いろいろな関数の微分

2022.7.4

復習十

微分係数と導関数

ullet a における微分係数 f'(a)

$$f'(a) = \lim_{z o a} rac{f(z)-f(a)}{z-a}$$

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- 導関数
 - ・微分係数 f'(a) は a の関数
 - ・a をx と書き,導関数という

$$f'(x) = \lim_{z o x} rac{f(z)-f(x)}{z-x}$$

・導関数を求めることを「微分する」

• 定数
$$c$$
について $(c)' = \lim_{z o x} rac{c-c}{z-x}$

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$$(x^2)' = \lim_{z \to x} \frac{z^2 - x^2}{z - x} = \lim_{z \to x} (z + x)$$

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 一般に $(x^n)' = ig| m{n} x^{n-1}$

$$\bullet \ (f+g)' = f' + g'$$

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例)
$$(x^2+3x+4)'=(x^2)'+(3x)'+(4)'$$

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- $\bullet \ (f-g)' = f'-g'$
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例)
$$(x^2+3x+4)'=(x^2)'+(3x)'+(4)'=2x+3$$

積と商の微分・記法

$$ullet$$
 $|(fg)'=f'g+fg'|$ 積の微分公式

(fg)' = f'g + fg' 積の微分公式

$$ig(f(x)g(x)ig)' = \lim_{z o x}rac{f(z)g(z)-f(x)g(x)}{z-x}$$

$$egin{aligned} ig(f(x)g(x)ig)' &= \lim_{z o x} rac{f(z)g(z)-f(x)g(x)}{z-x} \ &= \lim_{z o x} rac{ig(f(z)-f(x)ig)g(z)+f(x)ig(g(z)-g(x)ig)}{z-x} \ &= \lim_{z o x} igg(rac{f(z)-f(x)}{z-x}g(z)+f(x)rac{g(z)-g(x)}{z-x}igg) \end{aligned}$$

$$egin{aligned} ig(f(x)g(x)ig)' &= \lim_{z o x} rac{f(z)g(z) - f(x)g(x)}{z - x} \ &= \lim_{z o x} rac{ig(f(z) - f(x)ig)g(z) + f(x)ig(g(z) - g(x)ig)}{z - x} \ &= \lim_{z o x} igg(rac{f(z) - f(x)}{z - x}g(z) + f(x)rac{g(z) - g(x)}{z - x}igg) \ &= f'(x)g(x) + f(x)g'(x) \end{aligned}$$

例
$$(1)$$
 $y' = ((x+1)(x^2+2x+3))'$

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例
$$(2)$$
 $(x \cdot \frac{1}{x})' = (1)' = 0$

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$$ullet \left(rac{f}{g}
ight)' = rac{f'\,g - f\,g'}{g^2}$$
 商の微分公式

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 $\left(\frac{1}{x}\right)' = \frac{(1)'(x) - 1(x)'}{x^2} = \frac{0-1}{x^2}$

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例 (2) $\left(\frac{1}{x}\right)' = \frac{(1)'(x) - 1(x)'}{x^2} = \frac{0-1}{x^2} = -\frac{1}{x^2}$

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課題 0704-1 次を微分せよ.

[1]
$$y = \frac{x}{x+1}$$
 [2] $y = \frac{1}{x^2}$

• 関数 y=f(x) を変数 x で微分する $y',\ f'(x)$ (ラグランジュ)

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ullet 関数 y=f(x) を変数 x で微分する

$$y', \ f'(x) \ ($$
ラグランジュ $)$ $\frac{dy}{dx} \ ($ ライプニッツ $)$ $\lim_{z \to x} \frac{f(z) - f(x)}{z - x}$ $= \lim_{z \to x} \frac{\Delta y}{\Delta x}$

• 関数 y=f(x) を変数 x で微分する $y',\ f'(x)$ (ラグランジュ) $\lim_{z\to x} \frac{f(z)-f(x)}{z-x}$ 例) $y=f(x)=x^3$ $=\lim_{z\to x} \frac{\Delta y}{\Delta x}$

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べき関数の微分

ullet n が正の整数のとき $|(x^n)'=nx^{n-1}|$

$$(x^n)' = nx^{n-1}$$

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• 分数乗

$$(x^{\frac{1}{2}})'=(\sqrt{x})'$$

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 $\sqrt{z}=w,\sqrt{x}=u$ とおくと $z=w^2,x=u^2$

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$$(x^{rac{1}{2}})' = (\sqrt{x})' = \lim_{z o x} rac{\sqrt{z} - \sqrt{x}}{z - x} = \lim_{w o u} rac{w - u}{w^2 - u^2}$$
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 $\sqrt{z} = w, \sqrt{x} = u$ とおくと $z = w^2, x = u^2$
 $= \lim_{w o u} rac{1}{w + u} = rac{1}{2u}$

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$$(x^n)' = nx^{n-1}$$

$$(x^{rac{1}{2}})' = (\sqrt{x})' = \lim_{z o x} rac{\sqrt{z} - \sqrt{x}}{z - x} = \lim_{w o u} rac{w - u}{w^2 - u^2} \ orall_{z = w, \sqrt{x} = u} ag{55} < z = v^2, x = u^2 \ = \lim_{w o u} rac{1}{w + u} = rac{1}{2u} = rac{1}{2\sqrt{x}} = rac{1}{2}x^{-rac{1}{2}}$$

ullet n が正の整数のとき $|(x^n)' = nx^{n-1}|$

$$(x^n)' = nx^{n-1}$$

分数乗

課題 0704-2 $w^3-u^3=(w-u)(w^2+wu+u^2)$ を用い $(x^{\frac{1}{3}})'$ を求めよ.

$$ullet (x^p)' =$$

$$ullet (x^p)' = ig| px^{p-1}$$

- $ullet (x^p)' = ig| px^{p-1}$
- マイナス乗も同じ $(\frac{1}{x})'$

- $ullet (x^p)' = ig| px^{p-1}$
- マイナス乗も同じ $(\frac{1}{x})' = (x^{-1})'$

$$ullet (x^p)' = \boxed{px^{p-1}}$$

• マイナス乗も同じ

$$(\frac{1}{x})' = (x^{-1})' = -x^{-2}$$

$$ullet (x^p)' = \boxed{px^{p-1}}$$

• マイナス乗も同じ

$$(\frac{1}{x})' = (x^{-1})' = -x^{-2} = -\frac{1}{x^2}$$

$$ullet (x^p)' = \boxed{px^{p-1}}$$

マイナス乗も同じ

$$(rac{1}{x})' = (x^{-1})' = -x^{-2} = -rac{1}{x^2}$$

課題 0704-3 次の関数を微分せよ.

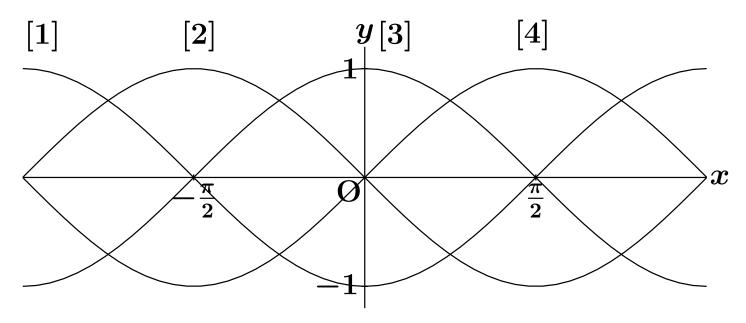
$$[1] \hspace{.15cm} \boldsymbol{y} \hspace{.15cm} = \hspace{.15cm} \boldsymbol{x}^{\frac{1}{4}}$$

$$[2] \,\,\, y \,\,=\,\, x^{-2}$$

$$[1] \,\, y \, = \, x^{rac{1}{4}} \qquad \qquad [2] \,\, y \, = \, x^{-2} \qquad \qquad [3] \,\, y \, = \, x^{-rac{1}{2}}$$

三角関数の微分

三角関数のグラフ



課題 0704-4 上の図は

 $y=\sin x, y=\cos x, y=-\sin x, y=-\cos x$ のグラフである. [1]–[4] の関数を答えよ.

$\sin x,\cos x$ の微分

課題 0704-5 「導関数の意味」を用いて導関数を求めよ.

$$[1] y = \sin x$$

$$[2] y = \cos x$$

$\sin x,\cos x$ の微分

課題 0704-5 「導関数の意味」を用いて導関数を求めよ.

$$[1] y = \sin x$$

$$[2] y = \cos x$$

• 微分公式

$$(\sin x)' = \cos x, \ (\cos x)' = -\sin x$$

$\sin x,\cos x$ の微分

課題 0704-5 「導関数の意味」を用いて導関数を求めよ.

$$[1] y = \sin x$$

$$[2] y = \cos x$$

• 微分公式

$$(\sin x)' = \cos x, \ (\cos x)' = -\sin x$$

課題 0704-6 次の問いに答えよ

[1] $y = \sin x$ の (0, 0) における接線の傾きを求めよ

$$[2]$$
 $y=2\sin x-3\cos x$ を微分せよ

tan x の微分

$$ullet (an x)' = rac{1}{\cos^2 x}$$

$$\tan x = \frac{\sin x}{\cos x}$$
$$\cos^2 x = (\cos x)^2$$

tan x の微分

$$\bullet \left| (\tan x)' = \frac{1}{\cos^2 x} \right|$$

$$(\tan x)' = (\frac{\sin x}{\cos x})'$$

$$\tan x = \frac{\sin x}{\cos x}$$

$$\cos^2 x = (\cos x)^2$$

an xの微分

$$\bullet \left[(\tan x)' = \frac{1}{\cos^2 x} \right] \quad \tan x = \frac{\sin x}{\cos x} \\
(\tan x)' = \left(\frac{\sin x}{\cos x} \right)' \\
= \frac{(\sin x)'(\cos x) - (\sin x)(\cos x)'}{\cos^2 x}$$

an x の微分

tan x の微分

$$\bullet \left[(\tan x)' = \frac{1}{\cos^2 x} \right] \quad \tan x = \frac{\sin x}{\cos x}
(\tan x)' = \left(\frac{\sin x}{\cos x} \right)'
= \frac{(\sin x)'(\cos x) - (\sin x)(\cos x)'}{\cos^2 x}
= \frac{(\cos x \cos x) - \sin x(-\sin x)'}{\cos^2 x}
= \frac{\cos^2 x + \sin^2 x}{\cos^2 x} = \frac{1}{\cos^2 x}$$

課題

課題 0704-7 次の関数を微分せよ

- $[1] y = \sin x \cos x$
- $[2] y = \sin^2 x (= \sin x \sin x)$
- $[3] y = x \tan x$
- $[4] y = \tan x x$

$$y'=(\sin(ax+b))'=\lim_{z o x}rac{\sin(az+b)-\sin(ax+b)}{z-x}$$

$$y' = (\sin(ax+b))' = \lim_{z \to x} \frac{\sin(az+b) - \sin(ax+b)}{z - x}$$
 $ax + b = u, \ az + b = w$ とおくと
 $w - u = a(z - x), \ w \to u$

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$$f(ax+b)$$
の微分

 $ullet \left| f(ax+b)' = af'(ax+b)
ight|$

$$f(ax+b)$$
の微分

•
$$f(ax+b)'=of'(ax+b)$$
 そのまま微分

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 $\bullet (\cos(3x+1))'$

•
$$f(ax+b)'=of'(ax+b)$$
 そのまま微分

•
$$(\cos(3x+1))' = 3(-\sin(3x+1))$$

•
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$$((2x+3)^5)'$$

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課題 0704-8 微分せよ

[1]
$$y = \sin 3x$$
 [2] $y = (5x+1)^3$
[3] $y = \sqrt{2x+3}$ [4] $y = \tan(-x+1)$