

# Lossless Image Compression

CS6025 Data Encoding

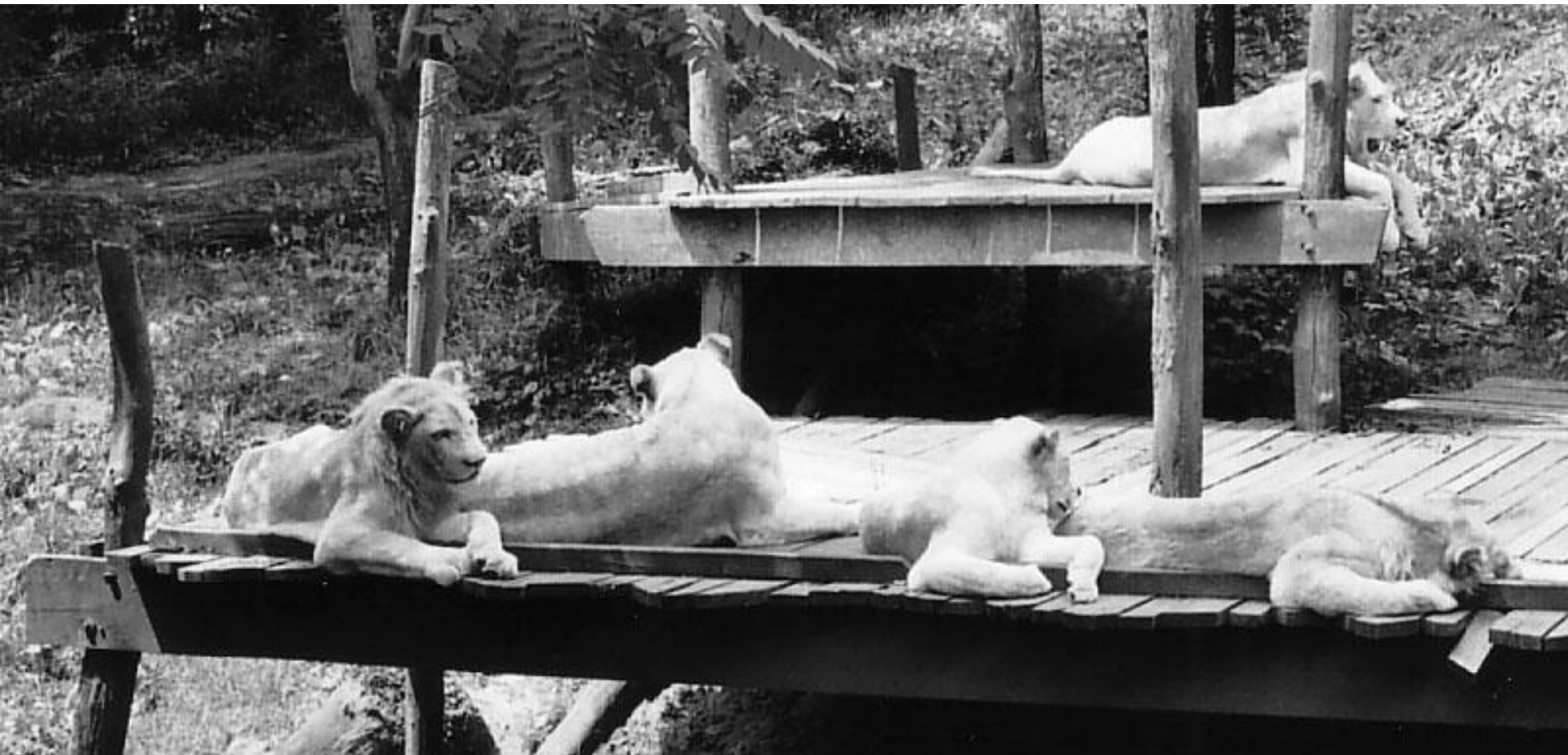
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1-22-15

# Continuous-Tone Image



# Grayscale Image of $2^8$ Shades



# Bi-level Image



# Raw Images

- Some digital cameras can produce raw images.
- Usually 24 bits (RGB) for each pixel.
- Easy to write a program to display the image.
- Each camera company has its own file format.
  - .cr2 (Canon), .dng (Adobe), .tif (Kodak)
- Windows has .bmp
  - Viewable with Microsoft Office, paint, Photoshop

# Windows BMP File Format

- 54 bytes for the header, beginning with “BM”.
- Then height \* width \* 3 bytes for the image.
- Can be viewed with IE or Windows Media tools.
- Uses little endian for multi-byte parameters.
- Image rows start at bottom.

# HexDump of BMP Header

- Highlighted are: (0x424d = “BM”)
  - Image offset (0x36) (14 + 40 = 54)
  - Header length (0x28 = 40 header begins here)
  - Width (0x0200 = 512)
  - Height (0x0200 = 512)
  - Depth (bits per pixel) ( 0x18 = 24)

0	424d 3600 0c00 0000 0000 0000 3600 0000 2800	BM6.....6...(. .....
10	0000 0002 0000 0002 0000 0100 1800 0000	.....
20	0000 0000 0c00 0000 0000 0000 0000 0000	.....
30	0000 0000 0000 0000 5d24 4f77 3a87 8b39	.....]\$Ow...9
40	8f88 48a4 8d3b 7188 214c 6530 7c80 3285	..H..;q.!Le0 .2.

# Reading Dimension from BMP Header

```
void readHeader(){
    byte[] header = new byte[54]; // 54 bytes for header
    try {
        System.in.read(header);
        System.out.write(header);
    } catch (IOException e){
        System.err.println(e.getMessage());
        System.exit(1);
    }
    if (header[0] != 'B' || header[1] != 'M'
        || header[14] != 40 || header[28] != 24)
        System.exit(1);
    int w1 = header[18]; int w2 = header[19];
    if (w1 < 0) w1 += 256; if (w2 < 0) w2 += 256;
    width = w2 * 256 + w1;
    int h1 = header[22]; int h2 = header[23];
    if (h1 < 0) h1 += 256; if (h2 < 0) h2 += 256;
    height = h2 * 256 + h1;
}
```



LenaRGB.bmp 512x512, 24-bit

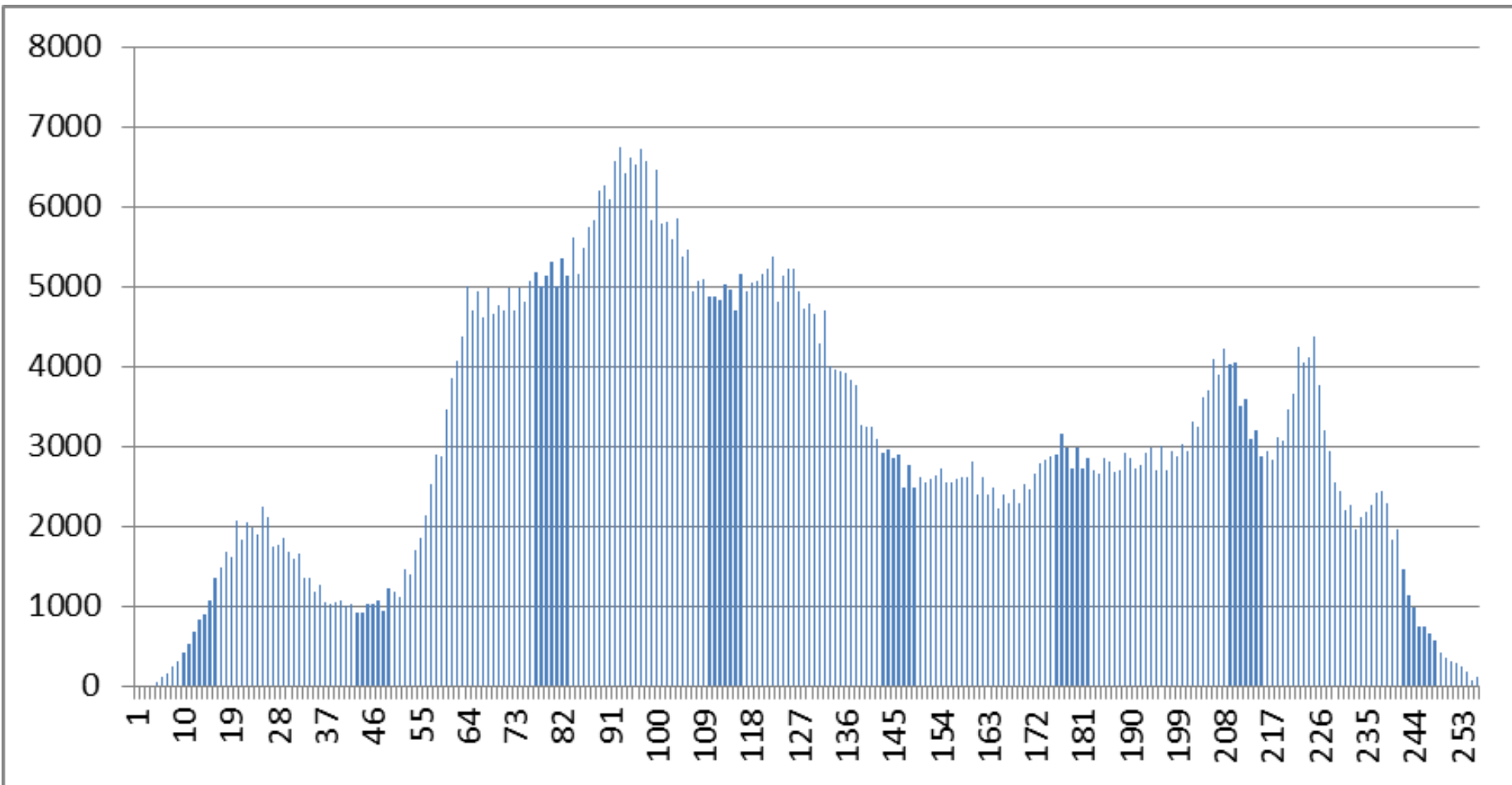


# Reading Pixel Values

```
void readImage(){
    byte[] image = new byte[height * width * 3];
    raw = new short[height][width][3]; // upside down
    try {
        System.in.read(image);
    } catch (IOException e){
        System.err.println(e.getMessage());
        System.exit(1);
    }
    int index = 0;
    for (int i = 0; i < height; i++)
        for (int j = 0; j < width; j++)
            for (int k = 0; k < 3; k++){
                raw[i][j][k] = (short)image[index++];
                if (raw[i][j][k] < 0) raw[i][j][k] += 256;
            }
}
```

# Lena Pixel Values

Entropy = 7.75



# JPEG-LS

- Predict  $x$  using  $a$ ,  $b$ , and  $c$ .
- If  $c = \max(a, b, c)$ , predict  $x = \min(a, b)$ .
- If  $c = \min(a, b, c)$ , predict  $x = \max(a, b)$ .
- Else predict  $x = a + b - c$ .

c	b
a	x

# Predicting Using Neighboring Values

```
int predict(int a, int b, int c){  
    int x;  
    if ((c >= a) && (c >= b)) x = (a >= b) ? b : a;  
    else if ((c <= a) && (c <= b)) x = (a >= b) ? a : b;  
    else x = a + b - c;  
    return x;  
}
```

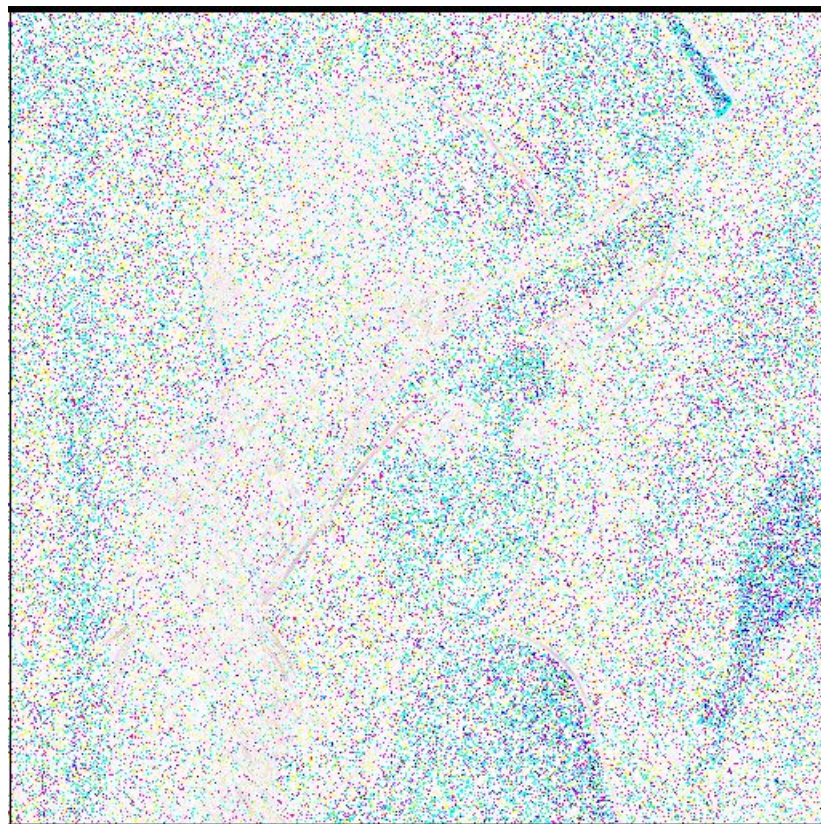
# Prediction Errors for Lena

- There are  $512 \times 512 \times 3 = 786,432$  pixel values.
- 74130 values (9.4%) are correctly predicted.
  - 2066 of them have  $a=b=c=x$ .
- Prediction error = actual value – predicted value.
- Error range  $[-255, 255]$

Lena |Error| from Prediction

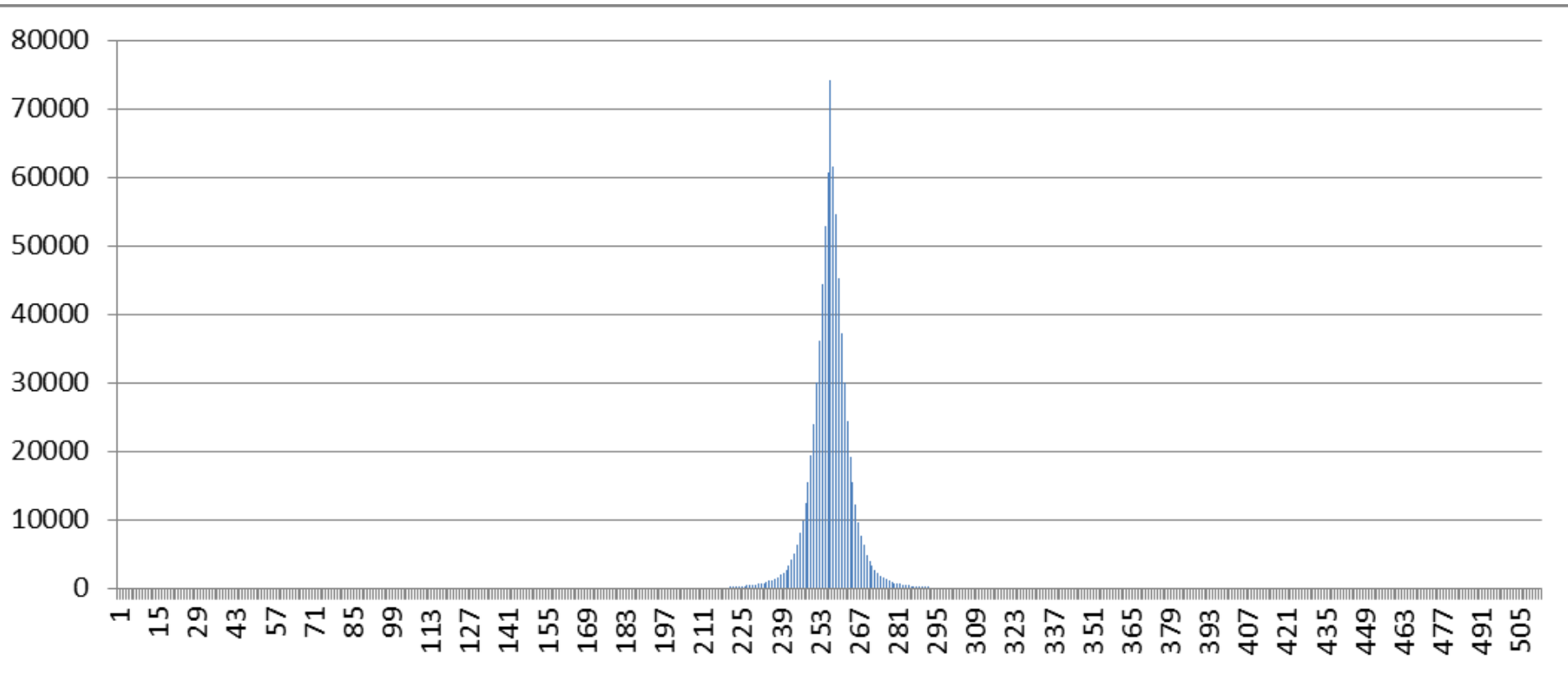


# 256 - Lena Prediction | Errors |





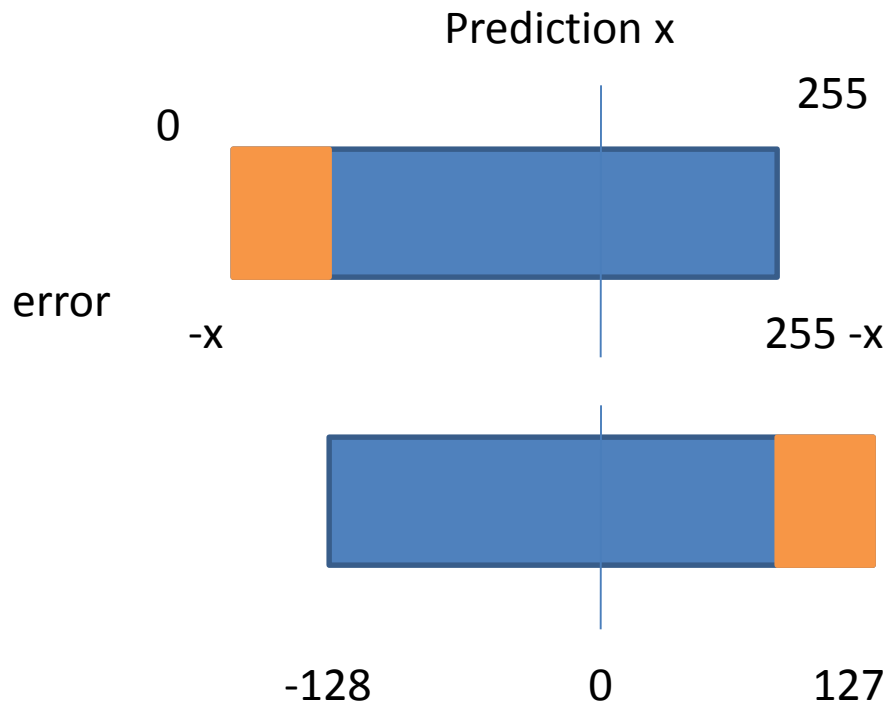
# Lena Prediction Error + 256 Distribution



# Error Mapping

- `int e = value - x;`
- `if (e > 127) e -= 256;`
- `else if (e < -128) e += 256;`
- `value` in  $[0, 255]$ , `e` in  $[-x, 255-x]$
- If  $255-x > 127$ ,  $-x > -255+127=-128$
- Move  $[128, 255-x]$  to  $[-128, -x-1]$
- This is `e -= 256` when `e > 127`

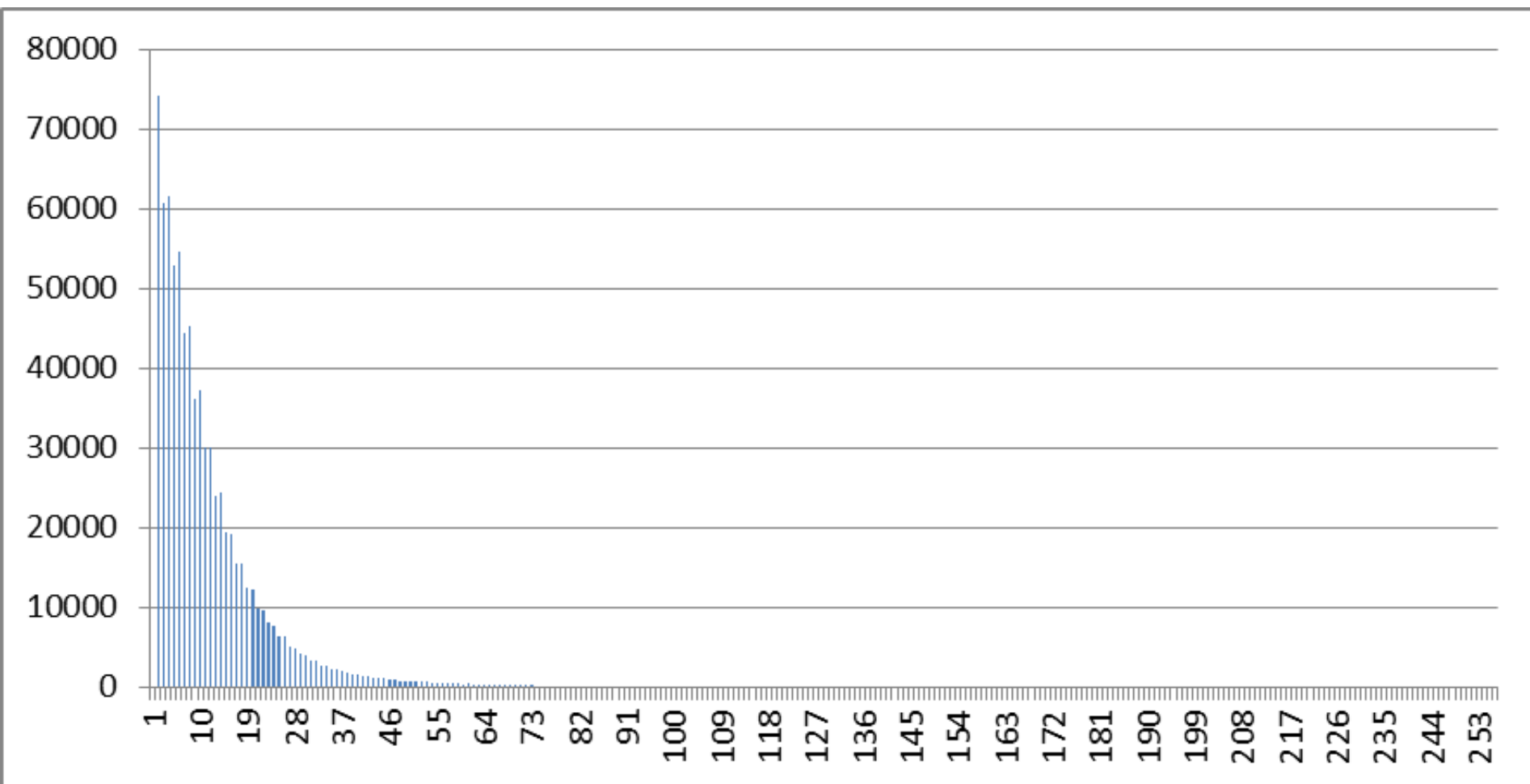
# Error Mapping



# Interlaced Error Array

- $e = (e \geq 0) ? e * 2 : -e * 2 - 1;$
- If  $e$  is nonnegative,  $e$  become an even number (multiplied by 2)
- If  $e$  is negative,  $e$  is mapped to a positive odd number.
- The mapping is 0 -1 1 -2 2 -3 3 ... into 0 1 2 3 4..
- Gamma or  $C^1$  (Fibonacci code) can now be used on these nonnegative integers.

# Lena Prediction Error $\text{Entropy} = 4.83$



# Mapping Error to [0, 255]

```
// map the prediction error to nonnegatives
int mapError(int value, int prediction){
    int e = value - prediction;    // prediction error
    if (e > 127) e -= 256; // putting error in [-128, 127]
    else if (e < -128) e += 256;
    int error = (e >= 0) ? e * 2 : -e * 2 - 1;
    // into 0 -1 1 -2 2 array (interlacing)
    return error;
}
```

# Unwrapping the Error

- Reverse error =  $(e \geq 0) ? e * 2 : -e * 2 - 1$ ;
- If  $e$  is less than  $-x$  ( $x$  is the prediction), then add 256 to it.
- If  $e$  is greater than  $255-x$ , then subtract 256 from it.
- $x+e$  is the decoded pixel value.

# Unmapping Error

```
short unmapError(int error, int predicted){  
    int e = 0;  
    // Your code to reverse the line in H4A:  
    // error = (e >= 0) ? e * 2 : -e * 2 - 1;  
    int value = predicted + e;  
    if (value > 255) value -= 256;  
    else if (value < 0) value += 256;  
    return (short)value;  
}
```



# Read in the $C^1$ Codeword

- Read bits in and if the  $i$ th bit is 1, add  $\text{fib}[i]$  to error, until two consecutive 1's are read.
- example:  $1001011 \rightarrow e = \text{fib}[0] + \text{fib}[4] + \text{fib}[6] = 1 + 5 + 13 = 19$
- This is performed by `int deFib()`, to read the next  $C^1$  codeword and return the value (in  $[0, 255]$ ) it encodes.

# Homework 4: due 1-28-15

- Complete H4B and H4C so that H4B is the inverse of H4A and H4C is the inverse of H3A c1code.txt.
- test4.c1 is the result of
  - `> java H4A < mystery.bmp > t`
  - `> java H3A c1code.txt < t > test4.c1`
- You may recover mystery.bmp using H4C and then H4B. Submit a report including your code and a jpg version of mystery.bmp.