Gitcon

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	4.33.3.1 app_main()

Chapter 1

Data Structure Index

1.1 Data Structures

Here are the data structures with brief descriptions:

2 Data Structure Index

Chapter 2

File Index

2.1 File List

Here is a list of all files with brief descriptions:

include/config.h
Gitcon Driver Configuration and Pin-Out File and dependencies
include/processed-data.h
lib/audio/i2s_sampler.c
I2S Sampler Driver Source for ESP32
lib/audio/i2s_sampler.h
I2S Sampler Driver for ESP32
lib/fft/fft.c
lib/fft/fft.h
lib/mcp3201/mcp3201.c
lib/mcp3201/mcp3201.h
lib/mcp3201/mcp3201_sampler.c
MCP3201 Sampler
lib/midi/midi.c
MIDI UART Driver Source for ESP32
lib/midi/midi.h
MIDI UART Driver for ESP32
lib/midi_utils.c
MIDI Message Utilities
src/gitcon.c
Gitcon Driver Source
src/gitcon.h
Gitcon Driver Header
src/main.c
Main File for Gitcon Project
test/test_fft/test_fft.c
Unit Test for FFT
test/test_midi/test_midi.c
Unit Tests for MIDI Driver

File Index

Chapter 3

Data Structure Documentation

3.1 fft_config_t Struct Reference

```
#include <fft.h>
```

Data Fields

- int size
- float * input
- float * output
- float * twiddle_factors
- fft_type_t type
- fft_direction_t direction
- unsigned int flags

3.1.1 Detailed Description

Definition at line 43 of file fft.h.

3.1.2 Field Documentation

3.1.2.1 direction

fft_direction_t direction

Definition at line 50 of file fft.h.

3.1.2.2 flags

unsigned int flags

Definition at line 51 of file fft.h.

3.1.2.3 input

float* input

Definition at line 46 of file fft.h.

3.1.2.4 output

float* output

Definition at line 47 of file fft.h.

3.1.2.5 size

int size

Definition at line 45 of file fft.h.

3.1.2.6 twiddle_factors

float* twiddle_factors

Definition at line 48 of file fft.h.

3.1.2.7 type

fft_type_t type

Definition at line 49 of file fft.h.

The documentation for this struct was generated from the following file:

• lib/fft/fft.h

3.2 gitcon_context_t Struct Reference

Gitcon Configuration.

#include <gitcon.h>

Data Fields

- i2s_sampler_t * sampler
- midi_handle_t midi_handle
- QueueHandle_t midi_queue

3.2.1 Detailed Description

Gitcon Configuration.

Parameters

sampler	Sampler Handler (MCP3201 or I2S)
midi_handle	MIDI Driver Context (MIDI over UART)
midi_queue	MIDI Queue Handler

Definition at line 25 of file gitcon.h.

3.2.2 Field Documentation

3.2.2.1 midi_handle

midi_handle_t midi_handle

Definition at line 32 of file gitcon.h.

3.2.2.2 midi_queue

QueueHandle_t midi_queue

Definition at line 33 of file gitcon.h.

3.2.2.3 sampler

```
i2s_sampler_t* sampler
```

Definition at line 30 of file gitcon.h.

The documentation for this struct was generated from the following file:

• src/gitcon.h

3.3 i2s_sampler_t Struct Reference

Sampler Configuration.

```
#include <i2s_sampler.h>
```

Data Fields

- QueueHandle_t dma_queue
- QueueHandle_t dsp_queue
- size t * buffer
- size_t buffer_pos
- size_t buffer_size

3.3.1 Detailed Description

Sampler Configuration.

Parameters

dma_queue	Samples are sent to this queue by the DMA
dsp_queue	Sampling result is sent to this queue
buffer	Buffer to store samples in
buffer_pos	Current position in buffer
buffer_size	Size of the buffer in samples

Definition at line 30 of file i2s_sampler.h.

3.3.2 Field Documentation

3.3.2.1 buffer

size_t* buffer

Definition at line 34 of file i2s_sampler.h.

3.3.2.2 buffer_pos

```
size_t buffer_pos
```

Definition at line 35 of file i2s_sampler.h.

3.3.2.3 buffer_size

```
size_t buffer_size
```

Definition at line 36 of file i2s_sampler.h.

3.3.2.4 dma_queue

QueueHandle_t dma_queue

Definition at line 32 of file i2s_sampler.h.

3.3.2.5 dsp_queue

QueueHandle_t dsp_queue

Definition at line 33 of file i2s_sampler.h.

The documentation for this struct was generated from the following file:

• lib/audio/i2s_sampler.h

3.4 mcp3201_config_t Struct Reference

#include <mcp3201.h>

Data Fields

- spi_host_device_t host
- gpio_num_t cs_io
- gpio_num_t miso_io
- gpio_num_t mosi_io
- int dma_chan

3.4.1 Detailed Description

Definition at line 36 of file mcp3201.h.

3.4.2 Field Documentation

3.4.2.1 cs_io

```
gpio_num_t cs_io
```

Definition at line 39 of file mcp3201.h.

3.4.2.2 dma_chan

```
int dma_chan
```

Definition at line 42 of file mcp3201.h.

3.4.2.3 host

```
spi_host_device_t host
```

Definition at line 38 of file mcp3201.h.

3.4.2.4 miso_io

```
gpio_num_t miso_io
```

Definition at line 40 of file mcp3201.h.

3.4.2.5 mosi_io

```
gpio_num_t mosi_io
```

Definition at line 41 of file mcp3201.h.

The documentation for this struct was generated from the following file:

• lib/mcp3201/mcp3201.h

3.5 mcp3201_context_t Struct Reference

MCP3201 Context struct for internal use.

Data Fields

- mcp3201_config_t cfg
- spi_device_handle_t spi
- spi_transaction_t * ongoing_transaction

3.5.1 Detailed Description

MCP3201 Context struct for internal use.

Parameters

cfg	MCP3201 Configuration
spi	SPI Device Handle
ongoing_transaction	Ongoing SPI Transaction

Definition at line 22 of file mcp3201.c.

3.5.2 Field Documentation

3.5.2.1 cfg

mcp3201_config_t cfg

Definition at line 24 of file mcp3201.c.

3.5.2.2 ongoing_transaction

spi_transaction_t * ongoing_transaction

Definition at line 26 of file mcp3201.c.

3.5.2.3 spi

```
spi_device_handle_t spi
```

Definition at line 25 of file mcp3201.c.

The documentation for this struct was generated from the following files:

- lib/mcp3201/mcp3201.c
- lib/mcp3201/mcp3201_sampler.c

3.6 mcp3201_sampler_t Struct Reference

```
#include <mcp3201.h>
```

Data Fields

- mcp3201_handle_t mcp_handle
- QueueHandle_t dma_queue
- QueueHandle_t dsp_queue
- size_t * buffer
- size_t buffer_pos
- size_t buffer_size

3.6.1 Detailed Description

Definition at line 58 of file mcp3201.h.

3.6.2 Field Documentation

3.6.2.1 buffer

```
size_t* buffer
```

Definition at line 63 of file mcp3201.h.

3.6.2.2 buffer_pos

```
size_t buffer_pos
```

Definition at line 64 of file mcp3201.h.

3.6.2.3 buffer_size

```
size_t buffer_size
```

Definition at line 65 of file mcp3201.h.

3.6.2.4 dma_queue

```
QueueHandle_t dma_queue
```

Definition at line 61 of file mcp3201.h.

3.6.2.5 dsp queue

```
QueueHandle_t dsp_queue
```

Definition at line 62 of file mcp3201.h.

3.6.2.6 mcp_handle

```
mcp3201_handle_t mcp_handle
```

Definition at line 60 of file mcp3201.h.

The documentation for this struct was generated from the following file:

lib/mcp3201/mcp3201.h

3.7 midi_config_t Struct Reference

MIDI UART Configuration.

```
#include <midi.h>
```

Data Fields

- uart_port_t uart_num
- · uint baudrate
- gpio_num_t rx_io
- gpio_num_t tx_io

3.7.1 Detailed Description

MIDI UART Configuration.

Parameters

uart_num	UART Port
baudrate	UART Baudrate
rx_io	UART RX Pin
tx_io	UART TX Pin

Definition at line 76 of file midi.h.

3.7.2 Field Documentation

3.7.2.1 baudrate

uint baudrate

Definition at line 79 of file midi.h.

3.7.2.2 rx_io

gpio_num_t rx_io

Definition at line 80 of file midi.h.

3.7.2.3 tx_io

gpio_num_t tx_io

Definition at line 81 of file midi.h.

3.7.2.4 uart_num

uart_port_t uart_num

Definition at line 78 of file midi.h.

The documentation for this struct was generated from the following file:

• lib/midi/midi.h

3.8 midi_context_t Struct Reference

MIDI Context (internal! not to be accessed externally, use midi_handle_t instead)

Data Fields

• midi_config_t cfg

3.8.1 Detailed Description

MIDI Context (internal! not to be accessed externally, use midi_handle_t instead)

Parameters

cfg	MIDI Config
0.9	9

Definition at line 24 of file midi.c.

3.8.2 Field Documentation

3.8.2.1 cfg

```
midi_config_t cfg
```

Definition at line 26 of file midi.c.

The documentation for this struct was generated from the following file:

• lib/midi/midi.c

3.9 midi_message_t Struct Reference

MIDI Message.

#include <midi.h>

Data Fields

- uint8_t param1
- midi_status_t status
- uint8_t channel
- uint8_t param2

3.9.1 Detailed Description

MIDI Message.

Parameters

status	MIDI Status Byte
channel	MIDI Channel
param1	MIDI Parameter 1
param2	MIDI Parameter 2

Definition at line 60 of file midi.h.

3.9.2 Field Documentation

3.9.2.1 channel

uint8_t channel

Definition at line 64 of file midi.h.

3.9.2.2 param1

uint8_t param1

Definition at line 62 of file midi.h.

3.9.2.3 param2

uint8_t param2

Definition at line 65 of file midi.h.

3.9.2.4 status

midi_status_t status

Definition at line 63 of file midi.h.

The documentation for this struct was generated from the following file:

• lib/midi/midi.h

Chapter 4

File Documentation

4.1 include/config.h File Reference

Gitcon Driver Configuration and Pin-Out File and dependencies.

```
#include <stdio.h>
#include <stdlib.h>
#include <string.h>
#include <math.h>
#include "freertos/FreeRTOS.h"
#include "freertos/task.h"
#include "freertos/queue.h"
#include "freertos/timers.h"
#include "driver/gpio.h"
#include "driver/spi_master.h"
#include "driver/uart.h"
#include "driver/adc.h"
#include "driver/i2s.h"
#include "esp_adc_cal.h"
#include "esp_log.h"
#include "fft.h"
#include "i2s_sampler.h"
#include "mcp3201.h"
#include "midi.h"
```

Macros

```
#define SPI_MOSI (GPIO_NUM_23)
#define SPI_MISO (GPIO_NUM_19)
#define SPI_SCLK (GPIO_NUM_18)
#define SPI_CS (GPIO_NUM_5)
#define SPI_DEV (VSPI_HOST)
#define MIDI_UART (UART_NUM_1)
#define MIDI_BAUD (115200)
#define MIDI_TX (GPIO_NUM_26)
#define MIDI_RX (GPIO_NUM_27)
#define DMA_CHAN 1
```

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- #define ADC_RES_BITS 12
- #define ADC_RES_BITS)
- #define INTERNAL_ADC_UNIT (ADC_UNIT_1)
- #define INTERNAL_ADC_CHANNEL (ADC_CHANNEL_5)
- #define INTERNAL_ADC_IO (GPIO_NUM_33)
- #define AUDIO_BUFFER_SIZE 512
- #define F_SAMPLE_HZ 15000
- #define FFT_WINDOW_SIZE 4
- #define FFT_SIZE (AUDIO_BUFFER_SIZE * FFT_WINDOW_SIZE)

4.1.1 Detailed Description

Gitcon Driver Configuration and Pin-Out File and dependencies.

Author

@s-grundner

Version

0.1

Date

2022-12-24

Copyright

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Definition in file config.h.

4.1.2 Macro Definition Documentation

4.1.2.1 ADC_RES

```
#define ADC_RES (1 << ADC_RES_BITS)</pre>
```

Definition at line 50 of file config.h.

4.1.2.2 ADC_RES_BITS

```
#define ADC_RES_BITS 12
```

Definition at line 49 of file config.h.

4.1.2.3 AUDIO_BUFFER_SIZE

```
#define AUDIO_BUFFER_SIZE 512
```

Definition at line 55 of file config.h.

4.1.2.4 DMA_CHAN

```
#define DMA_CHAN 1
```

Definition at line 48 of file config.h.

4.1.2.5 F_SAMPLE_HZ

```
#define F_SAMPLE_HZ 15000
```

Definition at line 56 of file config.h.

4.1.2.6 FFT_SIZE

```
#define FFT_SIZE (AUDIO_BUFFER_SIZE * FFT_WINDOW_SIZE)
```

Definition at line 58 of file config.h.

4.1.2.7 FFT_WINDOW_SIZE

```
#define FFT_WINDOW_SIZE 4
```

Definition at line 57 of file config.h.

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4.1.2.8 INTERNAL_ADC_CHANNEL

```
#define INTERNAL_ADC_CHANNEL (ADC_CHANNEL_5)
```

Definition at line 52 of file config.h.

4.1.2.9 INTERNAL_ADC_IO

```
#define INTERNAL_ADC_IO (GPIO_NUM_33)
```

Definition at line 53 of file config.h.

4.1.2.10 INTERNAL_ADC_UNIT

```
#define INTERNAL_ADC_UNIT (ADC_UNIT_1)
```

Definition at line 51 of file config.h.

4.1.2.11 MIDI_BAUD

```
#define MIDI_BAUD (115200)
```

Definition at line 44 of file config.h.

4.1.2.12 MIDI RX

```
#define MIDI_RX (GPIO_NUM_27)
```

Definition at line 46 of file config.h.

4.1.2.13 MIDI_TX

```
#define MIDI_TX (GPIO_NUM_26)
```

Definition at line 45 of file config.h.

4.1.2.14 MIDI_UART

```
#define MIDI_UART (UART_NUM_1)
```

Definition at line 43 of file config.h.

4.1.2.15 SPI_CS

```
#define SPI_CS (GPIO_NUM_5)
```

Definition at line 40 of file config.h.

4.1.2.16 SPI_DEV

```
#define SPI_DEV (VSPI_HOST)
```

Definition at line 41 of file config.h.

4.1.2.17 SPI_MISO

```
#define SPI_MISO (GPIO_NUM_19)
```

Definition at line 38 of file config.h.

4.1.2.18 SPI MOSI

```
#define SPI_MOSI (GPIO_NUM_23)
```

Definition at line 37 of file config.h.

4.1.2.19 SPI_SCLK

```
#define SPI_SCLK (GPIO_NUM_18)
```

Definition at line 39 of file config.h.

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4.2 config.h

```
Go to the documentation of this file.
```

```
00011 #ifndef CONFIG_H
00012 #define CONFIG_H
00013
00014 #include <stdio.h>
00015 #include <stdlib.h>
00016 #include <string.h>
00017 #include <math.h>
00018
00019 #include "freertos/FreeRTOS.h"
00020 #include "freertos/task.h"
00021 #include "freertos/queue.h"
00022 #include "freertos/timers.h"
00024 #include "driver/gpio.h"
00025 #include "driver/spi_master.h"
00026 #include "driver/uart.h"
00027 #include "driver/adc.h"
00028 #include "driver/i2s.h"
00029 #include "esp_adc_cal.h"
00030 #include "esp_log.h"
00031
00032 #include "fft.h"
00032 #include "i2s_sampler.h"
00034 #include "mcp3201.h"
00035 #include "midi.h"
00037 #define SPI_MOSI (GPIO_NUM_23)
00038 #define SPI_MISO (GPIO_NUM_19)
00039 #define SPI_SCLK (GPIO_NUM_18)
00040 #define SPI_CS (GPIO_NUM_5)
00041 #define SPI_DEV (VSPI_HOST)
00043 #define MIDI_UART (UART_NUM_1)
00044 #define MIDI_BAUD (115200)
00045 #define MIDI_TX (GPIO_NUM_26)
00046 #define MIDI_RX (GPIO_NUM_27)
00047
00048 #define DMA_CHAN 1
00049 #define ADC_RES_BITS 12
00050 #define ADC_RES (1 « ADC_RES_BITS)
00051 #define INTERNAL_ADC_UNIT (ADC_UNIT_1)
00052 #define INTERNAL_ADC_CHANNEL (ADC_CHANNEL_5)
00053 #define INTERNAL ADC IO (GPIO NUM 33)
00055 #define AUDIO_BUFFER_SIZE 512
                                                                     // Size of buffer for FFT and sampler
00056 #define F_SAMPLE_HZ 15000
                                                                     // Sample rate of FFT and sampler
00057 #define FFT_WINDOW_SIZE 4
                                                                      // Amount of buffers to take for FFT
00058 #define FFT_SIZE (AUDIO_BUFFER_SIZE * FFT_WINDOW_SIZE) // Amount of samples to take for FFT
00059
00060 // leave this commented out to use internal ADC
00061 // #define USE_MCP3201
00062
00063 #endif // CONFIG_H
```

4.3 include/processed-data.h File Reference

Variables

 $756, 0.77675, 0.79725, 0.8109999999999999, 0.820249999999999, 0.8255, 0.829249999999999, 0. \leftarrow$ 3135,0.28525,0.267,0.25325,0.24725,0.2494999999999997,0.261,0.2739999999999997,0.28675,0.05100000000000004, 0.00775, -0.03125, -0.06025, -0.084, -0.1052500000000001, -0.122, -0.135, -0.14275, -0.06025, -0.06025, -0.084, -0.0525, -0.06025, -0.06025, -0.084, -0.0525, -0.0602 $164, -0.17625, -0.18375, -0.187, -0.18375, -0.1785, -0.167749999999999, -0.15325, -0.1335, -0.106, -0. \leftrightarrow 1.000$ $0717500000000001, -0.032, 0.00925, 0.048, 0.08549999999999, 0.11825, 0.148, 0.1770000000000002, 0. \hookleftarrow$ 37,0.39525000000000005,0.41275,0.43325,0.447,0.466999999999997,0.48075,0.4935,0.50275,0. $5135, 0.5235, 0.53875, 0.5615, 0.5935, 0.63775, 0.69275, 0.756749999999999, 0.82775, 0.903999999999999, 0. \leftarrow$ 39475,1.41825,1.4375,1.448,1.4535,1.4565,1.4565,1.460249999999998,1.46475,1.47025,1.47925,1.49,1.503,1.5145,1.52425,1.52975,1.52675,1.513,1.484,1.4405,1.381,1.30475,1.2115,1.1025,0.972,0.82625.0.66525.0.492.0.30525.0.1129999999999999.-0.08925.-0.3045.-0.52575.-0.756749999999999.- $0.993250000000001, -1.23525, -1.4777500000000001, -1.72125, -1.96075, -2.191999999999997, -2. \\ \leftarrow$ 41474999999997, -2.6252500000000003, -2.82525, -3.009, -3.1655, -3.33025, -3.47675, -3.57675, -3.6675, 67349999999998,-3.7835,-3.90325,-4.03224999999994,-4.1595,-4.27325,-4.3685,-4.453250000000001,-4.529500000000005,-4.59825,-4.66375,-4.72575,-4.78275,-4.83925,-4.895000000000005,-4.94775,- $22625, -6.276750000000001, -6.327000000000001, -6.37675, -6.43475, -6.50175, -6.577249999999999, -6. \leftarrow$ 7.729999999995,-7.75524999999999,-7.78274999999999,-7.8155,-7.85825,-7.91175,-7.97800000000001,-8.0605, -8.157250000000001, -8.27024999999999, -8.3985, -8.53875, -8.68375, -8.825750000000001, -8.973500000000005, -4.40750000000001, -3.83225, -3.25325, -2.67575, -2.10425, -1.54725, -1.0085, -0.6237500000000002,2.8937500000000003,3.1425,3.3715,3.58275,3.7735,3.94675,4.098500000000005,4. $545, 5.556500000000001, 5.5665, 5.5755, 5.584, 5.59225, 5.60225000000001, 5.60999999999999, 5. \leftarrow$ $91125, 5.97525, 6.03725, 6.103499999999995, 6.16449999999999, 6.22175, 6.26525, 6.29649999999999, 6. \leftarrow$ 430749999999997,2.25075,2.08425,1.92875,1.786,1.6587500000000002,1.54025,1.43425,1.3375,1.54775, 0.55925, 0.5737500000000001, 0.59125, 0.60949999999999, 0.63175, 0.65525, 0.68199999999999, 0. $7095, 0.742250000000001, 0.77675, 0.810999999999999, 0.8444999999999, 0.875000000000001, 0. \leftarrow$ 42275,0.409,0.402,0.4035,0.415,0.4295,0.4485,0.469249999999994,0.4882499999999996,0.505,0.3455000000000003,0.3105,0.27775,0.25025,0.222749999999999,0.199249999999999,0.18075000000000002,0.1685, 0.16025, 0.154, 0.145, 0.1342499999999998, 0.11975, 0.1015, 0.0785, 0.052, 0.02124999999999999,

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3175,0.3165,0.32575,0.34550000000000003,0.373749999999997,0.4075,0.45175,0.502,0.55925,0. $68, 1.68, 1.67, 1.645, 1.60525, 1.54275, 1.45725, 1.349, 1.2185, 1.065, 0.893500000000001, 0.7035, 0.5005, 0. \hookleftarrow$ 2885, 0.068749999999999, -0.15025, -0.3715, -0.59049999999999, -0.808, -1.023, -1.236, -1.4435, -1.46495,-1.85625,-2.062999999999997,-2.27125,-2.47425,-2.671750000000003,-2.862500000000003,- $3.038000000000003, -3.2005, -3.34775, -3.4775, -3.59875, -3.707, -3.804, -3.8925, -3.97025, -4.04575, -4. \leftrightarrow -4.04575, -4.045$ 12225, -4.20075, -4.28475, -4.3725, -4.463249999999995, -4.557, -4.65475, -4.74925, -4.84775, -4.94075, -5.03225,-5.11925,-5.19799999999995,-5.26725,-5.33075,-5.38625,-5.43825,-5.49175,-5.54275,-5.59925,-5.65724999999994,-5.7227500000000004,-5.7952499999999,-5.88,-5.973,-6.076000000000005,-6.1845, -6.29875, -6.41475, -6.5299999999999999, -6.6382499999999, -6.7475, -6.84975, -6.9215, -6.99775, -6.9975, -7.46925, -7.5745000000000005, -7.69124999999999, -7.821, -7.9674999999999, -8.12, -8.28775, -8.464, 8.64475, -8.8265, -9.002, -9.163, -9.30475, -9.41925, -9.501, -9.5435, -9.54125, -9.49325, -9.39325, -9.601, -9.5435, -9.54125, -9.54125, -9.49325, -9.54125, - $2415, -9.034, -8.7775, -8.4725, -8.126, -7.74075, -7.32575, -6.88399999999995, -6.420249999999999, -5. \leftarrow$ 936500000000006,-5.436,-4.92700000000005,-4.41125,-3.891,-3.373,-2.8535,-2.336,-1.825,-1.32375,-0.833249999999999, -0.35925, 0.09375, 0.525, 0.92925, 1.307, 1.6555, 1.9775, 2.27125, 2.53675, 2.772 $245,4.34725,4.444,4.53725,4.628,4.71350000000001,4.79050000000001,4.8607499999999995,4. \hookleftarrow$ $64800000000001, 5.7075000000000005, 5.7725, 5.84500000000001, 5.92200000000001, 6.005, 6. \leftarrow$ 61499999999999,4.39525,4.1762500000000005,3.95825,3.7445,3.5385,3.3385,3.145499999999997,2.9579999999997,2.774,2.59775,2.42925,2.26974999999997,2.1165,1.97225,1.83725,1.709,1. $78275, 0.73625, 0.6842499999999999, 0.631, 0.58125, 0.53699999999999, 0.502, 0.473, 0.45175, 0. \leftarrow$ $45999999999996, 0.45625, 0.45025000000000004, 0.43949999999995, 0.428749999999996, 0. \leftarrow$ 3334999999999996,0.32275,0.30825,0.29675,0.283000000000003,0.2677500000000004,0.25025,0.02975000000000002,0.00925,-0.01075,-0.03275,-0.05425,-0.0785,-0.10225,-0.12825,-0.158,-0.1855,-0.2167500000000003, -0.2442499999999997, -0.26625, -0.283000000000003, -0.2945000000000004, -0.20625, -0.2065, -0.2065, -0.2065, -0.2065, -0.2065, -0.2065, -0.2065, -0.2065, -0.2065, -0.2065, -0 $0785, 0.093, 0.1, 0.1015, 0.1, 0.097, 0.0915, 0.09075, 0.09225, 0.0985, 0.10975, 0.126, 0.14575, 0.1677499999999998, 0. \leftarrow 0.0015, 0.$ $82625, 0.882, 0.9285, 0.969000000000001, 1.001, 1.02475, 1.04225, 1.0605, 1.08025, 1.101, 1.13075, 1. \leftrightarrow 1.001, 1$ $167250000000001, 1.21525, 1.2725, 1.3405, 1.4160000000000001, 1.496, 1.57625, 1.654, 1.7235, 1.78675, 1. \leftarrow 1.57625, 1.654, 1.7235, 1. \leftarrow 1.57625, 1. \leftarrow 1.57$ $62199999999999,1.52675,1.42125,1.3015,1.165749999999998,1.014,0.84525,0.662999999999999,0. \leftarrow$ 5105,-1.704500000000001,-1.88525,-2.05525,-2.21475,-2.3635,-2.5025,-2.636,-2.765,-2.8907499999999997,-3.0175, -3.14325, -3.27, -3.39725, -3.52475, -3.65375, -3.77875, -3.8985, -4.01075, -4.1122499999999995, -

4.20925, -4.293, -4.36775, -4.4350000000000005, -4.49524999999995, -4.55175, -4.60425, -4.654, -4.60425, -4.654, -4.60425, -7.087499999999,-4.76675,-4.82949999999995,-4.901,-4.9805,-5.063750000000001,-5.156000000000001,-5.25275,-5.3572500000000005,-5.46350000000001,-5.57625,-5.690749999999995,-5.806,-5.9205,-6.0302500000000006, -6.1355, -6.229500000000001, -6.32100000000001, -6.398, -6.462, -6.5125, -6.462, -54824999999995,-6.57574999999999,-6.59475,-6.6055,-6.61175,-6.61625,-6.62225,-6.63974999999999,-7.695,-7.90624999999999,-8.1275,-8.3495,-8.56925,-8.7775,-8.9745,-9.146,-9.298,-9.41625,-9.50475,-9.5605,-9.58100000000001,-9.5665,-9.50925,-9.414,-9.2787499999999,-9.1035,-8.89275000000001,-8.644, -8.3595, -8.0405, -7.6875, -7.30125, -6.88399999999995, -6.43625, -5.95400000000001, -5.471, -4.96675,-4.42725,-3.89325,-3.3845,-2.8945,-2.427,-1.973750000000001,-1.52675,-1.081,-0.648500000000001,- $4305.5.51225.5.60375.5.7052499999999995.5.8119999999999.5.92125000000001.6.029500000000005.6. \leftarrow$ 57125,3.379,3.1945,3.016,2.8457500000000002,2.68475,2.5315,2.38275,2.2407500000000002,2. $50425, 0.48975, 0.486, 0.4935, 0.5135, 0.54475, 0.58375, 0.629500000000001, 0.6775, 0.72475, 0.77125, 0. \leftarrow$ $81325, 0.846749999999999, 0.8757499999999999, 0.894250000000001, 0.903999999999999, 0. \leftarrow$ $805750000000001, 0.7835, 0.763, 0.74149999999999, 0.72175, 0.70425, 0.686750000000001, 0. \leftarrow$ $669750000000001, 0.653, 0.63775, 0.624749999999999, 0.612, 0.6005, 0.59049999999999, 0.5805, 0. \leftarrow$ 573,0.56600000000001,0.5615,0.557,0.55399999999999,0.55224999999999,0.547,0.54325,0.322,0.312,0.296,0.27625,0.24875000000000003,0.2145000000000002,0.17475,0.12975,0.080749999999999,0.0305,-0.0205,-0.068749999999999,-0.10824999999999,-0.14275,-0.16475,-0.18,-0.187,-0.1855,-0.18, -0.17175, -0.16025, -0.148, -0.13649999999999999, -0.125, -0.1144999999999999, -0.1015, -0.08625, -0.125, -0.11449999999999, -0.1015, -0.08625, -0.125, -0.11449999999999, -0.1015, -0.08625, -0.08625, -0.0865, -0.0865, -0.0865, -0.0865, -0.0865, -0.0865, $875749999999999, 0.9285, 0.9865, 1.043, 1.10625, 1.17025, 1.23525, 1.30225, 1.37025, 1.436499999999999, 1. \leftarrow$ $5015, 1.56775, 1.6327500000000001, 1.69675, 1.7585, 1.818749999999999, 1.873, 1.91725, 1.95, 1.968500000000001, 1. \leftarrow$ 97,1.9515,1.9105,1.84625,1.7607500000000003,1.6555,1.5305,1.384,1.2215,1.046,0.859,0.6715,0.4775, 0.28775, 0.097, -0.09375, -0.2845, -0.47075, -0.6577500000000001, -0.84075, -1.02225, -1.20075, -1.37875,-1.55575,-1.73425,-1.9105,-2.085,-2.256000000000002,-2.4245,-2.5895,-2.7487500000000002,- $2.90599999999997, -3.05475, -3.19525, -3.32875, -3.456, -3.57425, -3.6835, -3.785, -3.878, -3.95975, -4. \leftarrow 3.95975, -4.5975, -4$ 03975000000001,-4.123,-4.18624999999999,-4.2365,-4.29075,-4.348,-4.40675000000001,-4.47225,-4.5425,-4.6235,-4.71575,-4.81725,-4.9255,-5.043,-5.171250000000001,-5.306249999999995,-5.44575,-5.5785,-5.7082500000000005,-5.83050000000001,-5.94025,-6.03725,-6.1187499999999995,-6.1835,-6.25524999999999, -6.26375, -6.289, -6.32925, -6.392, -6.475000000000005, -6.58025, -6.70400000000001, -6.26375, -6.26575, - $6.845750000000001, -7.002999999999999, -7.176250000000005, -7.364750000000001, -7.56525, -7. \leftrightarrow -7.56252, -7.56252, -7.56252, -7.56252, -7.56252, -7.56252, -7.56252, -7.56252, -7.56252, -7.56252, -7.56252,$ 77275,-7.98574999999995,-8.20000000000001,-8.413,-8.62725,-8.830250000000001,-9.02700000000001,-9.20875, -9.36975, -9.50925, -9.62, -9.701500000000001, -9.7465, -9.75275, -9.7205, -9.64575, -9.52825, -9.64575, -9.65755, $4285, -5.9784999999995, -5.51825, -5.0475, -4.57149999999995, -4.0969999999995, -3.627, -3. \\ \leftarrow$

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2.76425,-2.858749999999997,-2.96925,-3.0945,-3.23175,-3.38375,-3.54625,-3.7155,-3.896249999999999,-
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29, 0.37225, 0.451, 0.52575, 0.5935, 0.6585, 0.71725, 0.7735, 0.8255, 0.876500000000001, 0.922500000000001, 0. \\ \leftarrow
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```

 $99775, -6.754250000000001, -6.502499999999995, -6.239999999999, -5.967750000000006, -5. \leftarrow$ $0.074, 0.0854999999999999, 0.23875, 0.38825, 0.535500000000001, 0.679, 0.820249999999999, 0. \leftarrow 0.074, 0.085499999999999, 0.094$ $36899999999998, 2.48175, 2.5932500000000003, 2.70075, 2.8075, 2.91149999999999, 3.01425, 3. \leftarrow$ 5394999999999,4.69274999999999,4.84325,4.9905,5.1315,5.26200000000005,5.38700000000005,5. $49925.5.59925.5.68849999999994.5.763999999999999.5.82425.5.877750000000001,5.9165.5. \leftarrow$ $9425, 5.95775, 5.964749999999996, 5.9615, 5.95175000000000005, 5.93349999999996, 5.908250000000001, 5.\\ \leftarrow$ 35124999999999,5.2787500000000005,5.20250000000001,5.124,5.03925,4.95224999999999,4.007500000000003, 2.919, 2.832000000000003, 2.74425, 2.658, 2.57425, 2.49325, 2.40925, 2.32925, 2.40925, 2.32925, 2.409 $25374999999997,2.180500000000003,2.11250000000003,2.044,1.9805,1.921749999999998,1. \leftarrow$ $863.1.80675.1.75475.1.702.1.6525.1.60675.1.5610000000000002.1.51675.1.474.1.43575.1.400750000000002.1. \leftarrow$ $22975, 1.21925, 1.207, 1.194, 1.1795, 1.1635, 1.14825, 1.133, 1.1185, 1.1055000000000001, 1.09625, 1. \leftarrow$ $0895, 1.085, 1.0865, 1.0887499999999999, 1.0955, 1.105500000000001, 1.11625, 1.126, 1.1375, 1.146, 1. \leftarrow$ 3685, 0.312, 0.2625, 0.22274999999999999, 0.19075, 0.16925, 0.16025, 0.161, 0.1709999999999999, 0.0275, -0.12125, -0.2249999999999999998, -0.31425, -0.3875, -0.44625000000000004, -0.496, -0.54475, -0.54475, -0.54575, -0.54575, -0.54575, -0.54575, -0.54575, -0.54575, -0.54575, -0.54575875,-0.62625,-0.65625,-0.679,-0.6890000000000001,-0.6875,-0.67225,-0.647,-0.612,-0.56775,-0.51275,- $0.4547500000000004, -0.38825, -0.31975, -0.2465000000000002, -0.17325000000000002, -0.097, -0. \\ \leftarrow$ 02375, 0.05025, 0.12125, 0.1915, 0.25625000000000003, 0.3205, 0.3785, 0.43499999999999994, 0.4875, 0.4975, 0 $06975, 1.1375, 1.208500000000001, 1.281, 1.35575, 1.4335, 1.509, 1.58375, 1.66025, 1.730249999999999, 1. \leftarrow$ $79975, 1.86375, 1.92325, 1.97975, 2.028, 2.06825, 2.10025, 2.12175, 2.13325, 2.1325, 2.11725, 2.08975, 2. \leftrightarrow 2.12175, 2.1325, 2.1325, 2.11725, 2.08975, 2. \leftrightarrow 2.12175, 2.12175, 2.1325, 2.117$ 951499999999999, 0.7607499999999999, 0.557, 0.34875, 0.136499999999999, -0.07625, -0.29075, -0.69075, -049975,-0.7035,-0.89875,-1.081,-1.253499999999998,-1.4115,-1.5525,-1.67775,-1.78825,-1.880750000000001,-1.958500000000001, -2.018, -2.0645000000000002, -2.097250000000003, -2.11725, -2.130249999999999, -2.018, -22.134000000000003,-2.1325,-2.1285,-2.12325,-2.11725,-2.11575,-2.11575,-2.12175,-2.13400000000000003,-2.15375,-2.18125,-2.21875,-2.26375,-2.32075,-2.3872500000000003,-2.461249999999997,-2.547500000000003,- $2.642, -2.748, -2.861, -2.983, -3.1165000000000003, -3.25325, -3.39725, -3.55075, -3.70875, -3.868, -4. \leftarrow$ 03525, -4.2029999999999, -4.3725, -4.544000000000005, -4.71725, -4.89124999999999, -5.06675, -6.71725, -4.8912499999999, -5.06675, -6.71725, -4.8912499999999, -5.06675, -6.71725, -4.8912499999999, -5.06675, -6.71725, -4.8912499999999, -5.06675, -6.71725, -4.89124999999999, -5.06675, -6.71725, -4.8912499999999, -5.06675, -6.71725, -4.89124999999999, -5.06675, -6.71725, -6.5.24374999999995,-5.42525,-5.60675,-5.7915,-5.98075,-6.16925,-6.362249999999995,-6.55675,-7079999999999, -7.88500000000001, -8.05125, -8.207, -8.35125, -8.483, -8.5975, -8.696, -8.77675, -8.77675, -8.825, -8.76, -8.6785, -8.58, -8.465499999999999, -8.336, -8.18875, -8.0215, -7.8415, -7.6415, -7.425750000000001, -7.195250000000001, -6.9487499999999995, -6.690250000000001, -6.421, -6.14025, -5.851, -5.56025, -5.62627500000000005, -4.96525, -4.666250000000001, -4.36925, -4.0765, -3.7872500000000002, -3.5027500000000003, -4.96525, -4.963.2265,-2.95725,-2.699249999999997,-2.449000000000003,-2.208749999999998,-1.97975,-1.75625,- $11375, 0.28225, 0.44925, 0.60949999999999999, 0.769, 0.92175, 1.06975, 1.21, 1.34575, 1.4755, 1.59825, 1. \leftarrow$ $7885, 2.9145, 3.04575, 3.18375, 3.32325, 3.47125, 3.6225, 3.77725, 3.9345, 4.09, 4.247999999999999, 4. \leftarrow 3.04575, 3.045755, 3.045755, 3.045755, 3.045755, 3.045755, 3.045755, 3.04575$ 404500000000005,4.559250000000005,4.7105,4.856,4.99425,5.12475000000001,5.246750000000005,5.359,5.462,5.55275,5.632000000000001,5.7015,5.75875,5.80525,5.84099999999999,5.8685,5.88824999999999,5. $89975, 5.90600000000001, 5.909, 5.9060000000001, 5.899, 5.8874999999999, 5.8715, 5.854, 5. \leftarrow$

24224999999999,5.1552500000000006,5.063750000000001,4.97125,4.877499999999995,4.782,4. $6875, 4.589, 4.49, 4.390750000000001, 4.2885, 4.18924999999995, 4.08925, 3.98475, 3.88325, 3.7795, 3. \leftarrow 3.795, 3$ $6765, 3.57675, 3.476, 3.37675, 3.28000000000000002, 3.18375, 3.093, 3.006, 2.91675, 2.8335, 2.7512499999999998, 2. \leftarrow 3.006, 2.91675, 3.476,$ 131,2.05925,1.99125,1.9265,1.864499999999998,1.809,1.7555,1.7075,1.66475,1.625,1.58925,1. $55875, 1.528249999999999, 1.50675, 1.484, 1.462500000000001, 1.44575, 1.42675, 1.4075, 1.387, 1. \leftarrow$ $36425, 1.3405, 1.3145, 1.29175, 1.27475, 1.25125, 1.2215, 1.19775, 1.17725, 1.15825, 1.145249999999999, 1. \leftarrow 1.17725, 1.15825, 1.1452499999999999, 1.17725$ $133,1.12925,1.1315,1.1375,1.14825,1.1627500000000002,1.184,1.207,1.22525,1.24425,1.262,1.2765,1. \leftarrow$ 28325, 1.2855, 1.27725, 1.25875, 1.2315, 1.196249999999999, 1.14975, 1.097, 1.039, 0.972, 0.901, 0.827, 0.57225,0.54325,0.50575,0.457,0.4012499999999994,0.3365,0.26475,0.18625,0.1045,0.02225,-0.064,-0.521, -0.573, -0.6165, -0.647, -0.6689999999999999, -0.68125, -0.67975, -0.6715, -0.65225, -0.62175, -0.5875, -0.62175, -0.65225, -0.65225, -0.0.5455, -0.4982499999999997, -0.44775, -0.393, -0.33575, -0.2785, -0.22125, -0.1625, -0.10375, -0.04575, 0.66501,0.06325,0.116,0.167,0.21825,0.27,0.319,0.3685,0.4165000000000004,0.4669999999999997,0.5217499999999999,}

4.3.1 Variable Documentation

4.3.1.1 test buffer

 $671, 5.70675, 5.7465, 5.78375, 5.82125, 5.854, 5.88375, 5.90975, 5.93175, 5.95250000000001, 5.9715, 5. \leftrightarrow$ $99125, 6.00824999999999, 6.026499999999995, 6.04249999999995, 6.057749999999995, 6.07149999999995, 6. \\ \leftarrow$ $0815, 6.08674999999999, 6.0815, 6.06300000000001, 6.028750000000005, 5.97849999999995, 5. \hookleftarrow$ $419, 1.291, 1.17575, 1.072, 0.982000000000001, 0.90325000000001, 0.8370000000001, 0.78425, 0. \hookleftarrow$ $4265, 0.43575, 0.44625000000000004, 0.4592500000000005, 0.4715, 0.484500000000004, 0.503500000000001, 0. \hookleftarrow$ $827, 0.817000000000001, 0.800249999999999, 0.776, 0.742250000000001, 0.70275, 0.66075, 0.615, 0. \\ \leftarrow$ $17625, -0.18375, -0.187, -0.18375, -0.1785, -0.167749999999998, -0.15325, -0.1335, -0.106, -0. \leftrightarrow -0.106, -0.$ $0717500000000001, -0.032, 0.00925, 0.048, 0.08549999999999, 0.11825, 0.148, 0.1770000000000002, 0. \hookleftarrow$ $201499999999999, 0.22425, 0.248, 0.27075, 0.294500000000004, 0.321250000000004, 0.34625, 0. \\ \hookleftarrow$ 37, 0.3952500000000005, 0.41275, 0.43325, 0.447, 0.46699999999997, 0.48075, 0.4935, 0.50275, 0.40275 $5135, 0.5235, 0.53875, 0.5615, 0.5935, 0.63775, 0.69275, 0.75674999999999, 0.82775, 0.90399999999999, 0. \leftarrow$ $98200000000001, 1.06275, 1.13825, 1.20774999999999, 1.271000000000001, 1.323, 1.36325, 1. \leftarrow$ 39475, 1.41825, 1.4375, 1.448, 1.4535, 1.4565, 1.4565, 1.46024999999998, 1.46475, 1.47025, 1.47925, $49, 1.503, 1.5145, 1.52425, 1.52975, 1.52675, 1.513, 1.484, 1.4405, 1.381, 1.30475, 1.2115, 1.1025, 0. \hookleftarrow$ $972, 0.82625, 0.66525, 0.492, 0.30525, 0.112999999999999, -0.08925, -0.3045, -0.52575, -0.75674999999999, -0. \\ \leftarrow$

414749999999997, -2.625250000000003, -2.82525, -3.009, -3.1655, -3.33025, -3.47675, -3.57675, -3.69675, $529500000000005, -4.59825, -4.66375, -4.72575, -4.78275, -4.83925, -4.895000000000005, -4.94775, -5. \\ \leftarrow$ $46350000000001, -5.564, -5.667, -5.77175, -5.87, -5.96225, -6.043250000000005, -6.112, -6.173, -6. \\ \longleftrightarrow$ $0605, -8.157250000000001, -8.270249999999999, -8.3985, -8.53875, -8.68375, -8.825750000000001, -8. \\ \leftarrow$ 9545, -9.0645, -9.147, -9.195, -9.20399999999999, -9.16525, -9.07825, -8.93925, -8.74625, -8.50225, -8.6025, $20474999999999, -7.85899999999999, -7.46775, -7.02975, -6.55749999999999, -6.05175, -5.523, -4. \leftarrow$ $49525, -0.004500000000000005, 0.45325, 0.88425, 1.28775, 1.663250000000001, 2.00875, 2.330749999999997, 2. \leftarrow 0.00875,$ $22825, 4.33725, 4.42725, 4.50125, 4.5625, 4.61574999999999, 4.662999999999, 4.7035, 4.74325000000001, 4. \\ \leftrightarrow$ $42, 5.426, 5.43300000000001, 5.442749999999999, 5.45425, 5.46725, 5.481, 5.497, 5.51225, 5.529, 5. \leftrightarrow 1.55425, 5.45425, 5.45425, 5.46725, 5.481, 5.497, 5.51225, 5.529, 5. \leftrightarrow 1.55425, 5.45425, 5.45425, 5.46725, 5.481, 5.497, 5.51225, 5.529, 5. \leftrightarrow 1.55425, 5.45425, 5.45425, 5.46725, 5.481, 5.497, 5.51225, 5.529, 5. \leftrightarrow 1.55425, 5.45425, 5.46725, 5.481, 5.497, 5.51225, 5.529, 5. \leftrightarrow 1.55425, 5.45425, 5.46725, 5.481, 5.497, 5.51225, 5.529, 5. \leftrightarrow 1.55425, 5.45425, 5.46725, 5.481, 5.497, 5.51225, 5.529, 5. \leftrightarrow 1.55425, 5.45425, 5.46725, 5.481, 5.497, 5.51225, 5.529, 5.45425, 5.46725, 5.481, 5.497, 5.51225, 5.529, 5.45425, 5.46725,$ $91125, 5.97525, 6.03725, 6.1034999999999995, 6.16449999999999, 6.22175, 6.26525, 6.29649999999999, 6. \\ \hookleftarrow$ $69074999999995, 5.52450000000001, 5.33975, 5.1400000000001, 4.926250000000005, 4.702, 4. \hookleftarrow$ $2475, 1.162, 1.085, 1.0125, 0.9497500000000001, 0.8920000000001, 0.8415, 0.79799999999999, 0. \hookleftarrow$ $756749999999999, 0.72025, 0.68599999999999999, 0.65374999999999, 0.62325, 0.59975, 0.57825, 0. \leftrightarrow$ $56075, 0.5485, 0.54025, 0.5355000000000001, 0.53099999999999, 0.53025, 0.534, 0.537750000000001, 0. \leftarrow$ $54775, 0.55925, 0.573750000000001, 0.59125, 0.60949999999999, 0.63175, 0.65525, 0.68199999999999, 0. \leftarrow \\$ $7095, 0.742250000000001, 0.77675, 0.81099999999999, 0.84449999999999, 0.875000000000001, 0. \leftarrow$ $4440000000000006, 0.42275, 0.409, 0.402, 0.4035, 0.415, 0.4295, 0.4485, 0.469249999999994, 0. \hookleftarrow$ $488249999999996, 0.505, 0.518, 0.521, 0.518, 0.50350000000001, 0.4822500000000007, 0.4525, 0. \hookleftarrow$ $11975, 0.1015, 0.0785, 0.052, 0.0212499999999999, -0.0085, -0.0375, -0.061, -0.0825, -0.09924999999999, -0. \leftrightarrow -0.0085,$ $11525, -0.109, -0.1, -0.08925, -0.07475, -0.059500000000000004, -0.0375, -0.00925, 0.02225, 0.05875000000000004, 0. \\ \hookleftarrow$ 097, 0.13725, 0.1755000000000000000, 0.21125, 0.2425, 0.27, 0.296, 0.31825, 0.33575, 0.34875, 0.35625, 0.4296, 0.31825 $4075, 0.45175, 0.502, 0.55925, 0.618, 0.6805, 0.74549999999999, 0.808, 0.8645, 0.9169999999999, 0. \hookleftarrow$ $3215, 1.358, 1.39225, 1.42825, 1.46175, 1.49525, 1.525, 1.55575, 1.58, 1.603, 1.62575, 1.64324999999999, 1. \leftrightarrow 1.5603, 1.603, 1.62575, 1.643249999999999, 1.5603, 1.603,$ $661, 1.67400000000000002, 1.68, 1.68, 1.67, 1.645, 1.60525, 1.54275, 1.45725, 1.349, 1.2185, 1.065, 0. \hookleftarrow$ $893500000000001, 0.7035, 0.5005, 0.2885, 0.06874999999999, -0.15025, -0.3715, -0.5904999999999, -0. \\ \leftarrow$ $862500000000003, -3.03800000000003, -3.2005, -3.34775, -3.4775, -3.59875, -3.707, -3.804, -3. \hookleftarrow$ $65475, -4.74925, -4.84775, -4.94075, -5.03225, -5.11925, -5.1979999999995, -5.26725, -5.33075, -5. \Leftrightarrow -5.26725, -5.33075, -5.26725, -5.33075, -5.26725, -5.33075, -5.26725, -5.33075, -5.26725, -5.33075, -5.26725, -5.33075, -5.26725, -5.33075, -5.26725, -5.33075, -5.26725, -5.33075, -5.26725, -5.33075, -5.26725, -5.33075, -5.26725, -5.33075, -5.26725, -5.$ 12, -8.28775, -8.464, -8.64475, -8.8265, -9.002, -9.163, -9.30475, -9.41925, -9.501, -9.5435, -9.54125, -9.602, -9.602, -9.603, -9.6

49325,-9.39325,-9.2415,-9.034,-8.7775,-8.4725,-8.126,-7.74075,-7.32575,-6.883999999999995,-6.↔ $6575, 3.7895, 3.91475, 4.0305, 4.14049999999999, 4.245, 4.34725, 4.444, 4.53725, 4.628, 4.71350000000001, 4. \leftarrow$ $79050000000001, 4.86074999999995, 4.92249999999999, 4.974250000000005, 5.02325, 5.065250000000001, 5. \hookleftarrow$ $104, 5.13925, 5.17200000000001, 5.20625, 5.239, 5.27125, 5.303999999999, 5.33674999999999, 5. \\ \longleftrightarrow$ $48924999999999, 5.48325, 5.4765, 5.47175, 5.471, 5.46725, 5.46875, 5.47325, 5.48325, 5.49925, 5. \hookleftarrow$ $523750000000001, 5.55725, 5.59775, 5.648000000000001, 5.70750000000005, 5.7725, 5.84500000000001, 5. \\ \leftarrow$ $92200000000001, 6.005, 6.089, 6.17525, 6.256, 6.332500000000005, 6.398, 6.44750000000001, 6. \hookleftarrow \\$ $482, 6.49575, 6.487999999999995, 6.461250000000001, 6.40949999999995, 6.337, 6.24074999999999, 6. \\ \leftarrow$ $122500000000005, 5.98450000000001, 5.8279999999999, 5.6557499999999, 5.46575, 5.264250000000005, 5. \\ \leftarrow$ 5225, 0.50275, 0.492, 0.483, 0.4815, 0.483, 0.48975, 0.5005, 0.51725, 0.53475, 0.557, 0.57975, 0.605 $63625, 0.669750000000001, 0.707249999999999, 0.743749999999999, 0.78125, 0.8125, 0.842249999999999, 0. \leftarrow \\$ $821750000000001, 0.78275, 0.73625, 0.68424999999999, 0.631, 0.58125, 0.5369999999999, 0. \leftrightarrow$ $460749999999994, 0.4599999999999996, 0.45625, 0.4502500000000004, 0.439499999999995, 0. \hookleftarrow$ $05950000000000004, 0.0785, 0.093, 0.1, 0.1015, 0.1, 0.097, 0.0915, 0.09075, 0.09225, 0.0985, 0.10975, 0. \\ \leftarrow$ $014, 0.84525, 0.6629999999999999, 0.4700000000000003, 0.2595, 0.039, -0.18475, -0.4135, -0.644, -0. \leftarrow$ 3635, -2.5025, -2.636, -2.765, -2.890749999999997, -3.0175, -3.14325, -3.27, -3.39725, -3.52475, -3. $65375, -3.77875, -3.8985, -4.01075, -4.112249999999995, -4.20925, -4.293, -4.36775, -4.43500000000005, -4. \\ \leftrightarrow -4.01075, -4.$ $32100000000001, -6.398, -6.462, -6.5125, -6.548249999999995, -6.57574999999999, -6.59475, -6. \hookleftarrow$ $6055, -6.61175, -6.61625, -6.62225, -6.63974999999999, -6.66874999999999, -6.717, -6.7894999999999, -6. \\ \leftarrow$ $88175, -7.00375, -7.14425, -7.309, -7.49274999999999, -7.695, -7.90624999999999, -8.1275, -8. \\ \leftarrow$ $89325, -3.3845, -2.8945, -2.427, -1.9737500000000001, -1.52675, -1.081, -0.648500000000001, -0. \hookleftarrow$ $19475, 4.29, 4.38225, 4.4677500000000006, 4.548, 4.62025, 4.6905, 4.754, 4.8125, 4.87125, 4.928500000000005, 4. \hookleftarrow \\$ $28874999999999, 5.2705, 5.25125, 5.23450000000001, 5.220000000001, 5.21249999999995, 5. \\ \hookleftarrow$ $20925, 5.2170000000000005, 5.233000000000005, 5.26200000000005, 5.30474999999999, 5.362, 5. \leftarrow$

 $4305, 5.51225, 5.60375, 5.7052499999999995, 5.8119999999999, 5.921250000000001, 6.02950000000005, 6. \hookleftarrow$ $1355, 6.2355, 6.32175, 6.39575, 6.4515, 6.490250000000005, 6.50875000000001, 6.50775, 6.487249999999995, 6. \\ \leftrightarrow$ $44525, 6.386500000000001, 6.3125, 6.218, 6.108750000000001, 5.986, 5.846500000000001, 5.693750000000005, 5. \\ \hookleftarrow$ $9369999999999, 0.882, 0.82625, 0.7735, 0.718, 0.66525, 0.614250000000001, 0.56675, 0.5295, 0. \hookleftarrow$ $50425, 0.48975, 0.486, 0.4935, 0.5135, 0.54475, 0.58375, 0.62950000000001, 0.6775, 0.72475, 0.77125, 0. \leftarrow$ $81325, 0.846749999999999, 0.875749999999999, 0.894250000000001, 0.9039999999999, 0.905500000000001, 0. \hookleftarrow$ $5615, 0.557, 0.5539999999999999, 0.552249999999999, 0.547, 0.54325, 0.53625, 0.5295, 0.518, 0.5065, 0. \leftarrow$ 3845, 0.36775, 0.3540000000000004, 0.344, 0.3365, 0.331, 0.32575, 0.322, 0.312, 0.296, 0.27625, 0.496, 0.27625, 0.496, 0.27625, 0.496, 0.27625, 0.496, 0.27625, 0.496, 0.27625, 0.496, 0.27625, 0.496, 0.27625, 0.496, 0.27625, 0.496, 0.27625, 0.496, 0.27625, 0.496, 0.27625, 0.496, 0.27625, 0.496, 0.27625, 0.496, 0.27625, 0.496, 0.27625, 0.496, 0.27625, 0.496, 0.27625, 0.496, 0.27625, 0.296, 0.29625, 0.2917175, -0.16025, -0.148, -0.136499999999999, -0.125, -0.11449999999999, -0.1015, -0.08625, -0. $029750000000000002, 0.039, 0.0572499999999995, 0.08549999999999, 0.122, 0.167749999999998, 0. \\ \leftarrow$ $58525, 0.60125, 0.61875, 0.63625, 0.65625, 0.67975, 0.7095, 0.742250000000001, 0.78275, 0.82775, 0. \\ \leftarrow$ $046, 0.859, 0.6715, 0.4775, 0.28775, 0.097, -0.09375, -0.2845, -0.47075, -0.6577500000000001, -0. \\ \hookleftarrow$ $4245, -2.5895, -2.7487500000000002, -2.90599999999997, -3.05475, -3.19525, -3.32875, -3.456, -3. \leftrightarrow -3.456, -$ 413, -8.62725, -8.83025000000001, -9.02700000000001, -9.20875, -9.36975, -9.50925, -9.62, -70150000000001, -9.7465, -9.75275, -9.7205, -9.64575, -9.52825, -9.3735, -9.17575, -8.941, -8.67, -8.69, -9.59, $51825, -5.0475, -4.571499999999995, -4.09699999999995, -3.627, -3.15775, -2.697, -2.24525, -1. \leftrightarrow -2.0475, -2.$ $68449999999999,1.9455,2.19125,2.42375,2.639750000000003,2.84275,3.02975,3.20575,3.3715,3. \leftarrow$ $5255, 3.6705, 3.8055, 3.9322500000000002, 4.049749999999995, 4.160250000000004, 4.2639999999999, 4. \leftarrow$ $364, 4.46025, 4.553999999999999, 4.64475, 4.7325, 4.818, 4.89875000000001, 4.96749999999999, 5. \leftarrow$ 0500000000001, 5.114, 5.15125, 5.20025, 5.26049999999995, 5.323, 5.3765, 5.4145, 5.426, 5.41925, 5.426, 5.41925, 5.426, 5.41925, 5.426, 5.41925, 5.426, 5.41925, 5.426, 5.41925, 5.426, 5.41925, 5.4192 $5175, 5.61149999999995, 5.71125, 5.815, 5.92425, 6.03325, 6.14325, 6.24925, 6.35, 6.44300000000005, 6. \\ \leftarrow$ $52775, 6.597250000000001, 6.650499999999999, 6.68725000000001, 6.70775, 6.70775, 6.685000000000005, 6. \\ \leftarrow$ $64525, 6.5879999999999, 6.514, 6.424749999999995, 6.32250000000001, 6.20949999999999, 6. \hookleftarrow$ $0845, 5.95025, 5.806, 5.655, 5.493250000000001, 5.324500000000005, 5.1475, 4.959750000000005, 4. \\ \hookleftarrow$ $0385, 1.931, 1.822, 1.7105, 1.59525, 1.48075, 1.36575, 1.2565, 1.1520000000000001, 1.05125, 0.9575, 0. \hookleftarrow$ 63025, 0.62625, 0.63175, 0.644, 0.66, 0.68125, 0.70124999999999, 0.724, 0.747, 0.766749999999999, 0.

 $62249999999999, 0.6035, 0.59125, 0.58125, 0.573750000000001, 0.573, 0.5715, 0.573, 0.5715, 0. \leftarrow$ $166249999999998, -0.2022499999999999, -0.235000000000001, -0.25875, -0.273999999999997, -0. \\ \leftarrow$ $33025, 0.35925, 0.39225, 0.4250000000000004, 0.459999999999996, 0.492749999999997, 0.528749999999999, 0. \leftarrow \\$ $911, 0.98200000000001, 1.06575, 1.15975, 1.25875, 1.3665, 1.47175, 1.57925, 1.68449999999999, 1. \leftarrow$ $9522500000000003, 1.8685, 1.772249999999999, 1.6595, 1.53725, 1.4045, 1.262, 1.11225, 0.9575, 0. \hookleftarrow 1.2025, 1$ $7965, 0.63325, 0.46775, 0.29675, 0.126, -0.04725, -0.22125, -0.3989999999997, -0.57975, -0.76225, -0. \Leftrightarrow$ 949000000000001, -1.139, -1.32975, -1.52275, -1.71574999999999, -1.90425, -2.09275, -2.2735, -2. $447500000000002, -2.61000000000003, -2.758, -2.896, -3.019, -3.128, -3.225, -3.3105, -3.38275, -3. \leftrightarrow -3.019, -3.128, -3.225, -3.3105, -3.38275, -3. \leftrightarrow -3.019, -3.128, -3.225, -3.3105, -3.38275, -3. \leftrightarrow -3.019, -3.128, -3.225, -3.3105, -3.38275, -3.019, -3.128, -3.225, -3.3105, -3.38275, -3.019, -3.128, -3.225, -3.3105, -3.38275, -3.019, -3.128, -3.225, -3.3105, -3.38275, -3.019, -3.128, -3.225, -3.3105, -3.38275, -3.019, -3.128, -3.225, -3.3105, -3.38275, -3.019, -3.128, -3.225, -3.019, -3.128, -3.019, -3.128, -3.019, -3.128, -3.019, -3.128, -3.019, -3.128, -3.019, -3.128, -3.019, -3.$ $4485, -3.50725, -3.56450000000000002, -3.62325, -3.68425, -3.753, -3.8315, -3.92225, -4.02675, -4. \\ \leftarrow$ $3695, -5.47725, -5.56875, -5.6457500000000005, -5.71125, -5.7625, -5.80375, -5.83275, -5.85325, -5. \leftrightarrow -5.85325, -5$ $86325, -5.86625, -5.86775, -5.864, -5.864, -5.86625, -5.87700000000001, -5.8930000000001, -5.\\ \longleftrightarrow -5.86625, -5.8662$ $0735, -7.7225, -7.3539999999999, -6.96575, -6.56125, -6.1455, -5.7189999999999, -5.28874999999999, -4. \\ \hookleftarrow$ $693250000000004, -2.27825, -1.87225, -1.4785, -1.0925, -0.72249999999999, -0.36475, -0.01975, 0. \leftarrow 0.01975, 0. -0.01975,$ $66874999999997, 2.8335, 2.99375, 3.148, 3.29975, 3.4515, 3.5995, 3.7475, 3.89325, 4.03125, 4.16400000000001, 4. \leftarrow$ $98274999999999, 5.0025, 5.01325, 5.01474999999999, 5.00575, 4.988, 4.9645, 4.93624999999999, 4. \leftarrow$ $90275, 4.8705, 4.8425, 4.820250000000001, 4.8065, 4.80500000000001, 4.81499999999995, 4.8415, 4. \\ \hookleftarrow$ $885, 4.947, 5.0225, 5.10950000000001, 5.21099999999999, 5.319999999999, 5.43375, 5.54875, 5. \leftrightarrow$ 66400000000001,5.77325,5.87925,5.978499999999995,6.07149999999995,6.1585,6.23775,6.↔ $47950000000001, 5.312250000000001, 5.142250000000001, 4.9674999999999, 4.79275, 4.61649999999999, 4. \Longleftrightarrow 2.99275, 4.61649999999999, 4. \Longleftrightarrow 2.99275, 4.61649999999999, 4. \Longleftrightarrow 2.99275, 4.61649999999999, 4. \Longleftrightarrow 2.99275, 4.616499999999999, 4. \Longleftrightarrow 2.99275, 4.616499999999999, 4. \Longleftrightarrow 2.99275, 4.616499999999999, 4. \Longleftrightarrow 2.99275, 4.616499999999999, 4. \Longleftrightarrow 2.99275, 4. \odot 2.992$ $681, 2.5382499999999997, 2.39575, 2.253, 2.1125000000000003, 1.976, 1.84325, 1.7175, 1.6, 1.48699999999999, 1. \hookleftarrow$ $82625, 0.81175, 0.80649999999999, 0.810999999999999, 0.82100000000001, 0.84075, 0.8619999999999, 0. \hookleftarrow \\$ $85825, 0.85749999999999, 0.861250000000001, 0.86374999999999, 0.869, 0.8734999999999, 0. \\ \leftarrow$ $876500000000001, 0.876500000000001, 0.87125, 0.865250000000001, 0.85375, 0.83700000000001, 0. \\ \leftarrow$ $68599999999999, 0.684249999999999, 0.68125, 0.67675, 0.669750000000001, 0.66, 0.65225, 0.64475, 0. \leftarrow$ $6165, 0.60275, 0.58375, 0.55775, 0.5225, 0.48075, 0.43325, 0.380750000000003, 0.32875, 0.27225, 0. \\ \leftarrow$ $05025, 0.04725, 0.04425000000000005, 0.04125, 0.03825, 0.0357500000000004, 0.03499999999999999, 0. \hookleftarrow$ $03575000000000004, 0.03499999999999996, 0.0335, 0.0275, 0.0245, 0.02225, 0.019, 0.021249999999998, 0. \\ \hookleftarrow$

 $028249999999997, 0.03975, 0.0572499999999995, 0.0755, 0.10225, 0.132, 0.16475, 0.2, 0.2365, 0. \hookleftarrow$

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27399999999997, 0.30525, 0.33575, 0.35775, 0.377, 0.38975, 0.39975, 0.40425, 0.4075, 0.40825, 0.4075, 0.40825, 0.40825, 0.40825, 0.40825, 0.40825, 0.40825, 0.40825, 0.40825, 0.40825, 0.40825, 0.40825, 0.40825, 0.40825, 0.40825, 0.40825, 0.40825, 0.40825, 0.40825, 0.40825, 0.40825, 0.40825, 0.40825, 0.40825, 0.40825, 0.40825, 0.40825, 0.40825, 0.40825, 0.40825, 0.40825, 0.40825, 0.40825, 0.40825, 0.40825, 0.40825, 0.40825, 0.40825, 0.40825, 0.40825, 0.40825, 0.40825, 0.40825, 0.40825, 0.40825, 0.40825, 0.40825, 0.40825, 0.40825, 0.40825, 0.40825, 0.40825, 0.40825, 0.40825, 0.40825, 0.40825, 0.40825, 0.40825, 0.40825, 0.40825, 0.40825, 0.40825, 0.40825, 0.40825, 0.40825, 0.40825, 0.40825, 0.40825, 0.40825, 0.40825, 0.40825, 0.40825, 0.40825, 0.40825, 0.40825, 0.40825, 0.40825, 0.40825, 0.40825, 0.40825, 0.40825, 0.40825, 0.40825, 0.40825, 0.40825, 0.40825, 0.40825, 0.40825, 0.40825, 0.40825, 0.40825, 0.40825, 0.40825, 0.40825, 0.40825, 0.40825, 0.40825, 0.40825, 0.40825, 0.40825, 0.40825, 0.40825, 0.40825, 0.40825, 0.40825, 0.40825, 0.40825, 0.40825, 0.40825, 0.40825, 0.40825, 0.40825, 0.40825, 0.40825, 0.40825, 0.40825, 0.40825, 0.40825, 0.40825, 0.40825, 0.40825, 0.40825, 0.40825, 0.40825, 0.40825, 0.40825, 0.40825, 0.40825, 0.40825, 0.40825, 0.40825, 0.40825, 0.40825, 0.40825, 0.40825, 0.40825, 0.40825, 0.40825, 0.40825, 0.40825, 0.40825, 0.40825, 0.40825, 0.40825, 0.40825, 0.40825, 0.40825, 0.40825, 0.40825, 0.40825, 0.40825, 0.40825, 0.40825, 0.40825, 0.40825, 0.40825, 0.40825, 0.40825, 0.40825, 0.40825, 0.40825, 0.40825, 0.40825, 0.40825, 0.40825, 0.40825, 0.40825, 0.40825, 0.40825, 0.40825, 0.40825, 0.40825, 0.40825, 0.40825, 0.40825, 0.40825, 0.40825, 0.40825, 0.40825, 0.40825, 0.40825, 0.40825, 0.40825, 0.40825, 0.40825, 0.40825, 0.40825, 0.40825, 0.40825, 0.40825, 0.40825, 0.40825, 0.40825, 0.40825, 0.40825, 0.40825, 0.40825, 0.40825, 0.40825, 0.40825, 0.40825, 0.40825, 0.40825, 0.40825, 0.40825, 0.40825, 0.40825, 0.40825, 0.40825, 0.40825, 0.40825, 0.40825, 0.40825, 0.40825, 0.40825, 0.40825, 0.40825
41125, 0.4135, 0.41875, 0.4287499999999996, 0.445499999999995, 0.468499999999997, 0.497500000000005, 0. \leftarrow
60375, 1.503, 1.39924999999999, 1.2885, 1.17025, 1.04375, 0.90550000000001, 0.756749999999999, 0. \leftarrow
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305750000000001, 6.192, 6.072249999999995, 5.9455, 5.815, 5.678500000000005, 5.53825, 5.3925, 5. \\ \leftarrow
24374999999995, 5.09174999999999, 4.9399999999995, 4.78525, 4.63025, 4.4769999999999, 4. \hookleftarrow
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57975, 0.55925, 0.53025, 0.4982499999999997, 0.458499999999996, 0.41875, 0.377, 0.333499999999996, 0. \\ \leftarrow
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978749999999999, 0.98875, 0.991749999999999, 0.98725, 0.97874999999999, 0.9605, 0.93449999999999, 0. \\ \leftarrow
673, 0.65075, 0.63325, 0.62025, 0.610250000000001, 0.605, 0.6035, 0.60725, 0.612, 0.615, 0.61725, 0. \leftrightarrow 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.6035, 0.603
613499999999999, 0.608, 0.59425, 0.5745, 0.547, 0.515, 0.476000000000003, 0.4325, 0.3845, 0.331, 0. \hookleftarrow
27775, 0.2265, 0.18, 0.13575, 0.097, 0.06325, 0.03499999999996, 0.01525, 0.0, -0.0085, -0.013, -0. \leftrightarrow 0.0085, -0.013, -0.0085, -0.013, -0.0085, -0.013, -0.0085, -0.0085, -0.0085, -0.0085, -0.0085, -0.0085, -0.0085, -0.0085, -0.0085, -0.0085, -0.0085, -0.0085, -0.0085, -0.0085, -0.0085, -0.0085, -0.0085, -0.0085, -0.0085, -0.0085, -0.0085, -0.0085, -0.0085, -0.0085, -0.0085, -0.0085, -0.0085, -0.0085, -0.0085, -0.0085, -0.0085, -0.0085, -0.0085, -0.0085, -0.0085, -0.0085, -0.0085, -0.0085, -0.0085, -0.0085, -0.0085, -0.0085, -0.0085, -0.0085, -0.0085, -0.0085, -0.0085, -0.0085, -0.0085, -0.0085, -0.0085, -0.0085, -0.0085, -0.0085, -0.0085, -0.0085, -0.0085, -0.0085, -0.0085, -0.0085, -0.0085, -0.0085, -0.0085, -0.0085, -0.0085, -0.0085, -0.0085, -0.0085, -0.0085, -0.0085, -0.0085, -0.0085, -0.0085, -0.0085, -0.0085, -0.0085, -0.0085, -0.0085, -0.0085, -0.0085, -0.0085, -0.0085, -0.0085, -0.0085, -0.0085, -0.0085, -0.0085, -0.0085, -0.0085, -0.0085, -0.0085, -0.0085, -0.0085, -0.0085, -0.0085, -0.0085, -0.0085, -0.0085, -0.0085, -0.0085, -0.0085, -0.0085, -0.0085, -0.0085, -0.0085, -0.0085, -0.0085, -0.0085, -0.0085, -0.0085, -0.0085, -0.0085, -0.0085, -0.0085, -0.0085, -0.0085, -0.0085, -0.0085, -0.0085, -0.0085, -0.0085, -0.0085, -0.0085, -0.0085, -0.0085, -0.0085, -0.0085, -0.0085, -0.0085, -0.0085, -0.0085, -0.0085, -0.0085, -0.0085, -0.00
04725, 0.0487499999999995, 0.0487499999999995, 0.0510000000000004, 0.05425, 0.055, 0.055, 0. \\ \leftarrow
05425, 0.0535, 0.05425, 0.05100000000000000, 0.0435, 0.0365, 0.0335, 0.02675, 0.01825, 0.0085, -0. \\ \hookleftarrow
8365, 1.934, 2.0187500000000003, 2.086, 2.139249999999997, 2.176, 2.19875, 2.20325, 2.19274999999998, 2. \hookleftarrow
2605, 1.17275, 1.0895, 1.01175, 0.938499999999999, 0.8704999999999, 0.80499999999999, 0.
```

 $55974999999997, -2.74125, -2.915250000000003, -3.07775, -3.228, -3.36749999999997, -3.49425, -3. \leftrightarrow -3.49425, -3.49$ 94525, -3.97725, -4.00700000000001, -4.00075, -3.98625, -3.98325, -3.98875, -4.0015, -4.01375, -4.6015, -4.01375, -4.0015, -4.01375, -4.0015, -4.01375, -4.0015, -4.01375, -4.0015, -4.01375, -4.0015, -4.01375, -4.0015, -4.01375, -4.0015, -4.01375, -4.0015, -4.01375, -4.0015, -4.01375, -4.0015, -4.01375, -4.0015, -4.12449999999999, -4.21375, -4.32825000000001, -4.464749999999996, -4.6235, -4.80275, -5.00575, -5.04075000000001, -9.16375, -9.26525, -9.346, -9.4055, -9.43975, -9.44975, -9.43525, -9.39625, -9.4055, -9.43975, -9.44975, -9.43525, -9.39625, -9.4055, -9. $3625, -8.16950000000001, -7.96749999999999, -7.7545, -7.53700000000001, -7.312, -7.0792499999999, -6. \\ \leftarrow$ $841250000000005, -6.5955, -6.343, -6.083, -5.81274999999999, -5.536, -5.247500000000005, -4. \hookleftarrow$ $97324999999997, -2.616, -2.254499999999997, -1.88975, -1.52425, -1.1605, -0.80099999999999, -0. \\ \leftarrow$ $91975, 6.012, 6.0975, 6.17375, 6.24225, 6.29725, 6.34374999999999, 6.3805, 6.40649999999999, 6. \Leftrightarrow$ $26300000000001, 6.20275, 6.133999999999995, 6.0554999999999, 5.967750000000006, 5.872999999999, 5. \hookleftarrow$ $985, 1.00325, 1.0215, 1.039, 1.05275, 1.065, 1.07125, 1.0705, 1.06275, 1.04975, 1.03, 1.00325, 0.97425, 0. \hookleftarrow$ $00450000000000005, 0.00525, 0.00675, 0.00675, 0.00675, 0.00675, 0.00675, 0.00675, 0.006, 0.00775, 0.00525, 0. \hookleftarrow$ 344, -0.37625, -0.39825, -0.41125, -0.41650000000000004, -0.40675, -0.38825, -0.357, -0.30975, -0.40675, -0.30975, -0.40675, -0.30975, -0.40675, -0.30975, -0.40675, -0.30975, -0.40675, -0.30975, -0.40675, -0.30975, -0.40675, -0.40675, -0.30975, -0.40675,779, 0.937750000000001, 1.088749999999999, 1.2375, 1.38324999999999, 1.51824999999999, 1. $64425, 1.7585, 1.854, 1.934, 1.99575, 2.037, 2.06224999999997, 2.069, 2.06075, 2.0425, 2.00875, 1. \hookleftarrow$ $50675, 1.451, 1.397, 1.34425, 1.29325, 1.24125, 1.1895, 1.13524999999999, 1.07725, 1.016249999999999, 0. \hookleftarrow$ $088500000000001, -0.0687499999999999, -0.2365, -0.41275, -0.59825, -0.78724999999999, -0. \\ \hookleftarrow$ $98125, -1.17575, -1.37025, -1.56475, -1.75775, -1.947, -2.13175, -2.31175, -2.48575, -2.6565, -2. \leftrightarrow 2.13175, -2.48575, -2.65655, -2.6565, -2.6565, -2.6565, -2.6565, -2.6565, -2.6565, -2.6565$ 819, -2.97324999999997, -3.11899999999999, -3.25475, -3.37825, -3.4905, -3.58725, -3.67125, -37359999999998, -3.7865, -3.82, -3.8375, -3.8415, -3.83075, -3.81, -3.785, -3.75375, -3.7215, -3.60, -3.785, $091, -8.2925, -8.47625, -8.64475, -8.79375, -8.93100000000001, -9.03925000000001, -9.12474999999999, -9. \hookleftarrow$ $97224999999999, -8.87675, -8.7685, -8.64575000000001, -8.509, -8.36325, -8.2030000000001, -8. \\ \hookleftarrow$

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62299999999999, -6.37675, -6.116499999999999, -5.8395, -5.5465, -5.23675, -4.910250000000004, -4. \leftarrow
63575, -1.2825, -0.94075, -0.6142500000000001, -0.303, -0.006, 0.27, 0.53025, 0.77275, 0.99574999999999, 1. \leftarrow 0.006, 0.27, 0.53025, 0.77275, 0.99574999999999, 0.99574999999999, 0.99574999999999, 0.995749999999999, 0.995749999999999, 0.995749999999999, 0.995749999999999, 0.995749999999999, 0.995749999999999, 0.995749999999999, 0.995749999999999, 0.995749999999999, 0.995749999999999, 0.995749999999999, 0.995749999999999, 0.99574999999999, 0.99574999999999, 0.99574999999999, 0.99574999999999, 0.995749999999999, 0.99574999999999, 0.99574999999999, 0.9957499999999, 0.9957499999999, 0.9957499999999, 0.9957499999999, 0.995749999999, 0.99574999999, 0.99574999999, 0.995749999999, 0.9957499999999, 0.99574999999, 0.99574999999, 0.99574999999, 0.99574999999, 0.995749999999, 0.9957499999, 0.99574999999, 0.9957499999, 0.995749999999, 0.99574999999, 0.9957499, 0.9957499, 0.9957499, 0.9957499, 0.9957499, 0.995749, 0.9957499, 0.995749, 0.995749, 0.995749, 0.995749, 0.995749, 0.995749, 0.995749, 0.995749, 0.995749, 0.995749, 0.995749, 0.995749, 0.995749, 0.995749, 0.995749, 0.995749, 0.995749, 0.995749, 0.995749, 0.995749, 0.995749, 0.995749, 0.995749, 0.995749, 0.995749, 0.995749, 0.995749, 0.995749, 0.995749, 0.995749, 0.995749, 0.995749, 0.995749, 0.995749, 0.995749, 0.995749, 0.995749, 0.995749, 0.995749, 0.995749, 0.995749, 0.995749, 0.995749, 0.995749, 0.995749, 0.995749, 0.995749, 0.995749, 0.995749, 0.995749, 0.995749, 0.995749, 0.995749, 0.995749, 0.995749, 0.995749, 0.995749, 0.995749, 0.995749, 0.995749, 0.995749, 0.995749, 0.995749, 0.995749, 0.995749, 0.995749, 0.995749, 0.995749, 0.995749, 0.995749, 0.995749, 0.995749, 0.995749, 0.995749, 0.995749, 0.995749, 0.995749, 0.995749, 0.995749, 0.995749, 0.995749, 0.995749, 0.995749, 0.995749, 0.995749, 0.995749, 0.995749, 0.995749, 0.995749, 0.995749, 0.995749, 0.995749, 0.995749, 0.995749, 0.995749, 0.995749, 0.995749, 0.995749, 0.995749, 0.995749, 0.995749, 0.995749, 0.995749, 0.995749, 0.995749, 0.995749, 0.995740, 0.9957400, 0.995740, 0.9957400, 0.9957400, 0.995740
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37775, 4.49, 4.60425, 4.7195, 4.835500000000001, 4.94925, 5.06275, 5.175, 5.285, 5.3925, 5.49775, 5. \\ \hookleftarrow
1965, 6.23775, 6.26899999999999, 6.289, 6.30025, 6.30099999999999, 6.29050000000001, 6.27049999999999, 6. \\ \leftarrow
558, 5.45275, 5.340500000000005, 5.2245, 5.104, 4.97975, 4.8500000000005, 4.71575, 4.57925, 4. \hookleftarrow
2995, 2.2355, 2.179, 2.1277500000000003, 2.07749999999997, 2.031, 1.986, 1.937749999999999, 1. \leftarrow
0545, 1.0415, 1.0255, 1.01025, 0.99025, 0.971250000000001, 0.95149999999999, 0.933750000000001, 0. \\ \leftarrow
9169999999999, 0.903250000000001, 0.890250000000001, 0.882, 0.876500000000001, 0.87125, 0. \leftarrow
87049999999999, 0.86599999999999999, 0.856, 0.84375, 0.827, 0.80725, 0.782, 0.753, 0.72025, 0.684249999999999, 0. \leftrightarrow 0.80725, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0.782, 0
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7975, 1.82275, 1.84475, 1.8615, 1.87075, 1.87225, 1.867, 1.8455, 1.81575, 1.772249999999999, 1.71275, 1. \leftarrow 2.881575, 1.881575, 1.881575, 1.881575, 1.881575, 1.881575, 1.881575, 1.881575, 1.881575, 1.881575, 1.881575, 1.881575, 1.881575, 1.881575, 1.881575, 1.881575, 1.881575, 1.881575, 1.881575, 1.881575, 1.881575, 1.881575, 1.881575, 1.881575, 1.881575, 1.881575, 1.881575, 1.881575, 1.881575, 1.881575, 1.881575, 1.881575, 1.881575, 1.881575, 1.881575, 1.881575, 1.881575, 1.881575, 1.881575, 1.881575, 1.881575, 1.881575, 1.881575, 1.881575, 1.881575, 1.881575, 1.881575, 1.881575, 1.881575, 1.881575, 1.881575, 1.881575, 1.881575, 1.881575, 1.881575, 1.881575, 1.881575, 1.881575, 1.881575, 1.881575, 1.881575, 1.881575, 1.881575, 1.881575, 1.881575, 1.881575, 1.881575, 1.881575, 1.881575, 1.881575, 1.881575, 1.881575, 1.881575, 1.881575, 1.881575, 1.881575, 1.881575, 1.881575, 1.881575, 1.881575, 1.881575, 1.881575, 1.881575, 1.881575, 1.881575, 1.881575, 1.881575, 1.881575, 1.881575, 1.881575, 1.881575, 1.881575, 1.881575, 1.881575, 1.881575, 1.881575, 1.881575, 1.881575, 1.881575, 1.881575, 1.881575, 1.881575, 1.881575, 1.881575, 1.881575, 1.881575, 1.881575, 1.881575, 1.881575, 1.881575, 1.881575, 1.881575, 1.881575, 1.881575, 1.881575, 1.881575, 1.881575, 1.881575, 1.881575, 1.881575, 1.881575, 1.881575, 1.881575, 1.881575, 1.881575, 1.881575, 1.881575, 1.881575, 1.881575, 1.881575, 1.881575, 1.881575, 1.881575, 1.881575, 1.881575, 1.881575, 1.881575, 1.881575, 1.881575, 1.881575, 1.881575, 1.881575, 1.881575, 1.881575, 1.881575, 1.881575, 1.881575, 1.881575, 1.881575, 1.881575, 1.881575, 1.881575, 1.881575, 1.881575, 1.881575, 1.881575, 1.881575, 1.881575, 1.881575, 1.881575, 1.881575, 1.881575, 1.881575, 1.881575, 1.881575, 1.881575, 1.881575, 1.881575, 1.881575, 1.881575, 1.881575, 1.881575, 1.881575, 1.881575, 1.881575, 1.881575, 1.881575, 1.881575, 1.881575, 1.881575, 1.881575, 1.881575, 1.881575, 1.881575, 1.881575, 1.881575, 1.881575, 1.881575, 1.881575, 1.881575, 1.881575, 1.881575, 1.881575, 1.88157
6395, 1.55325, 1.45025, 1.336, 1.20625, 1.063500000000001, 0.90950000000001, 0.743749999999999, 0. \leftarrow
614250000000001, -0.819499999999999, -1.0215, -1.21925, -1.41225, -1.59675, -1.77075, -1.93625, -2. \leftarrow
```

089, -2.23, -2.3575, -2.46975, -2.568749999999996, -2.6505, -2.71825, -2.77175, -2.8115, -2.83725, -2.6505, -2.71825, -2.7175, -2.8115, -2.83725, -2.6505, -2.71825, -2.71825, -2.71825, -2.8115, -2.83725, -2.6505, -2.71825, -2.71825, -2.71825, -2.8115, -2.81815, -2.81725, -2.81815, -2.81725, -2.81815, -2.81725, -2.81815, -2.81725, -2.81815, -2.81725, -2 $2115, -4.425, -4.6425, -4.86299999999995, -5.085, -5.3039999999999, -5.5215, -5.7349999999999, -5. \\ \leftarrow$ $944, -6.1469999999999, -6.3445, -6.5345, -6.7185, -6.89774999999999, -7.06875, -7.23725, -7. \Leftrightarrow$ $40274999999999, -7.5592500000000005, -7.710999999999999, -7.85675, -7.99875, -8.13225, -8.26025, -8. \\ \longleftrightarrow$ 561, -8.41974999999999, -8.25800000000001, -8.07725, -7.87724999999999, -7.6585, -7.425, -7. $1762500000000005, -6.91075, -6.632250000000001, -6.34374999999999, -6.045500000000005, -5. \hookleftarrow$ $739500000000005, -5.42675, -5.10875, -4.78975000000001, -4.467750000000006, -4.1457500000000005, -3. \\ \leftarrow$ $82625, -3.51025, -3.20125, -2.89925, -2.6025, -2.314, -2.031, -1.75925, -1.493, -1.238249999999999, -0. \\ \leftarrow$ $993999999999, -0.756749999999999, -0.528, -0.311249999999997, -0.099249999999999, 0. \leftarrow$ $16449999999999, 6.139250000000005, 6.10199999999999, 6.053999999999, 5.992999999999, 5. \Leftrightarrow$ $92350000000001, 5.844, 5.754000000000004, 5.66025, 5.5595, 5.45725, 5.35124999999999, 5.24449999999995, 5. \\ \leftarrow$ 136, 5.0299999999999, 4.9255, 4.8255, 4.72575, 4.63025, 4.53575, 4.444, 4.354, 4.26175, 4.16725, 4.449, 4.36175, 4.449, 4.36175, 4.4495, 4 $1135, 3.00449999999997, 2.8945, 2.79, 2.68925, 2.590999999997, 2.50025, 2.411, 2.33, 2.253, 2. \leftrightarrow 2.253, 2$ $625, 1.58475, 1.54425, 1.50525, 1.46625, 1.429, 1.387, 1.34425, 1.3145, 1.27475, 1.22525, 1.1895, 1. \hookleftarrow$ $172, 1.165, 1.165749999999999, 1.167250000000001, 1.1635, 1.15425, 1.14675, 1.14125, 1.13675, 1. \leftrightarrow 1.14125, 1$ $05825, 1.052, 1.04525, 1.03675, 1.0285, 1.0177500000000002, 1.0055, 0.98875, 0.9735, 0.952249999999999, 0. \\ \leftarrow$ $6775, 0.63475, 0.589000000000001, 0.5425, 0.492, 0.43949999999995, 0.388999999999996, 0. \leftrightarrow$ $338, 0.2885, 0.24175, 0.2022499999999999, 0.167749999999998, 0.1420000000000002, 0.125, 0. \leftarrow$ $5645, 0.53875, 0.502, 0.45325, 0.396, 0.32725, 0.25325, 0.1732500000000002, 0.08925, 0.0045000000000005, -0. \\ \leftarrow$ $08325, -0.167, -0.24725, -0.32125000000000004, -0.3905, -0.4502500000000004, -0.50125, -0.54175, -0. \\ \leftarrow$ 570000000000001, -0.588249999999999, -0.5935, -0.5875, -0.5715, -0.54325, -0.505, -0.45775, -0.669, $40049999999997, -0.333499999999999, -0.26175, -0.1815, -0.09625, -0.004500000000000005, 0. \hookleftarrow$ $37175, 1.406, 1.44125, 1.477, 1.517499999999999, 1.5565, 1.59825, 1.642499999999999, 1.6875, 1. \leftrightarrow 1.59825, 1.6424999999999999, 1.6875, 1.6875, 1.697$ $90975, -2.0545, -2.18425, -2.300249999999997, -2.401750000000003, -2.48575, -2.55275, -2.60325, -2. \leftrightarrow -2.50325, -2$ $60775, -2.5825, -2.5604999999999999, -2.53975, -2.5245, -2.5185, -2.5245, -2.5412500000000002, -2. \leftrightarrow -2.5185,$ $5735, -2.62149999999997, -2.683249999999997, -2.76425, -2.85874999999997, -2.96925, -3.0945, -3. \leftrightarrow 3.0945, -3. \leftrightarrow 3.0945, -3.094$ $66775, -4.86600000000005, -5.065250000000001, -5.262750000000005, -5.4594999999999, -5. \leftarrow$ $65574999999999, -5.85025, -6.03874999999999, -6.22625, -6.410250000000004, -6.59175, -6.77100000000001, -6. \\ \hookleftarrow$ $94525, -8.0985, -8.2405, -8.37625, -8.5045, -8.62275, -8.7295, -8.8235, -8.90425, -8.973, -9.0225, -9.\\ \leftrightarrow$

76125, -6.47974999999999, -6.192, -5.89825, -5.59925, -5.2970000000001, -4.995, -4.6905, -4 $4985, -1.2405, -0.99249999999999, -0.75674999999999, -0.5325, -0.3235, -0.126, 0.05875000000000004, 0. \leftarrow$ $227999999999998, 0.38525, 0.534, 0.6705, 0.80024999999999, 0.924, 1.04225, 1.159, 1.274, 1.38925, 1. \hookleftarrow 1.04225, 1.0422$ $7895, 3.9025, 4.016999999999995, 4.13200000000001, 4.25350000000001, 4.376250000000001, 4. \leftrightarrow$ 65799999999995, 5.7685, 5.86475, 5.951, 6.02649999999995, 6.08749999999995, 6.13399999999995, 6.16449999999999, 6.17899999999999, 6.1805, 6.1675, 6.14175, 6.1019999999999, 6.054749999999999, 6.1805, 6.1675, 6.1675, 6.1019999999999, 6.054749999999999, 6.1805, 6.1675, 6.1675, 6.1019999999999, 6.054749999999999, 6.1805, 6.1675, 6.1675, 6.10199999999999, 6.054749999999999, 6.1805, 6.1675, 6.1675, 6.10199999999999, 6.0547499999999999, 6.1805, 6.1675, 6.1675, 6.10199999999999, 6.0547499999999999, 6.1805, 6.1675, 6.1675, 6.1019999999999, 6.0547499999999999, 6.1805, 6.1675, 6.1675, 6.1019999999999, 6.054749999999999, 6.1805, 6.1675, 6.1675, 6.1019999999999, 6.054749999999999, 6.1805, 6.1675, 6.1975, 6.1019999999999, 6.054749999999999, 6.1805, 6.1675, 6.1975, 6.1 $89275, 1.83399999999999, 1.7770000000000001, 1.72050000000001, 1.664, 1.611249999999998, 1. \leftarrow$ $29925, 1.27725, 1.2565, 1.238249999999999, 1.22299999999999, 1.20850000000001, 1.19624999999998, 1. \\ \leftrightarrow$ $18325, 1.172, 1.162, 1.152000000000001, 1.14375, 1.13524999999999, 1.1285, 1.1215, 1.11625, 1. \hookleftarrow$ $11, 1.10625, 1.098750000000001, 1.09175, 1.085, 1.075, 1.06575, 1.059, 1.049, 1.03675, 1.0255, 1. \hookleftarrow$ $9627500000000001, 0.95300000000001, 0.937750000000001, 0.92250000000001, 0.90474999999999, 0. \leftarrow$ $869, 0.834750000000001, 0.8095, 0.766749999999999, 0.705, 0.63175, 0.5455, 0.4615, 0.3845, 0.31975, 0. \hookleftarrow \\$ $07625, 0.1052500000000001, 0.14275, 0.18475, 0.2305, 0.27699999999997, 0.325, 0.370749999999997, 0. \\ \leftarrow$ $41875, -0.33725, -0.25325, -0.1625, -0.07025, 0.02225, 0.114499999999999, 0.202249999999999, 0. \\ \leftarrow$ $29, 0.37225, 0.451, 0.52575, 0.5935, 0.6585, 0.71725, 0.7735, 0.8255, 0.876500000000001, 0.922500000000001, 0. \\ \leftarrow$ $677, -1.815, -1.9355, -2.03925, -2.1255, -2.192749999999998, -2.243, -2.27975, -2.3025, -2.3125, -2. \leftrightarrow -2.27975, -2.3025, -2.30$ $2155, -2.223249999999997, -2.23849999999997, -2.2675, -2.30725, -2.36275, -2.429999999999997, -2. \\ \leftrightarrow$ $8825, -3.57675, -3.27375, -2.977000000000003, -2.6870000000003, -2.4085, -2.139249999999997, -1. \leftarrow$ $48175, 2.593250000000003, 2.70075, 2.8075, 2.91149999999998, 3.01425, 3.118249999999997, 3. \hookleftarrow$ 69274999999999, 4.84325, 4.9905, 5.1315, 5.26200000000005, 5.38700000000005, 5.49925, 5.59925, 5. $68849999999994, 5.76399999999999, 5.82425, 5.877750000000001, 5.9165, 5.9425, 5.95775, 5.964749999999996, 5. \\ \leftarrow$ $9615, 5.9517500000000005, 5.933499999999996, 5.90825000000001, 5.87925, 5.8450000000001, 5. \hookleftarrow$

 $20250000000001, 5.124, 5.03925, 4.95224999999999, 4.86074999999995, 4.7645, 4.6645, 4.5615000000000006, 4. \\ \leftarrow$ $044, 1.9805, 1.921749999999998, 1.863, 1.80675, 1.75475, 1.702, 1.6525, 1.60675, 1.561000000000002, 1. \\ \hookleftarrow$ 475249999999995, 0.50425, 0.53025, 0.54925, 0.56075, 0.56775, 0.5645, 0.54999999999999, 0.53025, 0.6075, 0.5645, 0.5645, 0.5499999999999, 0.53025, 0.6075, 0 $49975, 0.4599999999996, 0.41275, 0.35475, 0.2915, 0.21825, 0.134249999999999, 0.05025, -0. \hookleftarrow 0.05025, -0$ $51275, -0.45475000000000004, -0.38825, -0.31975, -0.246500000000002, -0.1732500000000002, -0. \Leftrightarrow$ $79975, 1.86375, 1.92325, 1.97975, 2.028, 2.06825, 2.10025, 2.12175, 2.13325, 2.1325, 2.11725, 2.08975, 2. \longleftrightarrow 2.08975, 2.089750, 2.08975, 2.08975, 2.08975, 2.08975, 2.08975, 2.08975, 2.08975, 2.08975, 2.08975, 2.08975,$ $04849999999998, 1.98975, 1.91725, 1.8265, 1.719, 1.5975, 1.458, 1.30225, 1.134499999999998, 0. \hookleftarrow$ $951499999999999, 0.760749999999999, 0.557, 0.34875, 0.136499999999998, -0.07625, -0.29075, -0. \hookleftarrow$ $49975, -0.7035, -0.89875, -1.081, -1.25349999999999, -1.4115, -1.5525, -1.67775, -1.78825, -1. \leftrightarrow -1.0810, -1.$ $11725, -2.130249999999998, -2.1340000000000003, -2.1325, -2.1285, -2.12325, -2.11725, -2.11575, -2. \leftrightarrow 2.12325, -2.$ $46124999999997, -2.54750000000003, -2.642, -2.748, -2.861, -2.983, -3.116500000000003, -3. \hookleftarrow$ $25325, -3.39725, -3.55075, -3.70875, -3.868, -4.03525, -4.202999999999, -4.3725, -4.544000000000005, -4. \\ \leftarrow$ $0765, -3.7872500000000002, -3.5027500000000003, -3.2265, -2.95725, -2.699249999999997, -2.44900000000003, -2. \\ \hookleftarrow$ $7105, 4.856, 4.99425, 5.124750000000001, 5.246750000000005, 5.359, 5.462, 5.55275, 5.63200000000001, 5. \\ \leftarrow$ $909, 5.9060000000001, 5.899, 5.88749999999999, 5.8715, 5.854, 5.82875, 5.79825, 5.76325, 5.7189999999999, 5. \\ \leftarrow$ $6695, 5.61375, 5.552, 5.48325, 5.40775, 5.326750000000005, 5.24224999999999, 5.155250000000006, 5. \leftarrow$ $2885, 4.18924999999995, 4.08925, 3.98475, 3.88325, 3.7795, 3.6765, 3.57675, 3.476, 3.37675, 3.2800000000000002, 3. \\ \hookleftarrow$ $51225, 2.4322500000000002, 2.35525, 2.27725, 2.2025, 2.131, 2.05925, 1.99125, 1.9265, 1.864499999999998, 1. \leftarrow 2.05925,$ $44575, 1.42675, 1.4075, 1.387, 1.36425, 1.3405, 1.3145, 1.29175, 1.27475, 1.25125, 1.2215, 1.19775, 1. \\ \leftarrow$ $41725, 0.36475, 0.3212500000000004, 0.28675, 0.256250000000003, 0.23500000000001, 0.22425, 0. \\ \hookleftarrow$ $219749999999997, 0.222749999999998, 0.235000000000001, 0.25025, 0.27325, 0.303, 0.33575, 0. \hookleftarrow$

 $3707499999999997, 0.40825, 0.44625000000000004, 0.4822500000000007, 0.5135, 0.5425, 0.56775, 0. \leftarrow \\ 58525, 0.5950000000000001, 0.5975, 0.589000000000001, 0.57225, 0.54325, 0.50575, 0.457, 0.401249999999994, 0. \leftarrow \\ 3365, 0.26475, 0.18625, 0.1045, 0.02225, -0.064, -0.1487500000000002, -0.234249999999999, -0. \leftarrow \\ 3157500000000003, -0.3915, -0.460749999999994, -0.521, -0.573, -0.6165, -0.647, -0.66899999999999, -0. \leftarrow \\ 68125, -0.67975, -0.6715, -0.65225, -0.62175, -0.5875, -0.5455, -0.498249999999997, -0.44775, -0. \leftarrow \\ 393, -0.33575, -0.2785, -0.22125, -0.1625, -0.10375, -0.04575, 0.01, 0.06325, 0.116, 0.167, 0.21825, 0. \leftarrow \\ 27, 0.319, 0.3685, 0.416500000000000004, 0.4669999999999997, 0.521749999999999, \}$

Definition at line 1 of file processed-data.h.

4.4 processed-data.h

Go to the documentation of this file.

4.5 lib/audio/i2s_sampler.c File Reference

I2S Sampler Driver Source for ESP32.

```
#include "i2s_sampler.h"
```

Macros

- #define RESAMPLE DENOMINATOR 2
- #define READER TIMEOUT MS 10
- #define READER_TIMEOUT_TICKS (READER_TIMEOUT_MS / portTICK_PERIOD_MS)

Functions

i2s_sampler_t * i2s_sampler_start (adc_channel_t adc1_channel, QueueHandle_t recv_queue, const size ←
t buffer size, const size t f sample)

Starts a sampler Task that samples from the given ADC1 Channel and sends the samples to the given Queue.

esp_err_t i2s_sampler_stop (i2s_sampler_t *sampler)

Deletes sampler Task, frees memory and uninstalls adc as well as i2s driver.

4.5.1 Detailed Description

12S Sampler Driver Source for ESP32.

Author

@s-grundner

Version

0.1

Date

2023-03-26

Copyright

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Definition in file i2s_sampler.c.

4.5.2 Macro Definition Documentation

4.5.2.1 READER_TIMEOUT_MS

```
#define READER_TIMEOUT_MS 10
```

Definition at line 16 of file i2s_sampler.c.

4.5.2.2 READER_TIMEOUT_TICKS

```
#define READER_TIMEOUT_TICKS (READER_TIMEOUT_MS / portTICK_PERIOD_MS)
```

Definition at line 17 of file i2s_sampler.c.

4.5.2.3 RESAMPLE_DENOMINATOR

```
#define RESAMPLE_DENOMINATOR 2
```

Definition at line 15 of file i2s_sampler.c.

4.5.3 Function Documentation

4.5.3.1 i2s_sampler_start()

Starts a sampler Task that samples from the given ADC1 Channel and sends the samples to the given Queue.

Parameters

adc1_channel	ADC1 Channel to use (Only ADC1 Channels are supported)
recv_queue	Queue to send samples to
buffer_size	Size of the buffer in samples
f_sample	Sample rate

Returns

i2s_sampler_t* Sampler context or NULL if failed

Definition at line 53 of file i2s sampler.c.

4.5.3.2 i2s_sampler_stop()

Deletes sampler Task, frees memory and uninstalls adc as well as i2s driver.

Parameters

```
sampler Sampler to stop
```

Returns

ESP_OK if successful

Definition at line 92 of file i2s sampler.c.

4.6 i2s_sampler.c

Go to the documentation of this file.

```
00001
00012 #include "i2s_sampler.h"
00013 static const char *TAG = "I2S_SAMPLER";
00014
00015 #define RESAMPLE_DENOMINATOR 2
00016 #define READER_TIMEOUT_MS 10
00017 #define READER_TIMEOUT_TICKS (READER_TIMEOUT_MS / portTICK_PERIOD_MS)
00018
00019 static TaskHandle_t sampler_task_handle;
00020
00021 static void IRAM_ATTR sampler_task(void *arg)
00022 {
00023
          i2s_sampler_t *sampler = (i2s_sampler_t *)arg;
00024
          for (;;)
00025
00026
              i2s_event_t evt;
00027
              if (xQueueReceive(sampler->dma_queue, &evt, portMAX_DELAY) == pdTRUE)
00028
00029
                  if (evt.type == I2S_EVENT_RX_DONE)
00030
00031
                      size t bytes read = 0;
00032
00033
00034
                          // fill audio buffer
                          size_t bytes_to_read = RESAMPLE_DENOMINATOR * (sampler->buffer_size -
00035
       sampler->buffer_pos);
00036
                          void *buffer_position = (void *) (sampler->buffer + sampler->buffer_pos);
00037
00038
                          // read data from i2s
00039
                          i2s_read(I2S_NUM_0, buffer_position, bytes_to_read, &bytes_read,
       READER_TIMEOUT_TICKS);
00040
                          sampler->buffer_pos += bytes_read / RESAMPLE_DENOMINATOR;
00041
00042
                          if (sampler->buffer_pos == sampler->buffer_size)
00043
                          {
```

```
00044
                                sampler->buffer_pos = 0;
00045
                                xQueueSend(sampler->dsp_queue, &sampler->buffer, portMAX_DELAY);
00046
00047
                       } while (bytes_read > 0);
00048
00049
              }
00050
00051 }
00052
00053 i2s_sampler_t *i2s_sampler_start(adc_channel_t adc1_channel, QueueHandle_t recv_queue, const size_t
       buffer_size, const size_t f_sample)
00054 {
00055
           ESP_LOGI(TAG, "Initializing I2S Sampler...");
00056
00057
          QueueHandle_t dma_queue;
00058
00059
          i2s_config_t i2s_cfg = {
              .mode = (i2s_mode_t)(I2S_MODE_MASTER | I2S_MODE_RX | I2S_MODE_ADC_BUILT_IN),
00060
00061
               .sample_rate = f_sample,
               .bits_per_sample = I2S_BITS_PER_SAMPLE_16BIT,
00062
00063
              .channel_format = I2S_CHANNEL_FMT_ONLY_LEFT,
00064
              .communication_format = I2S_COMM_FORMAT_STAND_I2S,
               .intr_alloc_flags = ESP_INTR_FLAG_LEVEL1,
00065
              .dma_buf_count = 4,
.dma_buf_len = 1024,
.use_apl1 = false,
00066
00067
00068
               .fixed_mclk = 0);
00069
00070
00071
           // Initialize ADC
00072
          ESP_ERROR_CHECK(i2s_driver_install(I2S_NUM_0, &i2s_cfg, 4, &dma_queue));
00073
           ESP_ERROR_CHECK(i2s_set_adc_mode(ADC_UNIT_1, adc1_channel));
00074
          ESP_ERROR_CHECK(i2s_adc_enable(I2S_NUM_0));
00075
00076
           i2s_sampler_t *sampler = (i2s_sampler_t *)malloc(sizeof(i2s_sampler_t));
00077
00078
           *sampler = (i2s_sampler_t) {
00079
               .buffer = (size_t *)malloc(buffer_size * sizeof(size_t)),
08000
               .buffer_pos = 0,
00081
               .buffer_size = buffer_size,
00082
               .dma_queue = dma_queue,
00083
               .dsp_queue = recv_queue};
00084
          // DMA task: receives audio data from ADC and sends it to DSP task
if (xTaskCreatePinnedToCore(sampler_task, "sampler_task", 1 « 14, sampler, 5,
00085
00086
       &sampler_task_handle, 0) == pdFALSE)
00087
              return NULL;
00088
00089
          return sampler;
00090 }
00091
00092 esp_err_t i2s_sampler_stop(i2s_sampler_t *sampler)
00093 {
00094
          ESP_LOGI(TAG, "Stopping I2S Sampler...");
00095
          esp_err_t err;
00096
           // stop i2s
00097
           ESP ERROR CHECK(i2s adc disable(I2S NUM 0));
00098
          ESP_ERROR_CHECK(i2s_driver_uninstall(I2S_NUM_0));
00099
00100
00101
          vTaskDelete(sampler_task_handle);
00102
00103
           // free memory
00104
           free(sampler->buffer);
00105
          free(sampler);
00106
00107
           return ESP_OK;
00108 }
```

4.7 lib/audio/i2s sampler.h File Reference

I2S Sampler Driver for ESP32.

```
#include <stdint.h>
#include "driver/i2s.h"
#include "freertos/FreeRTOS.h"
#include "freertos/task.h"
#include "freertos/queue.h"
#include "freertos/timers.h"
```

```
#include "esp_log.h"
```

Data Structures

• struct i2s_sampler_t Sampler Configuration.

Functions

```
• i2s_sampler_t * i2s_sampler_start (adc_channel_t adc1_channel, QueueHandle_t recv_queue, size_ 
t buffer_size, size_t f_sample)
```

Starts a sampler Task that samples from the given ADC1 Channel and sends the samples to the given Queue.

• esp_err_t i2s_sampler_stop (i2s_sampler_t *sampler)

Deletes sampler Task, frees memory and uninstalls adc as well as i2s driver.

4.7.1 Detailed Description

I2S Sampler Driver for ESP32.

Author

@s-grundner

Version

0.1

Date

2023-03-26

Copyright

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Definition in file i2s_sampler.h.

4.7.2 Function Documentation

4.7.2.1 i2s_sampler_start()

Starts a sampler Task that samples from the given ADC1 Channel and sends the samples to the given Queue.

4.8 i2s_sampler.h 63

Parameters

adc1_channel	ADC1 Channel to use (Only ADC1 Channels are supported)
recv_queue	Queue to send samples to
buffer_size	Size of the buffer in samples
f_sample	Sample rate

Returns

i2s_sampler_t* Sampler context or NULL if failed

Definition at line 53 of file i2s_sampler.c.

4.7.2.2 i2s_sampler_stop()

Deletes sampler Task, frees memory and uninstalls adc as well as i2s driver.

Parameters

Returns

ESP OK if successful

Definition at line 92 of file i2s_sampler.c.

4.8 i2s_sampler.h

Go to the documentation of this file.

```
00001
00011 #ifndef SAMPLING_H
00012 #define SAMPLING_H
00013
00013 #include <stdint.h>
00015 #include "driver/i2s.h"
00016 #include "freertos/FreeRTOS.h"
00017 #include "freertos/task.h"
00018 #include "freertos/queue.h"
00019 #include "freertos/timers.h"
00020 #include "esp_log.h"
00021
00030 typedef struct
00031 {
00032
                  QueueHandle_t dma_queue;
00033
                  QueueHandle_t dsp_queue;
00034
                 size_t *buffer;
                 size_t buffer_pos;
size_t buffer_size;
00035
00036
00037 } i2s_sampler_t;
00038
```

4.9 lib/fft/fft.c File Reference

```
#include <stdlib.h>
#include <stdio.h>
#include <math.h>
#include <complex.h>
#include "fft.h"
```

Macros

- #define TWO PI 6.28318530
- #define USE SPLIT RADIX 1
- #define LARGE_BASE_CASE 1

Functions

- fft_config_t * fft_init (int size, fft_type_t type, fft_direction_t direction, float *input, float *output)
- void fft destroy (fft config t *config)
- void fft execute (fft config t *config)
- void fft (float *input, float *output, float *twiddle_factors, int n)
- void ifft (float *input, float *output, float *twiddle_factors, int n)
- void rfft (float *x, float *y, float *twiddle_factors, int n)
- void irfft (float *x, float *y, float *twiddle_factors, int n)
- void fft primitive (float *x, float *y, int n, int stride, float *twiddle factors, int tw stride)
- void split radix fft (float *x, float *y, int n, int stride, float *twiddle factors, int tw stride)
- void ifft primitive (float *input, float *output, int n, int stride, float *twiddle factors, int tw stride)
- void fft8 (float *input, int stride_in, float *output, int stride_out)
- void fft4 (float *input, int stride_in, float *output, int stride_out)

4.9.1 Macro Definition Documentation

4.9.1.1 LARGE BASE CASE

```
#define LARGE BASE CASE 1
```

Definition at line 11 of file fft.c.

4.9.1.2 TWO_PI

```
#define TWO_PI 6.28318530
```

Definition at line 9 of file fft.c.

4.9.1.3 USE_SPLIT_RADIX

```
#define USE_SPLIT_RADIX 1
```

Definition at line 10 of file fft.c.

4.9.2 Function Documentation

4.9.2.1 fft()

Definition at line 104 of file fft.c.

4.9.2.2 fft4()

Definition at line 627 of file fft.c.

4.9.2.3 fft8()

Definition at line 500 of file fft.c.

4.9.2.4 fft_destroy()

Definition at line 80 of file fft.c.

4.9.2.5 fft_execute()

Definition at line 92 of file fft.c.

4.9.2.6 fft_init()

Definition at line 13 of file fft.c.

4.9.2.7 fft_primitive()

Definition at line 237 of file fft.c.

4.9.2.8 ifft()

Definition at line 129 of file fft.c.

4.9.2.9 ifft_primitive()

Definition at line 464 of file fft.c.

4.9.2.10 irfft()

Definition at line 197 of file fft.c.

4.9.2.11 rfft()

Definition at line 149 of file fft.c.

4.9.2.12 split_radix_fft()

Definition at line 325 of file fft.c.

4.10 fft.c

Go to the documentation of this file.

```
00001
00002 #include <stdlib.h>
00003 #include <stdio.h>
00004 #include <math.h>
00005 #include <complex.h>
00006
00007 #include "fft.h"
80000
00009 #define TWO_PI 6.28318530
00010 #define USE_SPLIT_RADIX 1
00011 #define LARGE_BASE_CASE 1
00012
00013 fft_config_t* fft_init(int size, fft_type_t type, fft_direction_t direction, float* input, float*
       output)
00014 {
00015
00016
          * Prepare an FFT of correct size and types.
00017
00018
          \star If no input or output buffers are provided, they will be allocated.
00019
00020
         int k, m;
00021
00022
          fft_config_t* config = (fft_config_t*)malloc(sizeof(fft_config_t));
00023
00024
          \ensuremath{//} Check if the size is a power of two
00025
          if ((size & (size - 1)) !=0) // tests if size is a power of two
00026
              return NULL:
00027
00028
          // start configuration
00029
          config->flags = 0;
00030
          config->type = type;
00031
          config->direction = direction;
          config->size = size;
00032
00033
00034
          // Allocate and precompute twiddle factors
00035
          config->twiddle_factors = (float*)malloc(2 * config->size * sizeof(float));
00036
00037
          float two_pi_by_n = TWO_PI / config->size;
00038
00039
          for (k = 0, m = 0; k < config -> size; k++, m += 2)
00040
00041
              config->twiddle_factors[m] = cosf(two_pi_by_n * k);
00042
              config->twiddle_factors[m + 1] = sinf(two_pi_by_n * k); // imag
00043
00044
          // Allocate input buffer
00045
          if (input != NULL)
00046
00047
              config->input = input;
00048
00049
00050
              if (config->type == FFT_REAL)
                  config->input = (float*)malloc(config->size * sizeof(float));
00051
              else if (config->type == FFT_COMPLEX)
00052
                  config->input = (float*)malloc(2 * config->size * sizeof(float));
00053
00054
00055
              config->flags |= FFT_OWN_INPUT_MEM;
00056
         }
00057
00058
         if (config->input == NULL)
              return NULL;
00060
00061
          // Allocate output buffer
00062
          if (output != NULL)
              config->output = output;
00063
00064
          else
00065
          {
00066
              if (config->type == FFT_REAL)
00067
                  config->output = (float*)malloc(config->size * sizeof(float));
00068
              else if (config->type == FFT_COMPLEX)
                  config->output = (float*)malloc(2 * config->size * sizeof(float));
00069
00070
00071
              config->flags |= FFT OWN OUTPUT MEM;
00072
         }
00073
00074
          if (config->output == NULL)
00075
             return NULL;
00076
00077
          return config;
00078 }
00079
00080 void fft_destroy(fft_config_t* config)
00081 {
```

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```
if (config->flags & FFT_OWN_INPUT_MEM)
              free(config->input);
00083
00084
00085
          if (config->flags & FFT_OWN_OUTPUT_MEM)
00086
              free (config->output);
00087
          free(config->twiddle_factors);
00089
          free(config);
00090 }
00091
00092 void fft_execute(fft_config_t* config)
00093 {
00094
          if (config->type == FFT_REAL && config->direction == FFT_FORWARD)
00095
              rfft(config->input, config->output, config->twiddle_factors, config->size);
00096
          else if (config->type == FFT_REAL && config->direction == FFT_BACKWARD)
00097
              irfft(config->input, config->output, config->twiddle_factors, config->size);
00098
          else if (config->type == FFT_COMPLEX && config->direction == FFT_FORWARD)
          fft(config->input, config->output, config->twiddle_factors, config->size);
else if (config->type == FFT_COMPLEX && config->direction == FFT_BACKWARD)
00099
00100
00101
              ifft(config->input, config->output, config->twiddle_factors, config->size);
00102 }
00103
00104 void fft(float* input, float* output, float* twiddle_factors, int n)
00105 {
00106
00107
           * Forward fast Fourier transform
00108
           * DIT, radix-2, out-of-place implementation
00109
00110
           * Parameters
00111
00112
           * input (float *)
00113
                 The input array containing the complex samples with
00114
                 real/imaginary parts interleaved [\text{Re}(x0), \text{Im}(x0), ..., \text{Re}(x_n-1), \text{Im}(x_n-1)]
00115
              output (float *)
              The output array containing the complex samples with
00116
00117
                real/imaginary parts interleaved [Re(x0), Im(x0), ..., Re(x_n-1), Im(x_n-1)]
00118
           * n (int)
00119
                The FFT size, should be a power of 2
00120
00121
00122 #if USE_SPLIT_RADIX
00123
         split_radix_fft(input, output, n, 2, twiddle_factors, 2);
00124 #else
          fft_primitive(input, output, n, 2, twiddle_factors, 2);
00125
00126 #endif
00127 }
00128
00129 void ifft(float* input, float* output, float* twiddle_factors, int n)
00130 {
00131
00132
           * Inverse fast Fourier transform
00133
           * DIT, radix-2, out-of-place implementation
00134
00135
           * Parameters
00136
00137
           * input (float *)
00138
                The input array containing the complex samples with
00139
                 real/imaginary parts interleaved [Re(x0), Im(x0), ..., Re(x_n-1), Im(x_n-1)]
00140
              output (float *)
00141
                The output array containing the complex samples with
00142
                real/imaginary parts interleaved [Re(x0), Im(x0), ..., Re(x_n-1), Im(x_n-1)]
00143
           * n (int)
00144
                The FFT size, should be a power of 2
00145
00146
          ifft_primitive(input, output, n, 2, twiddle_factors, 2);
00147 }
00148
00149 void rfft(float* x, float* v, float* twiddle factors, int n)
00150 {
00151
00152
           // This code uses the two-for-the-price-of-one strategy
00153 #if USE_SPLIT_RADIX
00154
          split_radix_fft(x, y, n / 2, 2, twiddle_factors, 4);
00155 #else
00156
          fft_primitive(x, y, n / 2, 2, twiddle_factors, 4);
00157 #endif
00158
00159
           // Now apply post processing to recover positive
00160
          \ensuremath{//} frequencies of the real FFT
          float t = y[0];

y[0] = t + y[1]; // DC coefficient
00161
00162
          y[1] = t - y[1]; // Center coefficient
00163
00164
00165
          // Apply post processing to quarter element
          // this boils down to taking complex conjugate y[n / 2 + 1] = -y[n / 2 + 1];
00166
00167
00168
```

```
// Now process all the other frequencies
00170
           for (k = 2; k < n / 2; k += 2)
00171
00172
00173
               float xer, xei, xor t, xoi, c, s, tr, ti;
00174
00175
               c = twiddle_factors[k];
00176
               s = twiddle_factors[k + 1];
00177
               // even half coefficient
00178
               xer = 0.5 * (y[k] + y[n - k]);

xei = 0.5 * (y[k + 1] - y[n - k + 1]);
00179
00180
00181
00182
               // odd half coefficient
               xor_t = 0.5 * (y[k + 1] + y[n - k + 1]);

xoi = -0.5 * (y[k] - y[n - k]);
00183
00184
00185
00186
               tr = c * xor_t + s * xoi;
               ti = -s * xor_t + c * xoi;
00187
00188
               y[k] = xer + tr;
y[k + 1] = xei + ti;
00189
00190
00191
               y[n - k] = xer - tr;

y[n - k + 1] = -(xei - ti);
00192
00193
00194
          }
00195 }
00196
00197 void irfft(float* x, float* y, float* twiddle_factors, int n)
00198 {
00199
00200
           * Destroys content of input vector
00201
00202
           int k;
00203
           // Here we need to apply a pre-processing first
00204
00205
          float t = x[0];
          x[0] = 0.5 * (t + x[1]);

x[1] = 0.5 * (t - x[1]);
00206
00207
00208
00209
          x[n / 2 + 1] = -x[n / 2 + 1];
00210
          for (k = 2; k < n / 2; k += 2)
00211
00212
00213
               float xer, xei, xor_t, xoi, c, s, tr, ti;
00214
00215
               c = twiddle_factors[k];
00216
               s = twiddle_factors[k + 1];
00217
00218
               xer = 0.5 * (x[k] + x[n - k]);
               tr = 0.5 * (x[k] - x[n - k]);
00219
00220
00221
               xei = 0.5 * (x[k + 1] - x[n - k + 1]);
00222
               ti = 0.5 * (x[k + 1] + x[n - k + 1]);
00223
00224
               xor_t = c * tr - s * ti;
00225
               xoi = s * tr + c * ti;
00226
00227
               x[k] = xer - xoi;
00228
               x[k + 1] = xor_t + xei;
00229
              x[n - k] = xer + xoi;

x[n - k + 1] = xor_t - xei;
00230
00231
00232
00233
00234
          ifft_primitive(x, y, n / 2, 2, twiddle_factors, 4);
00235 }
00236
00237 void fft_primitive(float* x, float* y, int n, int stride, float* twiddle_factors, int tw_stride)
00238 {
00239
00240
           \star This code will compute the FFT of the input vector \boldsymbol{x}
00241
           * The input data is assumed to be real/imag interleaved
00242
00243
00244
           * The size n should be a power of two
00245
00246
           \star y is an output buffer of size 2n to accomodate for complex numbers
00247
           * Forward fast Fourier transform
00248
           * DIT, radix-2, out-of-place implementation
00249
00250
00251
           * For a complex FFT, call first stage as:
00252
           * fft(x, y, n, 2, 2);
00253
00254
           * Parameters
00255
```

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```
* x (float *)
00257
               The input array containing the complex samples with
00258
                real/imaginary parts interleaved [Re(x0), Im(x0), ..., Re(x_n-1), Im(x_n-1)]
00259
             y (float *)
               The output array containing the complex samples with real/imaginary parts interleaved [Re(x0), Im(x0), ..., Re(x_n-1), Im(x_n-1)]
00260
00261
00262
             n (int)
00263
                The FFT size, should be a power of 2
00264
           * stride (int)
00265
                The number of elements to skip between two successive samples
00266
          * tw_stride (int)
00267
               The number of elements to skip between two successive twiddle factors
00268
           */
00269
          int k;
00270
          float t;
00271
00272 #if LARGE BASE CASE
00273
         ^{-} End condition, stop at n=8 to avoid one trivial recursion
          if (n == 8)
00275
          {
00276
              fft8(x, stride, y, 2);
00277
              return;
00278
          }
00279 #else
00280
         // End condition, stop at n=2 to avoid one trivial recursion
00281
          if (n == 2)
00282
00283
              y[0] = x[0] + x[stride];
              y[1] = x[1] + x[stride + 1];
y[2] = x[0] - x[stride];
00284
00285
              y[3] = x[1] - x[stride + 1];
00286
00287
              return;
00288
00289 #endif
00290
00291
          \ensuremath{//} Recursion -- Decimation In Time algorithm
          00292
                                                                                                  // even half
00293
00294
00295
          // Stitch back together
00296
00297
          \ensuremath{//} We can a few multiplications in the first step
          t = y[0];
y[0] = t + y[n];
00298
00299
00300
          y[n] = t - y[n];
00301
00302
          t = y[1];
          y[1] = t + y[n + 1];

y[n + 1] = t - y[n + 1];
00303
00304
00305
00306
          for (k = 1; k < n / 2; k++)
00307
00308
              float x1r, x1i, x2r, x2i, c, s;
              c = twiddle_factors[k * tw_stride];
s = twiddle_factors[k * tw_stride + 1];
00309
00310
00311
00312
              x1r = y[2 * k];
00313
              x1i = y[2 * k + 1];
              00314
00315
00316
              y[2 * k] = x1r + x2r;

y[2 * k + 1] = x1i + x2i;
00317
00318
00319
00320
              y[n + 2 * k] = x1r - x2r;
00321
              y[n + 2 * k + 1] = x1i - x2i;
00322
          }
00323 }
00324
00325 void split_radix_fft(float* x, float* y, int n, int stride, float* twiddle_factors, int tw_stride)
00326 {
00327
00328
           * This code will compute the FFT of the input vector x
00329
00330
          * The input data is assumed to be real/imag interleaved
00331
00332
           * The size n should be a power of two
00333
00334
           \star y is an output buffer of size 2n to accomodate for complex numbers
00335
00336
          * Forward fast Fourier transform
00337
           * Split-Radix
00338
           * DIT, radix-2, out-of-place implementation
00339
00340
           \star For a complex FFT, call first stage as:
           * fft(x, y, n, 2, 2);
00341
00342
```

```
00343
            * Parameters
00344
00345
            * x (float *)
00346
                  The input array containing the complex samples with
00347
                  real/imaginary parts interleaved [Re(x0), Im(x0), ..., Re(x_n-1), Im(x_n-1)]
               y (float *)

The output array containing the complex samples with
00348
00350
                  real/imaginary parts interleaved [Re(x0), Im(x0), ..., Re(x_n-1), Im(x_n-1)]
00351
            * n (int)
                  The FFT size, should be a power of 2
00352
00353
            * stride (int)
                  The number of elements to skip between two successive samples
00354
00355
            * twiddle_factors (float *)
00356
                  The array of twiddle factors
00357
            * tw_stride (int)
00358
                 The number of elements to skip between two successive twiddle factors
            */
00359
00360
           int k;
00361
00362 #if LARGE_BASE_CASE
00363
           // End condition, stop at n=2 to avoid one trivial recursion
00364
            if (n == 8)
00365
                fft8(x, stride, y, 2);
00366
00367
                return;
00368
00369
           else if (n == 4)
00370
00371
                fft4(x, stride, y, 2);
00372
                return:
00373
00374 #else
00375
         // End condition, stop at n=2 to avoid one trivial recursion
00376
            if (n == 2)
00377
00378
                y[0] = x[0] + x[stride];
                y[1] = x[1] + x[stride + 1];
y[2] = x[0] - x[stride];
00379
00380
00381
                y[3] = x[1] - x[stride + 1];
00382
                return;
00383
00384
           else if (n == 1)
00385
00386
                y[0] = x[0];
00387
                y[1] = x[1];
00388
                return;
00389
00390 #endif
00391
00392
            // Recursion -- Decimation In Time algorithm
           split_radix_fft(x, y, n / 2, 2 * stride, twiddle_factors, 2 * tw_stride);
split_radix_fft(x + stride, y + n, n / 4, 4 * stride, twiddle_factors, 4 * tw_stride);
split_radix_fft(x + 3 * stride, y + n + n / 2, n / 4, 4 * stride, twiddle_factors, 4 * tw_stride);
00393
00394
00395
00396
00397
            // Stitch together the output
00398
            float ulr, uli, u2r, u2i, x1r, x1i, x2r, x2i;
00399
            float t;
00400
00401
            // We can save a few multiplications in the first step
00402
           u1r = y[0];
           uli = y[1];
00403
           u2r = y[n / 2];
u2i = y[n / 2 + 1];
00404
00405
00406
00407
           x1r = y[n];
           x1i = y[n + 1];
x2r = y[n / 2 + n];
x2i = y[n / 2 + n + 1];
00408
00409
00410
00411
00412
           t = x1r + x2r;
           y[0] = u1r + t;
y[n] = u1r - t;
00413
00414
00415
00416
           t = x1i + x2i;
           y[1] = u1i + t;
y[n + 1] = u1i - t;
00417
00418
00419
           t = x2i - x1i;
y[n / 2] = u2r - t;
y[n + n / 2] = u2r + t;
00420
00421
00422
00423
           t = x1r - x2r;
y[n / 2 + 1] = u2i - t;
y[n + n / 2 + 1] = u2i + t;
00424
00425
00426
00427
            for (k = 1; k < n / 4; k++)
00428
00429
```

4.10 fft.c 73

```
float ulr, uli, u2r, u2i, x1r, x1i, x2r, x2i, c1, s1, c2, s2;
                 c1 = twiddle_factors[k * tw_stride];
s1 = twiddle_factors[k * tw_stride + 1];
00431
00432
                 c2 = twiddle_factors[3 * k * tw_stride];
s2 = twiddle_factors[3 * k * tw_stride + 1];
00433
00434
00435
00436
                 u1r = y[2 * k];
00437
                 u1i = y[2 * k + 1];
                 u2r = y[2 * k + n / 2];

u2i = y[2 * k + n / 2 + 1];
00438
00439
00440
                 x1r = c1 * y[n + 2 * k] + s1 * y[n + 2 * k + 1];
x1i = -s1 * y[n + 2 * k] + c1 * y[n + 2 * k + 1];
x2r = c2 * y[n / 2 + n + 2 * k] + s2 * y[n / 2 + n + 2 * k + 1];
x2i = -s2 * y[n / 2 + n + 2 * k] + c2 * y[n / 2 + n + 2 * k + 1];
00441
00442
00443
00444
00445
                 t = x1r + x2r;
y[2 * k] = u1r + t;
y[2 * k + n] = u1r - t;
00446
00447
00448
00449
                 t = x1i + x2i;
y[2 * k + 1] = u1i + t;
y[2 * k + n + 1] = u1i - t;
00450
00451
00452
00453
00454
                 t = x2i - x1i;
                 y[2 * k + n / 2] = u2r - t;
00455
00456
                 y[2 * k + n + n / 2] = u2r + t;
00457
00458
                 t = x1r - x2r;
                 y[2 * k + n / 2 + 1] = u2i - t;

y[2 * k + n + n / 2 + 1] = u2i + t;
00459
00460
00461
            }
00462 }
00463
00464 void ifft_primitive(float* input, float* output, int n, int stride, float* twiddle_factors, int
        tw_stride)
00465 {
00466
00467 #if USE SPLIT RADIX
00468
            split_radix_fft(input, output, n, stride, twiddle_factors, tw_stride);
00469 #else
00470
          fft_primitive(input, output, n, stride, twiddle_factors, tw_stride);
00471 #endif
00472
00473
            int ks;
00474
00475
            int ns = n * stride;
00476
            // reverse all coefficients from 1 to n / 2 - 1
00477
            for (ks = stride; ks < ns / 2; ks += stride)</pre>
00478
00480
00481
00482
                 t = output[ks];
                 output[ks] = output[ns - ks];
output[ns - ks] = t;
00483
00484
00485
00486
                 t = output[ks + 1];
                 output[ks + 1] = output[ns - ks + 1];
output[ns - ks + 1] = t;
00487
00488
00489
            }
00490
00491
            // Apply normalization
00492
            float norm = 1. / n;
00493
            for (ks = 0; ks < ns; ks += stride)</pre>
00494
            {
00495
                 output[ks] *= norm;
                 output[ks + 1] *= norm;
00496
00497
00498 }
00499
00500 inline void fft8(float* input, int stride_in, float* output, int stride_out)
00501 {
00502
00503
             * Unrolled implementation of FFT8 for a little more performance
00504
00505
            float a0r, a1r, a2r, a3r, a4r, a5r, a6r, a7r;
            float a0i, ali, a2i, a3i, a4i, a5i, a6i, a7i;
float b0r, b1r, b2r, b3r, b4r, b5r, b6r, b7r;
00506
00507
00508
            float b0i, b1i, b2i, b3i, b4i, b5i, b6i, b7i;
00509
            float t;
00510
            float sin_pi_4 = 0.7071067812;
00511
00512
            a0r = input[0];
00513
            a0i = input[1];
            alr = input[stride_in];
00514
00515
            ali = input[stride_in + 1];
```

```
a2r = input[2 * stride_in];
              a2r = input[2 * stride_in];
a2i = input[2 * stride_in + 1];
a3r = input[3 * stride_in];
a3i = input[3 * stride_in + 1];
a4r = input[4 * stride_in];
a4i = input[4 * stride_in + 1];
a5r = input[5 * stride_in];
00517
00518
00519
00520
00521
00522
00523
              a5i = input[5 * stride_in + 1];
              a6r = input[6 * stride_in];
a6i = input[6 * stride_in];
a7r = input[7 * stride_in];
a7i = input[7 * stride_in + 1];
00524
00525
00526
00527
00528
00529
              // Stage 1
00530
              b0r = a0r + a4r;
b0i = a0i + a4i;
00531
00532
00533
00534
              b1r = a1r + a5r;
00535
              bli = ali + a5i;
00536
00537
              b2r = a2r + a6r;
             b2i = a2i + a6i;
00538
00539
00540
              b3r = a3r + a7r;
00541
              b3i = a3i + a7i;
00542
              b4r = a0r - a4r;
b4i = a0i - a4i;
00543
00544
00545
              b5r = a1r - a5r;
b5i = a1i - a5i;
00546
00547
              // W_8^1 = 1/sqrt(2) - j / sqrt(2)
t = b5r + b5i;
00548
00549
              b5i = (b5i - b5r) * sin_pi_4;
b5r = t * sin_pi_4;
00550
00551
00552
              // W_8^2 = -j
b6r = a2i - a6i;
b6i = a6r - a2r;
00554
00555
00556
00557
              b7r = a3r - a7r:
              b/r = a3r - a/r;

b7i = a3i - a7i;

// W_8^3 = -1 / sqrt(2) + j / sqrt(2)

t = sin_pi_4 * (b7i - b7r);

b7i = -(b7r + b7i) * sin_pi_4;
00558
00559
00560
00561
00562
              b7r = t;
00563
00564
              // Stage 2
00565
00566
              a0r = b0r + b2r;
00567
              a0i = b0i + b2i;
00568
              alr = blr + b3r;
ali = bli + b3i;
00569
00570
00571
00572
              a2r = b0r - b2r;
              a2i = b0i - b2i;
00573
00574
              // * j
a3r = b1i - b3i;
a3i = b3r - b1r;
00575
00576
00577
00578
00579
              a4r = b4r + b6r;
              a4i = b4i + b6i;
00580
00581
00582
              a5r = b5r + b7r;
              a5i = b5i + b7i;
00583
00584
              a6r = b4r - b6r;
a6i = b4i - b6i;
00585
00586
00587
              // * j
a7r = b5i - b7i;
00588
00589
              a7i = b7r - b5r;
00590
00591
00592
              // Stage 3
00593
              // X[0]
00594
              output[0] = a0r + a1r;
output[1] = a0i + a1i;
00595
00596
00597
00598
00599
              output[4 * stride_out] = a0r - a1r;
              output[4 * stride_out + 1] = a0i - a1i;
00600
00601
00602
              // X[2]
```

```
output[2 * stride_out] = a2r + a3r;
output[2 * stride_out + 1] = a2i + a3i;
00604
00605
00606
            // X[6]
            output[6 * stride_out] = a2r - a3r;
00607
            output[6 * stride_out + 1] = a2i - a3i;
00608
00609
00610
            output[stride_out] = a4r + a5r;
output[stride_out + 1] = a4i + a5i;
00611
00612
00613
00614
            // XI51
00615
            output[5 * stride_out] = a4r - a5r;
            output[5 * stride_out + 1] = a4i - a5i;
00616
00617
00618
            output[3 * stride_out] = a6r + a7r;
00619
            output[3 * stride_out + 1] = a6i + a7i;
00620
00621
00622
            output[7 * stride_out] = a6r - a7r;
output[7 * stride_out + 1] = a6i - a7i;
00623
00624
00625 }
00626
00627 inline void fft4(float* input, int stride_in, float* output, int stride_out)
00628 {
00629
00630
            * Unrolled implementation of FFT4 for a little more performance
00631
00632
            float t1, t2;
00633
00634
            t1 = input[0] + input[2 * stride_in];
00635
            t2 = input[stride_in] + input[3 * stride_in];
00636
            output[0] = t1 + t2;
00637
            output[2 * stride_out] = t1 - t2;
00638
            t1 = input[1] + input[2 * stride_in + 1];
t2 = input[stride_in + 1] + input[3 * stride_in + 1];
00639
00640
00641
            output[1] = t1 + t2;
00642
            output[2 * stride_out + 1] = t1 - t2;
00643
00644
            t1 = input[0] - input[2 * stride in];
            t2 = input[stride_in + 1] - input[3 * stride_in + 1];

output[stride_out] = t1 + t2;

output[3 * stride_out] = t1 - t2;
00645
00646
00647
00648
            t1 = input[1] - input[2 * stride_in + 1];
t2 = input[3 * stride_in] - input[stride_in];
output[stride_out + 1] = t1 + t2;
output[3 * stride_out + 1] = t1 - t2;
00649
00650
00651
00652
00653 }
```

4.11 lib/fft/fft.h File Reference

Data Structures

· struct fft config t

Macros

- #define FFT OWN INPUT MEM 1
- #define FFT OWN OUTPUT MEM 2

Enumerations

- enum fft_type_t { FFT_REAL , FFT_COMPLEX }
 ESP32 FFT. This provides a vanilla radix-2 FFT implementation and a test example.
- enum fft direction t { FFT FORWARD , FFT BACKWARD }

Functions

- fft_config_t * fft_init (int size, fft_type_t type, fft_direction_t direction, float *input, float *output)
- void fft_destroy (fft_config_t *config)
- void fft execute (fft config t *config)
- void fft (float *input, float *output, float *twiddle_factors, int n)
- void ifft (float *input, float *output, float *twiddle_factors, int n)
- void rfft (float *x, float *y, float *twiddle_factors, int n)
- void irfft (float *x, float *y, float *twiddle_factors, int n)
- void fft primitive (float *x, float *y, int n, int stride, float *twiddle factors, int tw stride)
- void split_radix_fft (float *x, float *y, int n, int stride, float *twiddle_factors, int tw_stride)
- void ifft primitive (float *input, float *output, int n, int stride, float *twiddle factors, int tw stride)
- void fft8 (float *input, int stride_in, float *output, int stride_out)
- void fft4 (float *input, int stride_in, float *output, int stride_out)

4.11.1 Macro Definition Documentation

4.11.1.1 FFT OWN INPUT MEM

#define FFT_OWN_INPUT_MEM 1

Definition at line 40 of file fft.h.

4.11.1.2 FFT_OWN_OUTPUT_MEM

#define FFT_OWN_OUTPUT_MEM 2

Definition at line 41 of file fft.h.

4.11.2 Enumeration Type Documentation

4.11.2.1 fft_direction_t

enum fft_direction_t

Enumerator

FFT_FORWARD
FFT BACKWARD

Definition at line 34 of file fft.h.

4.11.2.2 fft type t

```
enum fft_type_t
```

ESP32 FFT. This provides a vanilla radix-2 FFT implementation and a test example.

Author

This code was written by Robin Scheibler

Date

during rainy days in October 2017.

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Enumerator

FFT_REAL	
FFT_COMPLEX	

Definition at line 28 of file fft.h.

4.11.3 Function Documentation

4.11.3.1 fft()

Definition at line 104 of file fft.c.

4.11.3.2 fft4()

Definition at line 627 of file fft.c.

4.11.3.3 fft8()

Definition at line 500 of file fft.c.

4.11.3.4 fft_destroy()

Definition at line 80 of file fft.c.

4.11.3.5 fft_execute()

Definition at line 92 of file fft.c.

4.11.3.6 fft_init()

Definition at line 13 of file fft.c.

4.11.3.7 fft_primitive()

Definition at line 237 of file fft.c.

4.11.3.8 ifft()

Definition at line 129 of file fft.c.

4.11.3.9 ifft_primitive()

Definition at line 464 of file fft.c.

4.11.3.10 irfft()

Definition at line 197 of file fft.c.

4.11.3.11 rfft()

Definition at line 149 of file fft.c.

4.11.3.12 split_radix_fft()

```
void split_radix_fft (
    float * x,
    float * y,
    int n,
    int stride,
    float * twiddle_factors,
    int tw_stride )
```

Definition at line 325 of file fft.c.

4.12 fft.h

Go to the documentation of this file.

```
00001
00025 #ifndef __FFT_H_
00026 #define __FFT_H_
00027
00028 typedef enum
00029 {
00030 FFT_REAL,
00031 FFT_COMPLEX
00032 } fft_type_t;
00033
00034 typedef enum
00035 {
00036 FFT_FORWARD,
00037 FFT_BACKWARD
00038 } fft_direction_t;
00039
00040 #define FFT_OWN_INPUT_MEM 1
00041 #define FFT_OWN_OUTPUT_MEM 2
```

4.13 lib/mcp3201/mcp3201.c File Reference

```
#include "mcp3201.h"
```

Data Structures

struct mcp3201 context t

MCP3201 Context struct for internal use.

Typedefs

typedef struct mcp3201_context_t mcp3201_context_t

Functions

```
• esp err t mcp3201 init (mcp3201 context t **out ctx, const mcp3201 config t *cfg)
```

- esp_err_t mcp3201_read (mcp3201_context_t *ctx, uint16_t *out_value)
- esp_err_t mcp3201_exit (mcp3201_handle_t mcp_handle)

Exits the MCP3201 ADC device and frees all resources.

4.13.1 Detailed Description

Author

@s-grundner

Version

0.1

Date

2022-12-24

Copyright

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Definition in file mcp3201.c.

4.13.2 Typedef Documentation

4.13.2.1 mcp3201_context_t

```
typedef struct mcp3201_context_t mcp3201_context_t
```

Definition at line 28 of file mcp3201.c.

4.13.3 Function Documentation

4.13.3.1 mcp3201_exit()

Exits the MCP3201 ADC device and frees all resources.

Parameters

```
mcp_handle | MCP3201 Device to exit
```

Returns

ESP_OK on success

Definition at line 105 of file mcp3201.c.

4.13.3.2 mcp3201_init()

4.14 mcp3201.c 83

Definition at line 42 of file mcp3201.c.

4.13.3.3 mcp3201_read()

Definition at line 88 of file mcp3201.c.

4.14 mcp3201.c

Go to the documentation of this file.

```
00001
00012 #include "mcp3201.h"
00013
00014 static const char *TAG = "mcp3201";
00015
00022 struct mcp3201_context_t
00023 {
00024
          mcp3201_config_t cfg;
00025
          spi_device_handle_t spi;
00026
          spi_transaction_t *ongoing_transaction;
00027 };
00028 typedef struct mcp3201_context_t mcp3201_context_t;
00029
00030 static void cs_low(spi_transaction_t *t)
00032
          mcp3201_handle_t mcp_handle = (mcp3201_handle_t)t->user;
00033
          gpio_set_level(mcp_handle->cfg.cs_io, 0);
00034 }
00035
00036 static void cs high(spi transaction t *t)
00037 {
00038
          mcp3201_handle_t mcp_handle = (mcp3201_handle_t)t->user;
00039
          gpio_set_level(mcp_handle->cfg.cs_io, 1);
00040 }
00041
00042 \ \texttt{esp\_err\_t mcp3201\_init(mcp3201\_context\_t **out\_ctx, const mcp3201\_config\_t *cfg)}
00043 {
00044
          mcp3201_context_t *ctx = (mcp3201_context_t *)malloc(sizeof(mcp3201_context_t));
00045
          esp_err_t err = ESP_OK;
00046
             (ctx == NULL)
00047
              ESP_LOGE(TAG, "Failed to allocate memory for mcp3201 context");
00048
00049
              return ESP_ERR_NO_MEM;
00050
          }
00051
00052
          *ctx = (mcp3201_context_t) {
00053
              .cfg = *cfg};
00054
00055
          spi_device_interface_config_t dev_cfg = {
00056
              .clock_speed_hz = ADC_CLK,
00057
00058
              .spics_io_num = ctx->cfg.cs_io,
00059
              .queue_size = 1,
              .pre_cb = cs_low,
.post_cb = cs_high,
00060
00061
00062
              .command_bits = 0,
00063
              .address_bits = 0,
00064
              .dummy_bits = 0,
00065
              .flags = 0,
00066
          };
00067
00068
          err = spi_bus_add_device(ctx->cfg.host, &dev_cfg, &ctx->spi);
00069
          ESP_ERROR_CHECK(err);
00070
          if (err != ESP_OK)
00071
00072
              ESP_LOGE(TAG, "Failed to add device to spi bus");
00073
              goto cleanup;
00074
          *out_ctx = ctx;
```

```
return err;
00077
00078 cleanup:
00079
          if (ctx->spi)
08000
00081
              spi_bus_remove_device(ctx->spi);
              ctx->spi = NULL;
00083
00084
          free(ctx);
00085
          return err;
00086 }
00087
00088 esp_err_t mcp3201_read(mcp3201_context_t *ctx, uint16_t *out_value)
00089 {
00090
          esp_err_t err = ESP_OK;
00091
          spi\_transaction\_t t =
             .user = (void *)ctx,
.length = 16,
00092
00093
              .rx_buffer = out_value,
00094
00095
00096
          err = spi_device_polling_transmit(ctx->spi, &t);
00097
          if (err != ESP_OK)
00098
00099
              ESP_LOGE(TAG, "Failed to transmit to mcp3201");
00100
             return err;
00101
00102
          return err;
00103 }
00104
00105 esp_err_t mcp3201_exit(mcp3201_handle_t mcp_handle)
00106 {
00107
          esp_err_t err = ESP_OK;
00108
00109
          if (mcp_handle->spi)
00110
00111
              err = spi_bus_remove_device(mcp_handle->spi);
00112
              if (err != ESP_OK)
00113
00114
                  ESP_LOGE(TAG, "Failed to remove device from spi bus");
00115
00116
              mcp handle->spi = NULL;
00117
00118
         }
00119
00120
          free (mcp_handle);
00121
00122 }
```

4.15 lib/mcp3201/mcp3201.h File Reference

```
#include <stdio.h>
#include "freertos/FreeRTOS.h"
#include "freertos/task.h"
#include "freertos/queue.h"
#include "driver/gpio.h"
#include "driver/spi_master.h"
#include "hal/spi_types.h"
#include "esp_log.h"
```

Data Structures

- struct mcp3201_config_t
- struct mcp3201_sampler_t

Macros

• #define ADC_CLK SPI_MASTER_FREQ_8M

Typedefs

typedef struct mcp3201_context_t * mcp3201_handle_t

Functions

```
    esp_err_t mcp3201_init (mcp3201_handle_t *out_handle, const mcp3201_config_t *cfg)
    Initializes the MCP3201 ADC device.
```

• esp_err_t mcp3201_exit (mcp3201_handle_t mcp_handle)

Exits the MCP3201 ADC device and frees all resources.

• esp_err_t mcp3201_read (mcp3201_handle_t handle, uint16_t *out_value)

Reads a single value from the MCP3201 ADC.

mcp3201_sampler_t * mcp3201_sampler_start (mcp3201_handle_t mcp_handle, QueueHandle_t recv_
 queue, const size_t buffer_size, const size_t f_sample)

Starts the MCP3201 Sampler, which samples continuously and puts the samples into a queue.

void mcp3201_sampler_stop (mcp3201_sampler_t *sampler)

Stops the MCP3201 Sampler.

4.15.1 Detailed Description

Author

@s-grundner

Version

0.1

Date

2022-12-24

Copyright

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Definition in file mcp3201.h.

4.15.2 Macro Definition Documentation

4.15.2.1 ADC_CLK

#define ADC_CLK SPI_MASTER_FREQ_8M

Definition at line 24 of file mcp3201.h.

4.15.3 Typedef Documentation

4.15.3.1 mcp3201_handle_t

```
typedef struct mcp3201_context_t* mcp3201_handle_t
```

Definition at line 46 of file mcp3201.h.

4.15.4 Function Documentation

4.15.4.1 mcp3201_exit()

Exits the MCP3201 ADC device and frees all resources.

Parameters

mcp_handle	MCP3201 Device to exit
------------	------------------------

Returns

ESP_OK on success

Definition at line 105 of file mcp3201.c.

4.15.4.2 mcp3201_init()

Initializes the MCP3201 ADC device.

Parameters

out_handle	MCP3201 Handler to store initialization data
cfg	MCP3201 Configuration

Returns

4.15.4.3 mcp3201_read()

Reads a single value from the MCP3201 ADC.

Parameters

	handle	MCP3201 Device	
out	out_value	Value	

Returns

ESP_OK on success

4.15.4.4 mcp3201_sampler_start()

Starts the MCP3201 Sampler, which samples continuously and puts the samples into a queue.

Parameters

mcp_handle	MCP3201 Device Handler
recv_queue	queue to send the samples into
buffer_size	size of the audio buffer
f_sample	Sample rate

Returns

mcp3201_sampler_t* Sampler Handler

Definition at line 84 of file mcp3201_sampler.c.

4.15.4.5 mcp3201_sampler_stop()

Stops the MCP3201 Sampler.

Parameters

sampler | Sampler Handler to stop

Definition at line 110 of file mcp3201_sampler.c.

4.16 mcp3201.h

Go to the documentation of this file.

```
00001
00012 #ifndef MCP3201_DRIVER_H
00013 #define MCP3201_DRIVER_H
00014
00015 #include <stdio.h>
00016 #include "freertos/FreeRTOS.h"
00017 #include "freertos/task.h"
00018 #include "freertos/queue.h"
00019 #include "driver/gpio.h"
00020 #include "driver/spi_master.h"
00021 #include "hal/spi_types.h"
00022 #include "esp_log.h
00023
00024 #define ADC CLK SPI MASTER FREO 8M
00025
00036 typedef struct
00038
          spi_host_device_t host;
00039
          gpio_num_t cs_io;
00040
          gpio_num_t miso_io;
00041
         gpio_num_t mosi_io;
int dma_chan;
00042
00043 } mcp3201_config_t;
00044
00046 typedef struct mcp3201_context_t *mcp3201_handle_t;
00047
00058 typedef struct
00059 {
00060
          mcp3201_handle_t mcp_handle;
00061
          QueueHandle_t dma_queue;
00062
          QueueHandle_t dsp_queue;
00063
          size_t *buffer;
          size_t buffer_pos;
00064
00065
          size_t buffer_size;
00066 } mcp3201_sampler_t;
00075 esp_err_t mcp3201_init(mcp3201_handle_t *out_handle, const mcp3201_config_t *cfg);
00076
00083 esp_err_t mcp3201_exit(mcp3201_handle_t mcp_handle);
00084
00092 esp_err_t mcp3201_read(mcp3201_handle_t handle, uint16_t *out_value);
00103 mcp3201_sampler_t *mcp3201_sampler_start(mcp3201_handle_t mcp_handle, QueueHandle_t recv_queue, const
       size_t buffer_size, const size_t f_sample);
00104
00110 void mcp3201_sampler_stop(mcp3201_sampler_t *sampler);
00111
00112 #endif // MCP3201_H
```

4.17 lib/mcp3201/mcp3201_sampler.c File Reference

MCP3201 Sampler.

```
#include "mcp3201.h"
```

Data Structures

struct mcp3201_context_t
 MCP3201 Context struct for internal use.

Macros

- #define RESAMPLE_DENOMINATOR 2
- #define READER_TIMEOUT_MS 10
- #define READER_TIMEOUT_TICKS (READER_TIMEOUT_MS / portTICK_PERIOD_MS)

Typedefs

typedef struct mcp3201_context_t mcp3201_context_t

Functions

mcp3201_sampler_t * mcp3201_sampler_start (mcp3201_handle_t mcp_handle, QueueHandle_t recv_
 queue, const size_t buffer_size, const size_t f_sample)

Starts the MCP3201 Sampler, which samples continuously and puts the samples into a queue.

void mcp3201_sampler_stop (mcp3201_sampler_t *sampler)

Stops the MCP3201 Sampler.

4.17.1 Detailed Description

MCP3201 Sampler.

Author

@s-grundner

Version

0.1

Date

2023-03-26

Copyright

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Definition in file mcp3201_sampler.c.

4.17.2 Macro Definition Documentation

4.17.2.1 READER_TIMEOUT_MS

```
#define READER_TIMEOUT_MS 10
```

Definition at line 14 of file mcp3201_sampler.c.

4.17.2.2 READER_TIMEOUT_TICKS

```
#define READER_TIMEOUT_TICKS (READER_TIMEOUT_MS / portTICK_PERIOD_MS)
```

Definition at line 15 of file mcp3201_sampler.c.

4.17.2.3 RESAMPLE_DENOMINATOR

```
#define RESAMPLE_DENOMINATOR 2
```

Definition at line 13 of file mcp3201_sampler.c.

4.17.3 Typedef Documentation

4.17.3.1 mcp3201_context_t

```
typedef struct mcp3201_context_t mcp3201_context_t
```

Definition at line 24 of file mcp3201_sampler.c.

4.17.4 Function Documentation

4.17.4.1 mcp3201_sampler_start()

Starts the MCP3201 Sampler, which samples continuously and puts the samples into a queue.

Parameters

mcp_handle	MCP3201 Device Handler
recv_queue	queue to send the samples into
buffer_size	size of the audio buffer
f_sample	Sample rate

Returns

mcp3201_sampler_t* Sampler Handler

Definition at line 84 of file mcp3201_sampler.c.

4.17.4.2 mcp3201_sampler_stop()

Stops the MCP3201 Sampler.

Parameters

sampler	Sampler Handler to stop
---------	-------------------------

Definition at line 110 of file mcp3201_sampler.c.

4.18 mcp3201_sampler.c

Go to the documentation of this file.

```
00001
00011 #include "mcp3201.h"
00013 #define RESAMPLE_DENOMINATOR 2
00014 #define READER_TIMEOUT_MS 10
00015 #define READER_TIMEOUT_TICKS (READER_TIMEOUT_MS / portTICK_PERIOD_MS)
00016
00017 static const char *TAG = "MCP3201_SAMPLER";
00018 struct mcp3201_context_t
00019 {
00020
         mcp3201_config_t cfg;
00021
         spi_device_handle_t spi;
00022
         spi_transaction_t *ongoing_transaction;
00023 };
00024 typedef struct mcp3201_context_t mcp3201_context_t;
00025
00026 static TaskHandle_t sampler_task_handle;
00027 static TaskHandle_t reader_task_handle;
00028
00029 static void IRAM_ATTR sampler_task(void *arg)
00030 {
00031
          mcp3201_sampler_t *sampler = (mcp3201_sampler_t *)arg;
00032
          for (;;)
00033
00034
              spi_event_t evt;
00035
              if (xQueueReceive(sampler->dma_queue, &evt, portMAX_DELAY) == pdTRUE)
00036
              {
00037
                  if (evt == SPI_EV_SEND_DMA_READY)
```

```
{
00039
                       size t bytes read = 0;
00040
00041
                       {
                           // fill audio buffer
00042
                           size_t bytes_to_read = RESAMPLE_DENOMINATOR * (sampler->buffer_size -
00043
       sampler->buffer_pos);
00044
                           void *buffer_position = (void *) (sampler->buffer + sampler->buffer_pos);
00045
                           // read data from spi
00046
00047
                           spi_transaction_t t = {
                               .user = (void *)sampler->mcp_handle,
00048
                                .length = bytes_to_read,
00049
                               .rx_buffer = buffer_position,
00050
00051
00052
                           sampler->mcp_handle->ongoing_transaction = &t;
00053
                           spi_device_get_trans_result(
00054
                               sampler->mcp handle->spi,
00055
                                (spi_transaction_t **)(sampler->mcp_handle->ongoing_transaction),
00056
                                READER_TIMEOUT_TICKS);
00057
                           bytes_read = t.rxlength;
00058
00059
                           sampler->buffer_pos += bytes_read / RESAMPLE_DENOMINATOR;
00060
00061
                           if (sampler->buffer_pos == sampler->buffer_size)
00062
                           {
00063
                                // send data to DSP queue
00064
                                sampler->buffer_pos = 0;
00065
                               xQueueSend(sampler->dsp_queue, &sampler->buffer, portMAX_DELAY);
00066
00067
                       } while (bytes read > 0);
00068
                  }
00069
00070
00071 }
00072
00073 static void IRAM ATTR reader task(void *arg)
00074 {
00075
          mcp3201_sampler_t *sampler = (mcp3201_sampler_t *)arg;
00076
          for (;;)
00077
00078
              spi_device_queue_trans(sampler->mcp_handle->spi, sampler->mcp_handle->ongoing_transaction,
       portMAX_DELAY);
00079
              spi_event_t evt = SPI_EV_SEND_DMA_READY;
08000
              xQueueSendFromISR(sampler->dma_queue, &evt, NULL);
00081
00082 }
00083
00084 mcp3201_sampler_t *mcp3201_sampler_start(mcp3201_handle_t mcp_handle, QueueHandle_t recv_queue, const
       size_t buffer_size, const size_t f_sample)
00085 {
00086
           if (mcp_handle == NULL || recv_queue == NULL || buffer_size == 0 || f_sample == 0)
00087
00088
              ESP_LOGE(TAG, "Invalid arguments");
00089
              return NULL:
00090
          }
00091
00092
          mcp3201_sampler_t *sampler = (mcp3201_sampler_t *) malloc(sizeof(mcp3201_sampler_t));
00093
          *sampler = (mcp3201_sampler_t) {
              .mcp_handle = mcp_handle,
.buffer_size = buffer_size,
00094
00095
00096
              .buffer = (size_t *)malloc(sizeof(size_t) * buffer_size),
00097
              .buffer_pos = 0,
00098
              .dma_queue = xQueueCreate(4, sizeof(spi_event_t)),
00099
               .dsp_queue = recv_queue};
00100
          while (spi_device_acquire_bus(mcp_handle->spi, portMAX_DELAY) != ESP_OK)
    ESP_LOGE(TAG, "Failed to acquire bus\n retrying...");
00101
00102
00103
00104
          xTaskCreatePinnedToCore(sampler_task, "sampler_task", RESAMPLE_DENOMINATOR * buffer_size, sampler,
       5, &sampler_task_handle, 0);
00105
          xTaskCreatePinnedToCore(reader_task, "reader_task", 2048, sampler, 5, &reader_task_handle, 0);
00106
00107
          return sampler:
00108 }
00109
00110 void mcp3201_sampler_stop(mcp3201_sampler_t *sampler)
00111 {
00112
          vQueueDelete(sampler->dma_queue);
00113
          vQueueDelete(sampler->dsp_queue);
00114
00115
          spi_device_release_bus(sampler->mcp_handle->spi);
00116
00117
          vTaskDelete(sampler_task_handle);
00118
          vTaskDelete(reader_task_handle);
00119
00120
          free(sampler->buffer);
```

4.19 lib/midi/midi.c File Reference

MIDI UART Driver Source for ESP32.

```
#include "midi.h"
```

Data Structures

· struct midi_context_t

MIDI Context (internal! not to be accessed externally, use midi_handle_t instead)

Macros

- #define MIDI_BYTE_SIZE_DEFAULT 3
- #define MIDI_BYTE_SIZE_SHORT 2

Typedefs

typedef struct midi_context_t midi_context_t

Functions

```
    esp_err_t midi_init (midi_context_t **out_ctx, midi_config_t *out_cfg)
```

• esp_err_t midi_exit (midi_handle_t midi_handle)

Exits MIDI and frees all resources.

• esp_err_t midi_write (midi_handle_t handle, midi_message_t *msg)

Writes MIDI Message to UART.

• esp_err_t midi_read (midi_handle_t midi_handle, midi_message_t *msg, TickType_t timeout)

Reads MIDI Message from UART.

4.19.1 Detailed Description

MIDI UART Driver Source for ESP32.

Author

@s-grundner

Version

0.1

Date

2022-12-23

Copyright

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Definition in file midi.c.

4.19.2 Macro Definition Documentation

4.19.2.1 MIDI_BYTE_SIZE_DEFAULT

```
#define MIDI_BYTE_SIZE_DEFAULT 3
```

Definition at line 13 of file midi.c.

4.19.2.2 MIDI_BYTE_SIZE_SHORT

```
#define MIDI_BYTE_SIZE_SHORT 2
```

Definition at line 14 of file midi.c.

4.19.3 Typedef Documentation

4.19.3.1 midi_context_t

```
typedef struct midi_context_t midi_context_t
```

4.19.4 Function Documentation

4.19.4.1 midi_exit()

Exits MIDI and frees all resources.

Parameters

∟ <i>midi_handle</i> ∟ MID). Handle to be treed	midi handle	MIDI Handle to be freed
---	-------------	-------------------------

Returns

esp_err_t

Definition at line 80 of file midi.c.

4.19.4.2 midi_init()

Definition at line 33 of file midi.c.

4.19.4.3 midi_read()

Reads MIDI Message from UART.

Parameters

midi_handle	MIDI Handle to pass parameters
msg	MIDI Message to be read

Returns

```
esp_err_t
```

Definition at line 133 of file midi.c.

4.19.4.4 midi_write()

Writes MIDI Message to UART.

Parameters

midi_handle	MIDI Handle to pass parameters
msg	MIDI Message to be sent

Returns

esp_err_t

Definition at line 92 of file midi.c.

4.20 midi.c

Go to the documentation of this file.

```
00011 #include "midi.h"
00012
00013 #define MIDI_BYTE_SIZE_DEFAULT 3
00014 #define MIDI_BYTE_SIZE_SHORT 2
00016 static const char *TAG = "MIDI";
00017 static const char *MIDI_MON = "MIDI MONITOR";
00018
00024 typedef struct midi_context_t
00025 {
00026
          midi_config_t cfg;
00027 } midi_context_t;
00028
00029 // -----
00030 // MIDI CONFIG
00031 // ----
00032
00033 esp_err_t midi_init(midi_context_t **out_ctx, midi_config_t *out_cfg)
00034 {
00035
          \ensuremath{//} Allocate memory for context
00036
          midi_context_t *ctx = (midi_context_t *)malloc(sizeof(midi_context_t));
00037
          if (!ctx)
00038
              return ESP_ERR_NO_MEM;
00039
00040
          *ctx = (midi_context_t) {
00041
               .cfg = *out_cfg};
00042
         ESP_LOGI(TAG, "Initializing MIDI on %d (rx:%d, tx:%d) with %d baud...", ctx->cfg.uart_num,
00043
       ctx->cfg.rx_io, ctx->cfg.tx_io, ctx->cfg.baudrate);
00044
00045
          // Configure UART
00046
          gpio_config_t rx_pin_config = {
00047
              .pin_bit_mask = (1ULL « ctx->cfg.rx_io),
              .mode = GPIO_MODE_INPUT,
.pull_up_en = GPIO_PULLUP_DISABLE,
00048
00049
              .pull_down_en = GPIO_PULLDOWN_DISABLE,
.intr_type = GPIO_INTR_DISABLE};
00050
00051
00052
00053
          gpio_config_t tx_pin_config = {
00054
            .pin_bit_mask = (1ULL « ctx->cfg.tx_io),
               .mode = GPIO_MODE_OUTPUT,
00055
               .pull_up_en = GPIO_PULLUP_DISABLE,
00056
00057
               .pull_down_en = GPIO_PULLDOWN_DISABLE,
00058
               .intr_type = GPIO_INTR_DISABLE;;
00059
00060
          ESP_ERROR_CHECK(gpio_config(&rx_pin_config));
00061
          ESP_ERROR_CHECK(gpio_config(&tx_pin_config));
00062
00063
          uart_config_t uart_config = {
00064
              .baud_rate = ctx->cfg.baudrate,
00065
               .data_bits = UART_DATA_8_BITS,
00066
               .parity = UART_PARITY_DISABLE,
              .stop_bits = UART_STOP_BITS_1,
.flow_ctrl = UART_HW_FLOWCTRL_DISABLE,
00067
00068
00069
               .source_clk = UART_SCLK_APB};
00070
00071
          ESP_ERROR_CHECK(uart_param_config(ctx->cfg.uart_num, &uart_config));
00072
          ESP_ERROR_CHECK(uart_set_pin(ctx->cfg.uart_num, ctx->cfg.tx_io, ctx->cfg.rx_io,
       UART_PIN_NO_CHANGE, UART_PIN_NO_CHANGE));
00073
          ESP_ERROR_CHECK(uart_driver_install(ctx->cfg.uart_num, 1024 * 2, 1024 * 2, 0, NULL, 0));
00074
00075
          // Pass configured context to outer parameters
00076
          *out_ctx = ctx;
00077
          return ESP_OK;
00078 }
00079
00080 esp_err_t midi_exit(midi_handle_t midi_handle)
00081 {
00082
          esp_err_t err = ESP_OK;
```

4.20 midi.c 97

```
err = uart_driver_delete(midi_handle->cfg.uart_num);
00084
          free (midi_handle);
00085
          return err;
00086 }
00087
00088 //
00089 // MIDI TRANSMISSIONS
00090 //
00091
00092 esp_err_t midi_write(midi_handle_t handle, midi_message_t *msg)
00093 {
00094
          int len = 0:
00095
          const char data[] = {msg->status | msg->channel, msg->param1, msg->param2};
00096
00097
          // switch status to determine message length
00098
          switch (msg->status)
00099
00100
          case MIDI STATUS NOTE OFF:
          case MIDI_STATUS_NOTE_ON:
00101
00102
          case MIDI_STATUS_CONTROL_CHANGE:
00103
          case MIDI_STATUS_PITCH_BEND:
00104
          case MIDI_STATUS_POLYPHONIC_KEY_PRESSURE:
00105
              len = uart_write_bytes(handle->cfg.uart_num, data, MIDI_BYTE_SIZE_DEFAULT);
00106
              break;
00107
          case MIDI_STATUS_PROGRAM_CHANGE:
          case MIDI_STATUS_CHANNEL_PRESSURE:
00108
00109
              len = uart_write_bytes(handle->cfg.uart_num, data, MIDI_BYTE_SIZE_SHORT);
00110
              break;
00111
          default:
             ESP_LOGE(TAG, "midi_send: invalid status: %02X", msg->status);
00112
00113
              return ESP_ERR_INVALID_ARG;
00114
              break;
00115
00116
          switch (len)
00117
          case -1:
00118
             ESP_LOGE(TAG, "uart_write_bytes failed");
00119
              return ESP_FAIL;
00121
              break;
00122
          case 0:
             ESP_LOGE(TAG, "uart_write_bytes timed out");
00123
              return ESP_ERR_TIMEOUT;
00124
00125
              break:
00126
          default:
              // ESP_LOGI(MIDI_MON, "Status: %02X\tChannel: %02X\t Data: %02X %02X\t Length:%d",
00127
       msg->status, msg->channel, msg->param1, msg->param2, len);
00128
             break;
00129
          return ESP OK:
00130
00131 }
00132
00133 esp_err_t midi_read(midi_handle_t midi_handle, midi_message_t *msg, TickType_t timeout)
00134 {
00135
          char data[3];
          int len = uart_read_bytes(midi_handle->cfg.uart_num, (uint8_t *)data, 3, timeout);
00136
00137
          switch (len)
00138
00139
          case -1:
00140
             ESP_LOGE(TAG, "uart_read_bytes failed");
00141
              return ESP_FAIL;
00142
             break:
00143
          case 0:
00144
             ESP_LOGE(TAG, "uart_read_bytes timeout");
00145
              return ESP_ERR_TIMEOUT;
00146
             break;
00147
          case 2:
00148
             msg->status = data[0] & 0xF0;
              msg->channel = data[0] & 0x0F;
00149
              msg->param1 = data[1];
00150
              msg->param2 = 0;
00151
00152
              break;
00153
          case 3:
00154
              msg->status = data[0] & 0xF0;
              msg->channel = data[0] & 0x0f;
msg->param1 = data[1];
msg->param2 = data[2];
00155
00156
00157
00158
              break;
00159
              ESP_LOGE(TAG, "uart_read_bytes invalid message");
00160
              return ESP_ERR_INVALID_ARG;
00161
00162
              break;
00163
00164
          return ESP_OK;
00165 }
```

lib/midi/midi.h File Reference 4.21

MIDI UART Driver for ESP32.

```
#include <stdio.h>
#include <stdint.h>
#include "driver/gpio.h"
#include "driver/uart.h"
#include "esp_log.h"
```

Data Structures

```
· struct midi_message_t
     MIDI Message.

    struct midi_config_t

     MIDI UART Configuration.
```

Macros

- #define MIDI_LOG_LEVEL ESP_LOG_ERROR
- #define MIDI BYTE SIZE DEFAULT 3
- #define MIDI BYTE SIZE SHORT 2
- #define MIDI PITCH BEND MIN (0)
- #define MIDI PITCH BEND MAX (16383)
- #define MIDI PITCH BEND CENTER (8192)

Typedefs

typedef struct midi_context_t * midi_handle_t

Enumerations

```
• enum midi status t {
 MIDI_STATUS_NOTE_OFF = 0x80, MIDI_STATUS_NOTE_ON = 0x90, MIDI_STATUS_POLYPHONIC_KEY_PRESSURE
 = 0xA0, MIDI_STATUS_CONTROL_CHANGE = 0xB0,
 MIDI_STATUS_PROGRAM_CHANGE = 0xC0 , MIDI_STATUS_CHANNEL_PRESSURE = 0xD0 ,
 MIDI_STATUS_PITCH_BEND = 0xE0 }
    MIDI Status Bytes.
```

Functions

```
    esp err t midi init (midi handle t *out handle, midi config t *out cfg)

     initializes MIDI and allocates driver resources
• esp_err_t midi_exit (midi_handle_t midi_handle)
     Exits MIDI and frees all resources.

    esp_err_t midi_write (midi_handle_t midi_handle, midi_message_t *msg)

     Writes MIDI Message to UART.

    esp_err_t midi_read (midi_handle_t midi_handle, midi_message_t *msg, TickType_t timeout)

     Reads MIDI Message from UART.

    midi message t note off (uint8 t channel, uint8 t key num, uint8 t velocity)

• midi message t note on (uint8 t channel, uint8 t key num, uint8 t velocity)
• midi message t poly key pressure (uint8 t channel, uint8 t key num, uint8 t value)

    midi message t ctrl change (uint8 t channel, uint8 t controller num, uint8 t value)

• midi_message_t prg_change (uint8_t channel, uint8_t program)
```

• midi_message_t channel_pressure (uint8_t channel, uint8_t value) midi_message_t pitch_bend (uint8_t channel, uint16_t value)

4.21.1 Detailed Description

MIDI UART Driver for ESP32.

Author

@s-grundner

Version

0.1

Date

2022-12-23

Copyright

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Definition in file midi.h.

4.21.2 Macro Definition Documentation

4.21.2.1 MIDI_BYTE_SIZE_DEFAULT

```
#define MIDI_BYTE_SIZE_DEFAULT 3
```

Definition at line 23 of file midi.h.

4.21.2.2 MIDI_BYTE_SIZE_SHORT

```
#define MIDI_BYTE_SIZE_SHORT 2
```

Definition at line 24 of file midi.h.

4.21.2.3 MIDI_LOG_LEVEL

```
#define MIDI_LOG_LEVEL ESP_LOG_ERROR
```

Definition at line 21 of file midi.h.

4.21.2.4 MIDI_PITCH_BEND_CENTER

#define MIDI_PITCH_BEND_CENTER (8192)

Definition at line 28 of file midi.h.

4.21.2.5 MIDI_PITCH_BEND_MAX

#define MIDI_PITCH_BEND_MAX (16383)

Definition at line 27 of file midi.h.

4.21.2.6 MIDI_PITCH_BEND_MIN

#define MIDI_PITCH_BEND_MIN (0)

Definition at line 26 of file midi.h.

4.21.3 Typedef Documentation

4.21.3.1 midi_handle_t

typedef struct midi_context_t* midi_handle_t

Definition at line 85 of file midi.h.

4.21.4 Enumeration Type Documentation

4.21.4.1 midi_status_t

enum midi_status_t

MIDI Status Bytes.

Parameters

MIDI_STATUS_NOTE_OFF	0x80, requires param2
MIDI_STATUS_NOTE_ON	0x90, requires param2
MIDI_STATUS_POLYPHONIC_KEY_PRESSURE	0xA0, param2 is not used
MIDI_STATUS_CONTROL_CHANGE	0xB0, requires param2
MIDI_STATUS_PROGRAM_CHANGE	0xC0, param2 is is not used
MIDI_STATUS_CHANNEL_PRESSURE	0xD0, param2 is is not used

Generated by Doxygen

Enumerator

MIDI_STATUS_NOTE_OFF	
MIDI_STATUS_NOTE_ON	
MIDI_STATUS_POLYPHONIC_KEY_PRESSURE	
MIDI_STATUS_CONTROL_CHANGE	
MIDI_STATUS_PROGRAM_CHANGE	
MIDI_STATUS_CHANNEL_PRESSURE	
MIDI_STATUS_PITCH_BEND	

Definition at line 41 of file midi.h.

4.21.5 Function Documentation

4.21.5.1 channel_pressure()

Definition at line 67 of file midi_utils.c.

4.21.5.2 ctrl_change()

Definition at line 47 of file midi_utils.c.

4.21.5.3 midi_exit()

Exits MIDI and frees all resources.

Parameters

midi handle	MIDI Handle to be freed

Returns

```
esp_err_t
```

Definition at line 80 of file midi.c.

4.21.5.4 midi_init()

initializes MIDI and allocates driver resources

Parameters

out	out_handle	MIDI Handle to be initialized
out	out_cfg	MIDI Configuration

Returns

```
esp_err_t
```

4.21.5.5 midi_read()

Reads MIDI Message from UART.

Parameters

midi_handle	MIDI Handle to pass parameters
msg	MIDI Message to be read

Returns

esp_err_t

Definition at line 133 of file midi.c.

4.21.5.6 midi_write()

Writes MIDI Message to UART.

Parameters

midi_handle	MIDI Handle to pass parameters
msg	MIDI Message to be sent

Returns

```
esp_err_t
```

Definition at line 92 of file midi.c.

4.21.5.7 note_off()

Definition at line 17 of file midi_utils.c.

4.21.5.8 note_on()

Definition at line 27 of file midi_utils.c.

4.21.5.9 pitch_bend()

Definition at line 77 of file midi_utils.c.

4.21.5.10 poly_key_pressure()

Definition at line 37 of file midi_utils.c.

4.21.5.11 prg change()

Definition at line 57 of file midi_utils.c.

4.22 midi.h

Go to the documentation of this file.

```
00001
00012 #ifndef MIDI_DRIVER_H
00013 #define MIDI_DRIVER_H
00014
00015 #include <stdio.h>
00016 #include <stdint.h>
00017 #include "driver/gpio.h"
00018 #include "driver/uart.h"
00019 #include "esp_log.h"
00020
00021 #define MIDI_LOG_LEVEL ESP_LOG_ERROR
00022
00023 #define MIDI_BYTE_SIZE_DEFAULT 3
00024 #define MIDI_BYTE_SIZE_SHORT 2
00025
00026 #define MIDI_PITCH_BEND_MIN (0)
00027 #define MIDI_PITCH_BEND_MAX (16383)
00028 #define MIDI_PITCH_BEND_CENTER (8192)
00029
00041 typedef enum
00042 {
00043
           MIDI_STATUS_NOTE_OFF = 0x80,
00044
           MIDI\_STATUS\_NOTE\_ON = 0x90,
           MIDI_STATUS_POLYPHONIC_KEY_PRESSURE = 0xA0,
00045
          MIDI_STATUS_CONTROL_CHANGE = 0xB0,
MIDI_STATUS_PROGRAM_CHANGE = 0xC0,
00046
00047
        MIDI_STATUS_CHANNEL_PRESSURE = 0xD0,
00048
           MIDI_STATUS_PITCH_BEND = 0xE0,
00050 } midi_status_t;
00051
00060 typedef struct
00061 {
00062
           uint8 t param1;
00063
           midi_status_t status;
00064
           uint8_t channel;
00065
           uint8_t param2;
00066 } midi_message_t;
00067
00076 typedef struct
00077 {
00078
           uart_port_t uart_num;
00079
           uint baudrate;
00080
           gpio_num_t rx_io;
00081
           gpio_num_t tx_io;
00082 } midi_config_t;
00085 typedef struct midi_context_t *midi_handle_t;
```

```
00086
00094 esp_err_t midi_init(midi_handle_t *out_handle, midi_config_t *out_cfg);
00095
00102 esp_err_t midi_exit(midi_handle_t midi_handle);
00103
00111 esp_err_t midi_write(midi_handle_t midi_handle, midi_message_t *msg);
00112
00120 esp_err_t midi_read(midi_handle_t midi_handle, midi_message_t *msg, TickType_t timeout);
00121
00122 // functions to configure midi messages
00123 midi_message_t note_off(uint8_t channel, uint8_t key_num, uint8_t velocity);
00124 midi_message_t note_on(uint8_t channel, uint8_t key_num, uint8_t velocity);
00125 midi_message_t poly_key_pressure(uint8_t channel, uint8_t key_num, uint8_t value);
00126 midi_message_t ctrl_change(uint8_t channel, uint8_t controller_num, uint8_t value);
00127 midi_message_t prg_change(uint8_t channel, uint8_t program);
00128 midi_message_t channel_pressure(uint8_t channel, uint8_t value);
00129 midi_message_t pitch_bend(uint8_t channel, uint16_t value);
00130
00131 #endif // MIDI_DRIVER_H
```

4.23 lib/midi/midi_utils.c File Reference

```
MIDI Message Utilities.
```

```
#include "midi.h"
```

Functions

- midi_message_t note_off (uint8_t channel, uint8_t key_num, uint8_t velocity)
- midi message t note on (uint8 t channel, uint8 t key num, uint8 t velocity)
- midi_message_t poly_key_pressure (uint8_t channel, uint8_t key_num, uint8_t value)
- midi message t ctrl change (uint8 t channel, uint8 t controller num, uint8 t value)
- midi_message_t prg_change (uint8_t channel, uint8_t program)
- midi_message_t channel_pressure (uint8_t channel, uint8_t value)
- midi_message_t pitch_bend (uint8_t channel, uint16_t value)

4.23.1 Detailed Description

MIDI Message Utilities.

Author

@s-grundner

Version

0.1

Date

2023-03-26

Copyright

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Definition in file midi_utils.c.

4.23.2 Function Documentation

4.23.2.1 channel_pressure()

Definition at line 67 of file midi_utils.c.

4.23.2.2 ctrl_change()

Definition at line 47 of file midi_utils.c.

4.23.2.3 note_off()

Definition at line 17 of file midi_utils.c.

4.23.2.4 note_on()

Definition at line 27 of file midi_utils.c.

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4.23.2.5 pitch_bend()

Definition at line 77 of file midi_utils.c.

4.23.2.6 poly_key_pressure()

Definition at line 37 of file midi_utils.c.

4.23.2.7 prg_change()

Definition at line 57 of file midi utils.c.

4.24 midi_utils.c

Go to the documentation of this file.

```
00001
00011 #include "midi.h"
00012
00013 //
00014 // MIDI UTILS
00015 //
00016
00017 midi_message_t note_off(uint8_t channel, uint8_t key_num, uint8_t velocity)
00018 {
00019
         midi_message_t msg = {
            status = MIDI_STATUS_NOTE_OFF,
00021
             .channel = channel,
             .param1 = key_num,
00022
             .param2 = velocity};
00023
00024
         return msq;
00025 }
00026
00027 midi_message_t note_on(uint8_t channel, uint8_t key_num, uint8_t velocity)
00028 {
         midi_message_t msg = {
00029
           status = MIDI_STATUS_NOTE_ON,
00030
             .channel = channel,
00031
             .param1 = key_num,
00032
00033
             .param2 = velocity};
00034
         return msg;
00035 }
00036
00037 midi_message_t poly_key_pressure(uint8_t channel, uint8_t key_num, uint8_t value)
00038 {
00039
         midi_message_t msg = {
```

```
.status = MIDI_STATUS_POLYPHONIC_KEY_PRESSURE,
00041
              .channel = channel,
             .param1 = key_num,
.param2 = value);
00042
00043
00044
          return msg;
00045 }
00047 midi_message_t ctrl_change(uint8_t channel, uint8_t controller_num, uint8_t value)
00048 {
00049
          midi_message_t msg = {
           status = MIDI_STATUS_CONTROL_CHANGE,
00050
              .channel = channel,
00051
             .param1 = controller_num,
00052
00053
              .param2 = value);
00054
          return msg;
00055 }
00056
00057 midi_message_t prg_change(uint8_t channel, uint8_t program)
00058 {
          midi_message_t msg = {
             .status = MIDI_STATUS_PROGRAM_CHANGE,
00060
              .channel = channel,
00061
              .param1 = program,
.param2 = 0;;
00062
00063
00064
          return msq;
00065 }
00066
00067 midi_message_t channel_pressure(uint8_t channel, uint8_t value)
00068 {
          midi_message_t msg = {
    .status = MIDI_STATUS_CHANNEL_PRESSURE,
00069
00070
              .channel = channel,
00072
              .param1 = value,
              .param2 = 0;
00073
00074
          return msg;
00075 }
00076
00077 midi_message_t pitch_bend(uint8_t channel, uint16_t value)
00078 {
00079
          midi_message_t msg = {
         .status = MIDI_STATUS_PITCH_BEND,
.channel = channel,
00080
00081
             .param1 = value & 0x7F,
00082
              .param2 = (value » 7) & 0x7F};
00083
00084
          return msg;
00085 }
```

4.25 src/gitcon.c File Reference

Gitcon Driver Source.

```
#include "gitcon.h"
#include "processed-data.h"
```

Macros

- #define FLOAT_TO_UINT16(x) ((uint16_t)((x)*32767.0f))
- #define UINT16_TO_FLOAT(x) ((float)(x) / 32767.0f)
- #define SENSITIVITY 0.5f
- #define MIDI LOWEST NOTE 21
- #define MIDI HIGHEST NOTE 108
- #define MIDI_KEY_BOUNDARY(x) ((x) < MIDI_LOWEST_NOTE || (x) > MIDI_HIGHEST_NOTE)
- #define CONCERT_A 440.0f
- #define CONCERT_A_NOTE 69

Functions

```
esp_err_t gitcon_init (gitcon_context_t **out_handle)esp_err_t gitcon_exit (gitcon_handle_t handle)
```

frees all resources

4.25.1 Detailed Description

Gitcon Driver Source.

Author

@s-grundner @Laurenz03

Version

0.1

Date

2022-12-23

Copyright

Copyright (c) 2022

Definition in file gitcon.c.

4.25.2 Macro Definition Documentation

4.25.2.1 CONCERT_A

#define CONCERT_A 440.0f

Definition at line 26 of file gitcon.c.

4.25.2.2 CONCERT_A_NOTE

#define CONCERT_A_NOTE 69

Definition at line 27 of file gitcon.c.

4.25.2.3 FLOAT_TO_UINT16

Definition at line 20 of file gitcon.c.

4.25.2.4 MIDI_HIGHEST_NOTE

```
#define MIDI_HIGHEST_NOTE 108
```

Definition at line 24 of file gitcon.c.

4.25.2.5 MIDI_KEY_BOUNDARY

```
#define MIDI_KEY_BOUNDARY(  x \ ) \ ((x) \ < \ \mbox{MIDI_LOWEST_NOTE} \ || \ (x) \ > \ \mbox{MIDI_HIGHEST_NOTE})
```

Definition at line 25 of file gitcon.c.

4.25.2.6 MIDI_LOWEST_NOTE

```
#define MIDI_LOWEST_NOTE 21
```

Definition at line 23 of file gitcon.c.

4.25.2.7 SENSITIVITY

```
#define SENSITIVITY 0.5f
```

Definition at line 22 of file gitcon.c.

4.25.2.8 UINT16_TO_FLOAT

```
#define UINT16_TO_FLOAT( x ) ((float)(x) / 32767.0f)
```

Definition at line 21 of file gitcon.c.

4.25.3 Function Documentation

4.25.3.1 gitcon_exit()

frees all resources

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Parameters

handle	gitcon context handler
--------	------------------------

Returns

ESP_OK on success

Definition at line 271 of file gitcon.c.

4.25.3.2 gitcon_init()

Note

DSP task: receives audio data from DMA task and sends audio data to MIDI task MIDI task: receives midi messages from DSP task and sends them to MIDI UART

Definition at line 196 of file gitcon.c.

4.26 gitcon.c

Go to the documentation of this file.

```
00001
00012 #include "gitcon.h"
00013 #include "processed-data.h"
00014
00015 static const char *TAG = "gitcon";
00016
00017 static TaskHandle_t midi_task_handle;
00018 static TaskHandle_t dsp_task_handle;
00019
00020 #define FLOAT_TO_UINT16(x) ((uint16_t)((x)*32767.0f))
00021 #define UINT16_TO_FLOAT(x) ((float)(x) / 32767.0f)
00022 #define SENSITIVITY 0.5f
00023 #define MIDI_LOWEST_NOTE 21
00024 #define MIDI_HIGHEST_NOTE 108
00025 #define MIDI_KEY_BOUNDARY(x) ((x) < MIDI_LOWEST_NOTE || (x) > MIDI_HIGHEST_NOTE)
00026 #define CONCERT_A 440.0f
00027 #define CONCERT_A_NOTE 69
00028
00029 // uncomment to enable debug output for better_serial_plotter software
00030 // #define DEBUG_BETTER_SERIAL_PLOTTER
00031
00032 // uncomment to enable debug output for dsp_task
00033 // #define DEBUG_DSP
00034
00035 // -----
00036 // static functions
00037 // ---
00038
00043 static void dsp_task(void *arg)
00044 {
00045
           // gitcon driver context handler
00046
          gitcon_handle_t gitcon_handle = (gitcon_handle_t)arg;
00047
00048
          // audio buffer variables
00049
          uint16_t *audio_buffer = NULL;
00050
          float *audio_buffer_float = (float *)malloc(FFT_SIZE * sizeof(float));
```

```
if (audio_buffer_float == NULL)
00052
               ESP_LOGE(TAG, "Could not allocate memory for audio_buffer_float");
00053
               gitcon_exit(gitcon_handle);
00054
00055
               return;
00056
          }
00057
00058
          // fft variables
00059
          float fft_buffer[FFT_SIZE];
          float magnitude[FFT_SIZE / 2];
float frequency[FFT_SIZE / 2];
00060
00061
          unsigned char keyNR[FFT_SIZE / 2];
00062
00063
          float ratio = (float)F_SAMPLE_HZ / (float)FFT_SIZE;
00064
00065
           // active notes resulting from fft
00066
          midi_message_t *active_notes = (midi_message_t *)malloc(128 * sizeof(midi_message_t));
00067
          if (active_notes == NULL)
00068
          {
00069
               ESP_LOGE(TAG, "Could not allocate memory for active_notes");
00070
              gitcon_exit(gitcon_handle);
00071
00072
          }
00073
          // initialize active_notes
for (int i = 0; i < 128; i++)</pre>
00074
00075
00076
00077
               active_notes[i].channel = 0;
00078
               active_notes[i].status = MIDI_STATUS_NOTE_OFF;
               active_notes[i].param1 = i;
00079
00080
               active_notes[i].param2 = 0;
00081
          }
00082
00083
          // window counter to sweep through the audio_buffer_float
00084
          char window_counter = 0;
00085
00086
          for (;;)
00087
               // delay to avoid overflow and to allow other tasks to run
00089
               vTaskDelay(10 / portTICK_PERIOD_MS);
00090
00091
               // get audio buffer from sampler
               if (xQueueReceive(gitcon_handle->sampler->dsp_queue, &audio_buffer, portMAX_DELAY) == pdFALSE)
00092
00093
                   continue; // skip iteration if queue is empty
00094
00097
               float *start_pos = audio_buffer_float;
00098
               audio_buffer_float += (AUDIO_BUFFER_SIZE * window_counter); // move pointer to the next window
00099
               window_counter = (window_counter + 1) % (FFT_WINDOW_SIZE); // increment window counter
00100
               // starting in a new window and fill the buffer with the new data
00101
               for (int i = 0; i < AUDIO_BUFFER_SIZE; i++)
    audio_buffer_float[i] = UINT16_TO_FLOAT(audio_buffer[i]);</pre>
00102
00103
00104
               audio_buffer_float = start_pos;
00105
00106 #ifdef DEBUG_BETTER_SERIAL_PLOTTER
               for (int i = 0; i < FFT_SIZE; i++)</pre>
00107
                  printf("%f\n", audio_buffer_float[i]); // for debugging in BetterSerialPlotter
00108
00111
              fft_config_t *fft_plan = fft_init(FFT_SIZE, FFT_REAL, FFT_FORWARD, audio_buffer_float,
       fft_buffer);
00114
              if (fft_plan == NULL)
00115
               {
00116
                   ESP_LOGE(TAG, "FFT plan could not be created");
                   vTaskDelay(1000 / portTICK_PERIOD_MS);
00117
00118
00119
00120
               fft execute(fft plan);
00121
               bool invalid_key = false; // invalid key flag
00122
               for (int k = 1; k < FFT_SIZE / 2; k++)</pre>
00124
00125
                   // detect fundamental frequencies
00126
                   frequency[k] = k * ratio;
00127
                   // convert to note number on piano roll
                   keyNR[k] = (unsigned char)round(log2(frequency[k] / CONCERT_A) * 12 + CONCERT_A_NOTE) %
00128
00129
                   // calculate magnitude (absolute value of complex number)
00130
                   magnitude[k] = 2 * sqrt(pow(fft_buffer[2 * k], 2) + pow(fft_buffer[2 * k + 1], 2)) /
       FFT_SIZE;
00131
00132
               // calculate max magnitude for thresholding
00134
               float max = 0;
00135
               for (int i = 0; i < FFT_SIZE / 2; i++)</pre>
00136
                  max = (magnitude[i] > max) ? magnitude[i] : max;
00137
00141
              if (max < 0.0005)
```

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```
max = 100;
00142
00143
00144
               // check if magnitudes pass a certain threshold
00145
               for (int k = 1; k < FFT\_SIZE / 2; k++)
00146
                   // switch off notes that are not active
00147
                   if ((magnitude[k] < max * SENSITIVITY) || MIDI_KEY_BOUNDARY(keyNR[k]))</pre>
00148
00149
00150
                       active_notes[keyNR[k]].status = MIDI_STATUS_NOTE_OFF;
00151
                       continue; // skip to next iteration threshold is not passed
00152
00153 #ifdef DEBUG DSP
                   ESP_LOGI(TAG, "keyNR: %d, magnitude: %f, frequency: %f", keyNR[k], magnitude[k],
00154
       frequency[k]);
00155 #endif
                   active_notes[keyNR[k]].status = MIDI_STATUS_NOTE_ON;
active_notes[keyNR[k]].param2 = (uint8_t) (magnitude[k] / max * 127);
00156
00157
00158
00159
              // send saved notes to MIDI queue
00160
               xQueueSend(gitcon_handle->midi_queue, &active_notes, portMAX_DELAY);
00161
               fft_destroy(fft_plan);
          } // for(;;)
00162
00163 } // dsp_task
00164
00165 static void midi_task(void *arg)
00166 {
00167
           // gitcon driver context handler
          gitcon_handle_t gitcon_handle = (gitcon_handle_t)arg;
midi_message_t *active_notes = NULL;
00168
00169
00170
          midi_status_t previous_states[128] = {0};
00171
          for (::)
00172
          {
00174
               vTaskDelay(10 / portTICK_PERIOD_MS);
00175
00176
               if (xQueueReceive(gitcon_handle->midi_queue, &active_notes, portMAX_DELAY) == pdFALSE)
00177
                   continue; // skip iteration if queue is empty
00178
00180
               // send MIDI messages to UART
00181
               for (size_t i = 0; i < 128; i++)</pre>
00182
00183
                   if (active_notes[i].status == previous_states[i])
                       continue; // continue if note has not changed
00184
                   // send message to MIDI UART
00185
00186
                   ESP_ERROR_CHECK(midi_write(gitcon_handle->midi_handle, &active_notes[i]));
                   previous_states[i] = active_notes[i].status;
00187
00188
00189
          } // for(;;)
00190 } // midi_task
00191
00192 //
00193 // non-static functions
00194 // --
00195
00196 esp_err_t gitcon_init(gitcon_context_t **out_handle)
00197 {
00198
          gitcon_context_t *gitcon_cfg = (gitcon_context_t *)malloc(sizeof(gitcon_context_t));
          if (!gitcon_cfg)
00199
00200
              return ESP_ERR_NO_MEM;
00201
00202
           // create queue for audio data (passed into sampler)
00203
          QueueHandle_t dsp_queue = xQueueCreate(10, sizeof(size_t *));
00204
00205
           // create queue for midi messages
00206
          gitcon_cfg->midi_queue = xQueueCreate(5, sizeof(midi_handle_t *));
00207
           if (!gitcon_cfg->midi_queue)
00208
              return ESP_ERR_NO_MEM;
00209
00210 #ifdef USE_MCP3201
00211
          // SPI
00212
00213
00214
          spi_bus_config_t bus_cfg = {
           .miso_io_num = SPI_MISO,
00215
              .mosi_io_num = SPI_MOSI,
00216
00217
               .sclk_io_num = SPI_SCLK,
00218
              .max_transfer_sz = 32,
00219
00220
          spi_bus_initialize(SPI_DEV, &bus_cfg, DMA_CHAN);
00221
00222
          // MCP3201 (ADC)
00223
00224
00225
          mcp3201_handle_t mcp_handle;
          mcp3201_config_t mcp_cfg = {
00226
              .host = SPI_DEV,
.cs_io = SPI_CS,
.miso_io = SPI_MISO,
00227
00228
00229
```

```
00230
              .mosi_io = SPI_MOSI);
00231
          // initialize ADC and store in gitcon handle
00232
          ESP_ERROR_CHECK(mcp3201_init(&mcp_handle, &mcp_cfg));
00233
          gitcon_cfg->sampler = mcp3201_sampler_start(mcp_handle, dsp_queue, AUDIO_BUFFER_SIZE,
       F SAMPLE HZ):
00234 #else
          gitcon_cfg->sampler = i2s_sampler_start(INTERNAL_ADC_CHANNEL, dsp_queue, AUDIO_BUFFER_SIZE,
00235
       F_SAMPLE_HZ);
00236 #endif
00237
00238
00239
          // MIDI
00240
00241
00242
          // Configure a handle parameter for MIDI \,
00243
          midi_handle_t midi_handle;
00244
          midi_config_t midi_cfg = {
            .uart_num = MIDI_UART,
.baudrate = MIDI_BAUD,
00245
             .rx_io = MIDI_RX,
00247
              .tx_io = MIDI_TX);
00248
          // Initialize MIDI and store in gitcon handle
00249
          ESP_ERROR_CHECK(midi_init(&midi_handle, &midi_cfg));
00250
00251
          gitcon_cfg->midi_handle = midi_handle;
00252
00253
00254
          // INIT RTOS
00255
00256
          ESP_LOGI(TAG, "Creating RTOS tasks...");
00257
          if (xTaskCreatePinnedToCore(dsp_task, "dsp_task", 1 « 16, gitcon_cfg, 5, &dsp_task_handle, 1) ==
00259
       pdFALSE)
00260
00261
00263
          if (xTaskCreatePinnedToCore(midi_task, "midi_task", 2048, gitcon_cfg, 5, &midi_task_handle, 0) ==
       pdFALSE)
00264
              return ESP ERR NO MEM;
00265
00266
          // Pass final configuration to outer parameters
00267
          *out_handle = gitcon_cfg;
00268
          return ESP_OK;
00269 }
00270
00271 esp_err_t gitcon_exit(gitcon_handle_t handle)
00272 {
00273
          ESP_ERROR_CHECK(midi_exit(handle->midi_handle));
00274
00275
          // stop tasks
00276
          vTaskDelete(dsp_task_handle);
          vTaskDelete(midi_task_handle);
00277
00278
00279
00280 #ifdef USE_MCP3201
00281
          mcp3201_sampler_stop(handle->sampler->mcp_handle);
          ESP_ERROR_CHECK(mcp3201_exit(handle->sampler->mcp_handle));
00282
00283 #else
          i2s_sampler_stop(handle->sampler);
00285 #endif
00286
00287
          free (handle);
00288
          return ESP_OK;
00289 }
```

4.27 src/gitcon.h File Reference

Gitcon Driver Header.

```
#include "config.h"
```

Data Structures

· struct gitcon_context_t

Gitcon Configuration.

Macros

• #define GITCON_LOG_LEVEL ESP_LOG_ERROR

Typedefs

typedef gitcon_context_t * gitcon_handle_t

Functions

```
    esp_err_t gitcon_init (gitcon_handle_t *out_handle)
    initializes gitcon device and installs peripheral drivers
```

esp_err_t gitcon_exit (gitcon_handle_t handle)
 frees all resources

4.27.1 Detailed Description

Gitcon Driver Header.

Author

@s-grundner @Laurenz03

Version

0.1

Date

2022-12-23

Copyright

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Definition in file gitcon.h.

4.27.2 Macro Definition Documentation

4.27.2.1 GITCON_LOG_LEVEL

#define GITCON_LOG_LEVEL ESP_LOG_ERROR

Definition at line 17 of file gitcon.h.

4.27.3 Typedef Documentation

4.27.3.1 gitcon_handle_t

```
typedef gitcon_context_t* gitcon_handle_t
```

Definition at line 37 of file gitcon.h.

4.27.4 Function Documentation

4.27.4.1 gitcon_exit()

frees all resources

Parameters

handle gitcon context hand	ller
----------------------------	------

Returns

ESP_OK on success

Definition at line 271 of file gitcon.c.

4.27.4.2 gitcon_init()

initializes gitcon device and installs peripheral drivers

Parameters

out	out_handle	gitcon context handler

4.28 gitcon.h 117

Returns

esp_err_t ESP_OK on success, ESP_ERR_NO_MEM on memory allocation error

4.28 gitcon.h

Go to the documentation of this file.

```
00001
00012 #ifndef GITCON_H
00013 #define GITCON_H
00015 #include "config.h"
00016
00017 #define GITCON_LOG_LEVEL ESP_LOG_ERROR
00018
00025 typedef struct
00026 {
00027 #ifdef USE_MCP3201
00028
        mcp3201_sampler_t *sampler;
00029 #else
00030
       i2s_sampler_t *sampler;
00031 #endif
00032 midi_handle_t midi_handle;
00033 QueueHandle_t midi_queue;
00034 } gitcon_context_t;
00035
00037 typedef gitcon_context_t *gitcon_handle_t;
00045 esp_err_t gitcon_init(gitcon_handle_t *out_handle);
00046
00053 esp_err_t gitcon_exit(gitcon_handle_t handle);
00054
00055 #endif // GITCON_H
```

4.29 src/main.c File Reference

```
Main File for Gitcon Project.
```

```
#include "gitcon.h"
```

Macros

- #define USER_LOCAL_LEVEL ESP_LOG_ERROR
- #define PROTOTYPE 0

Functions

void app_main (void)

4.29.1 Detailed Description

Main File for Gitcon Project.

Author

@s-grundner

Version

0.1

Date

2022-12-23

Copyright

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Definition in file main.c.

4.29.2 Macro Definition Documentation

4.29.2.1 PROTOTYPE

#define PROTOTYPE 0

Definition at line 17 of file main.c.

4.29.2.2 USER_LOCAL_LEVEL

#define USER_LOCAL_LEVEL ESP_LOG_ERROR

Definition at line 14 of file main.c.

4.29.3 Function Documentation

4.30 main.c 119

4.29.3.1 app_main()

```
void app_main (
     void )
```

Definition at line 80 of file main.c.

4.30 main.c

Go to the documentation of this file.

```
00001
00012 #include "gitcon.h"
00013
00014 #define USER_LOCAL_LEVEL ESP_LOG_ERROR
00016 // when PROTOTYPE is 1, the prototype board is used
00017 #define PROTOTYPE 0
00018
00019 static const char *TAG = "main";
00020
00021 #if PROTOTYPE == 1
00022 #define DIP_POL 8
00023 #define DEBOUNCE_TIME_MS 50
00024
00025 static const char WHOLE_TONE[8] = {0, 2, 4, 5, 7, 9, 11, 12};
00026
00027 static const gpio_num_t DIP_IO[DIP_POL] = {
00028
          GPIO_NUM_32,
00029
          GPIO_NUM_33,
00030
          GPIO_NUM_25,
00031
          GPIO_NUM_26,
          GPTO NUM 27.
00032
00033
          GPIO_NUM_14,
00034
          GPIO_NUM_12,
00035
          GPIO_NUM_13,
00036 };
00037
00038 typedef struct
00039 {
00040
          QueueHandle_t midi_queue;
00041
          size_t *current_dip;
00042
          size_t *previous_dip;
00043
          TimerHandle_t *timer;
00044 } dip_switch_t;
00045
00046 static void IRAM_ATTR dip_isr(void *args)
00047 {
00048
          dip_switch_t *dip_switch = (dip_switch_t *)args;
00049
          for (size_t i = 0; i < DIP_POL; i++)</pre>
00050
              // read DIP switch
00051
00052
              dip_switch->current_dip[i] = !gpio_get_level(DIP_IO[i]);
00053
00054
              // continue if the dip state hasn't changed
00055
              if (dip_switch->current_dip[i] == dip_switch->previous_dip[i])
00056
                  continue;
00057
00058
              // send MIDI message
00059
              midi_message_t msg = {
00060
                  .status = (midi_status_t)(dip_switch->current_dip[i]) ? MIDI_STATUS_NOTE_ON :
       MIDI_STATUS_NOTE_OFF,
                  .channel = 0,
.param1 = 0x3C + WHOLE_TONE[i], // C4 + WHOLE_TONE[i]
.param2 = 127);
00061
00062
00063
00064
              xQueueSendFromISR(dip_switch->midi_queue, &msg, NULL);
00065
00066
              \ensuremath{//} disable interrupts for gpios to debounce
              ESP_ERROR_CHECK(gpio_intr_disable(DIP_IO[i]));
00067
00068
              dip_switch->previous_dip[i] = dip_switch->current_dip[i];
00069
              xTimerStartFromISR(dip_switch->timer[i], NULL);
00070
          }
00071 }
00072
00073 static void IRAM_ATTR debounce_task(TimerHandle_t debounce_timer)
00074 {
00075
          int i = (int)pvTimerGetTimerID(debounce_timer);
00076
          gpio_intr_enable(DIP_IO[i]);
00077 }
```

```
00078 #endif
00079
00080 void app_main(void)
00081 {
00082
          gitcon_handle_t handle;
00083
           if (gitcon_init(&handle) != ESP_OK)
00085
               ESP_LOGE(TAG, "gitcon_init failed");
00086
               ESP_ERROR_CHECK(gitcon_exit(handle));
00087
               return;
00088
00089 #if PROTOTYPE == 1
00090
          xTimerHandle debounce_timers[DIP_POL];
00091
00092
          for (size_t i = 0; i < DIP_POL; i++)</pre>
00093
              debounce_timers[i] = xTimerCreate("dip_switch", pdMS_TO_TICKS(DEBOUNCE_TIME_MS), pdFALSE,
       (void *)i, debounce_task);
00094
00095
          size_t current_dip[DIP_POL] = {0};
00096
          size_t previous_dip[DIP_POL] = {0};
00097
00098
           // setup debouncing for DIP Switches
00099
          dip_switch_t dip_switch = {
00100
               .current dip = current dip
               .previous_dip = previous_dip,
00101
               .timer = debounce_timers,
00102
00103
               .midi_queue = handle->midi_queue);
00104
00105
          // setup interrupt for DIP switches
          ESP_ERROR_CHECK(gpio_install_isr_service(0));
for (size_t i = 0; i < DIP_POL; i++)</pre>
00106
00107
00108
00109
               gpio_config_t io_conf = {
00110
                  .pin_bit_mask = (1ULL « DIP_IO[i]),
00111
                   .mode = GPIO_MODE_INPUT,
                   .pull_up_en = GPIO_PULLUP_ENABLE,
.pull_down_en = GPIO_PULLDOWN_DISABLE,
00112
00113
00114
                   .intr_type = GPIO_INTR_ANYEDGE };
00115
00116
               ESP_ERROR_CHECK(gpio_config(&io_conf));
00117
               ESP_ERROR_CHECK(gpio_isr_handler_add(DIP_IO[i], dip_isr, &dip_switch));
00118
00119 #endif
00120
          while (1)
00121
               vTaskDelay(1000 / portTICK_PERIOD_MS);
00122 }
```

4.31 test/test_fft/test_fft.c File Reference

Unit Test for FFT.

```
#include cessed-data.h>
#include <fft.h>
#include <unity.h>
```

Macros

- #define AUDIO_BUFFER_SIZE 512
- #define F_SAMPLE_HZ 44100
- #define FFT_WINDOW_SIZE 2
- #define FFT_SIZE 4096

Functions

- void setUp (void)
- void tearDown (void)
- · void test processed data (void)
- void app_main ()

4.31.1 Detailed Description

Unit Test for FFT.

Author

@s-grundner

Version

0.1

Date

2023-03-26

Copyright

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Definition in file test_fft.c.

4.31.2 Macro Definition Documentation

4.31.2.1 AUDIO_BUFFER_SIZE

#define AUDIO_BUFFER_SIZE 512

Definition at line 15 of file test_fft.c.

4.31.2.2 F_SAMPLE_HZ

#define F_SAMPLE_HZ 44100

Definition at line 16 of file test_fft.c.

4.31.2.3 FFT_SIZE

#define FFT_SIZE 4096

Definition at line 18 of file test_fft.c.

4.31.2.4 FFT_WINDOW_SIZE

```
#define FFT_WINDOW_SIZE 2
```

Definition at line 17 of file test_fft.c.

4.31.3 Function Documentation

4.31.3.1 app_main()

```
void app_main (
     void )
```

Definition at line 62 of file test_fft.c.

4.31.3.2 setUp()

```
void setUp (
     void )
```

Definition at line 20 of file test_fft.c.

4.31.3.3 tearDown()

```
void tearDown (
     void )
```

Definition at line 24 of file test_fft.c.

4.31.3.4 test_processed_data()

Definition at line 28 of file test_fft.c.

4.32 test fft.c 123

4.32 test fft.c

Go to the documentation of this file.

```
00001
00011 #include cessed-data.h>
00012 #include <fft.h>
00013 #include <unity.h>
00015 #define AUDIO_BUFFER_SIZE 512 // Size of buffer for FFT and sampler
00016 #define F_SAMPLE_HZ 44100 // Sample rate of FFT and sampler 00017 #define FFT_WINDOW_SIZE 2 // Amount of buffers to take for FFT
                                         //\left(\texttt{AUDIO\_BUFFER\_SIZE} \ \star \ \texttt{FFT\_WINDOW\_SIZE}\right) \quad \texttt{Amount of samples to take for}
00018 #define FFT_SIZE 4096
       FFT
00020 void setUp(void)
00021 {
00022 }
00023
00024 void tearDown(void)
00025 {
00026 }
00027
00028 void test_processed_data(void)
00029 {
00030
            // fft variables
           float fft_buffer[FFT_SIZE];
00031
00032
           float magnitude[FFT_SIZE / 2];
00033
           float frequency[FFT_SIZE / 2];
           unsigned char keyNR[FFT_SIZE / 2];
00034
00035
           float ratio = (float)F_SAMPLE_HZ / (float)FFT_SIZE;
00036
00037
           fft_config_t *real_fft_plan = fft_init(FFT_SIZE, FFT_REAL, FFT_FORWARD, test_buffer, fft_buffer);
           TEST_ASSERT_NOT_NULL(real_fft_plan);
00038
00039
           fft_execute(real_fft_plan);
00040
00041
            for (int k = 1; k < FFT SIZE / 2; k++)
00042
00043
                \texttt{magnitude[k]} = 2 \, \star \, \texttt{sqrt(pow(fft\_buffer[2 \, \star \, k], \, 2)} \, + \, \texttt{pow(fft\_buffer[2 \, \star \, k \, + \, 1], \, 2))} \, / \, \, \texttt{FFT\_SIZE;}
00044
                frequency[k] = k * ratio;
00045
                keyNR[k] = (unsigned char) round (log2 (frequency[k] / 440) * 12 + 69) % 128;
00046
00047
00048
           float max = 0:
00049
           for (int i = 0; i < FFT_SIZE / 2; i++)</pre>
                max = (magnitude[i] > max) ? magnitude[i] : max;
00050
00051
00052
           for (int k = 1; k < FFT\_SIZE / 2; k++)
00053
00054
                if (magnitude[k] >= max * 0.5)
00055
00056
                     TEST_ASSERT_EQUAL(45, keyNR[k]);
00057
00058
00059
            fft_destroy(real_fft_plan);
00060 }
00061
00062 void app_main()
00063 {
00064
           UNITY_BEGIN();
00065
           RUN_TEST(test_processed_data);
00066
           UNITY_END();
00067 }
```

4.33 test/test_midi/test_midi.c File Reference

Unit Tests for MIDI Driver.

```
#include <midi.h>
#include <unity.h>
```

Macros

- #define MIDI_UART (UART_NUM_1)
- #define MIDI BAUD (115200)
- #define MIDI_TX (GPIO_NUM_26)
- #define MIDI_RX (GPIO_NUM_27)

Functions

- void setUp (void)
- void tearDown (void)
- void test_midi_blink (void)
- void test_midi_bend (void)
- void test_midi_bent_note (void)
- void app_main ()

4.33.1 Detailed Description

Unit Tests for MIDI Driver.

Author

@s-grundner

Version

0.1

Date

2023-03-26

Copyright

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Definition in file test_midi.c.

4.33.2 Macro Definition Documentation

4.33.2.1 MIDI_BAUD

```
#define MIDI_BAUD (115200)
```

Definition at line 18 of file test_midi.c.

4.33.2.2 MIDI_RX

```
#define MIDI_RX (GPIO_NUM_27)
```

Definition at line 20 of file test_midi.c.

4.33.2.3 MIDI_TX

```
#define MIDI_TX (GPIO_NUM_26)
```

Definition at line 19 of file test_midi.c.

4.33.2.4 MIDI_UART

```
#define MIDI_UART (UART_NUM_1)
```

Definition at line 17 of file test_midi.c.

4.33.3 Function Documentation

4.33.3.1 app_main()

```
void app_main (
    void )
```

Definition at line 87 of file test_midi.c.

4.33.3.2 setUp()

```
void setUp (
     void )
```

Definition at line 22 of file test_midi.c.

4.33.3.3 tearDown()

```
void tearDown (
     void )
```

Definition at line 32 of file test_midi.c.

4.33.3.4 test_midi_bend()

Definition at line 46 of file test_midi.c.

4.33.3.5 test_midi_bent_note()

Definition at line 58 of file test_midi.c.

4.33.3.6 test_midi_blink()

Definition at line 37 of file test midi.c.

4.34 test midi.c

Go to the documentation of this file.

```
00001
00012 #include <midi.h>
00013 #include <unity.h>
00014
00015 static midi_handle_t midi_handle;
00016
00017 #define MIDI_UART (UART_NUM_1)
00018 #define MIDI_BAUD (115200)
00019 #define MIDI_TX (GPIO_NUM_26)
00020 #define MIDI_RX (GPIO_NUM_27)
00021
00022 void setUp(void)
00023 {
           static midi_config_t midi_cfg = {
   .uart_num = MIDI_UART,
   .baudrate = MIDI_BAUD,
00024
00025
00026
                .rx_io = MIDI_RX,
.tx_io = MIDI_TX);
00028
00029
           ESP_ERROR_CHECK(midi_init(&midi_handle, &midi_cfg));
00030 }
00031
00032 void tearDown(void)
00033 {
00034
            midi_exit (midi_handle);
00035 }
00036
00037 void test_midi_blink(void)
00038 {
00039
            midi_message_t msg = note_on(0, 0x3C, 0x7F);
00040
            TEST_ASSERT_EQUAL(ESP_OK, midi_write(midi_handle, &msg));
            vTaskDelay(1000 / portTICK_PERIOD_MS);
msg.status = MIDI_STATUS_NOTE_OFF;
00041
00042
00043
            TEST_ASSERT_EQUAL(ESP_OK, midi_write(midi_handle, &msg));
00044 }
00046 void test_midi_bend(void)
```

4.34 test midi.c 127

```
00047 {
00048
           midi_message_t msg = pitch_bend(0, MIDI_PITCH_BEND_MAX);
00049
           TEST_ASSERT_EQUAL(ESP_OK, midi_write(midi_handle, &msg));
           vTaskDelay(1000 / portTICK_PERIOD_MS);
msg = pitch_bend(0, MIDI_PITCH_BEND_MIN);
TEST_ASSERT_EQUAL(ESP_OK, midi_write(midi_handle, &msg));
00050
00051
00052
           vTaskDelay(1000 / portTICK_PERIOD_MS);
00054
           msg = pitch_bend(0, MIDI_PITCH_BEND_CENTER);
00055
           TEST_ASSERT_EQUAL(ESP_OK, midi_write(midi_handle, &msg));
00056 }
00057
00058 void test_midi_bent_note(void)
00059 {
00060
            midi_message_t msg = note_on(0, 0x3C, 0x7F);
00061
           TEST_ASSERT_EQUAL(ESP_OK, midi_write(midi_handle, &msg));
00062
           // ramp up and down pitch bend in 1 second
midi_message_t msg_bend = pitch_bend(0, MIDI_PITCH_BEND_CENTER);
for (int i = MIDI_PITCH_BEND_CENTER; i <= MIDI_PITCH_BEND_MAX; i += 128)</pre>
00063
00064
00065
00066
            {
00067
                msg_bend = pitch_bend(0, i);
                TEST_ASSERT_EQUAL(ESP_OK, midi_write(midi_handle, &msg_bend));
vTaskDelay(4 / portTICK_PERIOD_MS);
00068
00069
00070
00071
            for (int i = MIDI_PITCH_BEND_MAX; i >= MIDI_PITCH_BEND_MIN; i -= 128)
00072
00073
                msg_bend = pitch_bend(0, i);
00074
                TEST_ASSERT_EQUAL(ESP_OK, midi_write(midi_handle, &msg_bend));
00075
                vTaskDelay(2 / portTICK_PERIOD_MS);
00076
00077
           for (int i = MIDI_PITCH_BEND_MIN; i <= MIDI_PITCH_BEND_CENTER; i += 128)</pre>
00078
00079
                msg_bend = pitch_bend(0, i);
00080
                TEST_ASSERT_EQUAL(ESP_OK, midi_write(midi_handle, &msg_bend));
00081
                vTaskDelay(4 / portTICK_PERIOD_MS);
00082
00083
           msg.status = MIDI_STATUS_NOTE_OFF;
00084
           TEST_ASSERT_EQUAL(ESP_OK, midi_write(midi_handle, &msg));
00085 }
00086
00087 void app_main()
00088 {
00089
           UNITY BEGIN():
00090
00091
           RUN_TEST(test_midi_blink);
00092
           RUN_TEST(test_midi_bend);
00093
           RUN_TEST(test_midi_bent_note);
00094
00095
           UNITY END();
00096 }
```

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