# Multi-Agent Planning to Detect Obstacles and Navigate in an Unknown Environment

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*Abstract*— Rescue operations for individuals lost in a forest can use drones to quickly scan a large unknown environment and provide immediate relief. We propose to work on this problem by making multiple drones cooperatively scan the entire area with unknown obstacles communicating with each other to create a single map.

## I. INTRODUCTION

### A. Objective

- Multiple drones plan and scan the unknown environment. The unknown environment is broken down into a grid and the task of the drones is to visit each cell of the grid in a cooperative manner.
- The drones detect obstacles around them which are then transformed to the initial frame and updated on a common map.
- When a person is found, a different drone using the common map calculates the optimal path to reach their location and provide relief.

### B. Environment

- We will use PyBulletDrone environment for this project.
- The environment spawns these trees at random locations throughout the map which is unknown to the planning algorithm. These obstacles are sensed by the robot as they come within the sensing range of onboard sensors.

### C. Procedure

- Our workspace is $R^3$. Configuration space of the quadcopter is $R^3 \times SO(3)$. We will plan in the workspace $R^3$ itself.
- We use a global planner that directs the drones to scan the environment in a Breadth first search manner. The robots communicate with a central node that directs the search such that 2 drones do not explore the same region.
- The drone gets its next target location from the global planner. We use the $RRT^*$ algorithm on the common map to plan the path for the drone from its current location to the target location.
- Then make the quadcopters follow this path using PID algorithm.

## II. ROBOT MODEL

We have decided to use Quadrotor as our robot.

### A. Model of a rotor

Each rotor rotates with angular velocity $\omega$ and generates a lift force F and moment M. Moment is acting opposite to the directing of rotation.

The lift Force F and moment M of ith rotor can be calculated by:

$$F_i = k_f * \omega_i^2, \qquad k_f = k_T * \rho * D^4$$
$$M_i = k_m * \omega_i^2, \qquad k_m = k_Q * \rho * D^5$$

where:

### B. Equations of Motion

Total thrust and moment is the sum of individual ones in each of the 4 rotors.

Thrust: $F = \sum F_i$ - mga$_3$
Moment: $M = \sum r_i * F_i + \sum M_i$

### C. Newton-Euler Equations for Quadrotor

*Linear Dynamics*:

Applying Newton's Second Law for system of particles, we get (in inertial frame);

$F = m * a$

In matrix form, we get;

$$m * \ddot{r} = \begin{bmatrix} 0 \\ 0 \\ -m * g \end{bmatrix} + R_\psi \phi \theta \begin{bmatrix} 0 \\ 0 \\ \sum F_i \end{bmatrix}$$

*Rotational Dynamics*:

Applying General vector form of Euler's equation; $M_c = I\dot{\omega} + \omega \times (I\omega)$

For Quadrotor, after rearranging the general vector form, we get;

$$I \begin{bmatrix} \dot{p} \\ \dot{q} \\ \dot{r} \end{bmatrix} = \begin{bmatrix} L(F_2 - F_4) \\ L(F_3 - F_1) \\ M_1 - M_2 + M_3 - M_4 \end{bmatrix} - \begin{bmatrix} p \\ q \\ r \end{bmatrix} \times I \begin{bmatrix} p \\ q \\ r \end{bmatrix}$$

Let $\gamma = k_M / k_F$, $M_i = \gamma F_i$, we get;

$$I \begin{bmatrix} \dot{p} \\ \dot{q} \\ \dot{r} \end{bmatrix} = \begin{bmatrix} 0 & L & 0 & -L \\ -L & 0 & L & 0 \\ \gamma & -\gamma & \gamma & -\gamma \end{bmatrix} \begin{bmatrix} F_1 \\ F_2 \\ F_3 \\ F_4 \end{bmatrix} - \begin{bmatrix} p \\ q \\ r \end{bmatrix} \times I \begin{bmatrix} p \\ q \\ r \end{bmatrix}$$

Final equations using Linear and Rotational dynamics equations, we get;

$$\begin{bmatrix} T \\ \tau_1 \\ \tau_2 \\ \tau_3 \end{bmatrix} = \begin{bmatrix} k_F & k_F & k_F & k_F \\ 0 & Lk_F & 0 & -Lk_F \\ -Lk_F & 0 & Lk_F & 0 \\ k_M & -k_M & k_M & -k_M \end{bmatrix} \begin{bmatrix} \omega_1^2 \\ \omega_2^2 \\ \omega_3^2 \\ \omega_4^2 \end{bmatrix}$$

## III. MOTION PLANNING

### A. Global Path Planning

For global path planning, the environment is represented as a grid of a certain area size. The objective is to provide separate paths for all the drones while covering all the cells in the grid. A breadth-first search (BFS) strategy is employed for our multi-drone global path planning algorithm. BFS is chosen for its completeness. In BFS, one vertex is selected at a time, visited, and marked, and then its adjacent vertices are visited and stored in the queue. This process ensures that all cells are covered.

### B. Key Components

*1) GlobalPlanner Class:*

- `__init__(self, drone_id, start)`: Initializes a drone with a unique ID and starting position.
- `move(self, grid, queue, visited)`: Attempts to move the drone to neighboring cells based on a 2D grid. If a valid move is found, the drone updates its position, marks the new cell as visited, and appends the position to its path.

*2) bfs_multi_drones Function:*

- Accepts the size of the grid (`grid_size`) and the number of drones (`num_drones`) as parameters.
- Initializes a grid, starting positions for each drone which are same (0, 0), and a list of `GlobalPlanner` instances.
- Utilizes a BFS strategy to determine the paths for each drone, maintaining a queue of positions to visit using `deque` data structure.
- The algorithm ensures that each drone moves in a way that approximately covers similar cell counts, preventing significant discrepancies in their paths.
- Returns a dictionary containing paths for each drone, where keys are drone identifiers ("Drone 1", "Drone 2", etc.).

### C. Execution

The code initializes a grid of zeros with dimensions `grid_size` x `grid_size`. It then places drones at specified starting position (0, 0) and initiates the BFS algorithm from each drone's initial position. The BFS process continues until all drones have explored the grid exhaustively without revisiting any cell.

*1) RRT Star:* We use the RRT Star algorithm first described by Karaman et al.[1] for planning an error free path between the start and goal positions. The drones maintain a constant and unique altitude at all times ensuring they don't collide with each other. The drones are constrained to maintain the same yaw angle as this does not have any influence on the simulation in our chosen scenario. Therefore, planning is done in the X-Y 2 Dimensional space to reduce search space and improve performance. The start position is the drone's current position, goal position is received from the global planner. The occupancy map is sliced to contain the start and goal locations with sufficient padding. This reduces search space for $RRT^*$ algorithm and improves performance. We have implemented the RRT* algorithm in Python. The $RRT^*$ takes start, goal position, occupancy map and radius as input parameters. Occupancy map contains all the valid positions in XY space that the drone can visit. All vertices in RRT* including start and goal are stored as Node(s). The Node object stores their position, cost, parent nodes and child

nodes. cost = parent's cost + Euclidean distance from parent. All vertices and edges in the RRT* are stored in a networkx[2] undirected graph G. Algorithm:

1: **Do for n iterations**
2: Node: $x_{rand}$ = A random point sampled from the free space (uniform distribution)
3: Node: $x_{nearest}$ = Point nearest to $x_{rand}$
4: Node: $x_{new}$ = Point in free space along line (and farthest to) $x_{nearest}$ to $x_{rand}$ with distance $\leq$ radius
5: Node(s): $x_{arr}$ = List of nodes with Euclidean distance from $x_{new} \leq$ radius
6: Find node $x_{min} \in x_{arr}$ such that $x_{min}$ cost + Euclidean distance between $x_{min}$ and $x_{new}$ is minimum.
7: Add node $x_{new}$ and edge ($x_{min}$, $x_{arr}$) to G. Set $x_{min}$ as the parent of $x_{arr}$
8: **for** $x_{near}$ in $x_{arr}$ **do**
9:     Bool: collision = True if line between $x_{near}$ and $x_{arr}$ goes through an obstacle else False
10:    Float: $new\_cost$ = $x_{near}$ cost + Euclidean distance between $x_{near}$ and $x_{arr}$
11:    **if**(collision == False & $new\_cost <$ $x_{near}$ cost)
12:        Remove edge (parent $x_{near}$, $x_{near}$)
13:        Add edge ($x_{new}$, $x_{near}$) and set $x_{new}$ as parent of $x_{near}$
14:    **end if**
15: **end for**
16: After every 100 iterations check if goal is within the radius of a vertex and can be connected to it without collision

The algorithm terminates once the Goal can be connected. Path is found by connecting the parent node of all nodes starting with the goal node. While flying, at each timestep, the drone finds all the vertices in the path that are within distance radius. Then the drone flies towards the vertice that is furthest up the path.

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## IV. RESULTS

### A. Setup

The simulation uses pybullet for physics and few methods from gym-pybullet-drones modified to suit our needs. Important parameters used for experimenting are - number of drones, number of trees and area size. For the most part we've used 3 drones for exploring a forest area of $900m^2$ with 200 trees (obstacles) as shown in [picture].

The global planner provides way-points for each drone such that the entire forest is scouted. All way-points are considered as local intermediate goals used to reveal slices of the global occupancy map to the drone, which navigates using a obstacle free path provided by the RRT algorithm. The drone uses a PID controller (code reuse) to follow the desired path.

### B. Results

This video shows drones navigating in the aforementioned setup.

[picture] shows the path (in yellow) followed by each drone to explore the map using the path provided by global path planner, which took x mins.

[picture] shows the simulation running in a smaller area of $400m^2$ with 100 trees took x mins.

[picture] shows the RRT trees in a local map. As shown the drone doesn't have to know its final goal postion and such a series of local maps can guide the drone towards the goal while offering benefits of faster computation.

## V. DISCUSSION

### A. Path planning and Control



Area vs Time for path planning
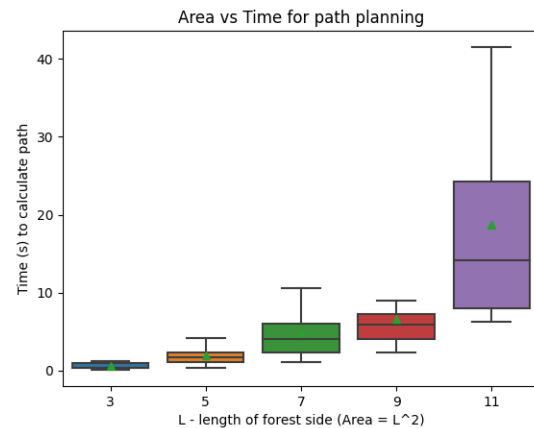
As shown, the computation time tends to increase exponentially with area and so we've solved RRTs on a smaller areas.

RRTs produce collision free paths but they are not necessarily smooth or optimal. In terms of improvements, the differential flatness property of a drone can be exploited to control motion upto the fourth derivative and generate smoother paths and simplifying trajectory generation.

### B. Global planner

The global planner provides a series of goals for every drone in the global frame, scouting the entire region. This is done by converting the grid into cells and providing separate paths for each drone to visit. This is indeed practical and efficient as it provides continuous cell path by covering immediate neighbouring cells.

In practice, the global planner could use a satellite image of a forest and plan drones to cover it.

### C. Local maps

To reduce overall computation time, RRT computes multiple obstacle free paths using a series of local maps to reach the global goal. This is done by slicing sections of the global occupancy map just enough to include the next goal given by the global planner to avoid use of a global occupancy map. The area vs time figure clearly shows that local maps of small areas combined would take shorter time to compute compared to the exponential increase of using a single global map.

### D. Obstacle detections

With that said, all obstacles are revealed within a local map for the drone to compute a obstacle free path. The local map's dimensions can differ depending on the global map and grid size, which means detecting all obstacles within a local map is unlikely in the real world where sensors have a limited range of detection. A potential improvement here to imitate a real world scenario is using a dynamic local map and revealing obstacles only within a certain radius of the drone.

### REFERENCES

[1] S. Karaman and E. Frazzoli, "Sampling-based algorithms for optimal motion planning," *The international journal of robotics research*, vol. 30, no. 7, pp. 846–894, 2011.

[2] A. A. Hagberg, D. A. Schult, and P. J. Swart, "Exploring network structure, dynamics, and function using networkx," in *Proceedings of the 7th Python in Science Conference* (G. Varoquaux, T. Vaught, and J. Millman, eds.), (Pasadena, CA USA), pp. 11 – 15, 2008.