

# Final Talk

## Simulation of EEG Activity based on Sequential Sampling Models

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2. Motivation & related work
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# Introduction



## What is this thesis about?

- Human **decision-making**
- **Sequential Sampling Models (SSMs)**
- Simulating **EEG activity**



## Why is this important?

- Insights **interpreting** decision-related signals
- Open **debate in research**
- **Simulated EEG** data is **useful** for multiple tasks

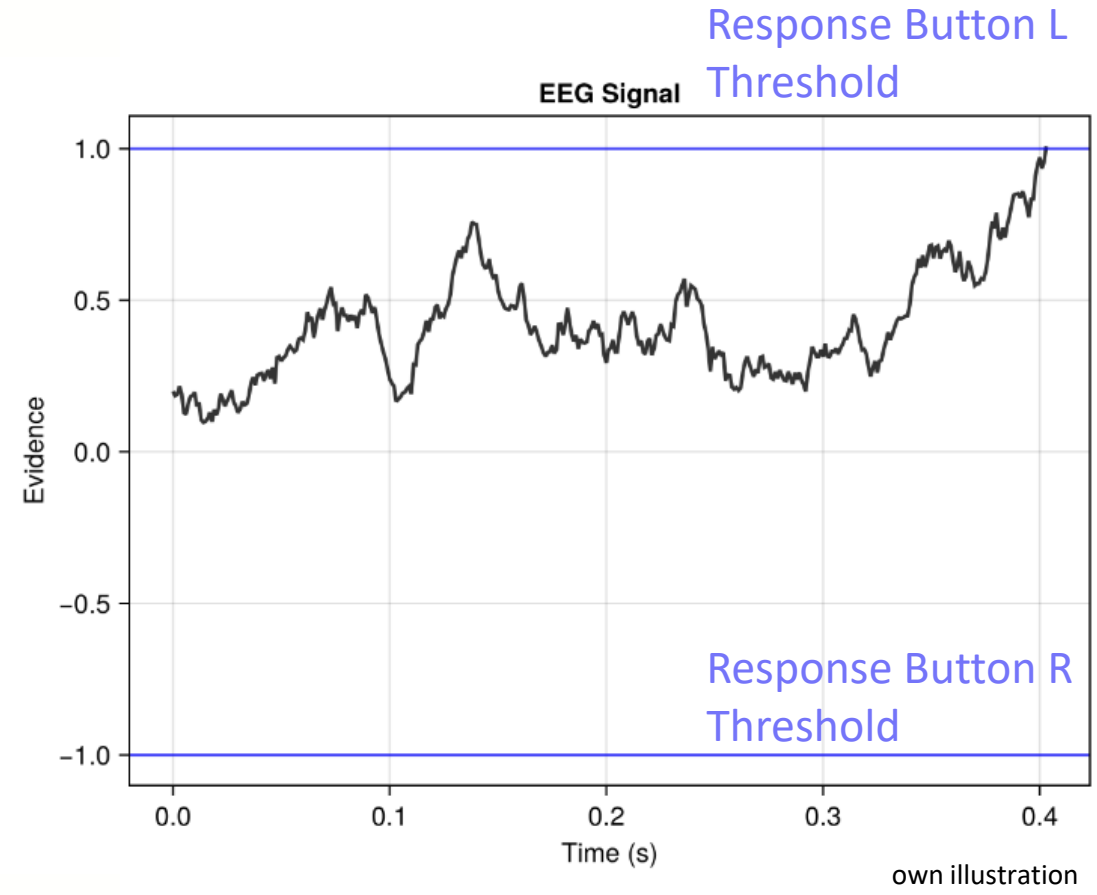
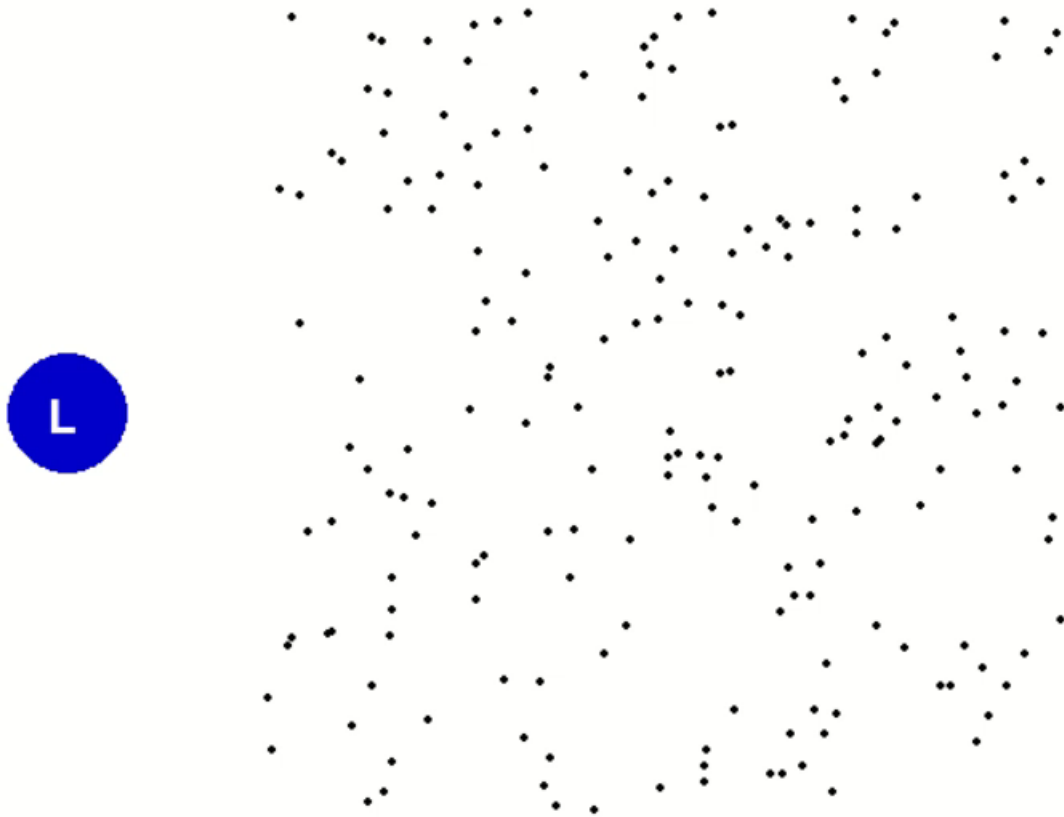


## Main Research Goal:

- Extension **development**
- Integration into **UnfoldSim.jl**
- **Investigate** how SSMs can replicate **decision-making**

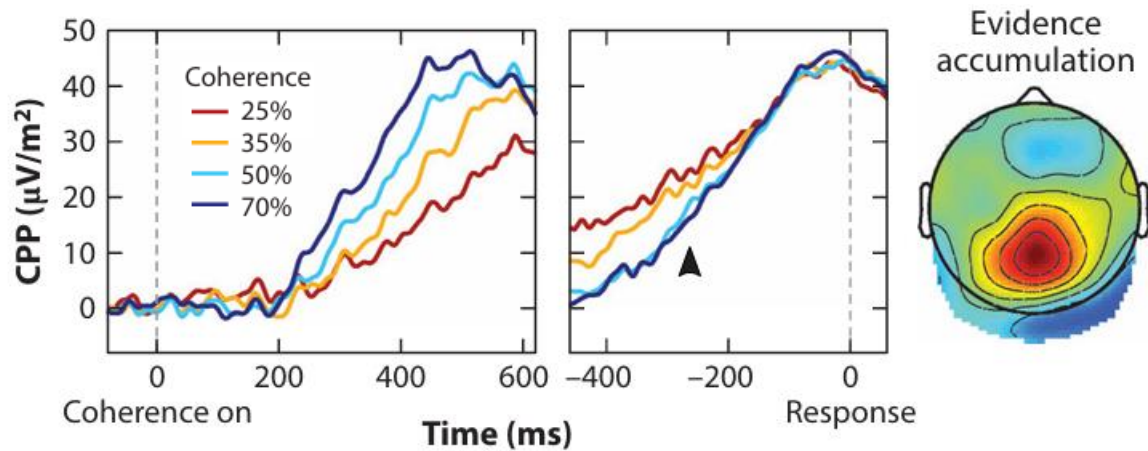
# Motivation & related work

## Changing coherence moving dots Experiment

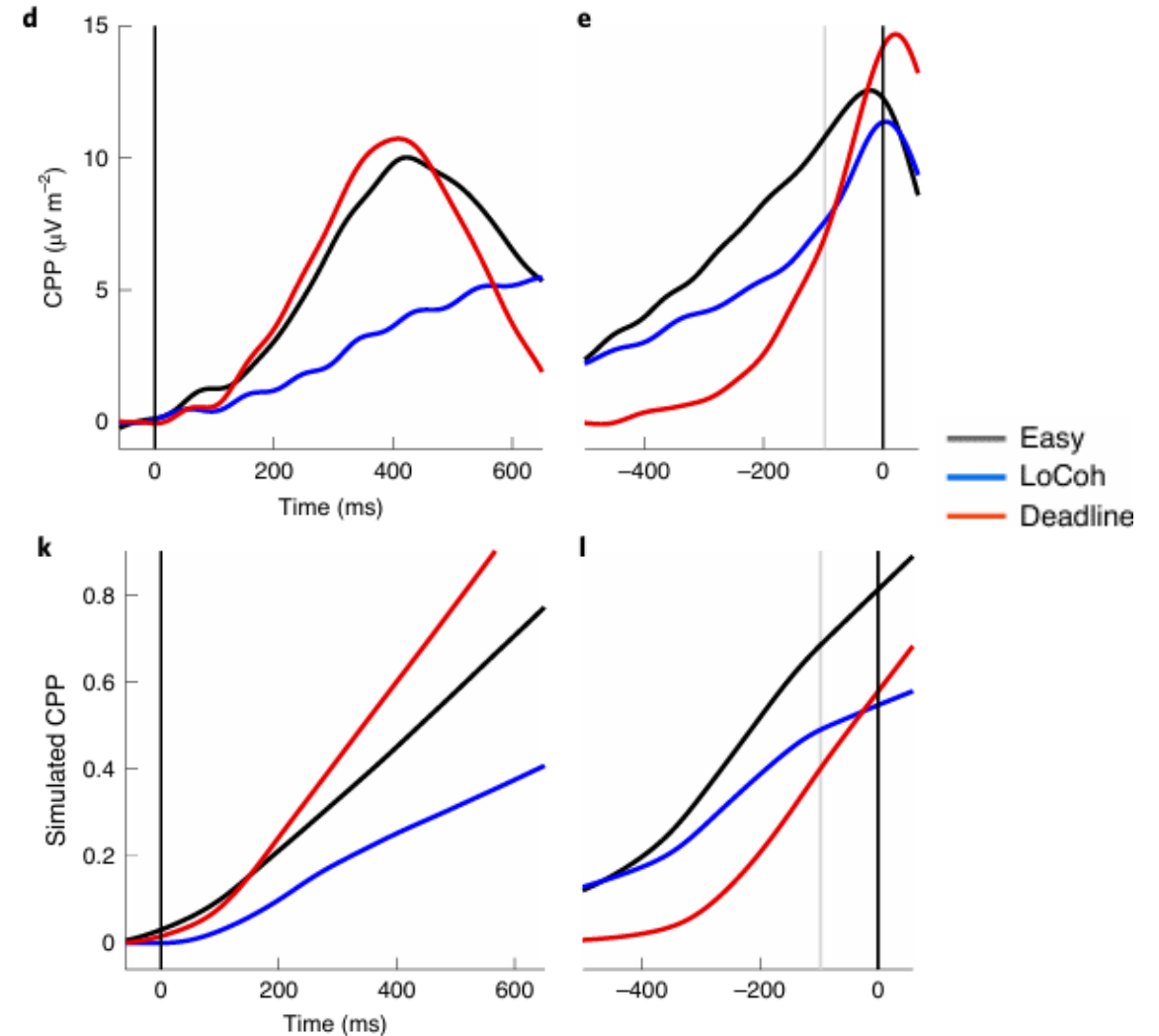


# Motivation & related work

Evidence-dependent structural dynamics of the component centroparietal positivity (CPP) in the brain

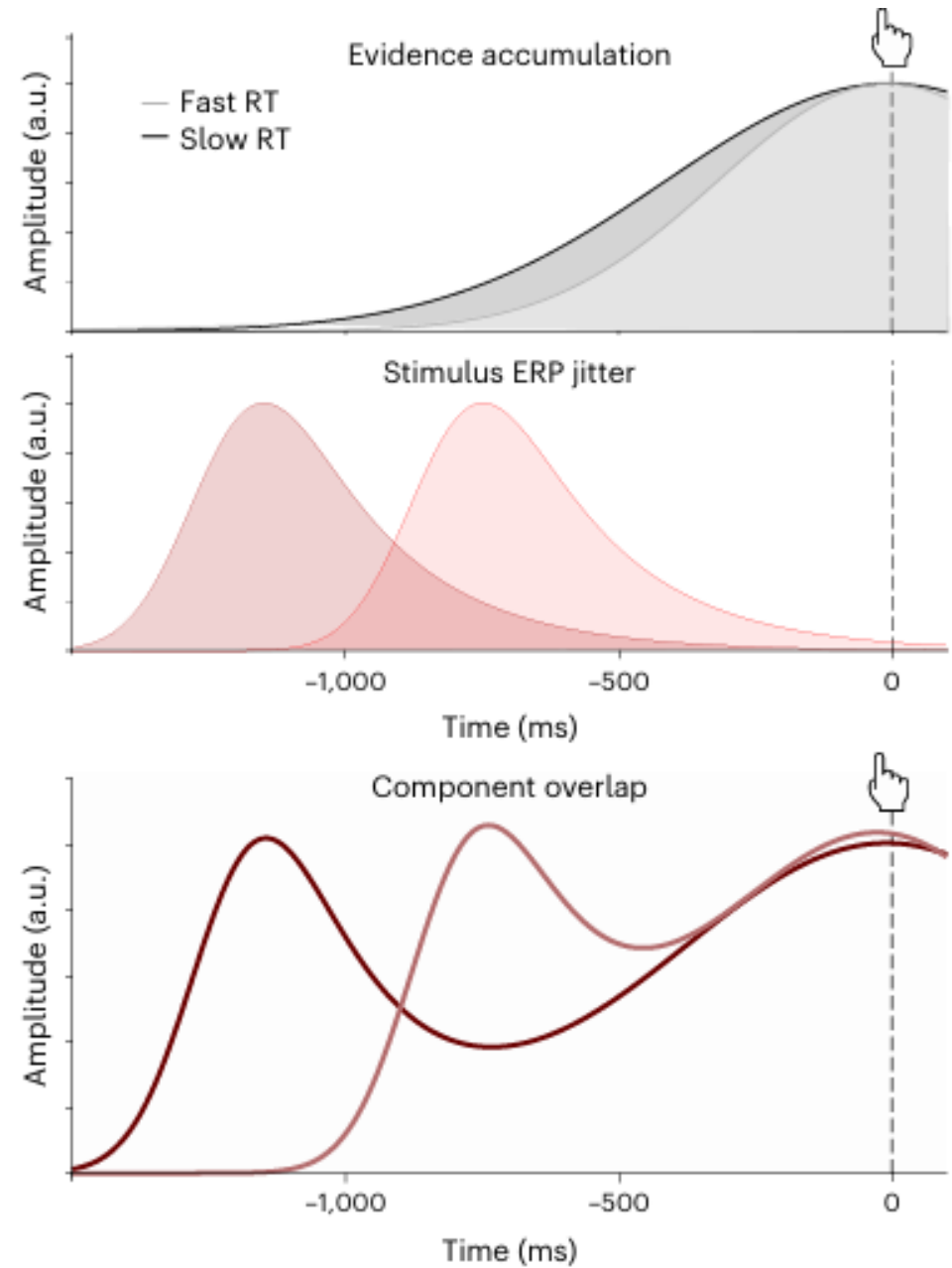


Kelly et al. Neurophysiology of Human Perceptual Decision-Making 2021 [1]

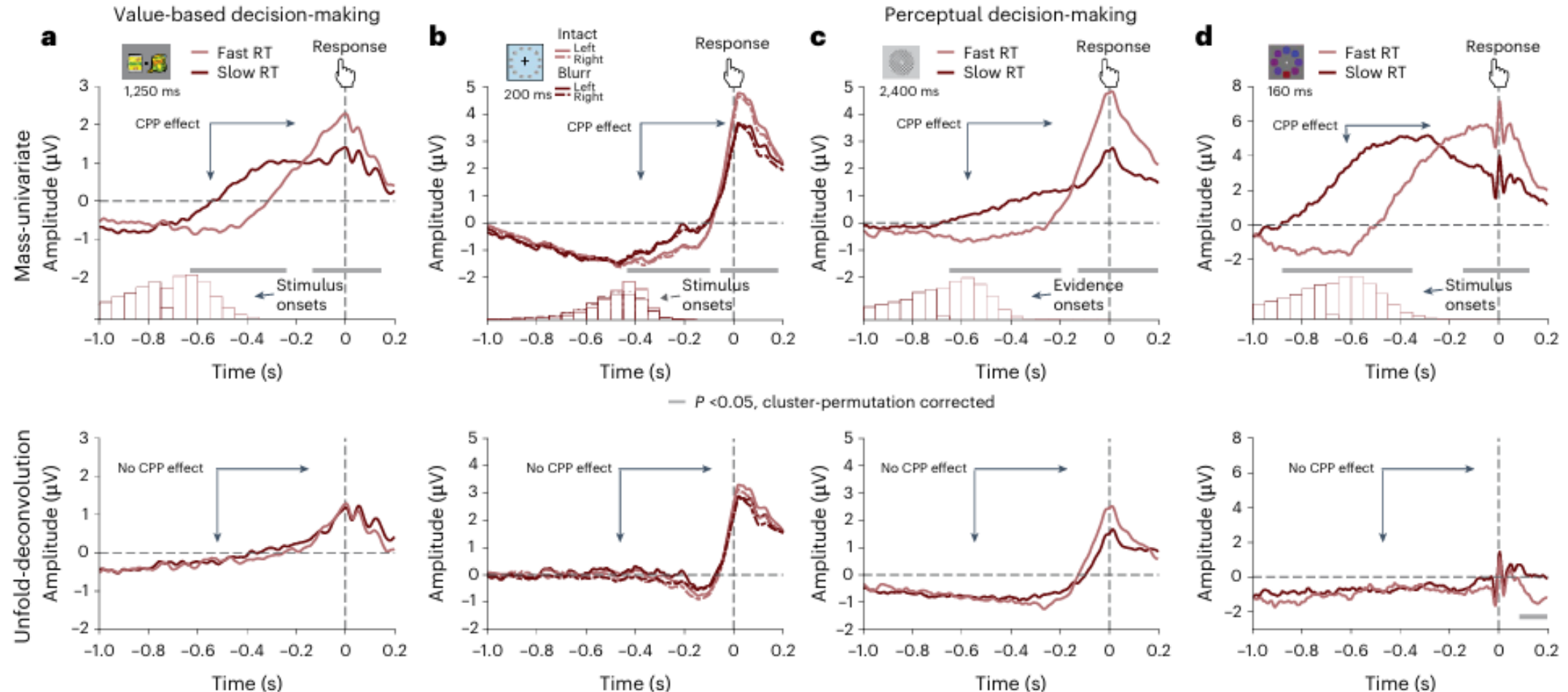


Kelly et al. Neurocomputational mechanisms of prior-informed perceptual decision-making in humans 2021 [2]

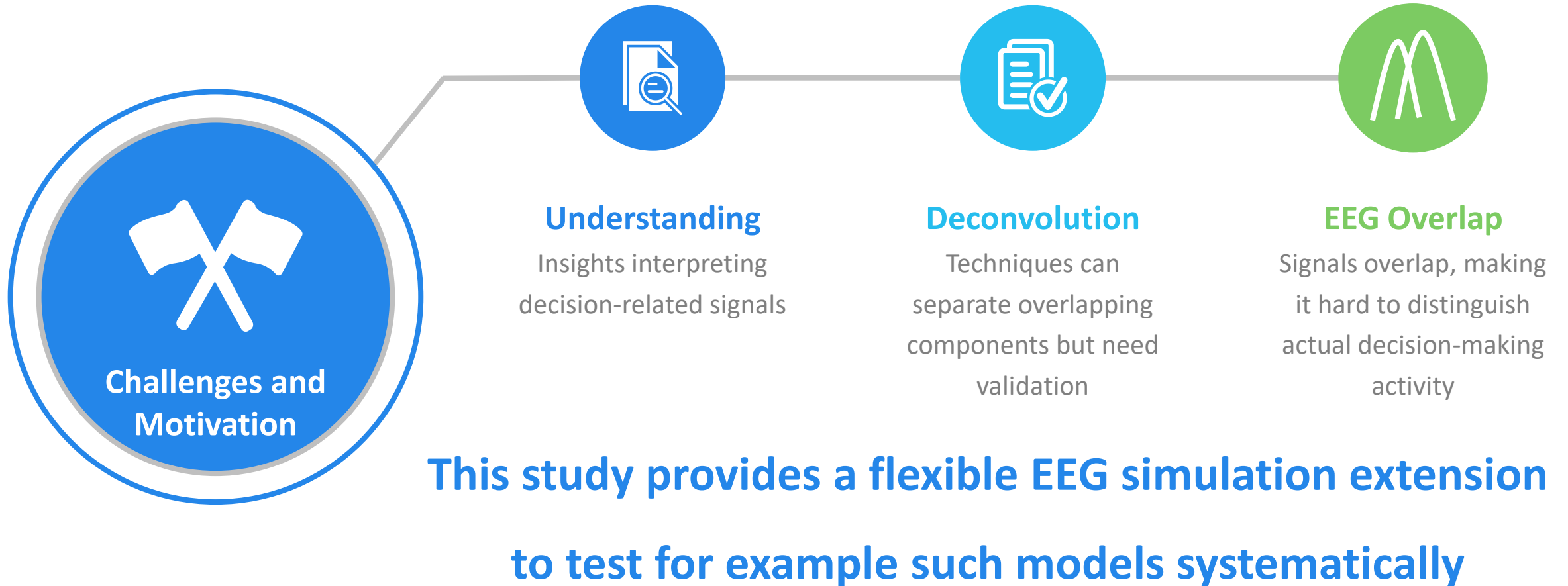
# Motivation & related work



# Motivation & related work



# Motivation & related work

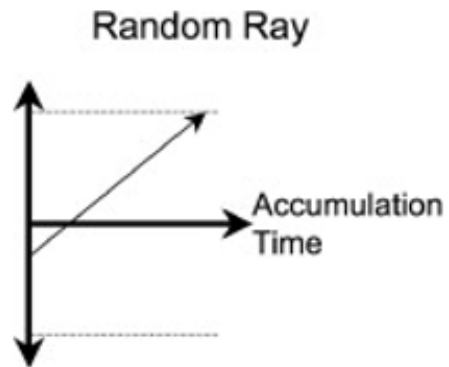




# Approach

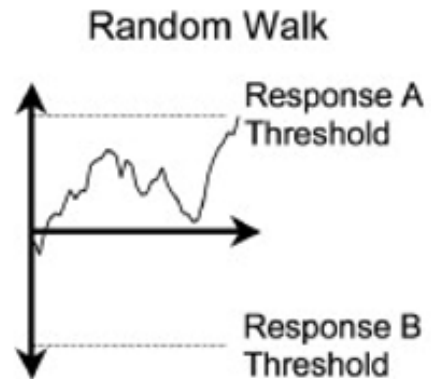
## 1. Theoretical Description of Sequential Sampling Models

### linear ballistic accumulator (LBA)

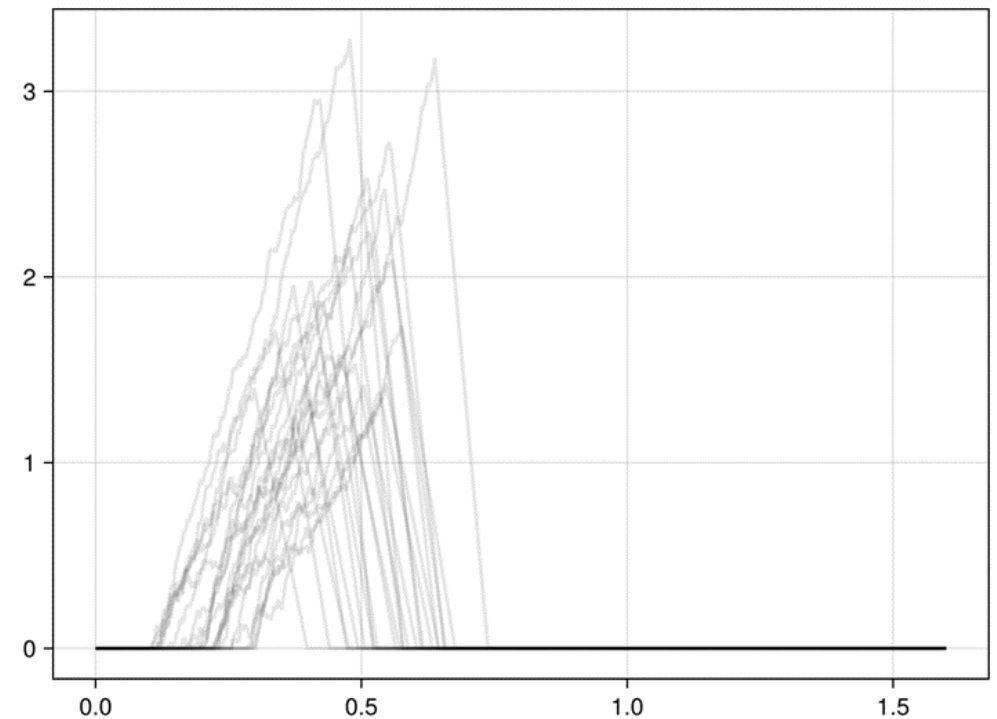


Brown et al. The simplest complete model of choice response time: Linear ballistic accumulation 2008 [4]

### drift-diffusion model (DDM)



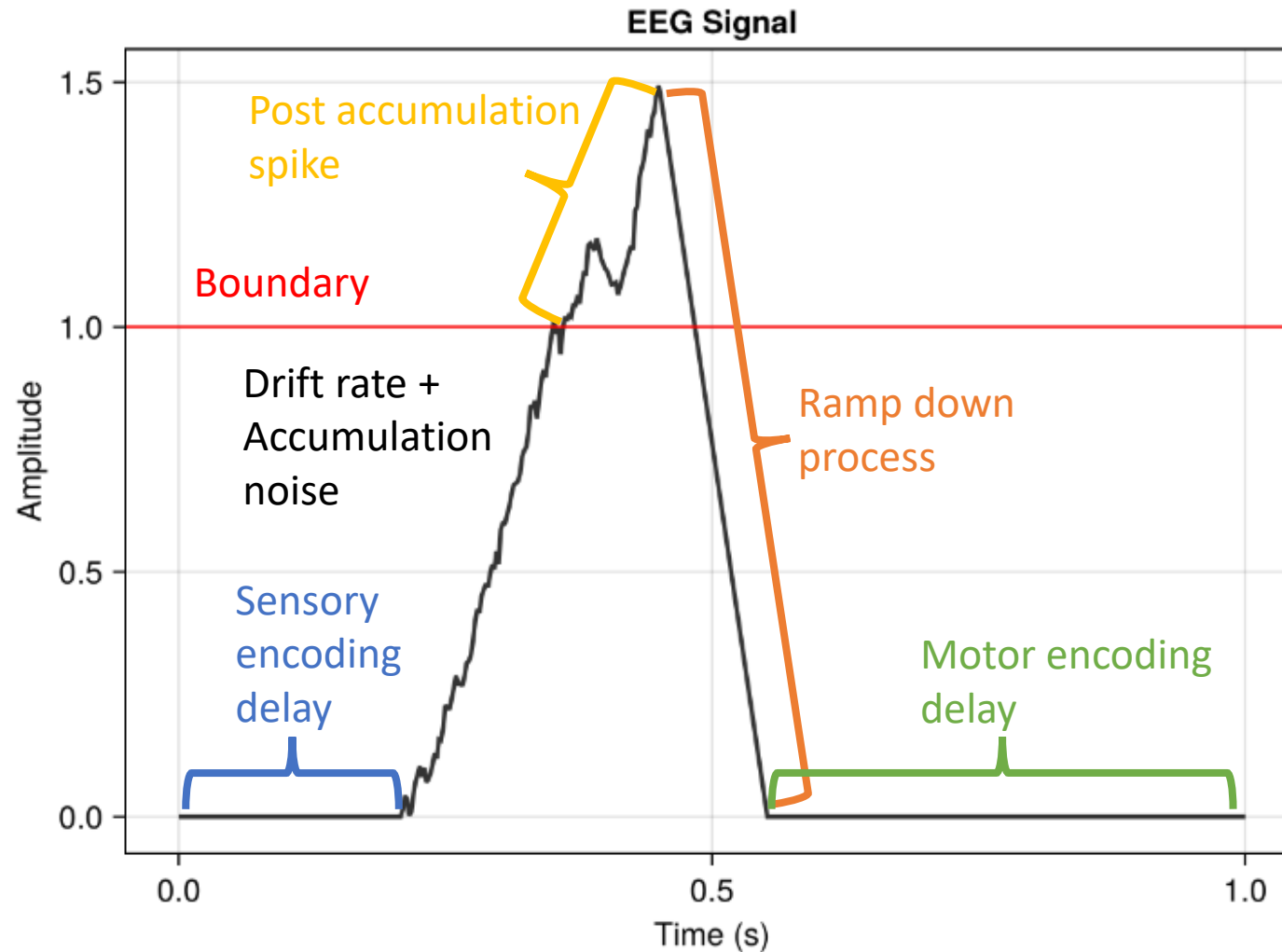
### Kelly et. al Model of neural activity



Own illustration based on Kelly et al. Code converted to Julia

# Approach

## Kelly et. al Model of neural activity



Own illustration based on Kelly et al. Code converted to Julia

# Approach

## 2. Reimplementation of the Kelly et. al Model



## 3. Integration into UnfoldSim



2.1 Understanding the code

3.1 Introduction to UnfoldSim.jl usage

2.2 Structured and methodical reimplementation

3.2 Adapting implementation to package paradigms

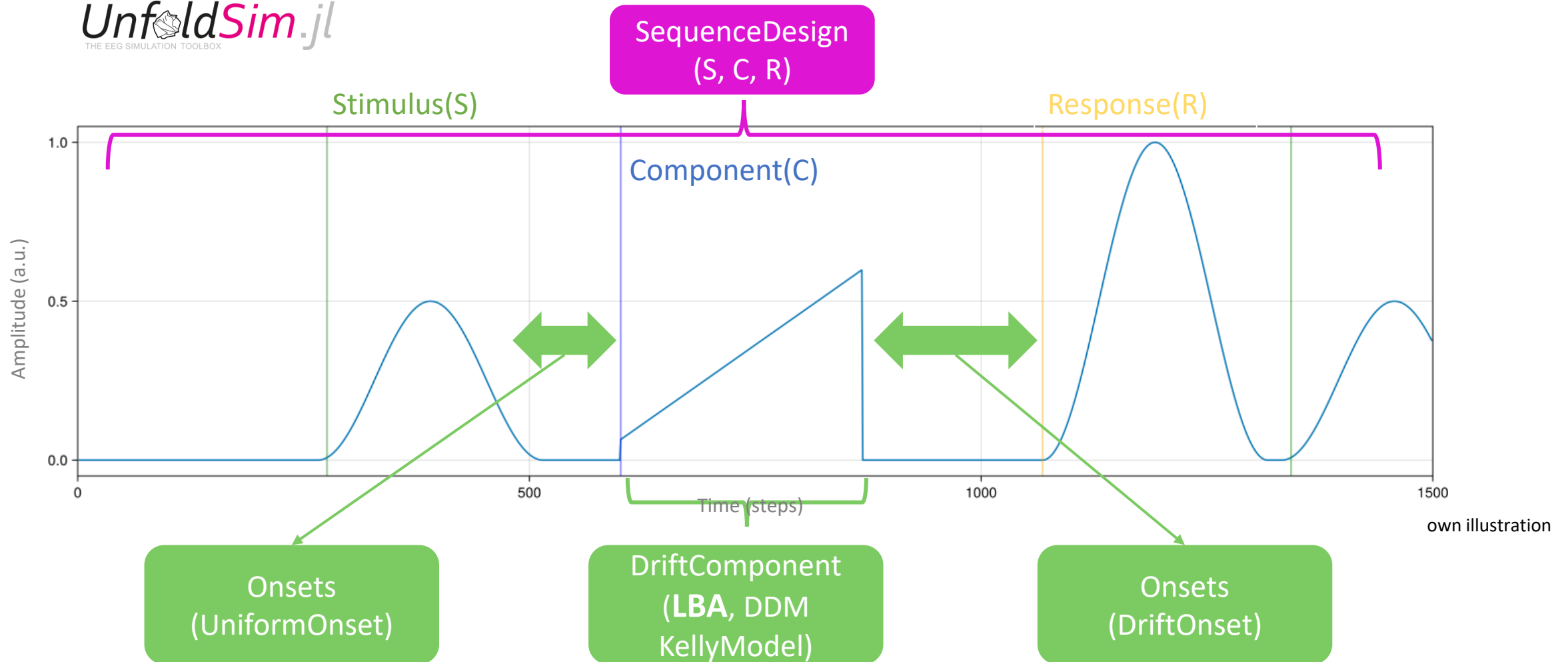
2.3  
Parameters  
Docu.

```
u1 = Z .+ (U.+randn(rng).*Su) .* timevec;  
u1 = u1 .+ (rand(rng)-.5)*Sz;  
u2 = Z .+ (U.+randn(rng).*Su) .* timevec;  
u2 = u2 .+ (rand(rng)-.5)*Sz;
```

3.3 Splitting functionalities and documenting code

# Implementation & Integration – Complete picture

*UnfoldSim.jl*  
THE EEG SIMULATION TOOLBOX



# Implementation & Integration



## Design

SingleSubjectDesign

SequenceDesign

RepeatDesign

## Component

## Model simulation

## Onset

# Implementation & Integration



## Design

SingleSubjectDesign

SequenceDesign

RepeatDesign

## Component

DriftComponent

DriftComponent  
functions

## Model simulation

## Onset

# Implementation & Integration



## Design

SingleSubjectDesign

SequenceDesign

RepeatDesign

## Component

DriftComponent

DriftComponent  
functions

## Model simulation

KellyModel

SSM\_Simulation  
functions

## Onset

# Implementation & Integration



## Design

SingleSubjectDesign

SequenceDesign

RepeatDesign

## Component

DriftComponent

DriftComponent  
functions

## Model simulation

KellyModel

SSM\_Simulation  
functions

## Onset

SequenceOnset

DriftOnset

SequenceOnset/  
DriftOnset  
functions



# Implementation & Integration

## Test

```
@testset "sequentialSamplingModelSimulation" begin
    fs = 500
    Δt = 1 / fs # time step
    tEnd = 1.0 # trial Duration
    time_vec = 0:Δt:tEnd # time base
    max_length = tEnd / Δt
    rng = StableRNG(1)
    @testset "KellyModel" begin
        assert_event_onset = 0.663
        assert_drift_rate = "drift_rate"
        km = KellyModel(event_onset = assert_event_onset, drift_rate = assert_drift_rate)

        @test km.event_onset == assert_event_onset
        @test km.drift_rate == assert_drift_rate
    end

    @testset "KellyModel_simulate_cpp" begin
        boundary = 1.0
        result_rt, result_trace = UnfoldSim.KellyModel_simulate_cpp(
            rng,
            KellyModel(boundary = boundary),
            time_vec,
            Δt,
        )
        @test size(result_rt) == ()
        @test size(result_trace) == (501,)
        @test isapprox(result_rt, 399.6903067274333, atol = 1e-8)
        @test any(result_trace .== 0)
        @test any(result_trace .>= boundary)

        result_sim_rt, result_sim_trace = UnfoldSim.SSM_Simulate(rng, KellyModel(), fs, max_length)
        @test result_rt == result_sim_rt
        @test result_trace == result_sim_trace
    end
end
```

## Documentation

```
SSM_Simulate(rng, model::KellyModel, sfreq, max_length)

Generate response time and evidence Vector of max_length by using the Kelly Model for the simulation.

# Arguments
- `rng::StableRNG`: Random seed to ensure the same traces are created for reconstruction.
- `model::KellyModel`: SequentialSamplingModel to simulate the evidence and response time.
- `sfreq::Real`: sample frequency used to simulate the signal.
- `max_length::Int`: maximum length of the simulated signal.

# Returns
- `Float64`: Simulated response time for the trial.
- `Vector{Float64}`: evidence values over time. The output dimension is `c.max_length`.

# Examples
```julia-repl
julia> model = KellyModel()

julia> SSM_Simulate(StableRNG(1), model, 500, 500)
Float64, Vector{Float64}:
(96.65745162948949, [0.0 0.0 ... 0.0 0.0])
...

function SSM_Simulate(rng, model::KellyModel, sfreq, max_length)
```

The screenshot shows the UnfoldSim.jl documentation page for the topic "Simulate an Evidence Accumulation Overlap and Deconvolution". The page includes a sidebar with navigation links like Home, Installing Julia & UnfoldSim.jl, Tutorials, Quickstart, and Reference. The main content area has a "Setup" section with a "Click to expand" button and a "Design" section with a "Let's generate a single subject design" button. Below the design button is a code block showing the creation of a SingleSubjectDesign object with specific conditions and event\_order\_function.

The screenshot shows the UnfoldSim.jl documentation page for the topic "HowTo Simulate an Evidence Accumulation EEG". The page includes a sidebar with navigation links like Home, Installing Julia & UnfoldSim.jl, Tutorials, Quickstart, and Reference. The main content area has a "Setup" section with a "Click to expand" button and a "Design" section with a "Let's generate a single subject design" button. Below the design button is a code block showing the creation of a SingleSubjectDesign object with specific conditions and event\_order\_function. The page also includes a "Now we convert the SingleSubjectDesign to a SequenceDesign with a Sequence of S: stimulus, C: component, R: response" section.

# Results

## 1. Simulation Space

1. Setup for all model simulations
2. LBA
3. DDM
4. KellyModel

## 2. Use Case

1. Setup for the use case
2. Results of a basic overlap deconvolution
3. Results of the simulated data

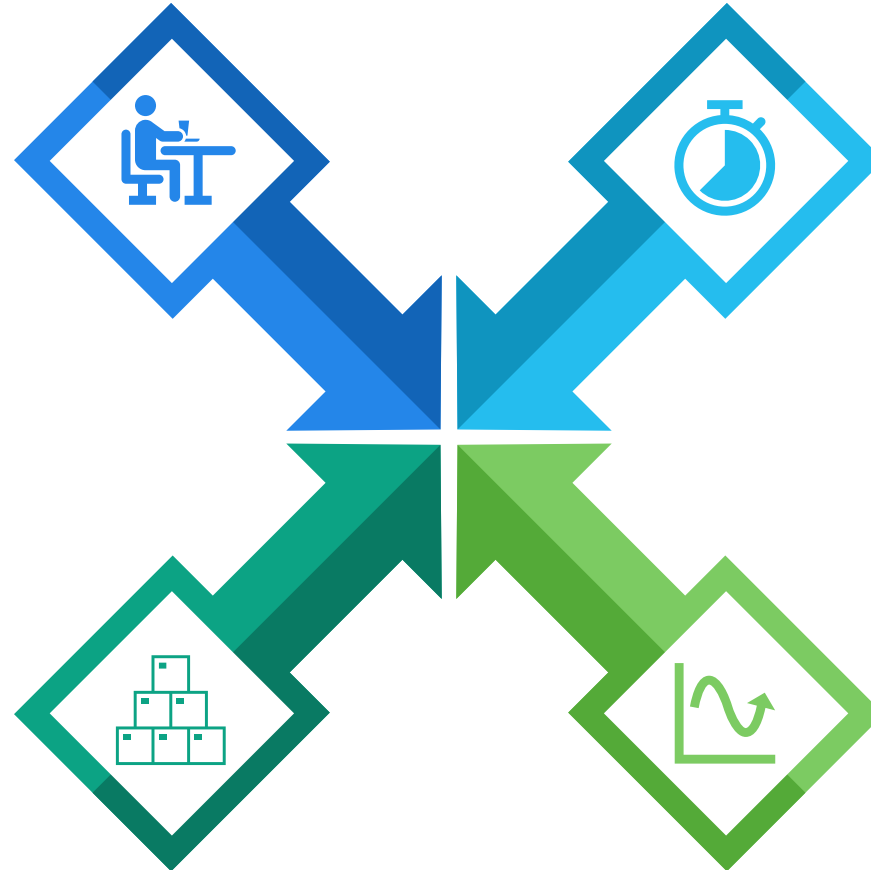
# Results – Simulation Space - Setup

## Design

```
design_single = SingleSubjectDesign(  
    conditions = Dict(  
        :drift_rate => [0.45, 0.8],  
        :condition => [1])  
)  
design_seq = SequenceDesign(design_single, "SCR")  
design_rep = RepeatDesign(design_seq, 100)
```

## Components

```
components = Dict(  
    'S' => [stimulus],  
    'C' => [drift_component],  
    'R' => [response]  
)
```



## Onsets

```
fs = 500  
component_length = 1.0  
seq_onset = SequenceOnset(  
    Dict('S'=> UniformOnset(  
        width=0,  
        offset=(comp_length*fs*1.2)),  
        'C'=> DriftOnset(),  
        'R'=> UniformOnset(  
            width=0,  
            offset=(comp_length*fs*1.5)))  
)
```

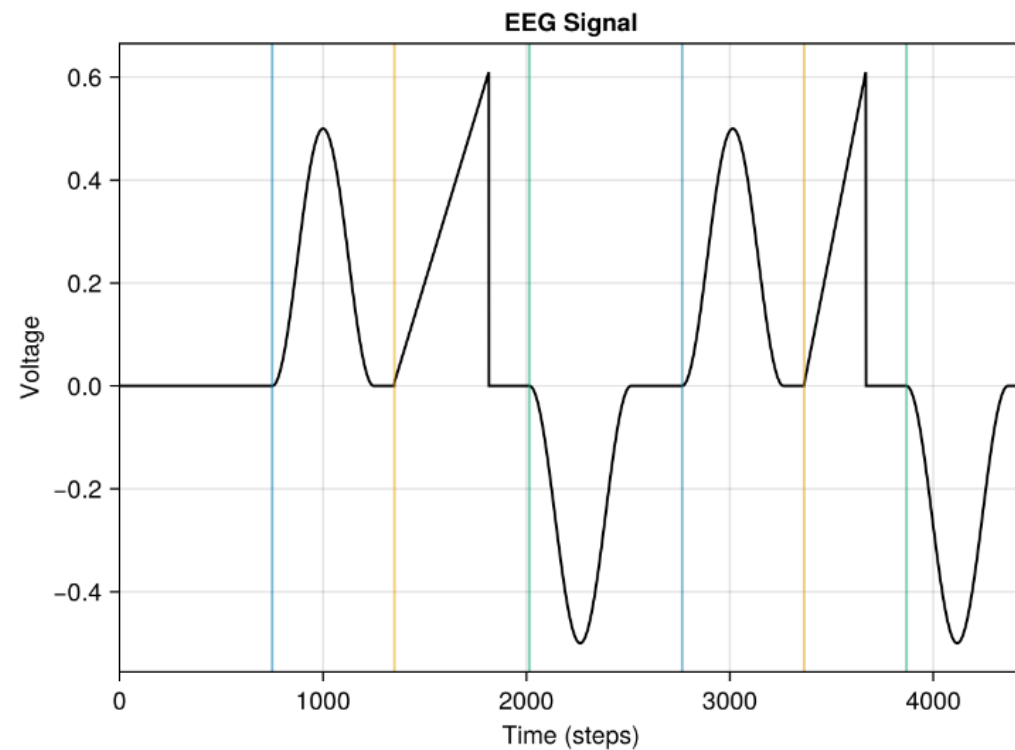
## Simulation

```
data, events = UnfoldSim.simulate(  
    StableRNG(12),  
    design_rep,  
    components,  
    seq_onset,  
    NoNoise()  
)
```

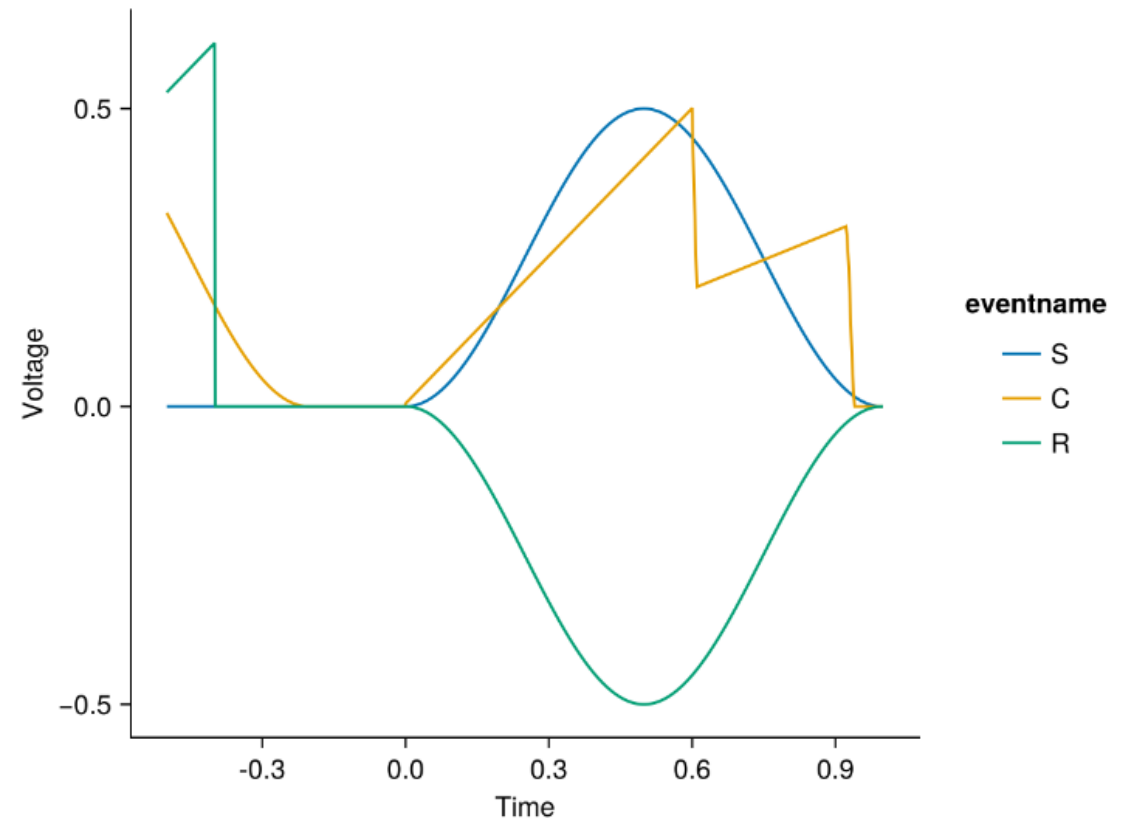
# Results – Simulation Space - LBA

Legend

Stimulus(S) Component(C) Response(R)



own illustration

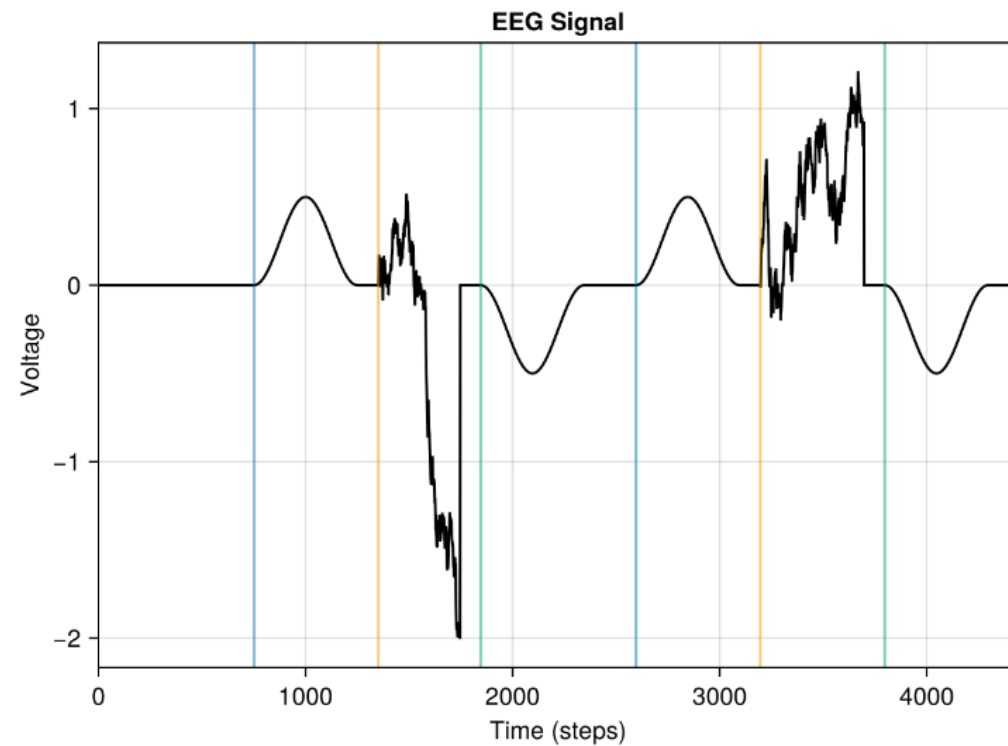


own illustration

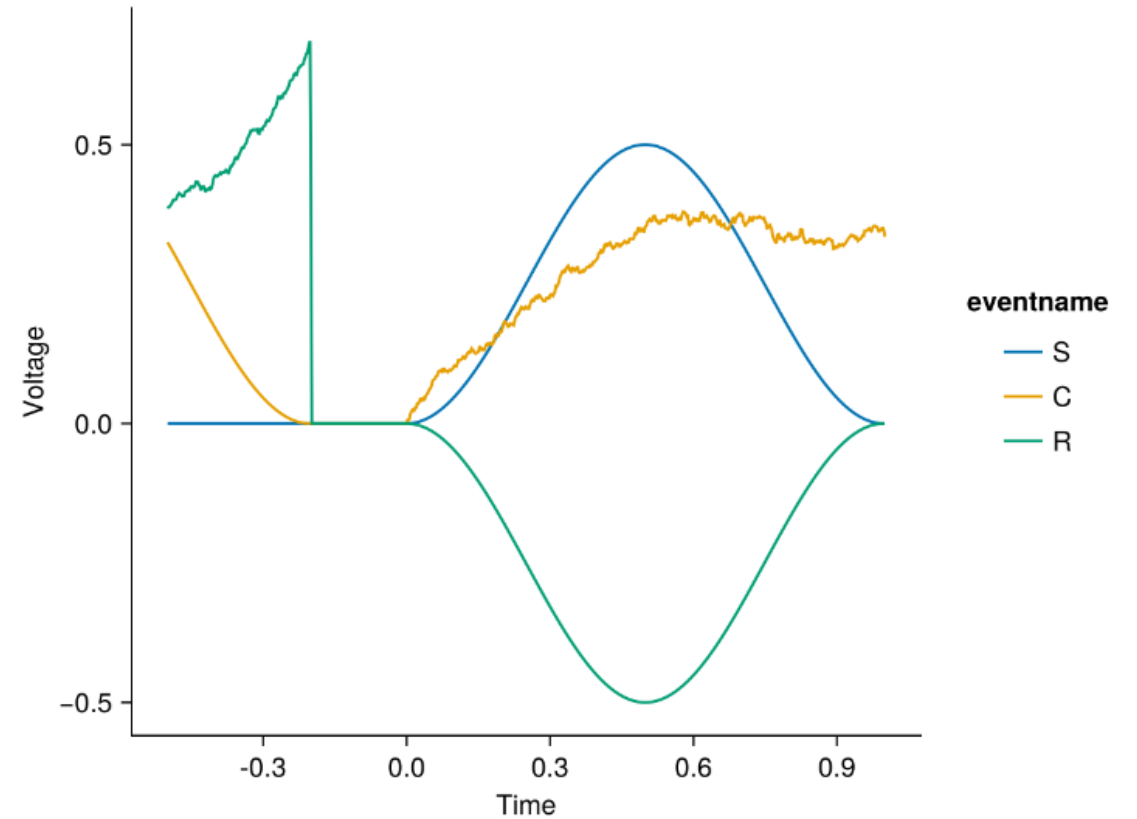
# Results – Simulation Space - DDM

Legend

Stimulus(S) Component(C) Response(R)



own illustration

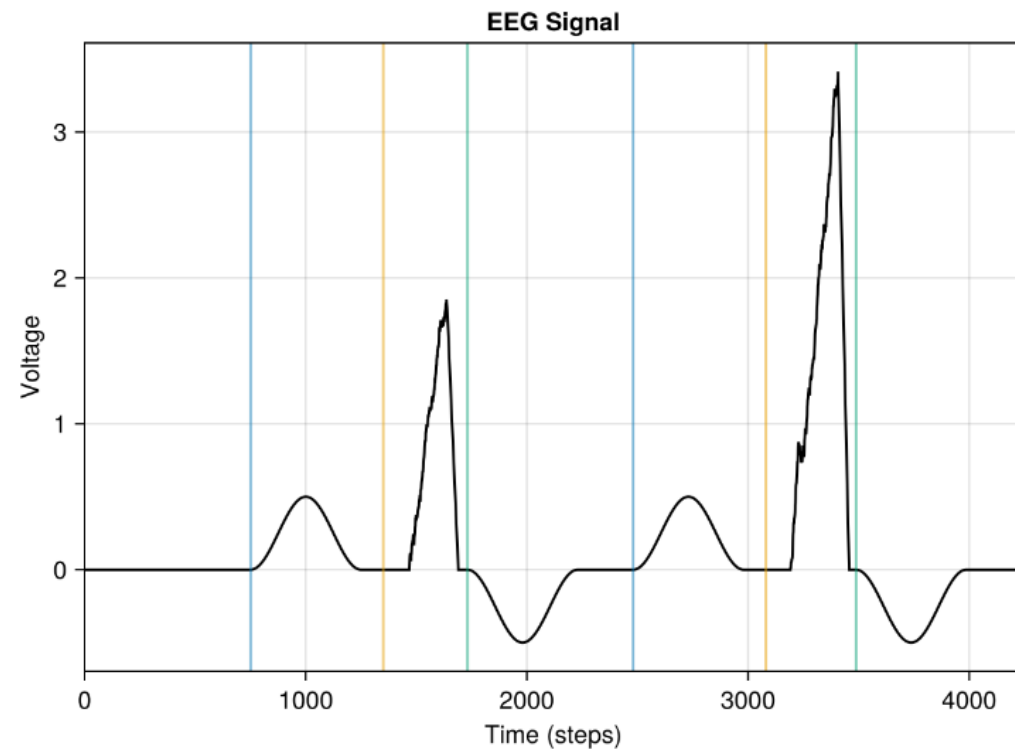


own illustration

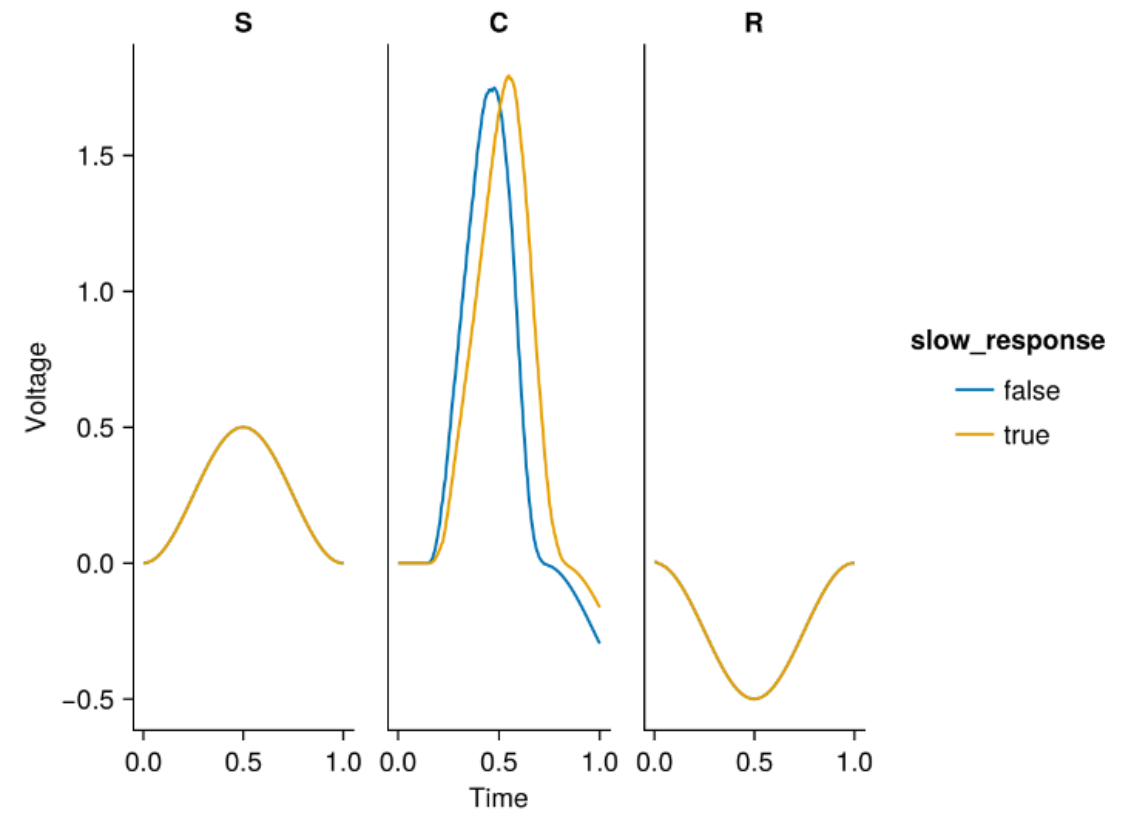
# Results – Simulation Space - KellyModel

Legend

Stimulus(S) Component(C) Response(R)

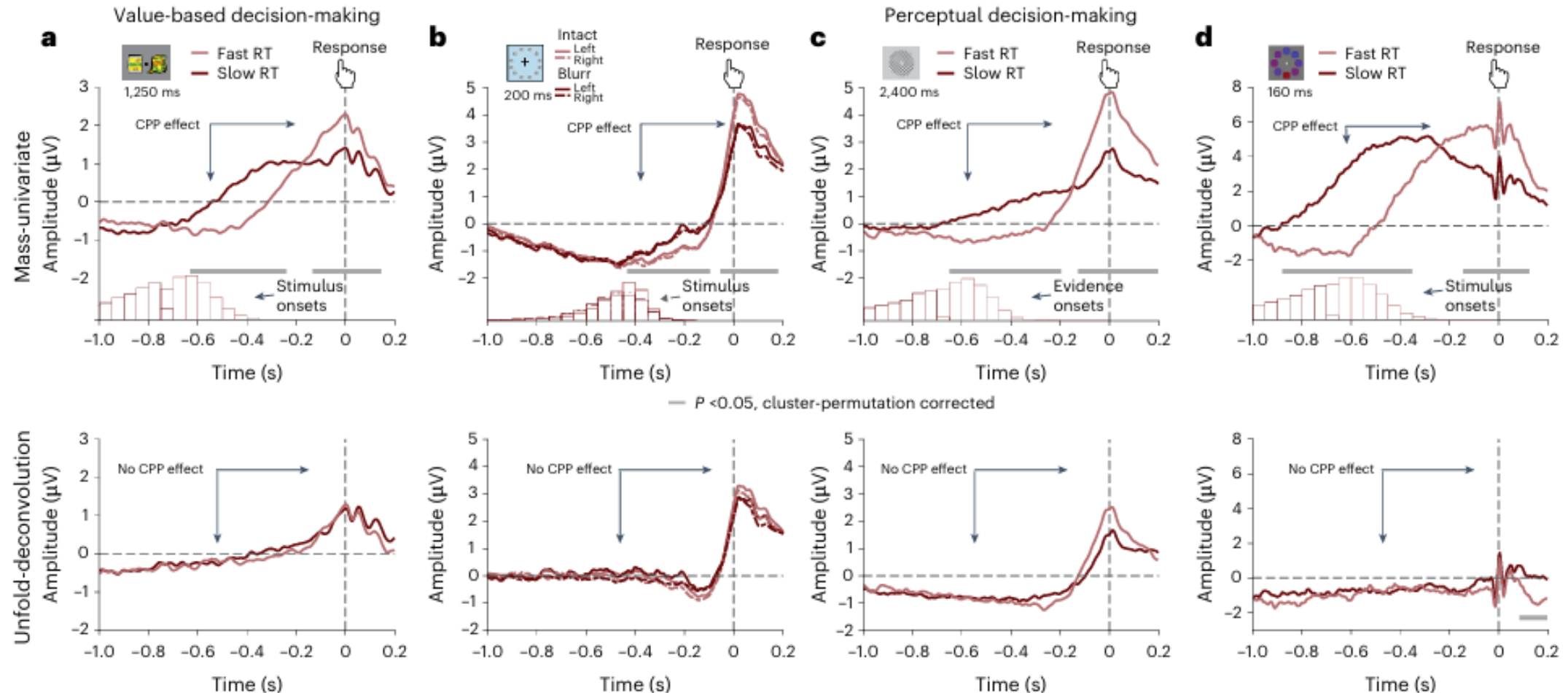


own illustration



own illustration

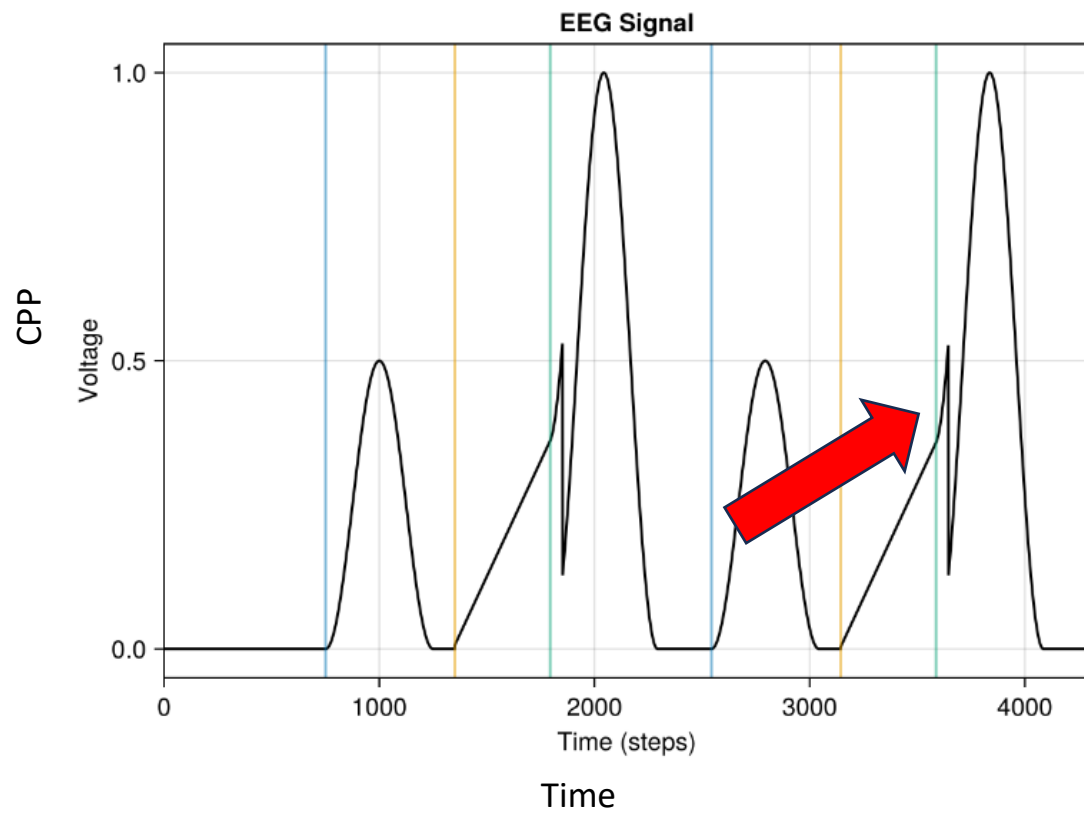
# Results – No component activity after deconv



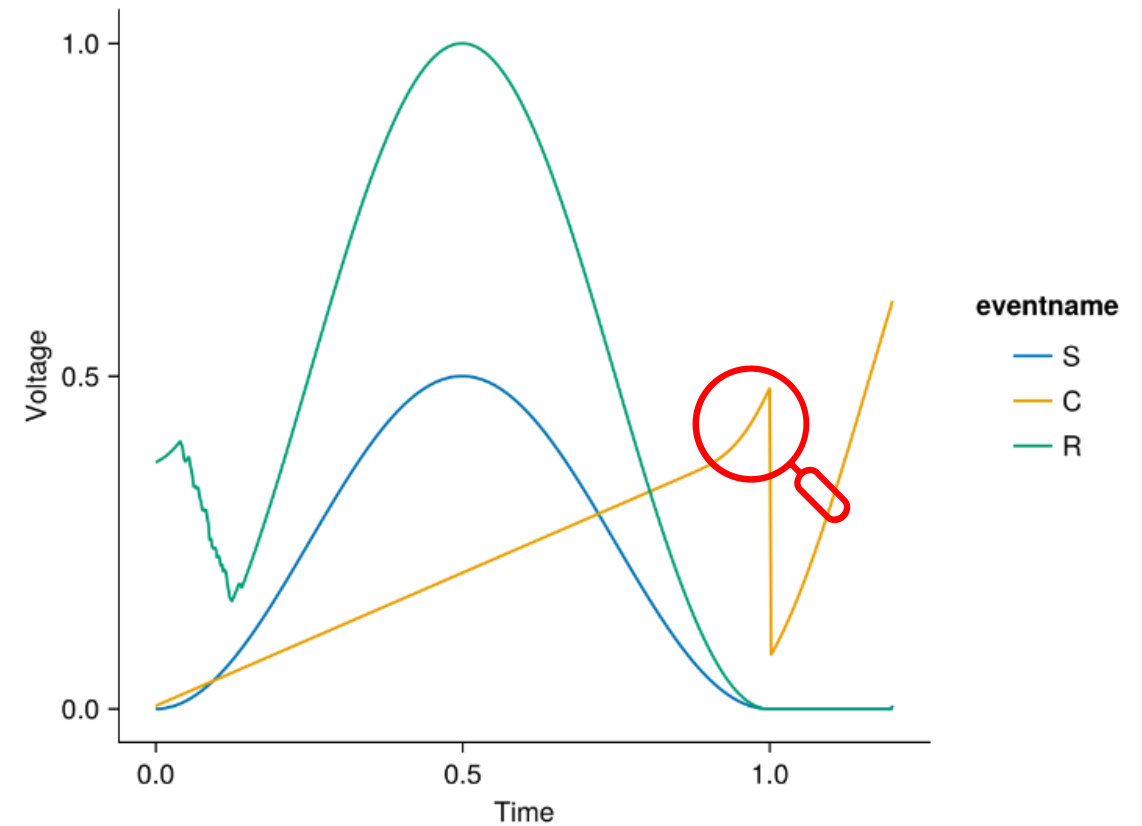
# Results – Overlap Simulation - LBA

Legend

Stimulus(S) Component(C) Response(R)



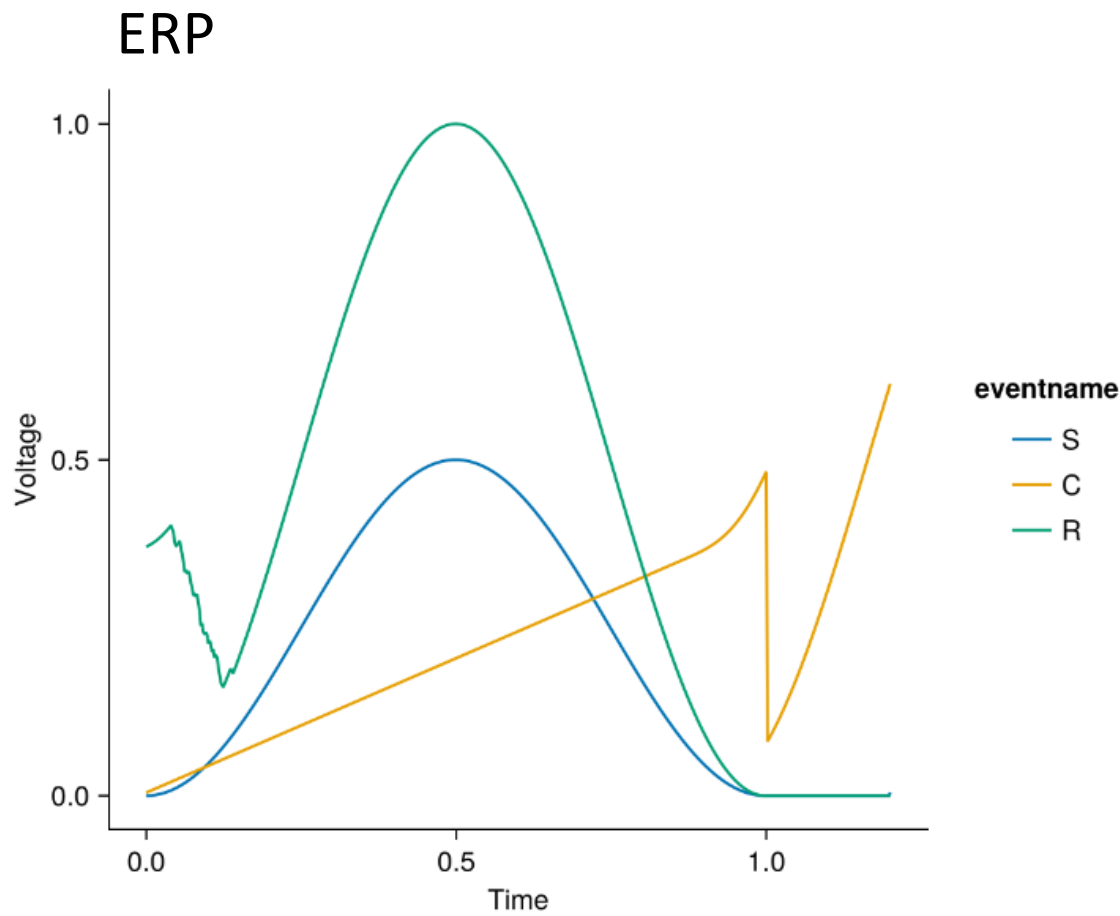
own illustration



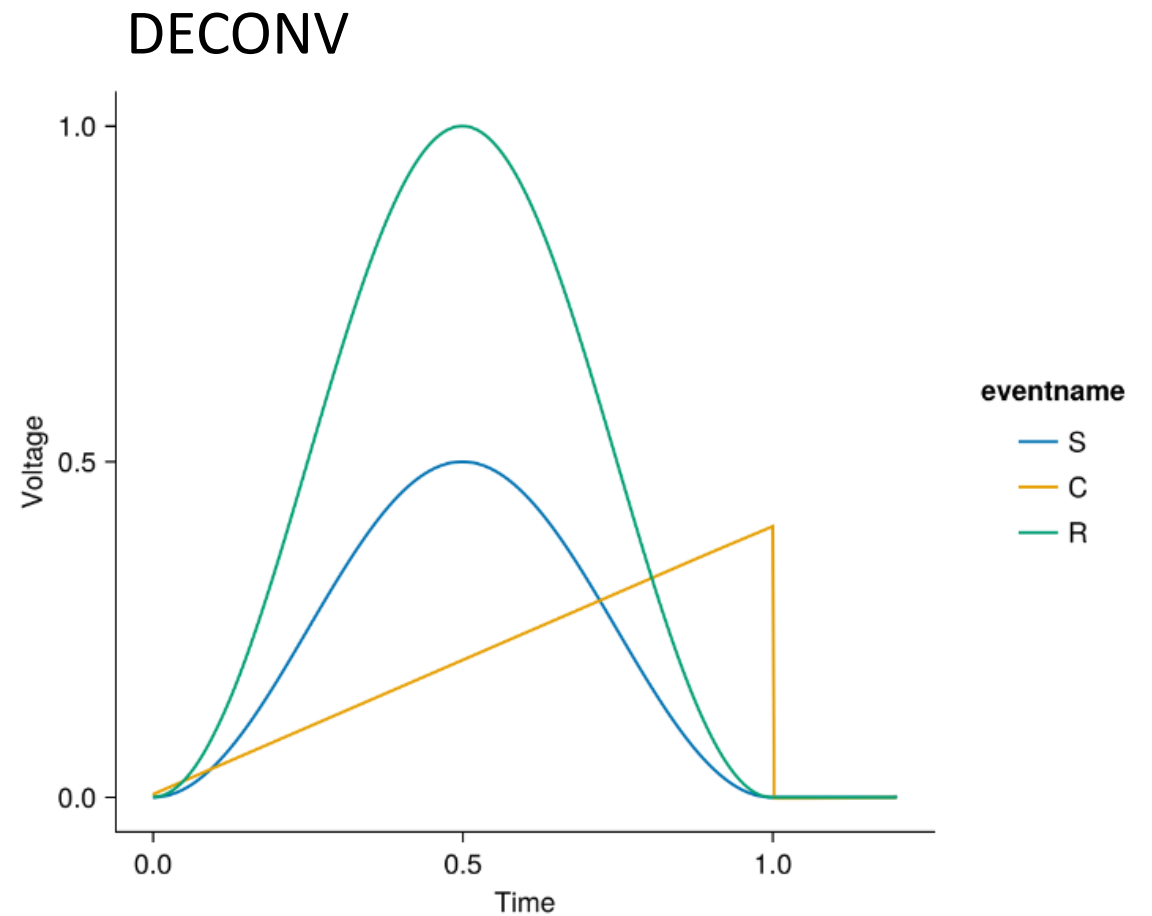
own illustration



# Results – Overlap Simulation - LBA



own illustration

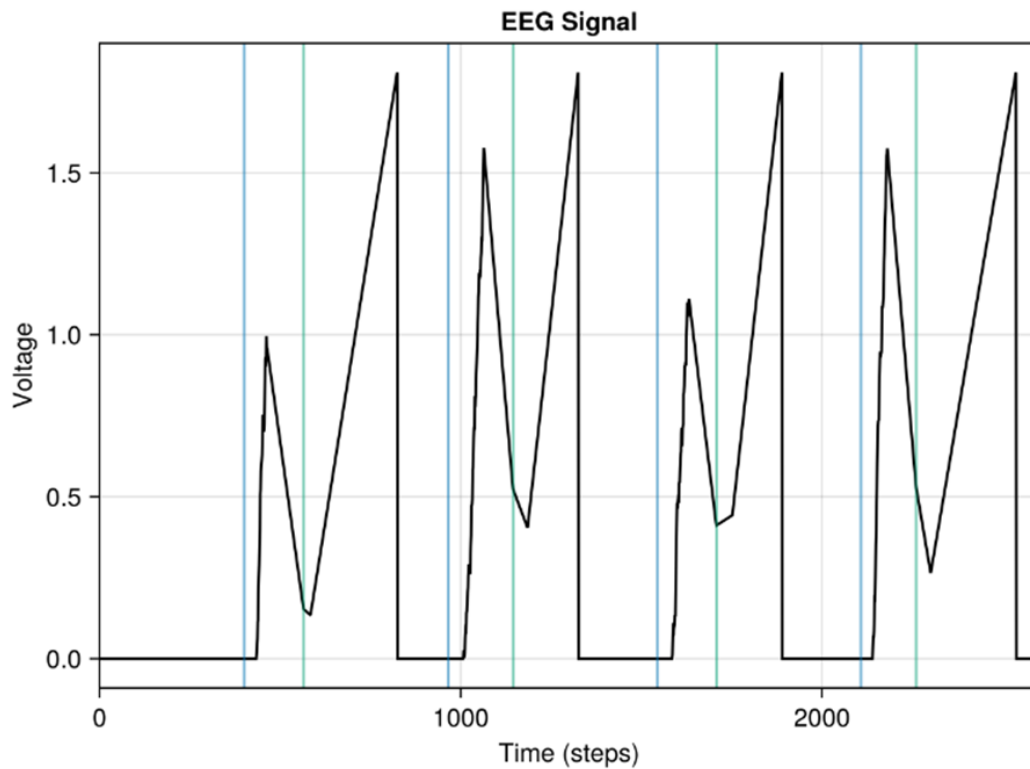


own illustration

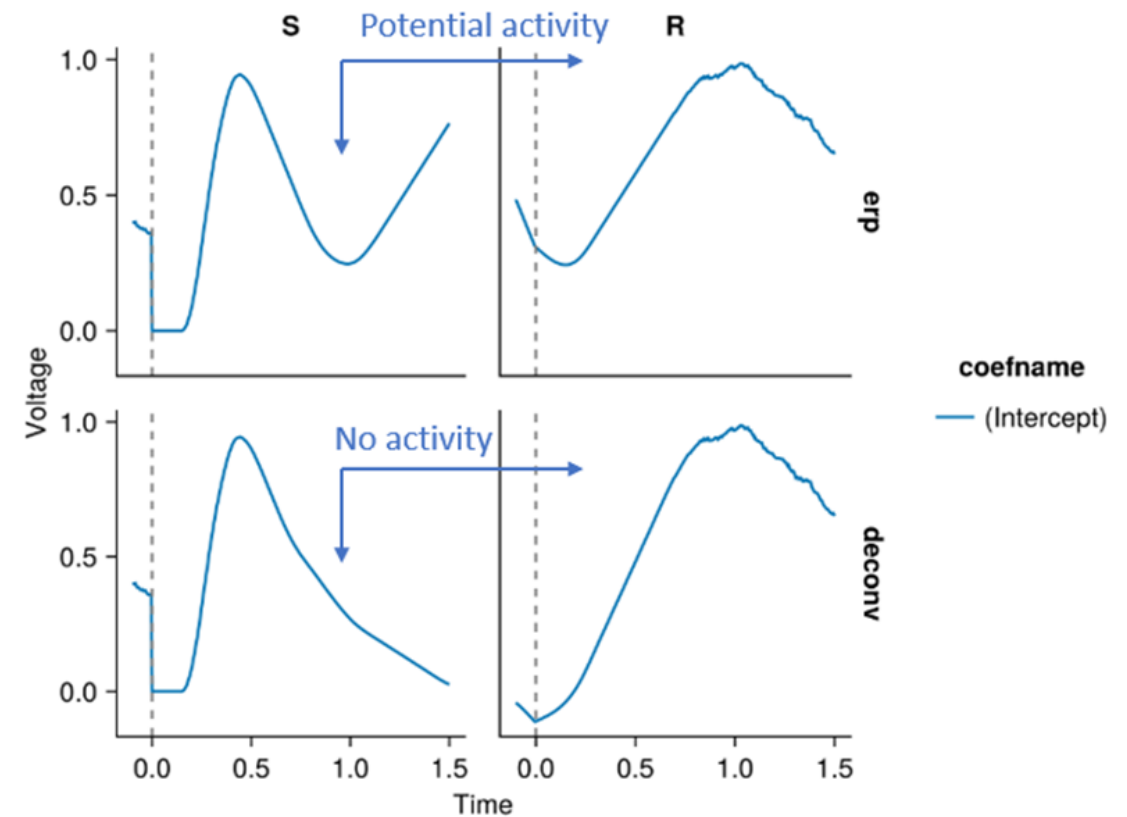
# Results – No component activity after deconv

Legend

Stimulus(S) Response(R)



own illustration



own illustration

# Discussion



## Main Contributions:

- **Extension** for **decision-making** research
- **Model-Based** EEG Simulation
- Overlap & Deconvolution **Use Cases**



## Limitations:

- **Biological** parameter validation
- Integration of other **models**
- **Deconv** could be **further investigated (RIDE)**

## Possible Next Steps

- **Refining** EEG simulations & **validating** with **real EEG** data
- **Parameter optimization** study & **integration** of new **models**

# Questions?

# Literature

- [1]: Redmond G. Connell and Simon P. Kelly. Neurophysiology of human perceptual decision making. *Annual Review of Neuroscience*, 44(Volume 44, 2021):495–516, 2021.
- [2]: Kelly, S. P., Corbett, E. A., & O'Connell, R. G. (2021). Neurocomputational mechanisms of prior informed perceptual decisionmaking in humans. *Nature Human Behaviour*, 5(4), 467–481. [https:// doi.org/10.1038/s41562020009679](https://doi.org/10.1038/s41562020009679)
- [3]: Frömer, R., Nassar, M. R., Ehinger, B. V., & Shenhav, A. (2024). Common neural choice signals can emerge artefactually amid multiple distinct value signals. *Nature Human Behaviour*, 8(11), 2194–2208. <https://doi.org/10.1038/s4156202401971z>
- [4]: S. D. Brown and A. Heathcote, “The simplest complete model of choice response time: Linear ballistic accumulation,” *Cognitive Psychology*, vol. 57, no. 3, pp. 153–178, 2008, doi: [https://doi.org/ 10.1016/j.cogpsych.2007.12.002](https://doi.org/10.1016/j.cogpsych.2007.12.002).