

University of Stuttgart  
Germany

# Mixed-effects models in EEG

Statistically evaluating mixed-effects models for EEG analysis  
using large-scale simulations

June 30, 2022

# About me



**Luis**  
Lips

## Education

- Information Systems B.Sc
- Computer Science M.Sc.

## Journey to master thesis

- got in touch via Bene's EEG course
- got excited and stayed for the FaPra



# Agenda

**Overview**



**Goals**



**Approach**



**Schedule**



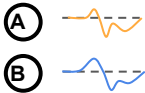
# Overview



**Number of subjects**



**Number of trials**



**Between-subject  
variability**



**Modelling  
Scheme**

Analysis



**Statistical  
Power**



# Modelling Schemes

**Two-way  
approach**

**Meta-  
models**

**Mixed-effects  
models**



# Goals

## Two-way approach

“Linear regression”  
 $y = X\beta + \epsilon$

$$\epsilon \sim N(0, R)$$

## Meta-model

$$y_{i\Box} = \mu + \delta_{\Box} + \epsilon_{i\Box}$$

$$\delta_{\Box} \sim N(0, \tau^2)$$

$$\epsilon_{i\Box} \sim N(0, \sigma_{\Box}^2)$$

## Mixed-effects model

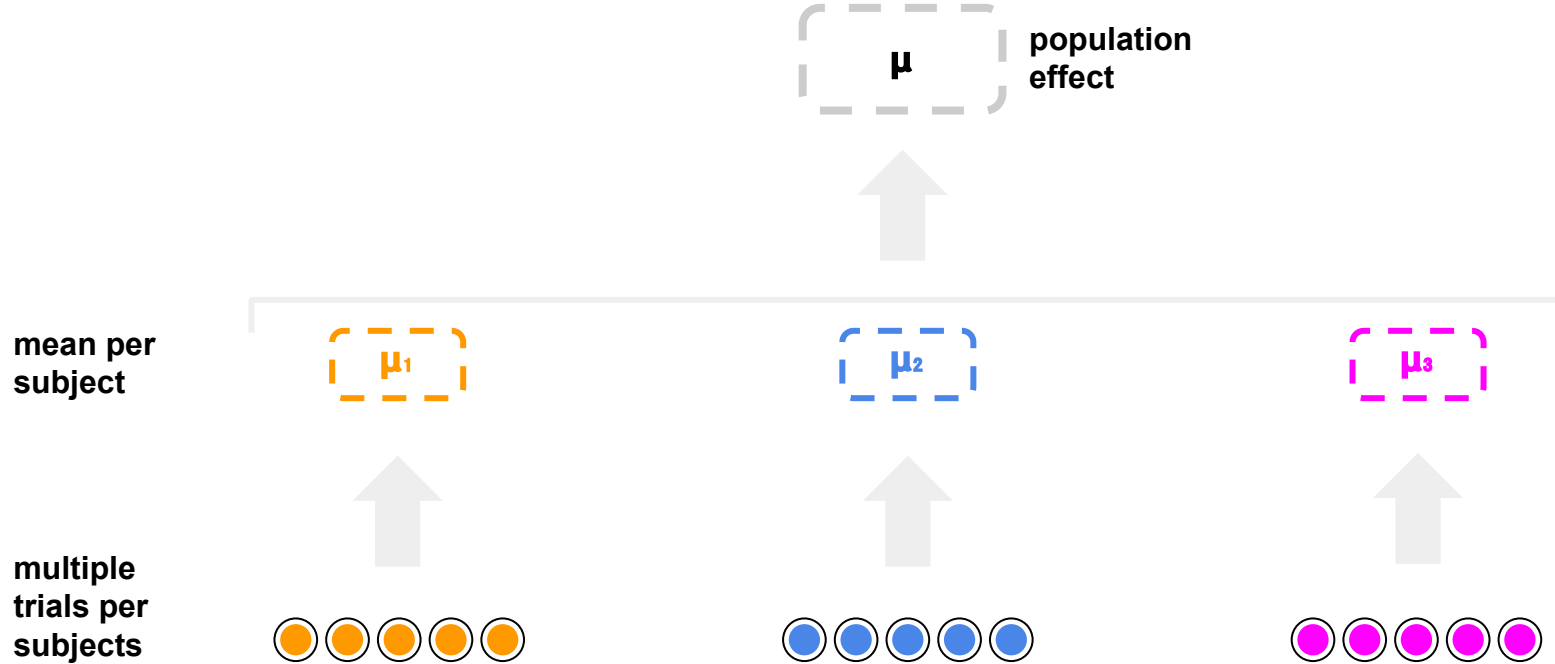
$$y = X\beta + Zu + \epsilon$$

$$u \sim N(0, G)$$

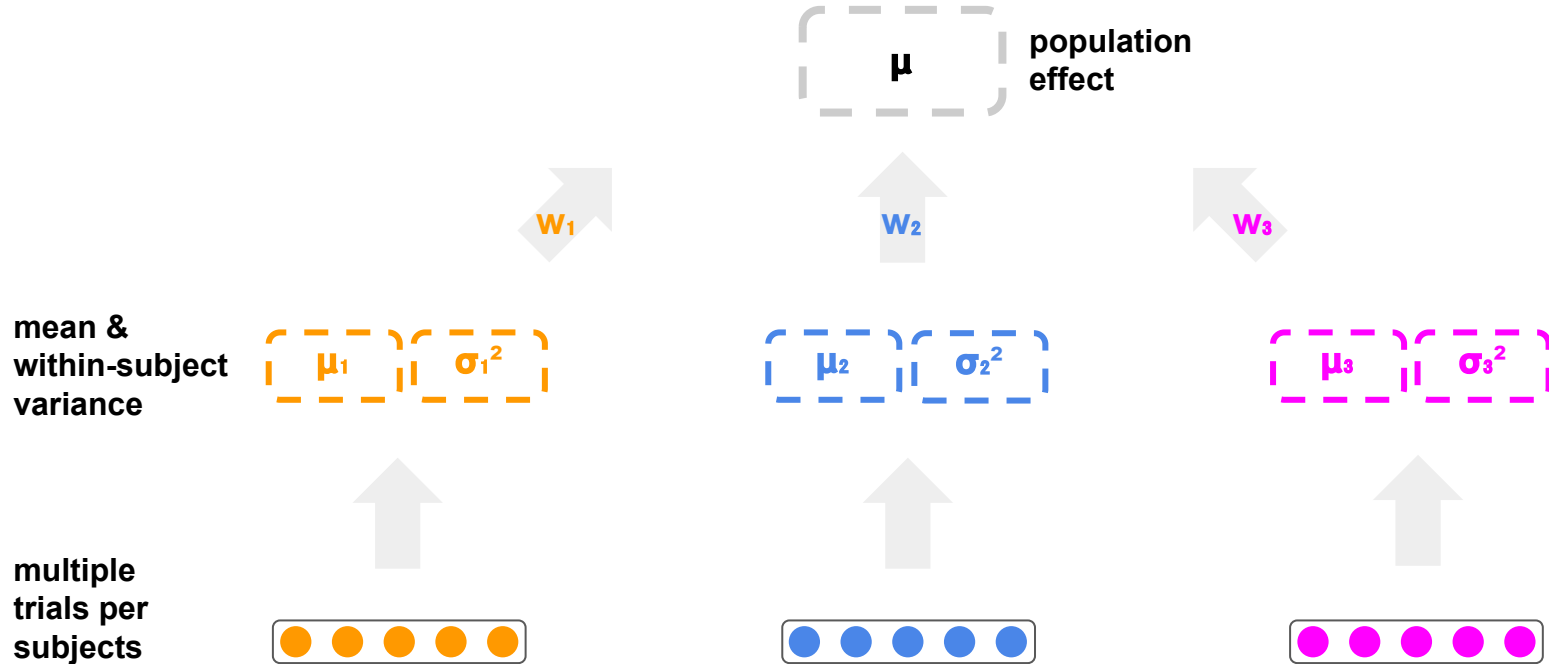
$$\epsilon \sim N(0, R)$$



# Two-way approach

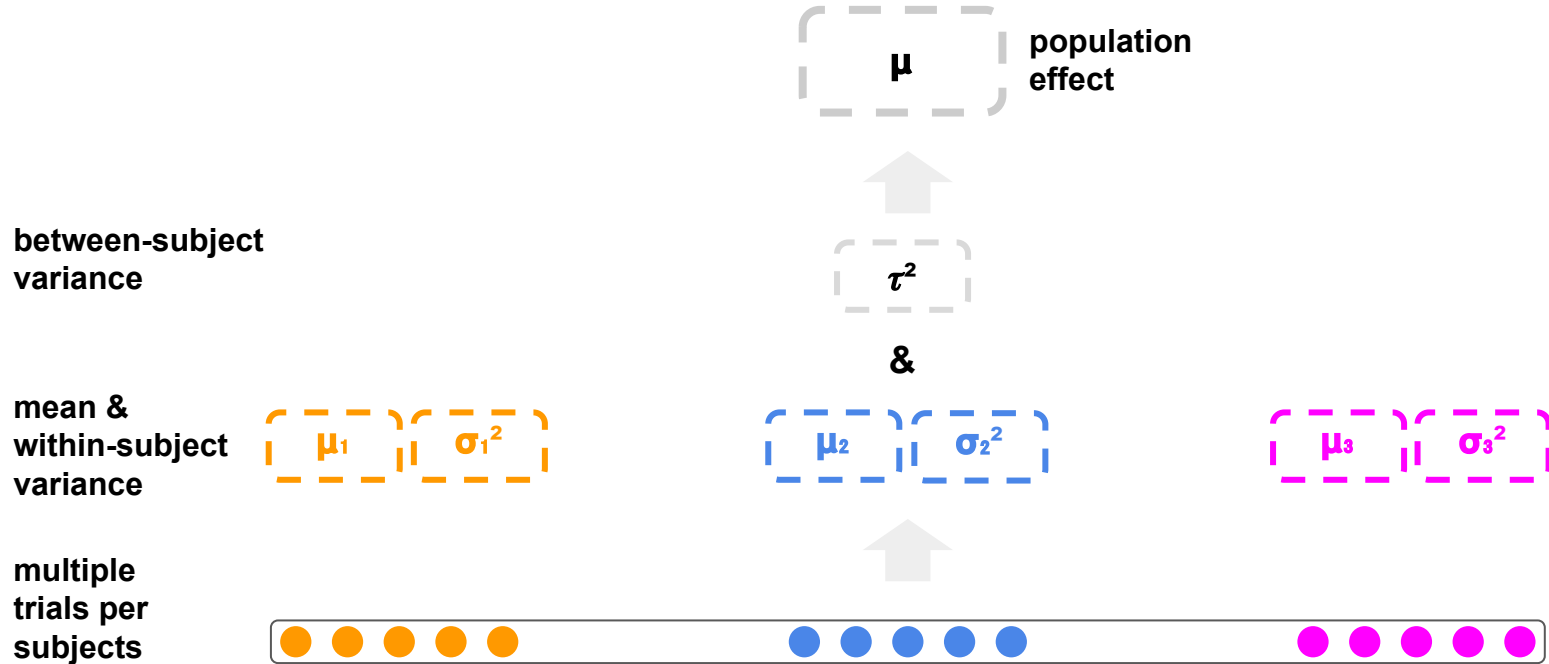


# Meta-model



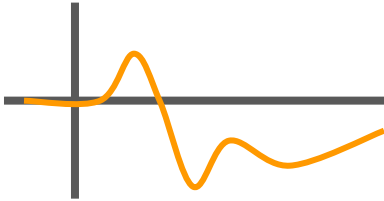


# Mixed-effects model

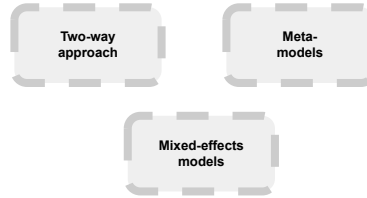


# Goals

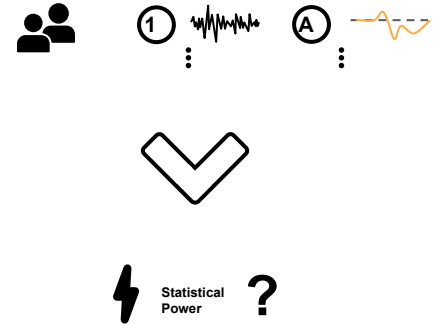
## Simulation toolbox



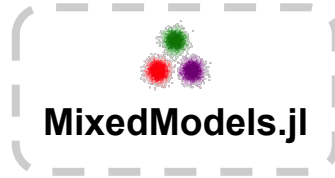
## Implementing of modelling-schemes



## Comparison



# Simulation toolbox



---

**Simulating  
experimental  
conditions**

**1**

**Fit mixed model  
to dummy  
variables**

**2**

**Change  
time-varying  
parameters**

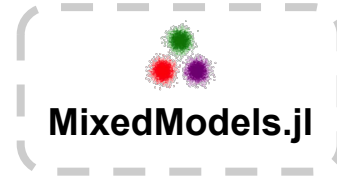
**3**

**Add noise to  
simulated signal**

**4**



# Implementation of modelling-schemes



---

Implementing  
two-way  
approach

1

Implementing  
mixed-effects  
model

2

Implementing  
meta-model

3

Sanity check

4



# Comparison

The Julia logo, consisting of the word "julia" in a lowercase, sans-serif font, with a small cluster of colored dots (blue, green, red, purple) above the 'i'.The text "Plots.jl" in a bold, sans-serif font.

**Simulating data**

**1**

**Analyse data via  
different modelling  
schemes**

**2**

**Plot power  
contour plots**

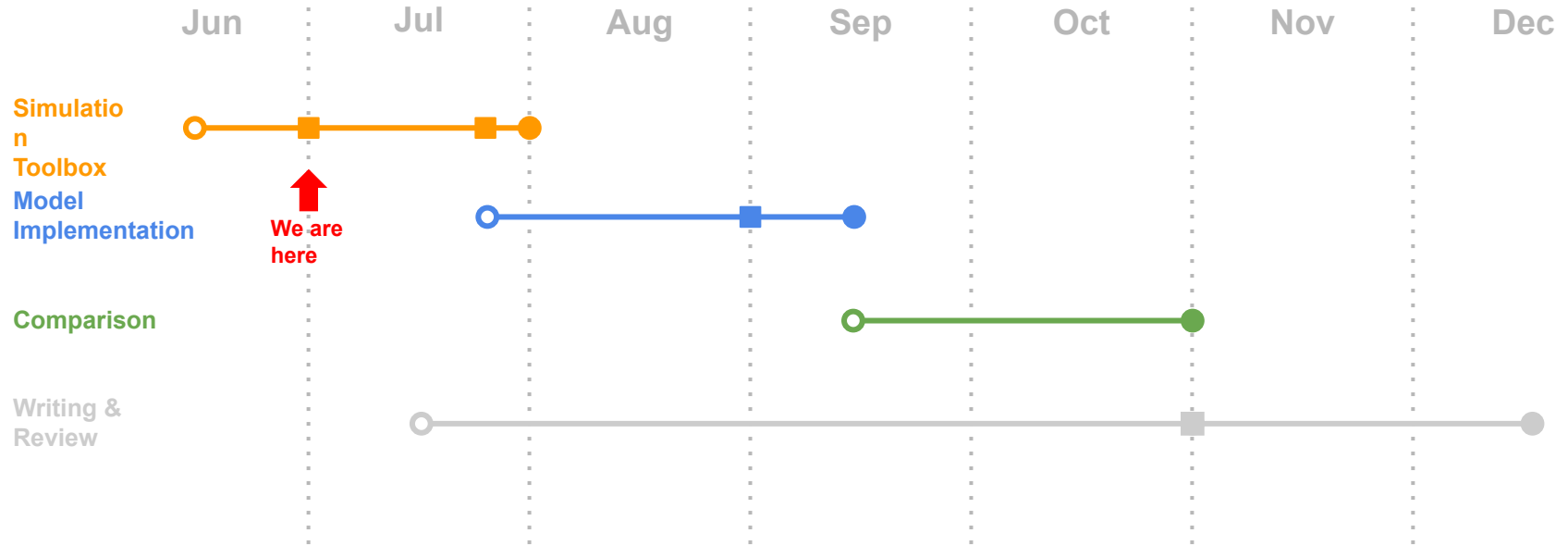
**3**

**(Multiple  
comparison  
correction)**

**4**



# Timeline



# References

Phillip Alday, Douglas Bates, Lisa DeBruine, PhD José Bayoán Santiago Calderón, and Lisa Schwetlick. Repsychling/mixedmodelssim.jl: v0.2.6, October 2021. URL <https://doi.org/10.5281/zenodo.5543934>.

Douglas Bates, Phillip Alday, Dave Kleinschmidt, PhD José Bayoán Santiago Calderón, Likan Zhan, Andreas Noack, Alex Arslan, Milan Bouchet-Valat, Tony Kelman, Antoine Baldassari, Benedikt Ehinger, Daniel Karrasch, Elliot Saba, Jacob Quinn, Michael Hatherly, Morten Piibeleht, Patrick Kofod Mogensen, Simon Babayan, and Yakir Luc Gagnon. Juliastats/mixedmodels.jl: v4.6.2, April 2022. URL <https://doi.org/10.5281/zenodo.6450229>.

R.H. Baayen, D.J. Davidson, and D.M. Bates. Mixed-effects modeling with crossed random effects for subjects and items. *Journal of Memory and Language*, 59(4):390–412, November 2008. ISSN 0749596X. doi: 10.1016/j.jml.2007.12.005. URL <https://linkinghub.elsevier.com/retrieve/pii/S0749596X07001398>.

Gang Chen, Ziad S. Saad, Audrey R. Nath, Michael S. Beauchamp, and Robert W. Cox. FMRI group analysis combining effect estimates and their variances. *NeuroImage*, 60 (1):747–765, March 2012. ISSN 10538119. doi: 10.1016/j.neuroimage.2011.12.060. URL <https://linkinghub.elsevier.com/retrieve/pii/S1053811911014625>.

Gang Chen, Ziad S. Saad, Jennifer C. Britton, Daniel S. Pine, and Robert W. Cox. Linear mixed-effects modeling approach to FMRI group analysis. *NeuroImage*, 73:176–190, June 2013. ISSN 10538119. doi: 10.1016/j.neuroimage.2013.01.047. URL <https://linkinghub.elsevier.com/retrieve/pii/S1053811913000943>.

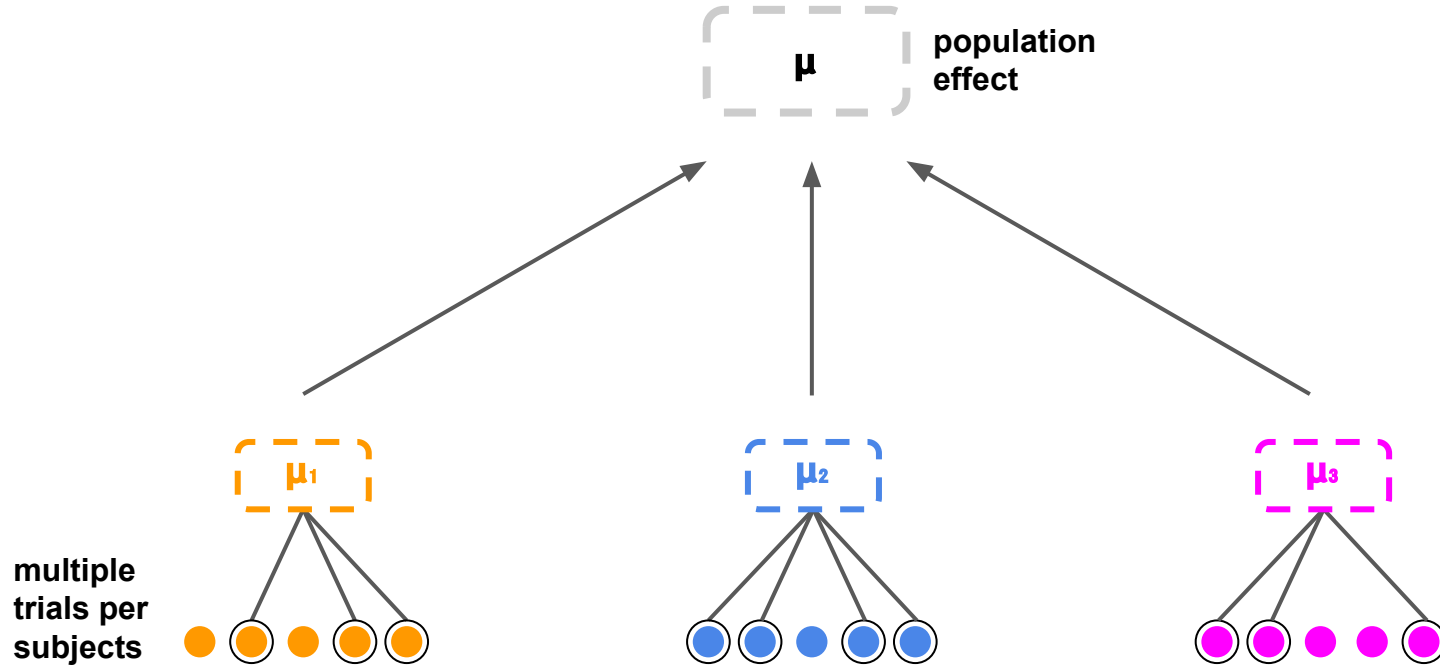
Daniel H. Baker, Greta Vilidaite, Freya A. Lygo, Anika K. Smith, Tessa R. Flack, Andr. D. Gouws, and Timothy J. Andrews. Power contours: Optimising sample size and precision in experimental psychology and human neuroscience. *Psychological Methods*, 26(3):295–314, June 2021. ISSN 1939-1463, 1082-989X. Mixed-effects models for EEG analysis 3 doi: 10.1037/met0000337. URL <http://doi.apa.org/getdoi.cfm?doi=10.1037/met0000337>.



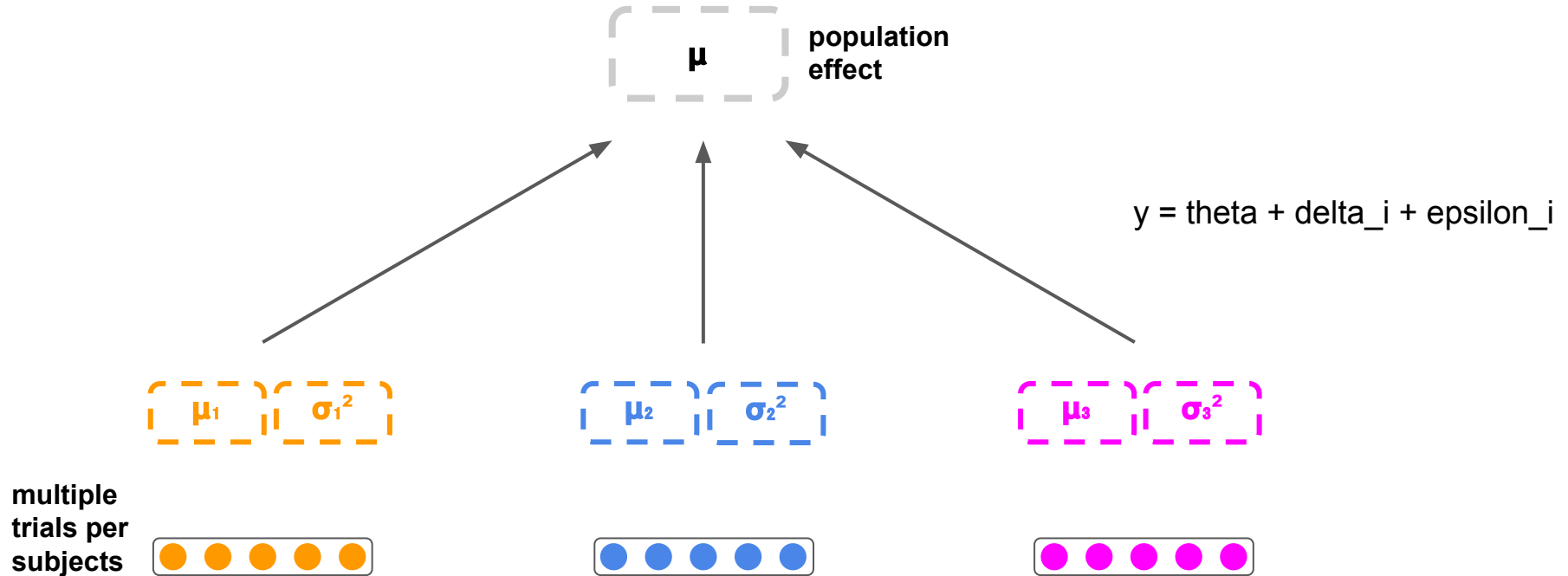
# Discussion



# Two-way approach



# Meta-model



# Mixed-effects model

$\mu$  population effect

$$y = X*b + Z*u + \text{epsilon}_{ij}$$

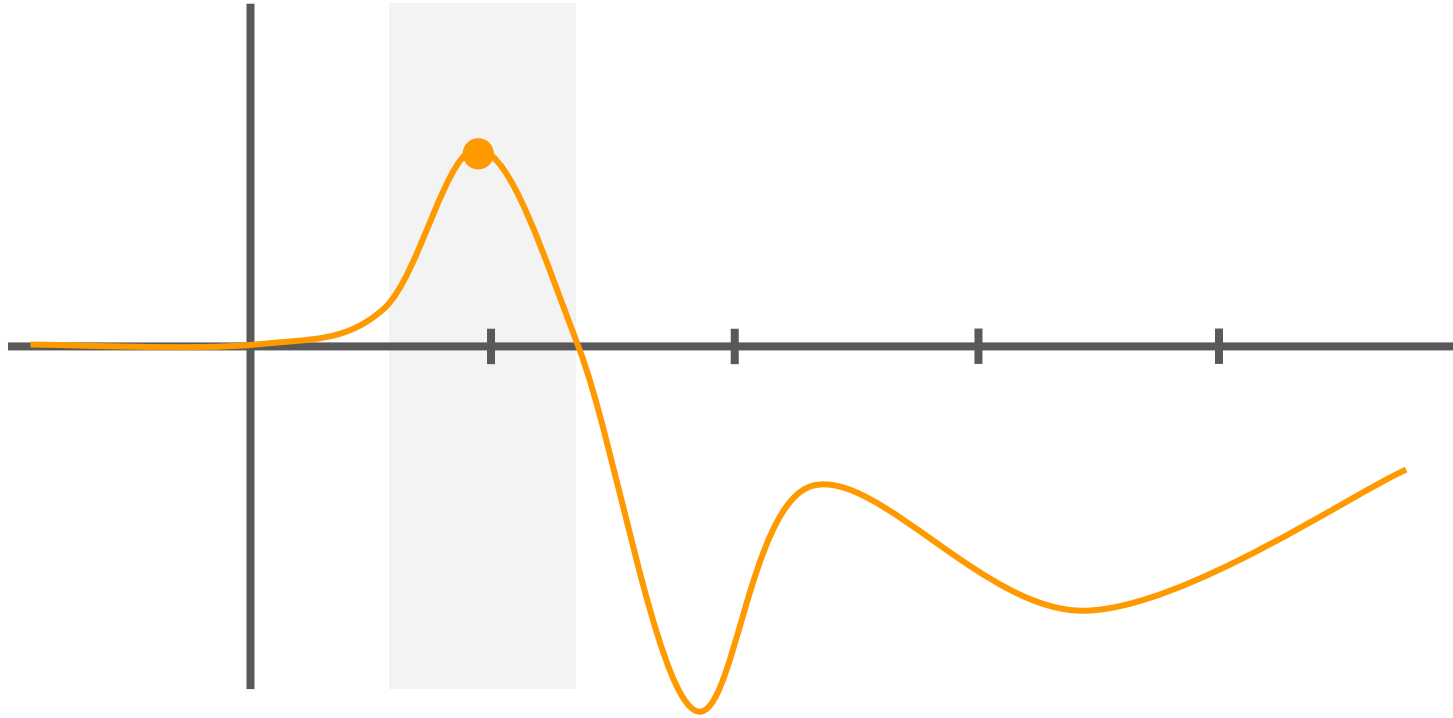
$\mu_1$

$\mu_2$

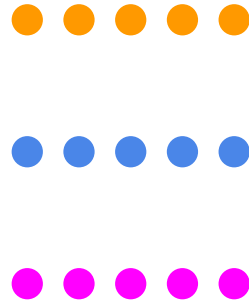
$\mu_3$



# 1 Subject, 1 Trial, 1 Measure



# Multiple subjects, multiple trials



**Repeated measures !**



# Data



# Data

