Bivariate analysis

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M1 MIDS/MFA/LOGOS Université Paris Cité Année 2024 Course Homepage Moodle



Objectives

In Exploratory analysis of tabular data, bivariate analysis is the second step. It consists in exploring, summarizing, visualizing pairs of columns of a dataset.

Setup

```
stopifnot(
  require(tidyverse),
  require(glue),
  require(magrittr),
  require(lobstr),
  require(arrow),
  require(ggforce),
  require(ycd),
  require(ggmosaic),
  require(httr),
  require(patchwork)
)
```

Bivariate techniques depend on the types of columns we are facing.

For numerical/numerical samples

- Scatter plots
- Smoothed lineplots (for example linear regression)
- 2-dimensional density plots

For categorical/categorical samples: mosaicplots and variants

For numerical/categorical samples

- Boxplots per group
- Histograms per group
- Density plots per group
- Quantile-Quantile plots

Dataset

Once again we rely on the Census dataset.

Since 1948, the US Census Bureau carries out a monthly Current Population Survey, collecting data concerning residents aged above 15 from 150000 households. This survey is one of the most important sources of information concerning the american workforce. Data reported in file Recensement.txt originate from the 2012 census.

Load the data into the session environment and call it df. Take advantage of the fact that we saved the result of our data wrangling job in a self-documented file format. Download a parquet file from the following URL:

https://stephane-v-boucheron.fr/data/Recensement.parquet



• Use httr::GET() and WriteBin().

"Administrat~ Bachelor

Solution

1

58 F

NE

C

```
fname <- "Recensement.parquet"</pre>
fpath <- paste(datapath, fname, sep="/")</pre>
if (!file.exists(fpath)) {
 tryCatch(expr = {
   url <- 'https://stephane-v-boucheron.fr/data/Recensement.parquet'
   rep <- httr::GET(url)
   stopifnot(rep$status_code==200)
   con <- file(fpath, open="wb")</pre>
   writeBin(rep$content, con)
    close(con)
 }, warning = function(w) {
    glue("Successful download but {w}")
 }, error = function(e) {
   stop("Houston, we have a problem!") # error-handler-code
 }, finally = {
    if (exists("con") && isOpen(con)){
      close(con)
   }
 }
  )
}
df <- arrow::read_parquet(fpath)</pre>
df |>
 glimpse()
## Rows: 599
## Columns: 11
## $ AGE
              <dbl> 58, 40, 29, 59, 51, 19, 64, 23, 47, 66, 26, 23, 54, 44, 56,~
## $ SEXE
               <fct> F, M, M, M, M, M, F, F, M, F, M, F, F, F, F, F, F, M, M, F,~
## $ REGION
               <fct> NE, W, S, NE, W, NW, S, NE, NW, S, NE, NE, W, NW, S, S, NW,~
## $ STAT_MARI <fct> C, M, C, D, M, C, M, C, M, D, M, C, M, C, M, C, S, M, S, C,~
                <dbl> 13.25, 12.50, 14.00, 10.60, 13.00, 7.00, 19.57, 13.00, 20.1~
## $ SAL_HOR
## $ SYNDICAT <fct> non, non, non, oui, non, non, non, non, oui, non, non, ~
## $ CATEGORIE <fct> "Administration", "Building ", "Administration", "Services"~
## $ NIV_ETUDES <fct> "Bachelor", "12 years schooling, no diploma", "As$ociate de~
## $ NB_PERS
               <fct> 2, 2, 2, 4, 8, 6, 3, 2, 3, 1, 3, 2, 6, 5, 4, 4, 3, 2, 3, 2,~
## $ NB_ENF
                ## $ REV_FOYER <fct> [35000-40000), [17500-20000), [75000-1e+05), [17500-20000),~
df |>
 head()
## # A tibble: 6 x 11
      AGE SEXE REGION STAT MARI SAL HOR SYNDICAT CATEGORIE NIV ETUDES NB PERS
   \langle dbl \rangle \langle fct \rangle \langle fct \rangle = 4 \langle dbl \rangle \langle fct \rangle = \langle fct \rangle
                                                                 <fct>
                                                                            <fct>
```

13.2 non

Categorical/Categorical pairs

```
df |>
  select(where(is.factor)) |>
  head()
```

A tibble: 6 x 9 SEXE REGION STAT_MARI SYNDICAT CATEGORIE NIV_ETUDES NB_PERS NB_ENF REV_FOYER <fct> <fct> <fct> <fct> <fct> <fct> <fct> <fct> <fct> 1 F NEС "Administ~ Bachelor 0 [35000-4~ non 2 M W М "Building~ 12 years ~ 2 0 [17500-2~ non 3 M S C "Administ~ Associate~ 2 [75000-1~ non 0 "Services" 12 years ~ 4 4 M NE D 1 [17500-2~ oui "Services" 9 years s~ 8 5 M W М non 1 [75000-1~ С "Services" 12 years ~ 6 6 M NW 0 [1e+05-1~ non

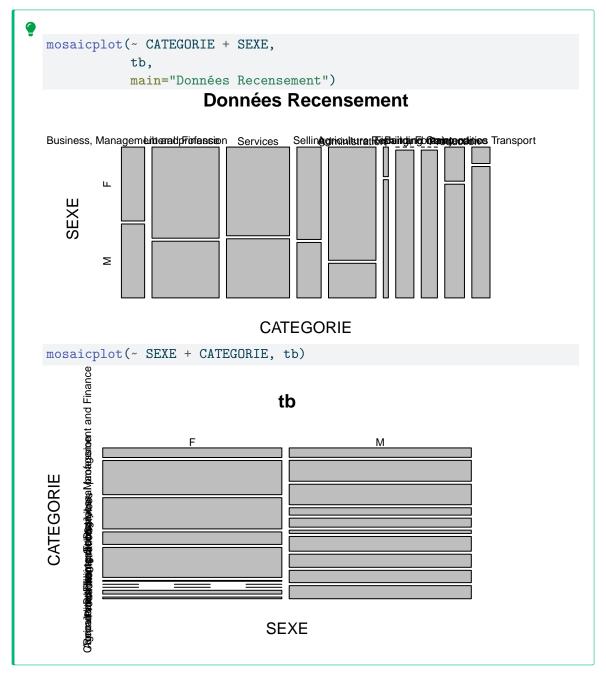
Explore the connection between CATEGORIE and SEX. Compute the 2-ways contingency table using table(), and count() from dplyr.

Use tibble::as_tibble() to transform the output of table() into a dataframe/tibble.

Use tidyr::pivot_wider() so as to obtain a wide (but messy) tibble with the same the same shape as the output of table(). Can you spot a difference?

```
Solution
tb <- df |>
  dplyr::select(CATEGORIE, SEXE) |>
  table()
# tb
tb2 <- df |>
  count(CATEGORIE, SEXE)
tb2
# A tibble: 18 x 3
   CATEGORIE
                                        SEXE
   <fct>
                                        <fct> <int>
 1 "Business, Management and Finance" F
 2 "Business, Management and Finance" M
 3 "Liberal profession"
                                                 82
 4 "Liberal profession"
                                       Μ
                                                 51
 5 "Services"
                                        F
                                                 75
 6 "Services"
                                        Μ
                                                 50
 7 "Selling"
                                        F
                                                 30
 8 "Selling"
                                        Μ
                                                 18
                                        F
                                                 72
 9 "Administration"
                                                 22
10 "Administration"
                                        Μ
11 "Agriculture, Fishing, Forestry"
                                        F
                                                  2
12 "Agriculture, Fishing, Forestry"
                                                  8
                                       Μ
13 "Building "
                                       Μ
                                                 36
14 "Repair and maintenance"
                                       Μ
                                                 32
15 "Production"
                                        F
                                                  9
16 "Production"
                                                 30
                                        М
17 "Commodities Transport"
                                        F
                                                  4
18 "Commodities Transport"
                                                 32
tb2 |>
  pivot_wider(id_cols=CATEGORIE,
              names_from=SEXE,
               values_from=n)
# A tibble: 10 x 3
   CATEGORIE
                                            F
                                                  М
                                        <int> <int>
   <fct>
 1 "Business, Management and Finance"
                                           23
 2 "Liberal profession"
                                           75
 3 "Services"
                                                 50
 4 "Selling"
                                           30
                                                 18
                                           72
 5 "Administration"
                                                 22
 6 "Agriculture, Fishing, Forestry"
                                           2
                                                 8
 7 "Building "
                                           NA
                                                 36
 8 "Repair and maintenance"
                                           NA
                                                 32
 9 "Production"
                                            9
                                                 30
                                            4
                                                 32
10 "Commodities Transport"
```

Use mosaicplot() from base R to visualize the contingency table.



Use geom_mosaic from ggmosaic to visualize the contingency table

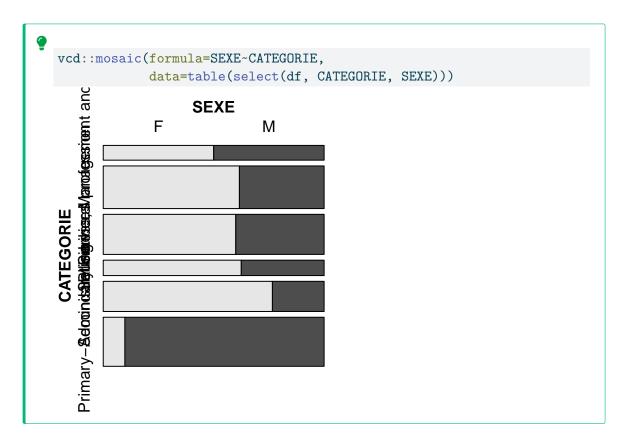
- Make the plot as readable as possible
- $\bullet\,$ Reorder CATEGORIE according to counts

```
rot_x_text <- theme(</pre>
        axis.text.x = element_text(angle = 45)
df |>
       ggplot() +
       geom_mosaic(aes(x=product(SEXE, CATEGORIE), fill=SEXE)) +
       rot_x_text
Warning: The `scale_name` argument of `continuous_scale()` is deprecated as of ggplot2
3.5.0.
Warning: The `trans` argument of `continuous_scale()` is deprecated as of ggplot2 3.5
i Please use the `transform` argument instead.
Warning: `unite_()` was deprecated in tidyr 1.2.0.
i Please use `unite()` instead.
i The deprecated feature was likely used in the ggmosaic package.
        Please report the issue at <a href="https://github.com/haleyjeppson/ggmosaic">https://github.com/haleyjeppson/ggmosaic</a>.
           M -
                                                                                                                                                                                                                                                                        SEXE
 SEXE
                                                                                                                                                                                                                                                                                        F
                                                                                                                                                                                                                                                                                        Μ
                                                                                                                                                       Administration | February | February | Repair | 
                                                                                                                CATEGORIE
```

• Collapse rare levels of CATEGORIE (consider that a level is rare if it has less than 40 occurrences). Use tools from forcats.

Solution

```
df |>
  count(CATEGORIE) |>
 arrange(desc(n))
# A tibble: 10 \times 2
   CATEGORIE
                                            n
   <fct>
                                        <int>
 1 "Liberal profession"
                                          133
 2 "Services"
                                          125
3 "Administration"
                                           94
 4 "Selling"
                                           48
5 "Business, Management and Finance"
                                           46
 6 "Production"
                                           39
7 "Building "
                                           36
8 "Commodities Transport"
                                           36
 9 "Repair and maintenance"
                                           32
10 "Agriculture, Fishing, Forestry"
                                           10
rare_categories <- df |>
 count(CATEGORIE) |>
  filter(n<=40)
rare_categories
# A tibble: 5 \times 2
  CATEGORIE
                                         n
1 "Agriculture, Fishing, Forestry"
                                        10
2 "Building "
                                        36
3 "Repair and maintenance"
                                        32
4 "Production"
                                        39
5 "Commodities Transport"
```



Testing association

Chi-square independence/association test

```
test_1 <- df |>
select(CATEGORIE, SEXE) |>
table() |>
chisq.test()

# test_1 |>
broom::tidy() |>
knitr::kable()

statistic p.value parameter method

140.6717 0 5 Pearson's Chi-squared test
```

The Chi-square statistics can be computed from the contingeny table

```
rowcounts <- apply(tb, MARGIN = 1, FUN = sum)
colcounts <- apply(tb, MARGIN = 2, FUN = sum)

expected <- (rowcounts %*% t(colcounts))/sum(colcounts)

# norm((tb - expected) / sqrt(expected), type = "F")^2

expected |>
as_tibble() |>
knitr::kable()

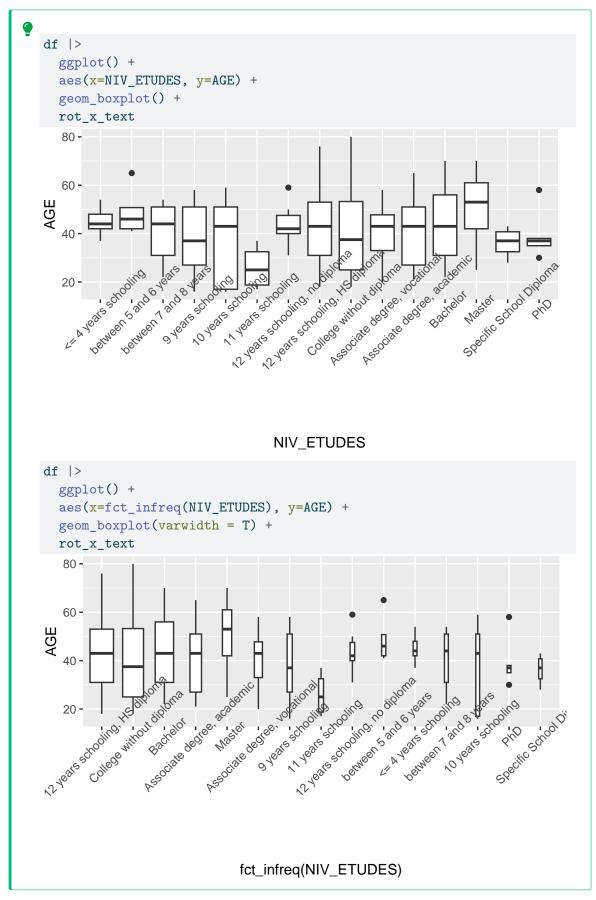
F M

22.80801 23.19199
65.94491 67.05509
61.97830 63.02170
23.79967 24.20033
46.60768 47.39232
75.86144 77.13856
```

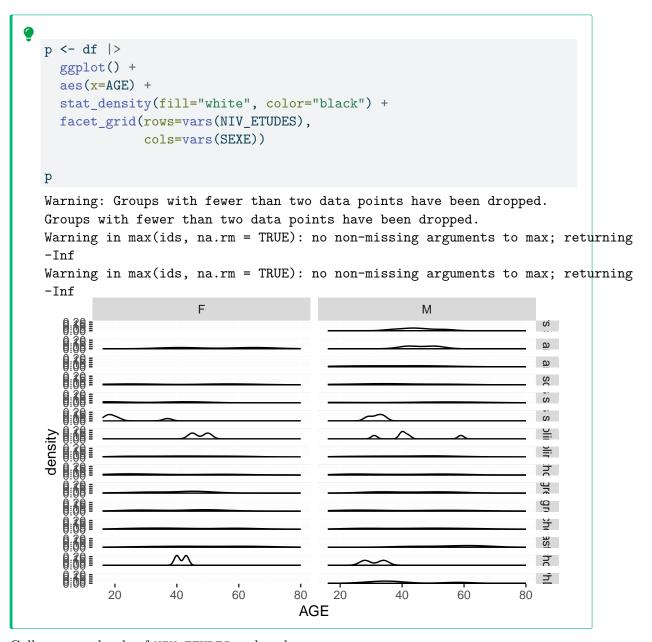
Categorical/Numerical pairs

Grouped boxplots

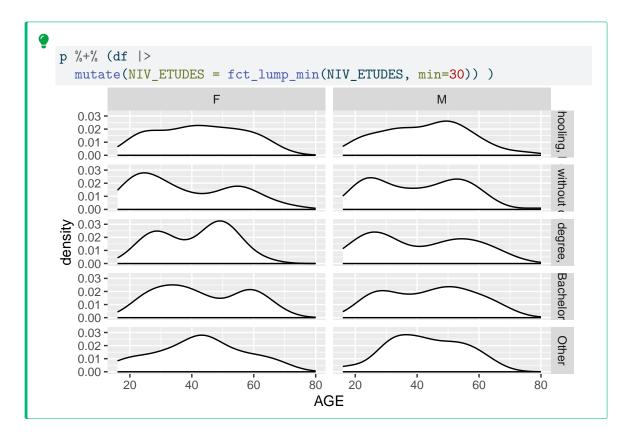
Plot boxplots of AGE according to NIV_ETUDES



Draw density plots of AGE, facet by NIV_ETUDES and SEXE



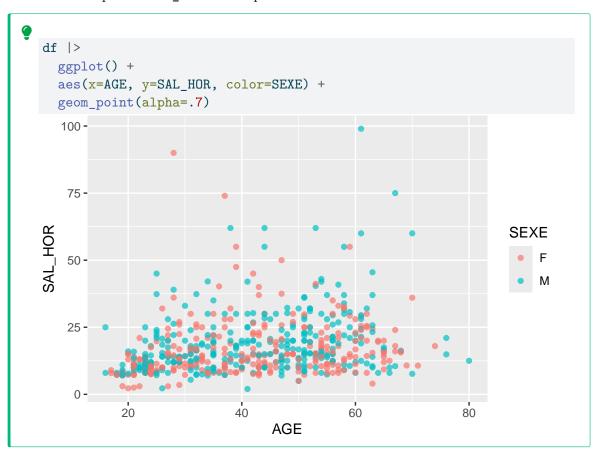
Collapse rare levels of ${\tt NIV_ETUDES}$ and replay.



Numerical/Numerical pairs

Scatterplots

Make a scatterplot of SAL_HOR with respect to AGE



Correlations

- Linear correlation coefficient (Pearson ρ)
- Linear rank correlation coefficient (Spearman, Kendall)
- ξ rank correlation coefficient (Chatterjee)

pairs from base R

ggpairs()

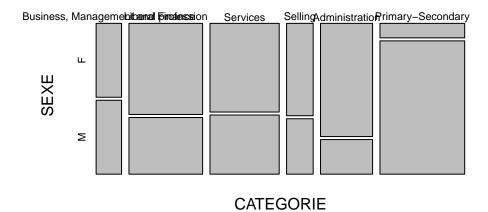
Useful links

- rmarkdown
- dplyr
- ggplot2
- R Graphic Cookbook. Winston Chang. O' Reilly.
- A blog on ggplot object
- skimr
- vcd
- ggmosaic
- ggforce
- arrow
- httr

expand.grid(levels(df\$CATEGORIE), levels(df\$SEXE))

```
Var1 Var2
1
   Business, Management and Finance
2
                                         F
                 Liberal profession
3
                            Services
                                         F
4
                             Selling
                                         F
5
                      Administration
6
                                         F
                  Primary-Secondary
7
   Business, Management and Finance
                                         Μ
8
                  Liberal profession
                                         Μ
9
                            Services
                                         Μ
10
                             Selling
                                         Μ
11
                      Administration
                                         Μ
12
                  Primary-Secondary
                                         Μ
df |>
  select(CATEGORIE, SEXE) |>
  table() |>
  mosaicplot()
```

table(select(df, CATEGORIE, SEXE))



pchisq(140, df=5, lower.tail = F)

[1] 1.789245e-28