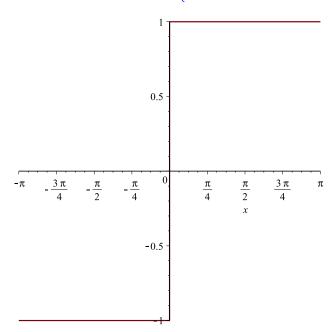
PRZYKAD 1

f := piecewise(x > -Pi and x < 0, -1, x = 0, 0, x > 0 and x < Pi, 1); plot(f, x = -Pi ...Pi)

$$\begin{cases} -1 & -\pi < x \text{ and } x < 0 \\ 0 & x = 0 \\ 1 & 0 < x \text{ and } x < \pi \end{cases}$$



$$ff1 := \frac{2 \cdot (1 - (-1)^1)}{\text{Pi} \cdot 1} \cdot \sin(1 \cdot x)$$

$$\frac{4\sin(x)}{\pi}$$
 (1)

$$ff2 := \frac{2 \cdot (1 - (-1)^2)}{\text{Pi} \cdot 2} \cdot \sin(2 \cdot x)$$

$$ff3 := \frac{2 \cdot (1 - (-1)^3)}{\text{Pi} \cdot 3} \cdot \sin(3 \cdot x)$$

$$\frac{4}{3} \frac{\sin(3x)}{\pi} \tag{3}$$

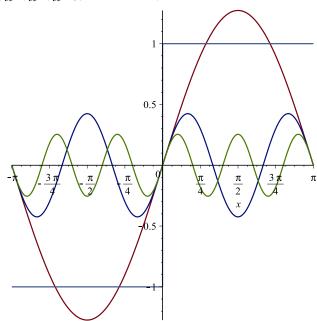
$$ff4 := \frac{2 \cdot \left(1 - \left(-1\right)^4\right)}{\text{Pi} \cdot 4} \cdot \sin(4 \cdot x)$$

0 (4)

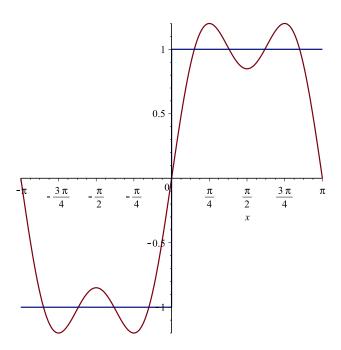
$$ff5 := \frac{2 \cdot \left(1 - \left(-1\right)^{5}\right)}{\text{Pi} \cdot 5} \cdot \sin(5 \cdot x)$$

$$\frac{4}{5} \frac{\sin(5x)}{\pi} \tag{5}$$

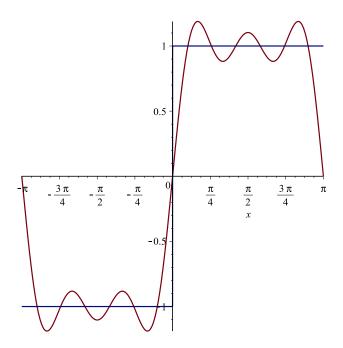
 $plot(\{f, ff1, ff3, ff5\}, x =-Pi...Pi)$



$$plot(\{f, ff1 + ff3\}, x = -Pi...Pi)$$



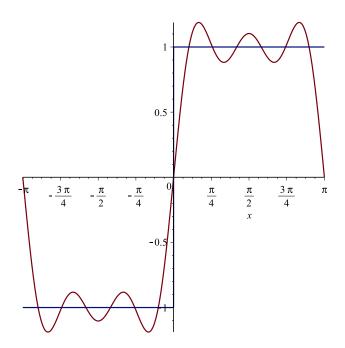
$$plot(\{f, ff1 + ff3 + ff5\}, x = -Pi..Pi)$$



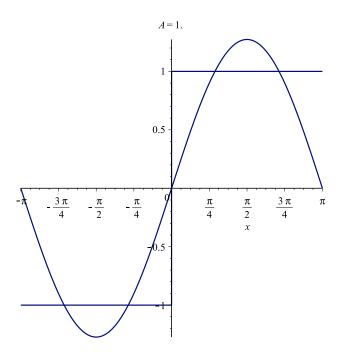
ffn := Sum
$$\left(\frac{2 \cdot (1 - (-1)^n)}{\text{Pi} \cdot n} \cdot \sin(n \cdot x), n = 1..5\right)$$

$$\sum_{n=1}^{5} \frac{2 (1 - (-1)^n) \sin(n x)}{\pi n}$$

$$plot(\{f, ffn\}, x = -\text{Pi} ..\text{Pi})$$
(6)



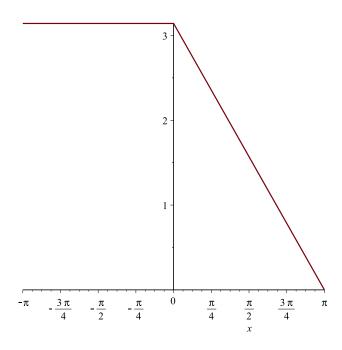
$$with(plots): animate \bigg(\text{plot}, \bigg[\bigg\{ f, Sum \bigg(\frac{2 \cdot \big(1 - (-1)^n \big)}{\text{Pi} \cdot n} \cdot \sin(n \cdot x), \, n = 1 \dots A \cdot 2 \bigg) \bigg\}, \, x = - \text{Pi} \dots \text{Pi} \bigg], \, A = 1 \dots 10, \, frames = 10, \, trace = 0 \bigg)$$



PRZYKAD 2

restart; f := piecewise(x > -Pi and x < 0, Pi, x = 0, Pi, x > 0 and x < Pi, Pi - x); plot(f, x = -Pi ..Pi)

$$\left\{ \begin{array}{ll} \pi & -\pi < x \text{ and } x < 0 \\ \pi & x = 0 \\ \pi - x & 0 < x \text{ and } x < \pi \end{array} \right.$$



$$ff0 := \frac{3 \cdot Pi}{4}; ff1 := \frac{\left(1 - (-1)^{1}\right)}{Pi \cdot 1^{2}} \cdot \cos(1 \cdot x) + \frac{(-1)^{1}}{1} \cdot \sin(1 \cdot x)$$

$$\frac{3}{4} \pi$$

$$\frac{2 \cos(x)}{\pi} - \sin(x)$$

$$ff2 := \frac{\left(1 - (-1)^{2}\right)}{Pi \cdot 2^{2}} \cdot \cos(2 \cdot x) + \frac{(-1)^{2}}{2} \cdot \sin(2 \cdot x)$$

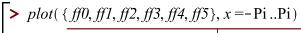
$$\frac{1}{2} \sin(2 x)$$

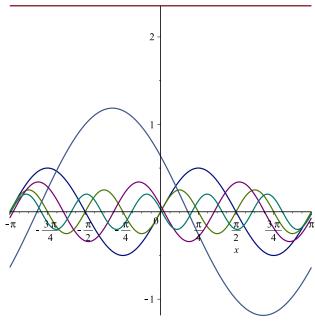
$$ff3 := \frac{\left(1 - (-1)^{3}\right)}{Pi \cdot 3^{2}} \cdot \cos(3 \cdot x) + \frac{(-1)^{3}}{3} \cdot \sin(3 \cdot x); ff4 := \frac{\left(1 - (-1)^{4}\right)}{Pi \cdot 4^{2}} \cdot \cos(4 \cdot x) + \frac{(-1)^{4}}{4} \cdot \sin(4 \cdot x); ff5 := \frac{\left(1 - (-1)^{5}\right)}{Pi \cdot 5^{2}} \cdot \cos(5 \cdot x) + \frac{(-1)^{5}}{5} \cdot \sin(5 \cdot x)$$

$$\frac{2}{9} \frac{\cos(3x)}{\pi} - \frac{1}{3} \sin(3x)$$

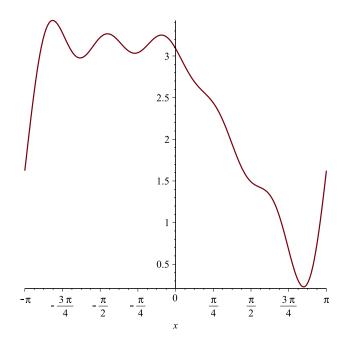
$$\frac{1}{4} \sin(4x)$$

$$\frac{2}{25} \frac{\cos(5x)}{\pi} - \frac{1}{5} \sin(5x)$$
(9)





$$plot\left(\frac{3\cdot \text{Pi}}{4} + Sum\left(\frac{\left(1 - \left(-1\right)^{n}\right)}{\text{Pi}\cdot n^{2}}\cdot \cos(n\cdot x) + \frac{\left(-1\right)^{n}}{n}\cdot \sin(n\cdot x), n = 1..5\right), x = -\text{Pi}..\text{Pi}\right)$$



$$with(plots): animate \left(\text{plot}, \left[\left\{ f, \frac{3 \cdot \text{Pi}}{4} + Sum \left(\frac{\left(1 - \left(-1 \right)^n \right)}{\text{Pi} \cdot n^2} \cdot \cos(n \cdot x) + \frac{\left(-1 \right)^n}{n} \cdot \sin(n \cdot x), n = 1 \dots 5 \right) \right] \right\}, x = -\text{Pi} \dots \text{Pi} \left[A = 1 \dots 8, frames = 8, trace = 0 \right)$$

