



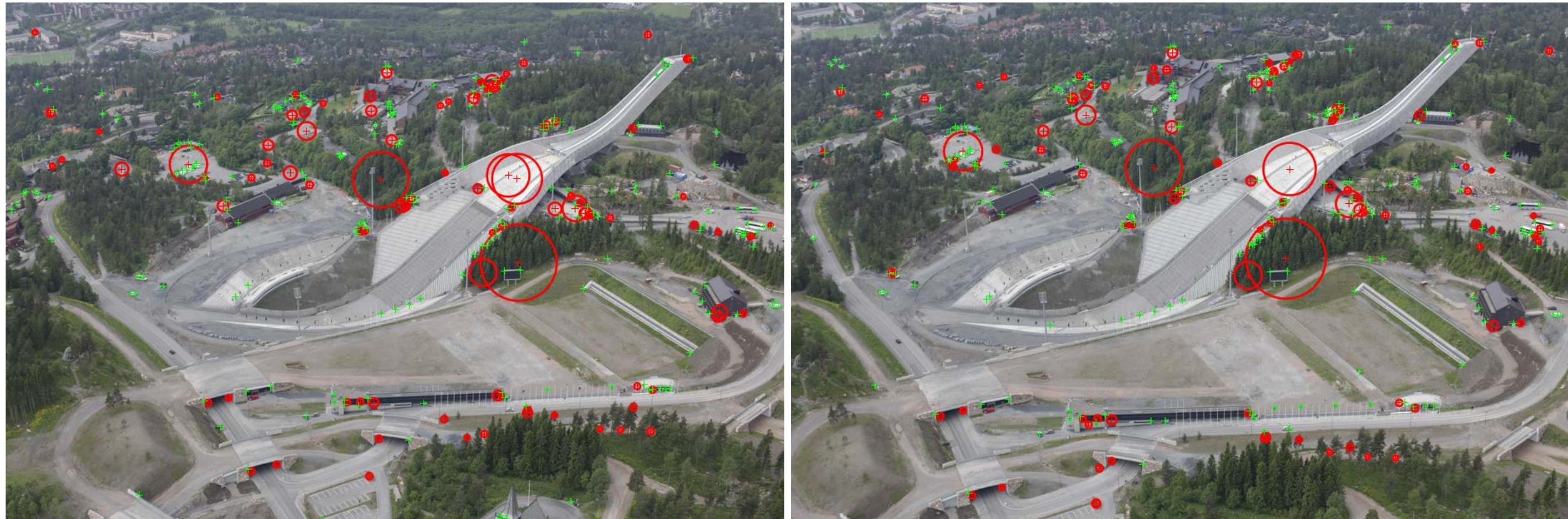
# Lecture 4.0

## From keypoints to correspondences

Trym Vegard Haavardsholm

Illustrations from K. Grauman, B. Leibe, Svetlana Lazebnik,  
David Lowe, Matthew Brown

# Point correspondences from keypoints



How do we match these keypoints?

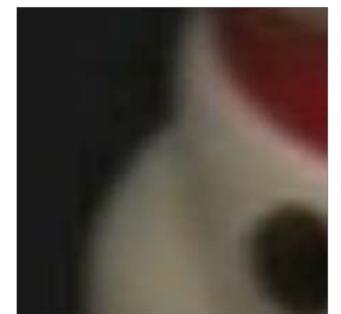
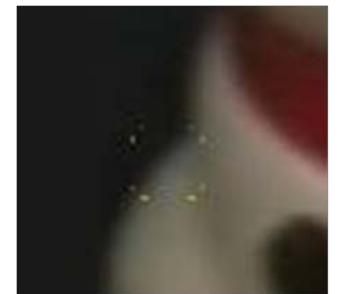
# Local patches

- Covariant feature point detectors
  - Location  $(x, y)$ , scale  $\sigma$  and orientation  $\theta$ .
- Normalize local patches surrounding keypoints
  - Canonical scale

Detect regions



Normalize regions



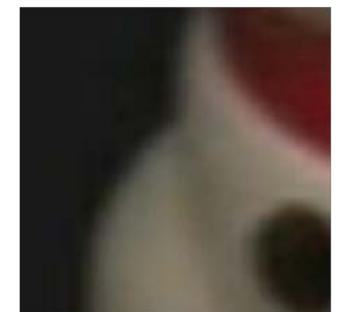
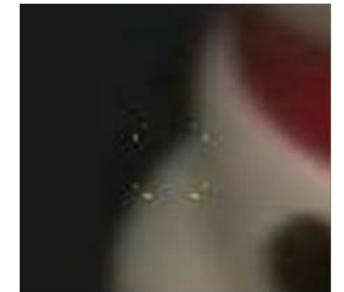
# Local patches

- Covariant feature point detectors
  - Location  $(x, y)$ , scale  $\sigma$  and orientation  $\theta$ .
- Normalize local patches surrounding keypoints
  - Canonical scale
  - Canonical orientation

**Detect regions**



**Normalize regions**



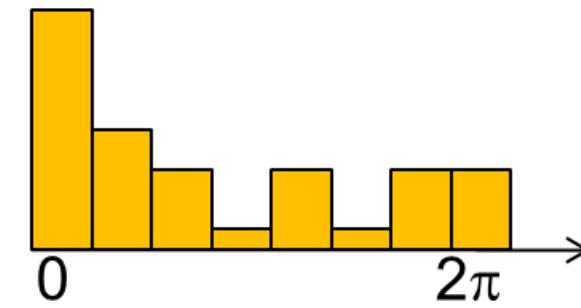
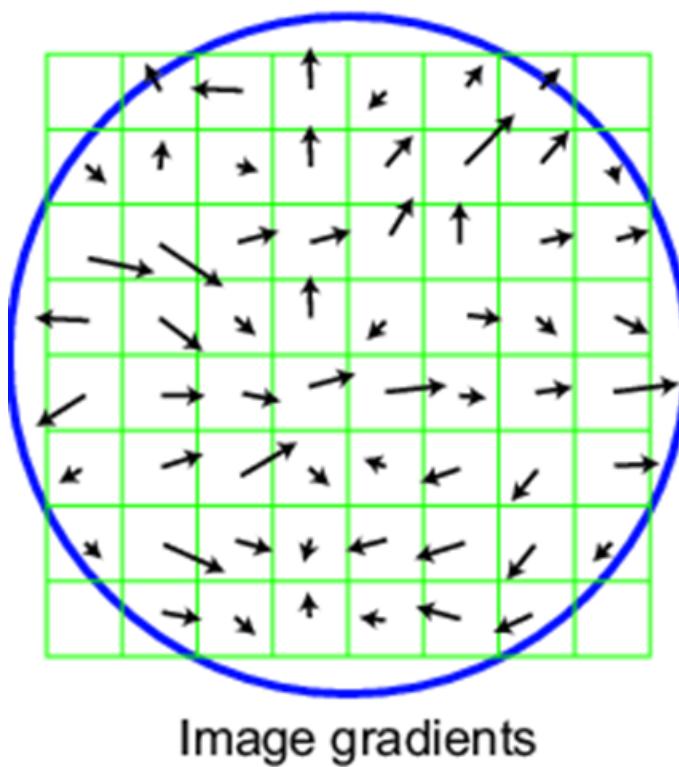
# Estimating canonical orientation

- Find dominant orientation of the image patch
  - This is given by  $\mathbf{x}_{\max}$ , the eigenvector of  $\mathbf{M}$  corresponding to  $\lambda_{\max}$  (the *larger* eigenvalue)
  - Rotate the patch according to this angle

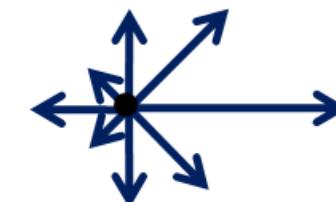


# Estimating canonical orientation

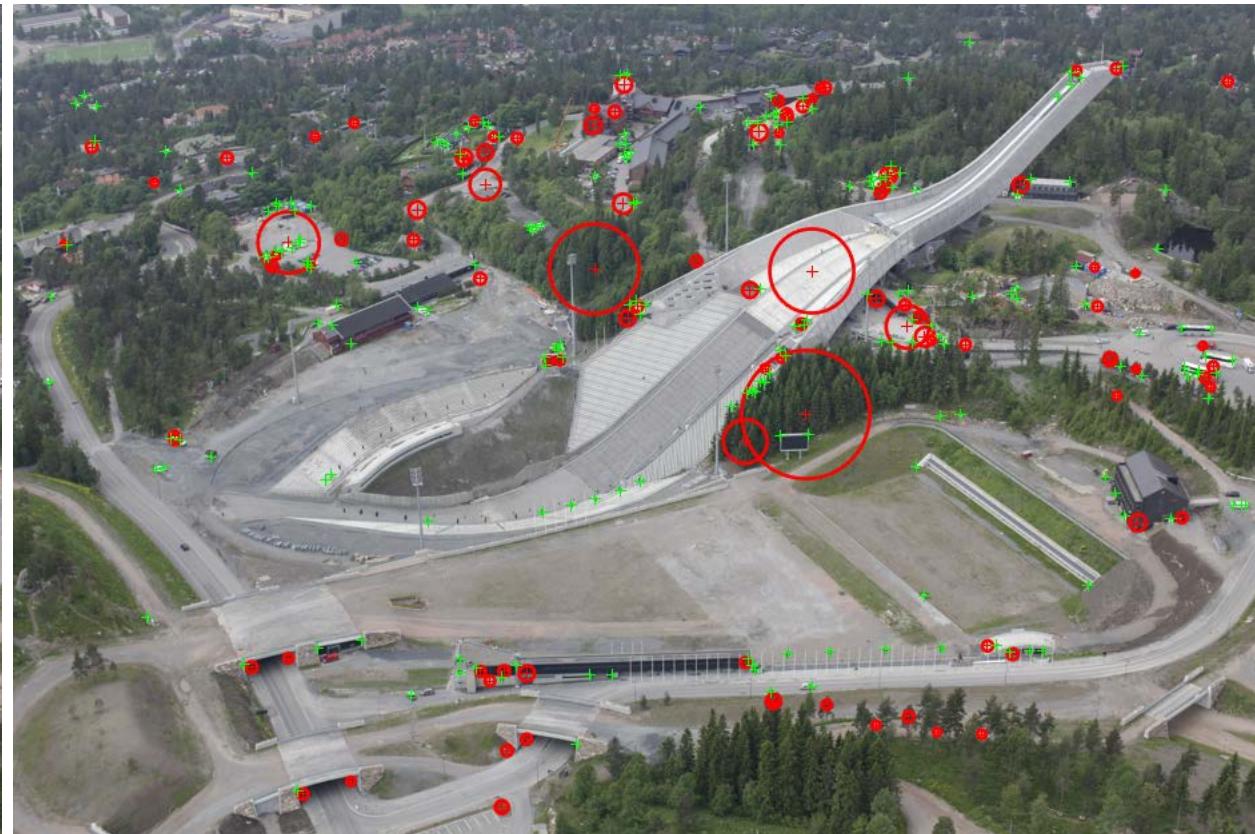
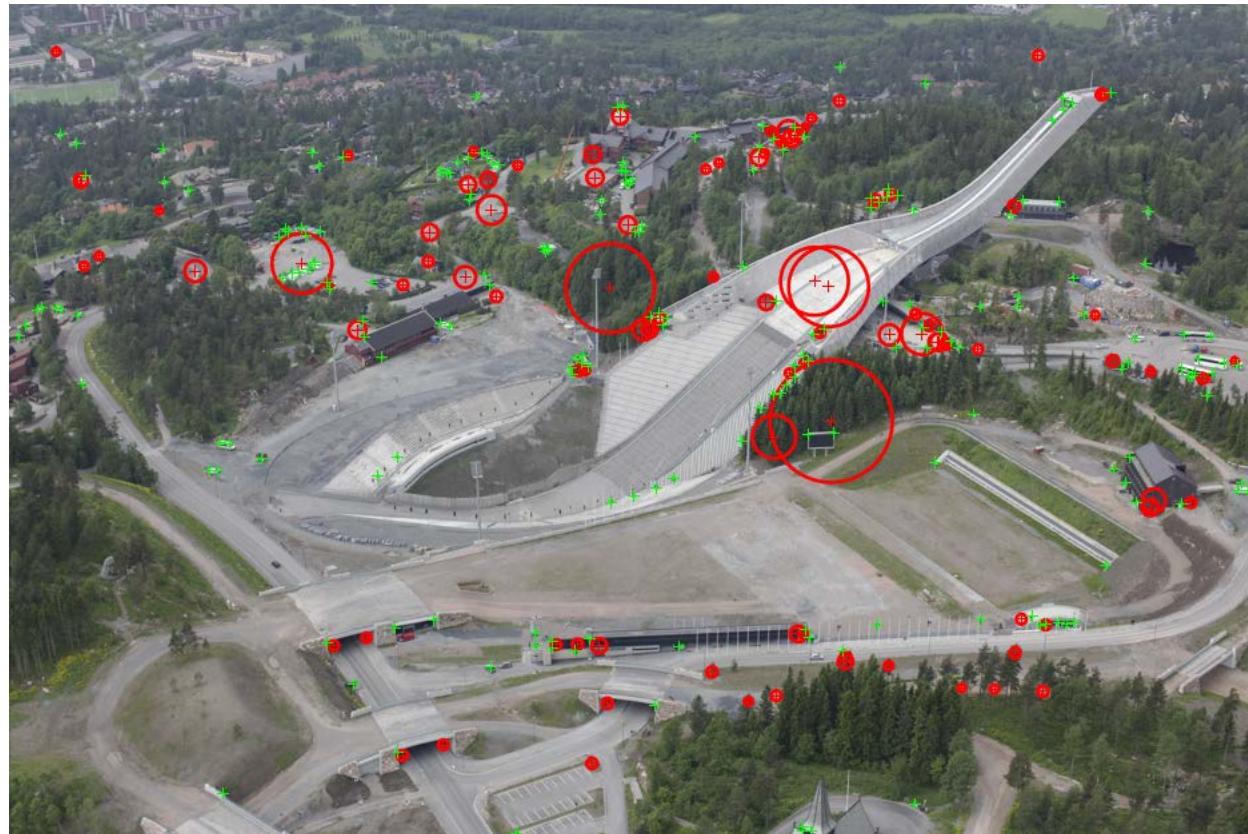
- Orientation from Histogram of Gradients (HoG)



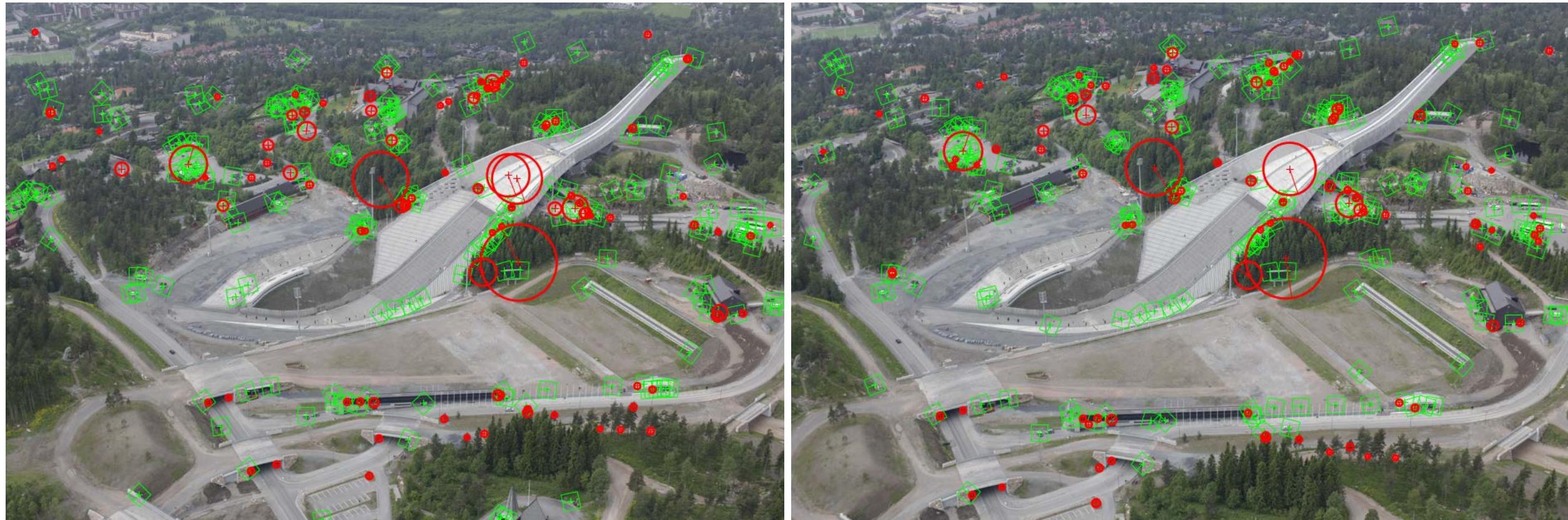
angle histogram



# Estimating canonical orientation: Example



# Estimating canonical orientation: Example



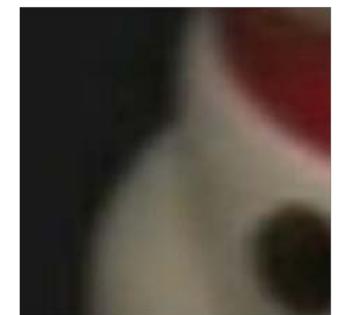
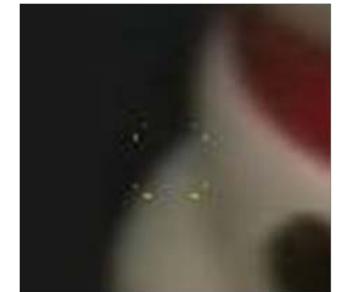
# Local patches

- Covariant feature point detectors
  - Location  $(x, y)$ , scale  $\sigma$  and orientation  $\theta$ .
- Normalize local patches surrounding keypoints
  - Canonical scale
  - Canonical orientation

**Detect regions**



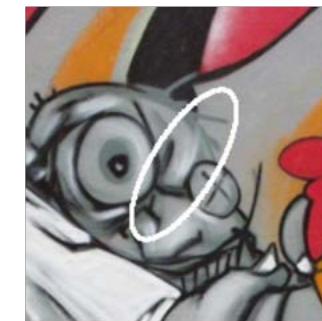
**Normalize regions**



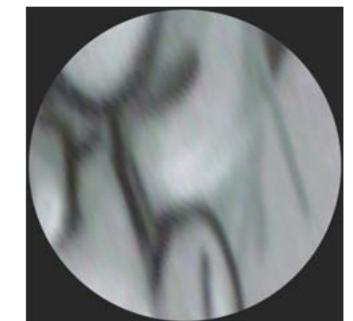
# Local patches

- Covariant feature point detectors
  - Affine transformation  $A$
- Normalize local patches surrounding keypoints
  - Canonical affine transformation

**Detect regions**



**Normalize regions**



# Overview of point feature matching

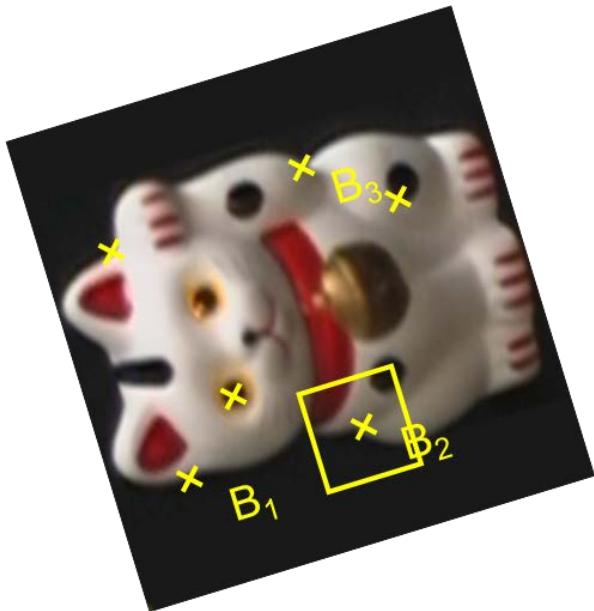
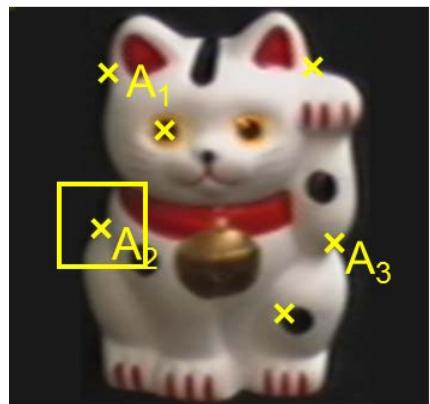


# Overview of point feature matching



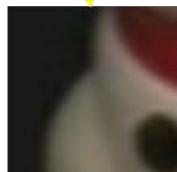
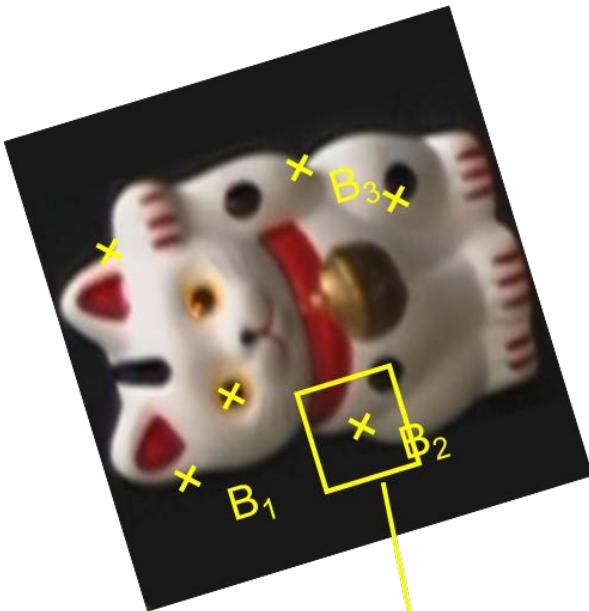
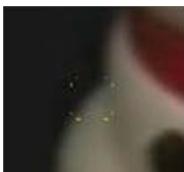
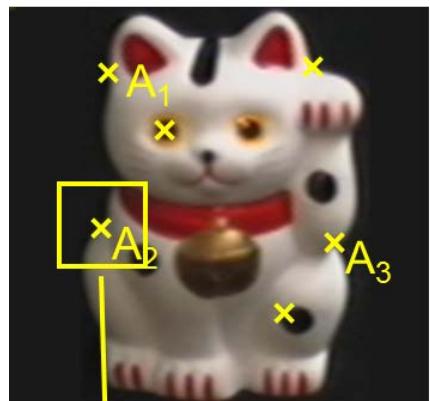
1. Detect a set of distinct feature points

# Overview of point feature matching



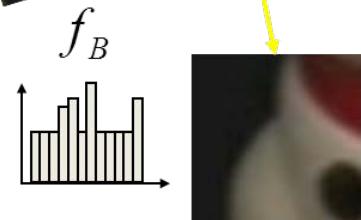
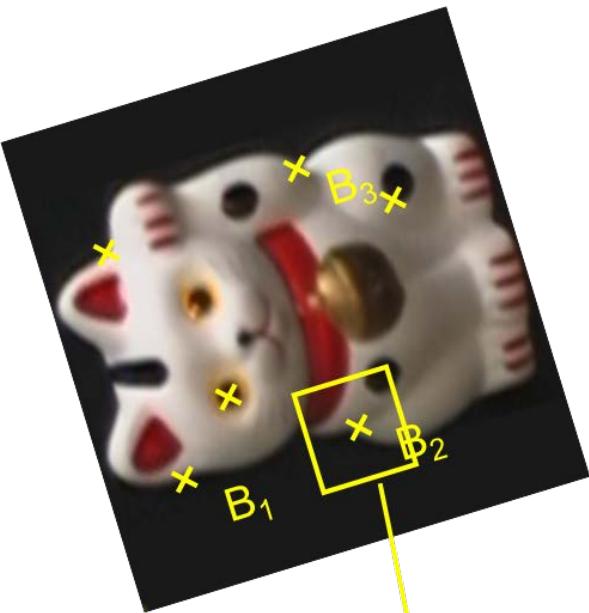
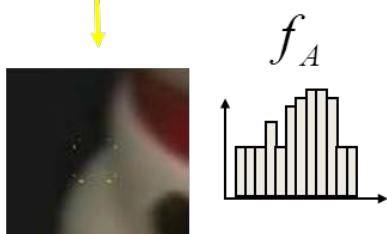
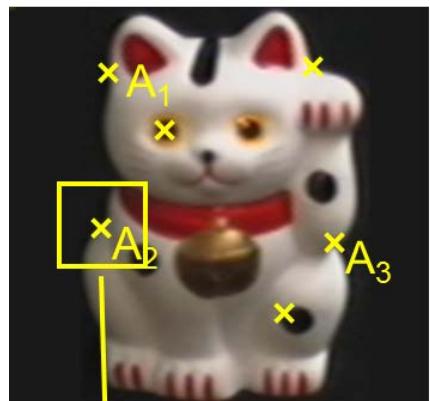
1. Detect a set of distinct feature points
2. Define a patch around each point

# Overview of point feature matching



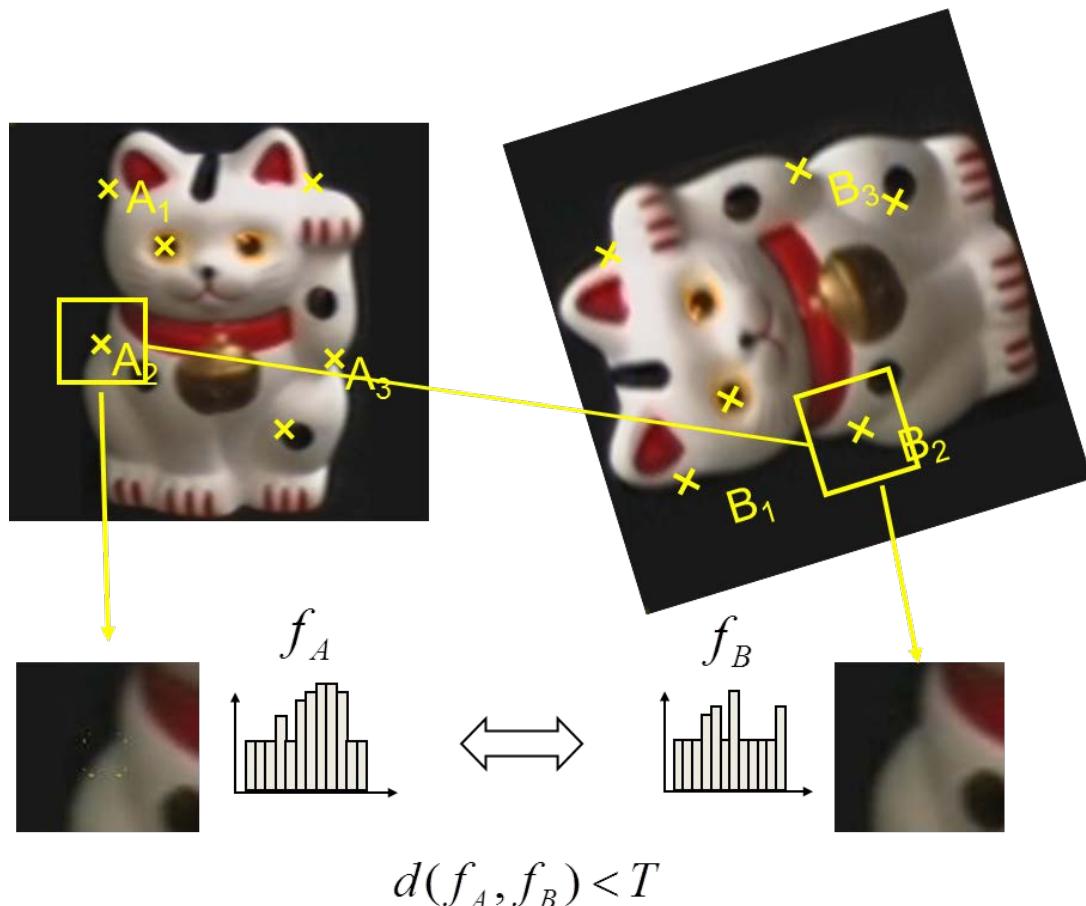
1. Detect a set of distinct feature points
2. Define a patch around each point
3. Extract and normalize the patch

# Overview of point feature matching



1. Detect a set of distinct feature points
2. Define a patch around each point
3. Extract and normalize the patch
4. Compute a local descriptor

# Overview of point feature matching



1. Detect a set of distinct feature points
2. Define a patch around each point
3. Extract and normalize the patch
4. Compute a local descriptor
5. Match local descriptors

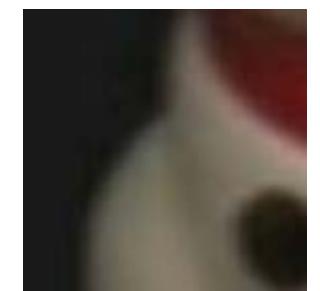
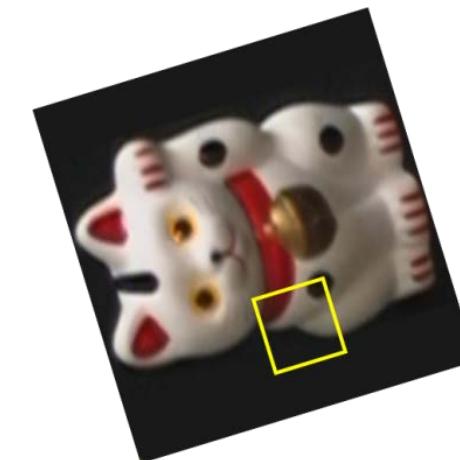
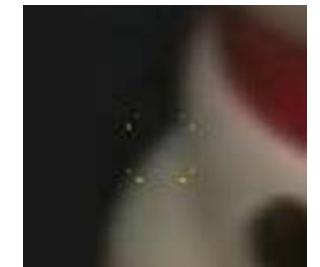
# Feature descriptors

- Simplest descriptor: Vector of raw intensity values
- How to compare two such vectors?

**Detect regions**



**Normalize regions**



# Feature descriptors

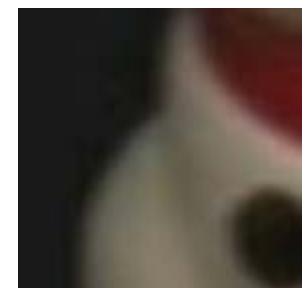
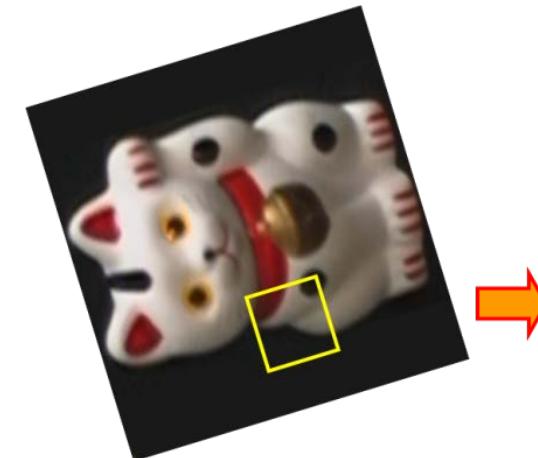
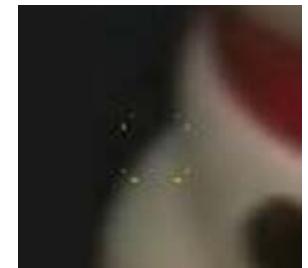
- Simplest descriptor: Vector of raw intensity values
- How to compare two such vectors?
  - Sum of squared differences (SSD)

$$\text{SSD}(u, v) = \sum_i (u_i - v_i)^2$$

Detect regions



Normalize regions



# Feature descriptors

- Simplest descriptor: Vector of raw intensity values

- How to compare two such vectors?

- Sum of squared differences (SSD)

$$\text{SSD}(u, v) = \sum_i (u_i - v_i)^2$$

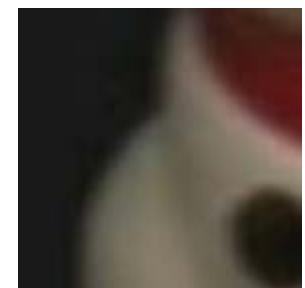
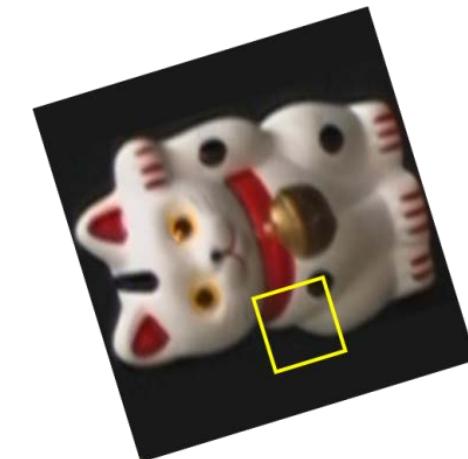
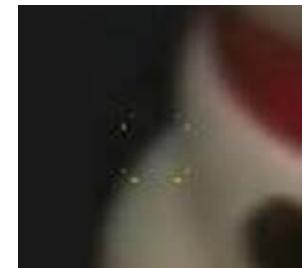
- Normalized correlation

$$\rho(u, v) = \frac{\sum_i (u_i - \bar{u})(v_i - \bar{v})}{\sqrt{\left( \sum_j (u_j - \bar{u})^2 \right) \left( \sum_j (v_j - \bar{v})^2 \right)}}$$

Detect regions



Normalize regions



# A better descriptor

- Robust to small deformations
- Distinctive
- Fast to construct
- Fast to compare

