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**Anomaly Detection** 

## Outlier Detection (Anomaly Detection)

- So far, we have focused on choosing models which will be useful to predict
- In many situations, this isn't really what we want to do with our data
  - Example: Enron project!
  - Our Y variable is really "fraud" which is unobserved
- The idea behind anomaly detection is to pick observations which seem unusual compared to the rest of the data



### What Is Unusual?

 We can determine what's "usual" in the data in the context of one of our models:

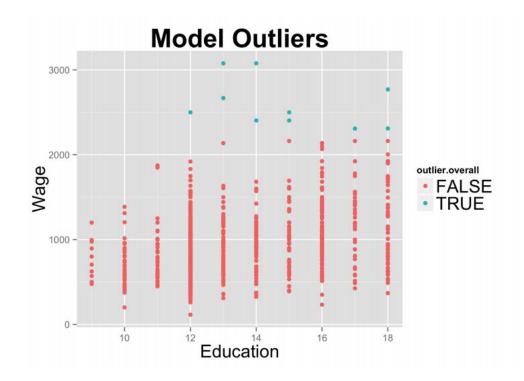
$$y = f(X) + \varepsilon$$

- Look at the distribution of ε
- Are there points very badly fit?
- Or we can do this without a model



### Outlier Detection: No Model

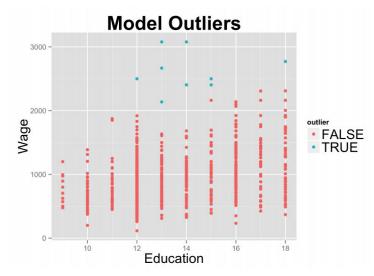
Definition: An outlier is more than 3 standard deviations from mean





# Outlier Detection: Using Regression Model

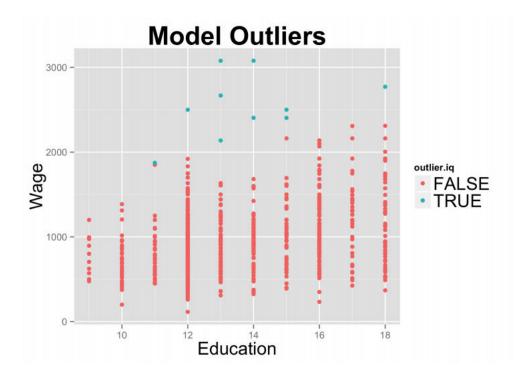
- Model:  $wage = \alpha + \beta \ educ + \varepsilon$
- **Definition**: An outlier has  $\hat{\varepsilon}$  more than 3 standard deviations from the mean





## Outlier Detection Depends on Modeling

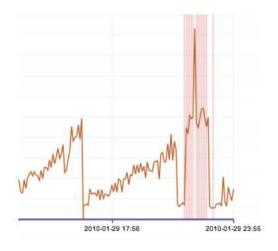
- Model:  $wage = \alpha + \beta \ educ + \gamma IQ + \varepsilon$
- **Definition**: An outlier has  $\hat{\varepsilon}$  more than 3 standard deviations from the mean





### We Can Have Time Series Anomalies

- Some points aren't necessarily anomalies except when considered in their context
- This can apply to time series as well





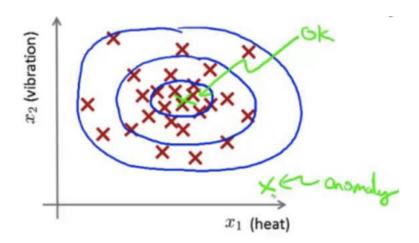
### Key Pieces of Outlier Detection

- Define a measure of distance
  - This can be based on a model (with residuals) or not
  - It can have multiple dimensions
- 2. Calculate this measure for each observation
- 3. Look at the points with the largest values



## Anomaly in 2 Dimensions

- Once you have a measure of distance in 2 dimensions, you can calculate anomalies this way too
- Or you could think about using a model and looking at residuals





## Lesson Summary

- Anomaly detection is to pick observations which seem unusual compared to the rest of the data
- It can be done with or without a model
- To find an anomaly, you pick a measure of distance, calculate it for each observation, then look at the points with the largest values
- Whether a point is an anomaly depends on its "context" or what model you're using to assess it.

