

Multi-Agent Planning to Detect Obstacles and Navigate in an Unknown Environment

Agarwal, Shantnav Deshmukh, Shlok Singh, Manupriya Theocharous, Alexandros
5939933 5928516 6050425 5930901

Abstract—Rescue operations for individuals lost in a forest can use drones to quickly scan a large unknown environment and provide relief. We propose a solution by making multiple drones cooperatively scan the entire unknown area. Through simulation we show that the combination of an efficient global and local planner can reduce search time significantly.

I. INTRODUCTION

Multiple drones efficiently navigate and survey an unfamiliar environment which is broken down into a grid and systematically covering each cell in a cooperative manner. The drones identify obstacles within their vicinity, relay the information to a central map, and update it collaboratively. In this project, we leverage the PyBulletDrone environment, where we have randomly placed trees. The robots sense these obstacles as they enter the sensing range of their onboard sensors. Our approach employs a global planner, guiding drones in a Breadth First Search fashion. Communication with a central node ensures strategic exploration, preventing overlap between two drones. The global planner dictates each drone's target location. Utilizing the *RRT** algorithm on the common map, we plan paths for the drones, subsequently employing the PID algorithm to precisely follow these paths.

II. ROBOT MODEL

We have decided to use Quadrotor as our robot.

A. Model of a rotor

Each rotor rotates with angular velocity ω and generates a lift force F and moment M . Moment is acting opposite to the directing of rotation.

The lift Force F and moment M of i th rotor can be calculated by:

$$\begin{aligned} F_i &= k_f * \omega_i^2, & k_f &= k_T * \rho * D^4 \\ M_i &= k_m * \omega_i^2, & k_m &= k_Q * \rho * D^5 \end{aligned}$$

where:

B. Equations of Motion

Total thrust and moment is the sum of individual ones in each of the 4 rotors.

$$\text{Thrust: } F = \sum F_i - m g a_3$$

$$\text{Moment: } M = \sum r_i * F_i + \sum M_i$$

C. Newton-Euler Equations for Quadrotor

Linear Dynamics:

Applying Newton's Second Law for system of particles, we get (in inertial frame);

$$F = m * a$$

In matrix form, we get;

$$m * \ddot{r} = \begin{bmatrix} 0 \\ 0 \\ -m * g \end{bmatrix} + R_\psi \phi \theta \begin{bmatrix} 0 \\ 0 \\ \sum F_i \end{bmatrix}$$

Rotational Dynamics:

Applying General vector form of Euler's equation; $M_c = I\dot{\omega} + \omega \times (I\omega)$

For Quadrotor, after rearranging the general vector form, we get;

$$I \begin{bmatrix} \ddot{p} \\ \ddot{q} \\ \ddot{r} \end{bmatrix} = \begin{bmatrix} L(F_2 - F_4) \\ L(F_3 - F_1) \\ M_1 - M_2 + M_3 - M_4 \end{bmatrix} - \begin{bmatrix} p \\ q \\ r \end{bmatrix} \times I \begin{bmatrix} p \\ q \\ r \end{bmatrix}$$

Let $\gamma = k_M/k_F$, $M_i = \gamma F_i$, we get;

$$I \begin{bmatrix} \ddot{p} \\ \ddot{q} \\ \ddot{r} \end{bmatrix} = \begin{bmatrix} 0 & L & 0 & -L \\ -L & 0 & L & 0 \\ \gamma & -\gamma & \gamma & -\gamma \end{bmatrix} \begin{bmatrix} F_1 \\ F_2 \\ F_3 \\ F_4 \end{bmatrix} - \begin{bmatrix} p \\ q \\ r \end{bmatrix} \times I \begin{bmatrix} p \\ q \\ r \end{bmatrix}$$

Final equations using Linear and Rotational dynamics equations, we get;

$$\begin{bmatrix} T \\ \tau_1 \\ \tau_2 \\ \tau_3 \end{bmatrix} = \begin{bmatrix} k_F & k_F & k_F & k_F \\ 0 & Lk_F & 0 & -Lk_F \\ -Lk_F & 0 & Lk_F & 0 \\ k_M & -k_M & k_M & -k_M \end{bmatrix} \begin{bmatrix} \omega_1^2 \\ \omega_2^2 \\ \omega_3^2 \\ \omega_4^2 \end{bmatrix}$$

III. MOTION PLANNING

A. Global Path Planning

For global path planning, the environment is represented as a grid of a certain area size. The objective is to provide separate paths for all the drones while covering all the cells in the grid. A breadth-first search (BFS) strategy is employed for our multi-drone global path planning algorithm. BFS is chosen for its completeness. In BFS, one vertex is selected at a time, visited, and marked, and then its adjacent vertices are visited and stored in the queue. This process ensures that all cells are covered.

B. Key Components

1) GlobalPlanner Class:

- `__init__(self, drone_id, start)`: Initialize a drone with a unique ID and starting position.
- `move(self, grid, queue, visited)`: Attempts to move the drone to neighboring cells based on a 2D grid. If a valid move is found, the drone updates its position, marks the new cell as visited, and appends the position to its path.

2) bfs_multi_drones Function:

- Accepts the size of the grid (`grid_size`) and the number of drones (`num_drones`) as parameters.
- Initializes a grid, starting positions for each drone which are same (0, 0), and a list of *GlobalPlanner* instances.
- Utilizes a BFS strategy to determine the paths for each drone, maintaining a queue of positions to visit using *deque* data structure.
- The algorithm ensures that each drone moves in a way that approximately covers similar cell counts, preventing significant discrepancies in their paths.
- Returns a dictionary containing paths for each drone, where keys are drone identifiers ("Drone 1", "Drone 2", etc.).

C. Execution

The code initializes a grid of zeros with dimensions `grid_size x grid_size`. It then places drones at specified starting position (0, 0) and initiates the BFS algorithm from each drone's initial position. The BFS process continues until

all drones have explored the grid exhaustively without revisiting any cell.

D. RRT Star

We use the RRT Star algorithm first described by Karaman et al.[1] for planning an error free path between the start and goal positions. The drones maintain a constant and unique altitude at all times ensuring they don't collide with each other. The drones are constrained to maintain a constant yaw angle as this does not have any influence on the simulation in our chosen scenario.

1) *Planning*: Therefore, planning is done in the X-Y 2 Dimensional space to reduce search space and improve performance. The start position is the drone's current position, goal position is received from the global planner. The occupancy map is sliced to contain the start and goal locations with sufficient padding. This reduces search space for *RRT** algorithm and improves performance.

2) *Algorithm & Execution*: We have implemented the *RRT** algorithm from scratch in Python. The *RRT** takes start, goal position; occupancy map and radius as input parameters. Occupancy map contains all the valid positions in XY space that the drone can visit. We calculate this occupancy map by convolving the drone's occupancy map over the world map (received from the simulation). All vertices in *RRT** including start and goal are stored as Node(s). The Node object stores their position, cost (cost = parent's cost + Euclidean distance from parent), parent nodes and child nodes. All vertices and edges in the *RRT** are stored in a `networkx[2]` undirected graph G.

1: Do for n iterations

- 2: Node: x_{rand} = A random point sampled from the free space (uniform distribution)
- 3: Node: $x_{nearest}$ = Point nearest to x_{rand}
- 4: Node: x_{new} = Point in free space along line (and farthest to) $x_{nearest}$ to x_{rand} with distance \leq radius
- 5: Node(s): x_{arr} = List of nodes with Euclidean distance from $x_{new} \leq$ radius
- 6: Find node $x_{min} \in x_{arr}$ such that x_{min} cost + Euclidean distance between x_{min} and x_{new} is minimum.
- 7: Add node x_{new} and edge (x_{min}, x_{arr}) to G. Set x_{min} as the parent of x_{arr}

```

8: for  $x_{near}$  in  $x_{arr}$  do
9:   Bool: collision = True if line between
      $x_{near}$  and  $x_{arr}$  goes through an obstacle else
     False
10:  Float:  $new\_cost$  =  $x_{near}$  cost + Eu-
        clidean distance between  $x_{near}$  and  $x_{arr}$ 
11:  if(collision == False &  $new\_cost$  <
      $x_{near}$  cost)
12:    Remove edge (parent  $x_{near}$ ,  $x_{near}$ )
13:    Add edge ( $x_{new}$ ,  $x_{near}$ ) and set
      $x_{new}$  as parent of  $x_{near}$ 
14:  end if
15: end for
16: After every 100 iterations check if goal is
     within the radius of a vertex and can be
     connected to it without collision

```

The algorithm terminates once the Goal can be connected.

3) *Path Following*: Path is found by connecting the parent node of all nodes starting with the goal node. While flying, at each timestep, the drone finds all the vertices in the path that are within a distance radius. Then the drone flies towards the vertex that is furthest up the path.

IV. RESULTS

A. Setup

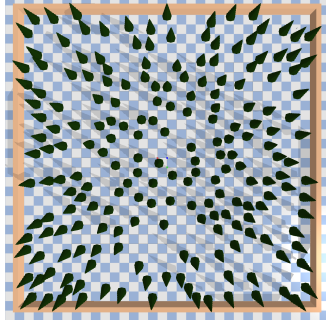


Fig. 1: Simulation (top view)

The simulation uses pybullet for physics and few control methods adapted from gym-pybullet-drones. Important parameters used for experimenting are - number of drones, number of trees and area size. For the most part we've used 3 drones for exploring a forest area of $900m^2$ with 200 trees (obstacles) as shown in Fig. 1.

Other parameters include simulation frequency set at 48Hz. In each step/loop the next

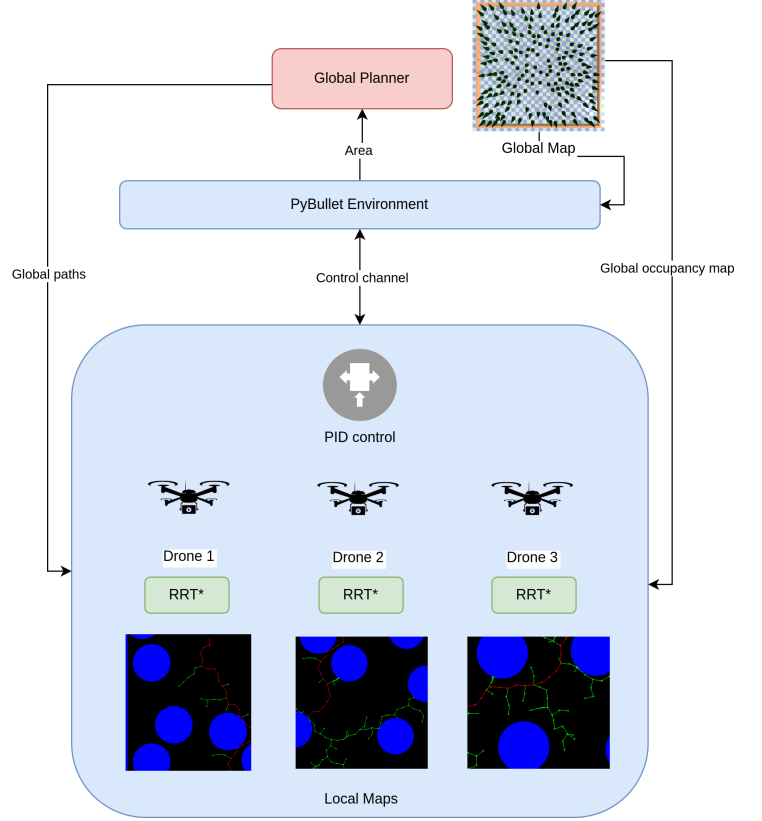


Fig. 2: Architecture diagram

action is either executed or sampled (planned) for a drone.

Fig 2. represents a high level overview of how all processes tie in together to calculate and execute a obstacle free path.

B. Results

This [video](#) shows drones navigating in the aforementioned setup.

Fig. 3 shows paths followed by each drone to explore the map using paths provided by global path planner and RRT algorithm, which took 8 hours in simulation time (3 mins in practice).

Fig. 4 shows the RRT trees in a local map. As shown the drone doesn't have to know its final goal position and such a series of local maps can guide the drone towards the goal while offering benefits of faster computation.

V. DISCUSSION

A. Path planning and Control

As shown in Figure 3, the computation time tends to increase exponentially with area, and

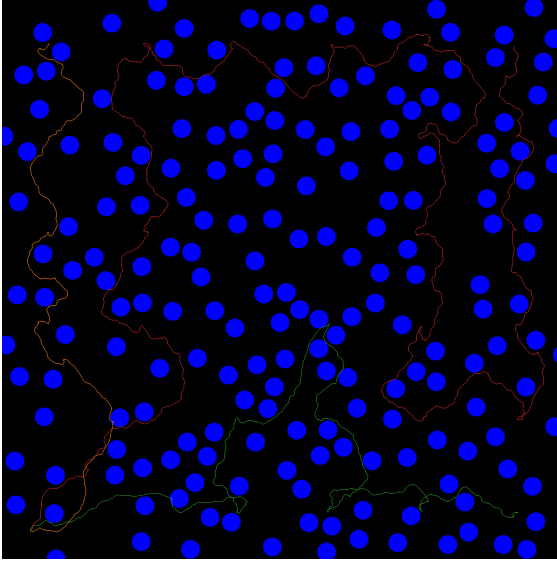


Fig. 3: Occupancy map on a 30 x 30 m area

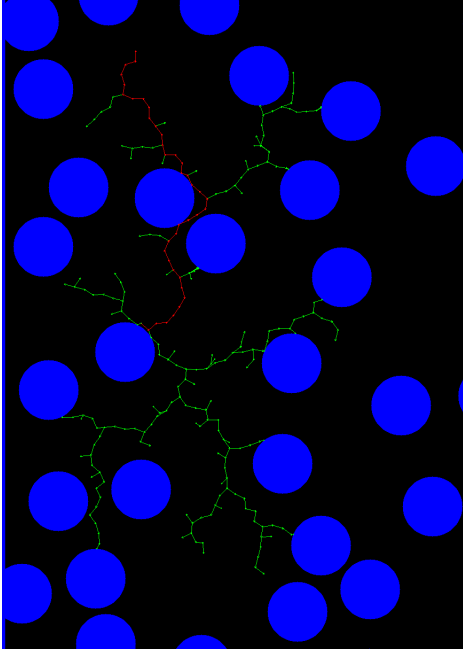


Fig. 4: RRT on a local occupancy map

so we've solved RRTs on smaller areas. The total time combined for solving RRTs on smaller maps is lesser than finding a path on the entire area.

RRTs produce a collision-free path, but they are neither smooth nor optimal. A smooth path that adheres to the differential flatness property of a drone (i.e., four times differentiable) will allow us to directly calculate the required rotor torques for controlling the drone. Using this information, a better controller with feed-forward

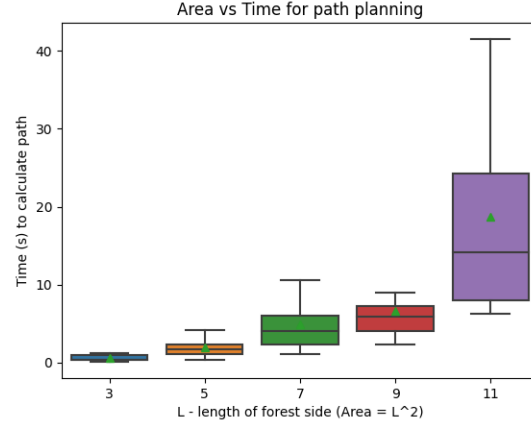


Fig. 5: Area to explore vs time for finding path

control can be implemented. Webb et al. introduced a Kindodynamic *RRT** algorithm that exactly and optimally connects any pair of states for any system with controllable linear dynamics in state spaces of arbitrary dimensions[3]. With this improvement, the drone can fly faster and cover more distance as well. In terms of improvements, the differential flatness property of a drone can be exploited to control motion upto the fourth derivative and generate smoother paths and simplifying trajectory generation.

B. Global planner

The global planner provides a series of goals for every drone in the global frame, scouting the entire region. This is done by converting the grid into cells and providing separate paths for each drone to visit using BFS. This is indeed practical and efficient as it provides continuous cell path by covering immediate neighbouring cells.

With this approach, the path pursued by multiple drones is suboptimal compared to a single drone navigating the grid, but this also reduces the total time since the work is distributed now.

Area	Optimal distance	Travelled distance	Drones
100	99	100.4	1
100	99	103.65	3
400	399	400.41	1
400	399	403.65	3
900	899	900.41	1
900	899	903.65	3

In practice, the global planner could use a satellite image of a forest and plan drones to cover it.

C. Local maps

To reduce overall computation time, RRT computes multiple obstacle free paths using a series of local maps to reach the global goal. This is done by slicing sections of the global occupancy map just enough to include the next goal given by the global planner to avoid use of a global occupancy map. The area vs time figure clearly shows that local maps of small areas combined would take shorter time to compute compared to the exponential increase of using a single global map.

D. Obstacle detections

With that said, all obstacles are revealed within a local map for the drone to compute a obstacle free path. The local map's dimensions can differ depending on the global map and grid size, which means detecting all obstacles within a local map is unlikely in the real world where sensors have a limited range of detection. A potential improvement here to imitate a real world scenario is using a dynamic local map and revealing obstacles only within a certain radius of the drone.

REFERENCES

- [1] Sertac Karaman and Emilio Frazzoli. "Sampling-based algorithms for optimal motion planning". In: *The international journal of robotics research* 30.7 (2011), pp. 846–894.
- [2] Aric A. Hagberg, Daniel A. Schult, and Pieter J. Swart. "Exploring Network Structure, Dynamics, and Function using NetworkX". In: *Proceedings of the 7th Python in Science Conference*. Ed. by Gaël Varoquaux, Travis Vaught, and Jarrod Millman. Pasadena, CA USA, 2008, pp. 11–15.
- [3] Dustin J. Webb and Jur van den Berg. "Kinodynamic RRT*: Optimal Motion Planning for Systems with Linear Differential Constraints". In: *CoRR* abs/1205.5088 (2012). arXiv: [1205.5088](https://arxiv.org/abs/1205.5088). URL: <http://arxiv.org/abs/1205.5088>.