Exercise 7

Simon A. Broda

1. Until 1971, as part of the Bretton-Woods system of fixed exchange rates, the US dollar was convertible to gold, i.e., it was possible for foreign central banks to redeem US dollars for gold at a fixed rate of 35$ per troy ounce, so that the price of gold was fixed. In 1971, US president Nixon unilaterally cancelled the direct convertibility, ultimately ending the Bretton-Woods agreement. Gold became a floating asset, and its price increased sharply; in other words, the US$ was massively devalued. In this exercise, we will analyze the hypothesis that the increasing price (in US$) of oil is not a consequence of an increased demand for (or a reduced supply of) oil, but rather of a continued devaluation of the US$. We have at our disposal monthly data from April 1968 to January 2017 (586 observations) on the following variables:

   - GOLD, the spot price of one troy ounce of gold in US$;
   - OIL, the spot price of one barrel of WTI crude oil in US$.

   (a) Assuming that GOLD is integrated of order one, explain why the hypothesis that the relative price of oil (in troy ounces of gold per barrel) is stationary implies cointegration between log(OIL) and log(GOLD).

   (b) Using the file `oil_gold_2017.wf1`, analyze whether this cointegrating relationship can be found in the data, based on the Engle-Granger procedure.

2. Consider the model

$$Y_t = \beta_1 + \beta_2 X_t + U_{1,t}$$
$$X_t = X_{t-1} + U_{2,t}$$

   where $\beta_2 \neq 0$, $U_{1,t}, U_{2,t} \overset{\text{iid}}{\sim} (0, \sigma^2)$ independently of each other.

   (a) Is X_t stationary?

   (b) Is Y_t stationary?

   (c) Are X_t and Y_t cointegrated? If yes, what is the cointegrating vector?

   (d) Derive the bivariate VECM for Y_t and X_t.