# CS4780/5780 Final

#### Fall 2018

#### **Instructions:**

- 1. Please turn off and stow away all electronic devices
- 2. This is a **closed book and notes** exam.
- 3. You have 150 minutes.
- 4. Please **don't** write on the back of the pages.
- 5. Write down individual steps to maximize for partial credit. If you believe a question is unclear, then please don't hesitate and ask us about it! Please always state any assumption you make. Good luck!

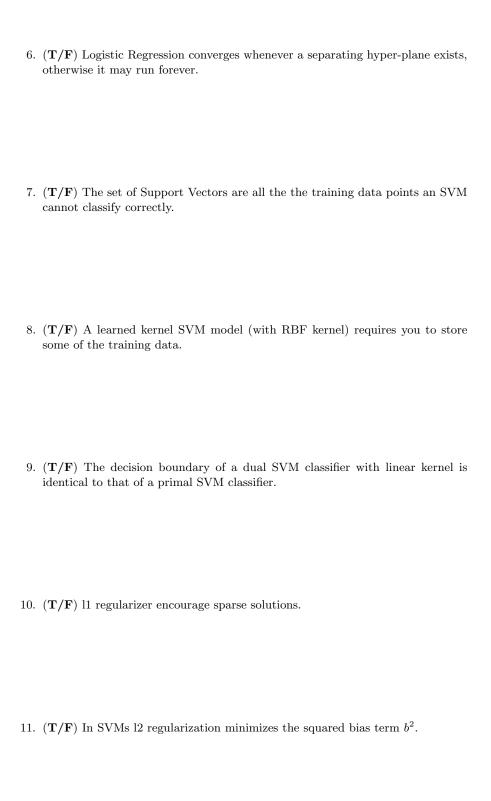
I promise to abide by Cornell's Code of Academic Integrity.

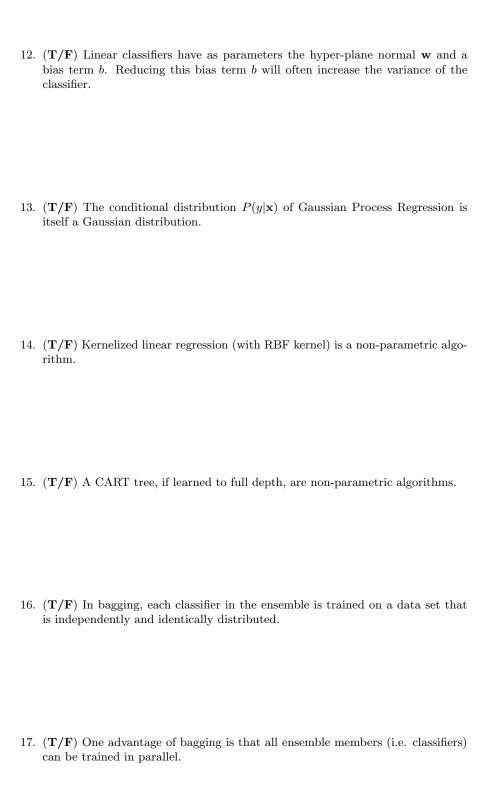
NAME:	
Net ID:	
Email:	

# 1 [??] General Machine Learning

Please identify if these statements are either True or False. Please justify your answer **if false**. Correct "True" questions yield 1 point. Correct "False" questions yield two points, one for the answer and one for the justification.

	yield two points, one for the answer and one for the justification.				
1.	(BONUS: 3 pts) I filled out the course evaluation for CS4780/5780. (True/False, no explanation required).				
2.	$(\mathbf{T}/\mathbf{F})$ The fewer assumptions an algorithm makes, the better it is. In practice the best algorithm is Genetic Programming which makes no assumptions at all.				
3.	$(\mathbf{T}/\mathbf{F})$ With Random Forests there is no need to perform a training/validation				
	split.				
4.	(T/F) MLE is great to learn the parameters of a binomial distribution, but it				
	cannot be used to learn the parameters of a separating hyper-plane.				
5.	$(\mathbf{T}/\mathbf{F})$ The Naive Bayes classifier assumes that all features are independent.				





18.	$(\mathbf{T}/\mathbf{F})$ Ada Boost with decision trees (depth 3) is non-parametric.
19.	$(\mathbf{T}/\mathbf{F})$ Ada Boost terminates the moment it reaches $0\%$ training error.
20.	$({\bf T/F})$ One advantage of Random Forests is that you obtain meaningful probability estimates as your output predictions $P(y {\bf x}).$
21.	$(\mathbf{T}/\mathbf{F})$ Deep convolutional neural networks are particularly well suited for image classification tasks.
22.	$(\mathbf{T}/\mathbf{F})$ The optimization of deep neural networks is a convex minimization problem.

### 2 [19] Bias Variance / Model Selection

1. (3) Your Decision Tree classifier has a training error of 0% and a testing error of 87%. What can you say about the bias/variance trade-off (assuming the data is not noisy). Name two possible interventions to reduce the testing error?

2. (3) For k-fold cross validation, describe the positive and negative effects as  $k \to n$ . When would you be most inclined to use k = n?

3. (6) The expected regression error decomposes into three terms. Write down the mathematical decomposition and label each term.

4. (3) Explain why adding more training data does not always help reduce your testing error below a desired threshold  $\epsilon > 0$ . Describe such a scenario.

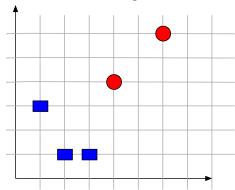
- 5. (4) Consider the following algorithms and highlighted hyper-parameters. Decide whether *increasing* these parameters could help reduce overfitting. Answer with "Yes" or "No" ("Ja", and "Nein" is also acceptable.)
  - a. The number of hidden units in the Neural Network.
  - b. The maximum depth in Decision Trees.
  - c.  $\lambda$  in Logistic Regression, trained with a  $\lambda \sum_{j} w_{j}^{2}$  penalty in the objective.
  - d. The number of iterations T in Boosting.

## 3 [22] Kernel Methods

1. (2) Name one condition that is necessary and sufficient for a matrix  ${\bf K}$  to be positive semi-definite.

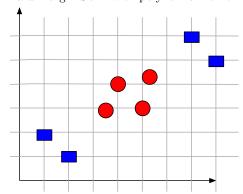
2. (3) Which of the following algorithms can be kernelized: a) Decision Trees, b) Linear Regression, c) Gaussian Processes. Justify your answer.

3. (4) Consider the following data set. Draw the decision boundary you would obtain with a hard margin linear SVM? Circle all the support vectors!



- 4. (3) Add two blue points (#1 and #2) such that #1 would and #2 would not affect the decision boundary if the SVM was re-trained.
- 5. (4) Let m be the number of support vectors of an SVM trained on n data points (with RBF kernel). For a fixed n imagine you increase the dimensionality d of the data until it becomes very large. How would you expect the ratio  $\frac{m}{n}$  to change as  $d \gg 0$ ?

- 6. (2) Describe a scenario in which you may want to use a kernel SVM with linear kernel instead of a standard linear (primal) SVM.
- 7. (2) Consider the following data set. Draw a plausible decision boundary for a hard-margin SVM with polynomial kernel.



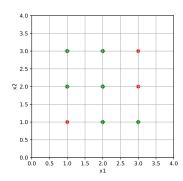
8. (2) You are given a non-linear regression data set. You are deciding between training a Gaussian Process or kernelized linear regression (both with RBF Kernel). Which one will have lower testing / training error?

## 4 [14] Decision Tree

1. (4) Name two advantages of decision tree over nearest neighbor algorithms.

2. (2) Name the CART stopping criteria (with unlimited depth).

3. (8) Consider the classification dataset S with |S|=9 visualized in the following figure and table:



i	$\mathbf{x}_i$	$y_i$
1	(1, 1)	+1
2	(1, 2)	-1
3	(1, 3)	-1
4	(2, 1)	-1
5	(2, 2)	-1
6	(2, 3)	-1
7	(3, 1)	-1
8	(3, 2)	+1
9	(3, 3)	+1

(a) (2) Compute the Gini impurity for this dataset before any split.

(b) (6) Perform the CART algorithm with *Gini impurity* on *S*. Please draw a resulting tree (with splitting values and features) and also draw the corresponding hyper-planes in the previous figure.

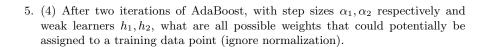
### 5 [21 points] Ensemble Methods

1. (3) What loss function does AdaBoost minimize? (Write down the precise mathematical form.)

2. (2) Imagine 10% of your binary training data (all points unique) are accidentally mislabeled. What is the training error that AdaBoost will converge to after sufficient rounds of boosting?

3. (2) Describe a data scenario in which AdaBoost is not a good choice. Justify your answer.

- 4. (6) Given a distribution P you can sample a training set D and obtain a classifier h. Imagine you train m such classifiers  $h_1, \ldots, h_m$  on m data sets  $D_1, \ldots, D_m$ , each drawn i.i.d. from the data distribution P. As you increase m from m = 1 to  $m \gg 0$ ,
  - show how you can use these models to obtain a low variance classifier  $\hat{h}$ .
  - what happens to the variance of  $\hat{h}$  in the limit,  $m \gg 0$ ?
  - how does the bias of  $\hat{h}$  compare to the bias of h?



6. (4) Robin is trying to use AdaBoost on full CART trees without depth limit (all training points are distinct). Although the code seems correct, it crashes in the very first round. What do you think is the problem?

## 6 [12] Deep Learning

1. (2) Name two reasons why Newton's Method typically is not used to train deep neural networks.

2. (2) Let the loss function be  $\ell(\mathbf{w}) = \frac{1}{2n} \sum_{i=1}^{n} (\mathbf{x}_{i}^{\top} \mathbf{w} - y_{i})^{2}$ . Write down the update for *Stochastic* Gradient Descent and Gradient Descent.

3. (2) Suppose you have a convolutional filter of size  $k \times k$ . When you apply this filter to a  $n \times n$  input image, what is the dimension of the output feature map with no padding?

4. (2) Suppose you have a  $3 \times 3$  matrix I from one patch of an image. Each matrix value corresponds to a pixel.

$$I = \begin{bmatrix} 3 & 1 & 1 \\ 3 & 0 & 2 \\ 4 & 4 & 0 \end{bmatrix}$$

and filter kernel

$$k = \begin{bmatrix} 1 & 0 \\ 1 & 1 \end{bmatrix}$$

What is the output matrix after convolving the input I with k (no flipping of the kernel in case you learned that in your computer vision/signal processing class)? We don't consider the padding and stride here. The output should be a  $2\times 2$  matrix.

#### 5. (4) Consider you have the following neural network:

• Input layer: 80 units

First hidden layer: 20 hidden units
Second hidden layer: 60 hidden units
Third hidden layer: 20 hidden units

• Output layer: 80 units

• Sigmoidal activation for each hidden layer and the output

 $\bullet$  Loss function: logistic loss

Each layer has a bias. How many parameters does this neural network have? You can leave your answer as an expression.

This page is left blank for jokes. (Nothing too inappropriate.)

This page is left blank for scratch space.