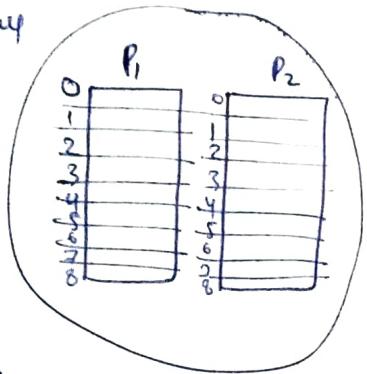


→ Internal fragmentation  
Can be there due to overhead of  $(P_1/2)$  in last page. But it is not considerable.

Consider a snapshot of system at any particular time,

Secondary m/m



Main memory

0	OS	OS
1	OS	
2	OS	
3	$P_1 : P_1$	
4	$P_1 : P_2$	
5	$P_2 : P_3$	
6	$P_2 : P_1$	
7	$P_2 : f$	
8	$P_1 : 3$	
9	$P_2 : p_7$	
10	$P_1 : P_4$	
11	Page table of $P_1$	
12		
13	Page table of $P_2$	
14		
15		

Page table of  $P_1$

	Name	PA	D	R	P
11+0		0	0	0	0
11+1	3	1	1	1	0
11+2	4	1	0	1	1
11+3	8	1	0	0	0
11+4	10	1	1	0	0
11+5	0	0	0	0	0
11+6	0	0	0	0	0
11+7	0	0	0	0	0

↳ Relocatable Address (11 + no.)

P/A are valid or invalid bit  
If its one (1) means page is present in main m/m if it is zero (0) then page is not present in m/m means page fault.

→ In case of page fault, OS reload the page from secondary m/m.

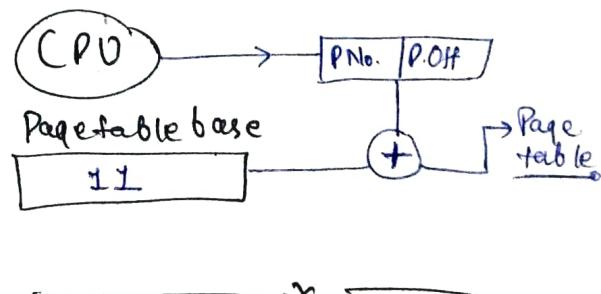
→ D (Dirty bit) or modified bit means page has been modified in main m/m or not  
If it is modified then the changes will reflect in lower level secondary m/m too called 'Write-back' policy at the time of replacement.

→ R (Reference bit) changes after each life cycle. So if page is not referred from long then we can replace it.  
For this we have various page replacement Algo.

→ P (Protection bit)  
Contains Read / Write / execute.  
 $CS \rightarrow R/E$        $SS \rightarrow R/W$   
 $DS \rightarrow R/W$

(Code, Data and Stack Sections)

If you have no permission then you can't perform actions.



## TLB

→ Paging also have a overhead as page table.

### Scenario

To reduce or avoid external fragmentation → Paging

for paging, page table is overhead

↓  
To reduce page table size we increase page size → It might leads to internal fragmentation

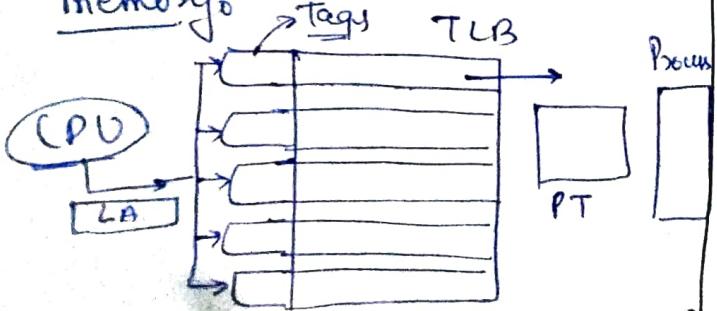
So we come with the concept of multi-level paging  
and it is also time consuming.

To make it more efficient we store the base address of table in registers, which is directly in contact with CPU

But registers are very costly and context switching time arises.

So, we introduce Cache, because cache is cheaper than registers and size greater than registers and also faster than memory. It introduces the concept of TLB [Translation Lookaside buffer].

TLB also called as associate memory.



CPU gives the logical address to tags in TLB and if they have same no regarding page no. then it will send further. This way we reduce the time taken in accessing page table.

→ TLB also contains page tables entries that is currently used.

→ (TLB size) > register  
^ Less than  
(main memory)

→ Accessing TLB is faster as compare to accessing page table.

→ But if entry is not in TLB then we should go in page table and get its and we will also insert the entry in TLB if space is available. But if there is no space in TLB then we have page replacement algo. or some other methods.

If entry found in TLB called as TLB Hit.

Say hit rate = 80%.

then, miss rate = 20%

$$\text{effective m/m access time} = 0.8(t_a) + (0.2)t_b$$

$t_a \rightarrow$  time taken by mapping if hit

$t_b \rightarrow$  time taken by mapping if miss.

Ex → Time taken in searching page inside TLB = 20ns

time taken in searching inside page table = 100ns

Hit rate = 0.8. find effective access time

$$\text{Sol}^n \text{ miss rate} = 1 - 0.8 = 0.2$$

If process hit in TLB -:

$$t_a = 20 + 100$$

for searching  
in TLB to get  
frame no

for accessing  
frame no.  
 $\frac{1}{12}$   
main memory

If process miss. in TLB -:

$$t_b = 20 + 100 + 100$$

for searching  
in TLB  
for a miss

for searching  
in page table

for accessing  
frame no.  
 $\frac{1}{12}$   
main m/m

$$\text{Access time} = 0.8(t_a) + 0.2(t_b)$$

$$= 0.8(120) + 0.2(220)$$

$$= 96 + 44$$

$$= 140 \text{ ns}$$

→ Searching time in page table and accessing time of frame is same bcoz both take place in main m/m.

So, access time is 140ns but if we don't have TLB then

each time we check page table and then access frame means  $(100 + 100) = 200 \text{ ns}$

So, somehow TLB is better approach

Note → Above discussion is for single level.

Generalise,

Efficient m/m access time = EMAT

$$\text{hit ratio} = p$$

$$\text{miss ratio} = (1-p)$$

$$\text{TLB time} = t$$

$$\text{main m/m time} = m$$

(for both  
page table and  
frame access)

then, for single level paging-

$$\text{EMAT} = p(t+m) + (1-p)(t+mtm)$$

for n-level paging,

$$\text{EMAT} = p(t+m) + (1-p)(t+nm+m)$$

$$= p(t+m) + (1-p)(t+m(n+1))$$

gap

we are neglecting the time to update the entry if hit doesn't occur.

Sometime  $m \gg t$ ,  
So, we can neglect t.  
It's completely depends on question.

Tags → Tags used to contain the page no.

→ If nothing is given consider single level paging.

### Q TLB Questions

TLBA	MA	TLB M	PT Level	EMAT
20ns	100ns	80%	1	140ns
20ns	100ns	80%	2	160ns
20ns	100ns	80%	3	180ns
20ns	100ns	90%	1	130ns
<u>20ns</u>	100ns	60%	1	160ns
20ns	100ns	50%	1	170ns

Complete the tables

Note → Do all the question during practice by self.

### TLB Summary

→ It might be given miss rate instead of hit rate.

$$TLB \text{ access} = t$$

$$M/M \text{ access} = m$$

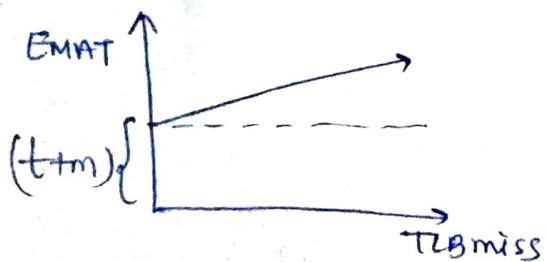
$$TLB \text{ miss rate} = p$$

↳ not hit rate

$$EMAT = p(t+m) + (1-p)(t+m)$$

$$EMAT \Rightarrow \frac{y}{c} + \frac{x}{a} = p(m)$$

$$y = ax + c$$



If TLB miss  $\uparrow$  EMAT  $\uparrow$ . So make less miss page replacement Algo. should be good.

So,

$$EMAT = (t+m) + pm$$

↳ for one-level page table

and  $p \rightarrow \text{miss ratio}$

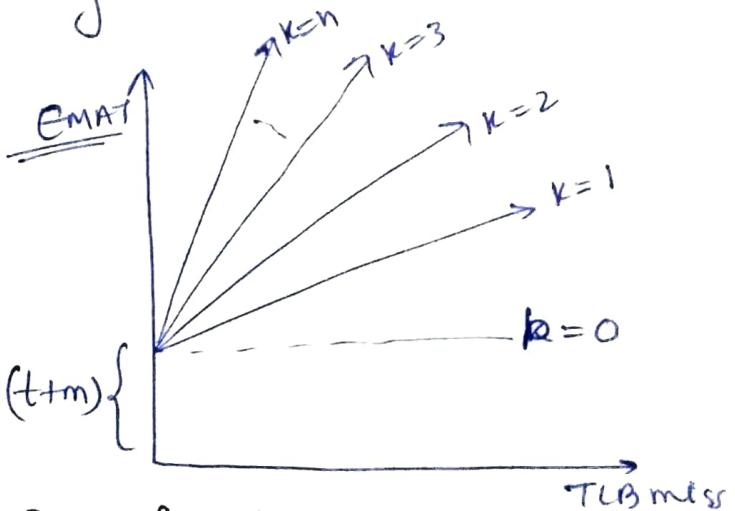
for multi-level paging

No. of page table level = k.

$$EMAT = p(t + km) + (1-p)(t+m)$$

$$\Rightarrow EMAT = (t+m) + p(km)$$

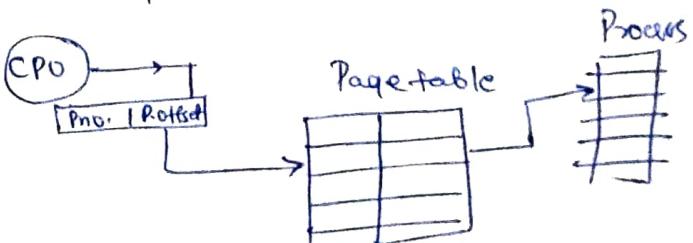
$$y = \frac{t+m}{c} + \frac{p}{m} \cdot a$$



### Page fault

Demand paging: We don't load any page in main M/M until required.

If page not present in M/M then page fault occurs.



TLB miss and page fault both are different things.

If entry not present in TLB  
called TLB miss and if entry  
not present in table due to  
concept of virtual m/m called  
as page fault.

If page fault occurs then,

- ① process calls OS to load the page from secondary m/m  
called context switching and its takes (usec).
- ② After getting CPU, OS loads the data from secondary m/m to page table takes (usec)
- ③ OS again calls process to xen via context switching takes (usec).
- ④ Now process will find the add. in page table takes (ns),  
and if no. page fault it will only takes step ④ time as (ns).

Thrashing → If large no. of page faults occur called as thrashing.

To avoid thrashing we have to come with algo. that can fulfill the future requirement but its not possible.

So, we can perform good page replacement algo.

Not final formula.

$$EMAT = p \times (\text{Service time or page fault time} + (t) \text{ fault time})$$

p → page fault rate

EMAT: Effective m/m access time

$$EMAT = \frac{p(\text{Service time}) + (1-p)m}{(t)}$$

$m$  → m/m access time.

So, final formula of EMAT is,

$$EMAT = p(S_t + m) + (1-p)m$$

$S_t$  → service time

→ grab and complete formula

Gate 2011 page fault

Given Service time → 10ms

$$m = 20\text{ns}$$

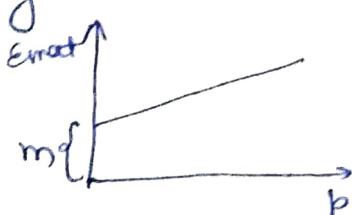
$$p = 10^{-6}$$

$$EMAT = 10^{-6}(20 + 10000) + \frac{(1-10^{-6})}{20} \times 20 \\ \Rightarrow 20 \times 10^{-6} + 10^2 + 20 - 2036 \\ \Rightarrow 20 + 10 \\ = 30\text{ ns}$$

$$Emat = p(Ps + m) + (1-p)m$$

$$\Rightarrow p(ps) + p/m + m - pm$$

$$\Rightarrow Emat = p(ps) + m \\ \downarrow \quad \downarrow \quad \downarrow \\ y = xm + c$$



Above question can be solved as

$$EMAT = p(ps) + m$$

$$\Rightarrow 10^{-6}(10\text{ms}) + 20\text{ns}$$

$$\Rightarrow 10\text{ns} + 20\text{ns}$$

$$= 30\text{ns}$$

Gate-1998.  $ps = j$ ,  $m = i$

$$EMAT = \frac{j}{k+1} \text{ ms}$$

Effective m/m access time and effective instruction time both are same. So,

$$E_{it} = \frac{g}{k+i}$$

Gate 2000 [Conversion of value of p is imp.]

$$St = 10 \text{ ms}$$

$$m = 1 \mu\text{s}$$

$$p = \left(\frac{1}{100}\right)\% = \frac{1}{10000}$$

$$EMAT = 10^{-2} (10 \text{ ms}) + 1 \mu\text{s}$$

$$\Rightarrow 10^{-4} \times 10 \times 10^3 \mu\text{s} + 1 \mu\text{s}$$

$$\Rightarrow 1 \mu\text{s} + 1 \mu\text{s}$$

$$\Rightarrow 2 \mu\text{s} (1.999 \mu\text{s})$$

or

$$EMAT = p(PS+m) + (1-p)m$$

$$= p(PS+m)^0 + (1-p)m$$

Reason  
We can neglect 'm' as compare to 'PS' but in  $(1-p)m$  m is independent,

$$\Rightarrow p(PS) + (1-p)m$$

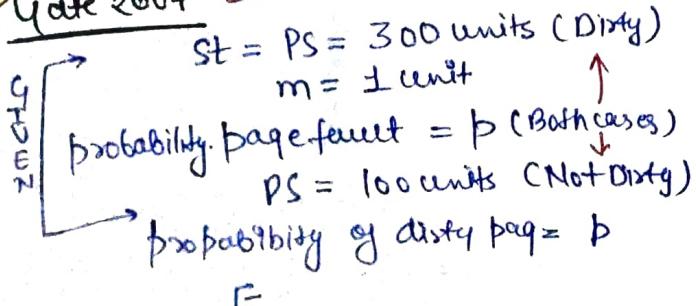
$$= 0.0001 (10^{-2}) + (0.999) 10^{-6}$$

$$\approx 1.999 \mu\text{s}$$

Here exact ans is 2 μs and approximate ans is 1.999 μs.

→ But you will get the two closest ans in both approaches and both are correct.

Q&A [New Concept]



So,

$$PS = (1-p)100 + p(300)$$

$$= (100 + 200p) \text{ unit}$$

$$m = 1 \text{ unit}$$

$$Emat = m + (p) PS$$

$$3 = 1 + p(100+200p)$$

$$\Rightarrow 100p + 200p^2 = 2$$

$$\Rightarrow 100p^2 + 50p - 1 = 0$$

$$\Rightarrow p = 0.0194 \text{ units}$$

but option given as 0.194, so they might miss a 0.

→ In case if dirty bit is set or page is dirty then, some time will take in updating the info. to secondary m/m.

So, if process have some pages in page table, they might be of both types either,

→ Dirty

→ Not Dirty.

Good: [first do it by reading the soln]

Gate 2003 [TLB and paging]

$$VA = PA = 32 \text{ bits}$$

VA

$$PTE(e) = 4B$$

10	10	12
----	----	----

→ find the given info. in questions of 2003 and solve it.

Sol'n

TLB and cache both uses as saving page table entry and process data respectively.

$$TLB \text{ hit} = 0.96$$

$$Cache \text{ hit} = 90\% = 0.9.$$

No, page fault means we have no need of service time.

Cont~

Gate 2004, 2014 on T2B

→ Do it by self and watch the video in downloaded video if require

### Inverted page table.

This concept is not widely popular because it saves space but waste the lot of time

→ We make a page table for each process and if m/m have large no. of processes then we have large no. of page tables in main m/m.

Say we have two process P<sub>1</sub> &

P<sub>2</sub> as -

	Page table of P <sub>2</sub>
0	X
1	X
2	f <sub>4</sub>
3	f <sub>5</sub>
4	f <sub>6</sub>
5	X
6	X
7	X

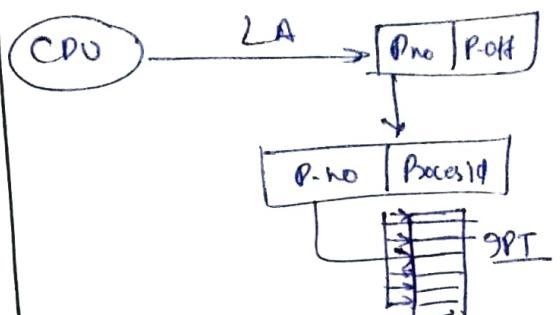
	Page table of P <sub>1</sub>
0	X
1	f <sub>1</sub>
2	X
3	f <sub>2</sub>
4	X
5	f <sub>3</sub>
6	X

So instead of making lots of page tables that contains lots of vacant entries we make a single inverted page table as,

frame no.	Process
1	P <sub>1</sub> : p <sub>1</sub>
2	P <sub>1</sub> : p <sub>3</sub>
3	P <sub>1</sub> : p <sub>5</sub>
4	P <sub>2</sub> : p <sub>2</sub>
5	P <sub>2</sub> : p <sub>3</sub>
6	P <sub>2</sub> : p <sub>4</sub>
7	
8	

Index are frame no. here instead of page no. in page tables

We maintain both page no. and process id in inverted page tables



In Inverted Page Table all the entries checked simultaneously at a time

Ex PA = 32 bits

$$PS = 4 \times B$$

$$(IPT) entry size = 4B$$

What is the size of IPT?

$$PS = 2^{12} B$$

$$\text{No. of frames} = 32 - 12 \\ = 20$$

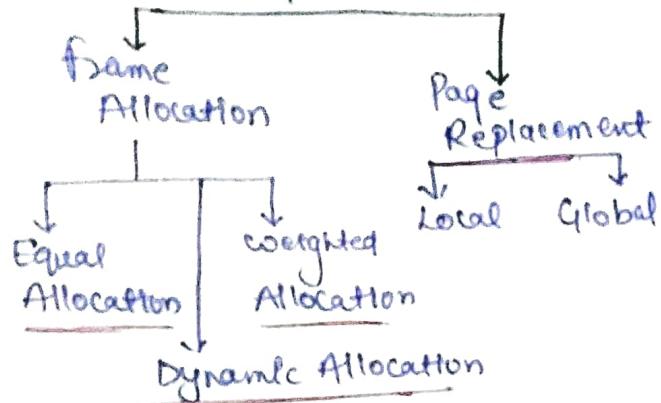
$$(\text{size of IPT}) = 2^{20} \times 4 \\ = \frac{2^{22} B}{= 4 MB}$$

### Importance of frame allocation and page replacement

If there is no virtual m/m then each time only a single process will get the main m/m,

but in virtual m/m multiple process can run simultaneously so it is difficult to maintain that each process get a fair chance to run bcz all the process want to access a shared common main m/m.

## Virtual Memory Implementation



→ Each process is allowed to access only certain number of frames in main mem. Once a process gets its max. limit and if it needs to load more page then it will take help of page replacements.

→ If we got page fault for every instruction then program time will increase exponentially called thrashing.

→ So, we have a min. value and max. value for frame allocation  
min. value → min. no. of frame required to run a instruction.  
max. value → size of process (no. of pg.)

So, we choose a number between them.

① Equal allocation : no. of frames = 30  
 no. of procs = 3  
 frames per proc = 10 frames.

② Weighted allocation,  
 no. of frames = 30  
 3 procs with (10, 100, 1000 pages)  
 then we can't do equal allocation.

Ex:  $P_1 = 20$  pages  $P_2 = 30$  pages

$P_3 = 50$  pages

no. of available frames = 10 frames.

no. of required pages =  $(20+30+50) = 100$

so,  $P_1$  gets  $\left(\frac{20}{100}\right) \times 10 = 2$  frames

Similarly  $P_2, P_3$  get 3, 5 frames.

→ This is weighted allocation.

### Generalise

if  $P_i \rightarrow$  Process and  $S_i \rightarrow$  size of process

$$S = \sum_{i=1}^n S_i$$

assume no. of frame available =  $F$

$$\Rightarrow (P_i \text{ gets}) = \left( \frac{S_i}{S} \right) \times F \text{ frames.}$$

→ Till now both the methods are static, means we can't change once we allot.

③ Dynamic allocation → We can change the allocation as they want according to process priority.

Assume

$P_1$
$P_2$
$P_1$
$P_2$

say Priority ( $P_1 > P_2$ )

and  $P_1$  needs one more page then

$P_1$
$P_1$
$P_1$
$P_2$

→ replaced

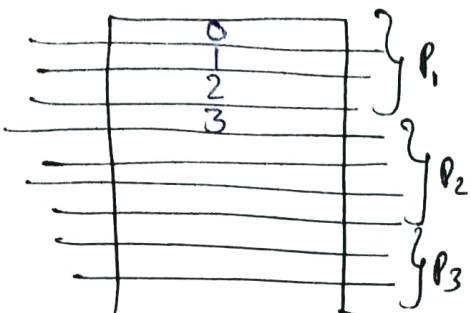
### Page replacement

$P_2$	$3 P_2$
$P_3$	$3 P_3$
$P_4$	

$P_1$  gets its 3 pages but it wants to load then it needs to replace.

which page will get replaced?

### ① Local (PR) :



Replacement will occur in frames allotted to P<sub>1</sub> process only.

② Global (PR) : But in global page of another process can also get replaced if they are free & using some parameters as priority.

→ Local is more preferred over global.

→ If nothing explained about type of algo. then go for local algo. in GATE exams.

Demand paging → we will not load the page until its required

→ Pre-paging is just opposite to demand paging.

Reference String → Strings or order of pages requires by the CPU to execute a process.

Ex → 0145716 -  
Shows page no.

Pre-paging → Assume a process with 15 pages got 4 frames in main m/m and 9+ allotted or filled the frames as 

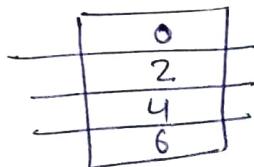
P <sub>2</sub>	P <sub>4</sub>
P <sub>7</sub>	P <sub>9</sub>

 means pre-paging.

bcoz, we don't know which pages required in future we filled the frames with any pages and in future if new page is require then we replace it.

Demand paging → Assume a process with 10 pages got 4 frames in main m/m and initially the frames are empty. Then it has a reference string as

02467532 -



Initially it is empty so page fault occurs and '0' get loaded. Similarly four page fault occurs in order to fill first four frames, but all the pages are necessary.

### Page-replacement Algo.

① Optimal : Page that not being referred from longest time replace it.

② LRU (Least recently used) : Replace the page which has not been referred for a long time.

③ (FIFO) : first In first Out

Optimal algo is for reference purpose. We compare each algo. with optimal algo. for benchmarking.

→ In optimal we search page that not referred 'for long in future', but in LRU we replace the page that not been referred 'from long in past'.

### Question

Demand paging used find page faults?

① 2014 (framesize = 5)

4, 7, 6, 1, 7, 6, 1, 2, 7, 2

→ Optimal:

4 7 6 1 7 6 1 2 7 2  
↑ ↑ ↑ ↑ ↑

4 1 2 No. of page-fault = 5  
|  
7  
|  
6

Bcoz initially all frames were empty so, 4, 7, 6 also get pagefault.

→ LRU

4 7 6 1 7 6 1 2 7 2  
↑ ↑ ↑ ↑ ↑ ↑ ↑

4 1 2 No. of page-fault = 6  
|  
X  
|  
X

→ FIFO

4 7 6 1 7 6 1  
| | | | | |  
4 2 7 2

No. of pg. fault = 6  
→ Sometimes we also maintain a queue in case of FIFO as,



→ 'No' any algo. can beat optimal.

② 1995 Q3P

0100, 0200, 0430, 0499, 0510, 0530, 0560, 0120, 0220, 0240, 0260, 0320, 0370.

100 records per page present with 1 free main m/m frame

Convert address no. to page no.  
first

[0000-0100) → Page 00  
[0100-0200) → Page 01  
[0200-0300) → Page 02  
[0300-0400) → Page 03  
[0400-0500) → Page 04  
[0500-0600) → Page 05

Reference string on given address.

01, 02, 04, 04, 05, 05, 05, 01,  
02, 02, 02, 03, 03

frame	01	02	04	04	05
	↑	↑	↑	↑	↑
05	05	01	02	02	02
03	03				
	↑	↑			

$$\text{Page fault rate} = \frac{7}{13}$$

No. of page fault = 7

→ There is no choice so every algo. will give the same results.

Gate 2009 (frame no = 3)

1, 2, 3, 2, 4, 1, 3, 2, 4, 1

Gate 2007 (frame no = 3)

1, 2, 1, 3, 7, 4, 5, 6, 3, 1

Gate 2014 (frame no = 3)

1, 2, 3, 4, 2, 1, 5, 3, 2, 4, 6

Do all the question by applying  
FIFO, LRU and Optimal Algo.  
find no. of page faults.

Note → Do it by self on rough copy  
and verify the answers.

### Belady's Anomaly

Reference string

0 1 2 3 0 1 4 0 1 2 3 4

① No. of frame = 3

→ Optimal.

0 1 2 3 0 1 4 0 1 2 3 4  
↑ ↑ ↑ ↑ ↑ ↑ ↑ ↑ ↑ ↑ ↑ ↑

0	1	2	3	0	1	4	0	1	2	3	4

 No. of page faults = 7

② No. of frame = 4

→ Optimal

0	3	0	1	2	3	0	1	4	0		

1	4	1	2	3	4						

No. of page fault = 6

→ More the frames contributes lesser  
number of page fault, except  
Belady's anomaly.

② LRU

No. of frame = 3

0	1	2	3	0	1
0	1	1	1	1	1
2	2	1	1	1	1
2	1	1	1	1	1
1	1	1	1	1	1

No. of page faults = 10

No. of frame = 4

0	4	0	1	2	3
1	1	1	1	1	1
2	2	3	0	1	4
2	2	1	1	1	1
2	1	3	0	1	4
1	1	1	1	1	1

No. of page faults = 8

③ FIFO

3 frames

0	3	4	0	1	2	3	0
X	0	2	1	1	1	1	↑
X	X	3	1	4	0	1	2

No. of page fault = 9

4 frames

No. of page fault = 10

ans ↗

In this example on  
increase no. of frames  
page fault also increases  
called as 'Belady's anomaly'

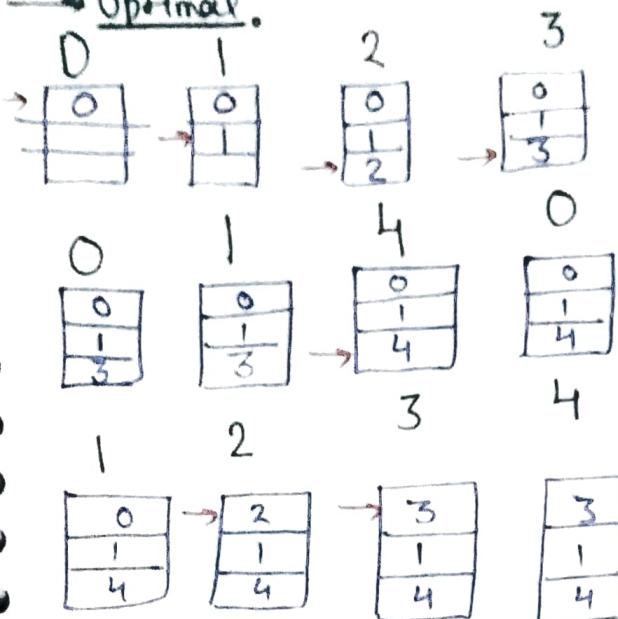
→ So, for this scenario

We have stack algorithms  
that doesn't follow Belady's  
anomaly.

~~Belady's anomaly applies on FIFO page replacement algorithm.~~

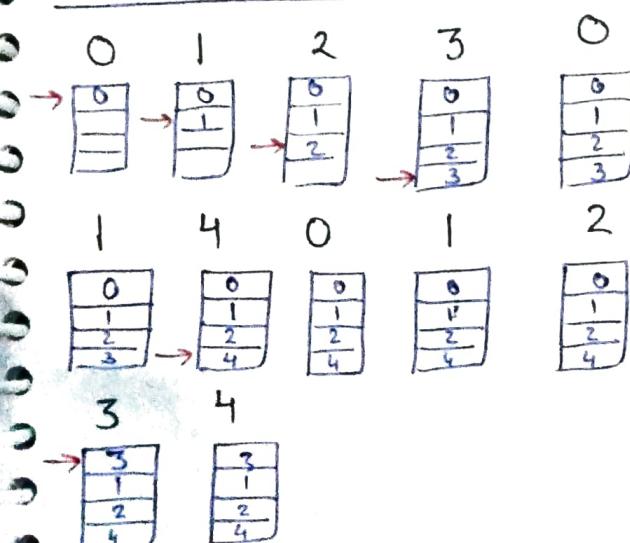
### Stack Algorithms

→ Reason for Belady's anomaly is stack property.  
→ Optimal.



→ Here we use optimal algo and represent the state after each page allocation.

for 4 frames



→ (In both the case ( 3 frames / 4 frames ) if we have multiple choice to replace page we go for first one here).

### Observation

Here, we can observe that the pages present in 3 frames are also the part of 4 frames. Corresponds to particular page.

Ex (1) 2 that comes 2nd in all



(2) 4 that comes first



Similarly, we can observe for each pages.

→ Order might be different but all are present.

→ This property is called stack property.

→  $\text{Pages}(3) \subseteq \text{Pages}(4)$   
 $\text{Pages}(m) \subseteq \text{Pages}(m+n)$

~~Algorithm that doesn't fail in Belady's anomaly~~ are called as stack algorithms.

→ FIFO.

On doing same kind of state observation in 3 frames and 4 frames.

0	1	2	3	0	1
00	00	00	30	30	30
—	11	11	12	02	02
	22	22	23	23	23
			2	3	4
4	0	1	2	3	4
44	44	44	44	43	43
—	00	00	00	20	20
	11	11	11	12	12
	22	22	22	32	32
0	1	2	3	4	5
12	12	13	13	32	32
—	23	23	23	31	31

with 3 and 4 frames combines states.

→ FIFO doesn't follow stack property, so it has Belady's anomaly.

and Similarly LRU also follows stack property, so it is stack algorithm.

Q A memory page containing a heavily used variable that was initialized very early and is in constant use is removed when \_\_\_\_\_ is used.

- ① LRU    ② FIFO    ③ LFU  
④ none

Not LFU (least frequently used) bcoz it is heavily used.

Not LRU bcoz it is in constant use.  
But its FIFO bcoz it was declared very earlier so it will get replaced, and it can also replace the page that is in constantly use.

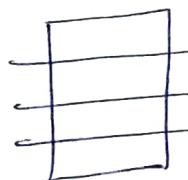
Gate 2007 on FIFO (P & Q statement)

→ Some programs do not exhibit the locality of references

→ Both the statements are right but Q is not the reason for P.

→ Reason for Belady's anomaly is stack property absence.

Gate-2010 Q 10 P  
If we are following demand paging then on 'n' pages we will have n page faults.



If we access 1-100 pages first at least 97, 96, 99, 100 will be in the same.

and when we access in reverse order 100, 99, 98, 97 pages are inside so they have no page fault and below 96 all have page fault.

$$\text{So, total page fault} = 100 + 96 \\ = \underline{\underline{196}}$$

→ Very Good and tricky question above one

Some interesting behaviour of optimal page replacement algo.

→ If looping follows in reference string as,

1 2 3 4 5 6 → 1 2 3 4 5 6 → 1 2 3 4 5 6 + 1

Say we have optimal algo. and 4 frames

1	2	3	→ Optimal behaviour as MRU
2	3	4	
3	4	5	
4	5	6	

Here we observed that we replace the page that is most recently used.

→ In case of most recently used

1	2	3
2	3	4
3	4	5

Same pattern as above

If we use LRU on same string then

X	8 3 Y 5
Y	8 4 X 6
Z	2 8 3 1
X	2 6 Y 2

So LRU works as worst performance

Similarly FIFO also did its worst performances [All page faults]

Note → If replacement called means (no. of frames < no. of pages) in case of looping then optimal and MRU is going to give best performance

Sequence Q.

1 2 3 4 5 6 7 8 8 7 6 5 4 3 2 1  
R                  Reverse(R)

In this case optimal work as LRU and FIFO and all the 3 will give same no. of page faults, but MRU give its worst performance and no. of page fault equals to no. of pages in string [all page faults].

Gate 2014 Question on LRU, MRU, LIFO, FIFO and optimal.

→ Simple and trick question So, Do it by self and write the trick if got (any) on the sticky CHT notes.

## Working set Algorithms

All the algo. we discussed till now have limitation that we had fix the number of frames called Static algorithm.

But in working set algo. we assume that the nearest future is close approximation of recent past.

1 2 3 1 2 4 1 4 2 1 5 1 2 4 2  
— — — — — — — — — — — — — — — —

Assume window size A = 4 then working sets are -

W <sub>0</sub> = {1, 2, 3}	W <sub>0</sub> = {1, 2, 4}
W <sub>1</sub> = {1, 2, 3, 4}	W <sub>1</sub> = {1, 2, 4, 5}
W <sub>2</sub> = {1, 2, 3, 4}	W <sub>2</sub> = {1, 2, 4, 5}
W <sub>3</sub> = {1, 2, 3, 4}	W <sub>3</sub> = {1, 2, 4, 5}
W <sub>4</sub> = {1, 2, 3, 4}	W <sub>4</sub> = {1, 2, 4, 5}

So, number of frames or pages required of a process is increasing or decreasing. So if process require all four we allot to it and if it require less than 4 we allot the other pages to other processes.

Average frame requirement

$$\begin{aligned} &= \frac{1+2+3 \times 10 + 4 \times 3}{\text{no. of working sets}} \rightarrow 15 \\ &= \frac{3+30+12}{15} = \frac{45}{15} = [3.0] = 3 \end{aligned}$$

Page fault limiting or decreasing Algo.  
→ It is the modification of working set algo.

Gate 1992 Question → Do it by self.

## Page replacement Algo. Implementation

NOT IMPORTANT FOR GATE

### Segmentation

Suppose that we have process that have allotted 4 frames in main m/m but process have 8 pages then system can manage the things using virtual m/m but in user point of view it is not considerable. User might think that how it works.

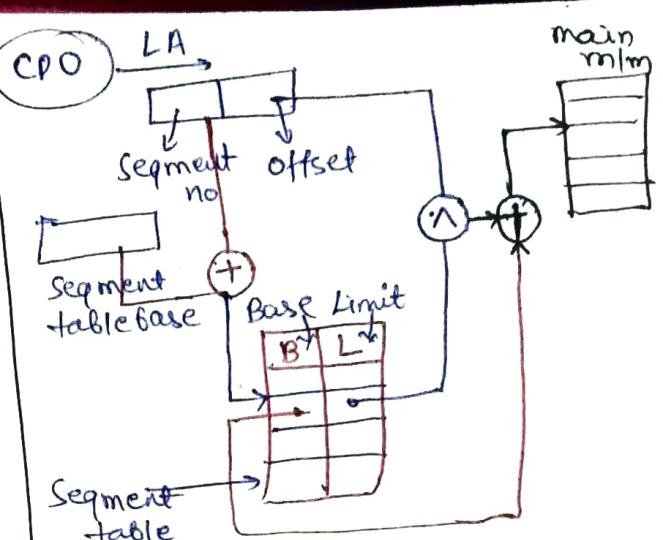
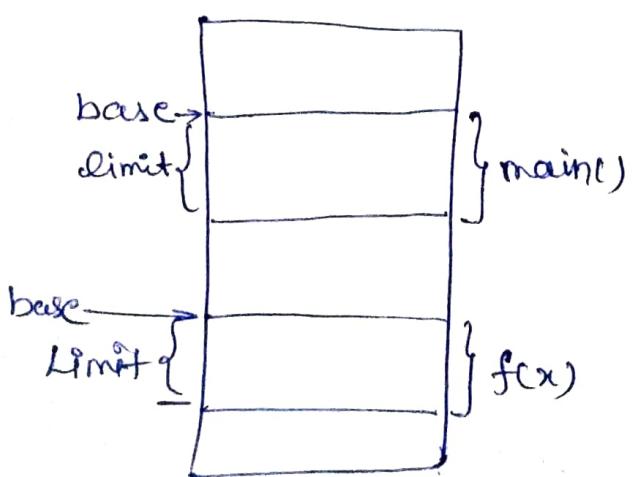
→ So, paging is a concept in System point of view and Segmentation is concept for User point of view.

In segmentation we devide the segments of a process as -



This way we form the segment for each program.

In main m/m we allotted space for each segment as

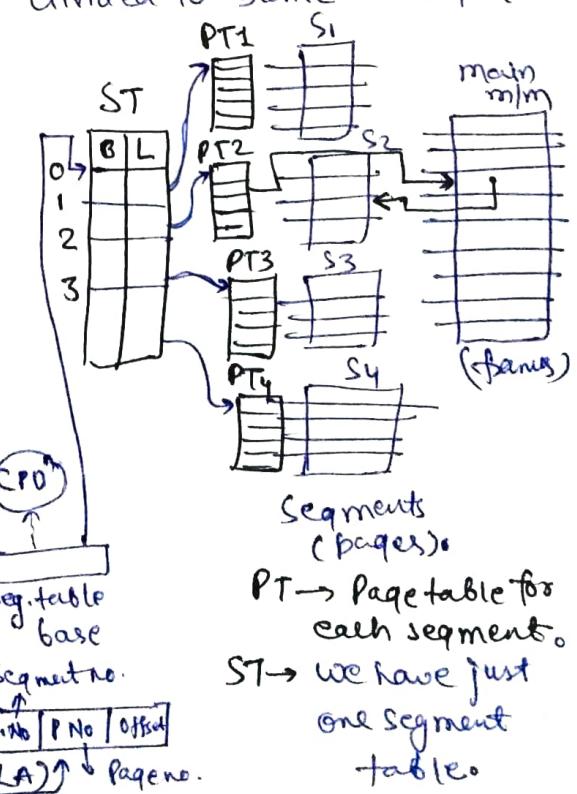


If value of offset < limit then add the value of offset to Base value and search it in main m/m.

Generally, segmentation doesn't used alone, we use segmentation and paging in a combine way.

### Segmented paging:

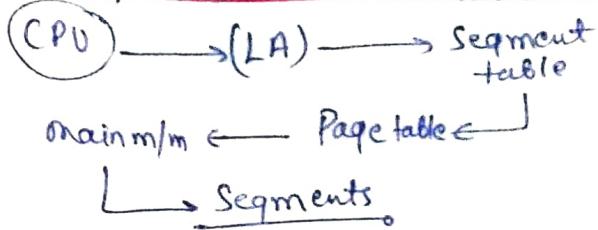
Segments need not be of same size but all the segments divided to same size pages.



Segments (pages).

PT → Page table for each segment.

ST → We have just one segment table.



- Each Page table take 1 frame and segment table also take 1 frame.
- Base register pointed to frame in which segment table is present (or segment table base).

Todo:  
Ques 1999 → [Do it by seeing question]  
 $PAS = VAS = 2^{16} B$ ,  
 $PA = VA = 16 \text{ bits}$  [Do by yourself first]

→ 8 non-overlapping equal size segments.  
 → Segment table have PA of Page table.  
 → Page table entry = 2B.

S.No	P.No	P. Offset
3	$(2^3=8)$	$x^0$ (say)

$$\begin{aligned} \text{Page size} &= 2^x \\ \text{No. of pages} &= 2^y \\ x+y+3 &= 16 \\ x+y &= 13 \quad \text{--- (1)} \end{aligned}$$

Ans  
 Page size  
 $= 2^7$

To fit page table in 1 page  
 Page table size = No. of entry \* size  
 $\Rightarrow 2^x = 2^y + 2$

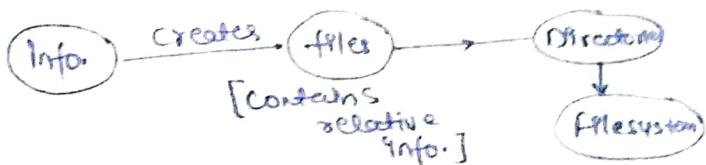
$$\Rightarrow 2^x = 2^y + 1$$

$$\Rightarrow x-y=1 \quad \text{--- (2)}$$

Using eqn (1) and eqn (2)  
 $x=7$      $y=6$

Ques file system, I/O and protection

Attributes and operations on file



# file is a abstract data structure that have following attributes -

- ① Name
- ② Identifier (.exe, .doc, .xls, .mp4)
- ③ Type (Text, video, Audio, etc)
- ④ Location [in case of more than two Hard disk]
- ⑤ Size (in bytes)
- ⑥ Protection [Password protected]
- ⑦ Time and Date

### File operations

- ① Creating [Some space allot in HD]
- ② Writing [Add some data in file]  
 Operating system maintain a pointer to maintain the last ended position of writing. So that we can start from forward to pointer.



- ③ Reading [Read the file sequentially]  
 $\checkmark$  It also have a read pointer  
 Both the pointers maintain by the OS.
- ④ Repositioning [Change the position of pointer]
- ⑤ Deleting [Delete the data and file attributes both]
- ⑥ Truncating [Delete the data of file only]  
 $\hookrightarrow$  Redo file

Cont-->

## Open/file Table

Information required to access a file -

- ① File pointer
- ② File open counter
- ③ Disk location of a file
- ④ Access right

Those files which are used by process very frequently. It's a good thing to maintain the info. about those files in main m/m.

Assume we have 2 processes,

P<sub>1</sub>                    P<sub>2</sub>

fileName	fb	AR

Each process has its own file table contains info. about file name, file pointer (fb) and access right (AR as read/write/exe).

Both the process might access the same file at a time and it is not to worry.

→ OS maintains this file table for each process along with this OS also maintains a open file table that contains location of file and open counters.

fileName	Location	OpenCount

As the process opens the file, open counter get incremented and as

file entry gets deleted in process file table (means process is not using file) file counter decremented.

→ If the value of open counter is '0' then entry gets deleted from Open file table.

## Accessing files

Access methods - :

- ① Sequential
- ② Direct
- ③ Indexed

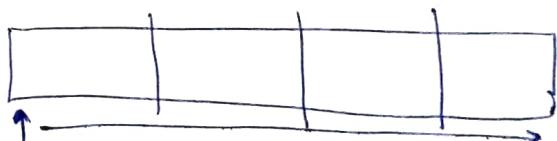
We divide the file into blocks called logical blocks.

In general file size is 512 B.

We divide HD into blocks called physical blocks (sector). Its size is also 512 bytes.

→ file might not always stored in the sequence.

file logical blocks



Access pointer

If you reading ~~scanning~~ or accessing bit by bit and incrementing the pointer sequentially called sequential access.

for direct access we have to maintain some entries like

- No. of records per block
- No. of records per file
- Block size

Indexed access uses by B and B+ trees generally

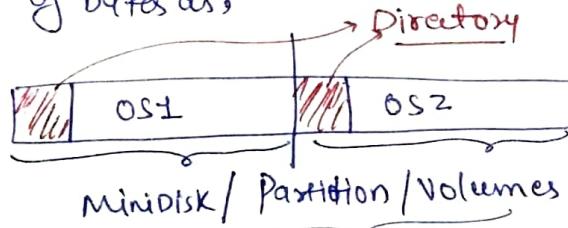
→ We access the record in file using index of records.

Most of OS provided sequential access.

### Directory Structure

We can have more than one file system in same computer bcoz we are using more than one OS in a single system.

Assume HD is continuous array of bytes as,



→ Divide the HD into various part and allocate to various file systems.

→ Each OS have different file system.

Ex. Windows have abc.dox  
Linux have abc.odt.

Each partition have special file called directory, that converts the file name to required info. for access.

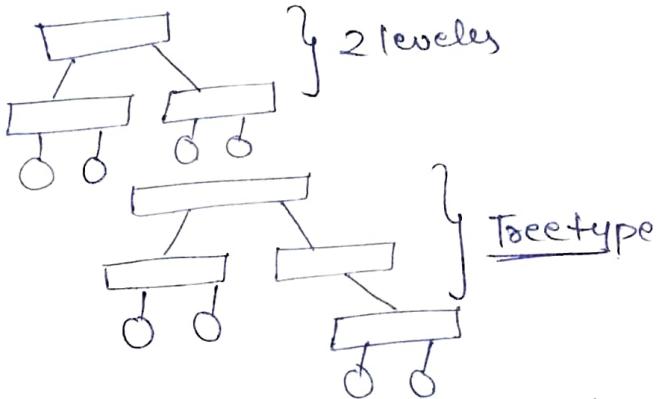
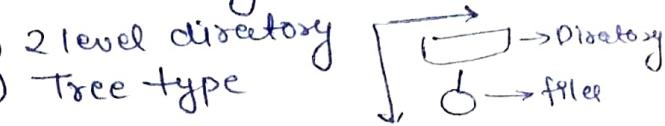
→ Directory contains metadata about files.

- i) Search
  - ii) Create a file
  - iii) Delete a file
  - iv) All the files in entry  
    ↳ List all the files
  - v) Traverse
  - vi) Rename
- Operations on directory

We generally have single level directory.

But if there is large no. of files then we sometimes need multi level directory as -

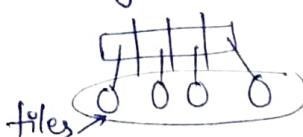
- i) 2 level directory
- ii) Tree type



We also have acyclic graph and graph directory. [Tree without cycle]

### Single level v/s two level directory

#### Single level

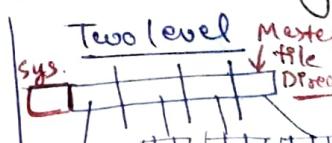


→ Simple implementation

→ Creating and searching is simple

→ Naming of file is difficult (Same names not allowed)

→ Access security is difficult



→ Master contain user info.

→ Each user have different directory so searching is easy.

→ Two users can have file with same name.

→ OS takes care of access rights to particular directory.

→ One user can't access the system file of another user. 😞 [Soln]

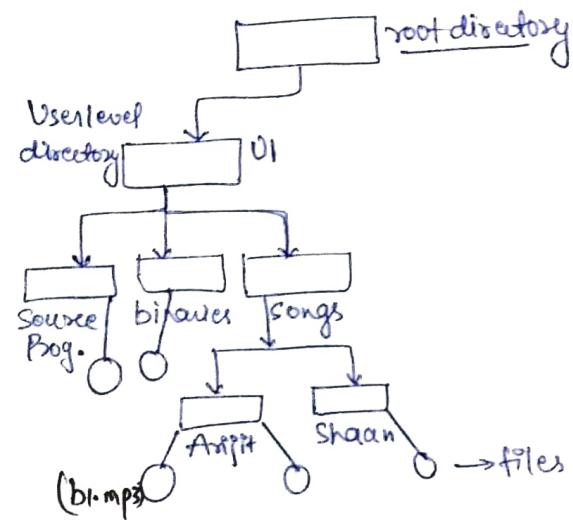
Soln → Create a separate directory in Master that contain only System files. [Sys]

→ Two level is difficult to implement

## Tree Structured Directory

Extension to 2-level directory.

→ In this directory user can also group same kind of files



→ files can be obtained at any level.  
→ Here, path used to access the file

root/U1/songs/Arijit/bl.mp3

# Absolute path name → from [root to bl.mp3]

# Relative Path name: If root/U1 taken from present working directory then we can do the same using the given path as,

songs/Arijit/bl.mp3

✓ We have variable that maintains the state of present working directory. It can be named varying from OS to OS.

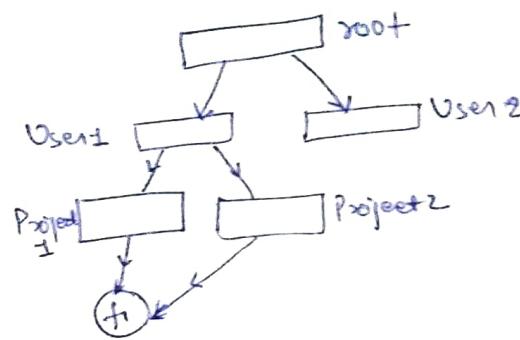
→ We can also change the present working directory if OS provide us permission using some System Calls.

Permission required → Read / Write / Execute Permission.

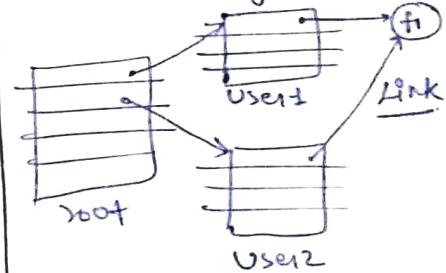
→ Traversing is not easy.

## Acyclic Graph

Now files can be shared between two directories.



→ Simplest way to share the file is make copies in both but if one user is update it will not reflect in another copy



This way using links we can share files. This way directories form a acyclic form (cycle not formed).

## Problem

Assume User1 delete the file and delete it but User2 is also pointing the same file that doesn't exist there. It arises the situation same as dangling pointer.

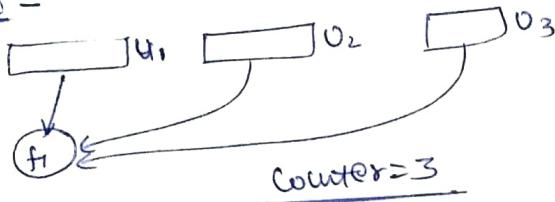
→ Same file can have different path names.

→ We can also share directory so links can be created for directory too.

To delete a file there is problem bcoz many links are connected to single file.

So, make variable as counter that have value equals to no. of references to file and if all the references get deleted then delete the file.

Ex -



## File Systems

File systems provides the mechanism for on-line storage and access to file contents including data and programs.

File-system is a software that deals with files.

file system deals with following issues:-

- (1) File structure
- (2) To allocate disk space
- (3) Recovering freed space
- (4) To track location of data
- (5) Interface other parts of OS to secondary storage

## File System Structure

File sys. provides efficient and convenient access to the disk by allowing data to be stored, located and retrieved easily.

We generally follows layer approach.

Benefit of layer approach is - if we change in any layer it will not reflect in another layer.

### Application Program

↓ ask for file to access  
Logical file System (Metadata, manage Directory str.)  
↓

### File Organization Module

↓ (Logical block → physical blocks)  
free space management

### Basic File System (Commands to

↓ I/O control buffering)

### I/O Control (Consist device drivers, interrupt handles)

### Devices

→ Logical file system manages directory str. and identifies which file is asked.

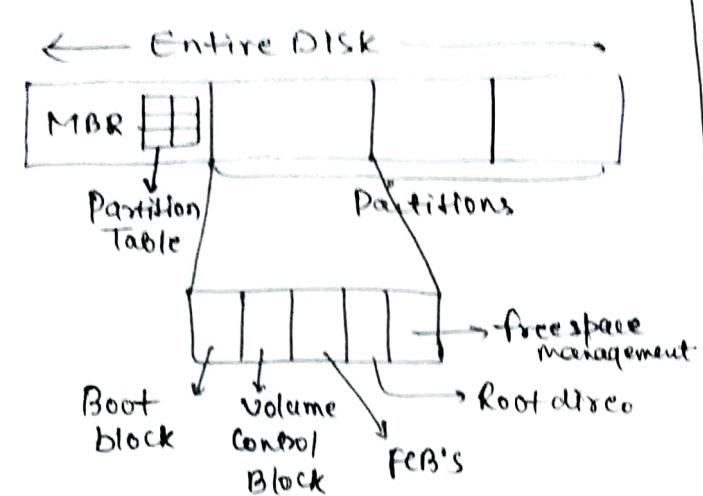
→ It also divide the file into logical blocks

→ File organization module map logical block with physical block and allot the free space to required files.

→ Store the block in main m/m in buffer that (maintain temporarily).

→ Basic file system issues command to I/O control and device drivers get the data using those commands.

## MBR (Master Boot Record)



When you turn ON the system the RAM have nothing to execute so a special program BIOS (Basic Input Output System) get loaded from ROM to RAM to start a procedure called as booting.

→ As BIOS get activated it loads the MBR in RAM and due to this you get options in front screen as-

- Windows
- Ubuntu
- Mac OS

If you have multiple OS then you get the options and select from your choice. MBR also have a partition table that contains starting of each partition.

→ Each system have an active file system (OS). If you have only one file system by default that is active otherwise you have to select it.

'On disk' data structure uses 'in file system implementation'

Each file system uses different data structures.

Several 'in memory' and 'on disk' structures are used to implement a file system.

These structures vary depending on the OS and file system but general principles apply.

### Boot Control block (per partition)

It contains info. need by System to boot an OS from that partition.

- In Unix file system called as boot block
- In NTFS called as partition boot sector

NTFS → New Technology file sys.

→ Every OS have suppose to maintain Boot control blocks

### Volume control block: It

Contains volume details such as no. of blocks and its size in partition.

In UFS called as Super block

In NTFS called as master-file table

→ You can also find about the empty blocks.

### Directory str per file system

It is used to organize the files.

In UFS this includes file

Names and associated 'inode' numbers  
[Index Block]

## File Control Block (FCB)

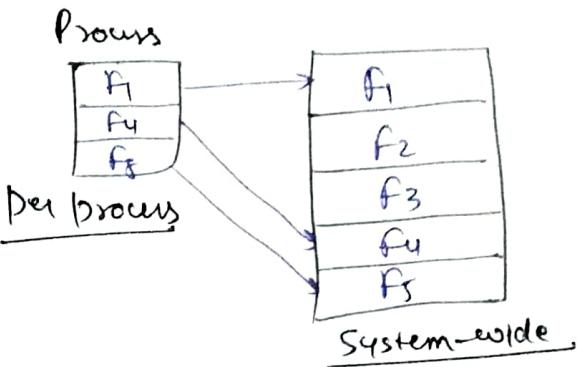
It contains details about files.

file permission
file dates (create, access, write)
file owner, group
file size
file data blocks or pointer to file data block

file control block

## (IV) per process open file table

It contains pointer to appropriate entry in the system wide open file table.

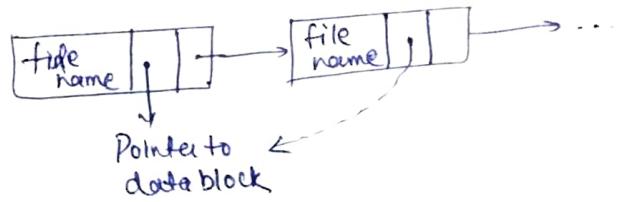


## Directory Implementation

The selection of directory allocation and directory management algo. significantly affects the performance and reliability of file systems.

### Algorithms:

#### 1. Linear List



Here, search operation is going to take lot of times

#### 2. Hash Table

key	value

It have Linear list and Hash table both.

→ It makes the searching easy in O(1) time

→ It have fixed size only and also have collisions.

→ We can also use B and B+ trees for implementation.

Mounting → Create new partition.

Ex → As you connect your pen-drive system creates a new partition for you.

(I) In-memory mount table: It contains information about each mounted volumes

(II) In-memory directory store Cache: It holds the directory info of recently accessed directory.

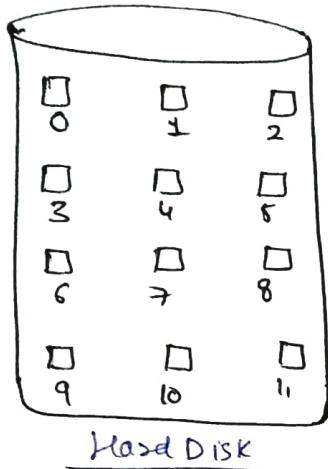
(III) System-wide Openfile table:

It contains the info. of each open file by OS and contains FCB.

## Allocation methods

→ How to allocate space to the files so that disk space is utilized effectively and files can be accessed quickly?

## Contiguous Allocation



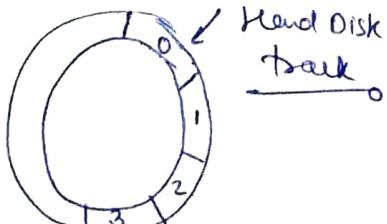
directory		
file	start	length
temp	0	2
tr	5	4
list	10	2

temp 0 [ ]

to	5	[ ]
=	6	[ ]
	7	[ ]
	8	[ ]

11st	10	[ ]
	11	[ ]

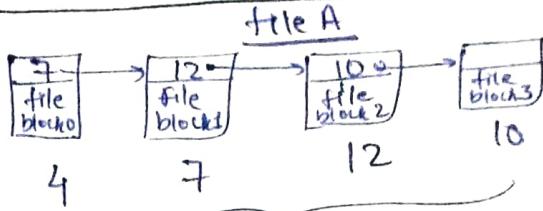
# So, we are using contiguous allocation  
→ Read performance is excellent due to sequential allocations



→ Disadvantages: Disk becomes fragmented  
→ Internal fragmentation can be possible as it needs required 2.5 blocks.  
But we can't avoid it.

We can avoid external fragmentation using non-contiguous methods

## Linked List allocation



(4, 7, 12, ) are physical blocks in which file blocks are saved.

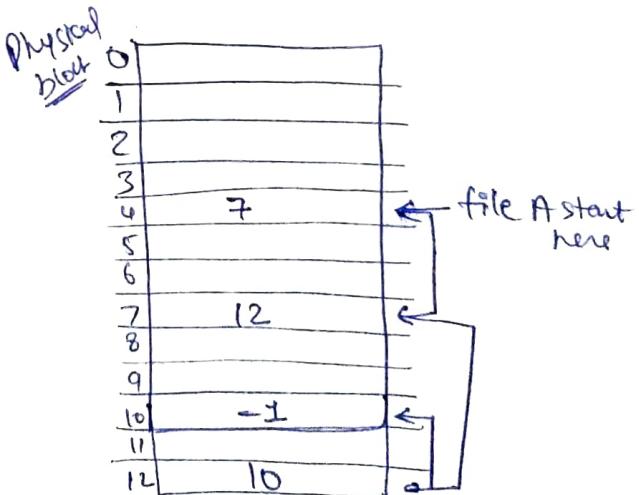
- Advantages → ① Every disk block can be used.
- ② No external fragmentation, so no space lost (except internal fragmentation).

Disadvantages → Random access is very slow  
→ Pointers takes few bytes.

[ 9mb. concept to learn ]

## File Allocation Table

If you want to access randomly in linked list allocation then we use file allocation table.



Each block contain index of next file blocks

- But its size might be large or very large.
- But it provides random access.

Hard Disk = 20GB (say)

Size of blocks = 1KB

$$\text{No. of blocks} = \frac{20\text{GB}}{1\text{KB}} = 20\text{M}$$

If blocksize = 4B

then

$$\text{Size of table} = 20\text{M} \times 4\text{B} \\ = 80\text{MB}$$

→ This table is also a  $(n-m)m$

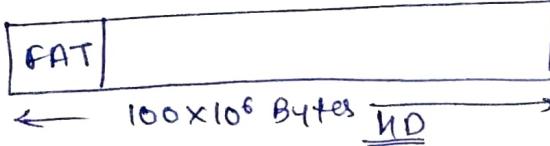
data structure, so we can do random access quickly.

~~Ans~~ [Must do by self first]  
Gately on File Allocation Table

$$\text{Disk size} = 100 \times 10^6 \text{ bytes}$$

$$\text{Data block size} = 10^3 \text{ B}$$

$$\text{FAT entry size} = 4\text{B}$$



$$\text{FAT} = \text{No. of entries} \times \text{size of entry}$$

$$\text{No. of blocks in HD} = \frac{100 \times 10^6}{10^3} \\ = 10^5$$

$$\text{No. of blocks} = \text{No. of entries in FAT}$$

$$\text{PAT} = 4 \times 10^5 = 0.4 \times 10^6 \text{ B}$$

Space available for file

$$= 100 \times 10^6 - 0.4 \times 10^6 \\ = 99.6 \times 10^6 \text{ bytes}$$

Ans - 99.6

## Indexed allocation

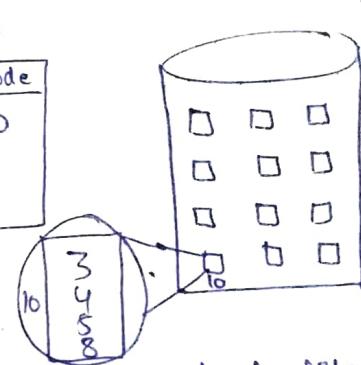
→ Linked allocation solves the external fragmentation and size declaration problem of contiguous allocations.

→ In the absence of FAT, linked allocation doesn't support direct access efficiently.

→ Indexed allocation solves the problem by bringing all the pointers together into one location: the inode.

→ inode → Index block are same directory

f-Name	inode
A	10



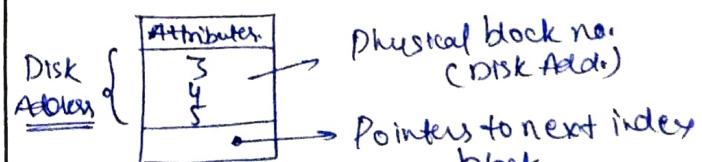
Index allocation is concept to avoid FAT table large size

The blocks allotted to file A are 3, 4, 5, 8 in physical m/m (HD).

→ If index block is not completely filled then internal fragmentation occurs and we can't manage this.

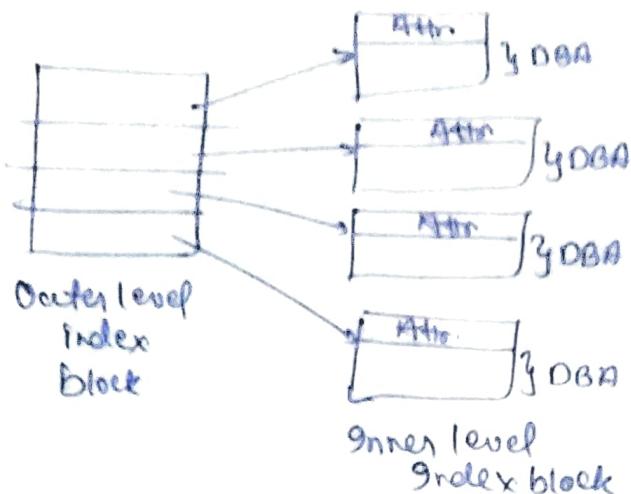
→ But if it is too small in size, however it will not be able to hold enough pointers to hold for a large file.

① Linked schema: We can link several index blocks.



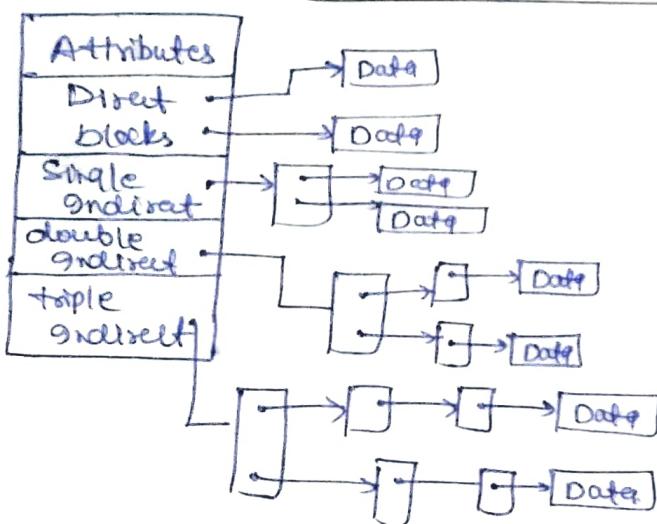
→ Maintain multiple inode for a single file.

## ② Multilevel Index



→ Inner Index block contains attributes and Disk Block Addresses.

## ③ Combined scheme → Used in UNIX [Remember the diagram]



This way we can use to store huge index file in just one block.

## Gate 2004 [Solve it using diagram] [Do it by reading question]

Direct block → 10 entries point to

$$\text{Single indirect} \rightarrow \frac{1024B}{4B \text{ bits}} = \frac{1024B}{6B} = 170 \text{ pointers}$$

$$\text{Double indirect} = (170 \times 170)$$

$$\text{Triple indirect} = (170 \times 170 \times 170)$$

$$\rightarrow \text{No of data blocks} = a$$

$$a = (10 + 170 + 170^2 + 170^3)$$

$$\rightarrow (\text{size of file})_{\text{max}} = a \times 1024B$$

Note → Above question is necessary to do. It might ask this time.

Gate-2012! Only S.29 in OS  
gmp Made easy PVG

## freespace Management

The first responsibility of file system is allocate blocks to each file and keep track of it.

The second responsibility is to manage how manage blocks are free for next allocation. The method used is -

## ① Bit Vector [Array of bits]

The free space list is implemented as a bit map or bit vector.

Each block is represented by 1 bit.

Say the block is free bit is 1 else bit is 0.

0	1	2	3	4	5	6	7	Initial State
1	1	1	1	1	1	1	1	

Say 2, 4, 5 blocks get filled then,

0	1	2	3	4	5	6	7
1	1	0	1	0	0	1	1