

Blockchain & Bitcoin Network

CS 5158/6058 Data Security and Privacy

Spring 2018

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Trans. ID	Sender	Receiver	Amount	Time
t1	Alice	Bob	\$20	03/10/2018
t2	Alice	David	\$100	03/15/2018
t3	Bob	David	\$50	03/21/2018

- A bank has a number of transactions
- Bank wants to ensure all the trans are correct.
 - Trans could be changed by hacker on server
 - Trans could be changed by attacker on channel

Use Hash Function

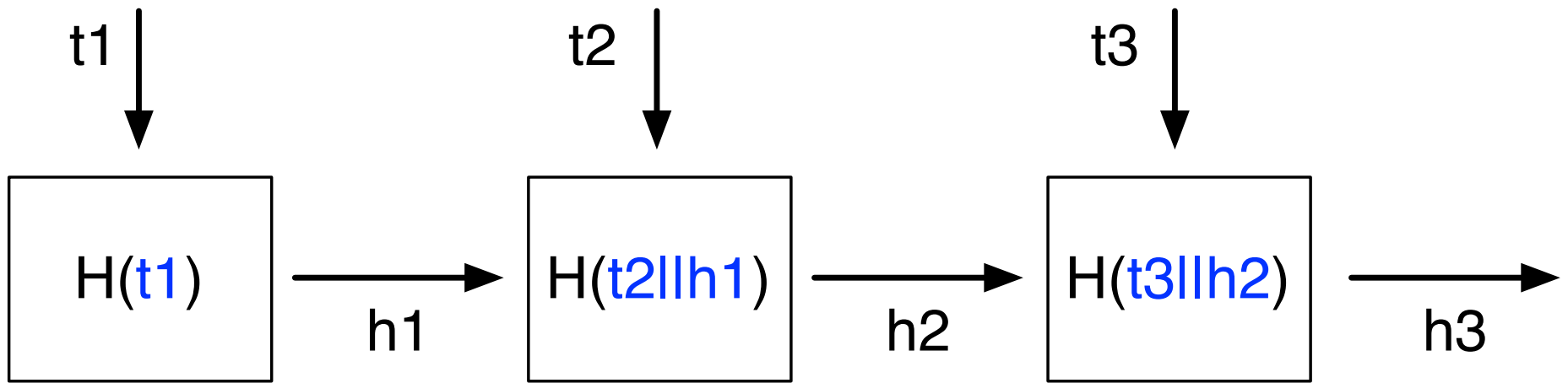
- Assume a bank has transactions: {t1, t2, t3}
 - Can use a hash function (e.g., SHA256)
 - Take all trans. as input, compute one hash value
 - E.g., $H(t1, t2, t3) = h$
- Bank publishes **h**, anyone can verify {t1, t2, t3}
 - Given {t1, t2, t3}, Alice checks $H(t1, t2, t3) \stackrel{?}{=} h$
 - If identical, all trans are correct;
 - otherwise, some trans is not correct

Trans. ID	Sender	Receiver	Amount	Time
t1	Alice	Bob	\$20	03/10/2018
t2	Alice	David	\$100	03/15/2018
t3	Bob	David	\$50	03/21/2018
t4	David	Alice	\$80	03/22/2018
t5	Charlie	David	\$10	03/23/2018

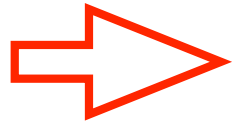
- Bank has new transactions every day
- Bank wants to ensure all the trans are correct.

Update Hash Value

- Bank has new transactions: {t1, t2, t3, t4, t5}
- Recompute/Update a hash value
 - Take all trans. as input, compute one hash value
 - E.g., $H(t1, t2, t3, t4, t5) = h$
 - Bank publishes **h**, anyone can verify all trans
- Inefficient: bank needs to take all the trans as input
 - E.g., reading 1,000,000 trans. takes long time

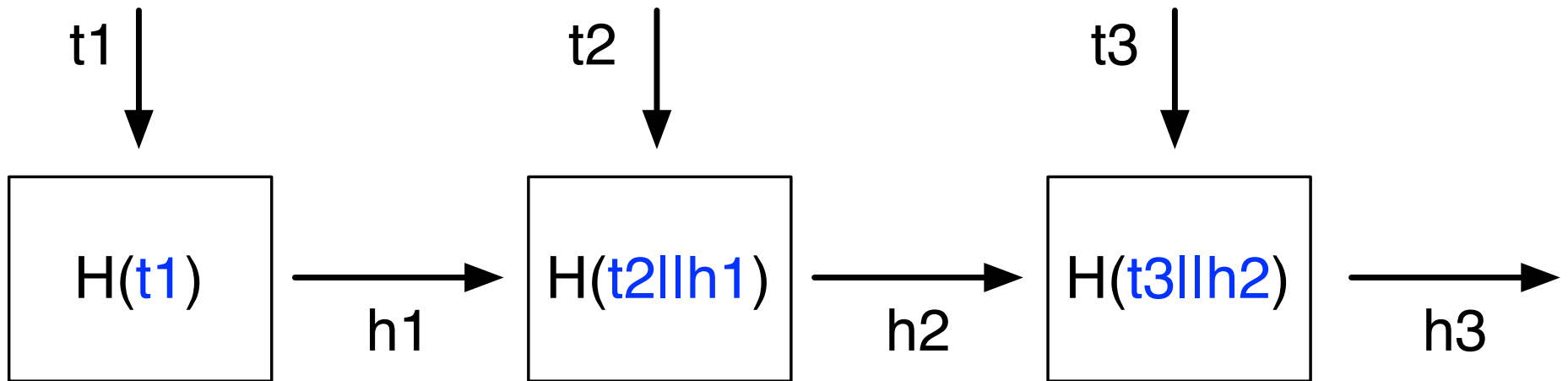


- Hash chain:
 - Given a new trans, bank computes a hash value of new trans with the current hash value
 - $h1$ can prove $\{t1\}$ is correct
 - $h2$ can prove $\{t1, t2\}$ are correct
 - $h3$ can prove $\{t1, t2, t3\}$ are correct
 - Bank always updates the latest hash value

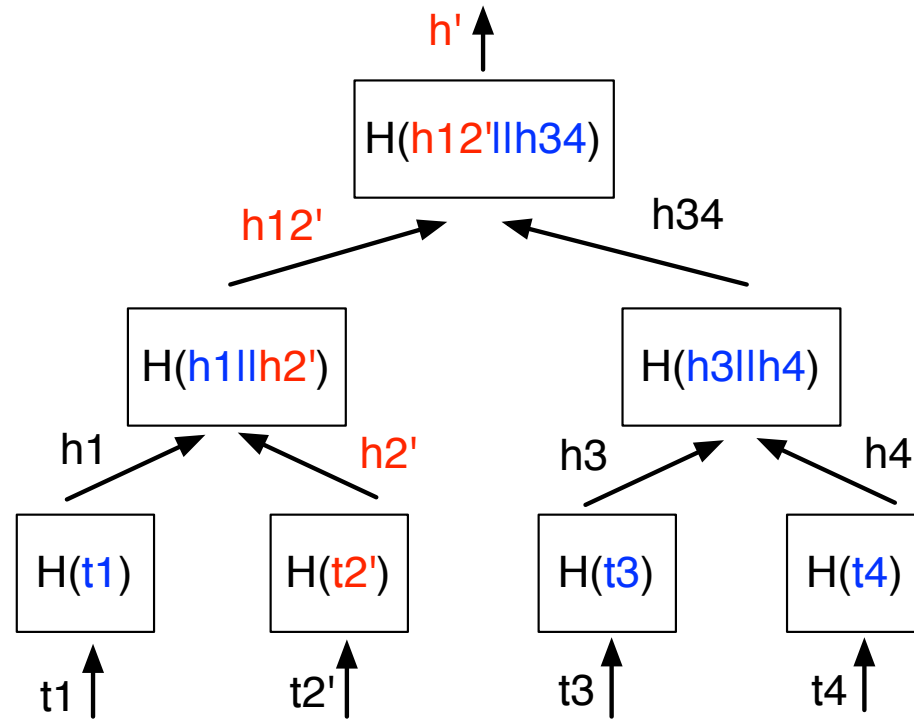


Trans. ID	Sender	Receiver	Amount	Time
t1	Alice	Bob	\$20	03/10/2018
t2	Alice	David	\$1000	03/15/2018
t3	Bob	David	\$50	03/21/2018
t4	David	Alice	\$80	03/22/2018
t5	Charlie	David	\$10	03/23/2018

- Bank has new transactions every day.
- Bank **updates** old transactions.
- Bank wants to ensure all the trans are correct.

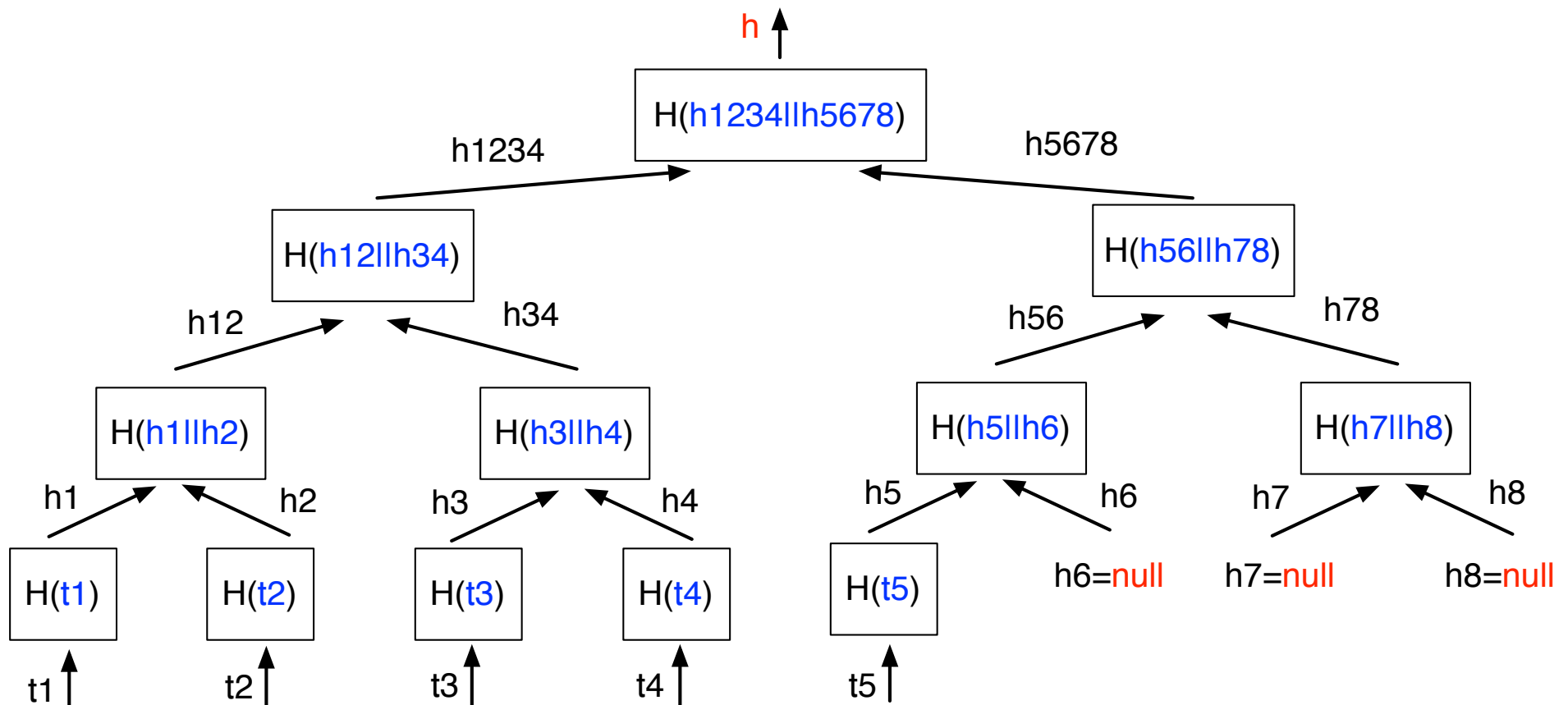


- Bank updates using Hash chain:
 - If $t3$ is updated to $t3'$
 - recompute $h3$, if still has a copy of $h2$; otherwise, recompute $h1, h2, h3$
 - If $t1$ is updated to $t1'$,
 - recompute $h1, h2, h3$
- Recompute $O(N)$ hashes, not very efficient
 - E.g., $N=1,000,000$

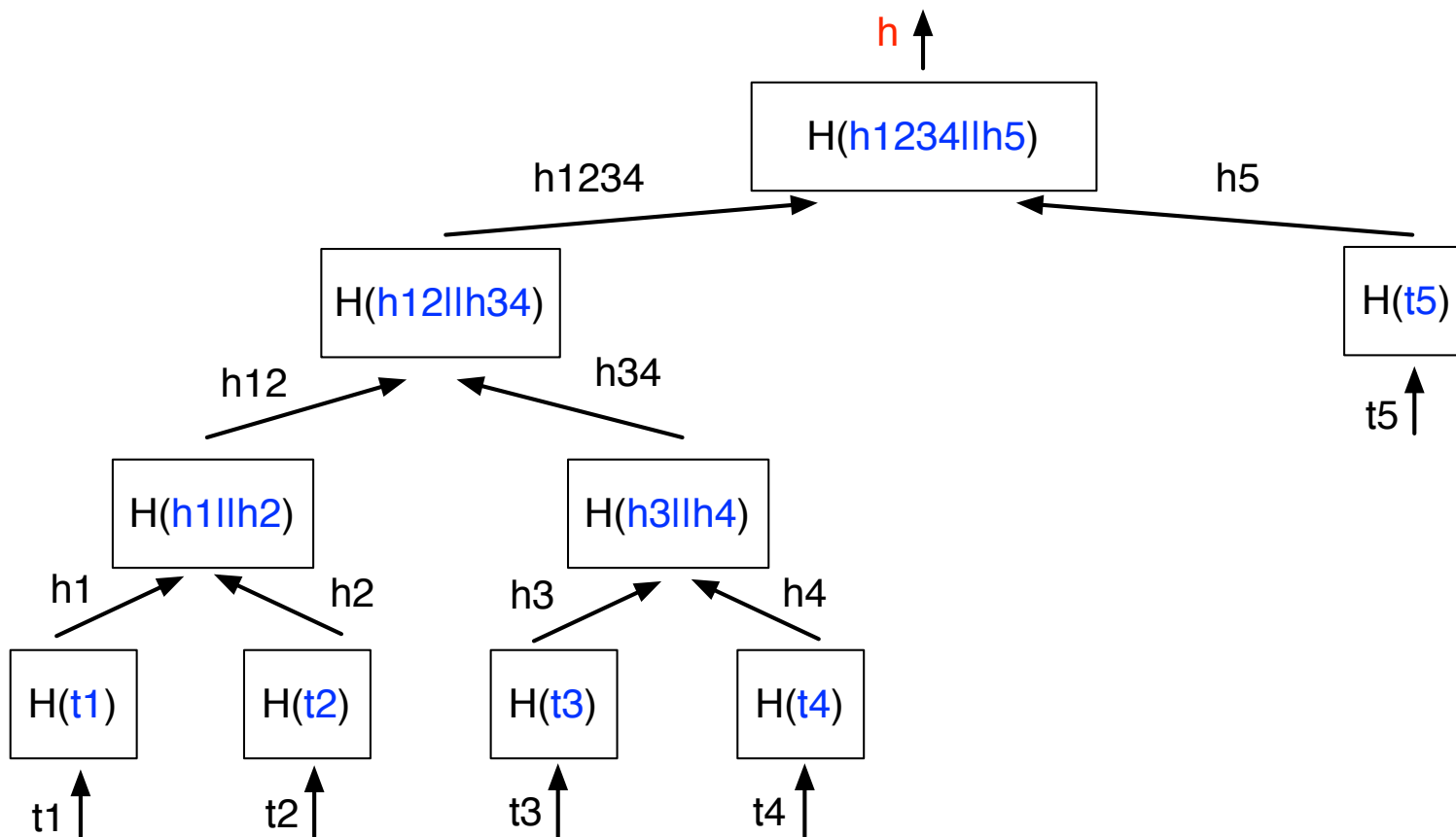


- Bank updates **t2 to t2'**
 - Recomputes h2', h12', h' in the tree
 - Assume bank maintains all the non-leaf nodes
 - $O(\log N)$ hashes v.s. $O(N)$ in hash chain
- Bank publishes **h'**, anyone can verify all trans

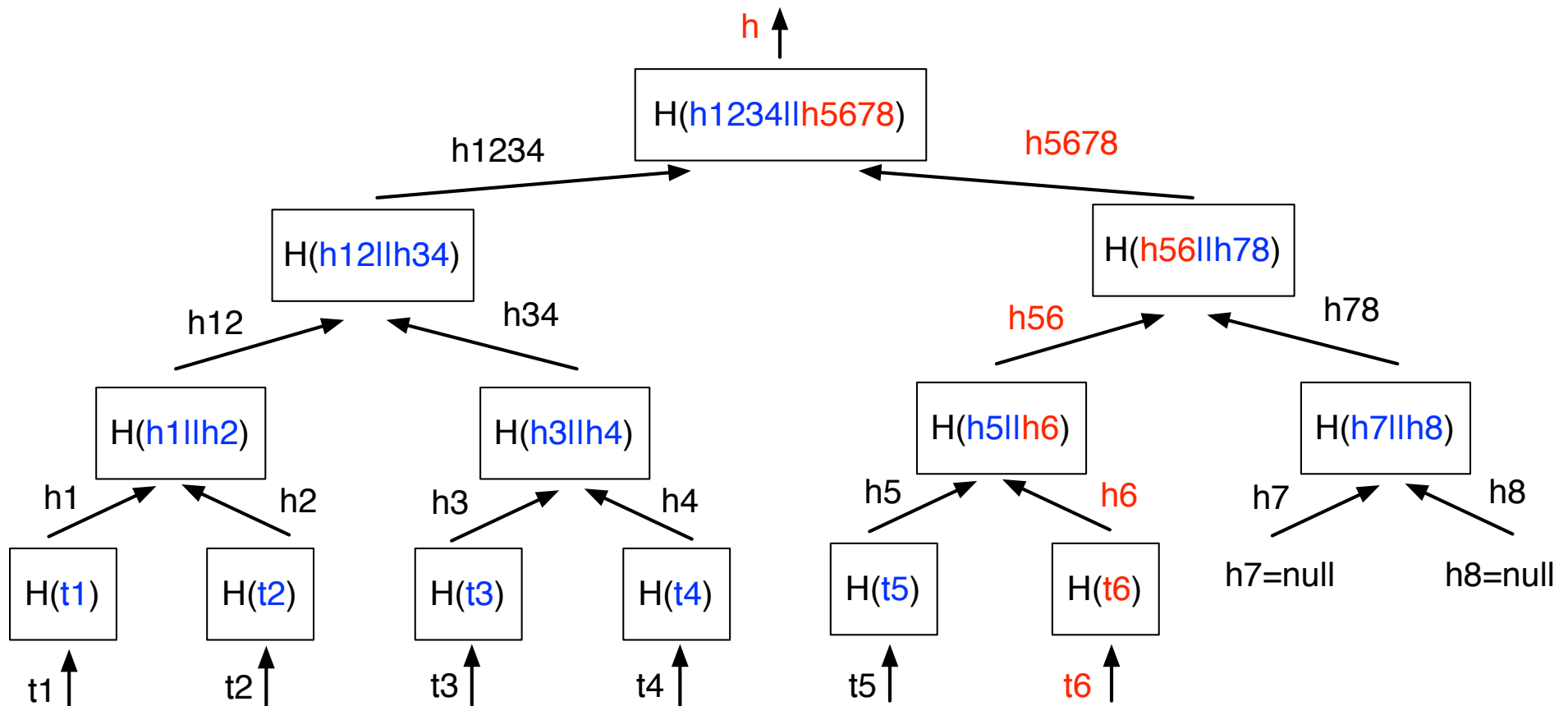
- Practice: if bank has 5 trans, {t1, t2, t3, t4, t5}
- How to compute the root hash?
- Leave h6, h7, h8 as **null** (easy to implement, all the leaf nodes are at the same level)



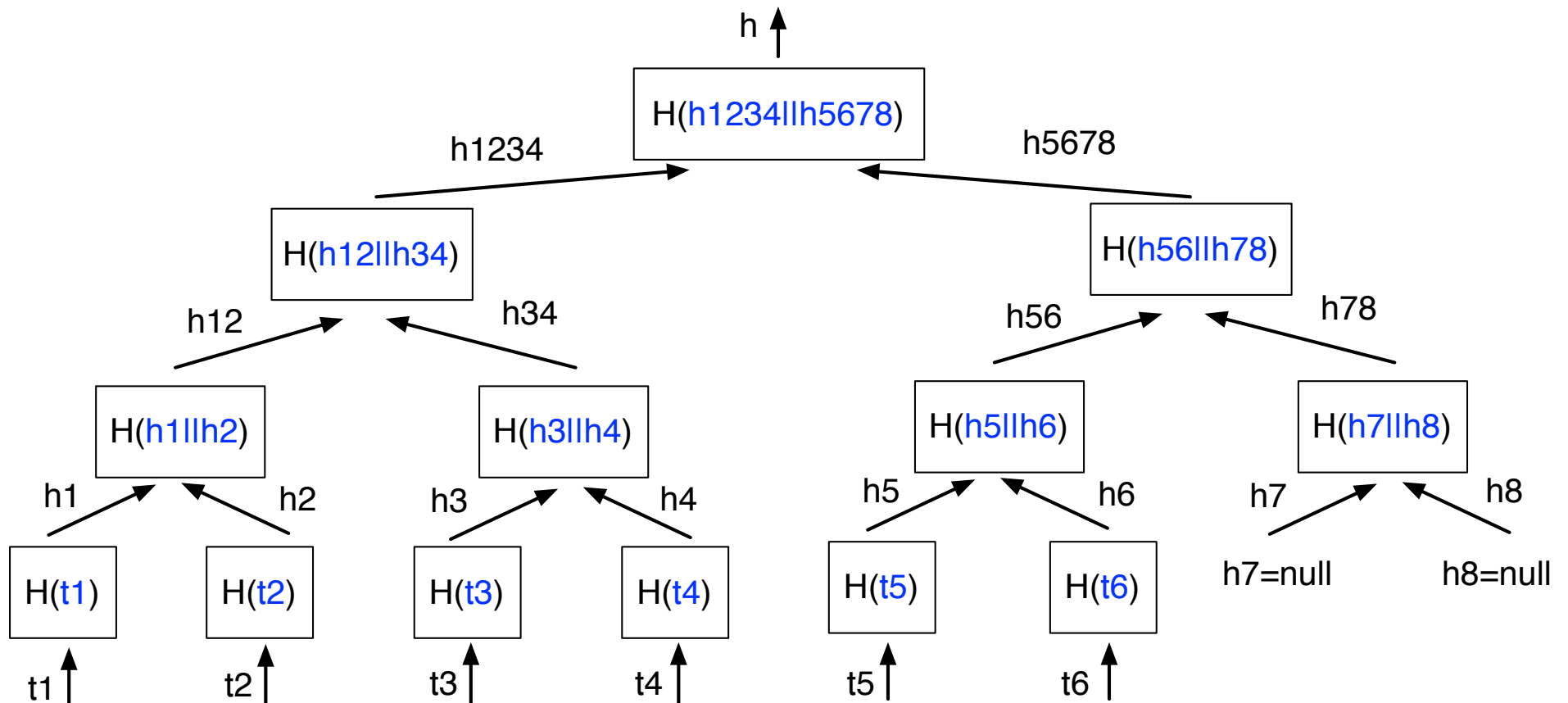
- Practice: if bank has 5 trans, $\{t1, t2, t3, t4, t5\}$
 - How to compute the root hash?
 - Another possible solution (also works, as long as verification algo. is consistent)



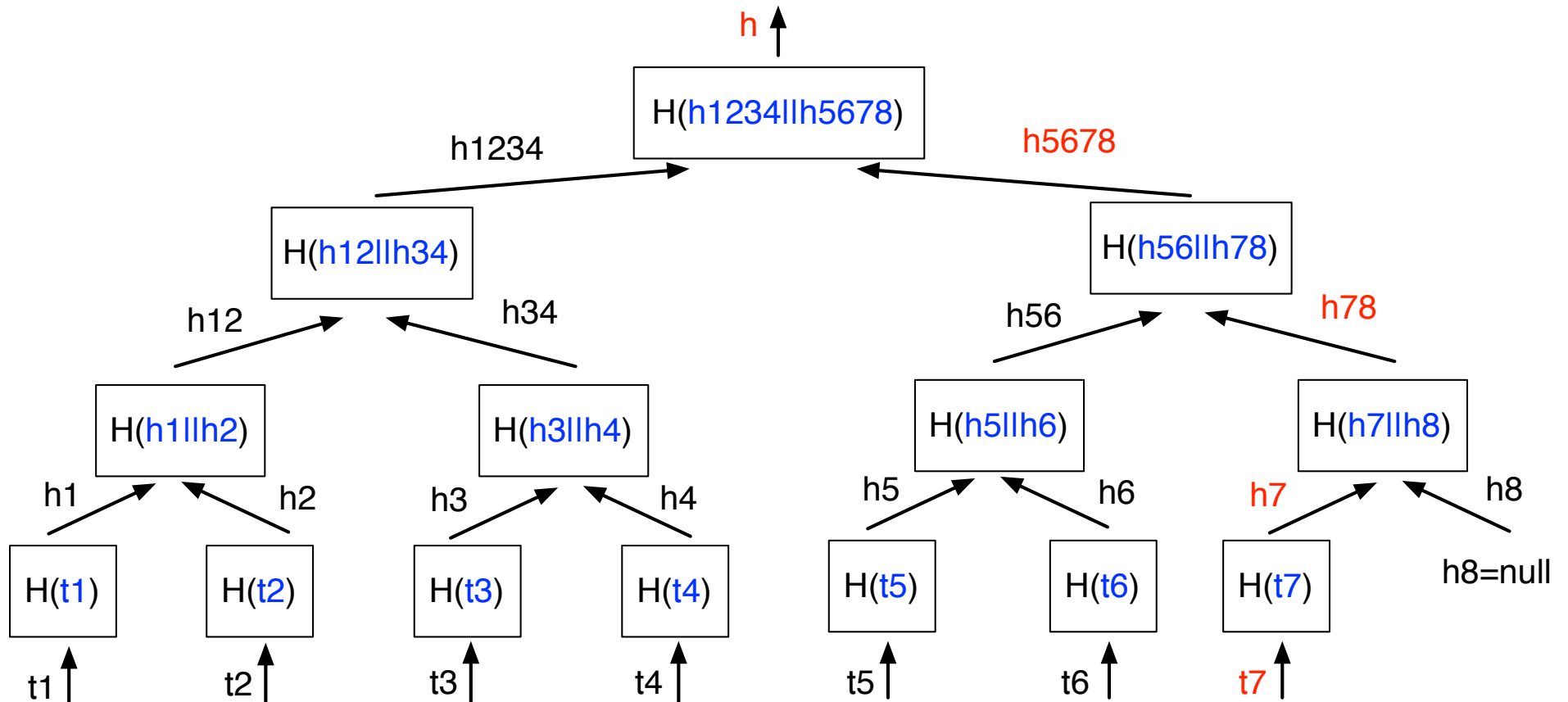
- Bank has 5 trans {t1, t2, t3, t4, t5}
- Bank has a new trans t6
- Bank needs to update h6, h56, h5678, h
- $O(\log N)$ v.s. $O(1)$ in hash chain

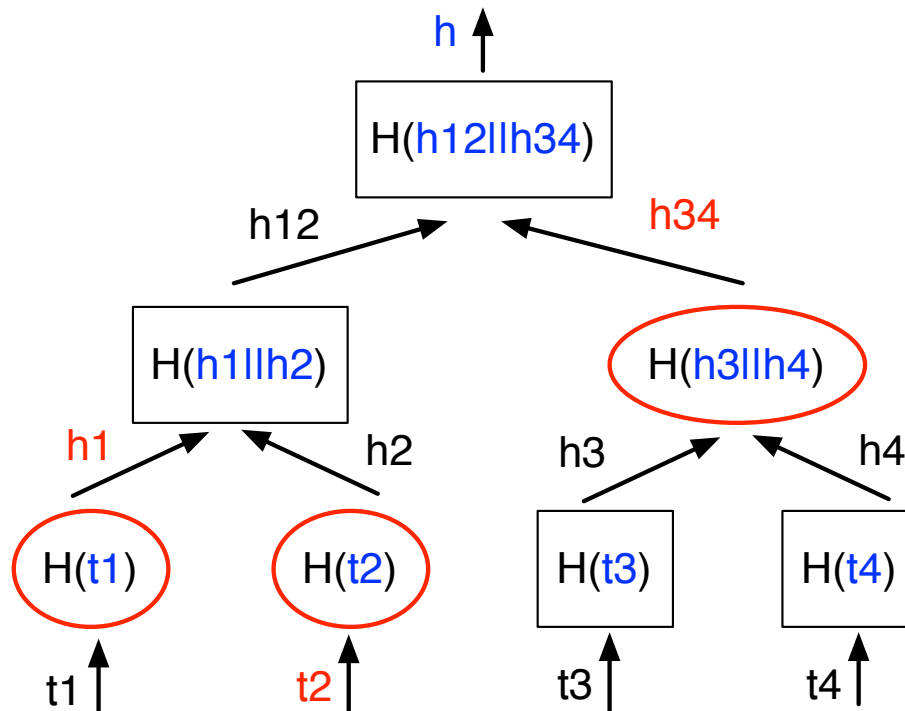


- Practice: Bank has 6 trans {t1, t2, t3, t4, t5, t6}
- Bank has a new trans **t7**
- Which hash values need to be recomputed?

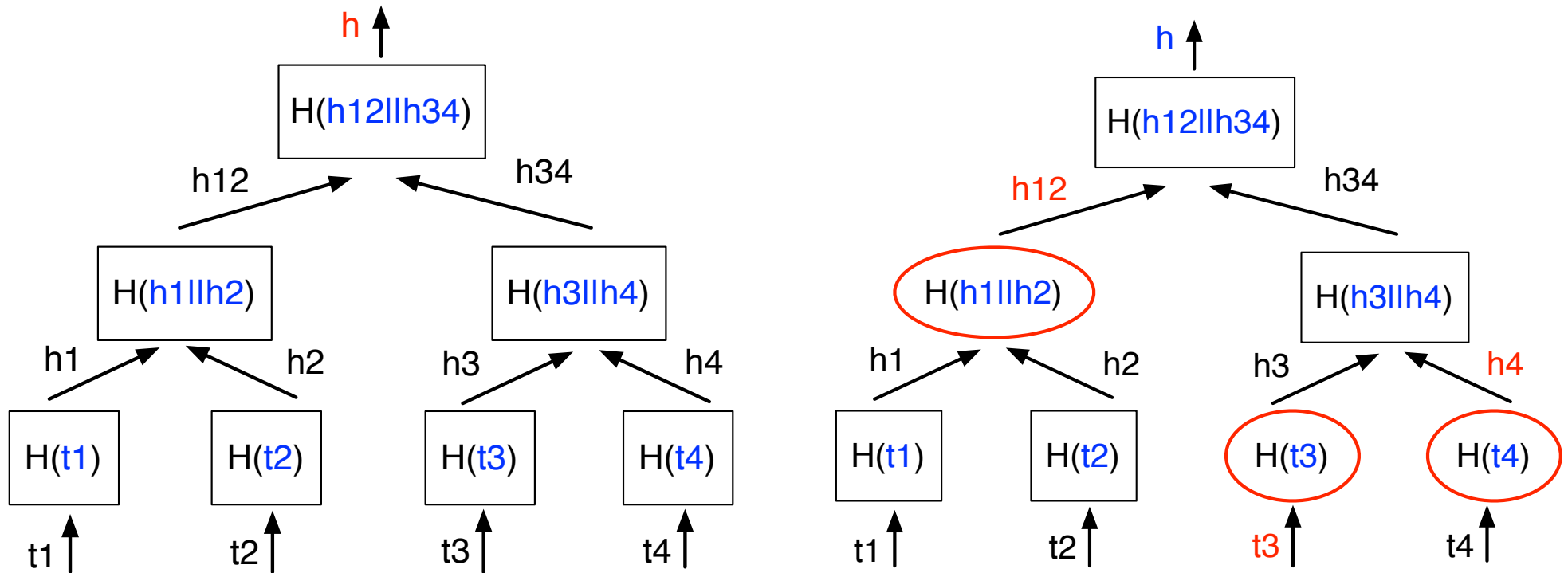


- Practice: Bank has 6 trans {t1, t2, t3, t4, t5, t6}
- Bank has a new trans **t7**
- Update **h7, h78, h5678, h**

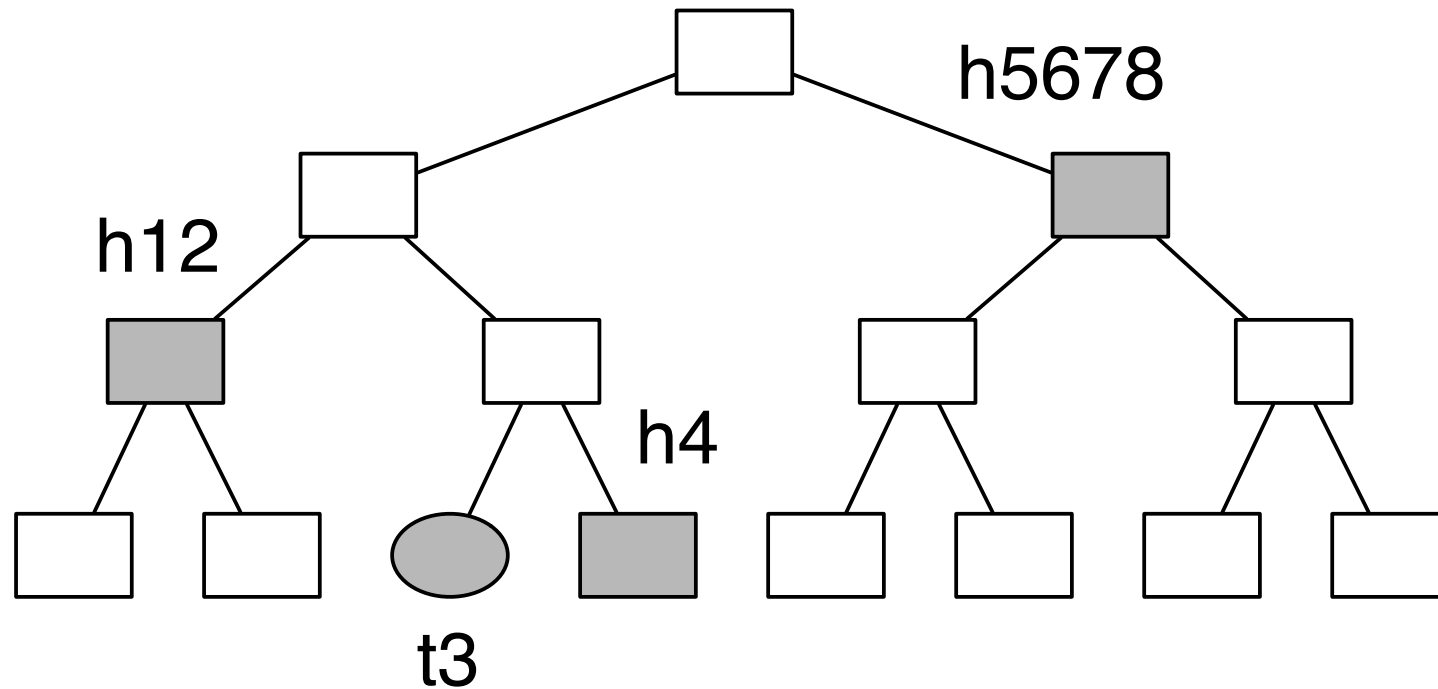




- Membership testing
- Alice wants to prove $t2$ is a member of all trans without knowing other trans.
- Alice gets $t2$, $h1$, $h34$ from bank, recompute h
 - 1 trans + 2 hashes, in total $O(\log N)$



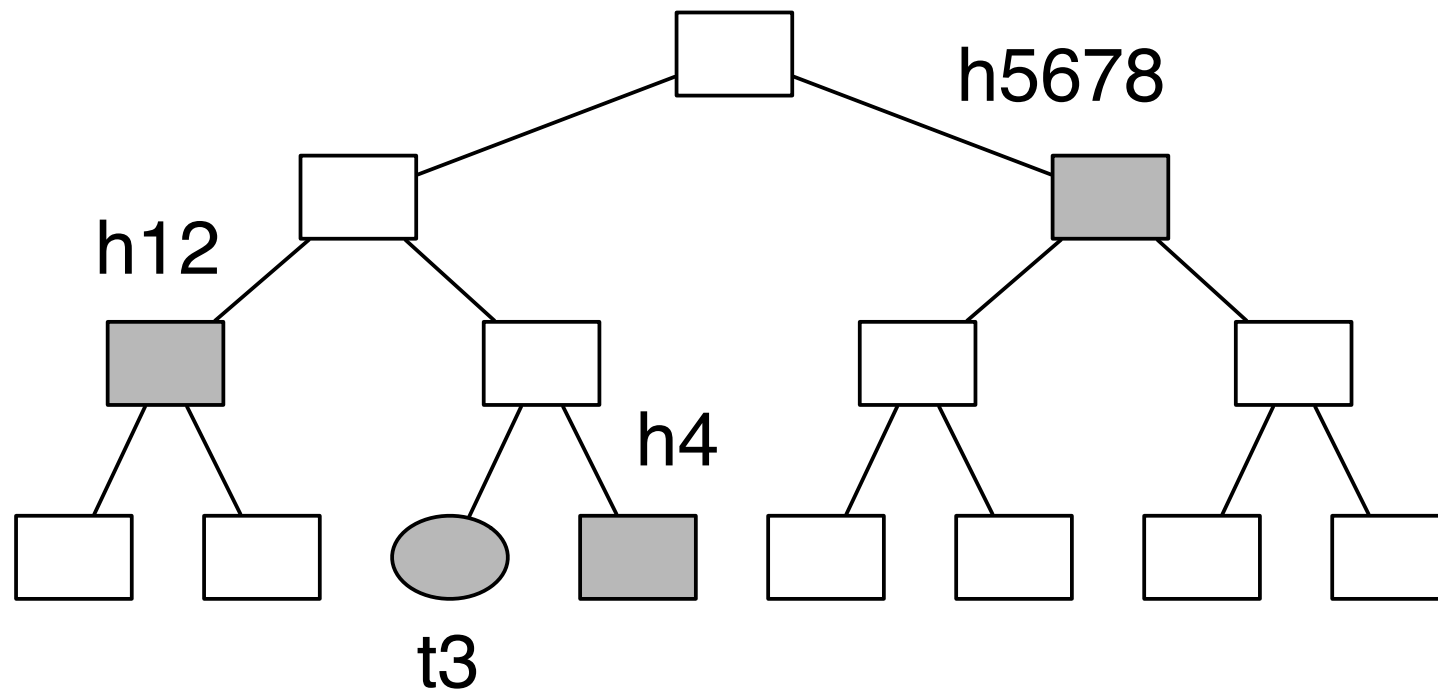
- Alice wants to prove t_3 is a member of all trans without knowing other trans.
- Practice: what information does Alice need?
- Alice gets t_3 , h_4 , h_{12} from bank, recompute h



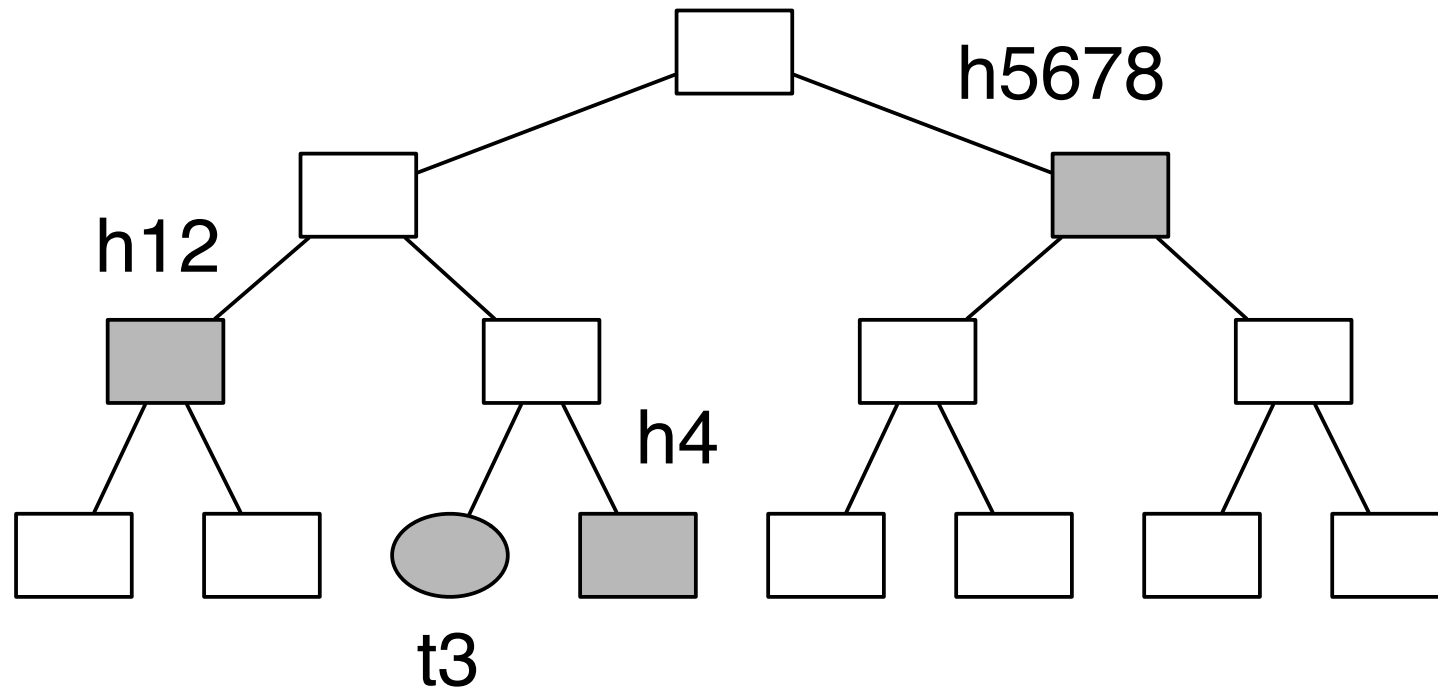
- Proving $t3$ is a member of all trans with Merkle tree
 - only need to get all the gray nodes $O(\log N)$
 - 1 trans + 3 hash values
- Hash chain needs to get all trans $O(N)$
 - need $t1, t2, t3, t4, t5, t6, t7, t8$
 - 8 trans

Comparison

	Hash Chain	Merkle Tree
Compute Proof	N hashes	$2N-1$ hashes
Size of Proof	1 hash value	1 hash value
Append	$O(1)$	$O(\log N)$
Update	$O(N)$	$O(\log N)$
Proof of Membership	$O(N)$	$O(\log N)$



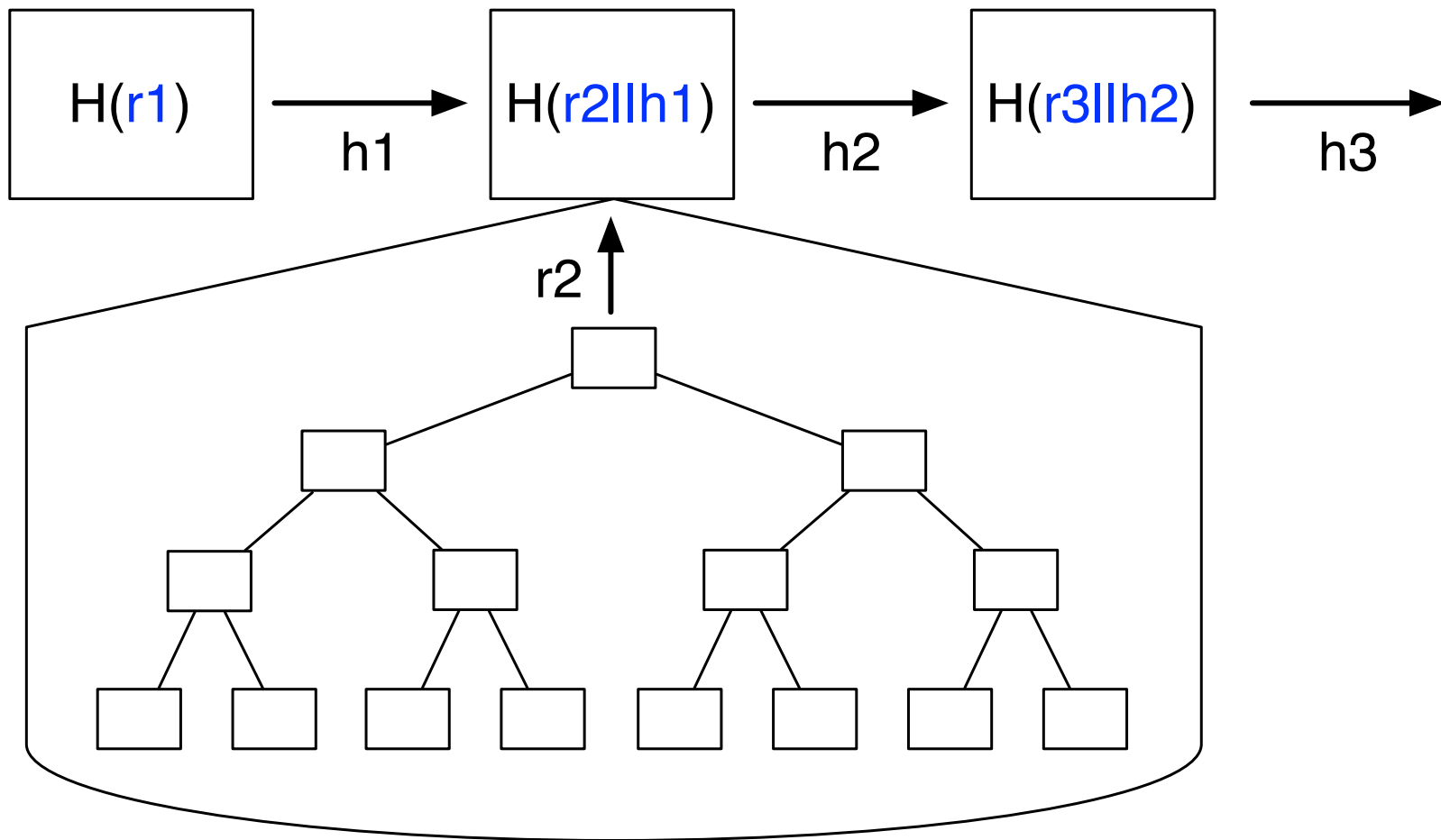
- Use Merkle tree in P2P networks, e.g., BitTorrent
 - Alice downloads **t3**, a piece of movie
 - Alice needs to check whether this **t3** is correct while other pieces have not been downloaded
 - Alice retrieves all the hashes of gray nodes
 - Alice computes root hash **h'**, compare with **h**



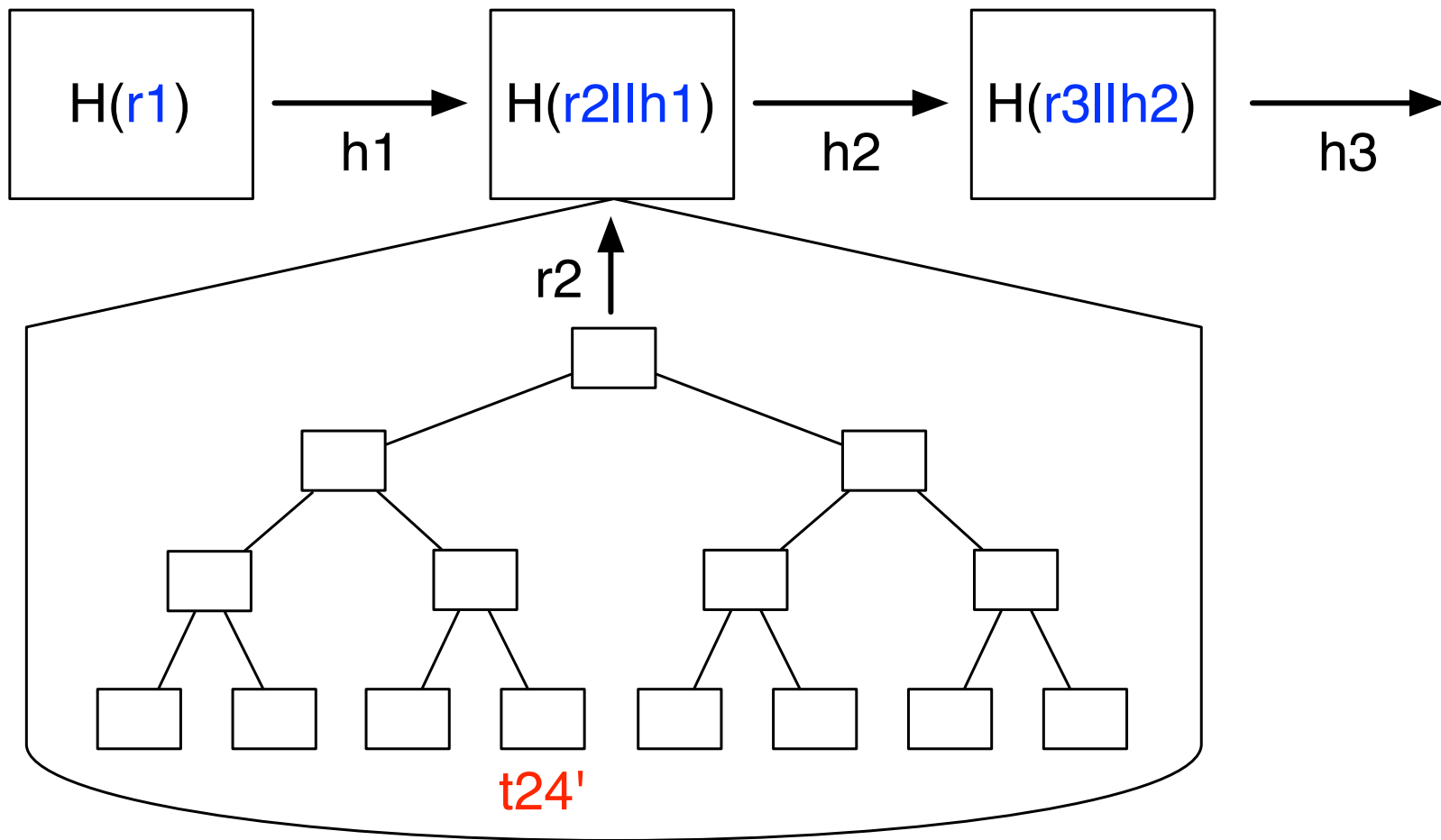
- Without using Merkle tree
 - Alice needs to wait the entire movie is downloaded (e.g., several hours later)
 - Waste bandwidth if the movie data (e.g., a small piece of the entire data) is not correct.

The Blockchain

- Bitcoin network has a large number of transactions.
 - About 196,000 trans per day
 - Bitcoin uses the blockchain to maintain integrity
- Blockchain includes [Hash chain + Merkle tree](#)
 - Each block has 1MB limit (1000~2000 trans)
 - Trans in one block form one Merkle tree
 - All the root hash values form a hash chain
 - Total blocks: 512,169 (as of 3/5/2018)



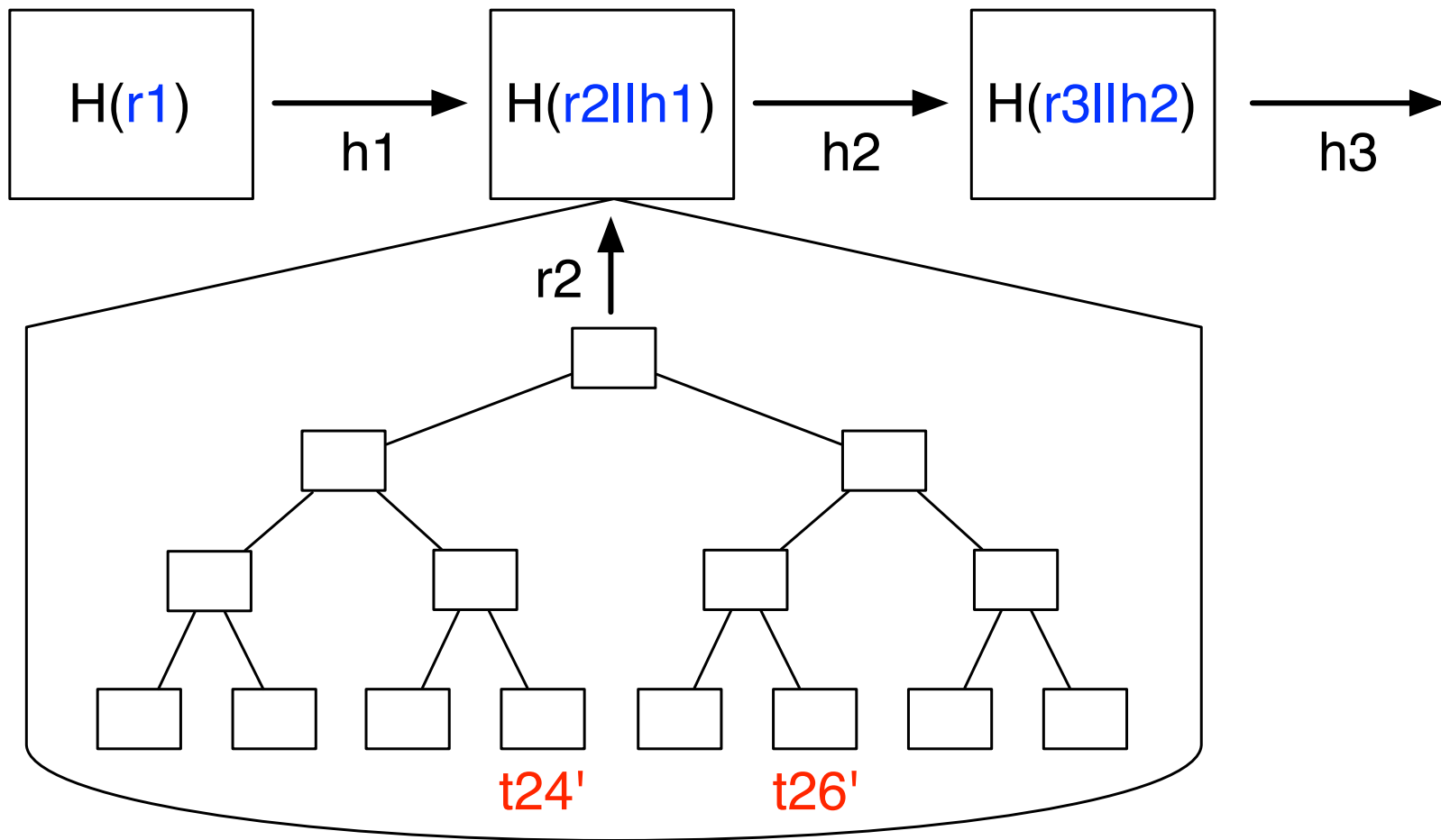
- Example: Assume each block has 8 transactions
 - 3 blocks, 24 transactions in total
 - Hash value **h3** proves all the 24 transactions



- Attacker wants to change 1 trans. ($t24$ to $t24'$)
 - Needs to find a collision s.t. $H(t24) == H(t24')$
 - Happens with a negligible probability

Changes in Blockchain

- t24: Alice pays 2 bitcoins to Bob
- There is a later trans related to t24
 - t26: Bob pays (the) 2 bitcoins to Charlie
 - t26 also includes info of t24
- Attacker changes t24 to t24'
- Attacker also needs to change t26 to t26'



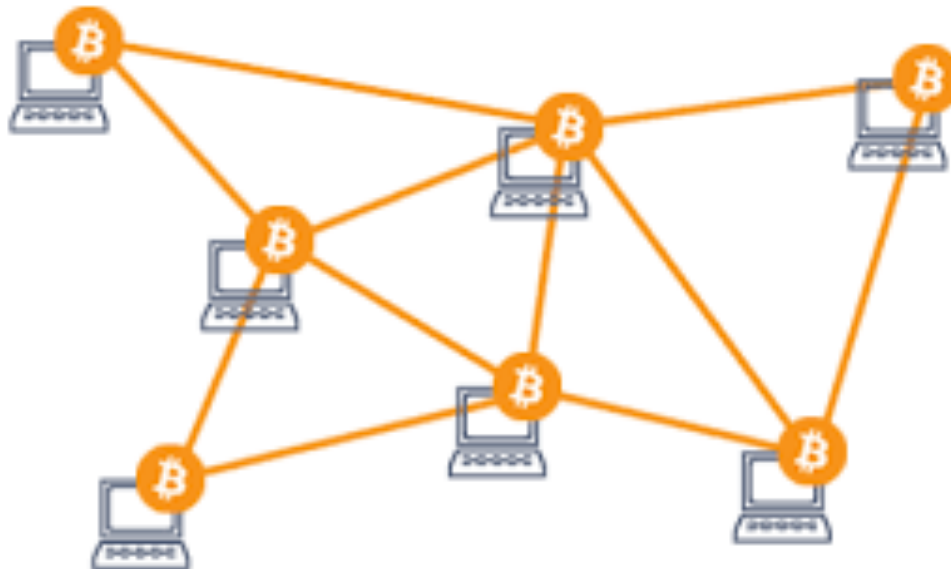
- Attacker wants to change 1 trans. ($t24$ to $t24'$)
 - $t26$ is associated with $t24$, needs to be changed
 - Needs to find 2 collisions s.t.
 - $H(t24) == H(t24')$ AND $H(t26) == H(t26')$

Changes in Blockchain

- Attacker changes t_{24} to t'_{24}
 - If there are $n-1$ later trans associated with t_{24}
 - Assume the prob. of finding a collision is p
 - p is negligible
 - Total prob. of success: p^n
 - A trans is more secure if it is older.
- Blockchain can be used distributed scenario
 - E.g., Supply chain, Internet of Things

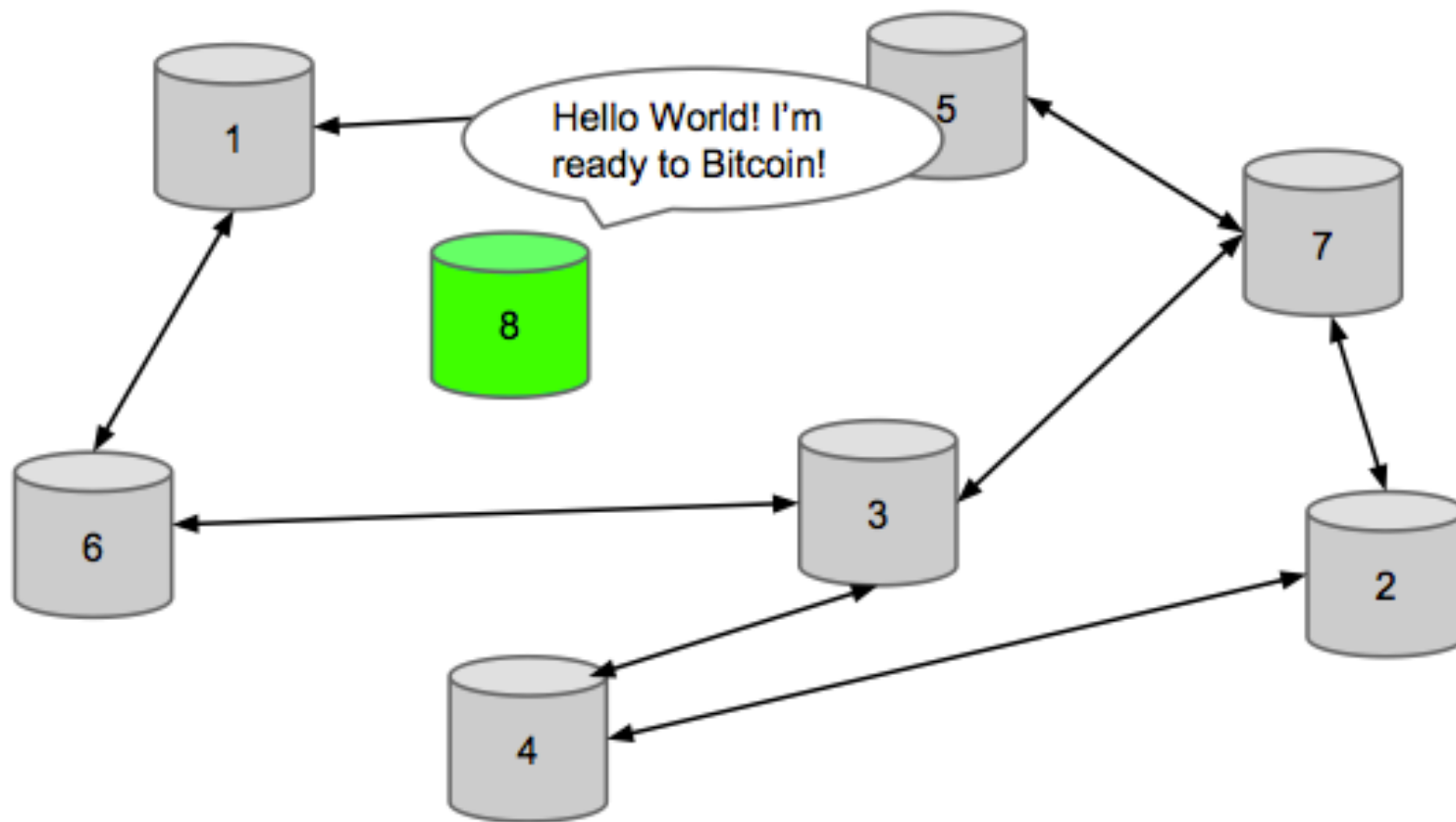
Bitcoin Network

- Bitcoin network is a [peer-to-peer](#) network
 - No central authority
 - All nodes are equal
 - Forget non-responding nodes after 3 hrs



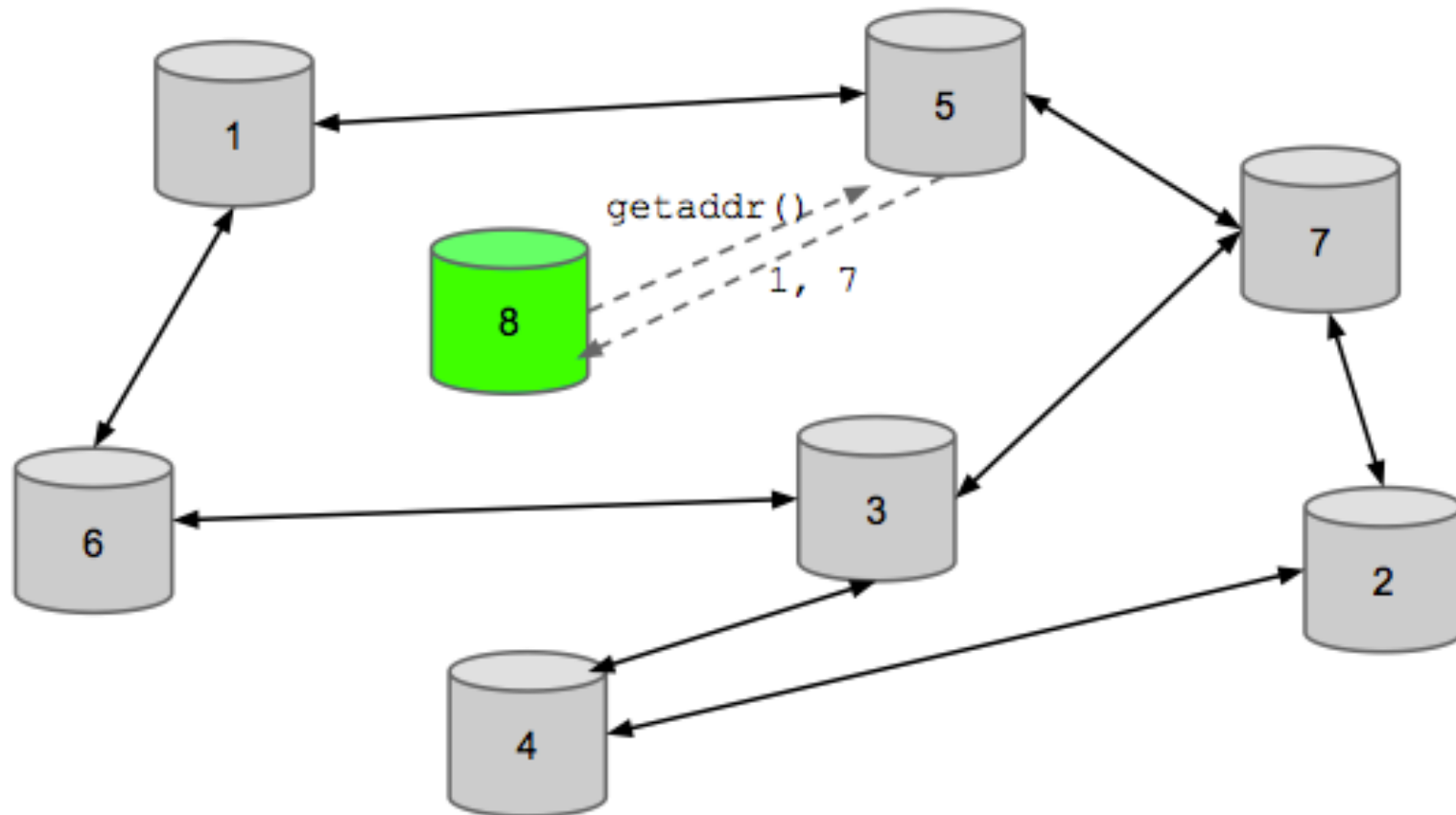
Join Bitcoin Network

- Can join anytime



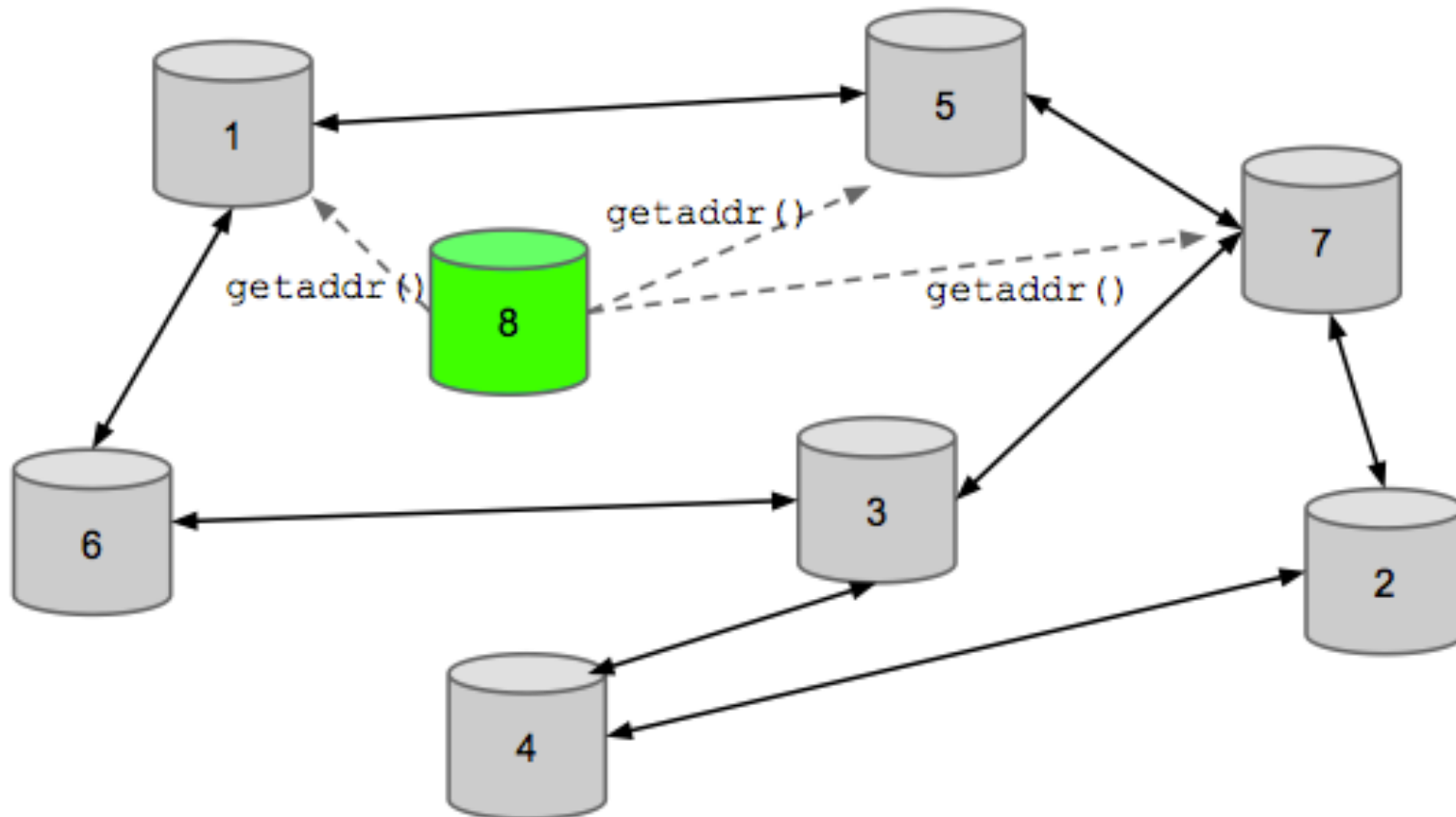
Join Bitcoin Network

- Find one node, and get its neighbors



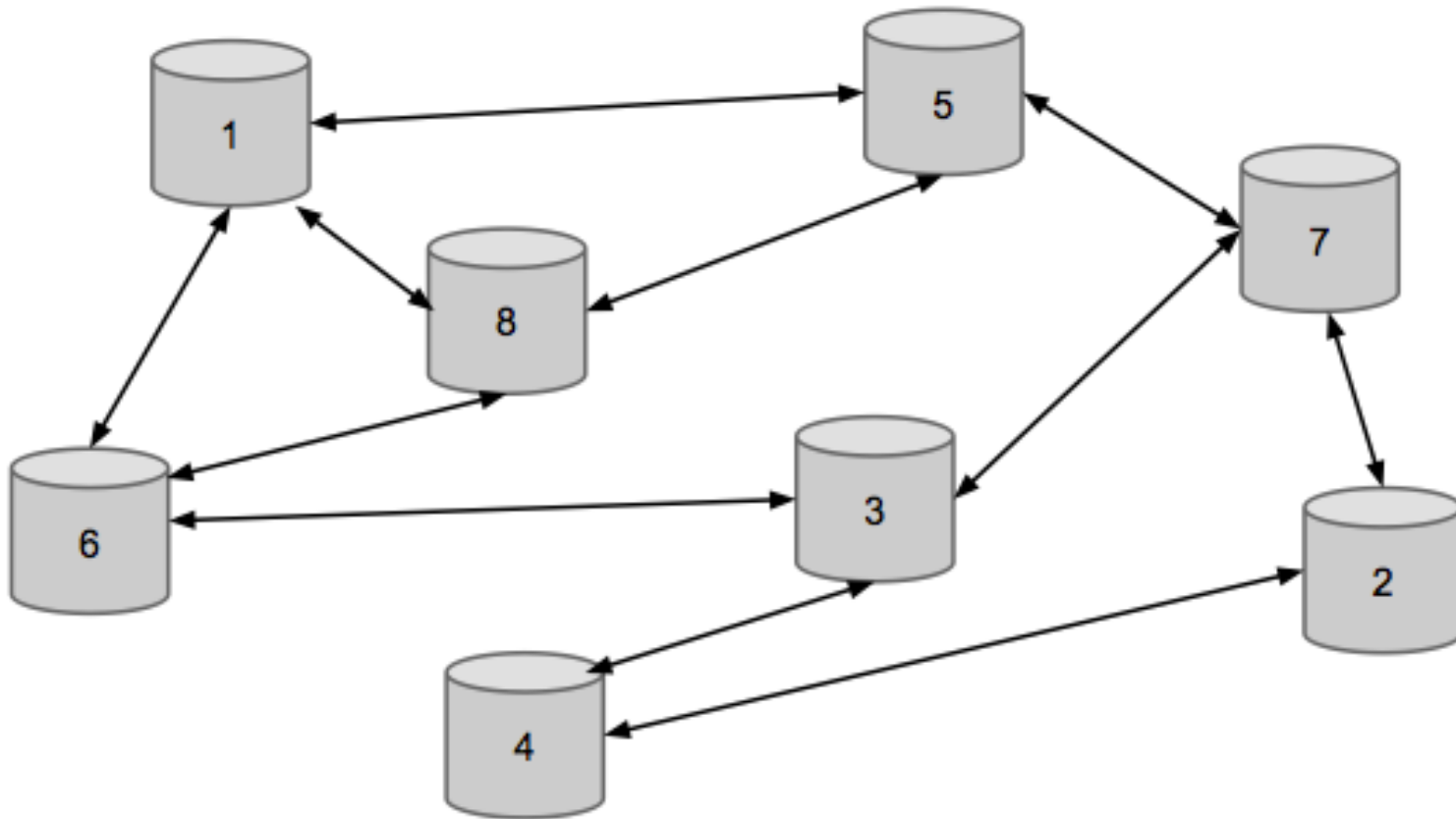
Join Bitcoin Network

- Based on neighbors, find neighbors' neighbors



Join Bitcoin Network

- Connect to nodes (some response, some not)



Join Bitcoin Network

- Two types of nodes
 - Bitcoin users (use Bitcoins)
 - Miners (use & generate Bitcoins)
- Each node has a **public key** and a **private key**
- Use hash value of public key as account number (e.g., routing number on your check)
 - SHA256: $H(pk)$, then convert to base56

1BvBMSEYstWetqTFn5Au4m4GFg7xJaNVN2

1JBonneauruSSoYm6rH7XFZc6Hcy98zRZz

Bitcoin Transaction

- Alice has 25 bitcoins
 - Transaction: Alice pays Bob 17 bitcoins
 - Alice signs this trans with her private key
 - Others can verify this trans with Alice's public key
- Transactions are [coin-based](#)
 - 1 trans destroys old “coins” and create new ones
 - E.g., Alice destroys its old coin with 25 bitcoins, create a new coin with 17 bitcoins for Bob, and create a new coin with 8 bitcoins for herself

Bitcoin Transaction

- Transactions are coin-based
 - E.g., coin #1 \rightarrow coin #2 & coin #3

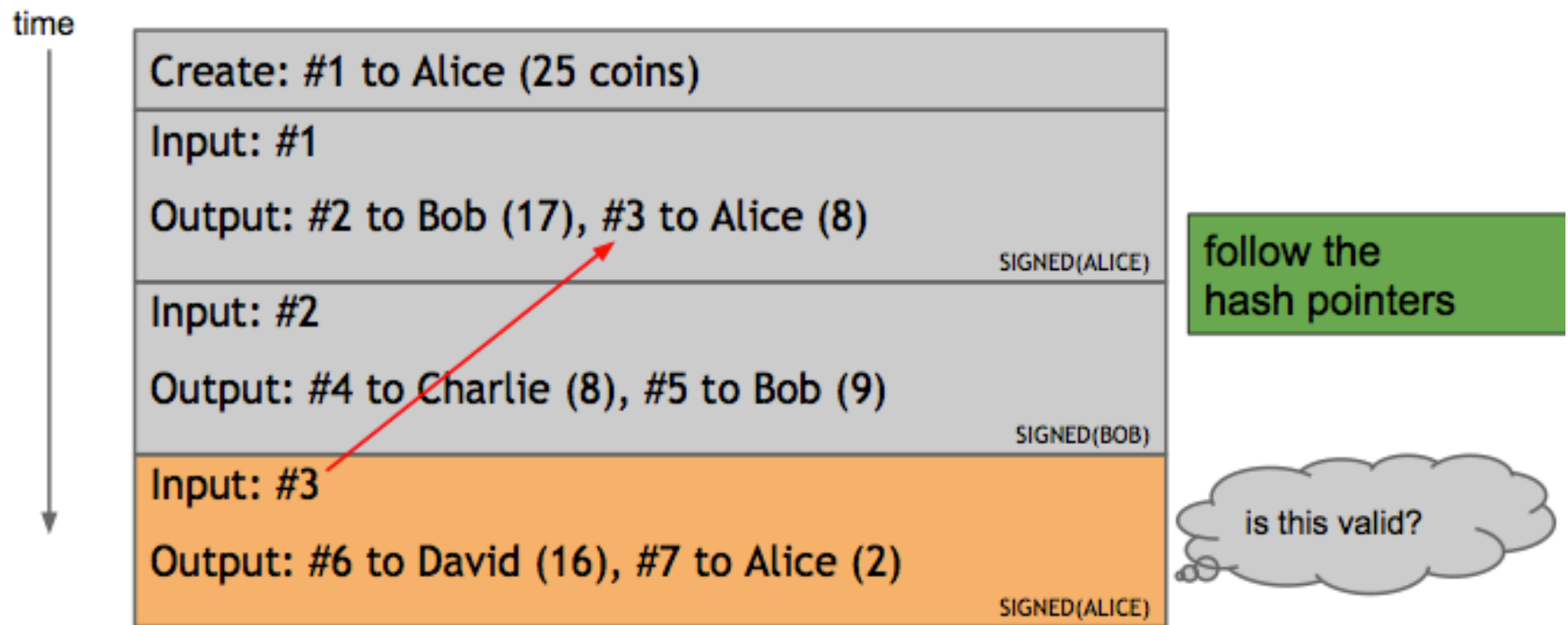
time

Create: #1 to Alice (25 coins)
Input: #1 Output: #2 to Bob (17), #3 to Alice (8) SIGNED(ALICE)
Input: #2 Output: #4 to Charlie (8), #5 to Bob (9) SIGNED(BOB)
Input: #3 Output: #6 to David (16), #7 to Alice (2) SIGNED(ALICE)

#6 to David (6)

Bitcoin Transaction

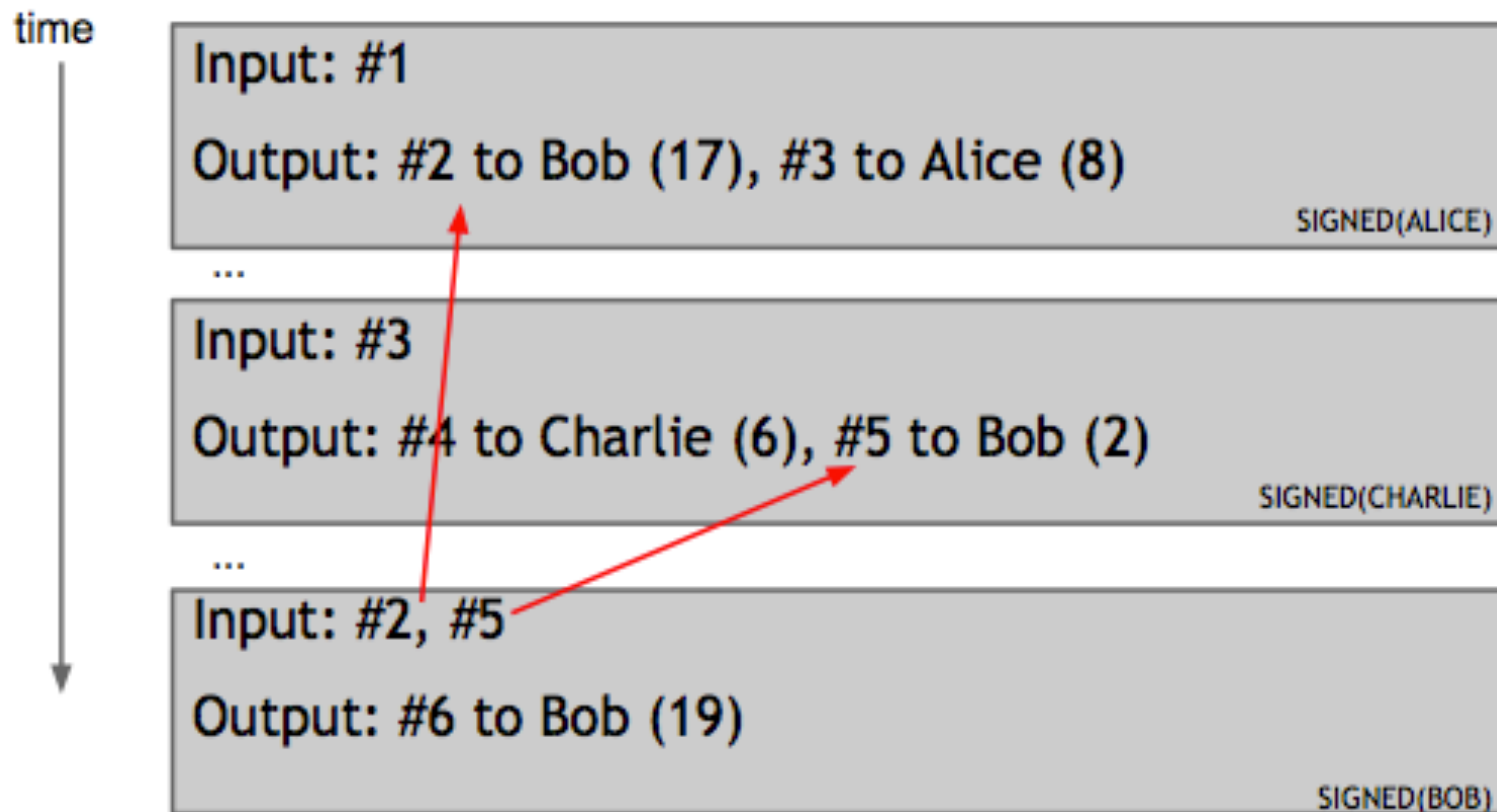
- A coin is related to its previous coin
 - E.g., Check coin #3 needs to check coin #1



#6 to David (6)

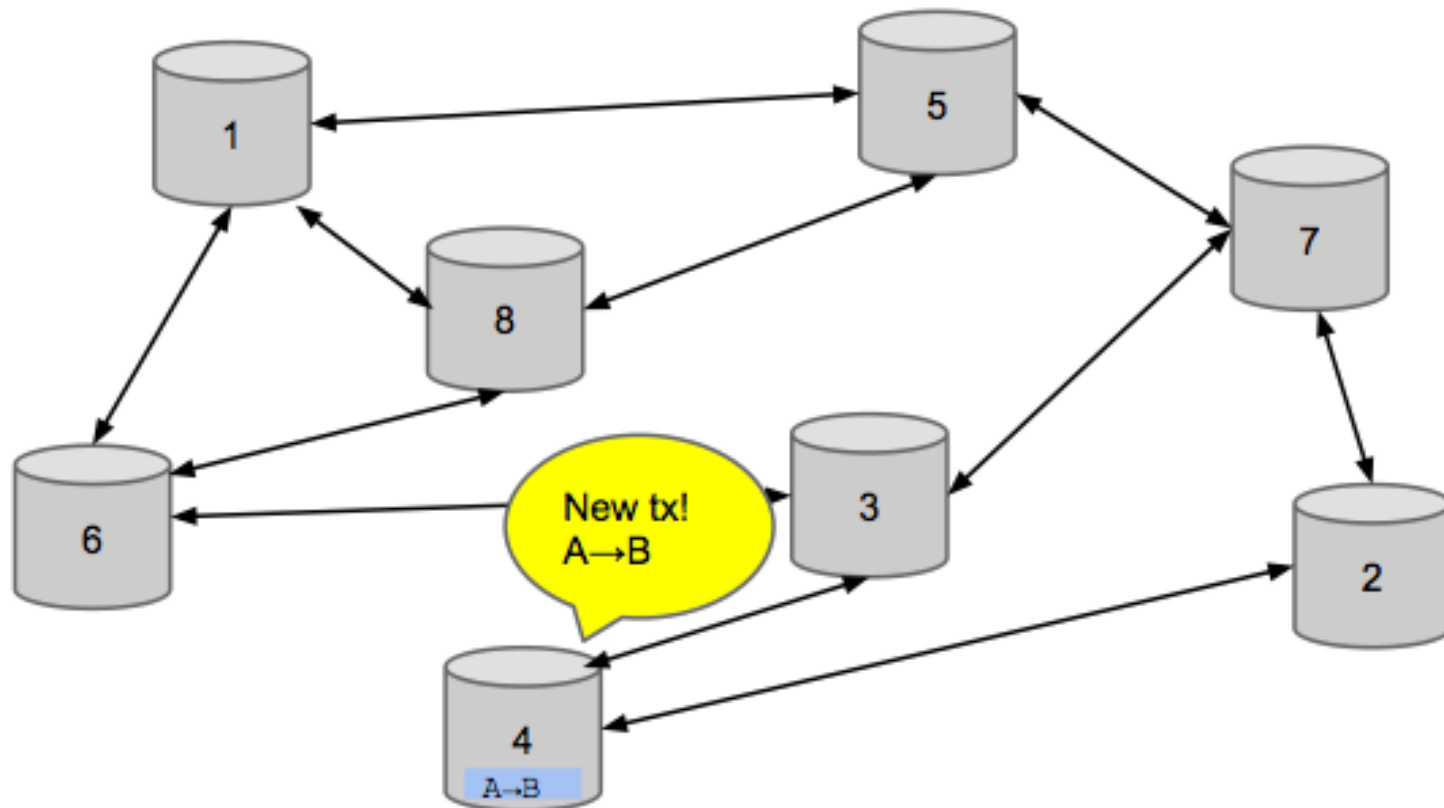
Bitcoin Transaction

- Bob can merge two coins into 1 coin
 - E.g., coin #2 and coin #5 \longrightarrow coin #6



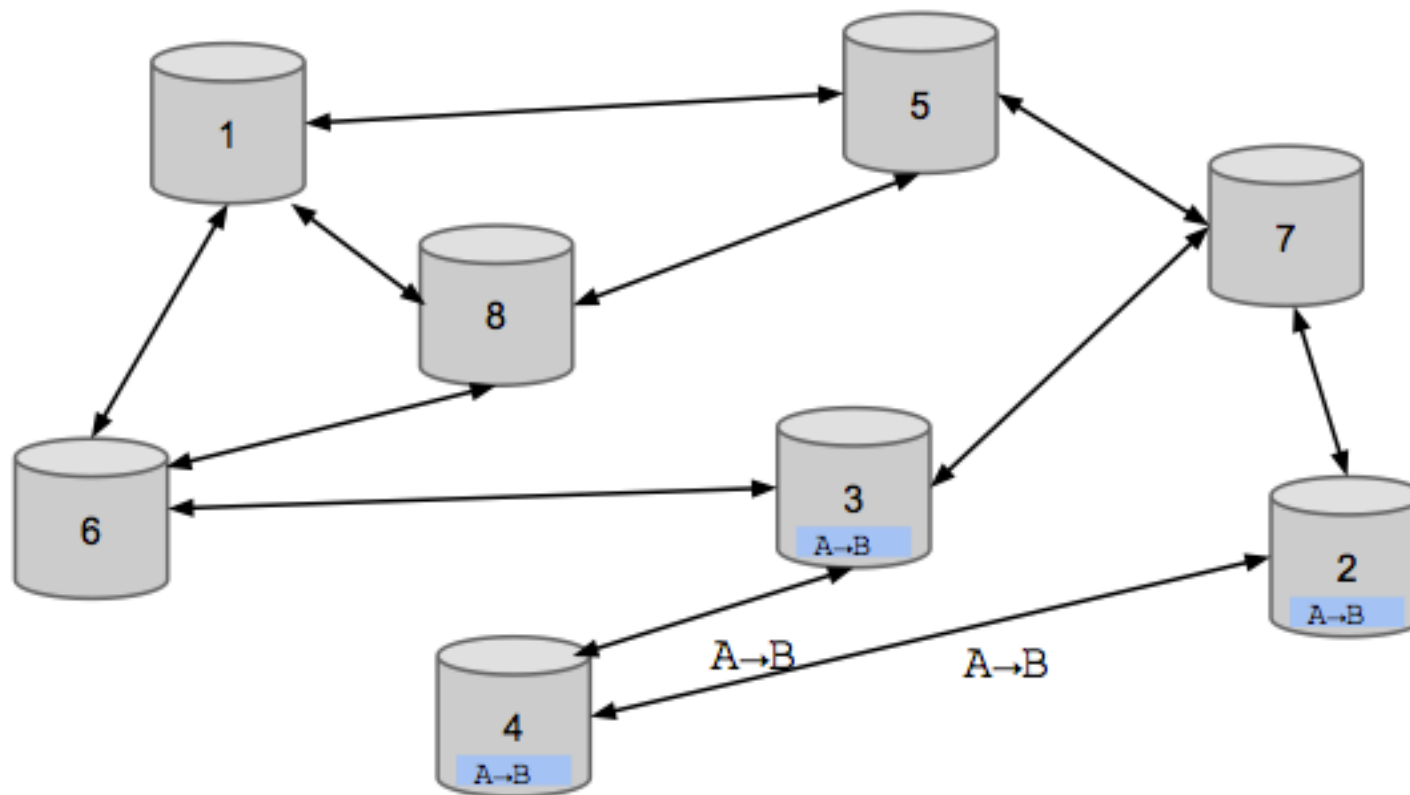
Transaction Propagation

- Each trans will be propagated to (almost) the entire network



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