# Clustering: hierarchical

#### 2024-09-02

- M1 MIDS/MFA
- Université Paris Cité
- Année 2024-2025
- Course Homepage
- Moodle



### Setup

```
stopifnot(
  require(DT),
  require(skimr),
  require(GGally),
  require(patchwork),
  require(ggforce),
  require(glue),
  require(ggfortify),
  require(ggvoronoi),
  require(magrittr),
  require(broom),
  require(ggdendro),
  require(dendextend),
  require(plotly),
  require(tidyverse)
tidymodels::tidymodels_prefer(quiet = TRUE)
old_theme <-theme_set(</pre>
  theme_minimal(base_size=9,
                base_family = "Helvetica")
knitr::opts_chunk$set(
```

```
knitr::opts_chunk$set(
  message = FALSE,
  warning = FALSE,
```

```
comment=NA,
prompt=FALSE,
cache=FALSE,
echo=TRUE,
results='asis'
)

gc <- options(ggplot2.discrete.colour="viridis")
gc <- options(ggplot2.discrete.fill="viridis")
gc <- options(ggplot2.continuous.fill="viridis")
gc <- options(ggplot2.continuous.colour="viridis")</pre>
```

## Objectives

## Preamble

Hierarchical clustering builds dendrograms

Explore the data structure: dendrograms (objects of class dendrogram) are represented by *lists of lists with attributes* (not by tibbles).

The dendrograms created from objects of class helust represent planar binary trees.

## Question

- How do you define abstractly planar binary trees?
- In dendrograms created from objects of class hclust, what do the leaf nodes represent?
- In dendrograms created from objects of class hclust, what do the internal nodes represent ?

Yeep an eye on Introduction to dendextend by the package author Tal Galili.

## Playing with a toy dendrogram

```
dend <- 1:5 %>%
  dist %>%
  hclust(method="ward.D2") %>%
  as.dendrogram
```

Nodes are identified by their prefix order index (note that this depend on the chosen rotation).

```
dend %>%
  rotate(c(1,2,4,5,3)) %>%
```

```
get_nodes_attr("members",
                 id = c(1, 2, 5, 7))
[1] 5 2 3 1
cophenetic(rotate(dend, c(1,2,4,5,3)))
                      3
         1
2 1.000000
3 3.872983 3.872983
4 3.872983 3.872983 1.000000
5 3.872983 3.872983 1.732051 1.732051
cophenetic(dend)
                  2
                           5
                                    3
2 1.000000
5 3.872983 3.872983
3 3.872983 3.872983 1.732051
4 3.872983 3.872983 1.732051 1.000000
dend %>%
 rotate(c(1,2,4,5,3)) %>%
 get_nodes_attr("height")
[1] 3.872983 1.000000 0.000000 0.000000 1.732051 1.000000 0.000000 0.000000
[9] 0.000000
as.ggdend(rev(dend))
# kmeans(tibble(x=1:5), centers = 2)
```

```
# Get various attributes
dend %>%
get_nodes_attr("height") # node's height
```

```
[1] 3.872983 1.000000 0.000000 1.732051 0.000000 1.000000 0.000000 [9] 0.000000
```

How is attributed height computed? What is its purpose?

What kind of tree traversal is used by get\_nodes\_... helpers?

```
dend %>%
  get_nodes_attr("members")
```

[1] 5 2 1 1 3 1 2 1 1

## Tweaking a dendrogram

Why should we do that?

How should we do that?

#### **USArrests**

We work on USArrests dataset. We want to classify the 50 (united) states on the basis of the arrests profile and the urbanization rate. We rely on hierarchical, bottom-up classification.

```
data("USArrests")

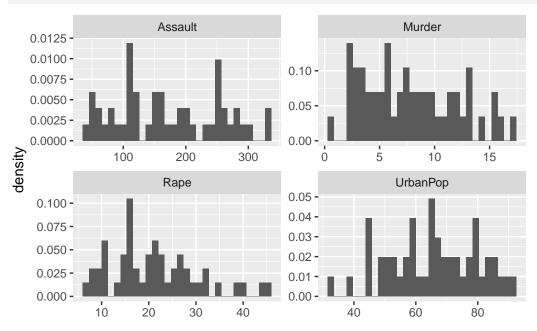
USArrests <- USArrests %>%
    tibble::rownames_to_column(var="region")

USArrests <- USArrests %>%
    mutate(region = tolower(region))

rownames(USArrests) <- USArrests$region

glimpse(USArrests)</pre>
```

#### make\_biotifoul(USArrests, .f=is.numeric)



The function dist is used to calculate pairwise distances between individuals.

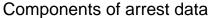
## Question

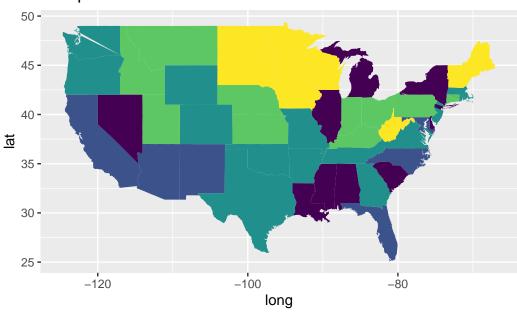
Compute pairwise distances between rows of USArrests (with and without scaling)

#### i Question

Perform hierarchical clustering on unscaled and scaled dataset.

#### Question





# The dendrogram class

## Question

Exploration of results of hierarchical clustering (objects of class hclust) is facilitated by converting to class dendrogram.

## i Question

## Ward method

The meth=ward.D2 option allows you to aggregate individuals according to the method of Ward, that is, according to the variance.

#### Question

What is the distance used? Describe the method of classification by variance?

#### i Question

- 1. How many groups are there at step 0? at the last step?
- 2. How many iterations are there?
- 3. Recall the definition of inter-class variance.
- 4. What is the inter-class variance at step 0? at the last step? How is it going according to the number of groups (or according to the number of iterations)?
- 5. By comparing the total inertia and the 'clas\$height' output, find the coefficient of proportionality between the loss of inter-class variance and height of jumps.

### Choice of the number of classes

#### i Question

- 1. Plot the curve corresponding to the loss of variance inter in as a function of the number of iterations:
- 2. Select the "optimal" number of classes.
- 3. Verify that, for the number of classes chosen, the number by class is sufficient (we can use the cutree function).
- 4. These classes can be represented using a dendrogram
- 5. You can also colour the leaves of the tree corresponding to a class. To do this, install and load the package 'dendextend'.

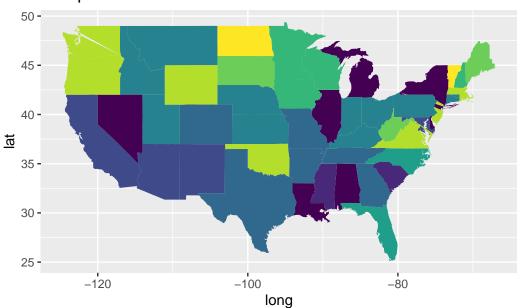
#### Link with PCA.

We will represent the classes obtained in the factorial design(s) obtained by the PCA. This will make it possible to represent the classes and describe them according to the variables initials.

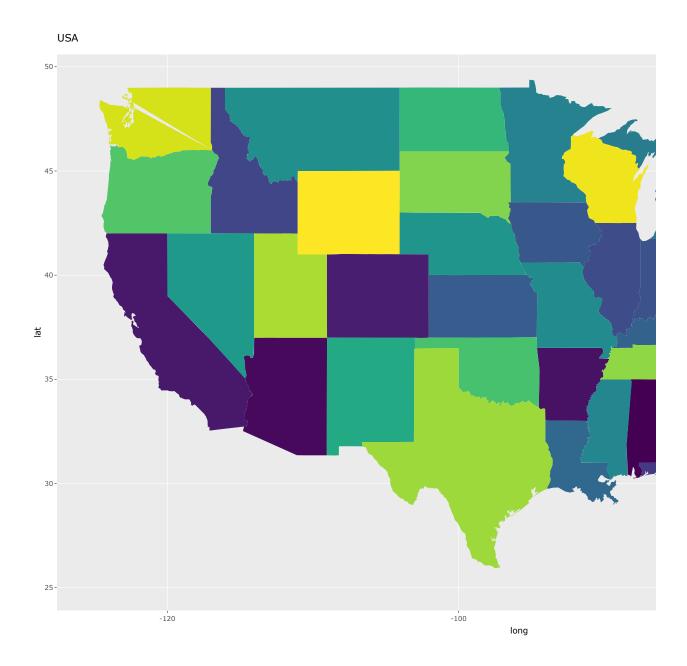
#### Question

Represent the coordinates of the individuals in each group in the first factorial plane (with one color for each class). The vector generated by 'cutree' can be used to form a color vector. Interpretation.

# Components of arrest data



### #data(france)



# Cophenetic distance

i Question

# ${\bf Cophenetic\ distance\ between\ dendrograms}$

# References

ggdendro

 ${\tt dendroextra}$ 

hier\_clust, tidyclust