

County Demographic Information: Case Study

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Radhika Kulkarni & Sameerah Helal STA 108 A01 Professor Jiming Jiang

Introduction

In this project we would like to determine:

- 1) the relationships, if any, between three predictor variables and the number of active physicians in a US county, and
- 2) whether the per capita income has any relationship with the percentage of the population with bachelor's degrees in the county.

The variables in 1) are the total population, number of hospital beds, and the total personal income. We hypothesized that each of these variables would have no relationship with the number of physicians in a county. We will determine whether or not this statement is true for each of the predictor variables.

We plan to test our hypothesis by comparing regression models, MSE calculations, residual plots, and normal probability plots. We will also use R squared calculations to determine how much of the variability in the number of active physicians in the county is explained by the regression functions involving, respectively, total population, number of hospital beds, and total personal income. We realize, however, that we cannot definitively prove whether or not our hypothesis is true because we will not have performed the standard method of hypothesis testing to use as sufficient evidence to support or reject our hypothesis.

Our second hypothesis deals with per capita income and the percent of population who have bachelor's degrees. We hypothesize that these two variables also share no linear relationship. By separating our data into four geographical regions, which may have a different per capita income, we aim to be more cognizant of any error we could make in that respect; hence we would like to generate estimated regression functions that are more accurate. To test our hypothesis we will compare the regression function data and use the F-test technique. We will use this to determine whether or not there is a relationship between per capita income and the proportion of a population who have bachelor's degrees in each region.

We believe that this project may be valuable to the medical community because it can prove to hospitals whether or not more beds in a hospital will mean that more physicians will be working there, which could save them money and help hospitals invest in their future. Additionally, urban planners and city officials can use the relationship between total population and number of physicians to build more medical centers in populous areas, since there could be a larger number of active physicians working there, and vice versa. Economists could also find out whether a county is fiscally thriving because the number of active physicians can change based on the total personal income. Similarly, the per capita income of a region may be able determine what percentage of the population has a bachelor's degree, which can be used as an advertisement for cities looking to attract college graduates to their workforce.

The main tool we will use to generate our graphs and output is R-Studio. Screenshots of code and output are given at the end of the document.

Part I: Fitting Regression Models

1.43

The number of active physicians in a CDI (Y) is expected to be related to total population, number of hospital beds, and total personal income. Assume that first-order regression model (1.1) is appropriate for each of the three predictor variables.

a. Regress the number of active physicians in turn on each of the three predictor variables. State the estimated regression functions.

```
REGRESSION FUNCTION 1:

For X = total population

\hat{Y} = -110.6348 + 0.002795425X

Estimated Number of Active Physicians = -110.6348 + 0.002795425 (Total Population)

REGRESSION FUNCTION 2:

For X = number of hospital beds

\hat{Y} = -95.93218 + 0.7431164X

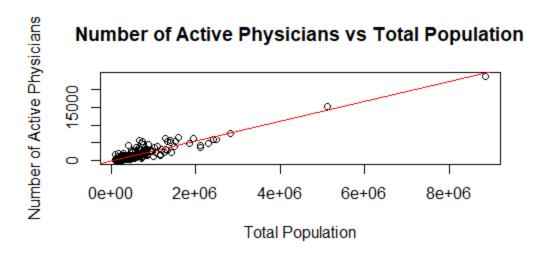
Estimated Number of Active Physicians = -95.93218 + 0.7431164 (Number of Hospital Beds)
```

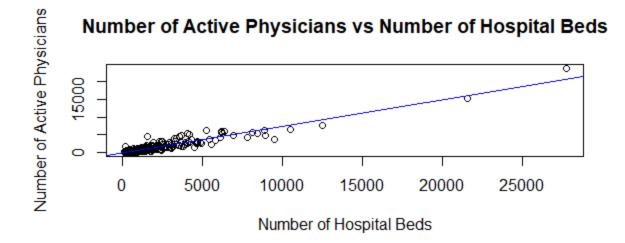
REGRESSION FUNCTION 3:

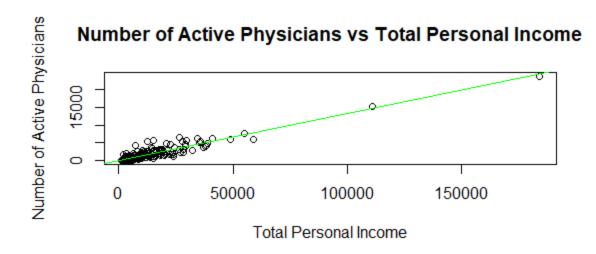
For X = total personal income $\hat{Y} = -48.39485 + 0.1317012X$

Estimated Number of Active Physicians = -48.39485 + 0.1317012 (Total Personal Income)

b. Plot the three estimated regression functions and data on separate graphs. Does a linear regression relation appear to provide a good fit for each of the three predictor variables?







Yes, the respective linear regression relations appear to be a good fit for each of the three predictor variables, the line fits the data and its trajectory, hitting almost every point.

c. Calculate MSE for each of the three predictor variables. Which predictor variable leads to the smallest variability around the fitted regression line?

MSE = 372203.5

MSE2 = 310191.9

MSE3 = 324539.4

The predictor variable which leads to the smallest variability around the regression line is the number of hospital beds.

1.44

a) For each geographic region, regress per capita income in a CD (Y) against the percentage of individuals in a county having at least a bachelor's degree (X). State the estimated regression functions. b. Are the estimated regression functions similar for the four regions? Discuss.

REGRESSION FUNCTIONS:

Region 1:

For X = percentage of individuals with bachelor's degrees in region 1 $\hat{Y} = 9223.8156 + 422.1588X$

Region 2:

For X = percentage of individuals with bachelor's degrees in region 1

 $\hat{Y} = 13581.4052 + 238.6694X$

Region 3:

For X = percentage of individuals with bachelor's degrees in region 1 $\hat{Y} = 10529.7851 + 330.6117X$

Region 4:

For X = percentage of individuals with bachelor's degrees in region 1 \hat{Y} = 8615.0527 + 440.3157X

b. Are the estimated regression functions similar for the four regions? Discuss.

The estimated regression functions for the 4 regions are somewhat similar. The intercepts range from 9000 to 13000, and the slopes are all positive and in the range of 230 to 530.

c. Calculate MSE for each region. Is the variability around the fitted regression line approximately the same for the four regions? Discuss.

The MSE was extracted from the ANOVA, which can be found below in part 3.

MSE for region 1 is 733,5008.

MSE for region 2 is 441,1341.

MSE for region 3 is 747,4349.

MSE for region 4 is 821,4318.

While the MSE for regions 1, 3, and 4 are fairly close, that of region 2 deviates noticeably. The variability around the fitted line cannot be said to be approximately the same for all 4 of the regions.

Part II: Measuring linear associations

2.62

Using R² as the criterion, which predictor variable accounts for the largest reduction in the variability in the number of active physicians?

Total Population:

R² is 0.8840674,

Hospital Beds:

R² is 0.9033826.

Total Personal Income:

 R^2 is 0.8989137.

The predictor variable that accounts for the largest reduction in the variability in the number of physicians is the number of hospital beds, because 90.338% of the variability in number of active physicians can be explained by the regression function with X = number of hospital beds.

Part III. Inference about regression parameters

2.63

Obtain a separate interval estimate of β_1 for each region. Use a 90 percent confidence coefficient in each case. Do the regression lines for the different regions appear to have similar slopes?

Also carry out the analysis of variance (ANOVA) for each regression model and state the results of the F-tests. What do you conclude in each case?

The interval estimate of β_1 for region 1 is [460.5177,583.80]. The interval estimate of β_1 for region 2 is [193.4858,283.853]. The interval estimate of β_1 for region 3 is [285.7076,375.5158]. The interval estimate of β_1 for region 4 is [364.7585,515.8729].

Comparing respectively the F* and F values for the 4 regions:

197.75 > 2.755868 76.826 > 2.753462 148.49 > 2.739275 94.195 > 2.773642.

For all four regions, the value of F* is greater than the quantity of F for the level 0.9 and the particular degrees of freedom. So we reject the null hypothesis that the slopes of any of the regression lines are 0, and accept the alternative hypothesis that all of the predictor variables have a relationship with the response variable.

ANOVA Tables:

```
> anova(regFit1)
Analysis of Variance Table
Response: perCapInc1
          Df
                Sum Sq
                         Mean Sq F value
                                             Pr(>F)
          1 1450517671 1450517671 197.75 < 2.2e-16 ***
Residuals 101 740835765 7335008
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' '1
> anova(regFit2)
Analysis of Variance Table
Response: perCapInc2
          nf
                Sum Sq
                        Mean Sq F value
                                            Pr(>F)
           1 338907694 338907694 76.826 3.344e-14 ***
bDeg2
Residuals 106 467602149 4411341
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' '1
> anova(regFit3)
Analysis of Variance Table
Response: perCapInc3
                           Mean Sq F value
          Df Sum Sq
                                              Pr(>F)
           1 1109873245 1109873245 148.49 < 2.2e-16 ***
Residuals 150 1121152411 7474349
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' '1
> anova(regFit4)
Analysis of Variance Table
Response: perCapInc4
         Df Sum Sq Mean Sq F value Pr(>F)
1 773745787 773745787 94.195 6.856e-15 ***
Residuals 75 616073841 8214318
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' '1
```

F-intervals

```
> confint(regFit1, level = 0.9)
                   5 % 95 %
(Intercept) 7809.8077 10637.82 bDeg1 460.5177 583.80
> confint(regFit2, level = 0.9) 5 % 95 %
(Intercept) 12627.0363 14535.774
bDeg2
              193.4858 283.853
> confint(regFit3, level = 0.9)
5 % 95 %
(Intercept) 9516.0773 11543.4929
            285.7076 375.5158
bDeg3
> confint(regFit4, level = 0.9)
                  5 %
                             95 %
(Intercept) 6862.6967 10367.4086
            364.7585 515.8729
bDeg4
```

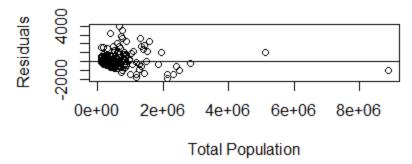
```
> regions <- CDI$V17
> percapinc <- CDI$V15
> bDeg <- CDI$V12
> reg1 <- regions==1
> reg2 <- regions==2
> reg3 <- regions==3
> reg4 <- regions==4
> perCapInc1 <- perCapInc[reg1]
> perCapInc2 <- perCapInc[reg2]
> perCapInc3 <- perCapInc[reg3]
> perCapInc4 <- perCapInc[reg4]
> bDeg1 <- bDeg[reg1]
> bDeg2 <- bDeg[reg2]
> bDeq3 <- bDeg[reg3]
> bDeg4 <- bDeg[reg4]
> regFit1 <- lm(perCapInc1~bDeg1)
> regFit2 <- lm(perCapInc2~bDeg2)
> regFit3 <- lm(perCapInc3~bDeg3)</pre>
> regFit4 <- lm(perCapInc4~bDeg4)
> coef1 <- coef(summary(regFit1))
> coef2 <- coef(summary(regFit2))
> coef3 <- coef(summary(regFit3))
> coef4 <- coef(summary(regFit4))
> # Region n: y = coefn[1] + coefn[2]x
> # Region 1: y = 9223.8156 + 522.1588x
> # Region 2: y = 13581.4052 + 238.6694x
> # Region 3: y = 10529.7851 + 330.6117x
> # Region 4: y = 8615.0527 + 440.3157x
> qf(.9,1,101)
[1] 2.755868
> qf(.9,1,106)
[1] 2.753462
> qf(.9,1,150)
[1] 2.739275
> qf(.9,1,75)
[1] 2.773642
> qf(.9,1,8)
[1] 3.457919
```

Part IV: Regression diagnostics

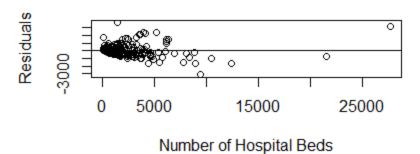
3.25

For each of the three fitted regression models, obtain the residuals and prepare a residual plot against X and a normal probability plot. Summarize your conclusions. Is linear regression model (2.1) more appropriate in one case than in the others?

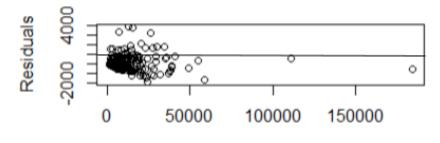
Residuals vs Total Population



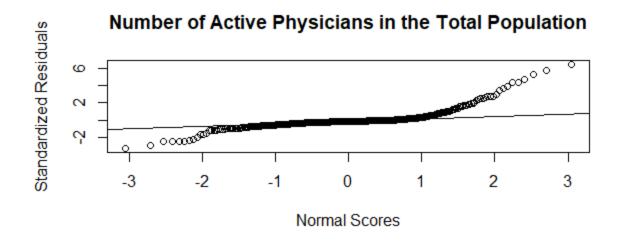
Residuals vs Number of Hospital Beds

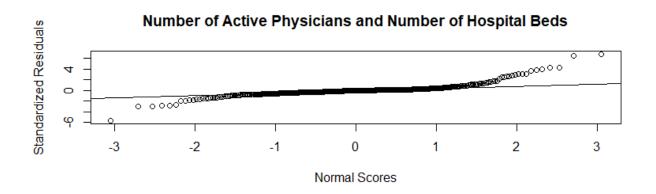


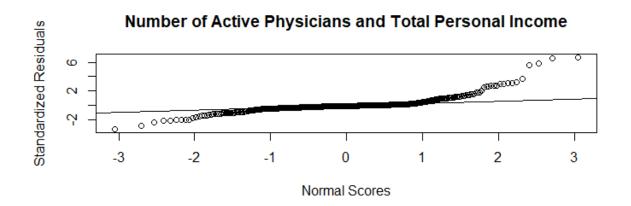
Residuals vs Total Personal Income



Total Personal Income







Yes, for us to obtain the best fitting linear regression model $Y_i = \beta_0 + \beta_1 X + \epsilon_i$, we must have the most accurate predictor. In this case, the number of hospital beds is the most accurate predictor variable for the number of active physicians in the county.

Part V: Discussion

In the first and second parts, we analyzed the relationship of the predictor variables (total population, number of hospital beds, and total personal income) with the number of active physicians in a county. Regressing the fourth variables in turn against the first three, i.e. trying out whether any of the three predictor variables had a relationship to our response variable- number of physicians- told us that, while there was a decent line through the data formed by plotting each pair, the line was most strongly connected to the data when the predictor was the number of hospital beds and weakest when it was the value of the total population. The number of hospital beds was also that variable that accounted for the largest reduction in the variability of the number of physicians. This means that the number of hospital beds had a stronger relationship than the other two variables with the number of physicians; the number of hospital beds makes it so that there is less chance that the reason for the number of physicians having a certain value will be unexplained by the predictor. This isn't enough evidence still to reject or accept our hypothesis that there is no relationship with each of the variables to the number of active physicians in the county.

In parts I and III, the number of people with bachelor's degrees in the four different regions all seemed to have a positive linear relationship with the per capita income in the region. So the more people there were with bachelor's degrees, the higher we would expect the per capita income to be. We found 90 percent confidence intervals for the slope of the line relating the two variables for each region, meaning that we are 90% confident that each slope value is in the interval we gave. We used the F-test to check that none of the slopes were 0 to confirm that there was a significant linear relationship present. As a result of our test, we have rejected our hypothesis and accepted that there is in fact a relationship between the per capita income of a county and the percent of the population who have bachelor's degrees in each region.

We might improve the linear regression models by testing every variable, not just a few, as a predictor to see which one gives us the optimized estimated regression function.

Outputs

```
> #PART II
                                                        > #MSE totalPop - 1:
> \#R^2 and r info:
                                                          > residualStandardError1 = summary(fit1)$sigma
                                                           > MSE1 = residualStandardError1^2
> summary(fit1)$r.squared
                                                           > \#MSE1 = 372203.5
[1] 0.8840674
> #summary(fit1)$adj.r.squared
                                                           > #MSE numHospBeds - 2:
                                                           > residualStandardError2 = summary(fit2)$sigma
  summary(fit2)$r.squared
                                                           > MSE2 = residualStandardError2^2
[1] 0.9033826
                                                           > \#MSE2 = 310191.9
> #summary(fit2)$adj.r.squared
                                                          > #MSE totalPersonalIncome - 3:
> residualStandardError3 = summary(fit3)$sigma
> MSE3 = residualStandardError3^2
> #MSE3 = 324539.4
  summary(fit3)$r.squared
> #summary(fit3)$adj.r.squared
> #****
[1] 0.8989137
lm(formula = numActivePhys ~ totalPop, data = CDI_dataset)
Residuals:
                 1Q Median
     Min
                                       30
                                                Max
 Min 1Q Median 3Q Max
-1969.4 -209.2 -88.0 27.9 3928.7
Coefficients:
Estimate Std. Error t value Pr(>|t|) (Intercept) -1.106e+02 3.475e+01 -3.184 0.00156 ** totalPop 2.795e-03 4.837e-05 57.793 < 2e-16 ***
Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' ' 1
Residual standard error: 610.1 on 438 degrees of freedom
Multiple R-squared: 0.8841, Adjusted R-squared: 0.8838
F-statistic: 3340 on 1 and 438 DF, p-value: < 2.2e-16
Call:
lm(formula = numActivePhys ~ numHospBeds, data = CDI_dataset)
Min 1Q Median 3Q Max
-3133.2 -216.8 -32.0 96.2 3611.1
Coefficients:
Estimate Std. Error t value Pr(>|t|) (Intercept) -95.93218 31.49396 -3.046 0.00246 ** numHospBeds 0.74312 0.01161 63.995 < 2e-16 ***
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
Residual standard error: 556.9 on 438 degrees of freedom
Multiple R-squared: 0.9034, Adjusted R-squared: 0.5
F-statistic: 4095 on 1 and 438 DF, p-value: < 2.2e-16
                                          Adjusted R-squared: 0.9032
lm(formula = numActivePhys ~ totalPersonalIncome, data = CDI_dataset)
Residuals:
                1Q Median 3Q Max
94.5 -66.6 44.2 3819.0
Min 1Q
-1926.6 -194.5
Coefficients:
Estimate Std. Error t value Pr(>|t|)
(Intercept) -48.39485 31.83333 -1.52 0.129
totalPersonalIncome 0.13170 0.00211 62.41 <2e-16 ***
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
Residual standard error: 569.7 on 438 degrees of freedom
Multiple R-squared: 0.8989, Adjusted R-squared: 0.8987
F-statistic: 3895 on 1 and 438 DF, p-value: < 2.2e-16
```

```
> regions
[1] 4 2 3 4 4 1 4 2 3 3 1 4 4 4 2 1 1 1 1 1 4 3 3 4 3 2 4 2 2 1 2 2 1 2 3 1 3 4 3 1 3 1 3 1 3 1
[44] 4 2 2 1 3 4 3 3 4 4 2 1 1 3 1 3 1 3 1 1 4 4 4 3 1 3 4 3 2 1 3 3 1 3 4 4 3 2 1 1 1 3 4 1
[87] 2 2 3 3 1 3 1 2 3 1 2 4 4 2 1 4 4 2 1 1 3 3 1 4 1 1 2 3 3 1 1 1 2 3 2 3 4 2 1 3 3 4 2 1 3 4 4 3 3
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[345] 1 2 2 1 2 2 4 3 3 2 4 2 1 2 3 4 3 2 3 1 1 1 3 4 3 1 2 3 4 3 2 2 3 1 3 3 2 4 3 1 2 2 3 3 1
[388] 4 3 2 4 2 1 2 3 3 3 3 4 3
```

```
> perCapInc
  [1] 20786 21729 19517 19588 24400 16803 18042 17461 17823 21001 16721 23779 25193 16399
 [15] 21086 25312 20681 24262 31679 22148 22355 15508 17185 18825 26884 18934 23705 24219
 [29] 18305 19040 18431 33330 20580 26798 24875 21610 21307 16876 32342 18430 32230 28999
 [43] 22197 25523 19148 26772 24523 30081 18625 17263 19568 15399 28532 20924 21641 19895
 [57] 23470 28462 17879 17662 24896 22834 21420 16365 15191 19140 23150 18624 28819 22819
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[197]
[211] 15776 18301 19320 21421 24035 18288 15443 16647 16963 17744 17221 17776 20543 19692
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[435] 19317 13919 27125 13169 18504 16458
```

```
> bDea
  [1] 22.3 22.8 25.4 25.3 27.8 16.6 22.1 13.7 18.8 26.3 15.2 32.8 32.6 14.9 20.1 35.4 22.6
 [18] 23.0 30.0 28.8 18.8 19.7 14.6 24.0 30.2 23.0 31.6 29.2 20.0 26.6 19.3 35.3 23.7 22.1
 [35] 25.8 18.5 24.6 20.2 34.2 20.8 31.7 49.0 24.2 31.6 21.4 36.0 24.0 49.9 13.8 15.5 25.5
 [52] 23.8 35.0 13.5 26.3 22.2 25.0 32.1 21.2 18.4 26.5 25.9 23.0 16.9 23.3 19.3 27.7 19.9
 [69] 31.3 31.6 20.0 34.4 33.3 22.6 18.3 15.2 17.5 23.7 34.7 20.0 28.4 19.7 24.8 32.7 13.3
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      9.1 23.6 21.9 16.2 27.6 16.6 32.3 12.3 24.1 33.0 13.0 14.0 39.1 26.2 14.7 18.2 16.8
[171]
[188] 12.0 24.8 21.8 20.7 26.4 16.7 16.7 14.4 18.2 16.7 19.2 25.9 27.6 38.3 15.5 30.1 16.8
[205] 18.6 44.0 18.1 29.7 17.5 11.4 14.3 30.2 30.6 42.1 16.4 27.1 23.4 13.6 14.8 19.3 22.9
[222] 18.6 27.6 17.5 27.6 21.2 20.7 13.0 15.5 24.2 20.7 17.6 24.9 13.6 17.3 22.9 11.5 17.7
      37.1 15.1 17.2 19.8 17.3 16.6 13.7 23.5 18.7 46.9 28.1 32.3 11.9 21.0 19.5 19.4 21.5
[256] 19.5 14.7 33.4 34.6 25.2 16.6 12.0 22.4 10.8 16.5 19.1 25.9 25.0 34.1 22.7 9.0 52.3
[273] 18.4 14.7 21.0 16.3 21.6 16.0 22.5 19.0 10.8 10.3 16.7 24.7 20.5 22.3 11.1 18.0 14.2
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     14.2 30.3 16.7 18.2 24.6 13.3 20.9 10.8 26.0 13.8 21.9 19.1 10.5 11.1 18.4 34.0 14.6
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[375] 17.5 12.3 18.7 14.2 14.8 8.2 14.2 18.1 19.6 13.5 14.4 14.8 11.8 21.5 20.0 21.9 23.3
[392] 36.5 15.1 11.0 18.4 48.5 15.0 13.4 13.6 22.3 11.7 29.1 11.4 9.7 32.9 36.2 8.5 14.6 [409] 21.9 34.6 11.2 17.7 11.7 10.5 12.7 26.4 9.1 29.5 18.1 17.9 12.6 11.0 17.7 12.7 21.7
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> perCapInc1
  [1] 16803 16721 25312 20681 24262 31679 18305 33330 24875 32342 32230 22197 24523 21641
      19895 28462 24896 22834 23150 26909 17866 27391 18463 23658 22548 18521 19930 26248
 [29] 19401 19073 21973 22284 21500 20974 18878 31520 23008 24732 17069 19502 19655 22581
 [43] 16405 26026 19788 21003 19785 16331 26757 22173 20259 16477 18336 21770 21362 33180
 [57] 18348 18523 24035 16647 16963 18058 16625 19254 23267 15162 18857 25161 18824 17908
 [71] 14473 20086 17774 15853 17251 20679 15521 17853 14051 24132 15197 20068 16819 19940 [85] 24405 14779 21944 15476 14834 16281 15177 20600 15778 17131 16500 12704 14946 15205
 [99] 19449 30255 16154 17182 18070
> perCapInc2
  [1] 21729 17461 21086 26884 23705 24219 19040 18431 20580 19148 26772 20924 18611 18410
 [15] 27378 18583 18674 20303 16327 17815 16829 19629 19276 18113 16898 20087 18787 26156
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 [15] 23470 17879 17662 19140 18624 22819 23603 17741 11545 18340 21005 20942 19505 19295
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 [99] 16924 17511 15113 19954 14137 17548 10190 14205 17129 14693 15803 15747 13869 16935
[113] 14934 14743 8973 14615 16713 14814 15079 22002 17119 12641 17898 17119 16021 14766
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[141] 14721 16029 10849 16775 13350 16514 11803 19317 13919 27125 13169 16458
> perCapInc4
 [1] 20786 19588 24400 18042 23779 25193 16399 22148 17185 18934 21307 25523 18625 15399
[15] 28532 21420 16365 15191 28819 16194 19215 15881 15453 17518 22156 18545 20997 16807
[29] 22507 22055 15238 21902 16365 19465 17268 14710 19932 15701 19942 16116 11467 21327
[43] 16790 37541 22025 16022 21421 17221 18786 17009 15374 13394 17140 15051 13961 20168
[57] 17312 15301 16277 15582 19727 11379 15874 16002 19250 14197 16728 16138 11396 17272
[71] 17332 22668 14523 13681 11490 13907 18504
```

```
> bDeg1
  [1] 16.6 15.2 35.4 22.6 23.0 30.0 20.0 35.3 25.8 34.2 31.7 24.2 24.0 26.3 22.2 32.1 26.5
 [18] 25.9 27.7 34.4 18.3 28.4 19.7 24.8 24.8 15.9 21.0 25.0 24.4 17.6 18.7 25.2 22.2 15.3
 [35] 16.7 36.7 23.6 34.7 15.4 13.9 15.1 26.4 13.1 29.5 19.5 28.3 19.6 16.2 33.0 24.8 21.8
 [52] 16.7 16.7 25.9 27.6 38.3 18.6 18.1 16.4 13.6 14.8 20.7 13.6 22.9 28.1 11.9 25.2 25.0 [69] 21.6 19.0 10.8 20.5 19.5 8.1 15.6 23.0 17.7 31.9 9.3 28.2 14.2 20.9 10.8 34.0 24.9
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[103] 16.8
> bDeg2
  [1] 22.8 13.7 20.1 30.2 31.6 29.2 26.6 19.3 23.7 21.4 36.0 13.5 20.0 20.0 32.0 19.7 20.7
 [18] 28.8 12.8 17.0 12.8 24.9 22.2 15.3 14.3 34.2 18.0 40.5 21.4 27.1 19.0 18.7 41.9 29.2
 [35] 27.6 12.3 14.0 14.7 16.7 14.4 19.2 11.4 27.1 17.5 27.6 21.2 13.0 20.7 17.3 17.7 18.7
 [52] 21.0 19.5 22.4 16.5 34.1 9.0 16.0 10.3 16.7 22.3 11.1 14.2 20.0 14.5 12.9 15.0 12.2
 [69] 26.2 10.7 17.6 16.7 18.2 13.3 26.0 13.8 10.5 11.7 30.7 29.0 18.5 13.0 12.7 11.6 21.3
 [86] 13.6 18.0 16.5 17.5 14.8 19.6 13.5 21.9 36.5 11.0 11.4 32.9 36.2 8.5 11.7 10.5 29.5
[103] 18.1 13.8 15.5 26.5 25.4 13.9
 [1] 25.4 18.8 26.3 18.8 19.7 24.0 22.1 18.5 20.2 20.8 49.0 49.9 15.5 25.5 25.0 21.2 18.4 [18] 19.3 19.9 31.6 33.3 22.6 15.2 34.7 32.7 28.3 24.4 23.7 22.4 18.8 33.0 24.6 35.3 12.9
 [35] 20.4 25.5 11.5 27.5 15.5 14.8 29.6 23.5 24.8 23.9 16.4 21.0 22.4 17.0 26.3 28.0 19.7
 [52] 9.1 21.9 16.6 32.3 24.1 39.1 18.2 16.8 12.0 26.4 18.2 15.5 30.1 14.3 30.2 30.6 23.4
 [69] 19.3 18.6 27.6 15.5 24.2 17.6 11.5 37.1 15.1 17.2 17.3 16.6 46.9 19.4 21.5 14.7 33.4
 [86] 34.6 16.6 10.8 19.1 25.9 52.3 18.4 14.7 21.0 16.3 22.5 12.7 22.3 16.9 19.8 20.0 22.0
[103] 13.1 17.0 13.4 12.9 23.1 16.0 21.0 15.6 18.9 17.0 24.6 19.1 11.1 14.6 16.9 15.7 10.0
[120] 19.6 16.5 35.8 17.2 21.2 20.7 11.4 18.7 14.2 14.2 14.4 14.8 20.0 18.4 48.5 13.4 11.7
[137] 14.6 21.9 11.2 26.4 9.1 17.9 11.0 17.7 12.7 14.4 15.0 16.2 9.7 20.3 16.5 15.5
> bDeg4
[1] 22.3 25.3 27.8 22.1 32.8 32.6 14.9 28.8 14.6 23.0 24.6 31.6 13.8 23.8 35.0 23.0 16.9 [18] 23.3 31.3 17.5 23.7 13.3 13.2 26.7 29.0 19.3 30.7 25.8 35.2 24.5 13.0 26.6 20.6 21.5
[35] 18.7 11.8 29.8 22.2 23.6 13.0 26.2 20.7 16.8 44.0 29.7 17.5 42.1 22.9 24.9 19.8 13.7
[52] 23.5 32.3 19.5 12.0 22.7 24.7 18.0 13.7 17.6 30.3 21.9 18.4 22.0 20.8 14.0 18.5 20.0
[69] 8.2 21.5 23.3 22.3 9.7 17.7 12.7 9.0 17.8
> coef1
              Estimate Std. Error t value
                                                 Pr(>|t|)
(Intercept) 9223.8156 851.77065 10.82899 1.347038e-18
bDeg1
              522.1588
                        37.13141 14.06246 1.589101e-25
> coef2
               Estimate Std. Error t value
                                                  Pr(>|t|)
(Intercept) 13581.4052 575.1441 23.61392 5.068448e-44
                           27.2296 8.76507 3.344138e-14
bDeg2
               238,6694
> coef3
               Estimate Std. Error t value
                                                  Pr(>|t|)
(Intercept) 10529.7851 612.48431 17.19193 2.751512e-37
bDeq3
               330.6117
                         27.13115 12.18569 3.539586e-24
> coef4
              Estimate Std. Error t value
                                                 Pr(>|t|)
(Intercept) 8615.0527 1052.19722 8.187679 5.242270e-12
```

Code

bDeg4

```
#PROJECT BEGINS: PART I

#Project 1.43:

# first predictor variable
  totalPop <- CDI_dataset$V5
# second predictor variable
  numHospBeds <- CDI_dataset$V9</pre>
```

440.3157 45.36812 9.705399 6.855606e-15

```
# third predictor variable
 totalPersonalIncome <- CDI dataset$V16</pre>
# response variable
numActivePhys <- CDI dataset$V8</pre>
# 1: totalPop vs numActivePhys
fit1 = lm(numActivePhys~totalPop, data = CDI dataset)
summary(fit1)
beta1hat1 = coef(summary(fit1))[2]
beta0hat1 = coef(summary(fit1))[1]
#a) REGRESSION FUNCTION 1:
#Yhat = -110.6348 + 0.002795425X
#Estimated Number of Active Physicians = -110.6348 + 0.002795425
(Total Population)
# 2: numHospBeds vs numActivePhys
fit2 = lm(numActivePhys~numHospBeds, data = CDI dataset)
summary(fit2)
beta1hat2 = coef(summary(fit2))[2]
beta0hat2 = coef(summary(fit2))[1]
#a) REGRESSION FUNCTION 2:
#Yhat = -95.93218 + 0.7431164X
#Estimated Number of Active Physicians = -95.93218 + 0.7431164 (Number
of Hospital Beds)
# 3: totalPersonalIncome vs numActivePhys
fit3 = lm(numActivePhys~totalPersonalIncome, data = CDI dataset)
summary(fit3)
beta1hat3 = coef(summary(fit3))[2]
beta0hat3 = coef(summary(fit3))[1]
#a) REGRESSION FUNCTION 3:
#Yhat = -48.39485 + 0.1317012X
\#Estimated Number of Active Physicians = -48.39485 + 0.1317012 (Total)
Personal Income)
#1.43 b)
#1st plot and regression line
```

```
plot(totalPop,numActivePhys, xlab = 'Total Population', ylab =
'Number of Active Physicians', main = 'Number of Active Physicians vs
Total Population')
abline(fit1, col = 'red')
#2nd plot and regression line
plot(numHospBeds,numActivePhys, xlab = 'Number of Hospital Beds',
ylab = 'Number of Active Physicians', main = 'Number of Active
Physicians vs Number of Hospital Beds')
abline(fit2, col = 'blue')
#3rd plot and regression line
plot(totalPersonalIncome, numActivePhys, xlab = 'Total Personal
Income', ylab = 'Number of Active Physicians', main = 'Number of
Active Physicians vs Total Personal Income')
abline(fit3, col = 'green')
#Yes, the linear regression relations appear to be a good fit for the
data.
#c)
#The predictor variable which leads to the smallest variability
around the regression line is number of hospital beds.
#MSE totalPop - 1:
residualStandardError1 = summary(fit1)$sigma
MSE1 = residualStandardError1^2
\#MSE1 = 372203.5
#MSE numHospBeds - 2:
residualStandardError2 = summary(fit2)$sigma
MSE2 = residualStandardError2^2
\#MSE2 = 310191.9
#MSE totalPersonalIncome - 3:
residualStandardError3 = summary(fit3)$sigma
MSE3 = residualStandardError3^2
\#MSE3 = 324539.4
```

#______#Project 1.44:

```
#data stored in regions
regions <- CDI dataset$V17</pre>
#per capita income
perCapInc <- CDI dataset$V15</pre>
#bachelor degree
bDeg <- CDI dataset$V12
#region 1: NE
reg1 <- regions==1</pre>
perCapInc1 <- perCapInc[reg1]</pre>
bDeg1 <- bDeg[reg1]</pre>
coef1 <- coef(summary(lm(perCapInc1~bDeg1)))</pre>
#region 2: NC
reg2 <- regions==2</pre>
bDeg2 <- bDeg[reg2]</pre>
perCapInc2 <- perCapInc[reg2]</pre>
coef2 <- coef(summary(lm(perCapInc2~bDeg2)))</pre>
#region 3: S
reg3 <- regions==3</pre>
bDeg3 <- bDeg[reg3]</pre>
perCapInc3 <- perCapInc[reg3]</pre>
coef3 <- coef(summary(lm(perCapInc3~bDeg3)))</pre>
#region 4: W
reg4 <- regions==4</pre>
bDeg4 <- bDeg[reg4]</pre>
perCapInc4 <- perCapInc[reg4]</pre>
coef4 <- coef(summary(lm(perCapInc4~bDeg4)))</pre>
#a) REGRESSION FUNCTIONS:
\# Region 1: y = 9223.8156 + 422.1588x
```

```
# Region 2: y = 13581.4052 + 238.6694x
# Region 3: y = 10529.7851 + 330.6117x
# Region 4: y = 8615.0527 + 440.3157x
#*******
#PART II
\#R^2 and r info:
summary(fit1)$r.squared
#summary(fit1)$adj.r.squared
summary(fit2)$r.squared
#summary(fit2)$adj.r.squared
summary(fit3)$r.squared
#summary(fit3)$adj.r.squared
#********
#PART III:
#2.63:
anova(lm(perCapInc1~bDeg1))
anova(lm(perCapInc2~bDeg2))
anova(lm(perCapInc3~bDeg3))
anova(lm(perCapInc4~bDeg4))
#********
# #
#PART IV:
#residuals 3.25:
residuals1 = fit1$residuals
residuals2 = fit2$residuals
residuals3 = fit3$residuals
#residual plots against x
resPlot1.lm = lm(numActivePhys ~ totalPop, data = CDI dataset)
numActivePhys.resid = resid(resPlot1.lm)
plot(totalPop,numActivePhys.resid , ylab="Residuals", xlab="Total
Population", main="Residuals vs Total Population")
abline(0, 0)
```

```
resPlot2.lm = lm(numActivePhys ~ numHospBeds, data = CDI dataset)
numActivePhys.resid = resid(resPlot2.lm)
plot(numHospBeds, numActivePhys.resid , ylab="Residuals", xlab="Number
of Hospital Beds", main="Residuals vs Number of Hospital Beds")
abline(0, 0)
resPlot3.lm = lm(numActivePhys ~ totalPersonalIncome, data =
CDI dataset)
numActivePhys.resid = resid(resPlot3.lm)
plot(totalPersonalIncome, numActivePhys.resid , ylab="Residuals",
xlab="Total Personal Income", main="Residuals vs Total Personal
Income")
abline(0, 0)
#aa plot 1
resplot1.lm = lm(numActivePhys ~ totalPop, data=CDI dataset)
numActivePhys.stdres1 = rstandard(resplot1.lm)
qqnorm(numActivePhys.stdres1, ylab="Standardized Residuals",
xlab="Normal Scores", main="Number of Active Physicians in the Total
Population")
qqline(numActivePhys.stdres1)
#aa plot 2
resplot2.lm = lm(numActivePhys ~ numHospBeds, data=CDI dataset)
numActivePhys.stdres2 = rstandard(resplot2.lm)
qqnorm(numActivePhys.stdres2, ylab="Standardized Residuals",
xlab="Normal Scores", main="Number of Active Physicians and Number of
Hospital Beds")
qqline(numActivePhys.stdres2)
#aa plot 3
resplot3.lm = lm(numActivePhys ~ totalPersonalIncome,
data=CDI dataset)
numActivePhys.stdres3 = rstandard(resplot3.lm)
qqnorm(numActivePhys.stdres3, ylab="Standardized Residuals",
xlab="Normal Scores", main="Number of Active Physicians and Total
Personal Income")
ggline(numActivePhys.stdres3)
```