CLR(1) then it must not be in LALR(1), but if there is no RR conflict in CLR(1) it is not necessary that there is no RR conflict in LALR(1).

<u>Ex</u>	$S \rightarrow AaAb \mid BbBa$	① LL(1) ✓
	$A \rightarrow \epsilon$	② LR(0) X
	$B \rightarrow \epsilon$	③ SLR(1) X
		④ CLR(1) ✓
		⑤ CLR(2) ✓

Canonical collection for CLR(1),



- here, CLR(1) is same as LALR(1) bcoz there is no state with same reduce move and different look aheads.
→ on terminal it is shift and on variable it is goto.

Example of CLR(1) and LALR(1) and comparison of all parsers.

Grammar

$S \rightarrow A$
 $A \rightarrow AB \mid E$
 $B \rightarrow aB \mid b$

Closure ($S \rightarrow \cdot A, \$$)

↓

imp

we add
same
production

twice bcoz we get
different look aheads,
but in case of LR(0) only
one production is enough.

② $E \rightarrow E + T \mid T$
 $T \rightarrow T * F \mid F$
 $F \rightarrow i$

\Rightarrow

$S \rightarrow \cdot A, \$$
 $A \rightarrow \cdot AB, \$$
 $\quad \quad \quad \mid \cdot , \$$
 $A \rightarrow \cdot AB, a/b$
 $\quad \quad \quad \mid \cdot , a/b$

Both are same

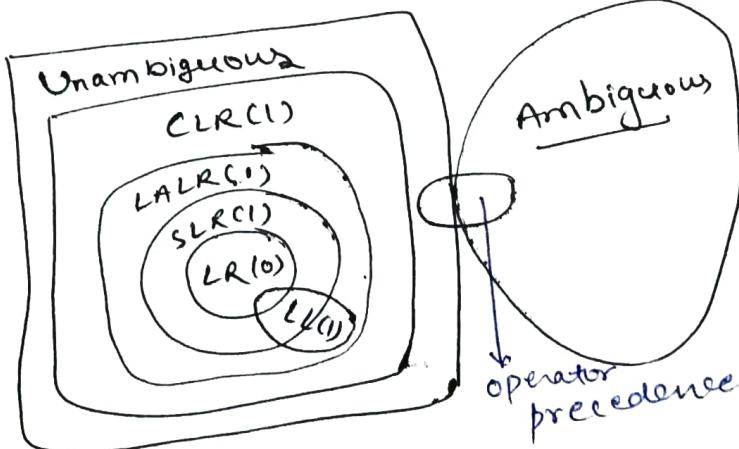
$E'' \rightarrow \cdot E, \$$
 $E \rightarrow \cdot E + T, \$$
 $\quad \quad \quad \mid \cdot T, \$$
 $E \rightarrow \cdot E + T, +$
 $\quad \quad \quad \mid \cdot T, +$
 $T \rightarrow \cdot T * F, \$ \mid + \mid *$
 $\quad \quad \quad \mid \cdot F, \$ \mid + \mid *$
 $F \rightarrow \cdot i, \$ \mid + \mid *$

\Rightarrow

$E' \rightarrow \cdot E, \$$
 $E \rightarrow \cdot E + T, \$ \mid +$
 $\quad \quad \quad \mid \cdot T, \$ \mid +$
 $T \rightarrow \cdot T * F, \$ \mid + \mid *$
 $\quad \quad \quad \mid \cdot F, \$ \mid + \mid *$
 $F \rightarrow \cdot i, \$ \mid + \mid *$

Reduced

Power of Parsers



* If grammar is
LL(1) then it
must be
LALR(1).

- + On SLR(1) and LALR(1)
 - ① Goto moves will always be identical.
 - ② Shift moves may be different.
 - ③ Reduce entries in tables may be different.
 - ④ Error entries in table may be different.
 - ⑤ Both have same no. of states.

$$S \rightarrow CC$$

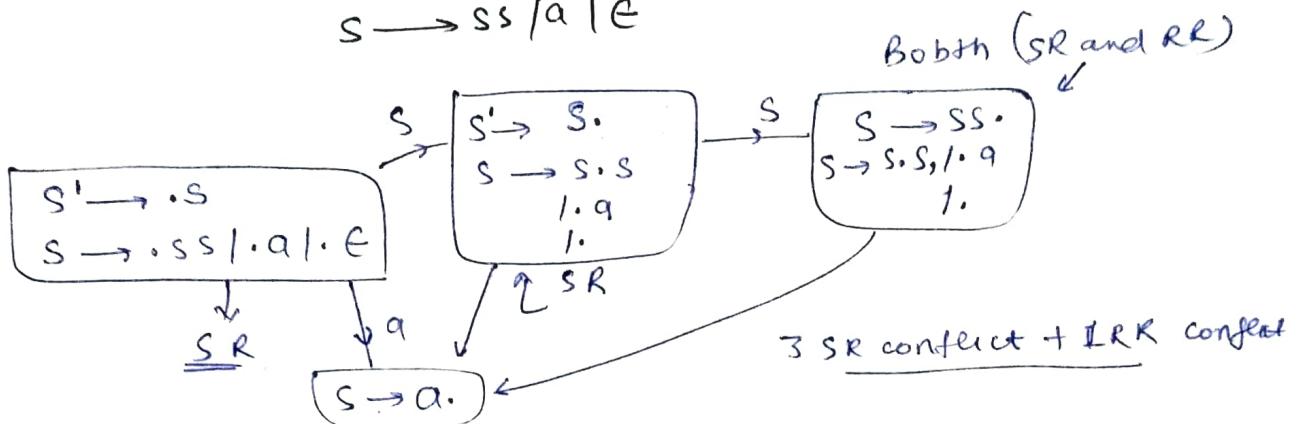
$$C \rightarrow CC/d$$

- a) LL(1)
- b) SLR(1) but not LL(1)
- c) LALR(1) but not SLR(1)
- d) CLR(1) but not in LALR(1)

→ Grammar is LL(1), LR(0), SLR(1), CRR(1) and LALR(1) all of them.

find the number of SR and RR conflicts in dfa with LR(0) items.

$$S \rightarrow SS/a/1/\epsilon$$

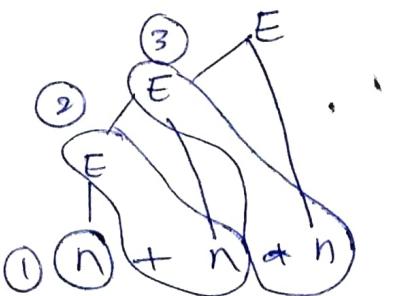


→ Total 4 conflicts are generated

Q $E \rightarrow E^n / E^{*n} / n$.

For the string $n+n+n$, the handles in right sequential form of reduction are-

Right segment form! Bottom-up parsing.



Handles means the element that is being reduced.

→ firstly n is reduced so first handle is $\underline{^n}$
 then we reduced $(E+n)$ to $E \rightarrow \underline{^n}$ is second handle
 then we reduced (E^{*n}) to $E \rightarrow \underline{^{*n}}$ is another handle

- option
- | | |
|---------------------------|---|
| a) $n, \text{ETH}, B+n+n$ | X |
| b) $n, \text{ETH}, B+E+n$ | |
| c) $n, n+n, n+n+n$ | |
- d) $n, \text{ETH}, B+n$ correct one

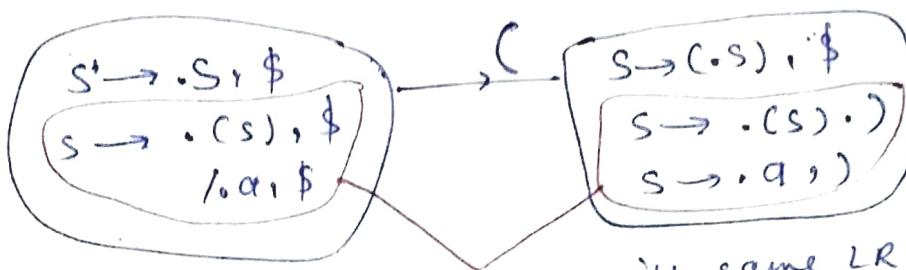
Q $S \rightarrow (S) \mid a$

SLRC(1) : n_1 , $\text{CLR}(1)$
or
 $\text{LR}(1)$: n_2 , LALRC(1) : n_3

n_1, n_2, n_3 are no. of states then,

- a) $n_1 < n_2 < n_3$
- b) $n_1 = n_3 < n_2$
- c) $n_1 = n_2 = n_3$
- d) $n_1 > n_3 > n_2$

Solⁿ



no need to move further
bcz we can take decision from here

Two states with same LR(0) Items
but different look aheads in LR(1). So they
will reduce to combine in LALRC(1) table so
size of LR(1) table > size of LALRC(1).

$$n_2 > n_3$$

and size of LALRC(1) = size of SLRC(1)
 $n_3 = n_1$

$$n_1 = n_3 < n_2$$

→ Ambiguous grammar can't use in parsing procedure bcz
in canonical structure all the final states will get conflicts
but if somehow we can remove those conflicts meaningfully.
then we can use that grammar for parsing.

YACC: Yet Another Compiler Compiler \rightarrow O/D LALR(1)

- It resolve both SR and RR conflicts
- SR conflict resolve by shift moves
- RR conflict resolve by first reduce

Syntax directed translation (SDT)

Syntax directed translations examples

(Grammar + Semantic rules) = SDT

SDT for evaluation of expression

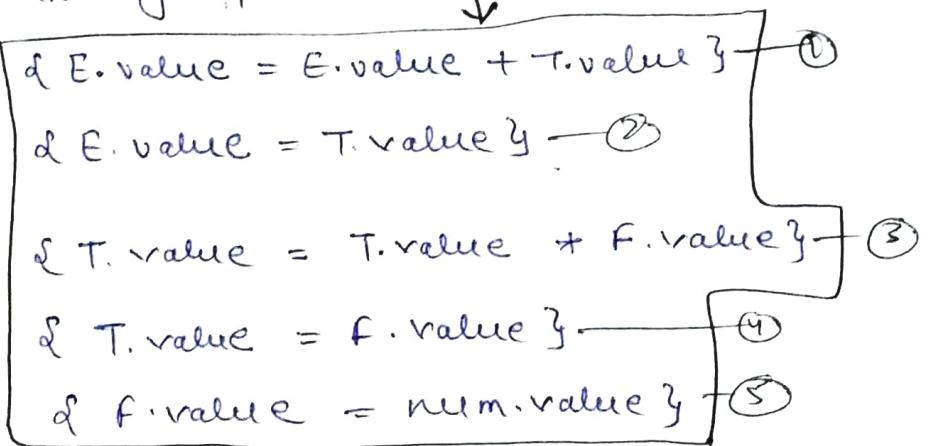
$$E \rightarrow E + T$$

/ T

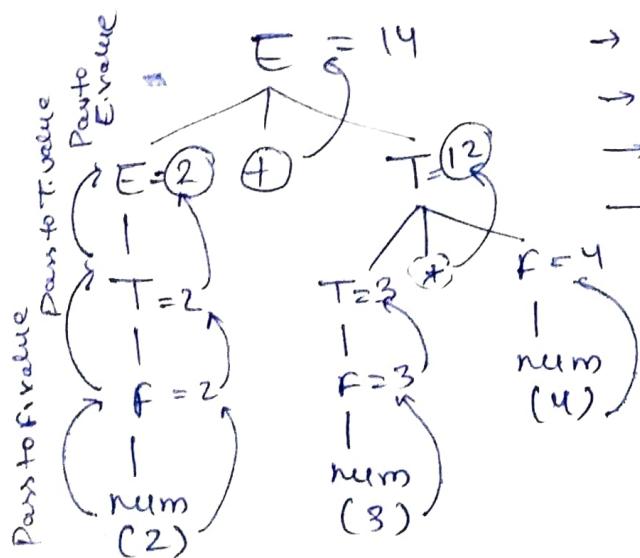
$$T \rightarrow T * F$$

/ F

$$F \rightarrow \text{num}$$



Take a expression $2 + 3 * 4$



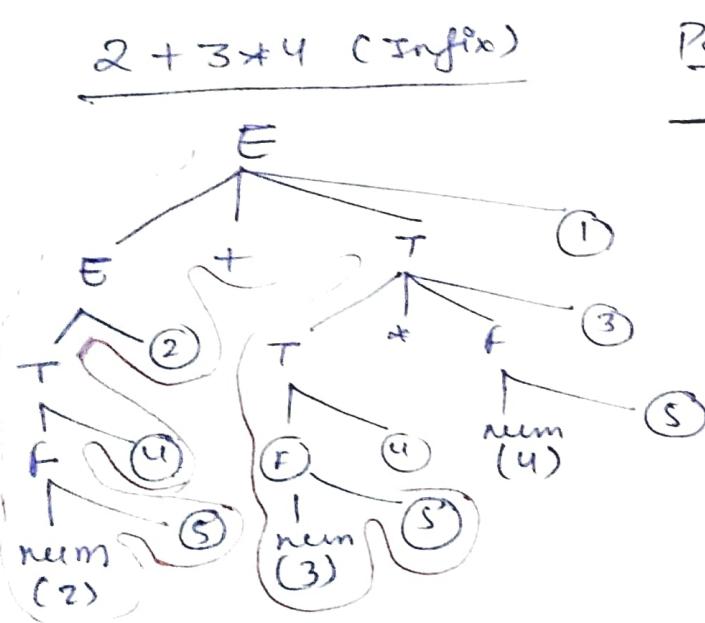
→ num \rightarrow token
→ 2, 3, 4 \rightarrow lexical values
→ value \rightarrow attribute
→ E, T, F \rightarrow variables

In SDT every variable can have any number of attributes from 0 to n.

→ Bottom-up Parsing.

Production +
Semantics
= semantic
action
and we give
no. to them

Above SDT is used to convert Infix to Postfix.



Postfix → 234 ++

→ Using top-down parser
we perform operation
top → down and left to
right and whenever we
look semantic action
we performed it.

o/p 2 3 4 + +

 (5) (4) (5) (4) (5) (3) (1)

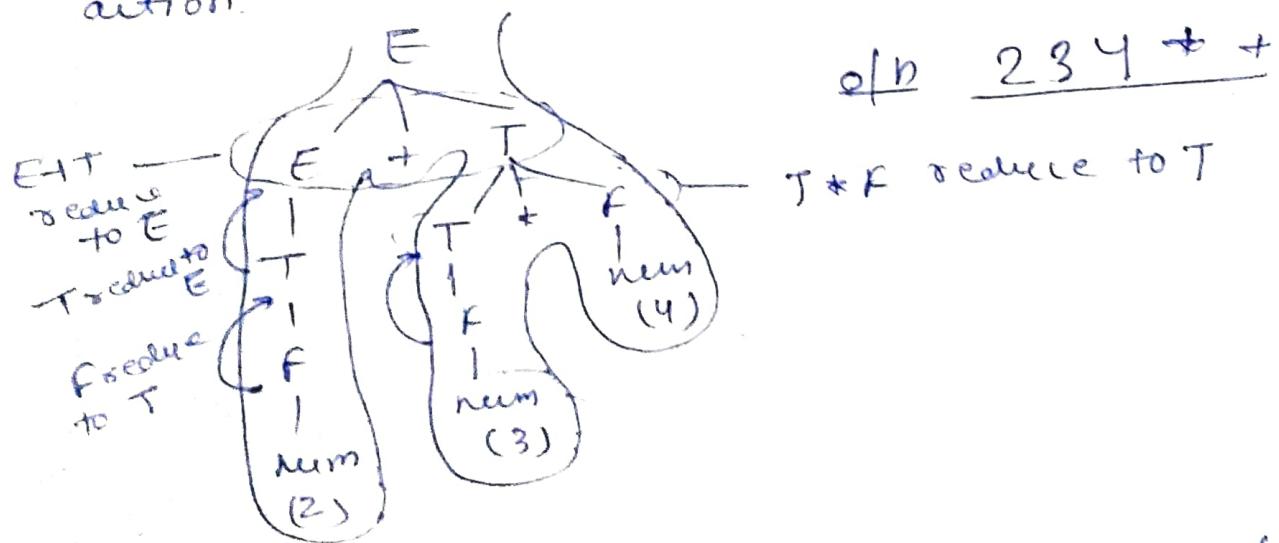
 (2)

 semantic action

 number and

 corresponding o/p

→ bottom-up Dases correspond
Mainly focused on sedation.
for sedation they take production and perform action.

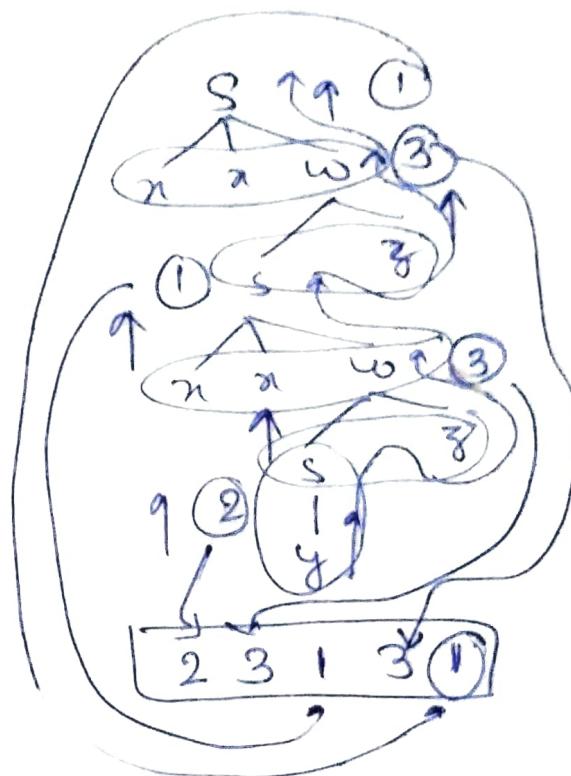
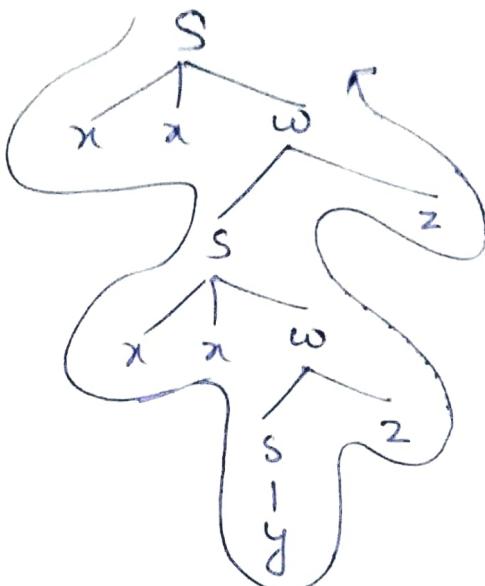


→ we get same output so SDT can be used for both topdown and bottom up parsers.

② $S \rightarrow \text{new } ly$ of $\text{printf}(1); y$
 $w \rightarrow Sz$ of $\text{printf}(2); y$

String: x x x x y z z

→ bottom up parsers (LR).



~~(4)~~ $E \rightarrow E + T$

$$\text{Evaluate : } u - 2 - u + 2$$

Observation from Grammar

$$T \rightarrow f - T$$

1 / F

107

1

F → 2 at lower levels

14 base front to left

⑤ have big

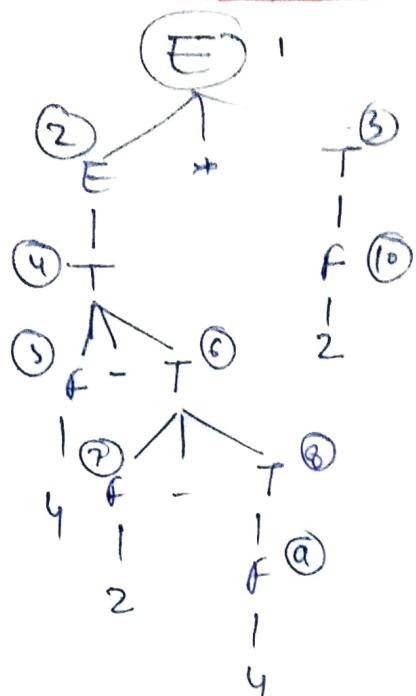
② Ⓛ have right to left

14 ② Ⓛ have right to left

predicates because (some) production T is right recursive

$$S_0 = \frac{\left((4 - \frac{(2-4)}{-2}) * 2 \right)}{6}$$

(12) Ans.

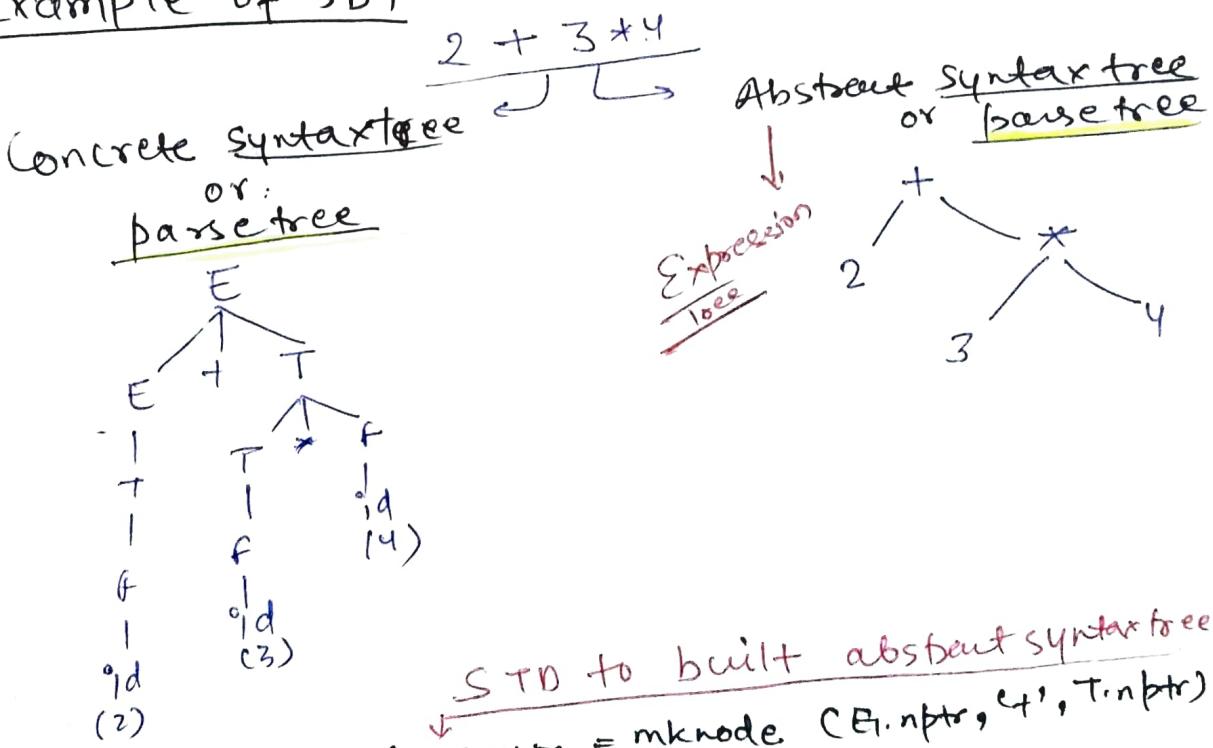


No. of reductions = 10

All the non-leaves are
reduction

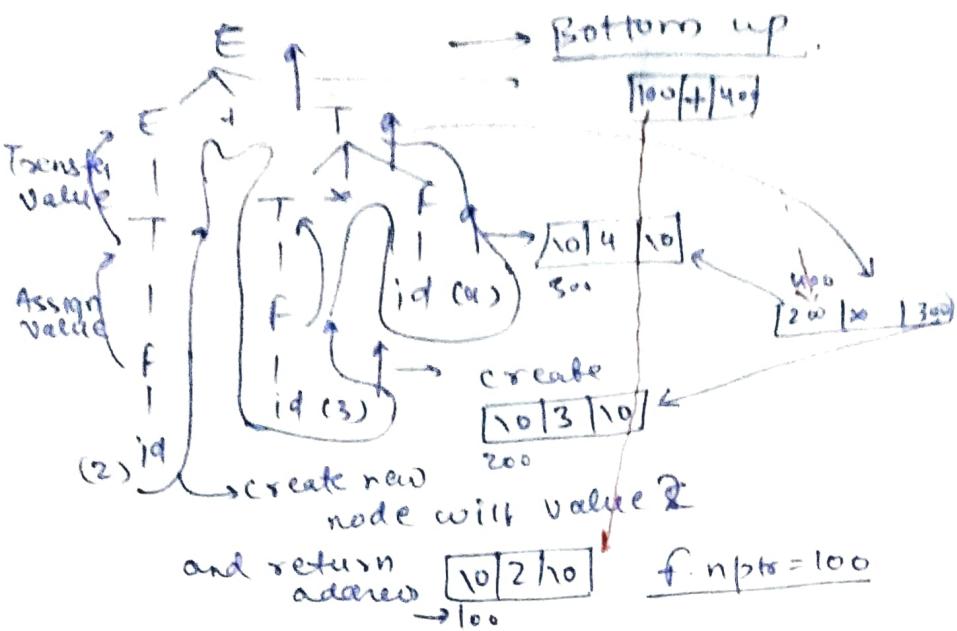
Note → Left associative means left to right say that grammar is left recursive and same for right associative too.

Example of SDT

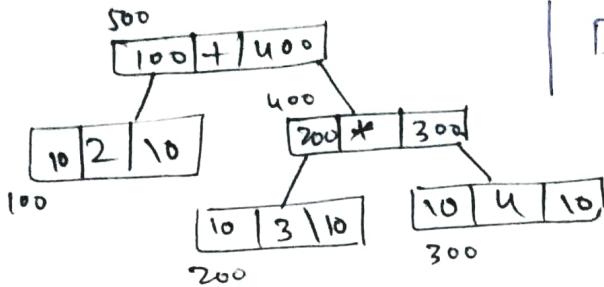


$$\begin{array}{l}
 E \rightarrow E + T \\
 | \\
 T \rightarrow T * F \\
 | \\
 F \rightarrow id
 \end{array}$$

SDT to built abstract syntax tree
 { E.nptr = mknode (E1.nptr, '+', T1.nptr); }
 { E.nptr = T1.nptr; }
 { T1.nptr = mknode (T11.nptr, '*', F1.nptr); }
 { T11.nptr = f1.nptr; }
 { f1.nptr = mknode (null, id.name, null); }



Data structure of
abstract parse
tree

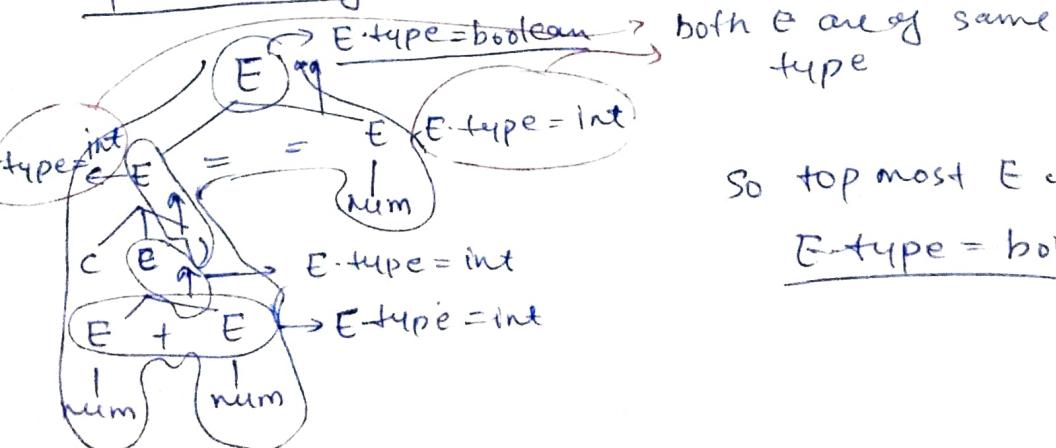


STD for type checking

$E \rightarrow E_1 + E_2 \quad \{ \text{if } ((E_1.\text{type} == E_2.\text{type}) \& (E_1.\text{type} = \text{int})) \text{ then } E.\text{type} = \text{int} \\ \text{else error;} \}$
 | $E_1 == E_2 \quad \{ \text{id } ((E_1.\text{type} == E_2.\text{type}) \& (E_1.\text{type} = \text{int} \text{ or boolean})) \text{ then } \\ E.\text{type} = \text{boolean} \text{ else error;} \}$
 | $(E) \quad \{ E.\text{type} = E.\text{type} \}$
 | $\text{num} \quad \{ E.\text{type} = \text{int} \}$
 | $\text{True} \quad \{ E.\text{type} = \text{boolean} \}$
 | $\text{False} \quad \{ E.\text{type} = \text{boolean} \}$

Both the E and E₂ are same as E but just for separation b/w LHS and RHS we make them.

operation string $(2+3) = 8$



So top most E will get
E.type = boolean

	Count 1's	Count 0's
$N \rightarrow L$	$\{ N.count = L.count \}$	$\rightarrow \text{same}$
$L \rightarrow L, B$	$\{ L.count = L_1.count + B.count \}$	$\rightarrow \text{same}$
$/ B$	$\{ L.count = B.count \}$	$\rightarrow \text{same}$
$B \rightarrow 0$	$\{ B.count = 0 \}$	$\{ B.count = 1 \}$
$/ 1$	$\{ B.count = 1 \}$	$\{ B.count = 0 \}$

$N \rightarrow \text{number}$ $L \rightarrow \text{List of bits}$ $B \rightarrow \text{bits}$

Convert binary to decimal using above grammar :-

$\frac{\text{decimal value}}{\text{Calculate or count of off bits before 1SB, multiply it with 2 and add 1SB.}}$

$\begin{array}{r} \text{MSB} \quad \text{LSB} \\ \overline{1 \ 0 \ 1 \ 1} \\ \overline{1} \quad \overline{1} \\ \underline{1 \times 2 + 0} \\ \underline{2 \times 2 + 1} \quad \overline{1 \ 1} \\ \underline{5 \times 2 + 1} \rightarrow 11 \end{array}$

$N \rightarrow L$	$\{ N.dval = L.dval \}$
$L \rightarrow L, B$	$\{ L.dval = L_1.dval + 2 + B.dval \}$
$/ B$	$\{ L.dval = B.dval \}$
$B \rightarrow 0$	$\{ B.dval = 0 \}$
$/ 1$	$\{ B.dval = 1 \}$

$$\begin{array}{r} L \\ \overline{1 \ 1 \ 0 \ 0 \ 1} \\ \overline{4} \end{array}$$

$$w = 1011 \quad \begin{array}{c} N \leftarrow \\ \downarrow \\ L \end{array} \quad \begin{array}{c} N.dval = 11 \\ \downarrow \\ 5 \times 2 + 1 = 11 \end{array}$$

$$\begin{aligned} (11)_2 &= (1011)_2 \\ (10)_2 &= (2)_{10} \\ &\quad \text{dual} = 0 \\ d &\oplus 1 \leftarrow \begin{array}{c} L \\ \downarrow \\ 1 \end{array} \quad \begin{array}{c} B \\ \downarrow \\ 0 \end{array} \quad \begin{array}{c} B \oplus d = 0 \\ \downarrow \\ 1 \end{array} \\ d &= 1 \leftarrow \begin{array}{c} B \\ \downarrow \\ 1 \end{array} \end{aligned}$$

Binary no. contain decimal

$$(11.01)_2 \rightarrow (3.25)_{10}$$

$$\begin{array}{r} 1 \quad 2^{-2} \times 1 \\ 2^{-1} \times 0 \end{array}$$

$$(\cdot 11)_2 \rightarrow (11)_2 \rightarrow (3)d$$

$$\begin{array}{r} 3 \\ \downarrow \\ 2^2 \end{array} = \underline{0.75}$$

$N \rightarrow L_1, L_2$	$\{ N.dval = L_1.dval + (L_2.dval / 2^{L_2.count}) \}$	$L_1.dval$
$L \rightarrow L, B$	$\{ L.count = L_1.count + B.count ; L.dval = B.dval \}$	
$/ B$	$\{ L_1.count = B.count \text{ & } L.dval = B.dval \}$	
$B \rightarrow 0$	$\{ B.count = 1, B.dval = 0 \}$	
$/ 1$	$\{ B.count = 1, B.dval = 1 \}$	

Both L_1 and L_2 are same

SDT to generate 3-address code

$S \rightarrow id = E \quad \{ \text{gen}(id.name = E.place) \}$

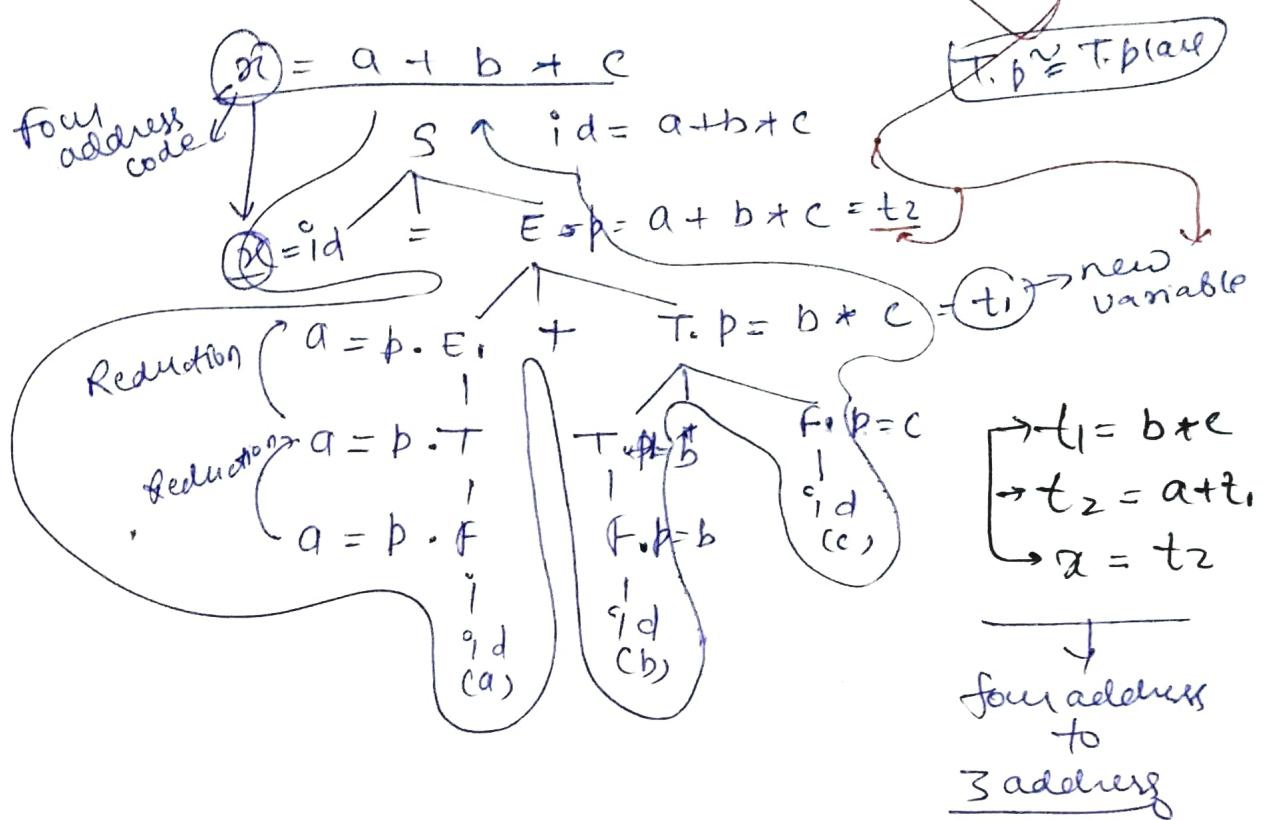
$E \rightarrow E_1 + T \quad \{ E.place = \text{new temp}(); \text{gen}(E.place = E.place + T.place) \}$

$| T \quad \{ E.place = T.place \}$

$T \rightarrow T_1 * F \quad \{ T.place = \text{new temp}(); \text{gen}(T.place = T.place * F.place) \}$

$| F \quad \{ T.place = F.place \}$

$F \rightarrow id \quad \{ F.place = id.name \}$



Classification of SDT and attributes

Synthesised attribute

Parent $\xrightarrow{A} \xrightarrow{BCD} \text{child}$

$A.att = f(B.att, C.att, D.att)$. means parent is taking attribute from children.

Inherit Attribute

$A \rightarrow BCD$

$C.att = f(A.att, B.att, D.att)$ here 'C' can be replaced with B and D only means child in inheriting attribute from parent.

~~S~~ - attributed SDT

- ① Use only synthesized attributes
- ② Semantic actions are placed at right end of productions.

$$A \rightarrow BCC \{ \cdot \}$$

↓
also called as postfix SDT

- ③ Attributes are evaluated using bottom up parsing



C L-attributed SDT

- ① Can have both kind of attribute but inherit only from parent or left siblings

$$\text{Ex } A \rightarrow XYZ$$

{ Y.S = A.S, Y.S = X.S, Y.S ≠ Z.S }

- ② Placed anywhere on RHS

$$A \rightarrow B \{ \cdot \} Y$$

$$/ C \{ \cdot \} D$$

$$/ \{ \cdot \} E$$

- ③ Traverse parse tree depth first, left to right.

Ex

$$A \rightarrow LM \quad \frac{\text{Not S}}{\text{① Inherit}}, \frac{M.i = L.S}{\text{② L attribute}}, \frac{A.S = M.S}{\text{③ L attribute}}$$

combiningly is it L-attributed SDT

$$A \rightarrow QR \quad \frac{R.i = A.i}{\text{④ L}}, \frac{Q.i = R.i}{\text{⑤ Not-L}}, \frac{A.S = Q.S}{\text{⑥ L}}$$

Due to ① it is not S-attributed and due to ⑥ it is not L-attributed. So it is neither L-attributed nor neither S-attributed

SDT to store type information in symbol table

$$D \rightarrow TL \quad \{ L.in = T.type \}$$

$$T \rightarrow \text{int} \quad \{ T.type = \text{int} \}$$

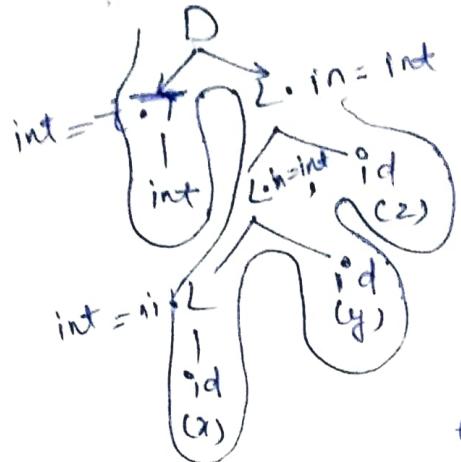
$$/ \text{char} \quad \{ T.type = \text{char} \}$$

$$L \rightarrow L, id \quad \{ L.in = L.in, \text{addtype}(id.name, L.in) \}$$

$$/ id \quad \{ \text{addtype}(id.name, L.in) \}$$

Above grammar is L-attributed grammar.

Ex → int x, y, z



(evaluate first visit)

visit on each id

x	int
y	int
z	int

when you come across any inherited attribute evaluate first time when you visit it and across synthesized attribute evaluate last time when you visited

All the L are inherited attribute so apply the action on first visit

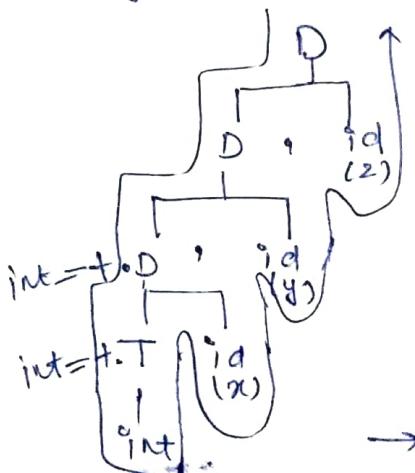
S → attributed SDT (Only synthesized attribute)

$D \rightarrow D_1, id \text{ of add type } \{ id.name, D_1.type \}, D_1.type = D_1.type \}$
 $/ T, id \text{ of add type } \{ id.name, T.type \}, D.type = T.type \}$

$T \rightarrow \text{int } \{ T.type = \text{int} \}$
 $/ \text{char } \{ T.type = \text{char} \}$

Both D and D₁ are same

Ex → int x, y, z



x	int
y	int
z	int

On each visit to id we add T.type and id.name in table

→ In S-attribute we will do action on last visit to the attribute

→ To convert a SDT from L-attributed to S-attributed we need to change grammar and semantics action both.